

Probabilistic Deep Learning on Spheres for Weather/Climate Applications

Speakers

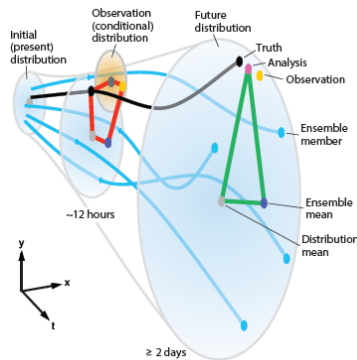
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Introduction

Geometric projection

Spherical modeling

Accuracy and efficiency

Why go probabilistic?

Methods

Results

Conclusion and future work

Introduction

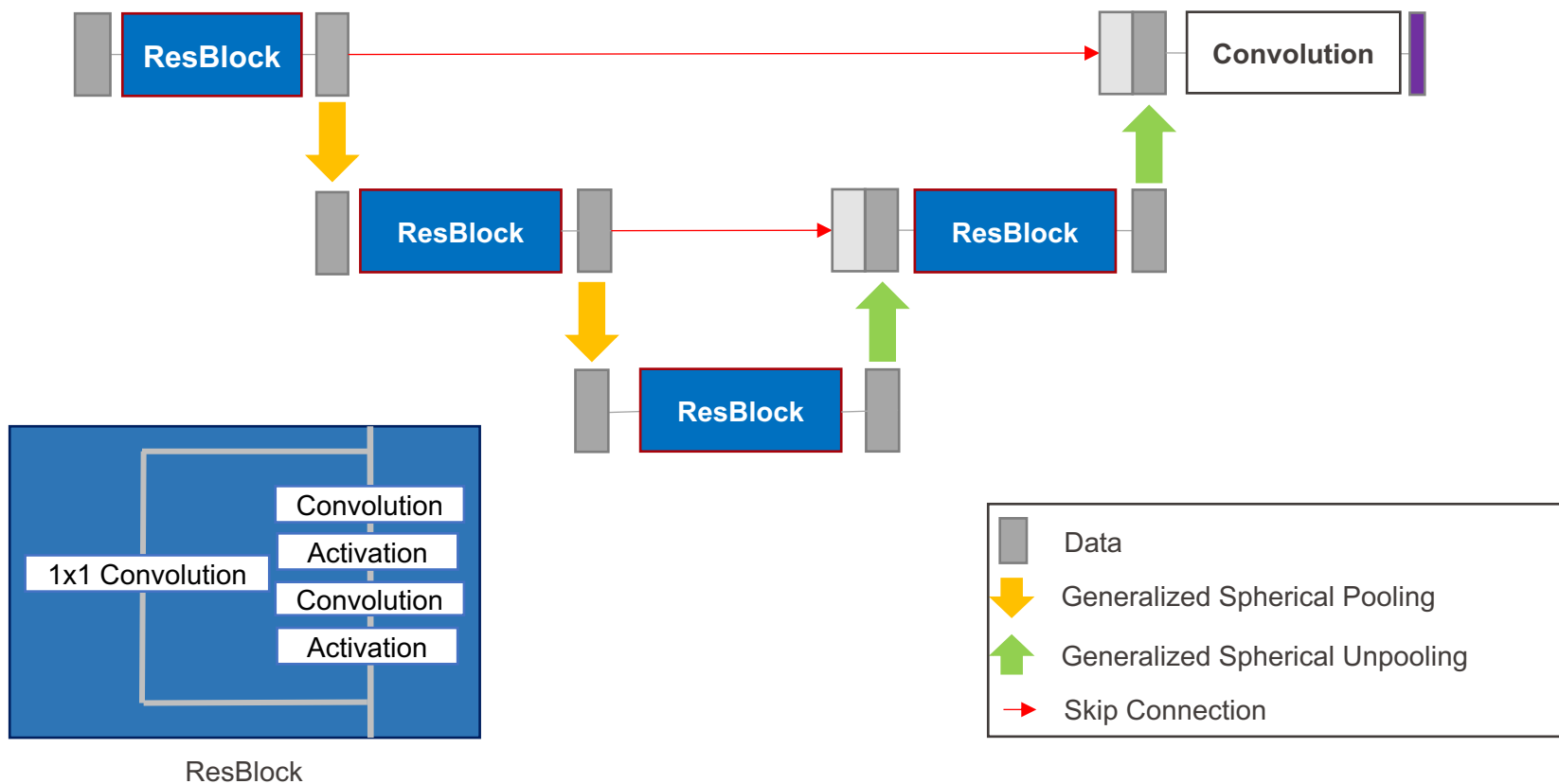
Our motivation:

1. Deep learning method cost less computation power than NWP models
2. Can help us understand the impact of initial conditions
3. Can be used on other atmospheric problem

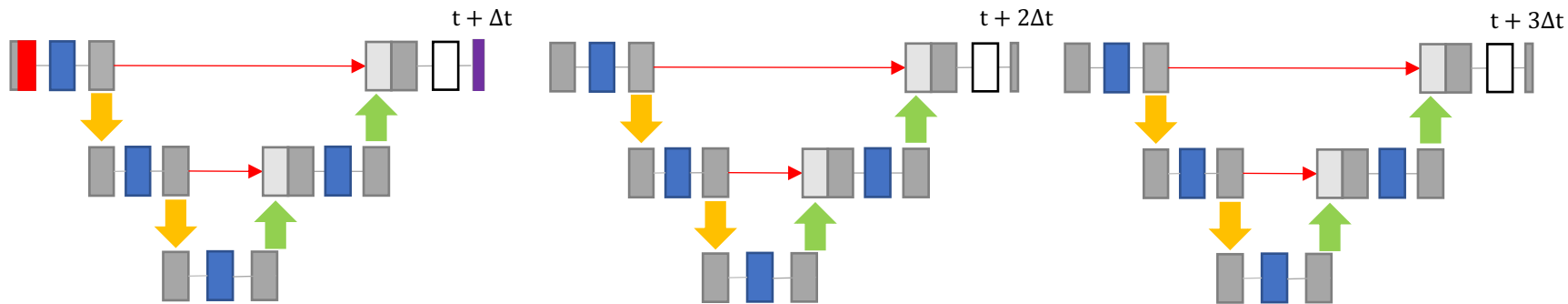
Our aim:

1. Design interpretable modeling method
2. Predict the weather with deep neural network

Introduction - U Net

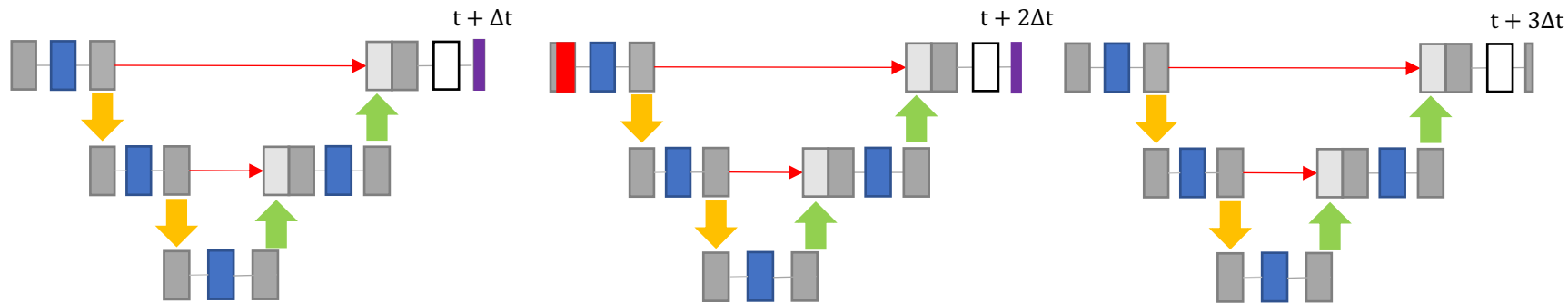


Introduction - Autoregressive model



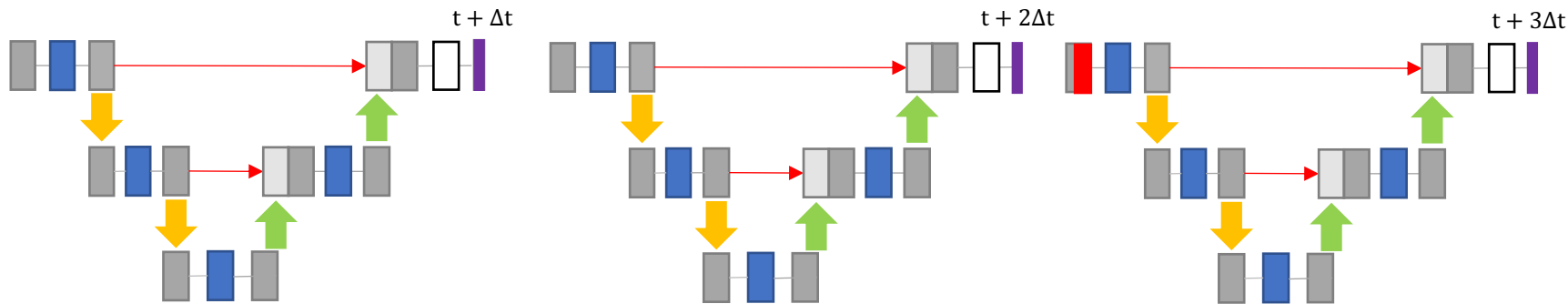
$\Delta t = 6$ hours

Introduction – Autoregressive model





$\Delta t = 6$ hours

Introduction – Autoregressive model



$\Delta t = 6$ hours

Loss function = $\text{MSE}(\text{Predictions}, \text{Observations})$

 Predictions
 Observations

Introduction – Input/Output

Input at time t

1. geopotential at 500 hPa (Z500)
2. temperature at 850 hPa (T850)

Additional feature at time t :

1. top-of-atmosphere solar radiation
2. orography
3. land-sea mask
4. latitude
5. soil type

Predict at $t + \Delta t$

1. geopotential at 500 hPa (Z500)
2. temperature at 850 hPa (T850)

Introduction – Metric

$$RMSE = \sqrt{\frac{1}{N} \sum_{n=0}^N (p_n - o_n)^2}$$

- p_n = predicted value at location n
- o_n = observed value at location n
- Measure the distance between prediction and observation
- Lower is better

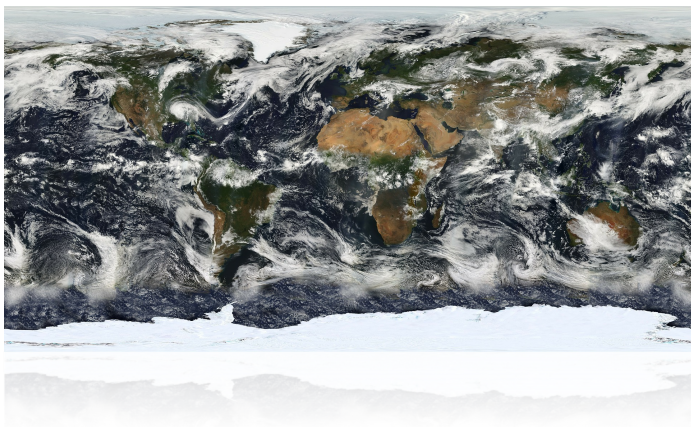
Introduction – Dataset

Results in this presentation:

- Weather Benchmark
- Region: Global
- Spatial resolution: 5.625° (approx. 600 km)
- Temporal resolution: 6h

Currently:

- ECMWF ERA5



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Accuracy and efficiency

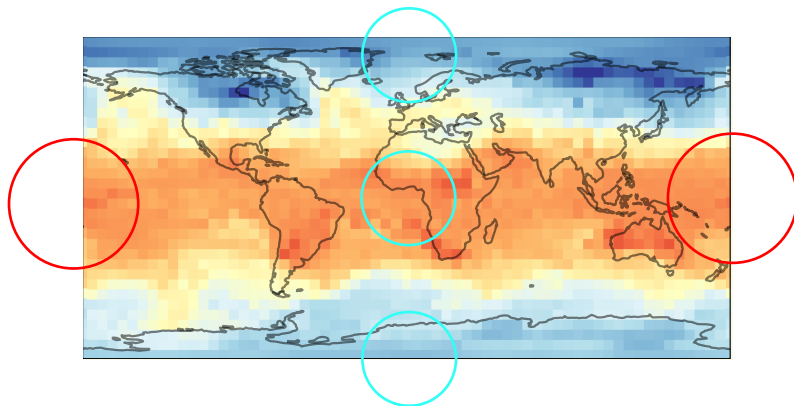
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Geometric projection – Planar

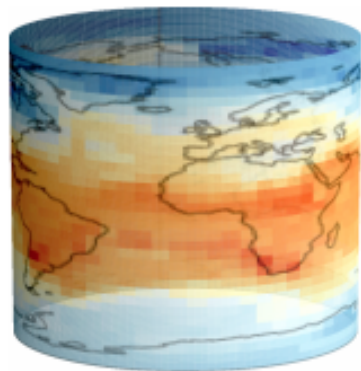


Project the sphere as planar



1. Discontinuity on borders
2. Imbalanced projection

Geometric projection – Cylinder



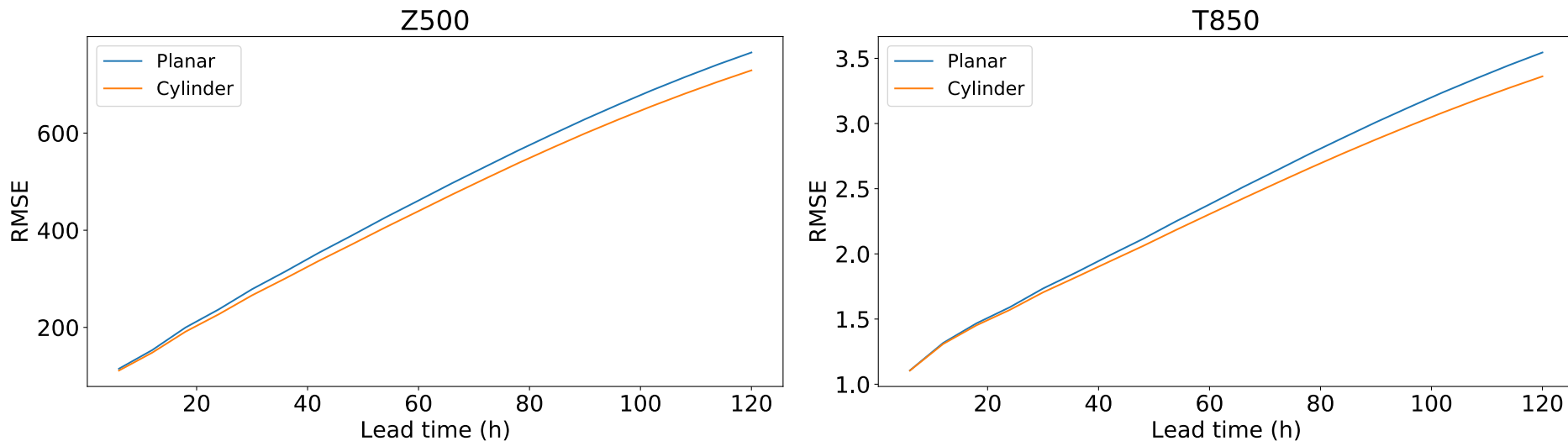
Project the sphere as cylinder



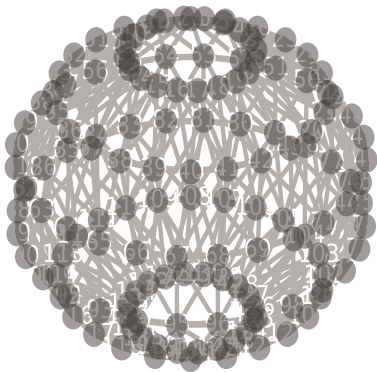
1. Discontinuity on borders
2. Imbalanced projection

Geometric projection – Cylinder

How much improvement?



How to solve imbalanced projection?



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Spherical modeling



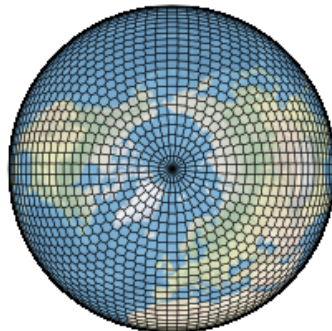
- Directly modeling on spherical sampling without projection
- Using graph to represent the sphere
- Graph nodes given by sampling points



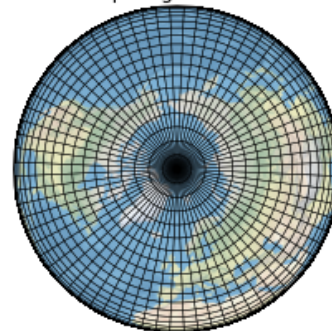
- Can approximate any 3D object
- Approximation quality is proportional to number of nodes.
- Solving imbalance by using an even sampling (e.g., HEALPix)
- Adaptive to any levels of resolution

Spherical modeling – Sampling methods

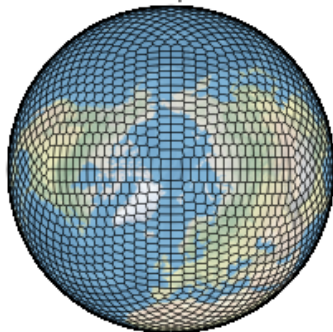
Reduced Gaussian Grid



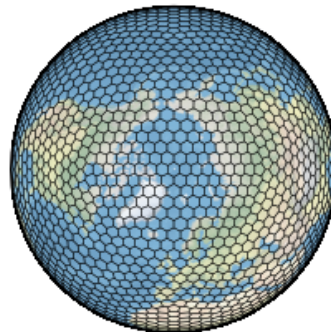
Equiangular Grid



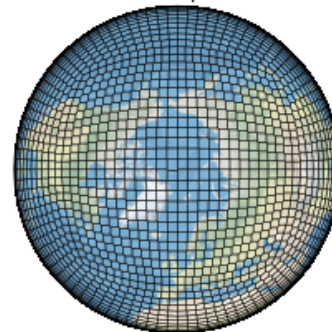
Healpix



Icosahedral



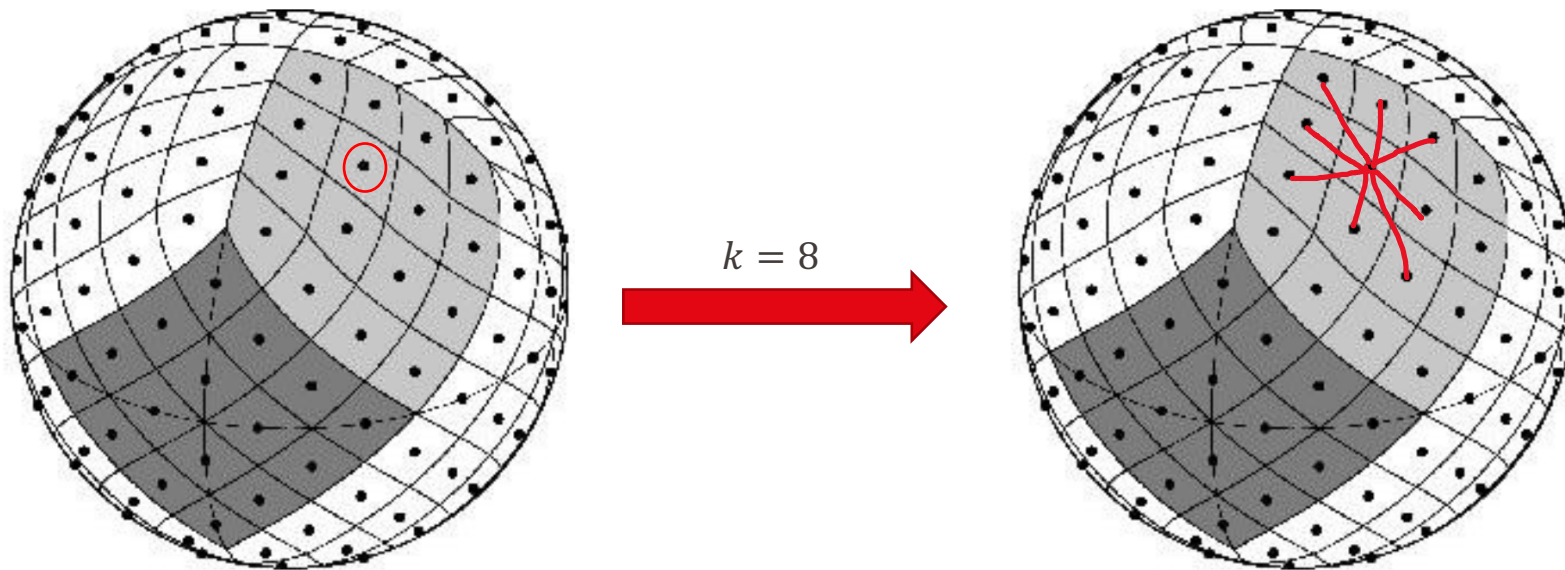
Cubed Sphere



Spherical modeling – Build the graph

k Nearest Neighbors (kNN) graph

- Each nodes is connected to k nearest neighbors undirectedly.
- If we have N nodes, then we have kN edges.



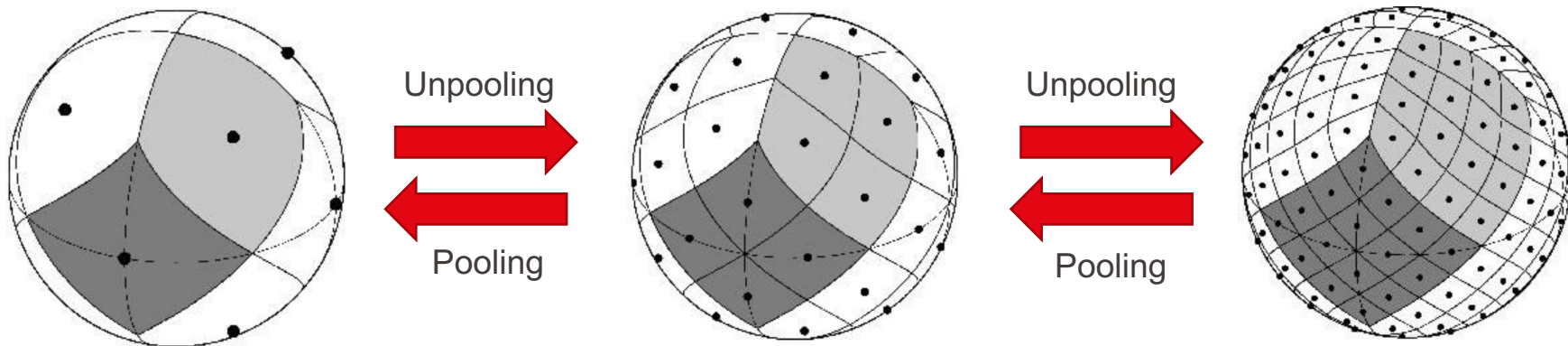
Spherical modeling – Computation on the graph

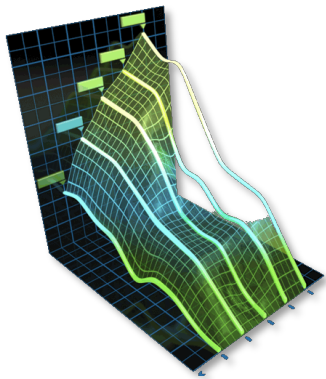
Graph convolution

1. Fourier transform to frequency domain
2. Multiply with (learnable) kernel function
3. Inverse Fourier transform

Graph pooling / unpooling

1. Max / Average aggregation
 - Not applicable to all spherical sampling
 - Easy to implement
2. General interpolation
 - Applicable to all spherical sampling





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Accuracy and efficiency

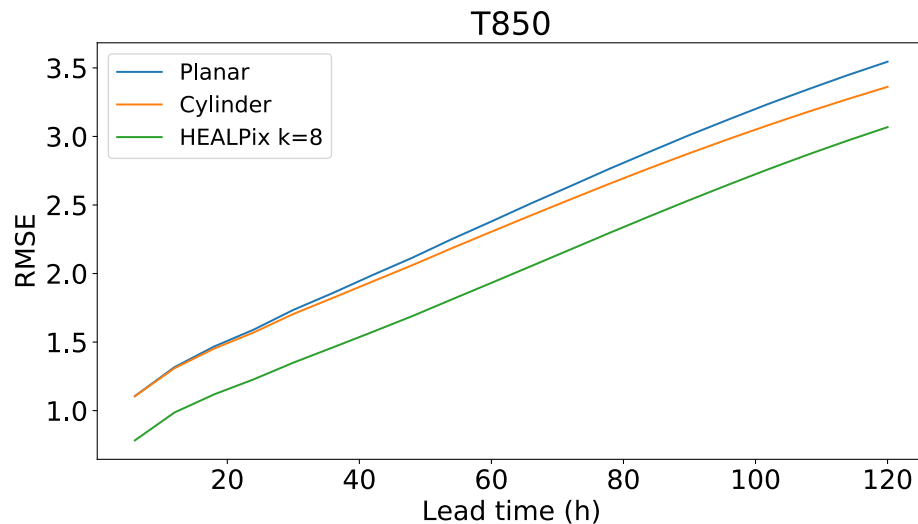
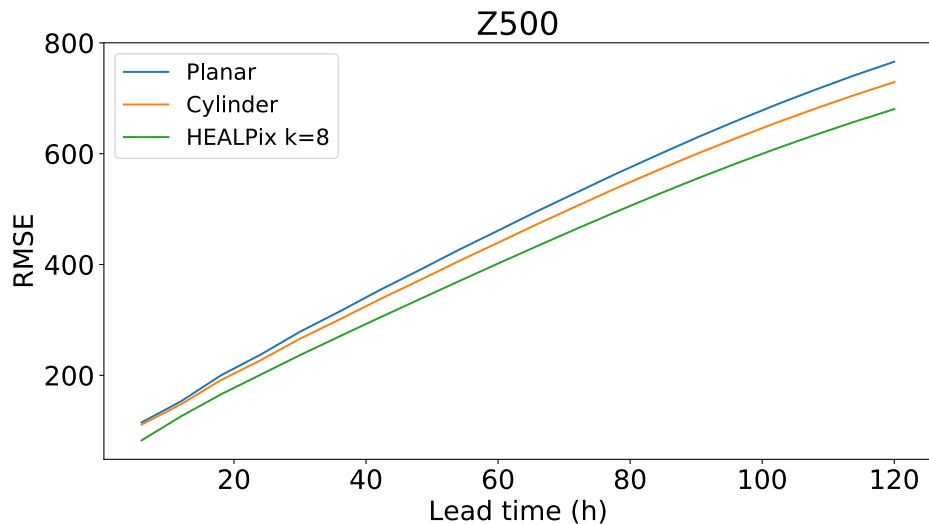
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Accuracy and efficiency



For fair comparison, the HEALPix data are interpolated from planar/cylinder data

Accuracy and efficiency - Scalability

Scalability matters:

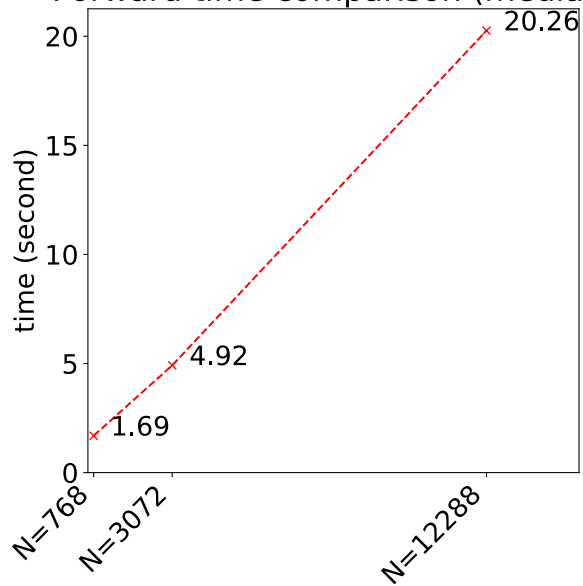
- In real life, spatial resolution can be less than 50 km (Large graph)
- The model need to handle real case efficiently (One of our motivation)

Accuracy and efficiency - Scalability on N

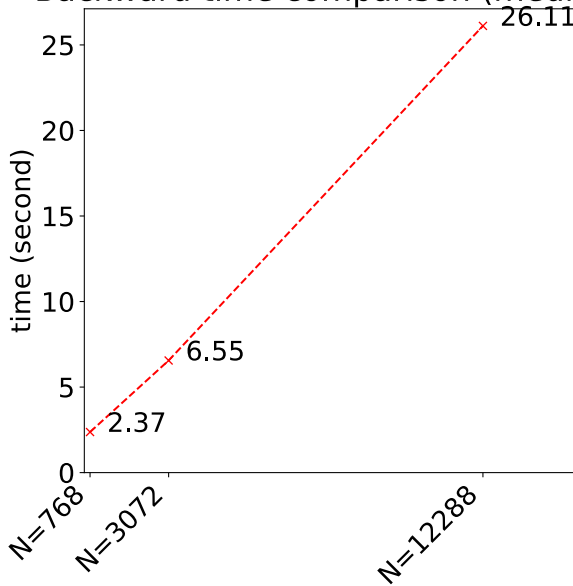
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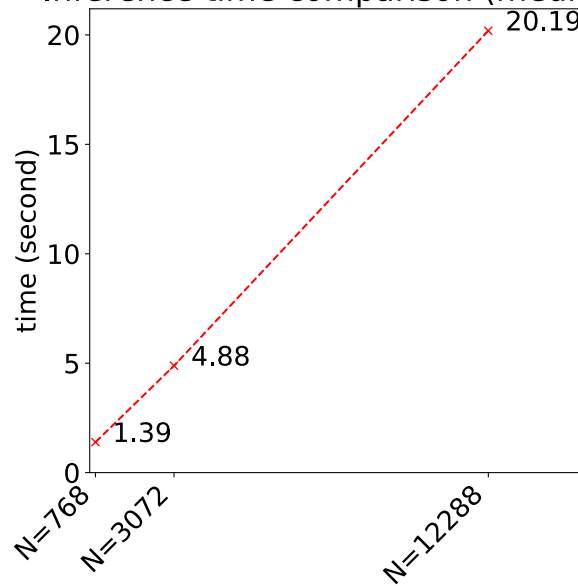
Forward time comparison (median)



Backward time comparison (median)



Inference time comparison (median)

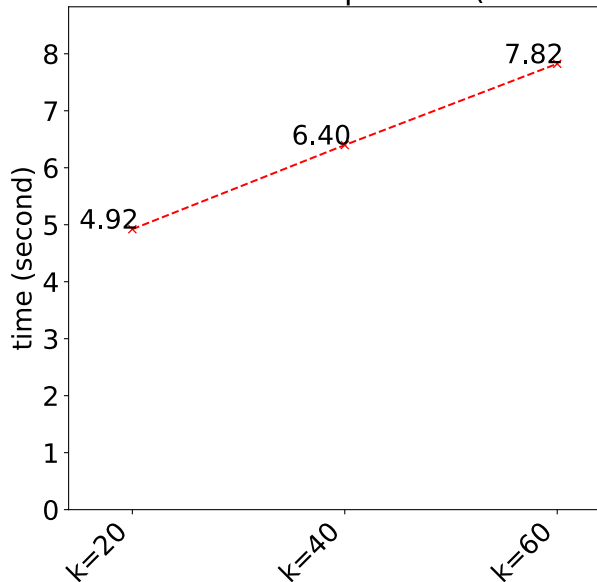


Accuracy and efficiency - Scalability on k

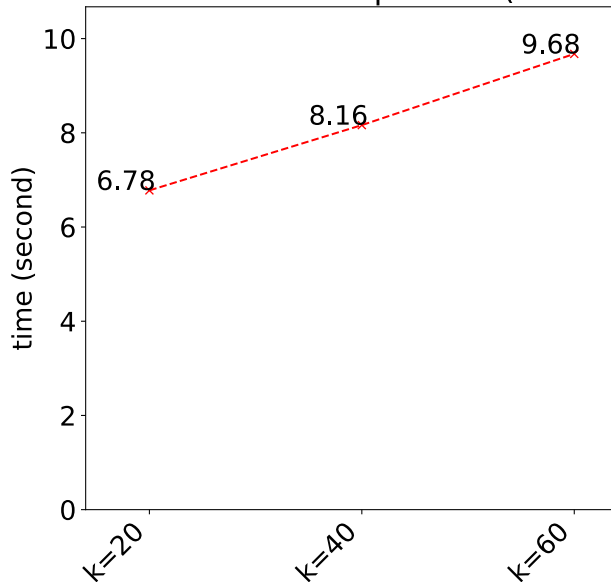
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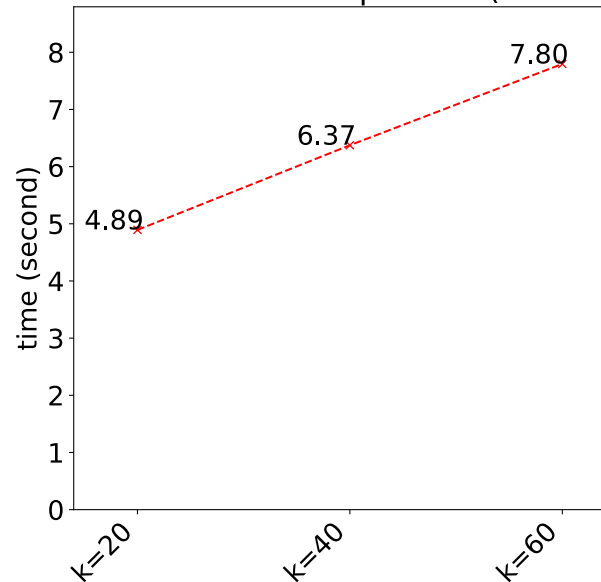
Forward time comparison (median)



Backward time comparison (median)



Inference time comparison (median)



Accuracy and efficiency - Costs

What kind of infrastructure we need to run the following model?

?

- $N = 12288$ (approx. 200km)
 - $k = 20$
 - Process 15 graphs in parallel
- or
- $N = 196608$ (approx. 50km)
 - $k = 20$
 - Process 1 graph

Answer: Single GTX 1080Ti with 8GB free graphical memory



Multiple GPUs can

- Process larger graph
- Process larger batch
- Accelerate the learning

Conclusion until now

1. Spherical modeling better approximates the earth
 - No information lost on borders
 - Graph evenly represents balanced sampling
2. The approximation quality can be adjusted by the number of sampling points
 - More sampling points mean smaller polyhedrons to approximate sphere
3. The computation complexity increases linearly
 - The ability to handle high resolution data
4. Lower requirements for infrastructures than classical NWP.
 - Single GPU can run the experiments efficiently
 - Multiple GPUs are capable of high-resolution simulation.

Reference

1. Images sources:
 - <https://developer.nvidia.com/>
 - <https://github.com/epfl-lts2/pygsp>
 - <https://pixabay.com/>
2. Gionata Ghiggi, slides about DeepSphere
3. Michaël Defferrard, slides about DeepSphere and the Earth
4. Icíar Lloréns Jover, Geometric deep learning for medium-range weather prediction