Integrated Backward Second-Harmonic Generation through Optically Induced Quasi-Phase-Matching

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Quasi-phase-matching for efficient backward second-harmonic generation requires sub-μm poling periods, a nontrivial fabrication feat. For the first time, we report integrated first-order quasiphase-matched backward second-harmonic generation enabled by seeded all-optical poling. The self-organized grating inscription circumvents all fabrication challenges. We compare backward and forward processes and explain how grating period influences the conversion efficiency. These results showcase unique properties of the coherent photogalvanic effect and how it can bring new nonlinear functionalities to integrated photonics.

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The efficiency of nonlinear wave mixing processes is clamped by the mismatch of momenta due to dispersion. Quasi-phase-matching (QPM) [1] is a technique used to compensate the momentum mismatch and recover the efficiency of the parametric conversion through the periodic reversal of nonlinear susceptibility in the medium. Integrated waveguiding structures are ideal candidates for nonlinear optical processes as they offer added flexibility for dispersion engineering, higher light intensities under reduced power, and access to a wide range of materials. In integrated platforms, QPM has been realized by domain inversion in lithium niobate on insulator ferroelectric waveguides through electric-field poling [2], with p-n junctions in silicon [3], or by optically inducing a periodic electric field by all-optical poling (AOP) enabled by the coherent photogalvanic effect. AOP, first extensively studied in optical fibers [4–9], was recently demonstrated in both silicon nitride (Si₃N₄) waveguides [10–12] and micro-resonators [13–15]. During AOP, multiphoton absorption interference leads to the inscription of periodic dc field automatically satisfying QPM condition for the participating waves. The obtained QPM grating and effective second-order susceptibility [χ(2)] overcome the typical trade-off between device functionality and performance and fabrication complexity. This effective χ(2) brings added functionalities to Si₃N₄, an already mature linear platform with its low loss and high damage threshold [16,17] and heavily exploited for third-order [χ(3)] nonlinear effects [18–22]. High level of second-harmonic (SH) powers commensurate with those obtained in typical χ(2) platforms can be obtained by leveraging the robustness and high power handling capability of Si₃N₄. As such, the demonstration of broadband second-harmonic generation (SHG) [12,23], difference-frequency generation [24] and spontaneous parametric down-conversion [25] were reported in Si₃N₄ waveguides.

Most of the QPM work, in any platform, has been devoted to forward second-harmonic generation (FSHG), where the pump and generated SH propagates in the same direction [Fig. 1(a)]. The required QPM period, Λ_{FSHG} is determined by the momentum mismatch between the pump and its SH given by Λ_{FSHG} = 2π/Δk = λ/(2|n_{2ω} − n_ω|), where Δk is the difference in wave vectors, λ is the pump wavelength, n_{2ω} and n_ω are the effective indices at the SH and pump, respectively. Typically the necessary periods, in both crystals and waveguides, are on the order of a few microns. The fabrication of external structures of such dimensions, as required for electric-field poling, is possible. However, submicron QPM periods necessary for mirrorless optical parametric oscillators [26], spontaneous parametric down-conversion with very narrow spectrum [27,28], or backward second-harmonic generation (BSHG) [29], where the pump and SH waves travel in opposite directions [Fig. 1(b)], face significant fabrication challenges [30,31]. As such, while BSHG has been studied theoretically for several configurations [32,33], there have been limited experimental demonstrations. BSHG has been achieved in bulk materials such as periodically poled lithium niobate [34] and potassium titanyl phosphate (KTP) using high-order QPM [35–37], or stacked metasurfaces [38] with first-order QPM. There is also a continuous effort to achieve BSHG in integrated photonics. Current demonstrations include using plasmonic structures...
with negative refractive index materials relying on perfect phase matching \[39,40\]. Nevertheless, these techniques face challenges related to fabrication constraints, which limit efficiency due to the tolerances and hinder the ability to replicate small structures. Moreover, they necessitate high power levels given the large beam sizes. Furthermore, plasmonic structures suffer from significant optical losses.

In this Letter, for the first time, we demonstrate AOP induced first-order QPM gratings with submicron periods \( \Delta n_{\text{BSHG}} = \lambda/(2(n_{2\omega} + n_{\omega})) \), see Fig. 1(b)] enabling BSHG with on-chip conversion efficiency (CE), defined as \( \eta_{2\omega} = P_{2\omega}/P_{\omega}^{0} \), of \( 1.2 \times 10^{-4}\% \text{/W} \), which in the C band is comparable with the highest CE value reached in any platform [34]. We achieve this by leveraging the self-organization properties of the optically written gratings, and by seeding the AOP process with counterpropagating coherent pump and SH seed light, bypassing the complex fabrication steps utilized in other platforms. We confirm that BSHG allows for narrow bandwidth SHG as well as very high thermal sensitivity compared to its bandwidth. We also explain how the grating period values affect the achievable CE.

The AOP process results in a grating with a periodicity of \( \chi^{(2)} \) automatically compensating the wave vector mismatch of the interfering coherent waves responsible for the effect. During the process, photogalvanic current \( (j_{\text{ph}}) \), proportional to \( (E_{\omega}^{*})^{2}E_{2\omega}e^{i2kz} + \text{c.c.} \), leads to charge separation and therefore inscription of a dc electric field with periodic modulation satisfying QPM condition. Here, \( E_{\omega} \) and \( E_{2\omega} \) are the complex electric field amplitudes of pump and SH fields, respectively, \( z \) is the propagation distance, * and c.c. denote complex conjugate, \( \Delta k \) is the difference of the wave vectors of pump and SH [Figs. 1(a) and 1(b)]. The inscribed field saturates due to photoconductivity (\( \sigma \)). As such, FSHG can be obtained by solely launching a pump wave in a waveguide or by a seeded process \[41,42\] where both the pump and its SH are simultaneously coupled to the waveguide. By injecting the pump and its SH from opposite sides of the waveguide, a QPM grating for BSHG could therefore be optically inscribed. The experimental setup for poling using two counterpropagating beams is shown in Fig. 1(c). We carried out the demonstration in an integrated Si\(_3\)N\(_4\) waveguide buried in SiO\(_2\) fabricated by LIGENTEC SA using its AN800 platform. The waveguide has a cross section of 1.3 \( \mu \text{m} \times 0.8 \mu \text{m} \) and is folded in nine meanders for a total length of 4.3 cm, including input and output tapers. Backward-seeded AOP is initiated by 1550 nm light together with its SH, externally generated using a nonlinear crystal: periodically poled KTP (PPKTP). The 1550 nm pump was first shaped into a 5 ns pulse train at 1 MHz repetition rate and was amplified to reach peak power up to 8.6 W in the waveguide. The pump and its SH are collimated by a parabolic mirror, split and coupled through opposite ends of the waveguide in transverse electric polarization. The power of both the forward pump and the backward SH seed can be controlled using variable attenuators. During this process, the optical path lengths are matched in order to ensure the overlap of pump and seed SH pulses inside the waveguide, as to enable grating inscription. It should be noted that the pulses, when not temporally overlapping inside the waveguide, can contribute to grating erasure. In our case we estimate that the inscription-to-erasure time ratio is around 35:1. The forward pump is monitored by detector \( D_1 \) while SH is collected by detector \( D_2 \) after a dichroic mirror. Initially, seeding SH is blocked with a beam block (BB\(_2\)) and no backward SH is observed. During seeded AOP, BB\(_2\) is kept open, and is occasionally shut for a short period of time as to record the dynamic evolution of BSHG in the waveguide. Once saturation is reached, the performance of the device such as maximum backward second-harmonic CE and QPM bandwidth is quantified using \( \text{cw} \) pump light.

The poling traces for three different SH powers and constant pump power of 8.6 W are presented in Fig. 2(a). First, we clearly measure SH being generated backward. Second, the initial growth rate \( (d\eta_{2\omega}/dt)_{\text{max}} \) increases with seed SH power. While the maximum CE also initially increases, it eventually saturates owing to the enhanced \( \sigma \) [42]. Evidently, the resulting CEs for BSHG are close to 2 orders of magnitude lower than for FSHG when similar pump and SH seed power levels are used. The main factor controlling the efficiency of AOP is the initial growth rate, which correlates to how the current is translated to the electric field. Compared to forward AOP, \( d\eta_{2\omega}/dt \) is numerically fitted following high-seed approximation [42], is here found to be close to 100 times less. This is explained by the small grating period and the closeness of the separated charges, leading to screening. As a
where $K$ is due to the screening of electric fields. The effect of the exponentially decaying function, $E_y$, is reduced compared to larger grating periods even consequence, the electric field is weaker and the growth rate is reduced compared to larger grating periods even under identical photogalvanic current. Using Eq. (S21) in

$$E_y(\Delta k; x, y, z) = \frac{2\Delta k \cos(\Delta k z)}{4\pi c} \int \int dx' dy' \rho(x' + x, y' + y) K_1(\Delta k \sqrt{x'^2 + y'^2}) \sqrt{x'^2 + y'^2},$$

(1)

where $K_1$ is the first-order modified Bessel function of the second kind (see Supplemental Material, Sec. 1). As $K_1$ is an exponentially decaying function, $E_y$ will decay with increasing $\Delta k$, namely, with decreasing grating period. This is due to the screening of electric fields. The effect of the period on the achievable electric fields was simulated using COMSOL MULTIPHYSICS software for a charge distribution of $C = C_{bulk}[1 + ye^{-y^2/r^2} \cos(\Delta k z)]$ using the material constants and physical model described in Ref. [45]. We showcase simulation results for two specific cases with periodicity $\Lambda$ of charge spatial modulation being 6 $\mu$m and 0.2 $\mu$m. Gratings with such period can satisfy the QPM condition for FSHG and BSHG, respectively, as will be shown below. In Figs. 3(a)–3(c) the simulated charge

FIG. 2. Experimental BSHG CE during AOP (dotted) and fit (solid line) according to Ref. [42] for a constant peak pump power of 8.6 W and varying peak SH seed power inside the waveguide. There is a 9% error in the CE measurements due to the sum of errors in detectors.

FIG. 3. The effect of poling period on the inscribed dc electric field is shown. A periodically oscillating charge concentration along the waveguide $C$ (related to charge density $\rho = qN_A C$, where $q$ is the electronic charge [44] and $N_A$ is the Avogadro constant) and resulting longitudinal ($E_z$) and transverse ($E_y$) components of the electric field are simulated for a period 6 $\mu$m (a)–(c) and 0.2 $\mu$m (d)–(f), respectively.
distribution $C$, longitudinal electric field $E_x$, and transverse electric field $E_y$ are shown for the case when $\Lambda = 6 \mu m$. It is important to note that the transverse field strength $E_y$ determines the effective second-order nonlinearity $\chi^{(2)}_{eff}$ and, hence the CE. In Figs. 3(d)–3(f) we also display the $C$, $E_x$ and $E_y$ with $\Lambda = 0.2 \mu m$. By comparing the $E_y$ in both cases, it can be recognized that the magnitude of $E_y$ reduces approximately tenfold because of screening when the period is decreased from 6 $\mu m$ to 0.2 $\mu m$. Notably, the longitudinal field $E_x$ is almost the same for both cases as can be seen from Figs. 3(b) and 3(e).

We measure the CE spectrum for both backward and forward directions. After AOP, if the propagation loss is ignored, the CE for BSHG becomes [42]

$$\eta_{\omega_0} \approx \frac{(\omega \chi^{(2)}_{eff} L)^2}{2c e_0 n^2 S} \sin^2\left(\left(\Delta k - \frac{2\pi}{\Lambda}\right)\frac{L}{2}\right),$$

where $\Delta k(\lambda) - (2\pi/\Lambda)$ is the net wave vector mismatch after AOP, $L$ is the grating length, $n = (n_x^2 n_{\omega_o})^{1/3}$ with $n_{\omega_o}$ being the effective refractive index at frequency $\omega_o$ ($q = 1, 2$), $S = (S_{omega} S_{\omega_0})^{1/3}$ is the effective area, where $S_{\omega_o} = (\int|dxdy| E_{\omega_o}^2)^{3/2}/(\int|dxdy| E_{\omega_o}^6)^{1/2}$. $\chi^{(2)}_{eff}$ is the effective second-order nonlinearity, and $\sin(x) = \sin(x)/x$. The experimental data and the fits using Eq. (2) are shown in Fig. 4(a). Here, the effective area and effective refractive index data used for fitting are obtained using finite element method simulations. We clearly see that forward SH is not generated while BSHG occurs with a very narrow band.

We experimentally investigate the thermal sensitivity of BSHG as shown in Fig. 4(c) by varying the chip temperature. We extract the thermal shift of the QPM peak to be 19 pm/°C. It can be seen that it is extremely sensitive compared to its bandwidth.

In conclusion, seeded AOP represents a straightforward way to induce exceptionally short-period QPM gratings that can satisfy BSHG in integrated platforms. Seeded AOP circumvents fabrication challenges of the standard electrical poling techniques for implementation of submicron nonlinear gratings, while the self-organized QPM grating results in a near perfect match between experimental and theoretical spectral response. As predicted by the theory, we observe that only the nonlinear grating strength changes with changing seeding conditions. The poled waveguides show extremely narrow QPM spectra, highly tunable with
temperature, with CE of $1.2 \times 10^{-4}$%/W, comparable to the highest one achieved in C band so far [34]. Apart from efficiency, optical poling of Si$_3$N$_4$ demonstrates a better performance regarding the losses, reconfigurability, control in dispersion, and ease of operation. This demonstration paves the way for the realization of theoretically proposed effects such as phase conjugation [48], pulse shaping [32], self-pulsing [29], and bistability [49] through second-order nonlinearity. We theoretically explain the reduction of efficiencies compared to FSHG due to the screening of electric fields with submicron periods. The efficiency could be improved by using longer waveguides, exploiting other materials such as silicon-rich silicon nitride or using structures like Bragg gratings to separate the charges further.

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