Abstract — This paper presents a general method for obtaining the exact power spectra of generic time hopping modulated signals. Based on a point process approach, it provides simpler proofs for existing results and a powerful rigorous and at the same time systematic tool for computing the spectra of more complex time-hopping models. Spectrum formula are easy to understand and the contribution of each component of the model appears explicitly.

The family of pulse modulation techniques has gathered increasing interest since the introduction of ultra-wide band (UWB) impulse radio [1]. Exact spectral computation of pulse modulation techniques has already received the attention in the communication society [1, 4].

Here we focus on the power spectrum computation of the class of time hopping pulse position modulations [2], which is of particular interest for being well suited for multi access implementation. We exploit the fact that pulse modulated signals can be view as shot noises, i.e. as filtered point process. The corresponding models are simple and tractable and can be easily generalized to take into account other random quantities. Moreover, our approach can be extended toward a unifying model that also takes into account the family of pulse interval modulations [3]. The computation of the power spectral in then performed using recent results on the power spectrum of a shot noise with random excitation [5, 6], and is given by

\[ f_S(\nu) = \frac{1}{L_n T} |\tilde{w}(\nu)|^2 \]

\[ \left\{ \begin{array}{l} E[|A|^2] \sum_{j=0}^{L_n - 1} e^{2\pi i \nu (c_1 - c_j) T_c + (j - 1) T_l} \sum_{k \in \mathbb{Z}} C_A(k L_c + l - j) e^{2\pi i \nu k L_c T} \\
+ \frac{\varphi_B(2\pi \nu T_b)^2}{\varphi_0(2\pi \nu)^2} \sum_{j=0}^{L_n - 1} e^{2\pi i \nu (c_1 - c_j) T_c + (j - 1) T_l} \\
\end{array} \right\} \]

where \( \varphi_Y \) denotes the characteristic function of the random variable \( Y \), and \( CY \) its covariance.

The above formula is easily generalized to take into account additional random events: this allows for various extensions of published results.

References


