

Methods of Trajectory Estimation in Challenging Mapping Scenarios

IUGG 2023 Berlin

G05f - Multi-signal positioning, Remote Sensing and Applications

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Challenges in LiDAR mapping technology



[Source : Wingtra]

Direct georeferencing & Continuous capture



Trajectory must be accurately determined at all times

Challenges in LiDAR mapping technology

Trajectory must be accurately determined at all times

What if we use a drone with low grade navigation sensor ?

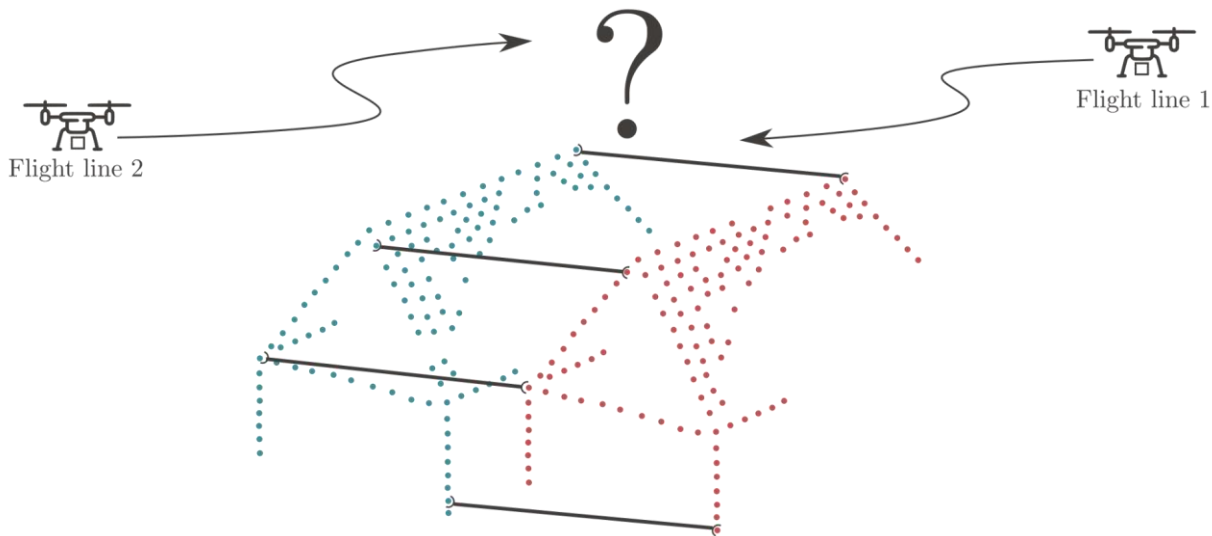
What if we lose GNSS signal ?

What if we miscalibrate our system ?

EPFL How to improve LiDAR reliability?

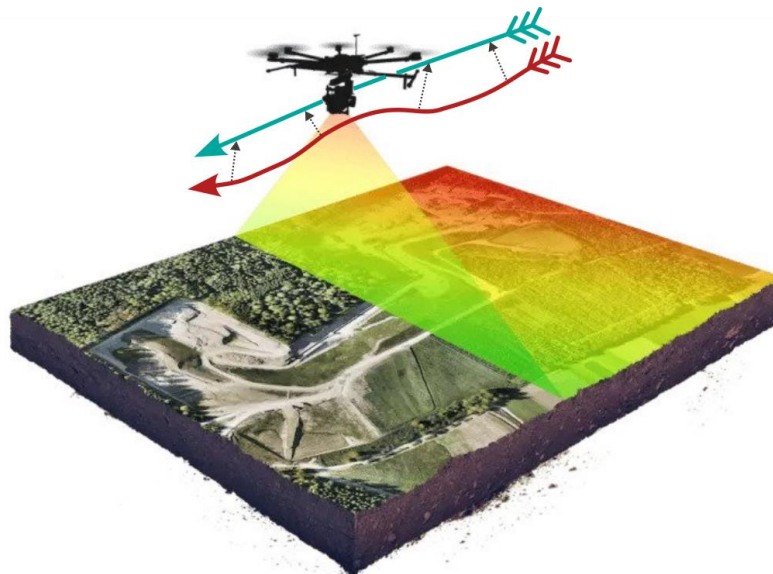
We propose a novel LiDAR based trajectory adjustment procedure:

1. Robust pipelines to establish **point to point correspondences** in point clouds



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2. Adjustment step to **refine the entire trajectory, calibrate system mounting**



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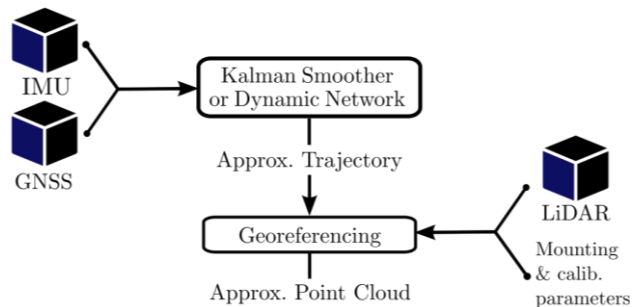
We propose a novel LiDAR based trajectory adjustment procedure:

1. Robust pipelines to establish **point to point correspondences** in point clouds
2. Adjustment step to **refine the entire trajectory, calibrate system mounting**

Objectives : allow post processing **system calibration & trajectory correction**, specifically when **GNSS outages occur**

Methods

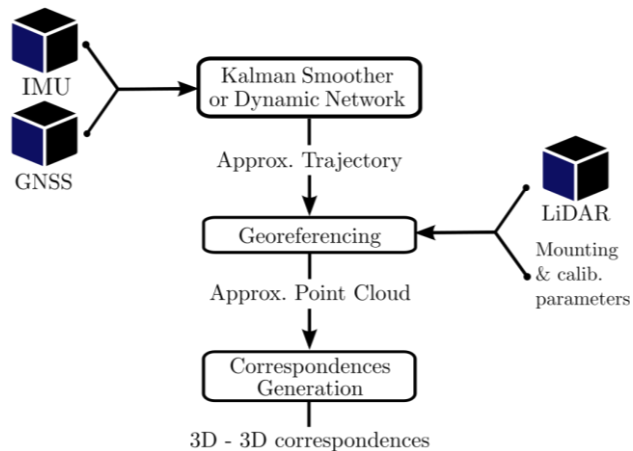
Processing pipeline



[A. Brun et. al., 2022, Lidar point-to-point correspondences for rigorous registration of kinematic scanning in dynamic networks, ISPRS Journal of Photogrammetry and Remote Sensing]

Methods

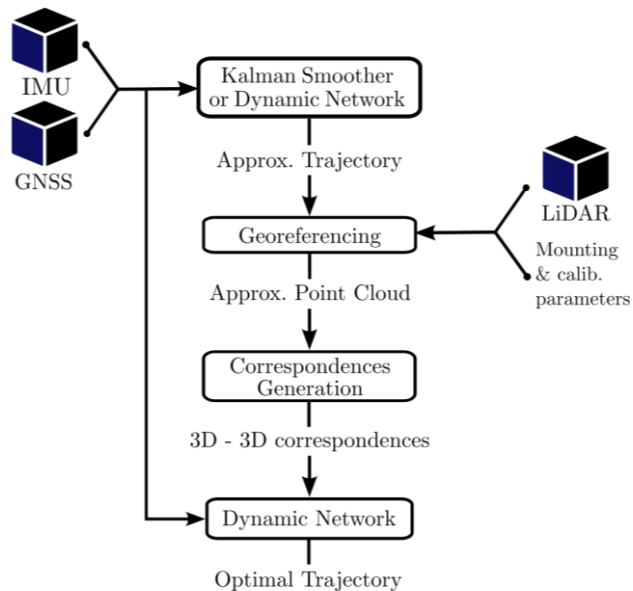
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[A. Brun et. al., 2022, Lidar point-to-point correspondences for rigorous registration of kinematic scanning in dynamic networks, ISPRS Journal of Photogrammetry and Remote Sensing]

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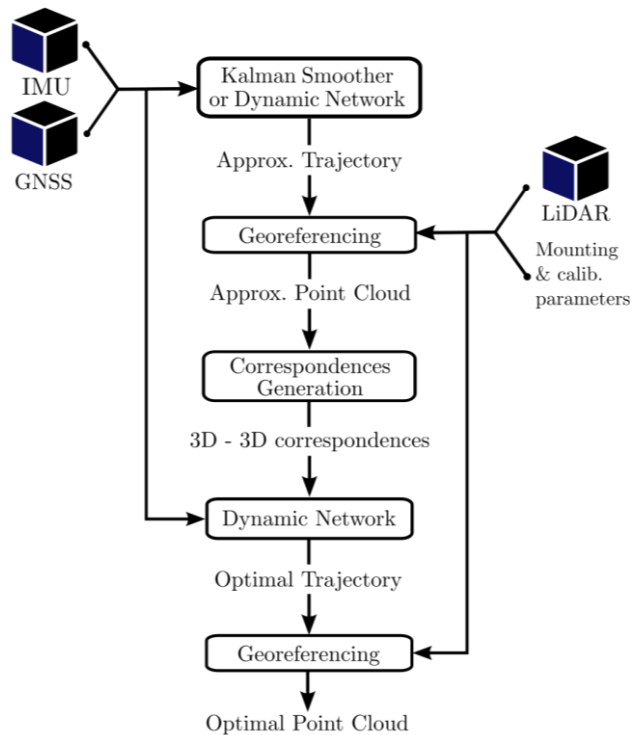
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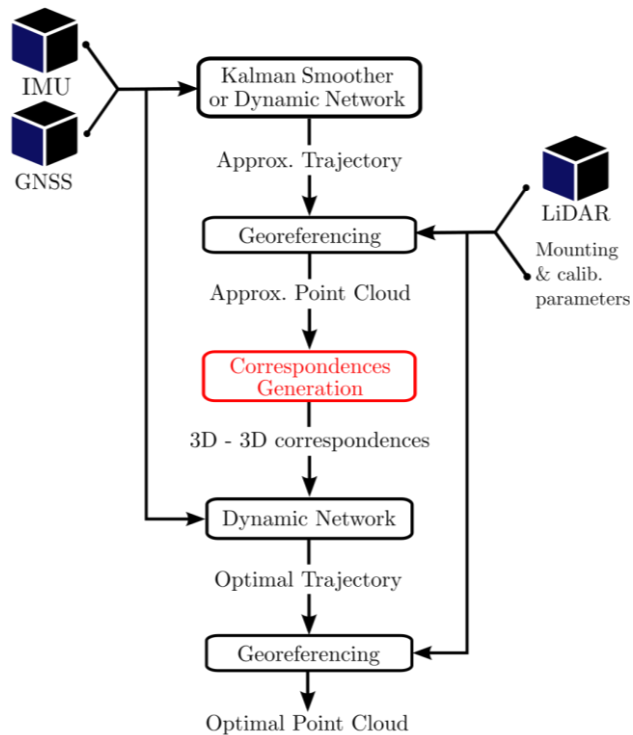
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Processing pipeline



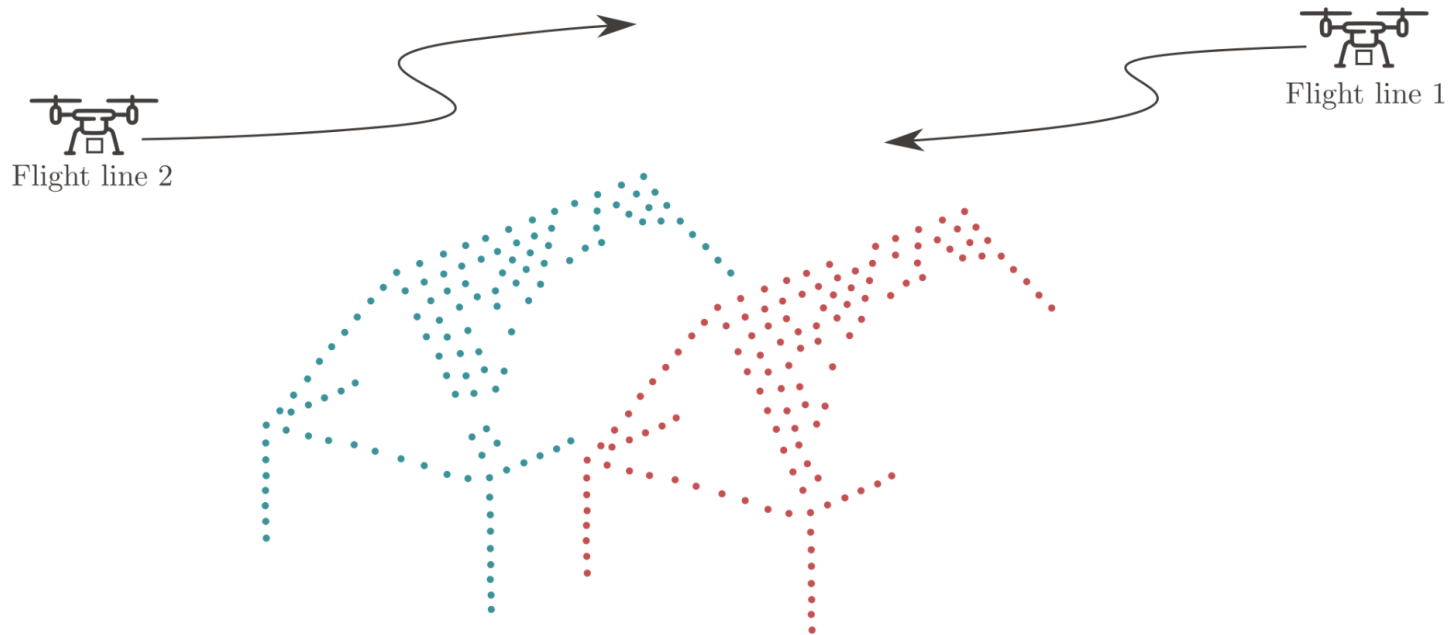
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Point to point correspondences generation



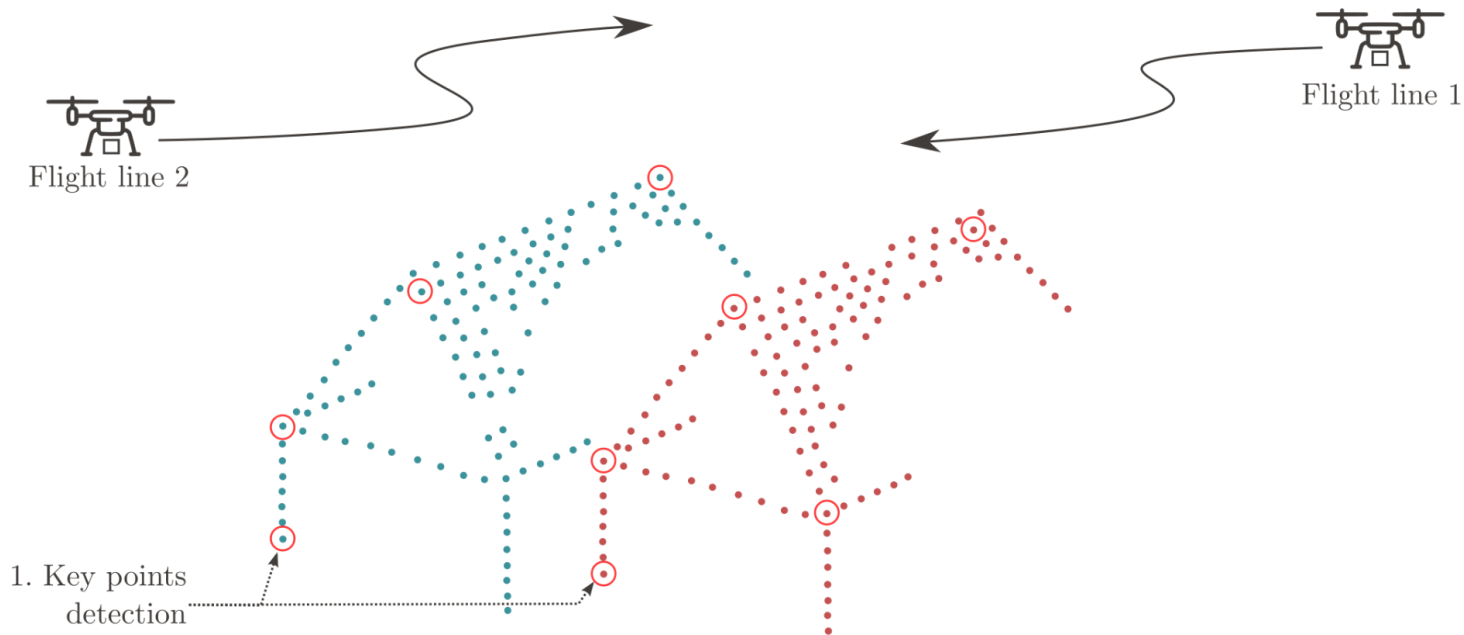
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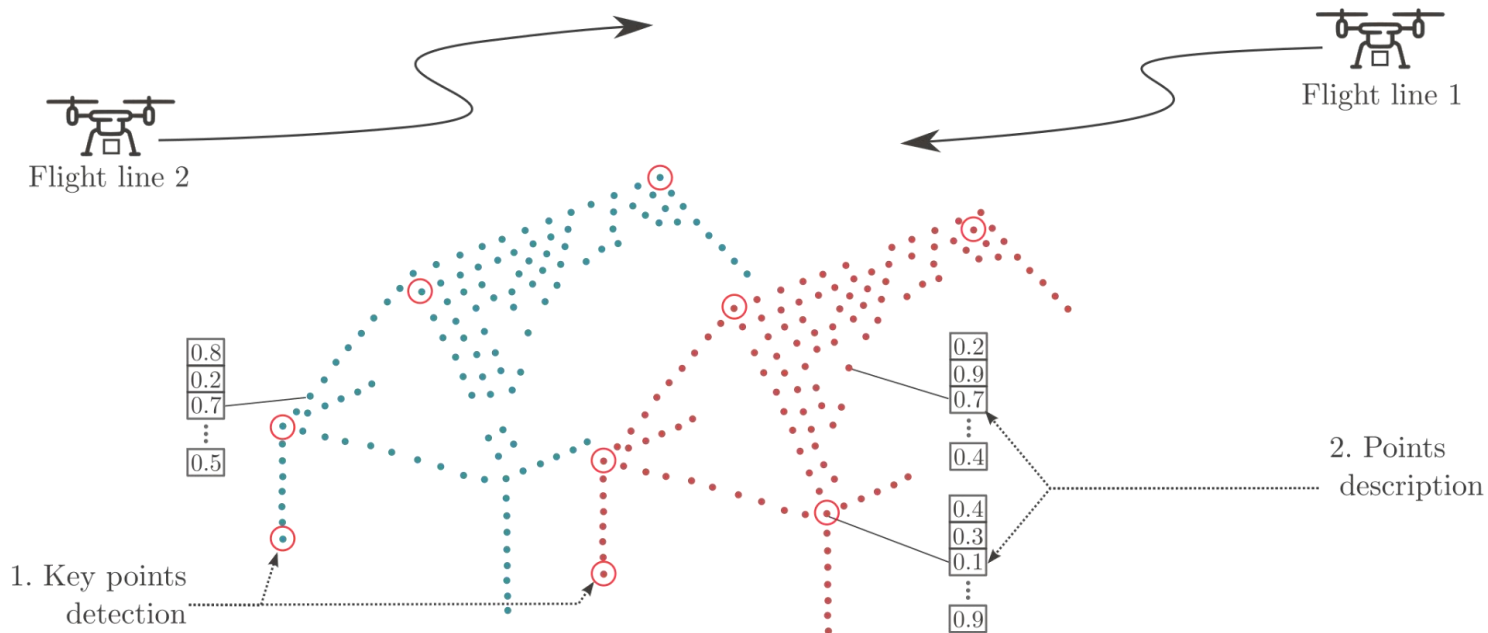
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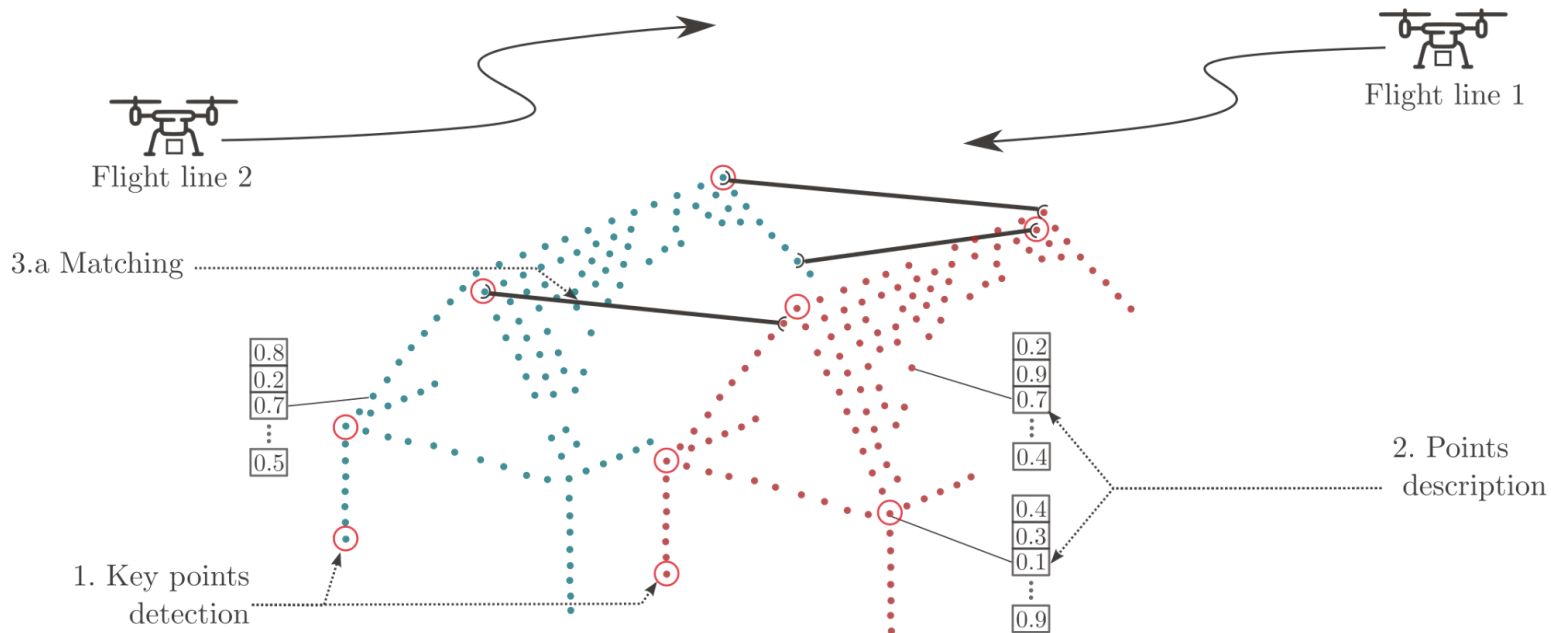
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Point to point correspondences generation



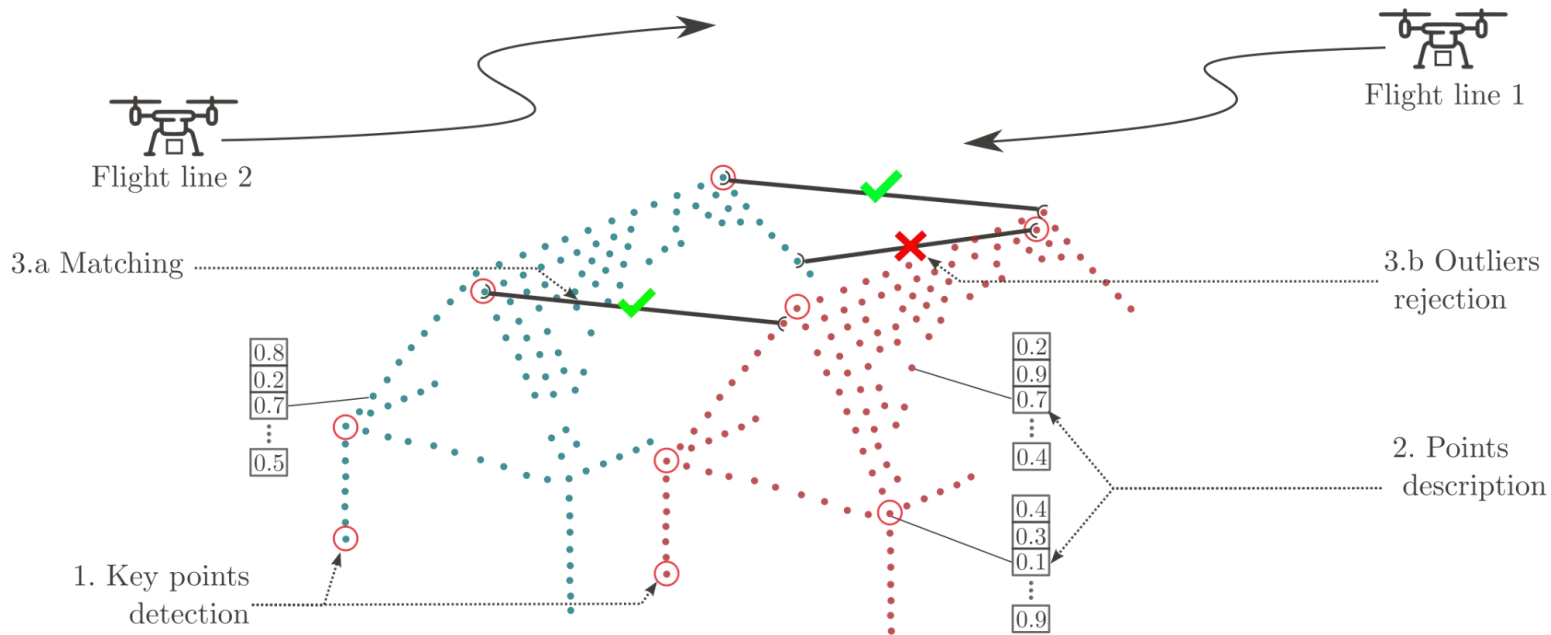
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Point to point correspondences generation

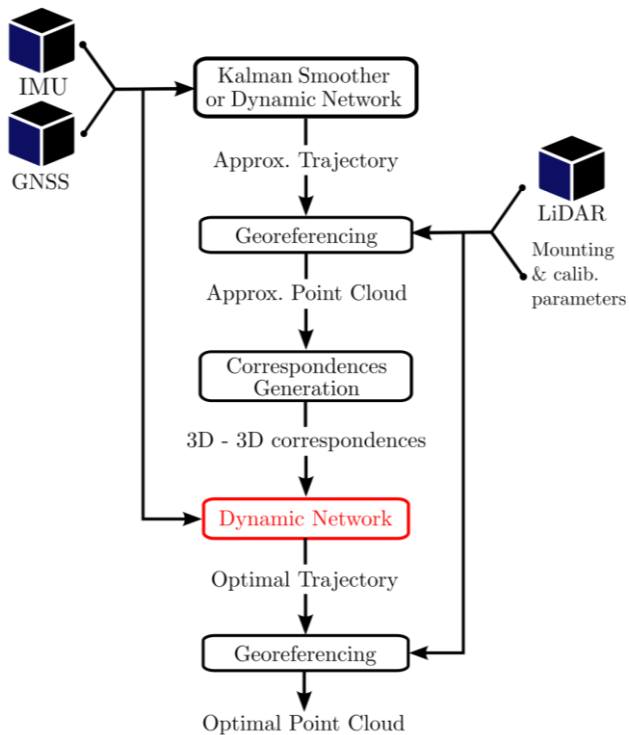


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Point to point correspondences generation



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An extension of conventional [geodetic networks](#):

1. Optimal solving of all [trajectory parameters and their derivatives](#) at once (e.g. specific forces + angular velocities) → ~300k parameters to solve per minute of trajectory¹

1. D. A. Cucci et. al., 2017. Bundle adjustment with raw inertial observations in UAV applications, ISPRS Journal of Photogrammetry and Remote Sensing

An extension of conventional **geodetic networks**:

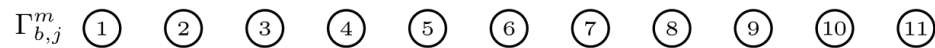
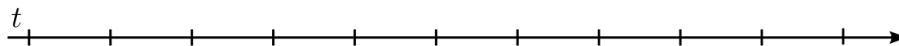
1. Optimal solving of all **trajectory parameters and their derivatives** at once (e.g. specific forces + angular velocities) → ~300k parameters to solve per minute of trajectory¹
2. Direct integration of **spatial constraints**, e.g. image tie points^{2,3} & LiDAR point to point
→ increase redundancy and improve numerical stability

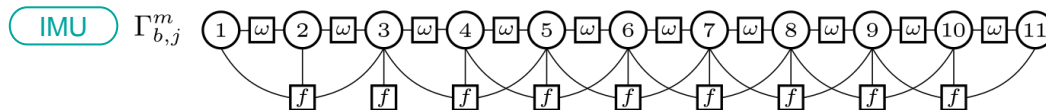
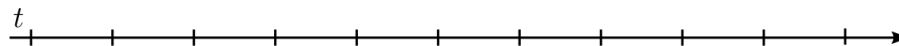
1. D. A. Cucci et. al., 2017. Bundle adjustment with raw inertial observations in UAV applications, *ISPRS Journal of Photogrammetry and Remote Sensing*
2. D. A. Cucci et. al., 2019. On Raw Inertial Measurements In Dynamic Networks. *ISPRS Annals of the Photogrammetry, Remote Sensing and Spatial Information Sciences*
3. K. Mouzakidou et. al., 2022. On The Benefit of Concurrent Adjustment Of Active And Passive Optical Sensors With GNSS & Raw Inertial Data, *ISPRS Annals of the Photogrammetry, Remote Sensing and Spatial Information Sciences*

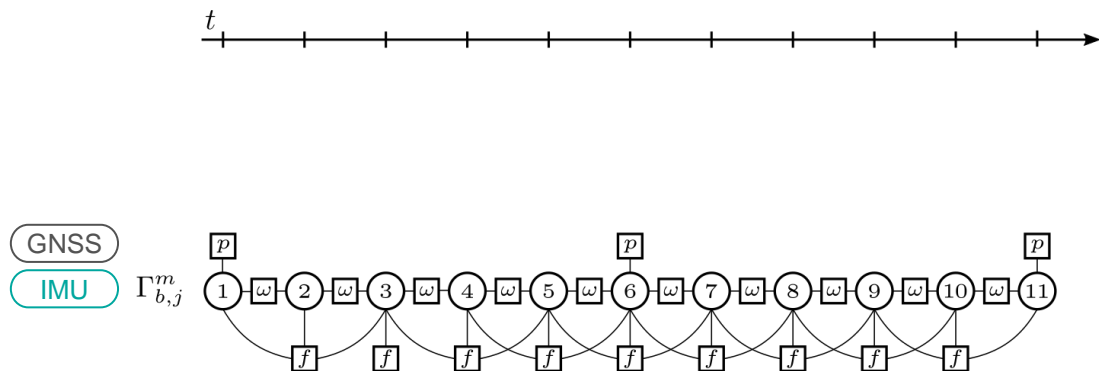
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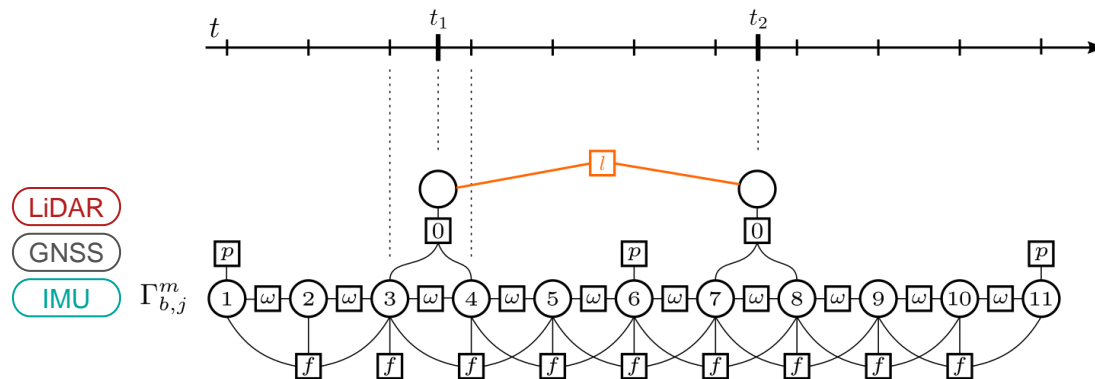
1. Optimal solving of all **trajectory parameters and their derivatives** at once (e.g. specific forces + angular velocities) → ~300k parameters to solve per minute of trajectory¹
2. Direct integration of **spatial constraints**, e.g. image tie points^{2,3} & LiDAR point to point
→ increase redundancy and improve numerical stability
3. Target the source of the errors (e.g. **IMU biases**) rather than the consequences (i.e. their **projection on the orientation**)

1. D. A. Cucci et. al., 2017. Bundle adjustment with raw inertial observations in UAV applications, *ISPRS Journal of Photogrammetry and Remote Sensing*
2. D. A. Cucci et. al., 2019. On Raw Inertial Measurements In Dynamic Networks. *ISPRS Annals of the Photogrammetry, Remote Sensing and Spatial Information Sciences*
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Aerial - Nominal Scenario

Trajectory. 1

GNSS

IMU

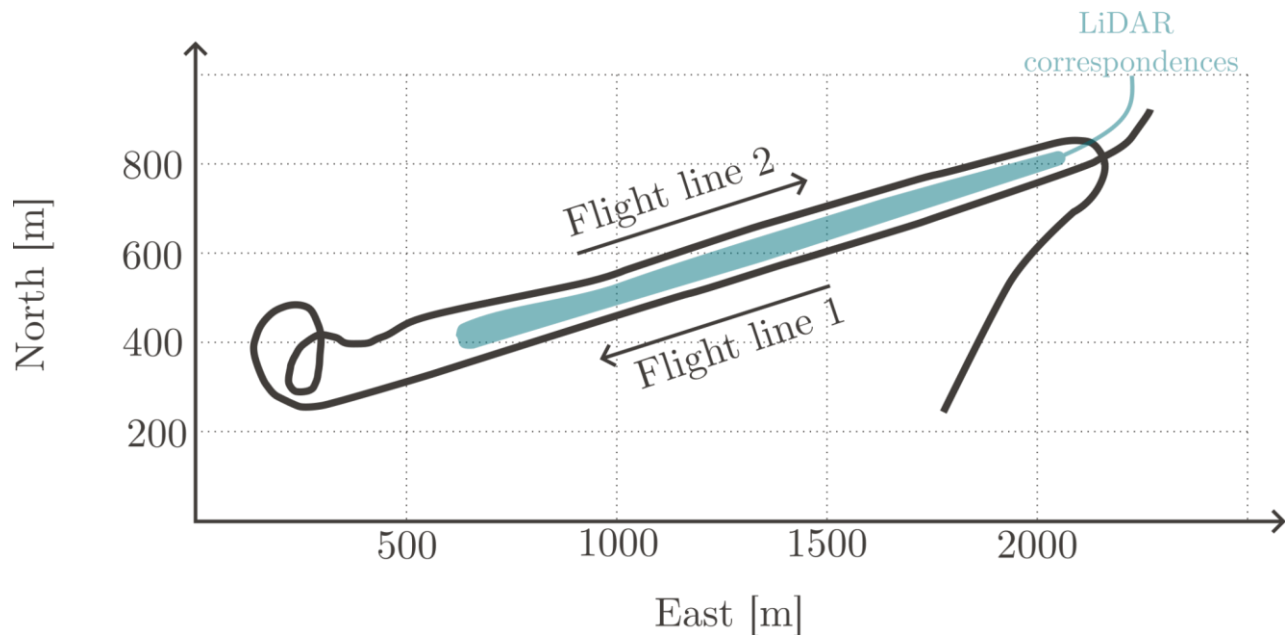
Trajectory. 2

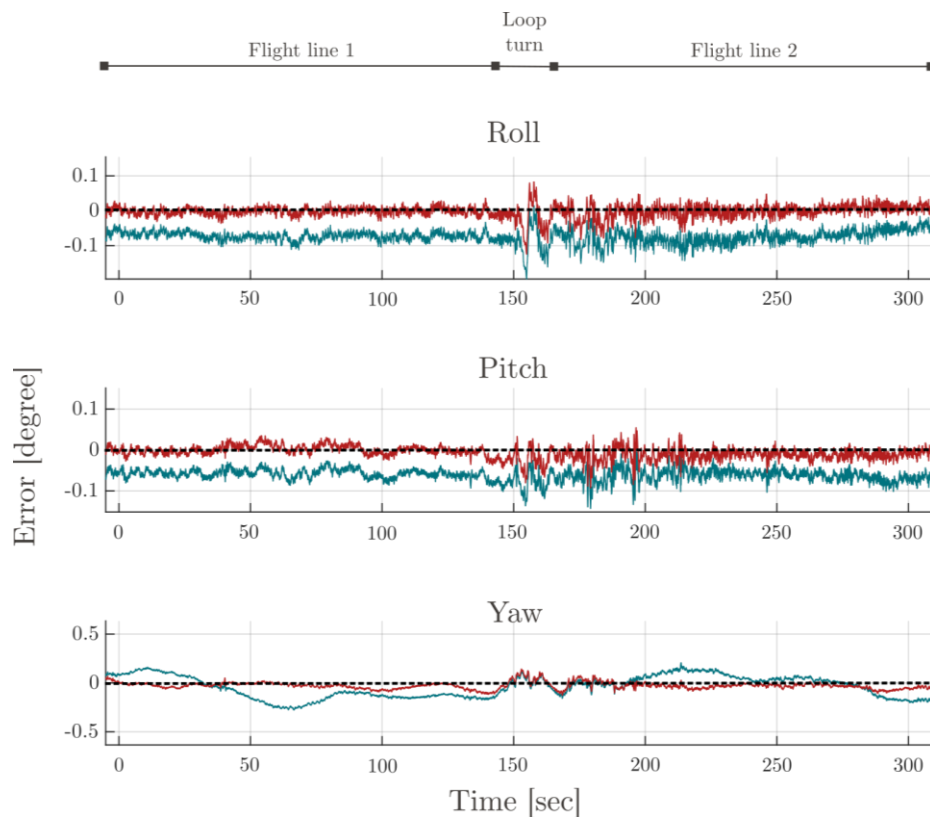
GNSS

IMU

LiDAR

- Flight duration ~ 5 minutes
- Precise laser & UAV grade IMU → large attitude errors
- Navigation grade (~ ground truth) trajectory available





Trajectory. 1 (GNSS) (IMU)

T. 1 attitude error

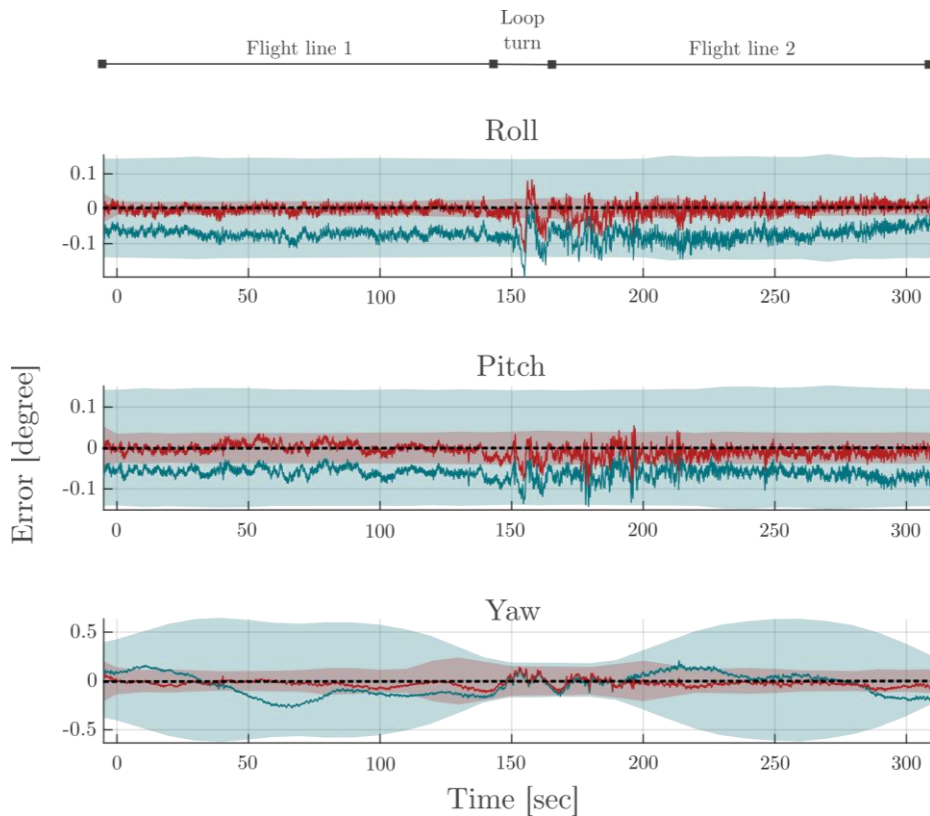
Trajectory. 2 (GNSS) (IMU) (LiDAR)

T. 2 attitude error

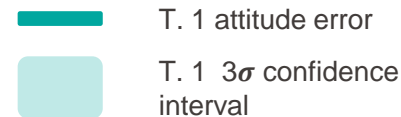
- Errors reduced by a factor 3→5 (attitude and subsequent point cloud)

Results

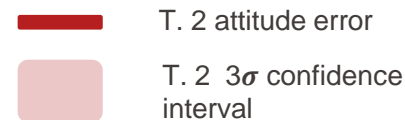
Aerial - Nominal Scenario



Trajectory. 1 (GNSS) (IMU)



Trajectory. 2 (GNSS) (IMU) (LiDAR)

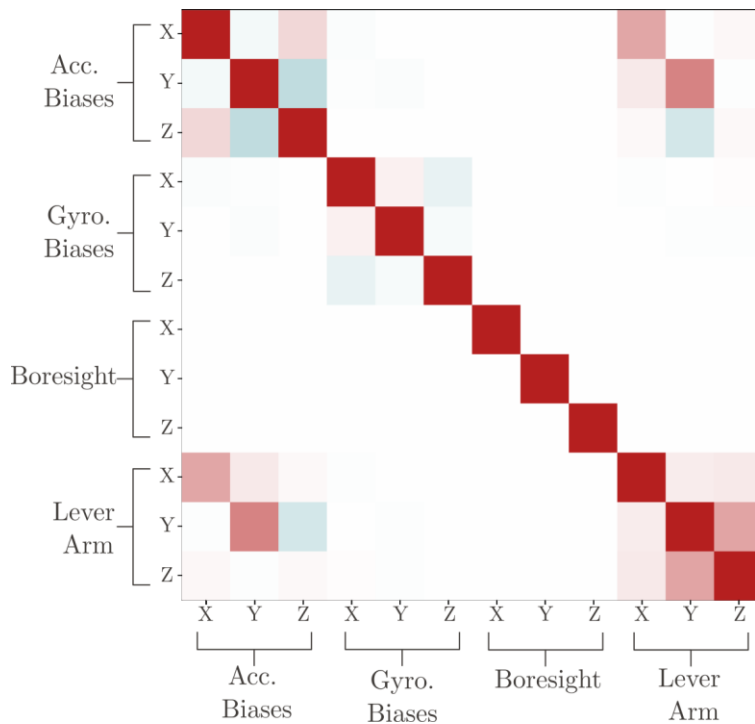


- Errors reduced by a factor 3→5 (attitude and subsequent point cloud)
- A posteriori confidence largely improved

Aerial - Nominal Scenario

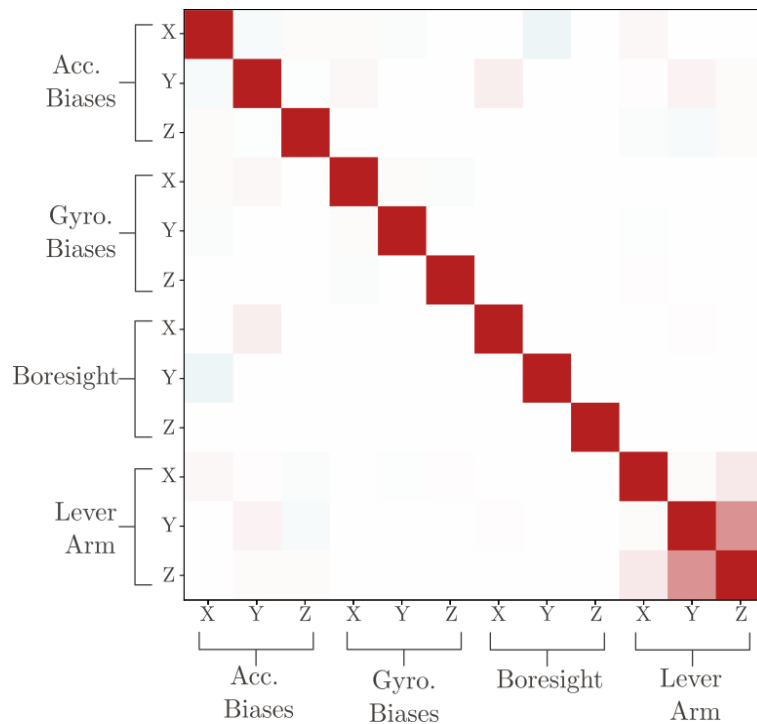
Trajectory. 1 GNSS IMU

Cross-correlation Matrix



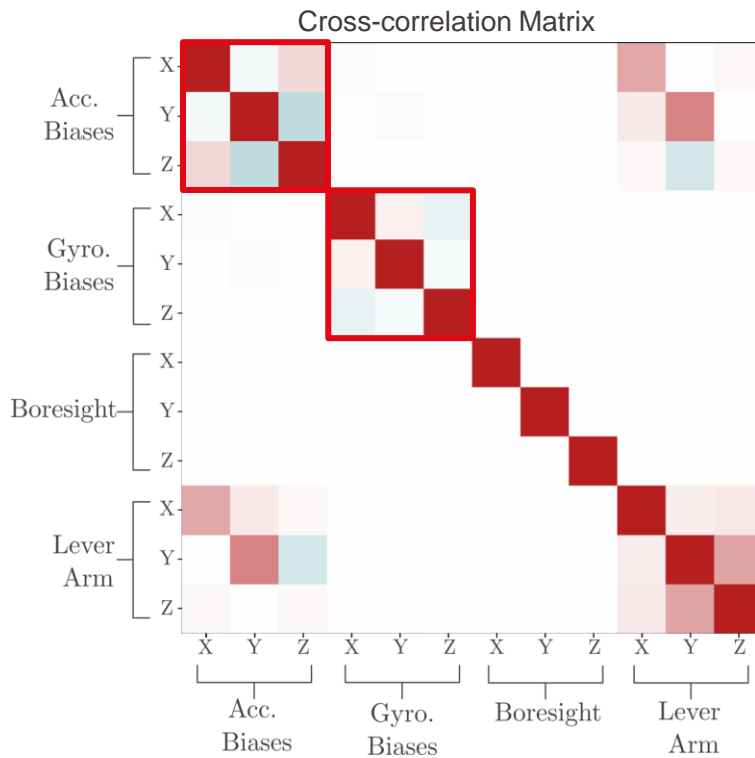
Trajectory. 2 GNSS IMU LiDAR

Cross-correlation Matrix

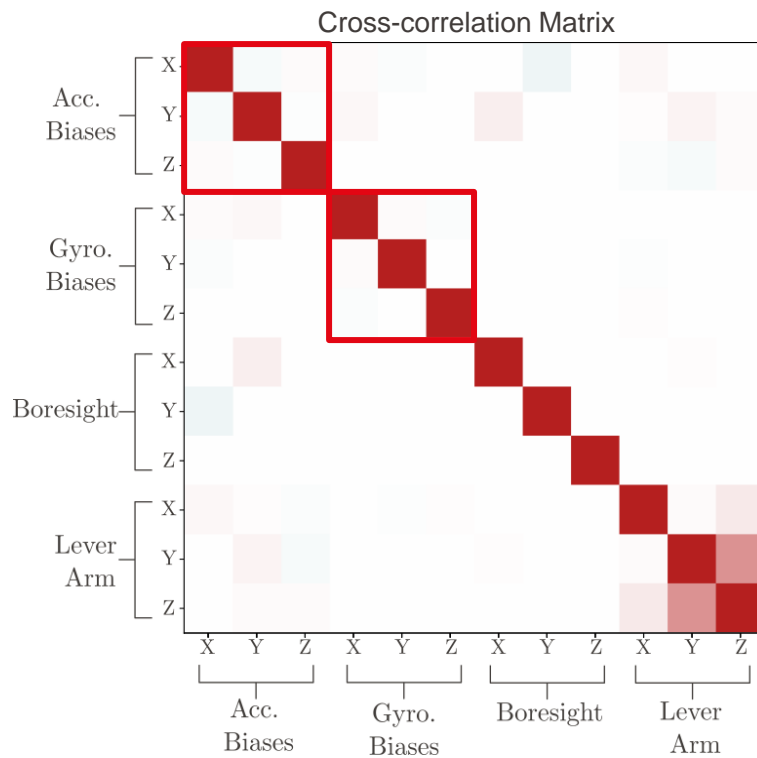


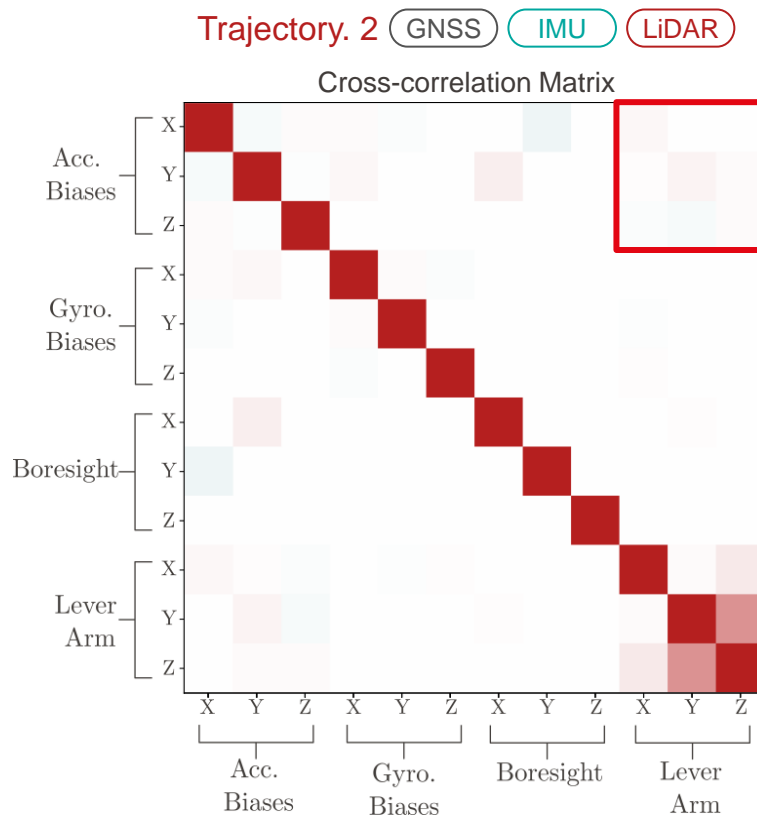
Aerial - Nominal Scenario

Trajectory. 1 GNSS IMU



Trajectory. 2 GNSS IMU LiDAR





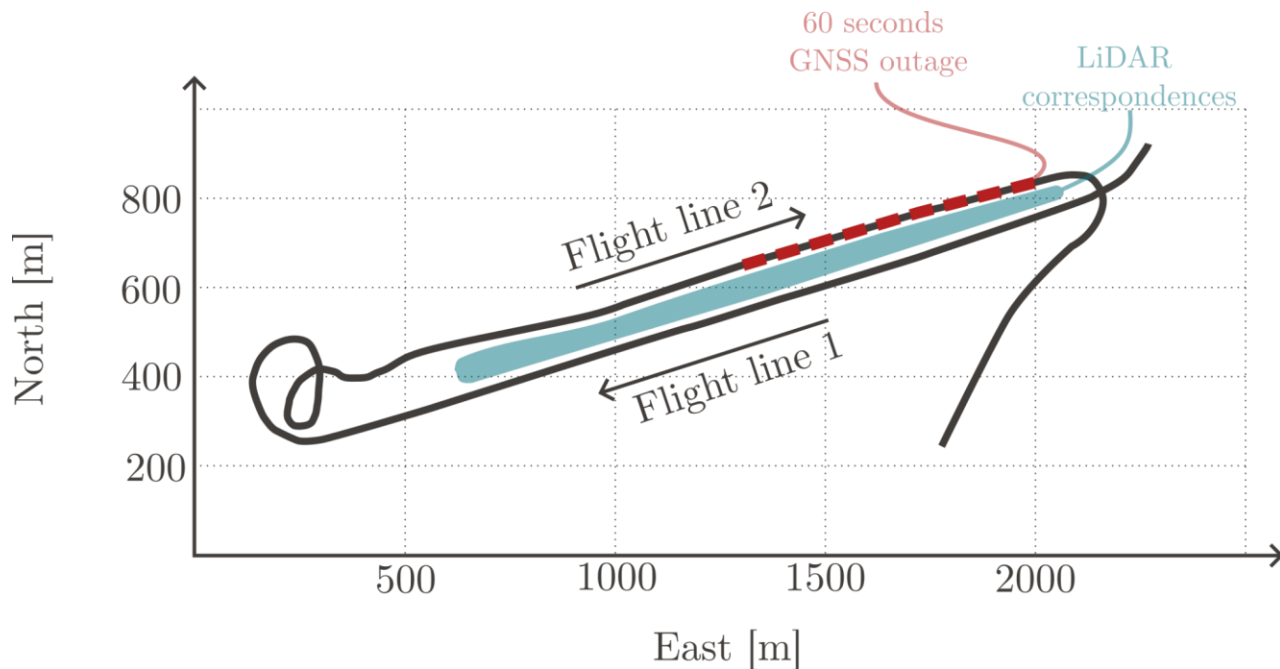
Setup

Aerial - GNSS Outage

Trajectory. 1 (GNSS) (IMU)

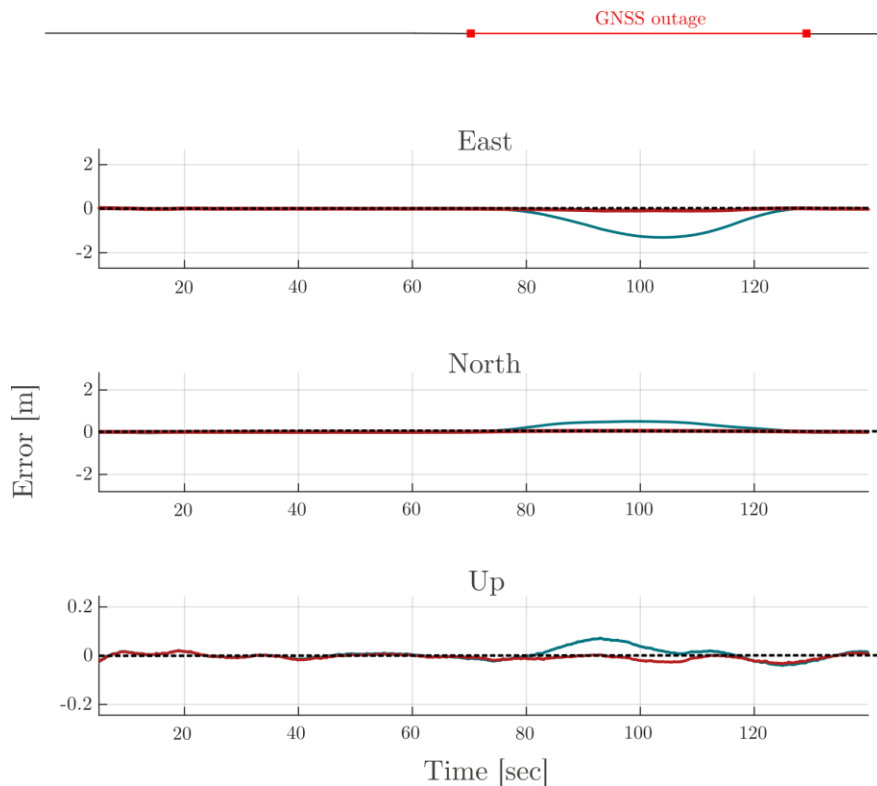
Trajectory. 2 (GNSS) (IMU) (LiDAR)

- Flight duration ~ 5 minutes
- GNSS Outage → large position errors
- Navigation grade (~ ground truth) trajectory available



Results

Aerial - GNSS Outage



Trajectory. 1 (GNSS) (IMU)



T. 1 position error

Trajectory. 2 (GNSS) (IMU) (LiDAR)



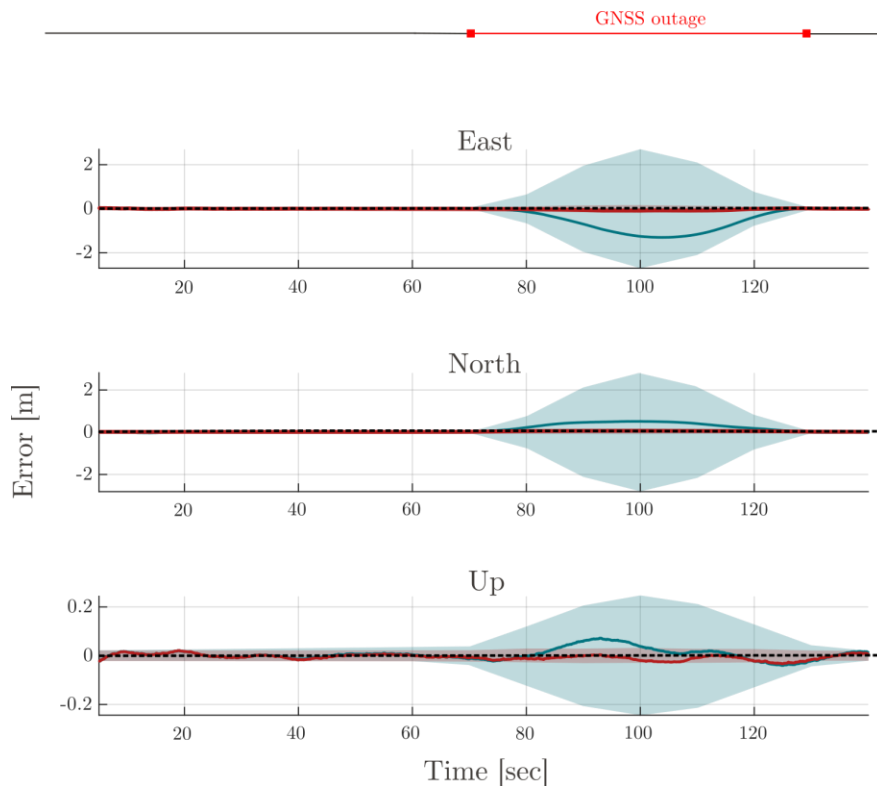
T. 2 position error

- Max. errors reduced by a factor 10→15 (position and subsequent point cloud)

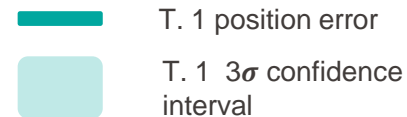


Results

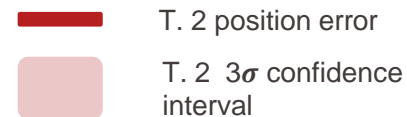
Aerial - GNSS Outage



Trajectory. 1 (GNSS) (IMU)

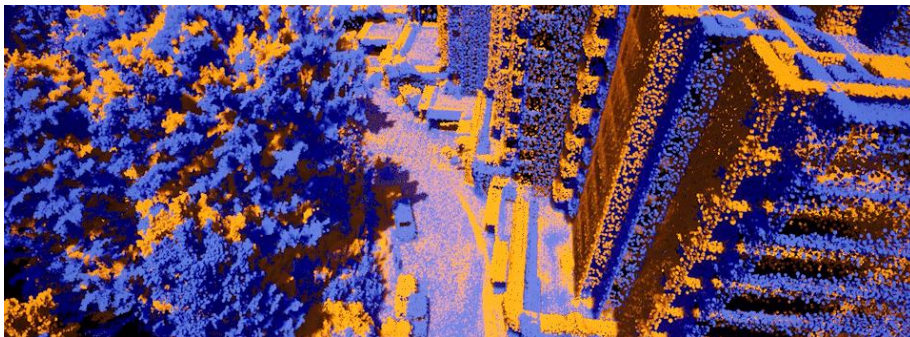


Trajectory. 2 (GNSS) (IMU) (LiDAR)

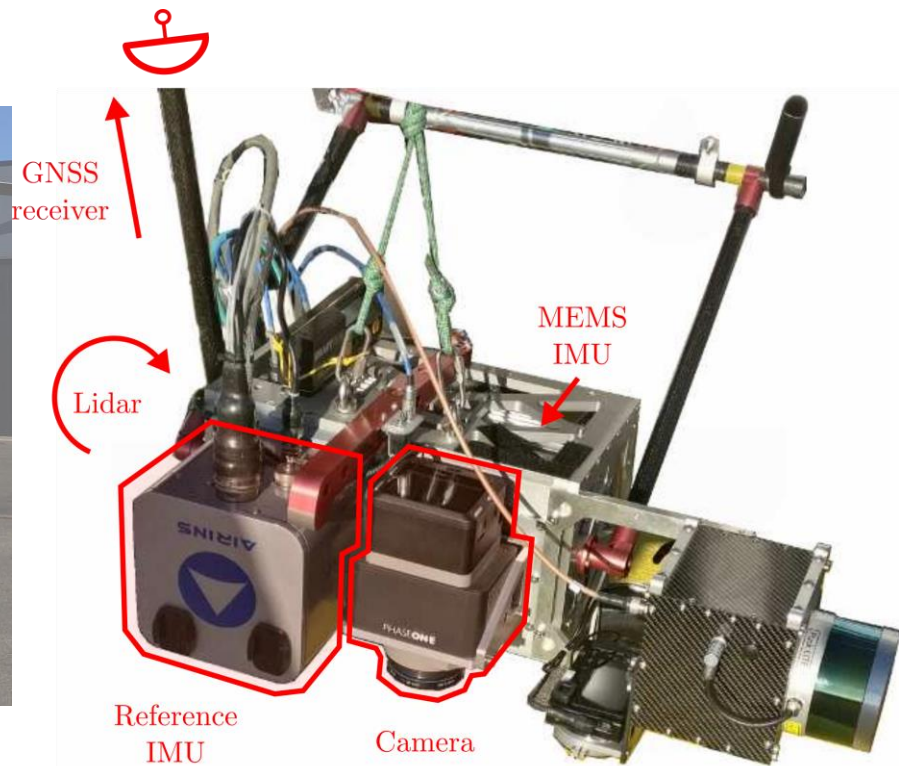


- Max. errors reduced by a factor **10→15** (position and subsequent point cloud)
- Quality and confidence inside the outage maintained comparable to outside of it

- Point to point correspondences in Dynamic Network **improve significantly** trajectory estimation
- Allow estimating **unknown mounting parameters** (i.e. lever-arm + boresight) up to certain accuracy
- Application to other navigation scenarios, e.g. **indoor SLAM** ...



1. A. Brun et. al., 2022, Lidar point-to-point correspondences for rigorous registration of kinematic scanning in dynamic networks, ISPRS Journal of Photogrammetry and Remote Sensing



Setup

Indoor (on-going)

Trajectory 1

IMU

RGB

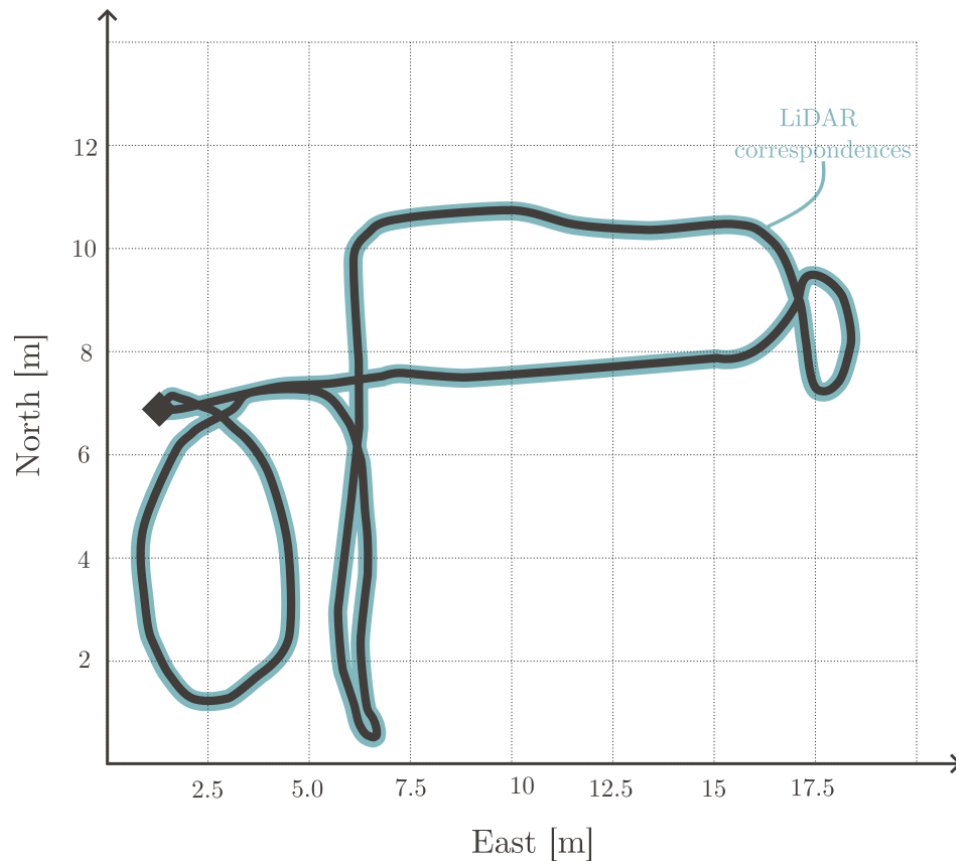
Trajectory 2

IMU

RGB

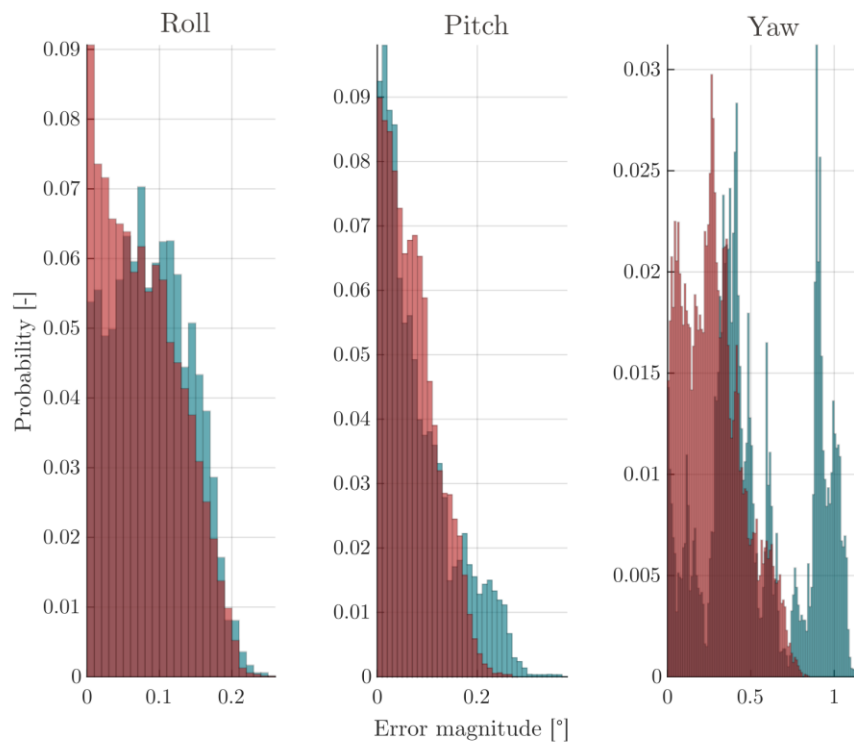
LiDAR

Scan duration ~2.2 minutes



Results

Indoor- GNSS denied



Trajectory. 1

IMU

RGB



T. 1 attitude error

Trajectory. 2

IMU

RGB

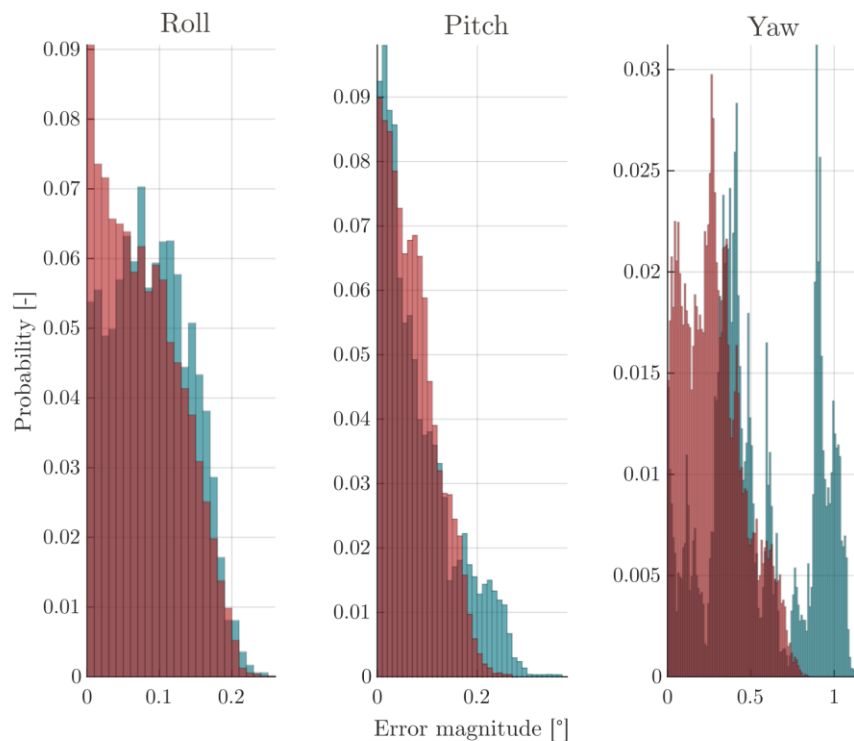
LiDAR



T. 2 attitude error

Results

Indoor- GNSS denied



Trajectory. 1

IMU

RGB



T. 1 attitude error

Trajectory. 2

IMU

RGB

LiDAR



T. 2 attitude error



- Attitude error reduced by 10%, 20% and 50% in roll, pitch and yaw
- Similar potential for system calibration as in aerial setup

LiDAR Soft constraint

