

# Model-based scale-up of a continuously operated consolidated bioprocess based on a microbial consortium for the production of ethanol

Présentée le 1er avril 2022

Faculté des sciences de base Groupe Kröcher Programme doctoral en chimie et génie chimique

pour l'obtention du grade de Docteur ès Sciences

par

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## Acknowledgements

I thank both of my thesis directors, Oliver Kröcher from the Group of Catalaysis for Biofuels at the École Polytechnique Fédérale de Lausanne and Michael Studer from the Laboratory of Biofuels and Biochemicals at the Bern University of Applied Sciences, who gave me the chance to work on a topic of great interest with various exciting challenges. The production of biochemicals is of great importance and being able to be part of this exciting research has been very fulfilling. I want to thank both of you for your great support and thoroughly interesting discussions.

For being part of the examination committee and attending my defense of my PhD work, I would like to thank Prof. Heather Trajano, Prof. Beat Fierz, Prof. em. Philipp Rudolf von Rohr and Prof. François Maréchal.

My special thanks to Simone Brethauer-Studer, Elisabeth Cazier, Simon Bowald, Patrice Bühler, Robert Shahab and Dominik Blaser for all the good times in the laboratory and the intellectual discussions, too . The work environment was very pleasant and I enjoyed the time very much.

Thank you Carsten Wagner, for your support regarding the Matlab® modeling. Your excellent understanding of modeling, from which I could benefit with an incredibly amount of understanding in modeling, helped to keep model consistent and rigorous. Thank you, Dilan Celebi, for your explanations regarding the techno-economic model.

I would like to thank Manfred Muhr and Roman Studer for their support in manufacturing experimental components and IT infrastructure, respectively. For your attentive, administrative support, thank you, Anne Lene.

The work of this PhD thesis was supported by the Swiss Confederation through Innosuisse - Swiss Innovation Agency in the framework of the SCCER BIOSWEET (contract number 1155002550). I am beyond thankful for this financial support.

For their unlimited support through my entire PhD, I want to cordially thank Christina and my family.

David Beat Dempfle, Lausanne 2021

#### **Abstract**

The conversion of non-edible biomass such as lignocellulose to valuable chemicals has been proven to maximize the CO<sub>2</sub> reduction potential of biomass without letting arise ethical conflicts regarding food and feed supply. 2<sup>nd</sup> generation ethanol, being the predominant product of lignocellulosic biomass conversion, however, lacks in economic competitiveness compared to 1<sup>st</sup> generation ethanol from corn or sugar crops. This is due to the required pretreatment of the lignocellulose to break its recalcitrance against microbial activity and the costly enzyme production and enzymatic hydrolysis to depolymerize the cellulose to glucose, which is fermented to ethanol. Consolidated bioprocessing (CBP) based on the synergistic collaboration of a filamentous, cellulolytic fungus Trichoderma reesei and the yeast Saccharomyces cerevisiae was identified as potential solution for economic competitiveness of 2<sup>nd</sup> generation ethanol. CBP involves the highest degree in process intensification for bioprocessing: Enzyme production, enzymatic hydrolysis and fermentation of the released glucose to ethanol are carried out in one process step. This thesis aims to investigate the economics of ethanol production from cellulosic substrates by CBP, to design and conduct continuous CBP experiments and to develop a deep understanding of the process from a chemical engineering point of view in order to enable scale-up of CBP from 2.7 L laboratory scale to 130 L pilot scale.

A techno-economic assessment was conducted to investigate the cost savings by consortium-based CBP at industrial scale and to identify the critical process parameters in terms of costs. Compared to conventional ethanol production from lignocellulose in individual process steps, CBP operated at full-scale  $(2,000\ t/d)$  saves up to 27.5 % of the total ethanol production costs. The cost savings are mainly achieved through lower CAPEX due to less apparatus requirements because of the integrated process, as well as through lower OPEX since no glucose is needed for enzyme production. As a result of a detailed sensitivity analysis, scale and yield were identified as the main cost-pushers from a process point of view, whereas the price level of the plant location has the highest impact on the investment conditions. In the EU, CBP yields enough margin for profitable production and the possibility to decentralize biomass valorization, whereas in the world's largest ethanol market, the US, profitable production of lignocellulosic ethanol can only be achieved by CBP combined with other cost saving techniques, such as

utilization of cost-free waste feedstocks, since ethanol has undergone a considerable price slump.

The conduction of continuous experiments is of central importance in this work for two reasons: First, the techno-economic assessment demonstrated the considerable cost savings when CBP is operated continuously. Second, continuous steady-state operation is time-invariant and thus, allows to fit and validate a rigorous process model without the need to account for growth dynamics. Steady-state operation was achieved multiple times with a maximum titer of  $3.258\pm0.007~\frac{g}{T}$  and a productivity of  $0.025~\frac{g}{T.*h}$ . It was proven, that *T. reesei* produces constantly enzymes over 750 h, which is in agreement with kinetic models considering enzyme production a growth-unrelated process carried out by the secondary mycelia of *T. reesei*. The continuous experiments showed that the oxygen flux per membrane area is a critical parameter for the process. Setups with identical volumetric oxygen transfer rate  $k_L a$ , but different oxygen fluxes per membrane area (large area & low concentration gradient vs. small area and high concentration gradient) showed titer differences of ca. 80 % (1.83  $\frac{g}{L}$  vs 3.26  $\frac{g}{L}$ ) in favor of setups with the large membrane surface. The difference was attributed to long diffusion paths in thicker biofilms and thus, shortage in nutrient supply. A rigorous process model, which included all reaction kinetics and mass transfer limitations of the system confirmed this hypothesis. The fungal biofilm thickness  $\delta_f$  was found to be a critical parameter with an optimum for every membrane configuration. Smaller  $\delta_f$  reduced the fungal biofilm volume and thus, the enzyme production unnecessarily and larger  $\delta_f$  increased the diffusion path length and caused shortage in nutrient supply as well as lower enzyme concentrations in the bulk.

Scaling up bioprocesses is a complex tasks because of the heterogeneity of the biological system as well as chemical and mechanical sensitivity of the cells, which often cause performance decrease at higher scales. In this work, the systematic scale-up approach of non-dimensionalizing the problem and requesting non-dimensional similarity was combined with the simulation outcome of the rigorous process model in order to scale up a membrane aerated biofilm reactor to produce lignocellulosic ethanol by consolidated processing. The synergy of identifying trade-offs with a basic, systematic approach and resolve them with a highly differentiated model with the minimum selling price as optimization criterion was proven. Regarding the final results, it was distinguished between an industrial favorable solution and an academically feasible solution to experimentally prove the scale-up guidelines at 150 *L* pilot scale fermenter based on model data with 3 *L* lab scale fermenter.

Finally, popular rate-controlled separation techniques in biotechnology, were investigated regarding their potential together with CBP. It was focused on in-situ and slip stream ethanol separation setups in order to reduce yeast inhibition additional to the general advantages of

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rate-controlled separations such as avoiding limitations by an azeotrope or the unfavorable vapor-liquid equilibrium of highly diluted ethanol-water mixtures.

However, except from CO<sub>2</sub> stripping and pervaporation, all mechanism fail to handle the solids of the fermentation broth. CO<sub>2</sub> stripping is limited by a poor ethanol recovery due to the trade-off between bubble residence time and stable bubble flow regime. Pervaporation, being the most promising concept for *in-situ* product removal, would be a cost-saving alternative to distillation for batch operation, but is limited by an unfavorable vapor-liquid equilibrium due to low bulk concentrations during continuous operations.

**Keywords:** Consolidated bioprocessing, lignocellulose, ethanol, techno-economic assessment, continuous bioprocess, rigorous model, scale-up, *in-situ* product removal, *Trichoderma reesei*, *Saccharomyces cerevisiae* 

## Zusammenfassung

Die Umwandlung von nicht-essbarer Biomasse wie Lignozellulose in wertvolle Chemikalien maximiert nachweislich das CO<sub>2</sub>-Reduktionspotenzial von Biomasse, ohne ethische Konflikte in Bezug auf die Lebensmittel- und Futterversorgung auszulösen. Ethanol der 2. Generation, das häufigste Produkt der Umwandlung von Lignozellulose-Biomasse, ist jedoch wirtschaftlich nicht gleichermassen wettbewerbsfähig wie Ethanol der 1. Generation. Dies liegt an der erforderlichen Vorbehandlung der Lignozellulose, um ihre Resistenz gegenüber mikrobieller Aktivität zu brechen, sowie an der kostspieligen Enzymproduktion und enzymatischen Hydrolyse zur Depolymerisierung der Zellulose zu Glukose, die zu Ethanol vergoren wird. Ein konsolidierter Bioprozess (CBP), welcher auf der synergetischen Zusammenarbeit eines filamentösen, zellulolytischen Pilzes Trichoderma reesei und der Hefe Saccharomyces cerevisiae basiert, stellt eine mögliche Lösung für die wirtschaftliche Wettbewerbsfähigkeit von Ethanol der 2. Generation dar. CBP erreicht den höchsten Grad der Prozessintensivierung in der Biotechnologie: Enzymproduktion, enzymatische Hydrolyse und Fermentation der freigesetzten Glukose zu Ethanol werden in einem Prozessschritt durchgeführt. Ziel dieser Arbeit ist es, die Wirtschaftlichkeit der Ethanolproduktion aus zellulosehaltigen Substraten mittels CBP zu untersuchen, kontinuierliche CBP-Experimente zu konzipieren und durchzuführen und ein verfahrenstechnisches Verständnis des Prozesses zu entwickeln, um einen Scale-up basierend auf CBP im 2.7-Liter-Laborvolumen hin zu einem Pilotfermenter mit 130-Liter-Volumen zu ermöglichen.

Es wurde eine technisch-ökonomische Bewertung durchgeführt, um die Kosteneinsparungen durch den Konsortium-basierten CBP im industriellen Massstab zu untersuchen und die kritischen Prozessparameter in Bezug auf die Kosten zu identifizieren. Im Vergleich zur konventionellen Ethanolproduktion aus Lignozellulose in einzelnen Prozessschritten spart CBP bei industriellem Massstab (2'000 t/d) bis zu 27.5 % der gesamten Ethanolproduktionskosten ein. Die Kosteneinsparungen werden vor allem durch geringere CAPEX erreicht, da aufgrund des integrierten Prozesses weniger Apparate benötigt werden, sowie durch geringere OPEX, da keine Glukose für die Enzymproduktion benötigt wird. Als Ergebnis einer detaillierten Sensitivitätsanalyse wurden die Grösse der Anlage und die Ausbeute als die wichtigsten Kostentreiber

aus verfahrenstechnischer Sicht identifiziert, während das Preisniveau des Anlagenstandorts den grössten Einfluss auf die Investitionsbedingungen hat. In der EU bietet CBP genügend Spielraum für eine rentable Produktion und die Möglichkeit, die Biomasseverwertung zu dezentralisieren, während im weltgrössten Ethanolmarkt, den USA, eine rentable Produktion von lignozellulosehaltigem Ethanol nur durch CBP in Kombination mit anderen kostensparenden Massnahmen, wie z.B. der Nutzung von kostenfreien Abfallrohstoffen, erreicht werden kann, da Ethanol einen erheblichen Preisverfall erlebt hat.

Die Durchführung von kontinuierlichen Versuchen ist in dieser Arbeit aus zwei Gründen von zentraler Bedeutung: Erstens hat die technisch-ökonomische Bewertung gezeigt, dass der kontinuierliche Betrieb von CBP zu erheblichen Kosteneinsparungen führt. Zweitens ist der kontinuierliche Betrieb im stationären Zustand zeitinvariant und ermöglicht somit die Anpassung und Validierung eines rigorosen Prozessmodells, ohne dass die Wachstumsdynamiken berücksichtigt werden müssen. Der stationäre Zustand wurde mehrfach erreicht und ein maximaler Titer von  $3.26\pm0.01~\frac{g}{L}$  sowie eine Produktivität von  $0.025~\frac{g}{L*h}$  gemessen. Es wurde nachgewiesen, dass T. reesei über 750 h konstant Enzyme produziert, was mit kinetischen Modellen übereinstimmt, die die Enzymproduktion als einen nicht direkt wachstumsabhängigen Prozess betrachten, der von den sekundären Myzelien von T. reesei durchgeführt wird. Die kontinuierlichen Experimente zeigten, dass der Sauerstofffluss pro Membranfläche ein kritischer Parameter für den Prozess ist. Bei Versuchen mit identischer volumetrischer Sauerstofftransferrate  $k_L a$ , aber unterschiedlichen Sauerstoffflüssen pro Membranfläche (grosse Fläche und niedriger Konzentrationsgradient vs. kleine Fläche und hoher Konzentrationsgradient) ergaben sich Titerunterschiede von ca. 80 % (1.83  $\frac{g}{L}$  vs. 3.26  $\frac{g}{L}$ ) zugunsten der Versuchsanordnung mit der grossen Membranfläche. Der Unterschied wurde auf die langen Diffusionswege in dickeren Biofilmen und damit auf einen Mangel an Nährstoffzufuhr zurückgeführt. Ein rigoroses Prozessmodell, das alle reaktionskinetischen und stofftransportbedingten Einschränkungen des Systems berücksichtigte, bestätigte diese Hypothese. Die Pilz-Biofilmdicke  $\delta_f$  erwies sich als relevanter Parameter mit einem Optimum für jede Membrankonfiguration. Ein kleineres  $\delta_f$ verringerte das Volumen des Pilzbiofilms und damit die Enzymproduktion unnötig, während ein grösseres  $\delta_f$  die Diffusionsweglänge vergrösserte und zu einem Mangel der Nährstoffzufuhr sowie zu geringeren Enzymkonzentrationen in der flüssugen Phase führte.

Die Skalierung von Bioprozessen ist eine komplexe Aufgabe, da die Heterogenität des biologischen Systems sowie die chemische und mechanische Empfindlichkeit der Zellen oft zu einem Leistungsabfall bei höheren Skalen führen. In dieser Arbeit wurde der systematische Scale-up-Ansatz der Entdimensionalisierung des Problems und der Forderung nach dimensionsloser Ähnlichkeit mit den Simulationsergebnissen des rigorosen Prozessmodells kombiniert, um einen membranbelüfteten Biofilmreaktor zur Herstellung von Ethanol aus Lignozellulose mithilfe eines konsolidierten Bioprozesses zu vergrössern. Die Synergie zwischen

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der Identifizierung von Zielkonflikten mit einem grundlegenden, systematischen Ansatz und deren Lösung mit einem hochdifferenzierten Modell und dem minimalen Verkaufspreis als Optimierungskriterium wurde nachgewiesen. In Bezug auf die Endergebnisse wurde zwischen einer industriell favorisierten Lösung und einer akademisch machbaren Lösung unterschieden, um die Scale-up-Richtlinien für einen 150 *L*-Fermenter auf der Grundlage von Modelldaten mit einem 3 *L*-Laborfermenter experimentell zu beweisen.

Zuletzt wurden gängige ratengesteuerte Trenntechniken in der Biotechnologie auf ihr Potenzial in Verbindung mit CBP untersucht. Zusätzlich zu den allgemeinen Vorteilen von ratengesteuerten Trennungen, wie z.B. die Vermeidung von Einschränkungen durch ein Azeotrop oder das ungünstige Dampf-Flüssigkeits-Gleichgewicht von stark verdünnten Ethanol-Wasser-Gemischen, lag der Schwerpunkt dabei auf *in-situ-* und Slip-Stream-Ethanolabtrennungen, um die Inhibierung der Hefe zu reduzieren.

Mit Ausnahme des CO<sub>2</sub>-stripping und der Pervaporation sind jedoch alle Verfahren nicht in der Lage, mit dem Feststoffgehalt der Fermentationsbrühe umzugehen. Das CO<sub>2</sub>-stripping ist durch eine schlechte Ethanolrückgewinnung aufgrund des Zielkonflikts zwischen Blasenverweilzeit und stabilem Blasenfluss begrenzt. Die Pervaporation, das vielversprechendste Konzept für die *in-situ-*Produktentfernung, wäre eine kostensparende Alternative zur Destillation für den Chargenbetrieb, wird aber durch ein ungünstiges Dampf-Flüssigkeits-Gleichgewicht aufgrund niedriger Endkonzentrationen im kontinuierlichen Betrieb eingeschränkt.

**Schlüsselwörter:** Konsolidierter Bioprozess, Lignozellulose, Ethanol, Techno-ökonomische Bewertung, kontinuierlicher Bioprozess, rigoroses Modell, scale-up, *in-situ* Produktentfernung, *Trichoderma reesei*, *Saccharomyces cerevisiae* 

#### Nomenclature

#### List of abbreviations

A. phoenicis
 BC
 Boundary condition
 CAPEX
 Capital expenditure
 CBH
 Cellobiohydrolase

CBP Consolidated bioprocessing CCS Carbon capture and storage

CDW Cell dry weight

CEPCI Chemical Engineering Plant Cost Index

CME Chicago mercantile exchange
CNC Computerized numerical control
CSTR Continuously stirred tank reactor

D. BruxellensisDoFDegree of freedomEGEndoglucanase

EPFL École Polytechnique Fédérale de Lausanne

FoB Free on board

FGD Flue gas desulfurization

FPU Filter paper unit GHG Greenhouse gas

GMO Genetically modified microorganism

HPLC High Performance Liquid Chromatography
IPCC Intergovernmental panel on climate change
ISO International organization for standardization

MESP Minimum ethanol selling price

NREL National Renewable Energy Laboratory

OPEX Operational expenditure
PDMS Polydimethylsiloxane
PFR Plug flow reactor

PID Proportional-integral-differential

PPP Purchasing power parity rpm Rounds per minute

S. cerevisiae Saccharomyces cerevisiae

SSF Simultaneous saccharification and fermentation

T. reesei Trichoderma reesei

UV Ultraviolet

## List of symbols

## Orders of magnitude

Nano  $[10^{-9}]$ n Mikro  $[10^{-6}]$ μ Milli  $[10^{-3}]$ т Centi [10<sup>-2</sup>] С k Kilo [10<sup>3</sup>] Mega  $[10^6]$ M G Giga [10<sup>9</sup>] Exa [10<sup>18</sup>] Е

#### Latin & Greek letters

A Surface area  $[m^2]$  β Selectivity [-] β-G β-glucosidase C Clearance [m]

[C] Concentration of active substrate sites  $\frac{kg}{m^3}$ 

*c* Concentration  $\frac{kg}{m^3}$ 

 $\delta_f$  Fungal biofilm thickness [m]

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D	Dilution rate $[s^{-1}]$ resp. diffusion coefficient $[\frac{m^3}{s}]$
d	diameter [m]
η	Dynamic viscosity $[Pa \cdot s]$ resp. yield $[-]$
[E]	Enzyme concentration $\frac{kg}{m^3}$
$E_A$	Activation energy $\frac{J}{mol}$
[EC]	Concentration of enzyme-substrate-complexes $\frac{kg}{m^3}$
Еи	Euler number
$\varphi$	Angular coordinate
$\gamma$	Arrhenius number $[-]$
8	Gravitational acceleration $\left[\frac{m}{s^2}\right]$
Н	Henry coefficient $\frac{kg}{m^3Pa}$ resp. height $[m]$
h	Height [m]
J	Mass flux $\frac{kg}{m^3s}$
K	Half-saturation constant $\frac{kg}{m^3}$
k	Rate constant $\left[\frac{1}{s}\right]$
$k_{conv}$	Konvective mass transfer coefficient $\left[\frac{m}{s}\right]$
$k_L$ a	Volumetric oxygen transfer coefficient $[s^{-1}]$
λ	Kolmogorov scale [m]
L	Length [m]
μ	Microbial growth rate $[s^{-1}]$
M	Maintenance coefficient $\left[\frac{1}{s}\right]$ resp. molar mass $\left[\frac{kg}{mol}\right]$
m	Mass $[kg]$
ν	Reaction rate $\frac{kg}{m^3s}$ resp. kinematic viscosity $\frac{m^2}{s}$
n	Mole fraction [-]
Nu	Nusselt number $[-]$
P	Performance $[-]$ resp. power $[W]$
p	Pressure [Pa]
Pe	Péclet number
Pr	Prandtl number
Q	Permeance $\frac{mol}{m^3 Pa}$
ρ	Density $\frac{kg}{m^3}$
R	Universal gas constant $\frac{J}{mol \cdot K}$
r	Radius $[m]$ resp. reaction rate $\frac{kg}{m^3s}$
Re	Reynolds number
$\sigma$	Adsorption capacity [-]

2	5	So	oluk	oility	$\frac{\kappa g}{m^3 Pa}$	resp.	pitch	[m]	

 $\begin{array}{ccc} Sc & & \text{Schmidt number} \\ Sh & & \text{Sherwood number} \\ \tau & & \text{Residence time } [s] \end{array}$ 

 $\begin{array}{ccc} t & & \text{Time } [s] \\ u & & \text{Velocity } \frac{m}{s} \end{array}$ 

V Volume  $[m^3]$  v Velocity  $[\frac{m}{s}]$ 

 $\dot{V}$  Volumetric flow rate  $\left[\frac{m^3}{s}\right]$ 

W Width wt.% weight %

[X] Concentration of microbial biomass  $\frac{kg}{m^3}$ 

x Liquid-phase mole fraction [-]

Y Yield coefficient [-]

y Gas-phase mole fraction [-]  $\zeta$  Pressure loss coefficient [-]

z Axial coordinate [m]

## List of superscripts & subscripts

abs Absoluteb Bulk phasebf Biofilm

 $\beta - G$   $\beta$ -glucosidase C Cellulose c conversion Cb Cellobiose

CBH Cellobiohydrolase

convConvectiveCSCentral screw

CSTR Continuously stirred tank reactor

d Delay resp. decaydegr Degradation

Nomenklatur xv

 $\begin{array}{ccc} \textit{diff} & & \text{Diffusive} \\ E & & \text{Enzyme} \\ \textit{eff} & & \text{Effective} \end{array}$ 

EG Endoglucanaseendo Endoglucanase

EtOH Ethanol

exo Exoglucanase

f Fungal biofilm layer resp. free

G Glucose

i Generic species i

in Inlet L Length m Membrane max maximum min minimum

o inner membrane phase

O<sub>2</sub> Oxygenout outletox Oxygen

*p* Primary resp. pressure*P* Particle resp. permeate

reacReactorssecondarysecsecondarysynthSynthesistotTotal

tr Trichoderma reesei

w water Y yeast

y yeast biofilm layer

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# CHAPTER 1

#### Introduction

In the framework of the Paris Agreement, 195 nations agreed on reducing the greenhouse gas (GHG) emissions in order to keep global warming below  $1.5\,^{\circ}$ C compared to pre-industrial level. [20] According to simulations of the intergovernmental panel on climate change (IPCC), the  $1.5\,^{\circ}$ C goal may be achieved by either a reduction of CO<sub>2</sub> emissions by  $50\,\%$  -  $70\,\%$  within 10 years a net negative CO<sub>2</sub> emissions below 5 Gt p.a. from 2060 onwards or by less reductions in the near future and net negative CO<sub>2</sub> emissions of 10 Gt p.a. - 20 Gt p.a. towards the end of the  $21^{st}$  century to compensate for the "overshoot" (Fig. 1.1 left). [1]

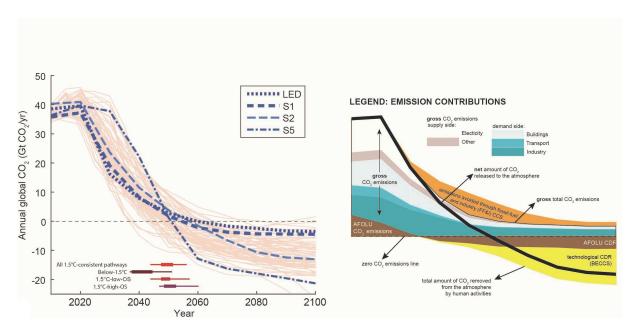


Figure 1.1: Left: The light orange lines show all emission scenarios leading to global warming below 1.5 °C relative to pre-industrial level according to IPCC models. The blue dashed, dotted and dashed-dotted lines show representative scenarios with low, medium and high overshoot in GHG emissions. Right: The scenario with medium GHG emission overshoot is decomposed into the net emissions of the sectors agriculture (brown), transport (blue), industry (turquoise), electricity buildings (white) as well as carbon capture and storage (CCS, orange & yellow), which reduces the net emissions. [1]

However, a GHG emission overshoot may kick off a cascade of self-reinforcing effects leading to a new equilibrium, the "hothouse earth", with serious disruptions to ecosystems society and economies. [20] In order to avoid these self-reinforcing effects, it is important to deploy any renewable resource in the short-term within the existing infrastructure. In the long term, the CO<sub>2</sub> saving potential of each renewable resource needs to be maximized to achieve CO<sub>2</sub> neutrality and more specifically net negative emissions.

Ethanol is a suitable example for distinguishing between short term and long term utilization: It has gained a lot of attention as a blend for biofuels despite the controversial discussion whether biofuels are a suitable way to decarbonize individual transport. [21,22] Given the fact, that in Switzerland, a 94 % fraction of the energy for the transport sector in 2019 was provided by fossil fuels, which contributes 34 % to the total fossil resource demand of Switzerland [23], ethanol as fuel blend or substitute could immediately contribute to emission reductions in the short term. However, in the long term, the concerns of using ethanol for individual transport are justified since the sustainable biomass potential in Switzerland is not even sufficient to supply aviation, cargo shipping with fuel and satisfy the Swiss chemical demand, which would lead to the largest CO<sub>2</sub> savings. [23–25] While being unsuitable as fuel for aviation or cargo shipping, ethanol is used as chemical in numerous industrial and consumer products as

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intermediate of other chemicals (e.g. in the production of drugs, plastics, lacquers etc.) or as solvent (e.g. cosmetics). [26] Concluding, it can be said, that depending of its use, ethanol is an important chemical to effectively mitigate climate change by reducing GHG emissions in the short and long run. [27]

However, currently bioethanol is produced mainly from edible feedstocks (share >96 %). [28] These so-called first generation biofuels not only cause a conflict between fuel supply and food/feed issues, but they may have a non-compensable carbon footprint [29]. Lignocellulosic biomass, the most abundant resource of fixed renewable carbon in the world, serves as feedstock for second generation biofuels having a much lower or even no carbon debt compared to first generation biofuels and the conflict with the feed and food industry is avoided since it is non-edible [29,30]. The production of lignocellulosic ethanol gained attraction in the context of the "bio-based economy" strategy of several entities such as the US & the EU and has been in growth on an industrial scale since the early 2000s [31,32].

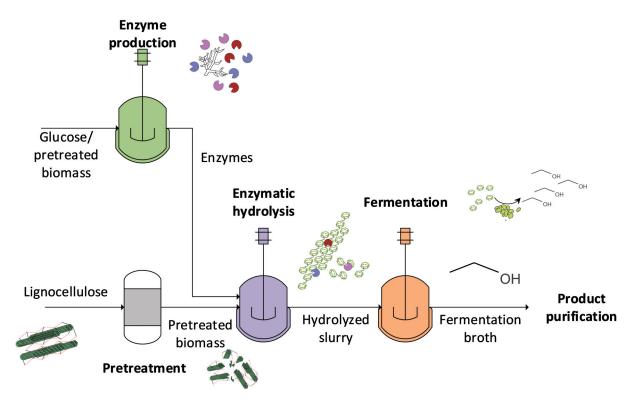


Figure 1.2: Process scheme of state-of-the-art ethanol production from lignocellulose. The lignocellulose is pretreated to break up its structure and make the cellulose fibers accessible for enzymes, which are produced by a fungus in a separate enzyme production unit. After enzymatic hydrolysis, where the polymeric cellulose is depolymerized to sugars, the slurry is sent to fermentation, where the fermenting microorganisms converts the released sugars to ethanol, which is purified afterwards. [2]

Lignocellulose is a non-edible, complex structure in the cell wall of plant biomass. [9] It consists of cellulose (40-50 %), hemicellulose (25-30 %) and lignin (15-20 %). [30] In contrast to edible carbon sources such as corn or sugar crops, lignocellulose needs to be pretreated to overcome the recalcitrance induced by the lignin and it needs to be hydrolyzed before fermentation, because the glucose molecules are covalently bonded in the  $\beta$ -(1–4) configuration (Fig. 1.2). [9] During hydrolysis, enzymes depolymerize the cellulose and release the glucose monomer (Fig. 1.2). [30] The necessary pretreatment and the hydrolysis lead to increased costs of so-called 2<sup>nd</sup> generation ethanol resulting in a competitive disadvantage compared to 1<sup>st</sup> generation ethanol from edible resources. [2,33]

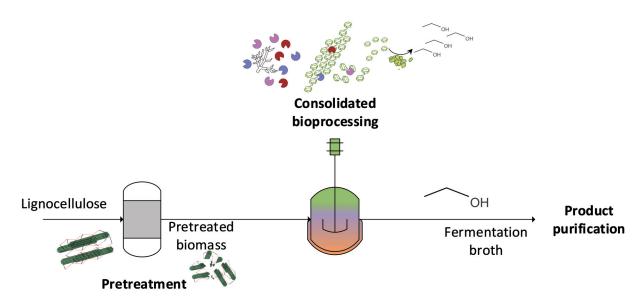


Figure 1.3: Process scheme of CBP ethanol production from lignocellulose. The pretreatment does not differ from state-of-the-art ethanol production, but enzyme production, enzymatic hydrolysis and fermentation are merged into one process step to reduce the number of apparatus and save costs. [3]

Continuously operated consolidated bioprocessing (CBP) was identified as strongest lever to reduce the processing costs of 2<sup>nd</sup> generation bioethanol in order to achieve profitable production. [33] CBP describes a highly integrated bioprocess, where enzyme production, enzymatic hydrolysis and fermentation of the released glucose to ethanol is carried out in one process step (Fig. 1.3). [4] CBP is either realized by deploying a genetically modified microorganism (GMO), which is able to do both, hydrolyzing cellulose and fermenting sugars to ethanol, in conventional bioreactors or by co-cultivating a microbial community, where the labor of hydrolysis and fermentation is divided between different species, in well-designed reactor systems with niches for each community member. [3,34]

In this work, CBP is realized based on a microbial consortium consisting of a filamentous,

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cellulolytic fungus *Trichoderma reesei* and a yeast *Saccharomyces cerevisiae*, which ferments glucose. [4] The community is stabilized by biofilm formation on an aerated membrane, which results in two well-established niches (Fig. 1.4): An aerobic biofilm layer on top of the membrane, where the aerobic fungus *T. reesei* secretes enzymes for cellulose hydrolysis, and an anoxic bulk phase, where enzymatic hydrolysis happens and relased glucose is fermented to ethanol by the facultative anaerobe *S. cerevisiae*. [4] This setup allows to take advantage of a stable community of robust industrial strains instead of using fragile genetically modified microorganisms [34] as well as to exploit the beneficial features of a biofilm such as higher enzyme expression of surface-attached cultures [35] or the immobilization of the microbial biomass allowing to omit the costly cell recycling processes, which are used in industry for bioprocesses with suspended cultures. [36,37]

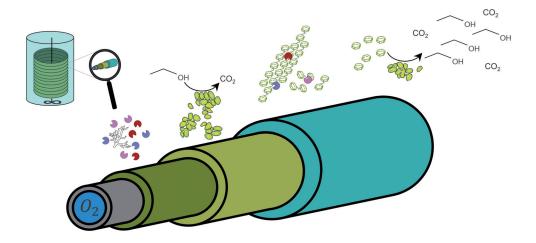


Figure 1.4: Schematic illustration of CBP based on a microbial consortium with well-established niches in a reactor system. An oxygen aerated membrane (grey tubular element) is winded in helical shape within a bioreactor (upper left corner). The oxygen (blue) diffuses across the membrane (grey) and creates an oxygen enriched layer around the membrane. The aerobic, enzyme producing fungus *T. reesei* (dark green) grows in this layer and consumes a large fraction of the oxygen. The remaining oxygen is consumed by a second layer on the biofilm (light green) consisting of yeast cells, which perform aerobic metabolism. In the anoxic bulk phase (turquoise), the cellulose is hydrolyzed by the enzymes, which diffused from the fungal biofilm layer into the bulk, and the suspended yeast cell ferment the released glucose to ethanol. A fraction of glucose diffuses back into the biofilm and feeds the aerobic fungus. [4]

This thesis is a project in the framework of the Swiss energy strategy 2050, which targets CO<sub>2</sub> neutrality and opting out of the nuclear energy program. [38] The Swiss competence center for energy research (SCCER) BIOSWEET was established to maximize the role of biomass in this energy transition. The clear objective was to bring innovative biomass conversion technologies, which can be implemented seamlessly, to the industry and with that to the market. [39] As

shown above, consortium-based consolidated bioprocessing of lignocellulose to ethanol is such an innovative conversion technology, for what reason this thesis is expected to deliver the engineering work for industrial implementation of CBP.

# 1.1 Thesis objectives

This thesis aims to pave the way for industrial implementation of consortium-based CBP in order to efficiently produce chemicals from lignocellulose and thus, maximize the CO<sub>2</sub> savings. [4] Prerequisites for industrial implementation of a process are profitability, a deep understanding of the process on an engineering level and a robust guideline for scale-up. These requirements laid the groundwork for the thesis goals, which are briefly described in the following.

- 1. Techno-economic assessment of consolidated bioprocessing of lignocellulose to ethanol at industrial scale. A techno-economic assessment of consortium-based CBP is essential as it depicts the economic potential of CBP when compared to conventional ethanol production as well as the critical process parameters in terms of costs. Furthermore, any design trade-offs during scale-up are likely to be resolved in favor of lower processing costs. A techno-economic model allows to set the ethanol selling price as optimization criterion and perform simulations with different process condition to identify the optimum conditions with the minimum selling price. The techno-economic model is presented in chapter 2.
- 2. Continuous operation of a membrane aerated biofilm reactor for consortium-based consolidated bioprocessing of cellulose to ethanol. Continuously operated CBP at steady-state conditions is beneficial in various aspects such as lower costs due to reduced downtimes or potentially higher productivity since product and substrate inhibition are avoided or at least effectively reduced. However, the continuous operation of consortium-based CBP was never proven at laboratory scale. Continuous CBP experiments were conducted within this project for two purposes: First, as proof-of-concept that the microbial consortium can be maintained at a productive state during continuous operation and second, the experimental results of the continuous steady-state were used to fit and validate the process model because they are time-invariant. Batch data is dominated by growth dynamics, which strongly depend on the given initial conditions and thus, useless for the process model. However, continuously operated consolidated bioprocessing is challenging: An insoluble substrate needs to be fed continuously and homogeneously, wash-out of enzymes has to be avoided and stable population equilibria of the microbial

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community members must be obtained. Chapter 3 discusses the design adjustments of the experimental setup for continuous operation and the respective results.

- 3. Development and validation of a rigorous, spatially resolved model of the kinetics and mass transfer limitations of consortium-based consolidated bioprocessing for ethanol production. The development and validation of a rigorous process model provides the above-mentioned and needed understanding of CBP from an engineering level, which is the prerequisite for successful scale-up. Both, the kinetics and the mass transfer limitations of CBP differ considerably from suspended cultures for separate enzyme production, hydrolysis and fermentation. This is due to the interaction of the microbial community members, the heterogeneous reactor layout with the different niches and the different aeration technique (membrane diffusion vs. bubble aeration). The process model is presented in chapter 4.
- 4. **Scale-up of 2.7** *L* **laboratory scale consortium-based consolidated bioprocessing to 130** *L* **pilot scale.** Based on the findings above, the economics of the process, the knowledge, how to operate the system continuously, and the rigorous model, the scale-up from 2.7 *L* laboratory scale to 130 *L* pilot scale was designed. Critical scale-up parameters were identified by a classic approach of non-dimenionalizing the system. The optimization for the critical parameters was done with the help of the process model as calculation basis and the techno-economic model as optimization criterion for the lowest costs. A pending experiment at pilot scale should serve as proof of concept that the rigorous process model is scale-invariant and provides a robust scale-up guideline when combined with the classic similarity approach based on non-dimensionalizing the problem. The scale-up calculations are found in chapter 5.
- 5. Evaluation of *in-situ* product removal strategies to improve the productivity and economics of consolidated bioprocessing. *In-situ* product removal seems to be a promising upgrade for consolidated bioprocessing of ethanol since rate-controlled separation techniques bypass the unfavorable equlibrium of low ethanol titers in the bulk of the CBP unit. Furthermore, ethanol losses due to degradation in the biofilm could be minimized by *in-situ* product removal and one option to perform *in-situ* product removal, the membrane, is already installed in the reactor. A detailed overview of different product removal strategies is given and their applicability for CBP is discussed in chapter 6.

# CHAPTER 2

# Techno-economic assessment of consolidated bioprocessing of lignocellulose to ethanol at industrial scale

#### 2.1 Abstract

Lignocellulose-based biofuels are of major importance to mitigate the impact of international traffic and transport on climate change while sustaining agricultural land for food supply. Highly integrated systems like consolidated bioprocessing (CBP), where enzyme production, enzymatic hydrolysis and fermentation of the released sugars are carried out in one reactor, offer the highest potential to save costs and to make lignocellulose-based biofuels economically competitive. The work described here showed that CBP based on a microbial consortium operated at full-scale  $(2,000 \ t/d)$  saves up to 27.5 % of the total ethanol production costs compared to conventional ethanol production from lignocellulose in individual process steps. The cost savings are mainly achieved through lower capital expenditures (CAPEX) due to less apparatus requirements because of the integrated process, as well as through lower operating expenditures (OPEX) since no glucose is needed for enzyme production. A comparison with literature estimations of cost savings of CBP based on genetically modified microorganisms results in approximately the same range. As a result of a detailed sensitivity analysis, scale and yield were identified as the main cost-pushers from a process point of view, whereas the price level of the plant location has the highest impact on the investment conditions. In the EU, CBP yields enough margin for profitable production and the possibility to decentralize biomass valorization, whereas in the world's largest ethanol market, the US, profitable production of lignocellulosic ethanol can only be achieved by CBP combined with other cost saving techniques, such as utilization of cost-free waste feedstocks, since ethanol has undergone a considerable price slump.

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This chapter is based on published work (without any permission needed): D. Dempfle, O. Kröcher, M. H. Studer *Techno-economic assessment of bioethanol production from lignocellulose by consortium-based consolidated bioprocessing at industrial scale*. New Biotechnology, 65 (2021) 53–60, doi: 10.1016/j.nbt.2021.07.005

# 2.2 Introduction

According to the international energy outlook 2020 of the US Energy Information Administration the world's energy consumption for transportation will continue to increase at an average annual rate of  $1.3\pm0.2$  %, leading to a projected total consumption of roughly 290 *Exajoule* (*EJ*) in 2050, which is mainly driven by a doubled energy demand in non-OECD countries in 2050 compared to 2018 [40]. The expected share of electrical power supply in the light duty transportation sector will not exceed 30 % until 2050 and will remain negligible in the heavy duty transportation sector (<1 % in 2040) due to several drawbacks such as low energy density and limited storage possibilities [41–43]. If these 290 *EJ* were to be provided by fossil fuels, the average world temperature would increase by about 6 °C, or 4 °C above the limit of the Paris agreement reached by the UN Framework Convention on Climate Change in 2015 [44]. Models based on the 2 °C International Energy Agency Technology Perspective claim that 12, 25 and 38 % of the world's transportation energy must be provided by liquid biofuels in 2030, 2050 and 2075, respectively [42,45].

As the predominant liquid biofuel, bioethanol plays a major role as reactant for heavy duty transport fuel additives or as fuel for adapted light duty vehicles [21,46]. However, currently bioethanol is produced mainly from edible feedstocks (share >96 %) [28]. These so-called first generation biofuels not only cause a conflict between fuel supply and food/feed issues, but they may have a non-compensable carbon footprint [29]. Lignocellulosic biomass, the most abundant resource of fixed renewable carbon in the world, serves as feedstock for second generation biofuels having a much lower or even no carbon debt compared to first generation biofuels and the conflict with the feed and food industry is avoided since it is non-edible [29,30]. The production of lignocellulosic ethanol gained attraction in the context of the "bio-based economy" vision and has been in growth on an industrial scale since the early 2000s [31,32]. Policy makers aim to further incentivize the use of lignocellulose, as was done by the US government with the "Second generation biofuel producer tax credit", which expired by the end of 2021. [47] The EU set a target of a 3.5 % share of second generation biofuels in the transport sector by 2030 with an intermediate milestone of a 1 % share in 2025 in the framework of the Renewable Energy Directive II [28].

State-of-the-art lignocellulosic bioethanol production is carried out in the following process steps (Fig. 2.1a). The raw feedstock is pretreated mechanically (e.g. chipping) to reduce the particle size and physiochemically (e.g. steam pretreatment or dilute acid pretreatment) to break up the entanglement between cellulose, hemicellulose and lignin and to make the poly-sugars accessible to enzymes [30,48]. The facilitated accessibility of the cellulose fibers increases the yield and rate of hydrolysis by a factor of 3-10 [49]. The pretreated biomass is conditioned to adjust pH and temperature for enzymatic hydrolysis. A washing step to reduce the concentration of inhibitors formed during the pretreatment is not mandatory since the abilities of white rot fungi to detoxify the fermentation broth are well-known [50]. The hydrolytic enzymes are either produced in a separate aerobic fed-batch culture or purchased from an external vendor. The sugars released by enzymatic hydrolysis are fermented in a subsequent step. Finally, the solids and the major part of the water is removed in a first distillation column (beer tower) and anhydrous ethanol is obtained from rectification in a second distillation column usually followed by dehydration using molecular sieves. Lignocellulosic bioethanol is currently more expensive than ethanol from sugar crops or corn despite the cheaper raw material price per unit mass of feedstock. This is due to: [3,30,31,51]

- Lower concentration of carbohydrates in the feedstock leading to lower final ethanol concentrations
- Lower conversion rates of lignocellulosic feedstocks leading to larger vessels and with that higher capital costs
- The necessity of an elaborate pretreatment

In 2008, the hypothesis was proposed that lignocellulosic ethanol will become cheaper than ethanol produced from corn or sugar crops as a result of improved technology due to maturing of the process [3]. Improvements by integration of several process steps were identified as the strongest levers to reduce processing costs, which is not only true for biotechnology but for chemical engineering in general [52]. The highest degree of process integration for bio-ethanol production is achieved by consolidated bioprocessing (CBP), where enzymatic hydrolysis, enzyme production and fermentation are performed in a single process step (Fig. 2.1b).

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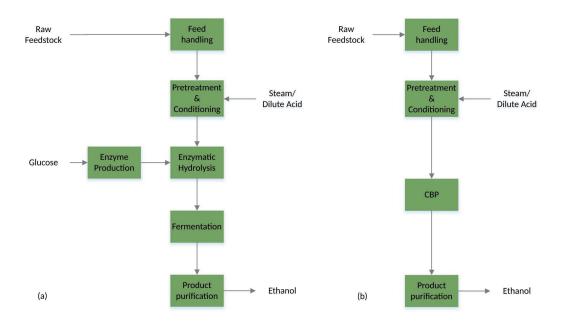


Figure 2.1: Simplified process flow diagrams for the production of lignocellulosic bioethanol employing separate hydrolysis and fermentation (a) and consolidated bioprocessing (CBP) (b). The recalcitrance of lignocellulose is overcome by a physicochemical pretreatment. After the pretreatment, pH, temperature and pressure are conditioned for enzymatic hydrolysis and CBP, respectively. In the case of conventional production, the enzymes are produced by a fungus using glucose as carbon source in a separate reactor system. During enzymatic hydrolysis, the cellulose is converted to glucose. The hydrolyzed slurry is sent to the fermentation, where the sugars are fermented to ethanol. In the case of CBP, enzyme production, hydrolysis and fermentation are carried out in the same vessel. Finally, the ethanol is recovered from the product stream by distillation and adsorption.

The enzyme production and the fermentation can be carried out simultaneously either with a single culture of a genetically modified microorganism or with a community of industrial, microbial strains [34]. A single culture strategy (hereafter termed GMO-based CBP) must employ a genetically modified microorganism, since no known natural strain is able to hydrolyze cellulosic substrates and to ferment the released sugars exclusively to the desired target product ethanol. In contrast, in a microbial community the task of hydrolysis and fermentation is divided and assigned to single strains, which are co-cultivated to act synergistically as consortium, with each community member having its own stable niche in the reactor [53,54]. Such a system, hereafter named consortium-based CBP, has been deployed by developing a suitable reactor design and co-cultivating a stable microbial community of a cellulolytic fungus and ethanolytic yeast [4]. Oxygen is fed through a membrane to the otherwise anaerobic reactor to introduce a stable oxygen gradient into the system, which provides an aerobic niche for the cellulolytic strain *T. reesei*. The fungus forms a biofilm on top of the membrane in the oxygen-enriched layer, while the fermenting strain, *S. cerevisiae*, grows suspended in the

anaerobic fermentation broth [4].

Considering a GMO-based CBP approach, cost savings of up to 41 % of the processing costs of lignocellulosic ethanol have been reported [3]. However, imposed metabolic burden, cytosolic or periplasmic space limitations, competing biochemical reactions and toxic intermediates limit the implementation possibilities of GMOs and yield poor fermentation performance. Therefore, complex tasks are distributed in nature either within subcellular compartments or between different microorganisms [53]. In a microbial community designed for synergistic division of labor, where each species has its own well-designed niche and a very specific task, complex biotransformations can be carried out in a stable and robust manner [34,55,56].

This work aims to investigate the cost savings of the consortium-based CBP approach compared to conventional bioethanol production from lignocellulose (separate hydrolysis and fermentation) and to GMO-based CBP. Furthermore, a sensitivity analysis of the profitability as a function of scale, feedstock price, yield, residence time, cost of capital and price level of the country is carried out to investigate the commercial potential of bioethanol production from lignocellulosic feedstocks via consortium-based CBP in the light of the current ethanol market situation.

#### 2.3 Materials & Methods

Base case conventional bioethanol production from lignocellulose

The most recent process design and economics of lignocellulose-to-ethanol conversion at a scale of 2,000 dry *tons* per year throughput published by the NREL was used as base case for the techno-economic analysis (hereinafter referred to as "base case") [2]. A MESP of 57 ¢/annual L ethanol results from the total processing costs and the cost of capital per year apportioned to the annual production of ethanol. All cost data of the base case refers to 2007 and the US.

Process parameters of the consortium-based CBP

Feedstock properties, ethanol titer and yield were assumed to be the same as in the base case in order to calculate the net savings by using CBP. The pretreatment was changed to a pure steam pretreatment instead of a dilute acid-catalyzed steam pretreatment used in the base case, because previous studies have successfully shown that steam-pretreated lignocellulose can be converted by consortium-based CBP and the CBP parameters are based on the available experimentally derived data with steam gun pretreatment [50,57,58]. The necessary, specific membrane surface was set to  $10 \ m^2/m^3$ . The temperature of the CBP unit was set to  $28 \ ^{\circ}$ C in favor of enzyme production to maximize the enzyme concentration, since the temperature

dependence of the activity per enzyme unit following the Arrhenius law is negligible in the temperature band where the cultivated microorganisms grow (27-32 °C) [4,59].

#### Cost estimations

Apparatus costs were either taken from the base case, from the previous NREL report of 2002 or by using well-accepted cost functions from the literature [60–63]. Any calculations, mass and energy balances as well as adapting cost values, were performed with Microsoft Excel®. Cost data for the same equipment at different scales were converted according to equation 2.1 with the help of a size exponent n taken either from the NREL base case or literature (Supplementary material A.2) [2,60–63]:

$$\left(\frac{size\ equipment_i}{size\ equipment_i}\right)^n = \frac{cost\ equipment_i}{cost\ equipment_i}$$
(2.1)

Unless otherwise stated, all equipment sizes are directly proportional to the volumetric flow. Installation factors were used to derive the installed costs, which include piping, armatures and sensors, from the equipment costs [2,60–63]. The calculation of the CAPEX proceeding from the apparatus costs was done according to the base case. The OPEX were subdivided into variable and fixed OPEX. The variable OPEX denote the costs for the consumables (mainly chemicals) and the feedstock. The costs per unit of consumable or feedstock were assumed to be the same as in the base case. The fixed OPEX consist of labor cost, maintenance, property insurance and tax. The same labor costs per worker are assumed as in the base case. All other fixed OPEX scale linearly with CAPEX and were calculated with the new CAPEX data according to the base case.

All costs are expressed either in absolute terms (US\$) or in annual costs divided by the annual ethanol production (¢/annual L ethanol). The chemical engineering plant cost index (CEPCI) was used to convert cost data from different years. Comparisons with the NREL base case were performed with a CEPCI from 2007, the reference year of the NREL base case. The sensitivity analysis is based on a CEPCI from 2019 in order to discuss the results with respect to the current situation in the ethanol market. Apart from re-dimensioning the apparatus (eq. 2.1), all cost calculations as well as the CEPCI are linear. Thus, the cost savings of each apparatus could also have been evaluated with the CEPCI of 2019. However, since single apparatus may differ strongly from the general cost trends, it was decided to retain the cost calculations for single apparatus as close as possible to the base case and convert the overall results, where single outliers are likely to be cancelled out, with the help of the CEPCI.

# 2.4 Results and discussion

Cost savings through consortium-based CBP with steam pretreatment

The process economics of ethanol production of lignocellulose reported by NREL serve as the base case to determine the saved costs by CBP (process scheme in Fig. 2.1a). [2] This section presents the cost savings of the different process steps, re-dimensioning of individual apparatus may be found in the Supplementary material A.1. The throughput of 2,000 dry tons of corn stover per day as feedstock, which are converted to 231 million L of ethanol per year was kept constant as the same yield range could be confirmed experimentally with CBP [4]. The costs for feedstock acquisition and handling were also kept constant. The pretreatment of the corn stover was changed from dilute acid-catalyzed steam pretreatment to pure steam pretreatment. This increased CAPEX, since the apparatus must withstand higher pressures necessary in a pure steam pretreatment. Variable OPEX are saved due to the substantially reduced need for chemicals (acid for the pretreatment and base for conditioning). Applying CBP through merging enzyme production, hydrolysis and fermentation in one process step saves CAPEX due to a reduced number of apparatus for hydrolysis and fermentation, as well as to the omission of the enzyme production unit. Variable OPEX are mainly saved by leaving off the use of glucose for enzyme production as the enzymes are produced in situ consuming carbon from the feedstock. The cellulose-to-ethanol yield in the CBP case was adjusted to 76 % in order to be the same as in the base [4]. Despite the fact that even small changes in yield might have considerable impact on the process economics, this adjustment was made to ensure comparability given the uncertainty of different operation modes (batch vs. continuous), substrates (corn stover vs. pure cellulose), resources for enzyme-production (insitu vs. ex-situ) and maturity levels of the technologies. The ethanol rectification, dehydration and storage do not underly appreciable changes. However, due to the considerably reduced salt concentration in the fermentation slurry as result of the changed pretreatment technique, a much larger fraction of the residues can be sent to combustion. This causes a net increase of CAPEX, since the increased CAPEX of an up-scaled combustor overcompensates the reduced CAPEX for a smaller wastewater treatment unit and the saved CAPEX because of flue gas desulfurization (FGD) may be omitted. The larger combustion unit produces a higher amount of excess electricity, which generates by-product revenues by selling it to the grid. These extra by-product revenues cause substantial OPEX savings compared to the base case.

To conclude, the CAPEX for a cellulosic ethanol production facility based on CBP increase by 4.77 % despite considerable savings by removing the enzyme production unit (A 400) completely (Fig. 2.2). The increase is mainly caused by the high apparatus costs for the larger combustor and boiler and the additional evaporators in the purification unit for the separation of process water and the solid residues after fermentation (A 500). Applying the base case

financing parameters (plant lifetime, equity share, interest rates on equity and debts, etc.), a capital recovery charge of 25.17 ¢/annual L ethanol over the lifetime of the plant instead of 24.02 ¢/annual L ethanol is obtained. The total variable OPEX per annual L ethanol for CBP amount to 13.86 ¢/annual L ethanol instead of 28.46 ¢/annual L ethanol in the base case, which corresponds to a reduction of 51.4 % (Fig. 2.2). 57.0 % of the OPEX savings result from the change in pretreatment (less use of chemicals and better valorization of the residuals due to lower salt concentrations) and 43 % come from applying CBP (omitting the need for glucose supply for enzyme production). The fixed OPEX are slightly reduced to 1.78 ¢/annual L ethanol, which corresponds to a reduction of 12.5 % (Fig. 2.2) The CAPEX-related fixed OPEX (e.g. insurance and maintenance) increase proportionally with the CAPEX, whereas labor costs are saved due the reduced number of process steps.

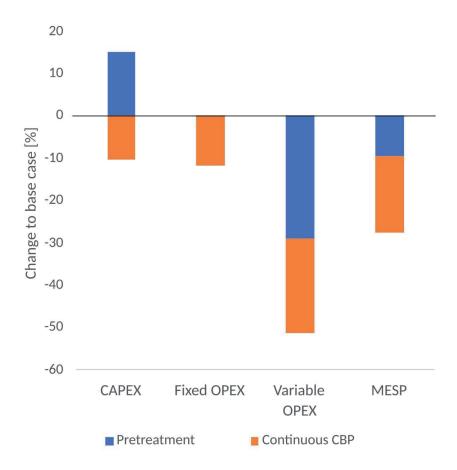


Figure 2.2: Relative cost savings of consortium-based CBP compared to the base case for CAPEX, fixed and variable OPEX and the resulting MESP. CBP leads to savings in CAPEX, fixed and variable OPEX. The change in pretreatment in- creases the CAPEX but reduces the variable OPEX. The fixed OPEX are almost not affected by the pretreatment. The resulting MESP is reduced by 27.5 % compared to the base case due to the change in pretreatment and implementation of consortium-based CBP.

The resulting minimum ethanol selling price (MESP) can be reduced from  $56.80\ e/annual\ L$  ethanol to  $41.22\ e/annual\ L$  ethanol (reduction of  $27.5\ \%$ ) (Fig. 2.3). According to CME Group (Chicago, US), one of the largest option exchange companies in the world, the average ethanol price in  $2007\ was\ 52.30\ e/L$  ethanol showing an attractive producer surplus in the case of consortium-based CBP, whereas the base case is not profitable under the given conditions [5].

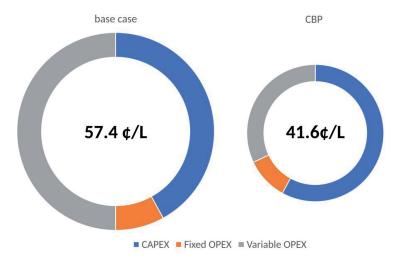


Figure 2.3: Share of CAPEX, fixed and variable OPEX of the MESP for the base case and the CBP scenario.

Sensitivity analysis of the cost savings through consortium-based CBP

In contrast to 2007, in 2019 the US MESP, including the cost savings achieved by CBP, was with  $41.60\ e/a$ nnual L ethanol higher than the average US price of ethanol, which amounted to only  $36.75\ e/L$  ethanol [5]. Despite fluctuations, the US ethanol price has decreased since 2007 on average by  $3.9\ \%$  per year, while the costs for chemical plants, represented by the CEPCI, have increased by  $16.0\ \%$  over the same period (Fig.2.4) [5].

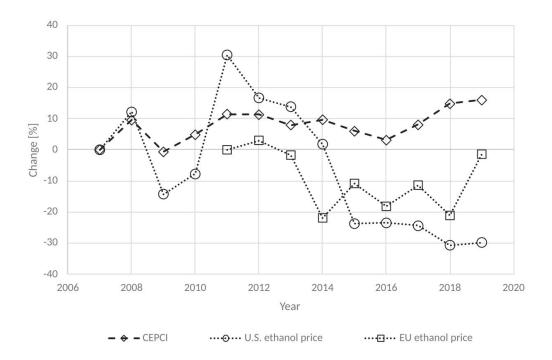


Figure 2.4: Development of the ethanol prices in the US and the EU compared to the costs for chemical plants represented by the CEPCI. From 2007 to 2019, the US ethanol price decreased by 30% [5], whereas the costs for chemical plants increased by 16%. For the EU ethanol price (domestic ethanol, FoB Rotterdam), data is available from 2011 to 2019 [6]. After a few years with lower price, the price level in 2019 stabilized around the same level as between 2011 and 2013.

CBP per se does not enable profitable bioethanol production from lignocellulose in the US nowadays. A sensitivity analysis of the MESP for several process parameters (scale, titer, yield, residence time) and investment parameters (feedstock price, price level in the country of the plant location, costs of capital) was conducted to investigate (a) necessary improvements of the process from an engineering point of view and (b) investment conditions, which allow profitable bioethanol production while still being interesting for shareholders (Fig. 2.5). In contrast to the base case, the total costs of the CBP scenario are dominated by the CAPEX (58 % vs. 42 % of MESP) as a result of the significant reduction of the variable OPEX (32 % vs. 50 % of MESP) (Fig. 2.3) by CBP. Thus, process/investment parameters affecting the CAPEX tend to be more relevant.

The MESP increases exponentially with a reduction in throughput (Fig. 2.5a), implying that the MESP is almost inelastic with varying scale above 50 and up to 120 % of the base case scale. For plants with a size below 10 % of the base case, the total costs tend to remain constant independent of the throughput. To calculate the MESP at different production scales, CAPEX and fixed OPEX were scaled with the weighted size exponent (Supplementary material A.1),

whereas the variable OPEX per L ethanol were kept constant. For scales below 10 % of the base case (i.e. <200 dry tons feedstock per day), a simple scaling with a size exponent was no longer applicable, since significant design adjustments to the process were economically favorable and/or technically necessary, such as omitting the combustion unit in order to operate the wastewater treatment at reasonable scales. A detailed listing of the design adjustments can be found in the Supplementary material A.1 and A.3. Given these calculations of the MESP at different scales, the exponential dependence is caused by the scaling of the CAPEX with the weighted size exponent. Since its overall value for the whole plant (between 10 % and 120 % of the base case scale) is 0.63 (Supplementary material A.1 and A.3), which is considerably lower than 1, strong economies of scale effects yield a high MESP sensitivity at lower scales. The economies of scale, and thus the MESP sensitivity, are further increased by synergies, such as production of process steam and electricity revenues due to lignin valorization as well as utilities, common facilities etc. working to capacity, which minimizes the specific costs at large scales. Above 50 % of the base case scale, i.e. 1,000 dry t/day, the economies of scale including all synergies seem to be fully exploited causing the low sensitivity. Below 10 % of the base case scale, economies of scale cannot be exploited further, resulting in almost constant equipment costs resulting in the tremendous increase of the MESP. The discontinuities in the curve below 10 % result from the necessary adaptation of the process layout mentioned above. Additionally, but less important, scale positively affects the variable OPEX, since the relative transport costs for the feedstock increase (Supplementary material A.1). It is not possible to match the ethanol US market price by only varying the scale of the plant.

The MESP also decreases exponentially with the obtained titer (calculations in Supplementary material A.1). The curvature is less remarkable than with throughput, but leading to high MESP sensitivities below 3 wt.% titer and almost inelastic MESP behavior above 4 wt.% (Fig. 2.5b). Thus, the calculations confirm literature stating that a minimum titer of 3-4 wt.% marks a threshold for any biofuel production process using distillation as part of the product purification [64]. The strong curvature results from the fact that distillation processes are rather inefficient from an exergetic point of view. The number of stages remains almost constant over varying titer (between 0.5 and  $10 \frac{g}{L}$ ) (cf. McCabe-Thiele diagram for ethanol water mixtures), but the reflux ratio and thus the energy demand of the rectification column strongly increases at low concentrations [65,66]. The final concentration offers no possibility of approaching the US ethanol market price.

The parameters of residence time, feedstock price, purchasing power parity (PPP) and the capital charge rate are all positively and linearly related to the MESP, while yield is negatively correlated. However, the different parameter sensitivity curves show vast differences in the constant of proportionality (Fig. 2.5c-g). The residence time has by far the lowest proportionality factor (calculations in Supplementary material A.1), causing +4/-2 % MESP by doubling/halving the residence time (Fig. 2.5d). The residence time affects only the CAPEX share of the hydrolysis and fermentation unit A 300, which is rather irrelevant due to the CBP savings.

The yield influences the MESP considerably more strongly (Fig. 2.5c): a 10 % difference in yield changes the MESP by around 5  $\phi/L$  ethanol (calculations in Supplementary material A.1). Higher yields cause a lower MESP due to lower feedstock costs since an increased yield would save a certain amount of feedstock per unit product. From a mathematical point of view, this leads to the same result as if the original feed stock amount was purchased at a lower price per feedstock unit (neglecting very minor changes to the apparatus). Since the feedstock price has a significant influence on the MESP (ca. 30 %), the yield is also relevant. However, despite its significant impact, yield improvements do not lead to profitable production in the US since the yield is already at a high level (76 %).

Feedstock price, PPP and capital charge rate have a comparable, positively correlated, linear influence on the MESP, since they cause a MESP variation width of ca. 55 c/L ethanol in the observed range (Fig. 2.5e-g). Since neither the feedstock price, nor the PPP or the capital charge rate affect the sizing of specific apparatus, no size exponent is used and the MESP sensitivity towards these parameters appears linear. The feedstock price has a direct impact on the raw materials' share of the variable OPEX. The PPP is used as an indicator to compare price levels in different countries by denoting the costs of a defined basket of representative goods in a specific country. The PPP of the US is chosen as reference and set to 100 % [66]. It only affects all costs associated with work and with variable OPEX, since a large fraction of the variable OPEX consists of locally traded raw materials such as the feedstock amongst others. The capital charge rate is the return required on invested capital. It is defined by the interest rate on debt capital and the return on equity, as well as the fraction of debt capital and equity, and thus affects the total CAPEX instead of single apparatus/units. Only variations of the PPP and the capital charge rate allow the US market price of ethanol to be met, whereas scale, yield and feedstock price only approach close to the market price. Varying titer and residence time does not allow the market price to be approached substantially.

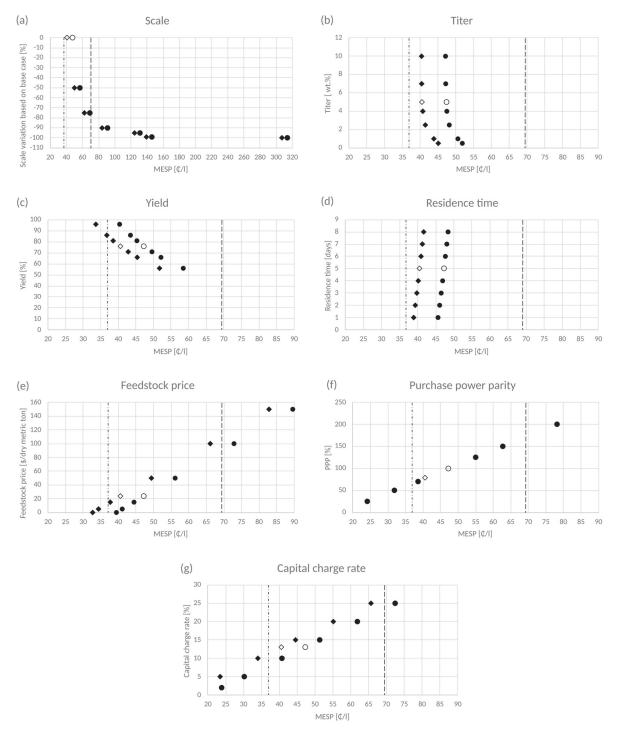


Figure 2.5: Sensitivity analysis for (a) scale [% of base case feedstock consumption], (b) titer [wt.%], (c) yield [%], (d) residence time [days], (e) feedstock costs [\$/dry metric ton], (f) purchasing power parity [% rel. to US] and (g) capital charge rate [%]. The results for the base case, including the cost savings by employing CBP, are represented by open markers in each case, whereas the filled markers denote the variation of the specific parameter. Circular markers show the US MESP and rhombic markers show the EU MESP. The dashed-dotted lines represent the average ethanol stock exchange price in the US in 2019 of 36.75 e/L [5]. The dotted line represents the 2019 EU ethanol price (T2 FOB Rotterdam) [6]. Flat curves denote a high variation of the MESP with little variation of the specific parameter and thus, a high cost sensitivity. These parameters are targeted to shift the MESP (rhombic and circular markers) to the left of the dashed-dotted and dashed line, respectively, in order to meet the market price in the respective region.

In contrast to the US, the situation in the EU appears to be much less restricted. The lower PPP in the EU (78 % of the US currency-adjusted [67]) yields an MESP reduction of  $6.75\ e/L$  ethanol (open rhombic marker in Fig. 2.5f). Furthermore, ethanol T2 (i.e. of domestic European origin) FOB Rotterdam, NL, has a market price of  $69.40\ e/L$  ethanol (dashed lines in Figure 2.5) [6]. Thus, the CBP base case is profitable in the EU (see open rhombic markers in Fig. 2.5). This allows either to decrease the size of the plant to 15 % of the base case size offering the possibility to valorize local biomass decentrally, which is important since plants with a throughput of 2000 dry *tons* feedstock per day are not feasible in Europe given the less centralized agricultural industry. Furthermore, beneficial economics give margin to imperfect process conditions or fluctuations of the feedstock price (filled rhombic markers and dashed lines in Fig. 2.5). With CBP at base case conditions, up to 30 % total return to shareholders (TRS) may be expected (Fig. 2.5f) meaning that applying CBP offers the potential to outperform the average TRS (24.0 %) of the chemical industry [68].

However, recalling that the US ethanol demand is ten times higher than that in the EU [28], it is worth showing profitable scenarios for the US with its much more competitive market environment. Under the given conditions, the only possible approaches to reduce the MESP to the US market price are (i) receiving the feedstock at negative costs (e.g. by utilizing waste feedstocks), (ii) to develop a business plan with much lower return on equity (assuming, that interest rates on debt stay constant), or (iii) production in a country with a lower price level. Considering a shift to waste feedstocks (e.g. solid manure), which could be obtained for free or at negative prices, it might be challenging to maintain the total costs and the amount of annually produced ethanol (e.g. due to abrasive wear as consequence of the high sand loading, which is not yet investigated). In case the use of corn stover as feedstock is required, price levels, which are low enough for the MESP to meet the stock exchange price, may be found in China, Ukraine, India, Indonesia and Russia among the largest corn producing countries [67, 69]. However, outsourcing second generation bioethanol production to countries with low price levels appears to be a missed opportunity both for exploiting valuable biomass potential in the US and stimulating the economy in their rural areas.

Other options for a profitable process include increasing the local ethanol price at the production site to levels above the world stock exchange price (e.g. due to tarif barriers or if regional production has a market value) or benefiting from an added-value through sustainable production. Alternatively, lower costs of capital or fiscal incentives such as CO<sub>2</sub> taxes/compensations or fuel tax exemptions for bioethanol may also enable profitable production.

Comparison of cost savings with GMO-based CBP

Another economic study using GMO-based CBP for bioethanol production [3] reports 41 % cost savings, which are considerably higher than those of 19 % coming from to the use of consortium-based CBP presented in this work. Slightly different input parameters were used

in [50] compared to the NREL base case and this scenario, i.e. costs of capital, scale, titer, yield and residence time and the pretreatment method.

In order to compare savings between GMO-based CBP and consortium-based CBP, the process conditions were levelled to base case conditions (Supplementary material A.2). By these adjustments, cost savings of around 20 % result for both variants of CBP, which can be considered identical given the uncertainty (+/- 30 %) of such early-stage cost estimations. [70] Thus, this work supports the conclusion that CBP is the strongest lever to reduce the costs of ethanol production from lignocellulose from a process point of view. [3] Cost savings in the production of cellulosic ethanol are urgently needed given the fact that several full-scale plants are currently either shut down or do not operate at full capacity because of profitability issues amongst others. [71–74]

# 2.5 Conclusion

The presented calculations have shown that hypothetically, consortium-based CBP with steam pretreatment can save up to 27.5 % of the total costs compared to conventional bioethanol production from lignocellulose, which is in the same range as published data on GMO-based CBP. However, even though CBP accounts for the strongest lever to reduce processing costs, per se it does not enable a competitive lignocellulosic ethanol production today. In the EU, the high ethanol market price combined with the low production costs when applying CBP offers a sufficient margin for profitable production or the possibility to decrease the plant size to 15 % and thus decentralize the biomass valorization. However, in the US where 56.2 % of the world's ethanol is currently consumed, the ethanol market is much more competitive. From 2007 to 2019, the ethanol price dropped by 31 % while the average CAPEX increased by 16 %, resulting in a strong competitive pressure for lignocellulosic bioethanol. A cost sensitivity analysis of several process parameters (scale, titer, yield and residence time) and investment parameters (feedstock price, price level in the country of the plant location and costs of capital) show that scale and yield are the main cost-pushers from a process point of view, whereas the price level of the plant location has the highest impact on the investment conditions. Since outsourcing second generation bioethanol production to third world countries with low price levels leaves valuable biomass potential unused and hinders economic growth in rural areas, it should be aimed at meeting the current ethanol market price by taking advantage of the cost levers of multiple process and/or investment parameters if necessary, such as utilizing cheaper waste feedstocks at comparable yields and reducing the costs of capital by accepting lower returns on equity. Alternatively, exploiting the added-value through sustainable production as well as local market disparities such as tariff barriers or tax exemptions may lead to profitable production of lignocellulosic bioethanol. In the short term, retrofitting of depreciated existing

24 2.5 Conclusion

corn ethanol plants to CBP operation, might be an interesting approach to reduce the CAPEX in order to meet the world market price of ethanol with lignocellulosic ethanol. Besides the recommendations for implementation of CBP at industrial scale, the presented model will serve as optimization criterion for under- and overspecified problems during scale-up (section 5) in order to resolve these constraints in favor of the lowest costs.

# CHAPTER 3

Continuous operation of a membrane aerated biofilm reactor for consortium-based consolidated bioprocessing of cellulose to ethanol

# 3.1 Abstract

A robust design for the conduction of continuous consolidated bioprocessing is of central importance: First, the techno-economic assessment demonstrated the considerable cost savings when CBP is operated continuously. Second, continuous steady-state operation is time-invariant and thus, allows to fit and validate a rigorous process model, the centerpiece of successful scaleup, without the need to account for growth dynamics. Steady-state operation was achieved multiple times with a maximum titer of  $3.26\pm0.01~\frac{g}{L}$  and a productivity of  $0.025~\frac{g}{L*h}$ . It was proven, that *T. reesei* produces constantly enzymes over 750 h. The experiments showed that the oxygen flux per membrane area is a critical parameter for the process. Setups with identical volumetric oxygen transfer rate  $k_L$ a, but different oxygen fluxes per membrane area (large area & low concentration gradient vs. small area and high concentration gradient) showed titer differences of ca. 80 % (1.83  $\frac{g}{I}$  vs 3.26  $\frac{g}{I}$ ) in favor of setups with the large membrane surface. The difference was attributed to long diffusion paths in thicker biofilms and thus, shortage in nutrient supply. Furthermore, it was proven that the continuous co-cultivation of two competitors, T. reesei & Aspergillus phoenicis, is possible, if the process conditions are adjusted to identical growth rate. The adding of A. phoenicis targeted the better utilization of the inhibiting intermediate cellobiose by balancing the fungal enzyme cocktail in terms of higher  $\beta$ -G concentrations. This goal was achieved, but however did not result in higher yields or productivities.

26 3.2 Introduction

#### 3.2 Introduction

Independent of the branch, continuous process operation offers various advantages such as omission of downtime for batch emptying and refilling, reduced CAPEX since the same productivity is maintained at lower reactor volume, the possibility to integrate continuous heating and cooling demands into an efficient heat management system and facilitated control due to time-invariance in steady-state operation. [75–77] In terms of bioprocesses, the reduced energy/chemicals demand for less frequent sterilization compared to batch processes as well as avoiding low productivities due to substrate and product inhibition at the beginning and the end of a batch process, respectively, are additional advantages. [78,79]

However, the interest in implementing of continuous bioprocesses compared to other process is rather new and successful industrial applications are rare. [80] The main obstacles of continuous operation are the handling of the solids for constant feeding, low productivities and maintaining long-term sterility. [75] Furthermore, in case of detecting a contamination, the contaminated batch can simply be disposed, whereas withdrawing the minimum, but sufficiently large amount of fermentation slurry in a continuous process is much more difficult. [81] Nevertheless, CBP and continuous processing were identified as most promising concepts to achieve economic competitiveness of bioproducts with fossil based products [3,82], which was confirmed for consortium-based consolidated bioprocess of lignocellulose to ethanol in the previous chapter. [33] Besides economics, consortium-based CBP predestined to overcome obstacles of continuous processing because the biofilm immobilizes cells and important extracellular products such as enzymes and surface-attached microbes are reported to show higher activity. [35] Two reactor concepts are available for continuous operation: The continuously stirred tank reactor (CSTR) and the plug flow reactor (PFR). [83] Bioprocesses are usually conducted in a CSTR since the viscous fermentation broth must be stirred. A CSTR is a well-mixed vessel with an inlet and an outlet. The concentration of the bulk is equal to the concentration of the outflow and the residence time (also referred to as hydraulic retention time) is defined as follows (eq. 3.1)

$$\tau = \frac{V_{CSTR}}{\dot{V}} \tag{3.1}$$

$$\tau^{-1} = D \tag{3.2}$$

The dilution rate D, the inverse of the residence time (eq. 3.2), is important for bioprocesses. If D is larger than the cell proliferation rate in the bulk, the reactor is washed-out. [84] The problem of wash-out is not relevant for immobilized biomass in the consortium-based CBP in contrast to industrial bioprocesses, where cell-recycling is mandataroy to keep the cell concentrations at a sufficient level. During industrial ethanol production from  $1^{st}$  generation biofuels, the yeast cells are regained by centrifugation and afterwards washed with sulfuric acid

to reduce bacterial contamination. [36] Considering the production of  $2^{nd}$  generation biofuels, where the solid fraction of the reactor outflow consists of yeast cells and undigested lignin, a more sophisticated process is necessary to recycle only the yeast cells without the lignin particles. Besides the economic aspects of this process, the possible number of yeasts, which could be cultivated is reduced to the ones resistant to the chemical and mechanical stresses introduced by these kinds of recycling processes. [36] In contrast, the extracellular matrix of a biofilm protects the cells from inhibiting chemicals of the bulk allowing for a wider range of possible yeast cultivations. [37] However, the secreted enzymes diffuse from the biofilm into the bulk because they are only partly immobilized by attachment to the cell walls. Therefore, the yields will be poor, if the dilution rate is not adjusted accordingly to the microbial activity in the system with a special focus on the total enzyme activity. During steady-state, the fungal growth in the biofilm is equal to the decay rate, which is very low  $(\mu_{\text{max}}/k_{\text{decay}} \approx 20 \text{ for } T.$  reesei [10]).

$$\mu \cdot [X]_p = k_{\text{decay}} \cdot [X]_s + [X]_p \cdot D \tag{3.3}$$

In a suspended culture, the mass balance additionally contains a wash-out term (eq. 3.3), which shifts the equilibrium towards higher concentrations of primary mycelia. In an immobilized biofilm, there is no wash-out (D=0) and the mass balance demands high concentrations of the enzyme producing secondary mycelia to "compensate" for the low decay rate. This explains the relatively high amount of enzymes within the system given the low concentration of microbial biomass compared to suspended cultures. In contrast, very low enzyme concentrations will be predicted by every model, which relates enzyme production to primary metabolism and thus, proportionally to the concentration of primary mycelia  $[X]_p$ . [85,86]

This work aims to prove that continuous consolidated bioprocessing based on a microbial consortium in a membrane aerated biomass immobilizing biofilm reactor is possible and results in good yields because enzyme production is not directly related to primary metabolism and the immobilization of the biomass and the cell-attached enzymes will lead to high enzyme activities per *g* biomass in the system. [10,87] Besides the proof-of-concept, which is important for the process economics (section 2), the time-invariant results of a parameter analysis with continuous experiments are intended to fit and validate a process model, which was developed to describe the process from an engineering point of view (chapter 4).

#### 3.3 Materials & Methods

Fungal strains & culturing models

T. reesei RUT C30 (ATCC 56765) was purchased from VTT, Finland. Spore-populated agar pieces of 15 mm<sup>2</sup> size, obtained from a five-day-long cultivated agar plate (recipe adapted

from NREL protocol [88]: 20  $\frac{g}{L}$  agar and 22  $\frac{g}{L}$  D-glucose · H<sub>2</sub>O in Mandel's medium) at 28 °C, were preserved in a 20 %(v/v) glycerol solution and stored at -80 °C as kryostocks. Mandel's medium consists of 2  $\frac{g}{L}$  KH<sub>2</sub>PO<sub>4</sub>, 1.4  $\frac{g}{L}$  (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub>, 0.3  $\frac{g}{L}$  MgSO<sub>4</sub> · 7H<sub>2</sub>O, 0.4  $\frac{g}{L}$  CaCl<sub>2</sub> · 6H<sub>2</sub>O, 0.3  $\frac{g}{L}$  urea, 0.75  $\frac{g}{L}$  peptone, 0.25  $\frac{g}{L}$  yeast extract, 5  $\frac{mg}{L}$  FeSO<sub>4</sub> · 7H<sub>2</sub>O, 1.6  $\frac{mg}{L}$  MnSO<sub>4</sub> · H<sub>2</sub>O, 1.4  $\frac{mg}{L}$  ZnSO<sub>4</sub> · 7H<sub>2</sub>O, 3.7  $\frac{g}{L}$  CoCl<sub>2</sub> · 6H<sub>2</sub>O, 10  $\frac{\mu L}{L}$  concentrated hydrochloric acid. The metallic salts and the hydrochloric acid were sterile filtered (pore size 0.2  $\mu$ m). MgSO<sub>4</sub> · 7H<sub>2</sub>O, CaCl<sub>2</sub> · 6H<sub>2</sub>O and the rest were autoclaved separately to avoid precipitation. Precultures of *T. reesei* consisting of Mandel's medium with 7.5  $\frac{g}{L}$  cellulose (Avicel PH-101, Merck KGaA, Darmstadt, Germany) were inoculated with 1.5 mL kryostock solution and incubated in a shaking incubator (Minitron, Infors-HT, Bottmingen, Switzerland) at 28 °C with 150 rpm. All chemicals were purchased either from Merck KGaA, Darmstadt, Germany, or from VWR International, Dietikon, Switzerland

Aspergillus phoenicis (VTT D-76019) was purchased from VTT, Finland. The preparation of kyrostocks and precultures was conducted analog to *T. reesei*.

Saccharomyces cerevisiae VTT C-79095 was purchased from VTT, Finland. Kryostocks were prepared by mixing cultures with an optical density of 0.5 at a wavelength of 600 nm (OD600) measured by spectrophotometry (Thermo Spectronic UV-1 (Thermo Fisher Scientific, Waltham, United States of America)) with glycerol to obtain a 20 % (v/v) glycerol solution. Precultures of *S. cerevisiae* consisting of YPD-medium were inoculated with a 1.5 mL kryostock and incubated in a shaking incubator (Minitron, Infors-HT, Bottmingen, Switzerland) at 28 °C with 150 rpm. YPD medium consists of 20  $\frac{g}{L}$  peptone, 10  $\frac{g}{L}$  yeast extract and 11  $\frac{g}{L}$  d-glucose · H2O. All chemicals were purchased either from Merck KGaA, Darmstadt, Germany, or from VWR International, Dietikon, Switzerland.

#### Experiments in Erlenmeyer flasks

**Ethanol degradation:** 50 mL Erlenmeyer flasks were sterilized and prepared with 30 ml of 5  $\frac{g}{L}$  ethanol in Mandel's medium. A triplicate was prepared without cellulose and another triplicate was prepared with the same way with additional 4.5  $\frac{g}{L}$  cellulose. The flasks were inoculated with 1.5 ml T. reesei preculture. The experiment was carried out at 28 °C in a shaking incubator with 150 rpm. Ethanol was measured by means of HPLC. Ethanol loss by evaporation was determined by a blank triplicate (only ethanol in Mandel's medium) and the results were calibrated accordingly.

**Growth rate comparison:** 50 mL Erlenmeyer flasks were sterilized and prepared with 30 ml of 7.5  $\frac{g}{L}$  cellulose in Mandel's medium. The flasks were inoculated with 1.5 ml T. reesei or A. phoenicis, respectively. The experiment was carried out in a shaking incubator with 150 rpm. The temperature was set to 27 °C or 28 °C, respectively, and at a pH=4 or pH=5. The pH was

adjusted by adding citrate buffer. For each experimental condition, one Erlenmeyer flask was harvested after 1, 3 and 5 days to determine the amount of cell mass with the glucosamine assay.

Experiments in the membrane aerated biofilm reactor

The membrane aerated biofilm reactor is based on a Labfors 5 bioreactors (Infors HT, Bottmingen, Switzerland) with 3 L nominal volume and 2.7 L working volume. The reactor is stirred with a helical ribbon impeller and a tubular polydimethylsiloxane (PDMS) membrane with 3.18 mm outer diameter and 1.58 mm inner diameter (Dow Corning, Midland, United States of America) is winded within the reactor. The standard length of the membrane was defined to 2.8 m. 1/2 standard length corresponds to 1.4 m, accordingly. The pH of 5 was controlled by 4 N phosphoric acid and 4 M sodium hydroxide and measured by an EasyFerm Plus PHI Arc probe (Hamilton, Bonaduz, Switzerland). The temperature was set to 28 °C and 27 °C, respectively, for the co-cultivation of A. phoenicis and T. reesei. The membrane was flushed at a volumetric flow rate of 0.368  $\frac{L}{min}$  with a 21 % and 42 % oxygen-nitrogen mixture, respectively. After each pass, the oxygen concentration was measured optically (EOM-tO2-mini-180-T4D-v3 electrooptical module for oxygen measurements, Presens, Regensburg, Germany) in an expansion bag and the amount of diffused oxygen was injected into the expansion bag (PID-controlled electromagnetic valve (type 0255, Bürkert, Ingelfingen, Germany)). Trace oxygen in the bulk phase was detected by means of measuring the redox-potential with an EasyFerm Plus ORP Arc probe (Hamilton, Bonaduz, Switzerland). The sampling line for sampling the bulk phase was exposed to a UV barrier to prevent contaminations. [89] The membrane reactors, the feed bottle and the collecting vessel were sterilized by autoclaving for 20 minutes at 121 °C. Any connecting lines within the reactor cascade were closed during sterilization and connected afterwards in a laminar flow cabinet under aseptic conditions. Mandel's medium was added after autoclaving and the reactors were inoculated with 5 % (v/v) fungal inoculum (either 5 % (v/v) T. reesei or 2.5 % (v/v) T. reesei and A. phoenicis each. Additional 5 % (v/v) yeast inoculum at was added after 48 h to reach OD600= 0.5 for the membrane reactor. For batch experiments, the yeast inoculate was centrifuged (3600 rpm at 4 °C for 30 min) and washed with Mandel's medium to exclude the impact of the preculture metabolites on the batch experiment. For continuous experiments, the feed solution was prepared analog to the reactor preparation. All technical gases were purchased from Pangas, Dagmarsellen, Switzerland.

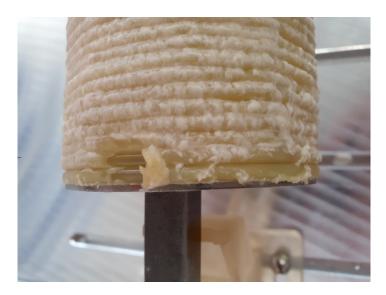


Figure 3.1: Close-up photograph of the biofilm on a helically winded membrane on its support. The white layer on the top is the yeast biofilm layer and the yellowish layer is the biofilm formed by *T. reesei*. The membrane is visible, where the biofilm was scraped away manually after the experiments.

#### Feeding device and pneumatic transport for continuous experiments

Avicel was sterilized and premixed with the sterile nutrients in a feed bottle (Volume 5 L, Schott Duran) with an impeller at 400 rpm. The nitrogen flow into the T-junction (Swagelok,  $\frac{1}{32}''$  inlet for nitrogen) to create the nitrogen bubbles was controlled by a mass flow controller (Vögtlin red-y series, 0-25  $\frac{NmL}{min}$ ) at 15  $\frac{NmL}{min}$ . The peristaltic pump (Watson Marlow 323d) was controlled at 15 % power to transfer the liquid-solid suspension from the feed bottle to the T-junction ( $\frac{1}{8}''$  inlet and outlet for the solid-liquid suspension) and subsequently the segmented flow through a  $\frac{1}{8}''$  pipe and peristaltic pump tubing (Tygon LMT-55, inner diameter 3.2 mm and outer diameter 6.4 mm) to the 1 $^{st}$  reactor. The segmented flow was fed every 38 min for 60 s. Before and after each feeding, the T-junction was emptied by nitrogen flow for 30 s without pumping. Pneumatic transport from the 1 $^{st}$  to the 2 $^{nd}$  reactor to the collecting vessel through pipes and tubes with inner diameter of 5 mm was conducted every 38 min ca. 20 min after the feeding procedure for 90 s with nitrogen flushing (pressure of 1.6 bar).

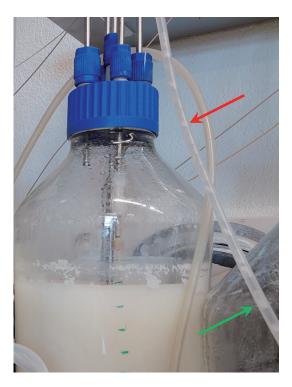


Figure 3.2: Photograph of the segmented flow from the feed bottle (background) to the 1<sup>st</sup> reactor. The green arrow exemplary shows a a droplet with the solid-liquid suspension and the red arrow points out the settling limitation of Avicel at the phase boundary between droplet and nitrogen bubble

#### Glucosamine assay

The glucosamine assay was conducted exactly according to [87]. By diluting the samples with distilled  $H_2O$  and a total volume of  $0.3\ mL$  for the assay, the measurements were in the linear range of the glucosamine calibration curve.  $0.3\ mL$  HCl (4 M) was added to hydrolyze the fungal biomass and the samples were captured in Pyrex screw capped tubes. After adding the HCl, nitrogen was used to flush the samples. The hydrolization of the samples took  $2\ h$  at 121 °C. After cooling down, a neutralization step with  $0.4\ mL\ 2\ M\ Na_2CO_3$  performed. In the meantime,  $\%\ v/v$  acetyl acetone in  $1.5\ M\ Na_2CO_3$  were prepared and  $0.5\ mL$  were added to the samples. With a boiling water bath, the samples were heated for  $20\ min$  followed by the addition of  $1\ mL$  ethanol. Determining the glucosamine content with the color formation at  $530\ nm$ ,  $0.5\ mL$  of the Ehrlich's reagent [2g p-dimethylaminobenzaldehyde in  $30\ mL$  EtOH and  $30\ mL$  concentrated HCl ( $3\ \%\ w/w$ )] were added. By using GlcN as a calibration curve, the linear range of the measurements were conducted. The cell dry weight (CDW) for each fungus, which were grown on glucose combined with their GlcN content correlated with the different calibration curves. [87]

#### Analytical methods

Cellobiose, glucose and ethanol concentrations were measured by HPLC (Waters 2695 Separation Module, Waters Corporation, Milford, United States of America). Separation was achieved in an Aminex HPX-87H column (Bio-Rad, Hercules, United States of America) at 65 °C with 5 mM H2SO4 solution as mobile phase at a flow rate of 0.6  $\frac{mL}{min}$ . The substances were detected by a refractive index detector (Waters 410) at 40 °C and a photodiode array detector (Waters 2998).

# 3.4 Results and Discussion

### 3.4.1 Continuous CBP with a consortium consisting of T. reesei and S. cerevisiae

Li et al. proposed 7 key challenges when operating a system continuously [79]: Continuous feeding, continuous product removal, prevention of contamination, immobilization of cells, immobilization of extracellular products, long-term stability and high cell density, titer, yield & productivity. In the following, it is presented, how each of these 7 points was addressed in order to successfully conduct continuous experiments of consolidated bioprocessing of cellulose to ethanol at lab scale.

#### Continuous feeding

Continuous feeding is indeed a key challenge since cellulosic substrates are insoluble, but homogeneous feeding is unequivocal for reaching steady state operation given the sensitivity of the microbial community to fluctuations of external parameters like the substrate concentration. [7, 8] A published 3-phase-flow feeding design was adapted to feed the reactor cascade continuously from a feed bottle (Fig. 3.3). [8] The solid-liquid suspension is sucked into a T-junction by a peristaltic pump, where it is segmented into droplets by injecting nitrogen via the perpendicular nozzle of the T-junction. The surface tension between the gas bubbles and the suspension droplets prevents the cellulose from sedimentation. The feed flow rate is adjusted by the nitrogen gas flow rate and the rotational speed of the peristaltic pump.

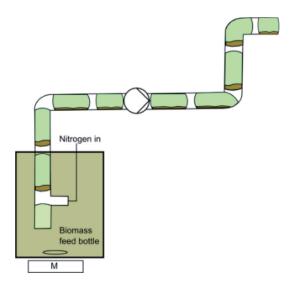


Figure 3.3: The 3-phase flow feed design for continuous feeding of suspensions with insoluble substrates. The well mixed solid-liquid suspension is sucked into the feeding device, a T-junction, by a peristaltic pump. Additionally, nitrogen is injected via the perpendicular nozzle of the T-junction. Consequently, a 3-phase flow with solid-liquid suspension droplets and intermitting gas bubbles is formed. Sedimentation of the solid particles ends at the phase boundary to the gas bubbles since the gravitational force is outweighed by the surface tension between the droplet and the bubble. Figure taken from [7].

Adjusting the residence time to 5 *days* like it was done for the industrial scale layout yields feeding rate of 22.5  $\frac{mL}{h}$  at lab scale. [33] The peristaltic pump works periodically since this flow rate is too low for steady feeding. Due to the periodically feeding & emptying, the reactor system may be regarded as a batch system between two feeding intervals. Eq. 3.4 compares the duration of such a batch period to the duration of the whole experiment (eq. 3.4).

$$\frac{t_{\text{batch}}}{t_{\text{Experiment}}} = \begin{cases}
1 & \text{for batch operation} \\
0.25 - 0.056 & \text{for repeated fed batch operation} \\
0.0056 & \text{for this work} \\
0 & \text{for continuous operation}
\end{cases} (3.4)$$

The spectrum of  $\frac{t_{\text{batch}}}{t_{\text{Experiment}}}$  ranges from 0 (permanent feeding during continuous operation) to 1 (only initial feeding for batch operation). The value for repeated batch usually ranges between 0.25 and 0.1. [90] However, the minimum was found at 0.056. [91] This work still has a 10 times higher feeding frequency than the maximum frequency found for repeated batch operation. Thus, the feeding may be assumed to be continuous, which is confirmed by the experimental results presented later on.

Continuous product removal

Continuous product removal is either achieved by direct product removal (in-situ or slip stream) or by removal of the fermentation broth with subsequent separation. [64] The latter is done in this work. The fermentation broth was transported pneumatically from the  $1^{st}$  reactor in the cascade to the  $2^{nd}$  reactor and finally to the collecting vessel (blue line in Fig. 3.4). [8] After each feeding interval, a valve opened to inject nitrogen in the gas phase below the reactor lid. The exhaust port of the reactor was a dip tube, which height was precisely adjusted to the filling level of the desired reactor volume. Thus, the overpressure of the gas phase pushed the well-mixed solid-liquid suspension from the CSTR through the tube to the  $2^{nd}$  reactor in the cascade or the collecting vessel. The nitrogen is vented through a sterile filter at the top of the collecting vessel to release the overpressure. As soon as the desired filling level in both reactors is reached, the opening of the dip tube is above the liquid level and the nitrogen flows directly through the dip tubes to the collecting vessel and is vented.

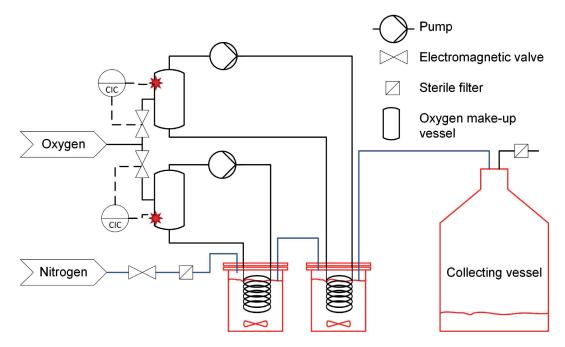


Figure 3.4: Schematic representation of the oxygen recirculation system for membrane aeration (black lines) and the pneumatic transport of the fermentation slurry by nitrogen injection (blue lines). Oxygen is pumped through the membrane, where a certain amount of oxygen is lost due to diffusion across the membrane wall. The oxygen concentration in the make-up vessel is measured optically and an electromagnetic valve is opened to add pure oxygen to make up for the loss by diffusion. After each feeding interval, an electromagnetic valve is opened to inject nitrogen in the gas phase above the liquid level of the 1<sup>st</sup> reactor. The fermentation broth is pneumatically pushed through a dip tube and flows into the second reactor and from the second reactor into the collecting vessel, where the nitrogen is vented via a sterile filter. As soon as the filling level of each reactor reaches the desired state, the dip tubes do not reach into the liquid phase anymore. The remaining nitrogen is directly transported through the dip tubes to the vent. Figure adapted from [8].

As there is no phase boundary to avoid settling during the pneumatic transport, the prevention of inhomogeneities has to be ensured otherwise: The maximum sedimentation velocity of cellulose particles is given by Stoke's law (assuming perfectly spherical cellulose particles settling in pure water) (eq. 3.5) [92]:

$$m_p g = 6\pi \eta_w r_p v_p \Leftrightarrow v_p = \frac{m_p g}{6\pi \eta_w r_p v_p} \approx 8.2 \frac{mm}{s}$$
(3.5)

According to Stoke's law, the driving force for sedimentation, the gravitational force  $m_p g$ , is equal to the fluid resistance force, which is defined by its viscosity  $\eta_w$ , the particle's diameter  $r_p$  and velocity  $v_p$ . [92] The fluid velocity during pneumatic transport is ca. 0.25 m/s as experiments have shown. Thus, sedimentation is not an issue during steady pneumatic flow because the mean fluid velocity is larger than the sedimentation velocity at least by a factor of 30. It can be concluded that settling of the cellulose particles is not an issue during steadypneumatic transport. However, there are ca. 900 start-ups of pneumatic transport during one experiment. Therefore, concentration distortions during start-up of the pneumatic transport could add up to considerable errors. The risk of concentration distortions during start-up is assessed by evaluating the control responses to pneumatic transport in a qualitative manner (Fig. 3.5). Pneumatic transport of the solid-liquid suspension is initialized by the control command to open the electromagnetic valve for nitrogen flushing at a certain point in time  $t_0$ . Since the opening of the valve is only damped by the inertia of the moving parts, which is negligible, its control response is a step function (step from off to on at  $t_0$  in Fig. 3.5). A step function describes a static control response. The response comes without any delay and the gradient between actual state and target state is equal to infinity. [93] Both, the overpressure and the superficial flow velocity are damped by a pressure loss due the sterile filter and the long dip tube. In both cases, the damping force is in the range of 5-10 % of the driving force. Thus, the control responses of the overpressure and the fluid velocity to reach their steady values are rather fast but show dynamic behavior. Dynamic behavior is characterized by the deviation to a step response: There is a delay time  $t_d$  until the response starts and the response gradient is smaller than infinity  $\frac{d\Delta P}{dt} < \infty$ . [93] As the settling of cellulose particles is damped by the fluid viscosity resulting in a damping force in the range of 100 % of the driving force, the dynamic response of the settling velocity is much slower than for the pneumatic transport (Fig. 3.5). Thus, there is no cellulose sedimentation during start-up as well as during steady pneumatic transport and continuous product removal is ensured.

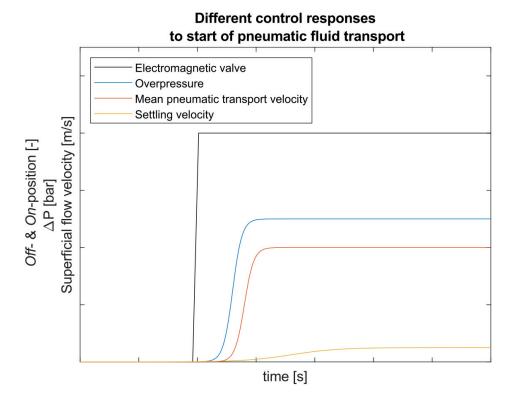


Figure 3.5: Qualitative comparison of estimated different control responses of the critical parameters after initializing nitrogen flushing for pneumatic fluid transport.

# Prevention of contamination

Li et al. discussed the prevention of contaminations in the light of open and continuous processes. [78] Open means that no sterilization procedure is conducted. This is impossible for the setup in this work, although it is known that T. reesei and other filamentous fungi secrete antimicrobial substances to protect their niche against bacteria and other invaders. [94] However, it was shown that amongst others, the ubiquitously present *Lactobacillus pentosus* is able to grow at high rates in the presence of T. reesei. [50,95] Thus, any kind of contamination needs to be prevented by sterilizations procedures. During the preparation of the experiments, all reactors, the feed bottle and the collecting vessel were autoclaved. Every gas injection into the system passes a  $0.2~\mu m$  sterile filter and the sampling line has a UV barrier to allow sampling without any contamination. [89] All actions, which involved opening the closed system of the two reactors, the feed bottle and the collecting vessel, such as inoculation of the reactors, refilling the feed bottle and emptying the collecting vessel, were performed under aseptic conditions in a laminar flow cabinet.

#### Immobilization of cells and extracellular products

The immobilization of cells is automatically given by the concept of deploying a biofilm. [4,35] The enzyme producer *T. reesei* is completely immobilized as biofilm on the membrane because there is no other oxygen source within the system. The enzymes produced by *T. reesei* are partly bound in the biofilm and partly released to the bulk. The ratio of immobilized enzymes to free enzymes is defined by the mass transfer equilibrium (Chapter 4) and the affinity of the enzyme to attach to the fungal cell wall. [87] *S. cerevisiae* also is present in both, the biofilm and the bulk phase. The yeast cells in the bulk phase convert the largest fraction of the released glucose to ethanol, whereas the yeast cells in the biofilm face higher oxygen concentrations and lower glucose concentrations, which allows them to overcome the Crabtree effect and perform aerobic metabolism, which is much more favorable in terms of cell proliferation rate. [96,97] Concluding it can be stated that all cells and extracellular products are either immobilized or the process is designed to prevent wash-out during continuous operation by keeping the dilution rate below the corresponding production/proliferation rates.

#### Long-term stability

Long-term stability is crucial in continuous systems as the start-up procedure to reach steady-state operation already takes 3-5 residence times. [83] In this work, it is accounted for the long-term stability in terms of material choice and the biological system. All used materials (especially the non-metal parts such as the membrane and the tubes for the peristaltic pumps) were known to withstand the wear for a sufficiently long-time. The biological system consists of 2 industrial strains, *T. reesei* RUT C30 and *S. cerevisiae* VTT C-79095 known for their robustness. [34] In contrast to CBP with genetically modified microorganisms (GMOs), where each cell proliferation comprises the risk of a back mutation, which were implemented. [34] Additionally to the robustness of the chosen microorganisms themselves, the consortium formed by these two microorganisms is stable too. The membrane aeration gives a stable aerobic niche, and the yeast relies on the cellulolytic activity of *T. reesei*. [35] Thus, according to the cheater-cooperator model, there is an equilibrium to what extent *S. cerevisae* will invade the niche of *T. reesei*. [34,35]

#### High cell density, titer, yield & productivity

The setup of the presented work is reported to reach a titer of 7  $\frac{g}{L}$  ethanol, a yield of 70 % and a productivity of 0.04  $\frac{g}{L*h}$ , which above-average numbers for CBP. [35,98] However, only the yield meets industrial requirements. The titer should be around 40  $\frac{g}{L}$  and the productivity around 0.3  $\frac{g}{L*h}$ . [2,64,98] In order to increase the titer and the productivity, the following adjustments were proposed: Higher solid loading, elimination of ethanol losses through the membrane and better utilization of cellobiose.

As the yield meets industrial specifications, the necessary titer could be obtained by simply

increasing the input solid loading assuming constant productivity. For batch operation, an increased solid loading would cause problems such as increased substrate inhibition and poor mixing behavior of the highly viscous fermentation broth, during the initial batch phase. [15,99] However, in a CSTR, the bulk composition is equal to the outflow composition. [83] Thus, high solid loadings would be diluted in the partly hydrolyzed bulk phase and substrate inhibition as well as mixing problems can be avoided. Ethanol losses through the membrane were avoided by recirculating the gas in the membrane (Fig. 3.4). Since ethanol is a volatile component, a certain amount of ethanol diffuses through the biofilm and the membrane wall into the membrane. With an open end approach (the residual gas is released to the atmosphere after passing the membrane), any ethanol in the membrane would be lost to the atmosphere. [35] In this work, the gas in the membrane is recirculated. After each pass of the membrane, the gas enters a make-up vessel, where the oxygen concentration is measured and any lost oxygen by diffusion through the membrane is replaced (Fig. 3.4). During start-up, ethanol is concentrated within the recirculation loop until an equilibrium concentration is reached and the ethanol diffusion into the biofilm is reduced to the amount of ethanol, which is degraded within the biofilm (Fig. 3.6).

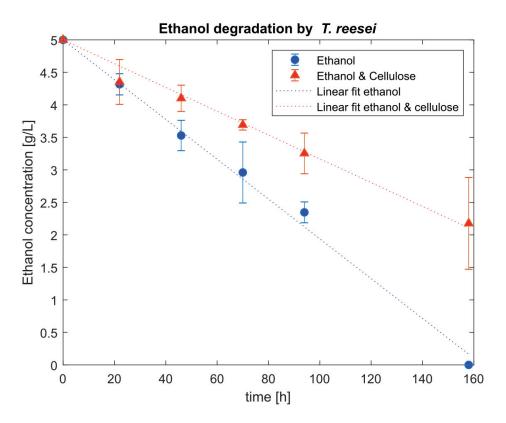


Figure 3.6: Ethanol degradation of *T. reesei* in an Erlenmeyer flask with ethanol as only substrate and ethanol together with cellulose as substrate at 28 °C. The dotted lines represent the linear fit with average degradation rates of  $0.0306 \frac{g}{L*h}$  and  $0.01183 \frac{g}{L*h}$  with ethanol as only substrate present and with ethanol and cellulose as substrate, respectively. The coefficients of determination are 0.9943 and 0.9922, respectively. The error bars are based on triplicate experiments.

Given the above-mentioned setup, steady-state could be achieved with the continuous cocultivation of only *T. reesei* and *S. cerevisiae* showing a yield of 40.3 %, a titer of  $3.258\pm0.007$   $\frac{g}{L}$  and a productivity of 0.025  $\frac{g}{L*h}$  (Fig. 3.7). The steady-state state was reached at around 560 h of operation, which corresponds to the rule of thumb, that a steady-state takes ca. 4-5  $\tau$  ( $\tau$ =130 h).

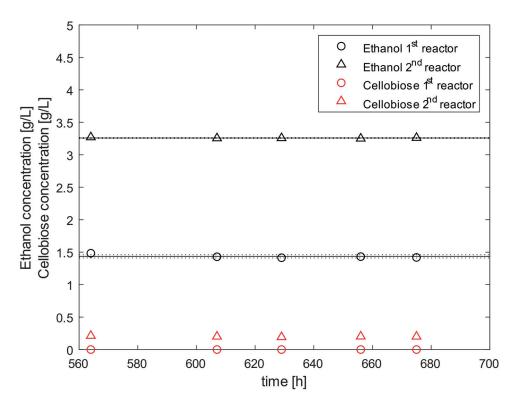


Figure 3.7: Steady-state results for continuous consolidated bioprocessing based on a microbial consortium consisting of T. reesei with S. cerevisiae in a cascade of 2 reactors. Steady-state operation was reached after 564 h. Cellobiose was depleted in the  $1^{st}$  reactor and only present to a little extent in the  $2^{nd}$  reactor (ca.  $0.2 \frac{g}{L}$ ). The solid and dashed lines denote the average ethanol concentration and its standard deviation, respectively, in the  $1^{st}$  and second reactor. Steady-state operation was maintained over 111 h. The membrane (inner diameter  $d_i = 1.58 \ mm$ , outer diameter  $d_o = 3.18 \ mm$ , length L=  $5.6 \ m$  was aerated with 21 % oxygen fraction. The cellulose feed concentration was  $17.5 \ \frac{g}{L}$  and the residence time  $\tau$  was  $130 \ h$ .

In order to investigate the influence of the oxygen transfer rate to the system, the experiment was repeated at different membrane lengths and oxygen concentrations (Fig. 3.8).

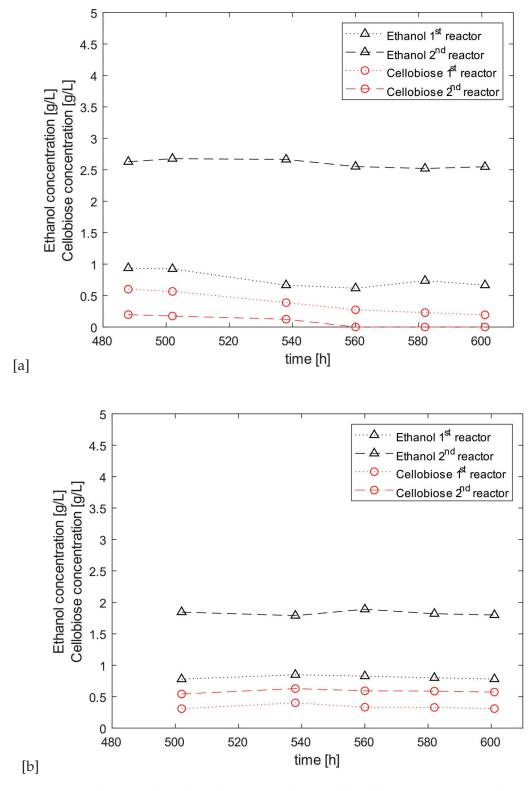


Figure 3.8: Steady-state ethanol production with consolidated bioprocessing based on a microbial consortium consisting of *T. reesei* and *S. cerevisiae* in a cascade of 2 reactors. The membrane (inner diameter  $d_i$ = 1.58 mm, outer diameter  $d_o$ = 3.18 mm, length L= 5.6 m (a) and L= 2.8 m (b), respectively, was aerated with 42 % oxygen fraction. The cellulose feed concentration was 17.5  $\frac{g}{L}$  and the residence time  $\tau$  was 130 h.

Doubling the oxygen concentration gradient across the membrane and halving the membrane length yields the same oxygen mass transfer into the system as the original setup (Fig. 3.7 & Fig. 3.8b). However, the ethanol titer is considerably lower (1.83  $\frac{g}{L}$  vs 3.26  $\frac{g}{L}$ ). Hence, there is a difference whether the same amount of oxygen is transferred across small surfaces or large surfaces, which also means that the volumetric mass transfer coefficient  $k_L a$  is not a sufficient parameter to describe the system. A more rigorous model is necessary to account for the influence of oxygen transfer per area. Considering the higher cellobiose amounts in Fig. 3.8b compared to 3.7, one reason for the lower productivity of the system could be the following: The higher oxygen input per area allows more biofilm formation per area and thus, a thicker biofilm. This has two implications: The diffusion path for glucose from the bulk to the fungus is longer on average. Additionally, the average diffusion path of the enzymes, especially for  $\beta$ -G, which is known to likely adhere to the fungal cell surface [87], increases. Thus, the inner biofilm layers lack in glucose supply due to inhibited glucose formation in the bulk as consequence of less available  $\beta$ -G and longer diffusion paths of the formed glucose through the biofilm. T. reesei was found out to consume ethanol at considerable rates if no other substrate is present (Fig. 3.6). Thus, besides cellobiose inhibited hydrolysis, the lower ethanol concentrations may be caused by ethanol degradation of *T. reesei* in the biofilm.

Nevertheless, 3 different steady-states of CBP of cellulose to ethanol based on a microbial consortium consisting of T. reesei and S. cerevisiae were reached, which proves the constant enzyme production of *T. reesei* during steady-state although the fungal growth in the steadystate much smaller than in a batch process. This disagrees with theories attributing enzyme production to fungal growth, which were mostly inspired by the theory of Reinhardt, that a filamentous fungus only grows at the hyphal tip. [100] During steady-state, the growth rate of the fungus is equal to its decay rate resulting in the required time-invariance. The decay constant  $k_d = 0.16 \text{ day}^{-1}$  was found to be roughly 20 times smaller than the maximum growth rate  $\mu_{\text{max}} = 3.0$  day  $^{-1}$ . [10] Thus, half of the productivity (Fig. 3.7), which was obtained in batch experiment, would be impossible to reach relating the enzyme production to a 20 times lower growth rate. [35] Gaden [101] expanded the kinetics of fermentation process to three types: Kinetics as result of primary metabolism (e.g. ethanol production by the yeast or oxygen consumption for fungal growth), kinetics related to primary metabolism (e.g. intermediate metabolites) and non-growth related kinetics. For T. reesei, it was found out that primary mycelia are formed during growth. Later on, these primary mycelia ere converted to secondary mycelia, which are responsible for enzyme production. [10] Therefore, enzyme production of T. reesei is not directly related to primary metabolism, but can be described by the following kinetics (eq. 3.6-3.9) [10, 101]:

$$\frac{d\left[X_{s}\right]}{dt} = 0 = k_{c}\left[X_{p}\right] - k_{d}\left[X_{s}\right] \tag{3.6}$$

$$\Leftrightarrow [X_s] = \frac{k_c}{k_d} [X_p] = \frac{k_c}{k_d} [X_{tot} - X_s] = \frac{2.4}{0.16} [X_{tot} - X_s]$$
 (3.7)

$$\Leftrightarrow [X_s] = 93.75\% [X_{tot}] \tag{3.8}$$

$$\frac{d[E]}{dt} \propto [X_s] \tag{3.9}$$

The mass balance for the concentration of secondary mycelia  $[X_S]$  is given by a formation term (the conversion of primary to secondary mycelia  $k_c[X_P]$ ) and a depletion term (decay of secondary mycelia  $k_d[X_S]$ ) (eq. 3.6). These two terms are equal during steady-state. As the conversion of primary mycelia to secondary mycelia occurs much faster than the decay of secondary mycelia, a large fraction of the total fungal biomass  $[X_{tot}]$ , namely 93.75 %, consists of secondary mycelia (eq. 3.8). [10] Recalling that the enzyme formation rate is proportional to the amount of secondary mycelia (eq. 3.9), it becomes clear, that the biofilm immobilization, which eliminates a wash-out depletion term in the mass balance, strongly favors the accumulation of secondary mycelia, which ensures high, steady enzyme production. [10]

# 3.4.2 Improvement of continuous CBP by enhanced utilization of cellobiose

Considering the optimization measures presented in the introduction (section 3.2), increasing the solid loading for higher titers, avoiding ethanol losses across the membrane with a closed oxygen loop and making better use of cellobiose, only the closed membrane loop was addressed. Given the maximum observed productivity of 0.025  $\frac{g}{I*h}$ , increasing the titer would demand residence times in the order of 240 h. Thus, increasing the productivity by better utilization of cellobiose was priorized. Cellobiose is the intermediate product of cellulose hydrolysis to glucose. Hydrolysis of cellulose in general is a reactions process with 3 kind of enzymes involved: Cellobiohydrolases (CBHs) cleave cellobiose molecules from the end of cellulose chains. Endoglucanases (EGs) cleave cellulose chains unselectively and thus, create more chain ends for CBH activity. The resulting cellobiose molecules are cleaved by  $\beta$ -glucosidase ( $\beta$ -G) to glucose monomers. [102] As cellulose is insoluble in water, the enzymatic reactions of CBH and EG follow the same scheme of enzyme adsorption to the substrate surface, formation of an enzyme-substrate complex with subsequent enzymatic hydrolysis reaction. [103] Cellobiose is soluble in water, but cannot be digested, neither by T. reesei nor by S. cerevisiae. Furthermore, cellobiose can bind the active sites of CBH and EG, which results in deactivation of CBH and EG and a blockage for  $\beta$ -G to cleave the cellobiose. [104] Concluding, that cellobiose is not only an unused dimer of two glucose molecules, but also inhibits the activity of all 3

enzyme, its concentration needs to be kept as low as possible. Unfortunately, T. reesei lacks in  $\beta$ -G production to effectively reduce the cellobiose concentration. [87] Thus, two options to decrease cellobiose concentrations were evaluated: The co-cultivation of T. reesei and Dekkera bruxellensis and the co-cultivation of T. reesei, A. phoenicis and S. cerevisiae. D. bruxellensis is a yeast strain which is able to ferment both, glucose and cellobiose, to ethanol. [105] A. phoenics is filamentous, aerobic fungus like *T. reesei* and is known as  $\beta$ -G hyperproducer. [87] Therefore, A. phoencis is cultivated in the same niche as T. reesei to balance the enzyme cocktail. [87] The fermentation is carried out with *S. cerevisiae* as usual. An experimental comparison of the two configurations (Fig. 3.9) showed that both consortia lead to ethanol production and depletion of cellobiose after time. However, the co-cultivation of *T. reesei* and *A. phoenics* with *S. cerevisiae* lead much faster to the desired results. Cellobiose was depleted completely already after 28 h and 50 % yield was reached after 120 h. With T. reesei and D. bruxellensis, the yield after 319 h was still below 5 % (42.7 %) and the cellobiose concentration was temporary at 2.7  $\frac{g}{l}$ , which reduces the hydrolysis speed by over 30 % based on literature data. [102] Such considerable hydrolysis inhibitions could cause a wash-out of enzymes during start-up of the continuous experiments. Therefore, the configuration with T. reesei, A. phoenicis and S. cerevisiae was chosen for the continuous experiment.

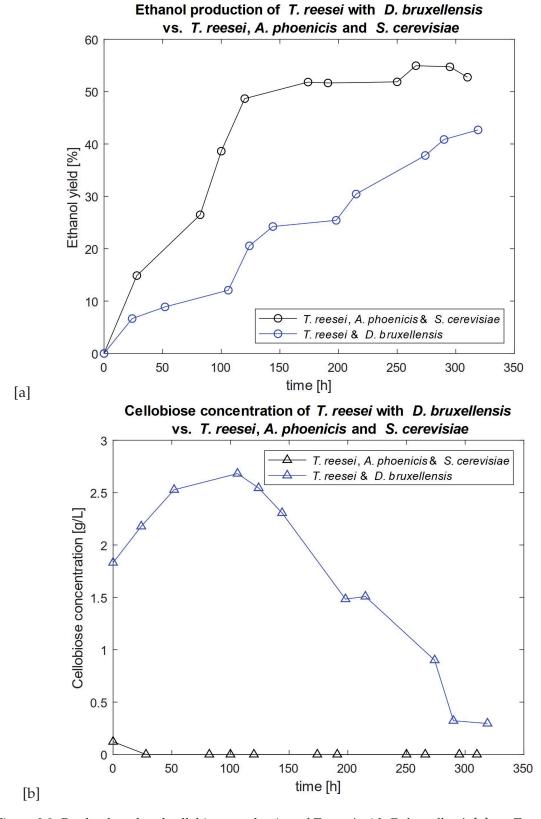


Figure 3.9: Batch ethanol and cellobiose production of *T. reesei* with *D. bruxellensis* [a] vs. *T. reesei* with *A. phoenicis* and *S. cerevisiae* [b].

The co-cultivation of *T. reesei*, *A. phoenicis* and *S. cerevisiae* imposes special requirements on the continuous setup since A. phoenicis and T. reesei share the same niche. Although their enzyme cocktails complement each other well [87], they are both aerobic, cellulolytic fungi, which will result in competition for the oxygen in the niche. [106] During batch experiments, the weaker competitor with the lower growth rate at the given conditions (temperature and pH) may be strengthened by an earlier inoculation to provide it with a longer growing time. [87] T. reesei was inoculated 24 h before A. phoenicis in batch experiments. [87] Fig. 3.10 depicts schematically the difference between co-cultivations in batch processes and continuous processes. The differently colored squares denote the temperature and pH range, where the respective species are able to grow. Consequently, overlapping squares represent possible conditions for co-cultivations. However, the growth rate of the involved species may differ vastly in the range of the given co-cultivation conditions (see accordingly colored lines at pH and T-axis in Fig. 3.10). In a batch experiment, a difference in growth rate may be compensated with an advantage in time as mentioned above. In a continuous steady-state process, which is time-invariant, the faster growing species would overgrow the slower growing species. Therefore, the range of possible co-cultivation conditions of *T. reesei* and *A. phoenicis* is reduced to one condition, where the growth rate of both fungi is identical. Note that this constraint does not apply for S. cerevisiae because the yeast will develop the earlier mentioned cheater-cooperator equilibrium with the fungus. [34] The growth rate constraint only applies to the two competing species, T. reesei and A. phoenicis. A temperature of 27 °C and a pH of 5 was identified to yield identical growth rates for *T. reesei* and *A. phoenicis* (Fig. 3.11).

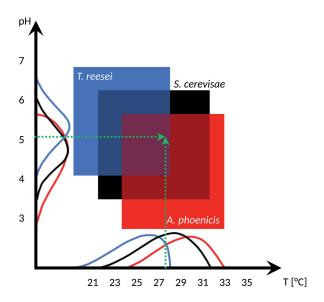


Figure 3.10: Schematic representation of the co-cultivation conditions for a microbial consortium consisting of *T. reesei*, *A. phoenicis* and *S. cerevisiae*. The blue, black and red square denote the range of temperature and pH, which allow growth for the respective species. The corresponding curves at the temperature and pH axis denote the growth rate as function of the axis variable, pH or T. The overlapping areas possibly allow co-cultivation. The green arrows denote the pH and Temperature condition, where *T. reesei* and *A. phoenicis* grow exactly at the same rate. Note that other parameters, which influence a co-cultivation such as secretion of antimicrobial substances are not considered in this plot. Figure adapted from [9].

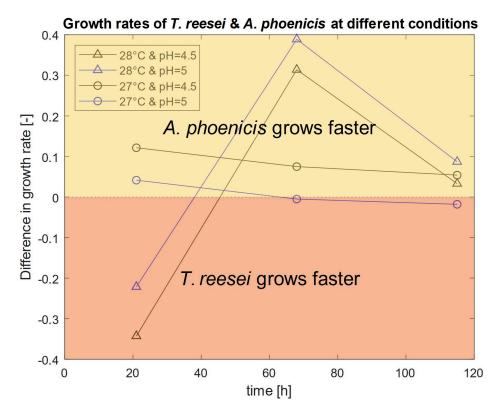


Figure 3.11: Growth rate comparison of *T. reesei* and *A. phoenicis* grown in separate Erlenmeyer flasks under identical conditions at different temperature and pH. The difference in growth rate is plotted against the time, meaning that values of zero correspond to identical growth rates. Positive values indicate faster growth of *A. phoenicis* and negative values faster growth of *T. reesei*, respectively. The growth rate does not have a unit since it was determined by means of spectrophotometry.

could not give an ethanol concentration of  $0.784 \frac{g}{L}$  because A. phoenicis does not provide enough CBH and EG activity. Given the enzyme production distribution of T. reesei and A. phoenicis [87], an ethanol concentration of  $0.91 \frac{g}{L}$  is the maximum for a co-cultivation of A. phoenicis and S. cerevisiae.

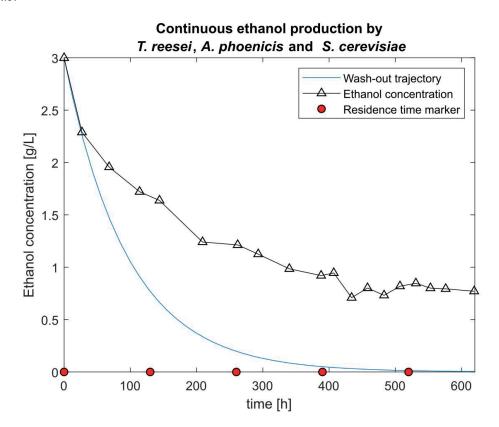


Figure 3.12: Continuous ethanol production with consolidated bioprocessing based on a microbial consortium of *T. reesei*, *A. phoenicis* & *S. cerevisiae*. The membrane (inner diameter  $d_i$ = 1.58 mm, outer diameter  $d_o$ = 3.18 mm, length L= 2.8 m was aerated with 21 % oxygen fraction. The cellulose feed concentration was 17.5  $\frac{g}{L}$  and the residence time  $\tau$  was 130 h.

However, the titer (0.784  $\frac{g}{L}$ ), the yield (9.7%) and the productivity (0.006  $\frac{g}{L*h}$ ) are low regarding the fact that *A. phoenicis* was added to improve the performance of the system by utilizing the cellobiose better. The same experiment without *A. phoenicis* (only *T. reesei* and *S. cerevisiae*) appeared to be much more productive (by a factor of ca. 4) showing a yield of 40.3%, a titer of  $3.26\pm0.01$   $\frac{g}{L}$  and a productivity of 0.025  $\frac{g}{L*h}$  (Fig. 3.7). On the one hand, this seems to be due to the less inhibiting effect of cellobiose during continuous operation as it cannot accumulate unlike in batch operation. On the other hand, the ethanol degradation rate in the biofilm may be higher since there are two species present, which are able to utilize ethanol as carbon source. Furthermore, the metabolic activity of the two fungi may be affected by the competition. When facing competition, the microorganisms shift their metabolism towards optimized defense

50 3.5 Conclusion

against competitors and invaders resulting in maximized growth whereas it is optimized for efficient nutrient uptake in a cooperative scenario. [107–109] Thus, it may be hypothesized that the degradation rate of ethanol in the biofilm increases despite the presence of favored substrates because both fungi utilize any carbon source to maximize growth.

# 3.5 Conclusion

The key challenges for continuous CBP of cellulose to ethanol, namely continuous feeding and product removal, prevention of contamination, immobilization of cells and extracellular products, long-term stability were overcome and a steady-state operation was achieved multiple times with a maximum titer of 3.26 $\pm$ 0.01  $\frac{g}{l}$  and a productivity of 0.025  $\frac{g}{l*h}$ . It was proven that T. reesei produces constantly enzymes over 750 h, which is in agreement with kinetic models considering enzyme production a process, which is unrelated to primary metabolism and carried out by the secondary mycelia of T. reesei. Furthermore, it was proven that the continuous co-cultivation of two competitors, T. reesei & A. phoenicis, is possible, if the process conditions are adjusted to identical growth rate. The addition of A. phoenicis targeted the better utilization of the inhibiting intermediate cellobiose by balancing the fungal enzyme cocktail in terms of higher  $\beta$ -G concentrations. This goal was achieved, but however did not result in higher yields or productivities. Furthermore, the continuous experiments showed that the oxygen flux per membrane area is a critical parameter for the process. Setups with identical volumetric oxygen transfer rate  $k_L$ a, but different oxygen fluxes per membrane area (large area & low concentration gradient vs. small area and high concentration gradient) showed titer differences of ca. 80 % (1.83  $\frac{g}{L}$  vs 3.26  $\frac{g}{L}$ ) in favor of setups with the large membrane surface. It is hypothesized that the difference is attributed to long diffusion paths in thicker biofilms and thus, shortage in nutrient supply. A rigorous process model is needed to examine this hypothesis in a quantitative manner.

# CHAPTER 4

Set-up and validation of a rigorous, spatially resolved model of the kinetics and mass transfer limitations of consortium-based consolidated bioprocessing for ethanol production

## 4.1 Abstract

The high degree of process intensification with CBP based on a microbial consortium in a membrane aerated biofilm reactor demands high standards for modeling. Various microbial interactions need to be considered and the heterogeneous reactor design causes considerable mass transfer limitations. A rigorous process model, which included all reaction kinetics and mass transfer limitations of the system was developed in this work. 9 species were considered (oxygen, glucose, T. reesei, secondary mycelia of T. reesei, enzymes, cellulose, cellobiose, yeast density and ethanol). 8 of these 9 species (all except cellulose) are present in the biofilm. In order to account properly for mass transfer limitations due to length of diffusion paths, these 8 spaces needed to be modeled spatially resolved. The fungal biofilm thickness  $\delta_f$  was found to be a critical parameter with an optimum for every membrane configuration. Smaller  $\delta_f$  reduced the fungal biofilm volume and thus, the enzyme production unnecessarily and larger  $\delta_f$  increased the diffusion path length and caused shortage in nutrient supply as well as lower enzyme concentrations in the bulk. The results of the model were able to explain the different productivities observed in the continuous experiments. The enzyme synthesis rate of the secondary mycelia was used as fitting parameter of the model. A reduction of ca. 40 %  $(0.67 \frac{FPU}{mL*d} \text{ vs } 1.152 \frac{FPU}{mL*d} \text{ compared to batch models yielded agreement with the continuous}$ experiments.

52 4.2 Introduction

## 4.2 Introduction

The efficient conversion of cellulosic substrates to various chemicals by CBP based on a microbial consortium in membrane aerated biofilm reactor has been proven numerous times. [4,9,50,110] Research was undertaken regarding the compatibility of different consortia and optimized biological pathways for maximized metabolic activity and minimized losses by CO<sub>2</sub> as byproduct of metabolism (e.g. by introducing the "lactate platform"). [9,50,110] A fundamental understanding of the process on a chemical engineering level is however still missing because modeling CBP rigorously is a complex task.

The complexity arises through the need to resolve a reaction network spatially (Fig. 4.1 & 4.2). Compared to other CBP experiments mentioned earlier, this is a rather simple layout, but still results in a complex reaction network (Fig. 4.1): *T. reesei* grows in the biofilm with oxygen and glucose as the two limiting substrates. The produced cellulases, consisting of cellobiohydrolase (CBH), endoglucanase (EG) and  $\beta$ -glucosidase ( $\beta$ -G), act synergistically to cleave cellulose to cellobiose and finally to glucose. Glucose is consumed by *T. reesei* and by *S. cerevisiae*, which ferments the sugar to ethanol. The target product ethanol may be depleted by aerobic metabolism of *S. cerevisiae* and by *T. reesei* if there is a shortage in a favored nutrient such as glucose.

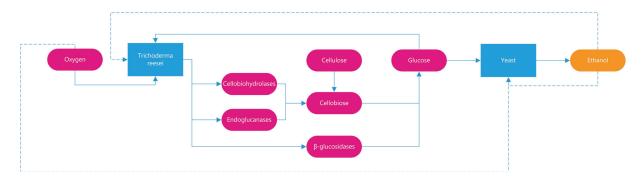


Figure 4.1: Kinetic network of consolidated bioprocessing of cellulose to ethanol by a microbial consortium of T. reesei & S. cerevisiae. T. reesei grows in the biofilm with oxygen and glucose as the two limiting substrates. The produced cellulases, consisting of cellobiohydrolase (CBH), endoglucanase (EG) and  $\beta$ -glucosidase ( $\beta$ -G), act synergistically to cleave cellulose to cellobiose and finally to glucose. Glucose is consumed by T. reesei and by S. cerevisiae, which ferments the sugar to ethanol. The target product ethanol may be depleted by aerobic metabolism of S. cerevisiae and by T. reesei if there is a shortage in a favored nutrient such as glucose. The solid lines represent desired reaction pathways. The dotted lines denote undesired side-reactions.

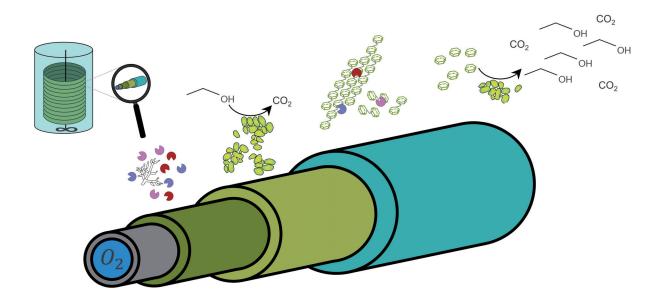


Figure 4.2: Schematic representation of consolidated bioprocessing of cellulose to ethanol by a microbial consortium of *T. reesei* & *S. cerevisiae*. Oxygen (blue) diffuses through a membrane (grey) and establishes an aerobic layer above the membrane in an otherwise anoxic reactor system. The aerobic, cellulolytic fungus *T. reesei* grows in this aerobic layer (dark green) and releases cellulases to the bulk (turquoise), where the cellulases hydrolyze cellulose to glucose. The glucose feeds both, *T. reesei* and *S. cerevisiae*, which grows anaerobically in the bulk, fermenting glucose to ethanol, as well as aerobically in the outer biofilm layer (light green), where oxygen residues are present.

Fig. 4.2 depicts the spatial arrangement of ethanol production by CBP. An aerobic, cellulolytic fungus, T. reesei, grows in an cylindrical aerobic layer provided by membrane aeration and releases cellulolytic enzymes, which diffuse to the bulk and synergistically hydrolyze the cellulose to glucose as mentioned above. The released soluble substances glucose and cellobiose are partly converted in the bulk and diffuse partly into the biofilm. Every component given in the reaction network except cellulose (Fig. 4.1) is present in the biofilm. Thus, a spatially resolved model accounting for mass transfer of every species except cellulose is necessary. Models are available describing each aspect of CBP: The mass transfer within a biofilm grown on a membrane [111,112], the growth kinetics of T. reesei and S. cerevisiae [10,19,102], microbial interaction in a community [34] and simultaneous enzymatic saccharification and fermentation (SSF) in a homogeneous bulk phase [102]. The key to rigorously modeling the present system is interlinking the different models, account for the interactions of the different submodels according to the reaction network (Fig. 4.1) and include any mass transfer limitations. Specifically, this implies a spatially resolved model with defined mass transfer mechanisms in the different reactor compartments such as the biofilm or the bulk. Moreover, the growth kinetics taken from other models are linked with the mass transfer equations and the dilution

of each species in the bulk due to the continuous operation. Applying time-invariance because of the steady-state assumption gives the set of equations, which needs to be solved.

This works aims to provide such a rigorous model for steady-state consolidated bioprocessing of cellulose to ethanol in order to enable a 50-fold scale-up from laboratory scale to pilot scale. The model data is validated with the results of the continuous CBP experiments (chapter 3).

## 4.3 Results and Discussion

Degrees of freedom & validation of the model

Before advancing to the set-up and solution of the model equation, it is worth overviewing the degrees of freedom (DOFs) of the model as well as its validation parameters since the ratio of validation parameters to the DoFs has a large impact on the quality of the model. A model, which satisfies a lot of validation points with only a few DoFs without too large errors, can be considered as highly precise. In contrast, any poor model with much more DoFs than validation points could be fitted to the same problem. Regarding the DoFs it is important to distinguish between DoFs of the experimental setups (e.g. the oxygen concentration within the membrane, the membrane area or the dilution rate) and DoFs of the model. Any design and set parameters are DoFs of the experimental setup. These DoFs need to be exploited to create a set of representative validation points for the model. In this work, the oxygen concentration within the membrane and the membrane area was varied (section 3) to create a set of 24 validation parameters (the bulk concentrations of ethanol, glucose, cellobiose and enzyme activity of three steady-states in reactor cascades with two reactors each). The number of DoFs of the model reduces to its fitting parameters. Since this work builds upon published model literature for the single bioprocesses occurring in the CBP reactor [10, 19, 34, 102, 111, 112], the model parameters, where the greatest deviation between a biofilm culture and a suspended culture was expected, were chosen as fitting parameters. The set of fitting parameters and thus, DoFs, was kept as small as possible in order to guarantee a good model quality, which is necessary for the optimization work to scale-up the system (section 5.3). In this work, the enzyme synthesis rate constant  $k_{synth}$  and the effective diffusivity of  $\beta$ -glucosidase  $D_{BG,eff}$  due to its affinity to cell wall attachment were used as fitting parameters. Varying  $k_{synth}$  allows to adjust the quantity of enzymes within the system to fit the model to the overall conversion results.  $D_{BG,eff}$  determines the fraction of cellobiose conversion in the bulk to cellobiose conversion in the biofilm, which influences the glucose supply for the two community members and thus, the microbial equilibrium. The fitting of these two parameters allowed for less than 0.5 % numerical error of model iterations and less than 15 % deviation of experimental results (validation parameters) and model results.

# Spatial structure of the model

As mentioned above, a spatially resolved model is crucial to account for mass transfer limitations. The biofilm forms two layers on the membrane, which are defined by the oxygen gradient (Fig. 4.2). The inner layer provides enough oxygen for growth of *T. reesei* and the outer layer provides enough oxygen for aerobic yeast metabolism. A tubular membrane design leads to the same layer formation, with cylindrical instead of plane shape (Fig. 4.3a). Note: Technically, the yeast is also a fungus. However, the yeast does not produce cellulase enzymes, but is able to perform anaerobic metabolism. The label "fungal biofilm" refers to the filamentous enzyme producing fungus *T. reesei*.

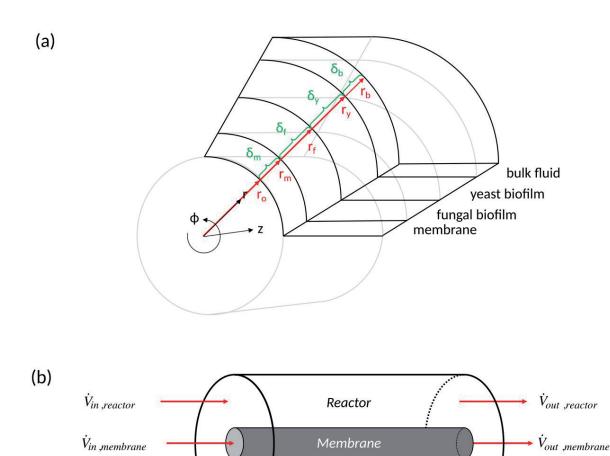


Figure 4.3: Schematic representation of the layer formation with a tubular membrane (a) and the concept of the bulk phase as cylindrical shell around the membrane and biofilm layers (b). Note: The straight membrane tube is a simplification for illustration purposes. The actual setup contains a helically winded membrane (Fig. 1.4).

From a mathematical point of view, the bulk phase is also considered to be a cylindrical layer element around the biofilm (Fig. 4.3b). Obviously, this does not hold for many reactor designs. However, since the bulk is defined to be perfectly mixed, the geometry of the bulk does not matter and assuming tubular shape serves to keep the model structure consistent. The radius of the bulk phase layer element is defined by the reactor volume subtracting the membrane and biofilm volume.

Although the membrane is winded densely within the reactor causing the upper and lower

side of the membrane touch each other, the system is considered to be of perfect tubular nature. Thus, there is no variance in the angular coordinate  $\varphi$ . A factor  $A_{eff} \in [0,1]$  is used to account for the effectively reduced membrane surface area. Hence, the 2D projection in the r-z-plane is sufficient to characterize the system keeping in mind that the outer layers have larger area/volume due to the cylindrical geometry of the system (Fig. 4.4).

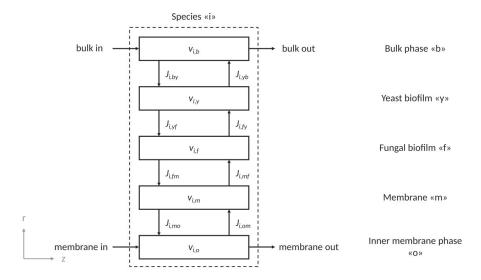


Figure 4.4: 2D projection of the layer formation in the r-z-plane. Each layer is characterized by a reaction term  $v_i$  for species i. The mass fluxes between the layers are denoted by  $J_i$ .

Each layer element (inner membrane phase, membrane, fungal biofilm, yeast biofilm & bulk phase) is characterized by different properties, which allow different simplifications of the governing equations.

#### *Set up of the model equations*

The model is based on the mass conservation law at steady-state for each layer element (Fig. 4.4). Note that only the important parameters and coefficients are introduced in this chapter for the purpose of readability. A definition of each physical quantity used in this model including its units is given in the nomenclature and in the Matlab® code (section B.2). Given the spatial structure of the model, specification can be set up for each species i, which is considered in the model (Tab. 4.1). The number of species i includes all species of the reaction network (Fig. 4.1), whereby the enzymes are grouped together to one species and *T. reesei's* total concentration as well as the concentration of secondary mycelia is considered. The enzymes are grouped

together since the composition of the enzymatic cocktail of *T. reesei* is known and assumed to be a material constant (eq. 4.1). [87]

$$c_{E} \begin{cases} \frac{0.7IU/ml}{81.93IU/ml} = 0.85\% \ c_{E,CBH} \\ \frac{81.1IU/ml}{81.93IU/ml} = 98.99\% \ c_{E,EG} \\ \frac{0.13IU/ml}{81.93IU/ml} = 0.16\% \ c_{E,\beta-G} \end{cases}$$

$$(4.1)$$

Distinguishing between the total cell density of *T. reesei* and the density of its secondary mycelia is necessary since enzyme synthesis of *T. reesei* is proportional to the concentration of secondary mycelia of *T. reesei*, whereas oxygen and glucose uptake are growth-related and thus depend on the primary mycelia density. The conversion of primary to secondary mycelia is modeled with 1<sup>st</sup> order reaction terms (Tab. 4.1). Note that the mass conservation law always requires a governing equation (e.g. Fick's law for diffusion) and a set of boundary conditions (BCs) depending on the order of the governing equations. Tab. 4.1 only refers to the specifications of the governing equations. The BCs for each species i are discussed later.

Table 4.1: Specifications for each species *i* considered in the model in every layer considered in the model.

Drocont				Drocont				Danielan terri
Present	iliass transier	generated by	-	Present	Present	mass transfer		Depletion term generated by
			convection to				0 ,	0 ,
,			membrane wall	,	,			
√	Convection	Inlet flow			<b>√</b>	Diffusion	X	Х
Х				Х	Х			
.,				.,	v			
Х				X	,			
Х				Х	Х			
Y				X	X			
Χ				X	Х			
Χ				X	Х			
Х				Х	X			
1	Convection	Convection from membrane wall	Outlet flow	1	✓	Diffusion	Х	X
	x x x x	Present Dominating mass transfer  ✓ Convection  X  X  X  X  X  X	Present mass transfer generated by  Convection Inlet flow  X  X  X  X  X  X  X  X  X  X  X  X  X	Present Dominating mass transfer generated by Source term generated by Outlet flow and convection to membrane wall  Convection Inlet flow  X  X  X  X  X  X  X  X  X  X  Convection from	Present Dominating mass transfer generated by generated by Outlet flow and convection to membrane wall  ✓ Convection Inlet flow  X  X  X  X  X  X  X  X  X  X  X  X  X	Present Dominating mass transfer generated by generated by Outlet flow and convection to membrane wall  Convection Inlet flow  Convection Inlet flow  Convection Inlet flow  Convection Inlet flow  X  X  X  X  X  X  X  X  X  X  X  X  X	Present Dominating mass transfer generated by enerated by Outlet flow and convection to membrane wall  Convection Inlet flow  X  X  X  X  X  X  X  X  X  X  X  X  X	Present

Table 4.2: Specifications for each species i considered in the model in every layer considered in the model. (continued)

					Yeast biofilm "y"			
						Dominating	Source term	Depletion term
Species\spatially resolved specifications			Fungal biofilm "f"		Present	mass transfer	generated by	generated by
species (spatially resolved specifications		Dominating	Source term	Depletion term				Growth and
	Present	mass transfer	generated by	generated by				maintenance
			,	Growth and	✓	Diffusion	X	of S. cerevisae
				maintenance	X			
Oxygen	✓	Diffusion	Х	of T. reesei				
			Monod growth	1st order	X			
Trichoderma reesei Trichoderma reesei	✓	Stationary	kinetics 1st conversion	decay reaction 1st order				
secondary mycelia	✓	Stationary	reaction of primary mycelia	decay reaction				1st order
secondary mycena	•	Stationary	1st order enzyme synthesis	accay reaction	✓	Diffusion	X	decay reaction
			reaction of T. reesei	1st order			, 	
Enzymes	✓	Diffusion	secondary mycelia	decay reaction	X			
					,.			Enzymatic
Cellulose	Χ			F	✓	Diffusion	X	hydrolysis
Cellobiose	✓	Diffusion	Х	Enzymatic hydrolysis	•	Dinasion	^	, α. σ. γ. σ. σ
Cellobiose	•	Dillusion	^	llyulolysis				Growth and
				Growth and			F	maintenance
			Enzymatic	maintenance	✓	Diffusion	Enzymatic hydrolysis	of S. cerevisae
Glucose	✓	Diffusion	hydrolysis	of T. reesei	<b>V</b>	Dillusion	nyarotysis	or S. Cerevisae
	.,				,		Monod growth	1st order
Yeast	Х				✓	Stationary	kinetics	decay reaction
				Degradation by			Fermentation	Respiration
Ethanol	✓	Diffusion	X	T. reesei	_		kinetics	kinetics
			•		✓	Diffusion	of S. cerevisiae	of S. cerevisiae

Table 4.3: Specifications for each species *i* considered in the model in every layer considered in the model. (continued)

Species\spatially resolved specifications			Bulk phase "b"	
	Present	Dominating mass transfer	Source term generated by Convection from the	Depletion term generated by
Oxygen	✓		biofilm	Outlet flow
Trichoderma reesei	X			
Trichoderma reesei				
secondary mycelia	X		Convection	1st order
			from the	decay reaction
Enzymes	✓		biofilm	& outlet flow
Cellulose	<b>√</b>		Inlet flow	Enzymatic hydrolysis and outlet flow
Cellobiose	✓		Enzymatic hydrolysis	Enzymatic hydrolysis and outlet flow
				Growth and maintenance
Glucose	✓		Enzymatic hydrolysis	of S. cerevisae and outlet flow
Yeast	√		Monod growth kinetics	1st order decay reaction and outlet flow
			Fermentation kinetics of S.	Respiration kinetics of S. cerevisiae
Ethanol	✓		cerevisiae	and outlet flow

## Inner membrane phase "o":

Only oxygen and ethanol are present in the inner membrane phase. The steady-state assumption cancels out the time variance. The transport of gases from the inner membrane bulk to the membrane wall and vice versa is dominated by forced convection due to the gas flow within the membrane. In both cases, the mass balance shows that the difference in inlet and outlet flow of the membrane corresponds to the quantity of oxygen or ethanol, respectively, which is transported to or from the membrane wall by forced convection (eq. 4.2 & 4.3).

$$\frac{\partial \left(V_{o}c_{ox}\right)}{\partial t} = 0 = \dot{V}_{o,feed}c_{ox,o,feed} - J_{conv,0x,om} - \dot{V}_{o,out}c_{ox,o,out}$$

$$\tag{4.2}$$

$$\frac{\partial \left(V_{o}c_{EtOH}\right)}{\partial t} = 0 = \dot{V}_{o,feed}c_{EtOH,o,feed} + J_{conv,EtOH,om} - \dot{V}_{o,out}c_{EtOH,o,out} \tag{4.3}$$

The convective mass transfer flux is defined as follows for both species:

$$J_{conv,i,om} = 2\pi r_o k_{\text{conv,i,om}} \left( c_{i,o} - c_i |_{r=r_o} \right)$$

$$\tag{4.4}$$

The convective mass transfer coefficient is calculated by a Nusselt correlation and the Colburn analogy for either laminar or turbulent flow resp. the interpolation between both for transitional flow. [113,114] The model contains an if-loop to obtain the right Nusselt correlation for each flow regime. The correlation for laminar flow is shown here for illustration purpose (eq. 4.5).

$$Nu = \left\{ 3.66 + 0.08 \left[ 1 + 0.8 \left( \frac{d}{D_w \left[ \left( \frac{h}{\pi D_w} \right)^2 \right]} \right)^{0.9} \operatorname{Re}^{0.5 + 0.2903} \left( \frac{d}{D_w \left[ \left( \frac{h}{\pi D_w} \right)^2 \right]} \right)^{0.194} \operatorname{Pr}^{1/3} \right] \right\} \left( \frac{Pr}{Pr_W} \right)^{0.14}$$
(4.5)

The Nusselt correlation for a helically winded pipe is of empirical nature und depends only on the fluid properties and the geometry of the tube. The Colburn analogy allows to replace Nu with the Sherwood number Sh and the Prandtl number Pr with the Schmidt number Sc. Sh relates the convective mass transfer coefficient to the diffusivity, which is a known material constant (eq. 4.6).

$$Sh = \frac{k_{\text{conv}} d_i}{D_i} \tag{4.6}$$

Knowing  $k_{conv,i}$  allows to solve the mass balances for ethanol and oxygen in the inner membrane phase. However, at the membrane wall, both oxygen and ethanol will change from the gaseous/vapor phase to the dissolved phase as they can only diffuse through the membrane matrix as dissolved species. The absorption by the membrane is modeled with a Henry type law (eq. 4.7):

$$c_i|_{r=r_o} = S_{i,m} n_i p_m \tag{4.7}$$

The wall concentration of ethanol and oxygen is equal to their partial pressure times their solubility constant in PDMS. [14]

#### Membrane "m":

As no reactions occur in the membrane, the local concentrations of oxygen and ethanol are given by Fick's law of diffusion:

$$\frac{\partial c_i}{\partial t} = \vec{\nabla} J_{i,f} + v_{i,f} \tag{4.8}$$

$$\Leftrightarrow \frac{\partial c_i}{\partial t} = 0 = \vec{\nabla} \left( \vec{\nabla} D_{i,f} c_i \right) + v_{i,f}$$
(4.9)

$$\Rightarrow 0 = D_{i,f} \Delta c_i + v_{i,f} \tag{4.10}$$

$$\Rightarrow 0 = D_{i,f} \left( \frac{2}{r} \frac{\partial c_i}{\partial r} + \frac{\partial^2 c_i}{\partial r^2} + \frac{\partial^2 c_i}{\partial z^2} \right) + v_{i,f}$$
 (4.11)

Eq. 4.8 denotes the continuity equation. Applying Fick's law of diffusion yields eq. 4.9. Assuming isotropic diffusivity (eq. 4.10) and neglecting the variance in the angular coordinate  $\varphi$  gives the final mass balance for the local concentrations (eq. 4.11). The first derivative term,  $\frac{2}{r}\frac{\partial c_i}{\partial r}$ , accounts for the cylindrical geometry of the system, whereas  $\frac{\partial^2 c_i}{\partial r^2} + \frac{\partial^2 c_i}{\partial z^2}$  simply describe a 2-D diffusion problem. [115] Note that the common approach to model diffusion is the solution-diffusion approach where the driving force is expressed as the gradient in the chemical potential. [116] However, since the pressure difference across the membrane is negligible, the difference in chemical potential is reduced to the difference in concentration. Furthermore, the Henry law is considered for the solution part of the solution diffusion model. The convective boundary layer and the gradient in z-direction were the reason, why the solution diffusion model could not be applied.

## Fungal biofilm "f":

The fungal biofilm is a more complex layer since more species are present in the fungal biofilm layer and reactions take place. However, the mass transfer mechanism is diffusion for every species in the fungal biofilm except the stationary mycelia. Thus, Fick's law will be applied again. The analysis of the fungal biofilm layer is started with the kinetic growth model of *T. reesei*.

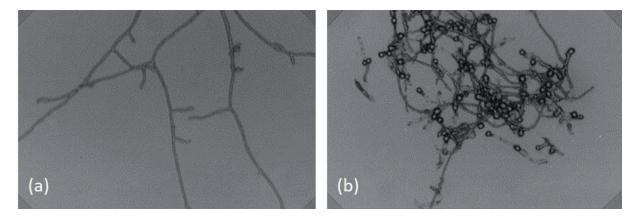


Figure 4.5: Primary mycelia (a) and secondary mycelia (b) of T. reesei. Figure taken from [10]

The growth kinetics of *T. reesei* were adapted from a published kinetic model for batch cultivation [10]:

The fungus consumes nutrients to grow primary mycelia (eq. 4.12 and Fig. 4.5a), which are converted to secondary mycelia (eq. 4.12 & 4.13 and Fig. 4.5b) responsible for the enzyme production, and finally, the secondary mycelia decay (eq. 4.13).

$$\frac{d[X]_{Tr,prim}}{dt} = \mu_{\text{max}} \min \left[ \frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}} \right] [X]_{Tr, \text{ prim}} - k_{Tr,p-s} [X]_{Tr, \text{ prim}}$$
(4.12)

$$\frac{d[X]_{Tr,sec}}{dt} = k_{Tr,p-s}[X]_{Tr, \text{ prim }} - k_{\text{decay }}[X]_{Tr, \text{ sec}}$$

$$(4.13)$$

Mycelia conversion and decay are modeled as  $1^{st}$  order reactions with reaction constants  $k_{Tr,p-s}$  and  $k_{decay}$ , respectively. The fungal growth is modeled with substrate-limited Monod-kinetics.  $\mu_{max}$  is the maximum growth rate,  $K_G$  and  $K_{ox}$  are the half-saturation constants for glucose and oxygen, respectively. The limiting nutrient at each position in the biofilm is identified and considered by min  $\left\lceil \frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}} \right\rceil$ .

Given  $[[X]_{Tr,sec} + [X]_{Tr,prim} = [X]_{Tr}$  (the fungus consists only of primary and secondary mycelia), allows to derive the local fraction of secondary mycelia and primary mycelia from eq. 4.13 with steady-state assumption:

$$0 = k_{Tr,p-s} ([X]_{Tr} - [X]_{Tr,sec}) - k_{decay} [X]_{Tr,sec}$$
(4.14)

$$\Leftrightarrow [X]_{Tr,sec} = \frac{k_{Tr,p-s}}{k_{Tr,p-s} + k_{\text{decay}}} [X]_{Tr}$$
(4.15)

$$\Rightarrow [X]_{\text{Tr,prim}} = \frac{k_{\text{decay}}}{k_{\text{Tr,}p-s} + k_{\text{decay}}} [X]_{Tr}$$
(4.16)

Applying steady-state for eq. 4.12 gives:

$$0 = \mu_{\text{max}} \min \left[ \frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}} \right] [X]_{Tr,prim} - k_{Tr,p-s} [X]_{Tr,prim}$$
(4.17)

$$\Leftrightarrow \mu_{\text{max}} \min \left[ \frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}} \right] = k_{Tr, p-s}$$
 (4.18)

The conversion rate of primary to secondary mycelia is equal to the growth rate, which is limited either by glucose or by oxygen, because these two are the scarcest nutrients in the system. As the nutrient limitation will be time-invariant, but space-dependent, the conversion constant  $k_{Tr,p-s}$  cannot be a constant as proposed for batch operation. [10] It is a function of the concentration of the limiting nutrient and the material constants  $\mu_{max}$ ,  $K_G$  and  $K_{ox}$ .

Inserting eq. 4.18 into eq. 4.15 and applying stead-state yields:

$$[X]_{Tr,sec} = \frac{\mu_{\text{max}} \min\left[\frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}}\right]}{\mu_{\text{max}} \min\left[\frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}}\right] + k_{\text{decay}}} [X]_{Tr}$$
(4.19)

 $\mu_{max}$  and  $K_G$  for T. reesei are taken from Velkovska et al. [10], whereas there is little information about the half-saturation constant of oxygen  $K_{ox}$ . T. reesei is usually cultivated in bubble aerated tanks with high oxygen concentrations of 5-13.5  $\frac{mg}{L}$ . [8,17] Oxygen half-saturation constants between 0.26  $\frac{mg}{L}$  and 1.1  $\frac{mg}{L}$  were published for different kinds of bacteria. [18–20] After evaluating the impact of  $K_{ox}$  values in the given range (Fig. 6), it was chosen to start the model with  $K_{ox} = 1$   $\frac{mg}{L}$  and fit  $K_{ox}$  to the experimental results if necessary.

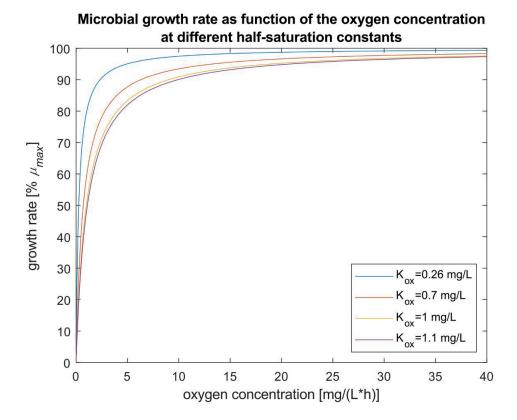


Figure 4.6: Microbial growth rate as function of the oxygen concentration at different half-saturation constants, which were published for bacteria. [11–13]

Hence, all parameters to determine  $[X]_{Tr,sec}$  from  $[X]_{Tr}$  are given, but  $[X]_{Tr}$  is still unknown. The given equations for  $[X]_{Tr}$ , the steady-state mass balance and the two boundary conditions (eq.4.20-4.22) form a homogeneous set of equations meaning that there is no constant part in any of the equations.

$$\frac{d[X]_{Tr}}{dt} = \frac{d[X]_{Tr,prim}}{dt} + \frac{d[X]_{Tr,sec}}{dt} = \mu_{\text{max}} \min \left[ \frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}} \right] [X]_{Tr,prim} - k_{\text{decay}} [X]_{Tr,sec} = 0$$
(4.20)

$$[X]_{Tr}|_{r=r_{uv}} = 0 (4.21)$$

$$[X]_{Tr}|_{r=r_f} = 0 (4.22)$$

The mass balance is equal zero because of steady-state operation and the boundary conditions result from zero fungal growth in the membrane and the yeast biofilm. A homogeneous set of

equations has either only the zero-solution  $[X]_{Tr}$  or infinite solutions with the 0 solution among them. [117] Thus, the concentration profile of  $[X]_{Tr}$  has to be solved elsewise: The fungal biofilm has a certain thickness  $\delta_f$ , which is yet unknown, but defined by the oxygen concentration. Below a certain oxygen concentration threshold, T. reesei will either be unable to perform aerobic metabolism, or the yeast will overgrow T. reesei at the given oxygen concentration. In any way, this oxygen concentration  $c_{O_2}^*$  will mark the end of the fungal biofilm:

$$\delta_f = r_f - r_m = r|_{c_{ox} = c_{ox}^*} - r_m \tag{4.23}$$

The density of fungal biomass of *T. reesei* is reported to be  $\bar{\rho}_{Tr} = 334 \frac{g}{L}$  and the mean cell fraction in biofilms is  $\bar{n}_{Tr,bf} = 0.15$ . [118,119] Thus, the mean cell concentration of *T. reesei* in the biofilm will be 50.1  $\frac{g}{L}$  (eq. 4.24):

$$\bar{\rho}_f = \bar{\rho}_{Tr} * \bar{n}_{Tr,bf} = 50.1 \frac{g}{L} = [X]_{Tr}|_{r_m < r < r_f}$$
 (4.24)

Assuming a constant  $[X]_{Tr}$  over the biofilm is a improper simplification considering the vastly varying growth rate. Therefore, the cell concentration of T. reesei was adjusted to the local growth limitation while maintaining the given mean value (eq. 4.25):

$$[X]_{Tr} = \bar{\rho}_f * \frac{\mu}{\bar{\mu}} \tag{4.25}$$

Eq. 4.25 completes the set of equations for the *T. reesei* growth dynamics: Eq. 4.25 relates the fungal cell concentration to the oxygen and glucose concentration, eq. 4.19 gives the secondary mycelia concentration for the enzyme synthesis as function of the oxygen, glucose and total cell concentration.

Each other species diffuses across the biofilm and has source and/or depletion terms. The concentration profiles for oxygen and glucose can be derived from eq. 4.12, eq. 4.17 and Tab. 4.1: (eq. 4.26 & 4.27.

$$0 = D_{ox,f}\left(\frac{2}{r}\frac{\partial c_{ox}}{\partial r} + \frac{\partial^2 c_{ox}}{\partial r^2} + \frac{\partial^2 c_{ox}}{\partial z^2}\right) - \frac{\mu_{\text{max}}}{Y_{X,\text{tr}/o}}\min\left[\frac{c_g}{K_G + c_g}; \frac{c_{ox}}{K_{ox} + c_{ox}}\right] \frac{k_{\text{decay}}}{k_{Tr,p-s} + k_{\text{decay}}} [X]_{Tr} - M_{X,\text{tr}/O}[X]_{Tr}$$
(4.26)

$$0 = D_{G,f}\left(\frac{2}{r}\frac{\partial c_{G}}{\partial r} + \frac{\partial^{2}c_{G}}{\partial r^{2}} + \frac{\partial^{2}c_{G}}{\partial z^{2}}\right) + \frac{K_{Cb}c_{Cb}0.16\%c_{E}}{K_{m}\left(1 + \frac{c_{g}}{K_{CbG}}\right) + c_{Cb}} - \frac{\mu_{\max}}{Y_{X,tr/G}}\min\left[\frac{c_{g}}{K_{G} + c_{g}}; \frac{c_{ox}}{K_{ox} + c_{ox}}\right] \frac{k_{\text{decay}}}{k_{Tr,p-s} + k_{\text{decay}}}[X]_{Tr}$$

$$-M_{X,tr/G}[X]_{Tr}$$

$$(4.27)$$

T. reesei consumes oxygen and glucose for growth of new mycelia and maintenance of the existing mycelia. The corresponding consumption rate is determined by the product of a

yield coefficient respectively maintenance coefficient and the growth rate respectively the concentration of mycelia. These coefficients may be regarded as material constants and were taken from literature (Tab. 4.1). [19] The source term for glucose is hydrolysis of cellobiose in the fungal biofilm. [102]

Table 4.4: Overview of the yield and maintenance coefficients of *T. reesei* for oxygen and glucose. [19]

	Oxygen	Glucose
Growth	$Y_{X,tr/O} = 1.01 \frac{g_{X,tr}}{g_{o2}}$	$Y_{X,tr/G} = 0.44 \frac{g_{X,tr}}{g_G}$
Maintenance	$M_{X,tr/O} = 0.0272 \frac{g_{O2}}{g_{X,tr}*h}$	$M_{X,tr/G} = 0.0252 \frac{g_G}{g_{X,tr}*h}$

The mass balance for the enzymes in the fungal biofilm is given as follows (eq. 4.28)

$$0 = D_{E,f} \left( \frac{2}{r} \frac{\partial c_E}{\partial r} + \frac{\partial^2 c_E}{\partial r^2} + \frac{\partial^2 c_E}{\partial z^2} \right) + k_{\text{synth}} [X]_{Tr,sec} - k_{E,decay} C_E$$
 (4.28)

Fick's law accounts for the diffusive mass transfer of enzymes within the biofilm,  $k_{synth}[X]_{Tr,sec}$  denotes the enzyme synthesis source term in the fungal biofilm and  $k_{E,decay}c_E$  is the enzyme decay depletion term.  $k_{synth}$  and  $k_{E,decay}$  again are material constants taken from literature. [10] Including cellobiose diffusion into the fungal biofilm in the model is important since it is an important nutrient support for T. reesei. Cellobiose cannot be digested by the yeast, but is hydrolyzed to glucose by  $\beta$ -G, which adheres mostly to the T. reesei cell surface (80 % adhesion, 20 % free enzymes). [87]

$$0 = D_{Cb,f} \left( \frac{2}{r} \frac{\partial c_{Cb}}{\partial r} + \frac{\partial^2 c_{Cb}}{\partial r^2} + \frac{\partial^2 c_{Cb}}{\partial z^2} \right) - \frac{K_{Cb} c_{Cb} 0.16\% c_E}{K_m \left( 1 + \frac{c_g}{K_{CbG}} \right) + c_{Cb}}$$
(4.29)

The mass balance for ethanol consists of the diffusion terms and a *T. reesei* degradation term for depletion.

$$0 = D_{EtOH,f} \left( \frac{2}{r} \frac{\partial c_{EtOH}}{\partial r} + \frac{\partial^2 c_{EtOH}}{\partial r^2} + \frac{\partial^2 c_{EtOH}}{\partial z^2} \right) - k_{degr}[X]_{Tr}$$
(4.30)

## Yeast biofilm "y":

The mass balances in the yeast biofilm are formed analog to the fungal biofilm. Accordingly, the same problem of a homogeneous equation system arises for the immobilized yeast. The mean density for yeast cells is  $1100 \frac{g}{L}$ . [120,121]

$$\bar{\rho}_y = \bar{\rho}_Y * \bar{n}_{Y,y} = 0.15 * 1100 \frac{g}{I} = 165 \frac{g}{I} = [X]_Y|_{r_f < r < r_y}$$
 (4.31)

The thickness of the yeast biofilm layer is defined by the so-called Pasteur point. [122] The Pasteur point denotes the oxygen threshold, where *S. cerevisiae* switches to anaerobic metabolism. Since there is no point for the yeast to attach to the biofilm for anerobic metabolism because the bulk is much richer in nutrients, it is assumed that the biofilm ends at the Pasteur point of the yeast. The mass balances for oxygen and glucose are formed by replacing the fungal depletion terms by yeast depletion terms: [102]

$$0 = D_{ox,f} \left( \frac{2}{r} \frac{\partial c_{ox}}{\partial r} + \frac{\partial^2 c_{ox}}{\partial r^2} + \frac{\partial^2 c_{ox}}{\partial z^2} \right) - \frac{\mu_{max}}{Y_{X,Y/0}} \left( \frac{c_g}{K_{GY} + c_g} \right) \left( 1 - \frac{c_{EtOH}}{K_{X\_EtOH}} \right)$$
(4.32)

$$0 = D_{G,f} \left( \frac{2}{r} \frac{\partial c_G}{\partial r} + \frac{\partial^2 c_G}{\partial r^2} + \frac{\partial^2 c_G}{\partial z^2} \right) + \frac{K_{Cb}c_{Cb}0.16\%c_E}{K_m \left( 1 + \frac{c_g}{K_{Cb}c_D} \right) + c_{Cb}} - \frac{\mu_{\text{max}}}{Y_{X,Y/G}} \left( \frac{c_g}{K_{GY} + c_g} \right) \left( 1 - \frac{c_{EtOH}}{K_{X\_EtOH}} \right)$$
(4.33)

Enzymes are not synthesized anymore in the yeast biofilm layer:

$$0 = D_{E,f} \left( \frac{2}{r} \frac{\partial c_E}{\partial r} + \frac{\partial^2 c_E}{\partial r^2} + \frac{\partial^2 c_E}{\partial z^2} \right) - k_{E, \text{ decay }} c_E$$
 (4.34)

The cellobiose mass balance does not change compared to the fungal biofilm:

$$0 = D_{Cb,f} \left( \frac{2}{r} \frac{\partial c_{Cb}}{\partial r} + \frac{\partial^2 c_{Cb}}{\partial r^2} + \frac{\partial^2 c_{Cb}}{\partial z^2} \right) - \frac{K_{Cb} c_{Cb} 0.16\% c_E}{K_m \left( 1 + \frac{c_g}{K_{CbG}} \right) + c_{Cb}}$$
(4.35)

The ethanol formation by the yeast needs to be considered in the ethanol mass balance:

$$0 = D_{EtOH,f} \left( \frac{2}{r} \frac{\partial c_{EtOH}}{\partial r} + \frac{\partial^2 c_{EtOH}}{\partial r^2} + \frac{\partial^2 c_{EtOH}}{\partial z^2} \right) + Y_{EtOH-G} \frac{\mu_{\text{max}}}{Y_{X,Y/G}} \left( \frac{c_g}{K_{GY} + c_g} \right) \left( 1 - \frac{c_{EtOH}}{K_{X-EtOH}} \right) - k_{degr}[X]_Y$$
(4.36)

## Bulk phase "b":

The bulk phase is well-mixed and thus, there is no mass transfer limitation. The source term for all species from the immobilized phase is the convective mass flux into the bulk, which is calculated again with a Nusselt correlation and the Colburn analogy as explained above. The mass balances for the oxygen, glucose, enzymes and ethanol are:

$$0 = \frac{1}{V} J_{ox,conv,y} - \frac{1}{\tau} c_{ox}$$
 (4.37)

$$0 = \frac{1}{V} J_{G,conv,y} + \frac{K_{Cb}c_{Cb}0.16\%c_E}{K_m \left(1 + \frac{c_g}{K_{CbG}}\right) + c_{Cb}} - \frac{\mu_{\text{max}}}{Y_{X,Y/G}} \left(\frac{c_g}{K_{GY} + c_g}\right) \left(1 - \frac{c_{EtOH}}{K_{X_-EtOH}}\right) - \frac{1}{\tau}c_G \quad (4.38)$$

$$0 = \frac{1}{V} J_{E,conv,y} - \left(\frac{1}{\tau} + k_{E,decay}\right) c_E \tag{4.39}$$

$$0 = \frac{-1}{V} J_{EtOH, \text{ conv }, y} + Y_{EtOH-G} \frac{\mu_{\text{max}}}{Y_{X,Y/G}} \left( \frac{c_g}{K_{GY} + c_g} \right) \left( 1 - \frac{c_{EtOH}}{K_{X-EtOH}} \right) - \frac{1}{\tau} c_{EtOH}$$
(4.40)

The cellulose and cellobiose mass balance is governed by the kinetics of the enzymatic hydrolysis, which were taken from literature and adapted to continuous operation: [102]

$$[C]_{\text{in,endo}} + [C]_{\text{in,exo}} = [C]_{\text{in}}$$
 (4.41)

$$[C]_{\text{endo}} + [C]_{\text{exo}} = [C]$$
 (4.42)

$$[C] = [C]_{in} + \frac{r_C}{D} \tag{4.43}$$

$$0 = -k_{\text{endo}} \times \frac{[\text{EC}]_{\text{endo}}}{1 + \sigma_{\text{endo}}} \times \left(\frac{K_{\text{C-Cb}}}{[\text{Cb}] + K_{\text{C-Cb}}}\right) \times \left(\frac{K_{\text{C-EtOH}}}{[\text{EtOH}] + K_{\text{C-EtOH}}}\right) + D\left([C]_{\text{in,endo}} - [C]_{\text{endo}}\right)$$

$$(4.44)$$

$$0 = -k_{\text{exo}} \times \frac{[\text{EC}]_{\text{exo}}}{1 + \sigma_{\text{exo}}} \times \left(\frac{K_{\text{C-Cb}}}{[\text{Cb}] + K_{\text{C-Cb}}}\right) \times \left(\frac{K_{\text{C-EtOH}}}{[\text{EtOH}] + K_{\text{C-EtOH}}}\right) + D\left([C]_{\text{in,exo}} - [C]_{\text{exo}}\right)$$

$$(4.45)$$

$$0 = k_{fc} \left[ E_{f, \text{ endo}} \right] \times \left[ C_{f, \text{ endo}} \right] \left( 1 + \sigma_{\text{endo}} \right) - \frac{k_{fc}}{K_{\text{endo}}} \left[ EC \right]_{\text{endo}} - D[EC]_{\text{endo}}$$
(4.46)

$$0 = k_{fc} [E_{f,exo}] \times [C_{f,exo}] \times (1 + \sigma_{exo}) - \frac{k_{fc}}{K_{exo}} [EC]_{exo} - D([EC]_{exo})$$
(4.47)

$$[E_{f,endo}] = [E_T] - \frac{[EC]_{endo} \times \sigma_{endo}}{(1 + \sigma_{endo})}$$
(4.48)

$$[E_{f,exo}] = [E_T] - \frac{[EC]_{exo} \times \sigma_{exo}}{(1 + \sigma_{exo})}$$

$$(4.49)$$

$$[C_{f,endo}] = [C] - \frac{[EC]_{endo}}{(1 + \sigma_{endo})}$$

$$(4.50)$$

$$[C_{f,exo}] = [C] - \frac{[EC]_{exo}}{(1 + \sigma_{exo})}$$
 (4.51)

$$0 = -\left(\frac{342}{324}\right) r_{C} - \left(\frac{K_{Cb}[Cb][BG]}{K_{m} \times \left(1 + \frac{[G]}{K_{Cb-G}}\right) + [Cb]}\right) - D[Cb]$$
(4.52)

$$0 = -\left(\frac{360}{342}\right) \times \left(\frac{K_{Cb}[Cb][BG]}{K_{m} \times \left(1 + \frac{[G]}{K_{Cb}G}\right) + [Cb]}\right) - \left(\frac{1}{Y_{X,Y,G}}r_{Y,b} + D[G]\right)$$
(4.53)

$$\mathbf{r}_{Y,b} = \left(\frac{\mu_{\text{max}}[G]}{K_{G} + [G]}\right) \times [X]_{Y} \times \left(1 - \frac{[EtOH]}{K_{X_{-}EtOH}}\right)$$
(4.54)

$$0 = r_{Y,b} - D[X]_Y (4.55)$$

$$0 = \left(\frac{Y_{\text{EtOH,G}}}{Y_{X,Y,G}}\right) \times r_{Y,b} - D[EtOH]$$
(4.56)

As mentioned above, the mass conservation law demands a set of boundary conditions besides the governing equations. At the boundaries of each layer element, a BC of one of the following type is present:

- Dirichlet BC:  $c_i|_{r_0} = \text{const.}$  (fixed values of certain species in the bulk or inner membrane phase)
- Neumann BC:  $\frac{dc_i}{dr}\Big|_{r_0} = \text{const.}$  (fixed gradients e.g. same diffusion flux between the fungal and yeast biofilm layer)
- Robin BC:  $c_i|_{r_0} + \frac{dc_i}{dr}|_{r_0} = \text{const.}$  (fixed balance between gradient an absolute value, e.g. due to balance of diffusion and convection at the yeast biofilm boundary to the bulk)

In general, the BCs are straightforward except for the microbial biomass, which was discussed before and the oxygen BC at the inner membrane phase. Thus, this BC is derived below.

The Henry law needs to be applied at the inner membrane wall since oxygen is dissolved in the membrane for the diffusion process:

$$c_{ox}|_{r_o} = H_{cp}^{ox} p_{ox}|_{r_o} (4.57)$$

If convective mass transfer in the boundary layer at the inner membrane wall is neglected, the BC at the inner membrane side simplifies to the above-mentioned Henry equation and depends only on the absolute pressure and the oxygen concentration of the flushing gas. However, the BC becomes more complex, if (a) pressure loss within the membrane is considered and (b) convective mass transfer at the inner membrane side is not neglected. Since the aim of this work is to model the system as rigorously as possible in order to achieve scale-independent results, the BC is calculated as follows: The factor  $p_{ox}|_{r_o}$  needs to be corrected for the pressure gradient within the membrane and the convective mass transfer at the inner membrane side. The pressure loss in a helical coil without any armatures is defined as [114]:

$$\Delta p = \zeta \frac{L}{d_i} \rho \frac{u^2}{2} \tag{4.58}$$

 $\zeta$  denotes the friction factor for helical coils, which depends on the flow regime and the curvature of the helix. L,  $d_i$  and u are fixed values and denote, the membrane length, inner diameter and the superficial velocity within the membrane, respectively. The fluid density  $\rho$  is either constant for incompressible fluids such as oxygen-saturated water or calculated with the ideal gas law for gases. Thus, the gas density is a function of the coordinate z due to the pressure loss.

$$\rho = M_{fluid} \frac{p(z)}{RT} \tag{4.59}$$

An iterative procedure with p=1 atm  $\forall z$  as starting value gives  $p(m*\Delta z)$  and  $\rho(m*\Delta z)$  for every grid nod along the membrane. The partial pressure of oxygen in the inner membrane bulk is obtained from the absolute pressure and the mole fraction of oxygen within the gas. The partial pressure of oxygen at the membrane wall  $p_{ox}|_{r_o}$  is expected to be lower due to oxygen losses as result of diffusion through the membrane. Empirical correlations for convective mass transfer are used to relate  $p_{ox}|_{r_o}(z)$  to p(z):

$$Nu = f(Re, Pr) \rightarrow Sh = f(Re, Sc) \tag{4.60}$$

The convective heat transfer is calculated with a Nusselt correlation as explained above, which depends on the flow regime, the Reynolds number and the Prandtl number. The Colburn

analogy between heat and mass transfer is used to derive the Sherwood number, which relates convective mass transfer to diffusive mass transfer, from the Nusselt number and finally obtain the convective mass transfer coefficient.

 $p_{ox}|_{r_o}(z)$  is calculated with the mass balance for the membrane:

$$-J_{diff,i,mf} = J_{conv,i,om} \tag{4.61}$$

$$-\frac{2\pi D_{ox,m}L}{\ln\left(\frac{r_o}{r_m}\right)M_{ox}}\left(c_{ox}|_{r_o}-c_{ox}\mid r_m\right) = -\frac{2\pi D_{ox,m}L}{\ln\left(\frac{r_o}{r_m}\right)M_{ox}}\left(H_{cp}^{ox}p_{ox}\Big|_{r_o}-c_{ox}|_{r_m}\right) = \frac{k_{conv,ox,m}A}{RT}\left(p_{ox}|_{r=0}-p_{ox}|_{r_o}\right)$$

$$= \frac{k_{conv,ox,m}2\pi r_oL}{RT}\left(p_{ox}|_{r=0}-p_{ox}|_{r_o}\right)$$

$$(4.62)$$

$$\Leftrightarrow p_{ox} \mid r_o = \left\lceil \frac{\frac{2\pi D_{ox,m}L}{\ln\left(\frac{r_o}{r_m}\right)M_{ox}} c_{ox} \mid r_m - \left(\frac{k_{conv,0x,m}2\pi r_oL}{RT} * p_{ox}\right|_{r=0}\right)}{\frac{2\pi D_{ox,m}L}{\ln\left(\frac{r_o}{r_m}\right)} H_{cp}^{ox} - \frac{k_{conv,ox,m}2\pi r_oL}{RT}}\right\rceil$$
(4.63)

$$\Leftrightarrow c_{ox}|_{r_o} = H_{cp}^{ox} \left[ \frac{\frac{D_{ox,m}}{\ln(\frac{r_o}{r_m})M_{ox}} c_{ox}|_{r_m} - \left(\frac{k_{\text{conv},0x,m}r_o}{RT} * p_{ox}|_{r=0}\right)}{\frac{D_{ox,m}}{\ln(\frac{r_o}{r_m})} H_{cp}^{ox} - \frac{k_{conv,ox,m}r_o}{RT}} \right]$$
(4.64)

Since this expression depends on  $c_{ox}|_{r_m}$ , a part of the solution for internal nods, which depends on the boundary conditions, again an iterative procedure is necessary to solve the equation.

#### Solving model equations

Matlab R2019a® was used to model the above-mentioned equations. Since a PDE with solution  $c_i = f(r,z)$  cannot be solved analytically, a numerical method needs to be applied. Finite difference method (FDM) in 2D and cylindrical coordinates was chosen as there is no need to include unequal grid cell sizes (finite element method), but reactions are important ( $\nabla c_i \neq 0$ , thus the finite volume method is not suitable). [14,123] According to FDM, a grid pattern of suitable resolution is applied to each layer element (see Fig. 4.7).

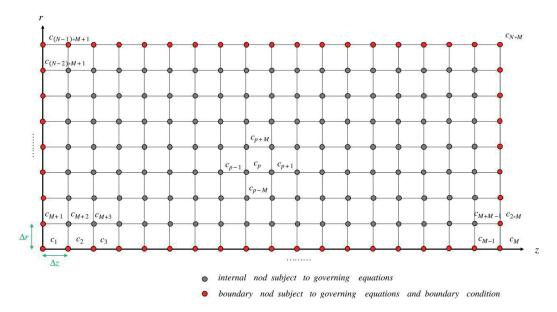


Figure 4.7: Grid system applied for finite difference method. A coordinate transformation of the form  $c_{ij} \rightarrow c_{(j-1)*M+i} = c_P$  is necessary to reduce the index to one variable. [14] Otherwise, it is impossible to address a certain element in the matrix/vector structure of the numerical solution procedure. The red nods are subject to governing equations and boundary conditions whereas the inner nods (grey) only are subject to the governing equations. Note that the coordinate system is still of cylindrical nature and the grid cell size is not constant.

The concept of FDM relies on the negligible impact of grid cells, which are far distant to the examined grid cell. Thus, the PDE can be discretized for each grid cell by means of the Taylor series expansion. The discretized forms of dr and dz,  $\Delta r$  and  $\Delta z$ , respectively, correspond to the dimension of one grid cell. The degree of the Taylor series expansion defines the number of neighboring cells, which are not neglected. A  $1^{st}$  order Taylor series expansion only includes the directly neighbored elements in r- and z-direction. This leads to an error term, which is proportional to  $\Delta r^2$  and  $\Delta z^2$ , respectively. Higher order Taylor series expansion decrease the error further because the  $2^{nd}$  and further rows of neighboring elements are included. Thus, an infinite Taylor series expansion would result in the analytical solution considering the impact of each grid cell on every other grid cell. Applying  $1^{st}$  order Taylor series expansion to a defined number of grid cells leads to a set of algebraic equations, which include mass transfer and all kinetics of the system.

Eq. 4.71 shows exemplarily the result of a discretization (eqs. 4.67 - 4.70) of a concentration profile (eqs. 4.65 & 4.66) within the biofilm. Diffusion is the dominating mass transfer, and a  $1^{st}$  order reaction is added for illustrating purposes. [123]

$$\frac{\partial c_i}{\partial t} = \nabla \left( D \nabla c_i \right) + v_{i,j} \tag{4.65}$$

Assuming steady-state, isotropic diffusion coefficient and first order reactions:

$$0 = D\Delta c_i + k_{i,j}c_i \Leftrightarrow 0 = D\left[\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial c_i}{\partial r}\right) + \frac{1}{r^2}\frac{\partial^2 c_i}{\partial \varphi^2} + \frac{\partial^2 c_i}{\partial z^2}\right] + k_{i,j}c_i \tag{4.66}$$

Applying rotational symmetry:

$$0 = 2\pi D \left[ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial c_i}{\partial r} \right) + \frac{\partial^2 c_i}{\partial z^2} \right] + k_{i,j} c_i = 2\pi D \left[ \frac{1}{r} \left( \frac{\partial c_i}{\partial r} + r \frac{\partial^2 c_i}{\partial r^2} \right) + \frac{\partial^2 c_i}{\partial z^2} \right] + k_{i,j} c_i = 2\pi D \left[ \frac{1}{r} \frac{\partial c_i}{\partial r} + \frac{\partial^2 c_i}{\partial r^2} + \frac{\partial^2 c_i}{\partial r^2} + \frac{\partial^2 c_i}{\partial r^2} \right] + k_{i,j} c_i = 2\pi D \left[ \frac{1}{r} \frac{\partial c_i}{\partial r} + \frac{\partial^2 c_i}{\partial r^2} + \frac{\partial^2 c_i}{\partial r^$$

Discretization with a truncated Taylor series expansion (m,n define the node in z-/r-direction with M and N nodes in total per direction) yields:

$$0 = 2\pi D \left[ \frac{c_{i,m,n+1} - c_{i,m,n-1}}{2r_n \Delta r} + \frac{c_{i,m,n+1} - 2c_{i,m,n} + c_{i,m,n-1}}{(\Delta r)^2} + \frac{c_{i,m+1,n} - 2c_{i,m,n} + c_{i,m-1,n}}{(\Delta z)^2} \right] + k_{i,j} c_{i,m,n}$$
(4.68)

With 
$$r_n = r_i + (n-1)\Delta r$$
:  

$$0 = 2\pi D \left[ \frac{c_{i,m,n+1} - c_{i,m,n-1}}{2r_n\Delta r} + \frac{c_{i,m,n+1} - 2c_{i,m,n} + c_{i,m,n-1}}{(\Delta r)^2} + \frac{c_{i,m+1,n} - 2c_{i,m,n} + c_{i,m-1,n}}{(\Delta z)^2} \right] + k_{i,j}c_{i,m,n}$$
(4.69)

$$0 = \left[ \left( \frac{-2 * 2\pi D}{(\Delta r)^2} + \frac{-2 * 2\pi D}{(\Delta z)^2} \right) + k_{i,j} \right] c_{i,m,n} + \frac{2\pi D}{(\Delta z)^2} c_{i,m+1,n} + \frac{2\pi D}{(\Delta z)^2} c_{i,m-1,n} + \left( \frac{2\pi D}{(\Delta r)^2} + \frac{2\pi D}{2 (r_i + (n-1)\Delta r) (\Delta r)} \right) c_{i,m,n+1} + \left( \frac{2\pi D}{(\Delta r)^2} - \frac{2\pi D}{2 (r_i + (n-1)\Delta r) (\Delta r)} \right) c_{i,m,n-1}$$

$$(4.70)$$

Transforming the coordinate system (Fig. 4.7) to obtain single indices for numerical processing gives:

$$0 = \left[ \left( \frac{-2 * 2\pi D}{(\Delta r)^2} + \frac{-2 * 2\pi D}{(\Delta z)^2} \right) + k_{i,j} \right] c_{i,p} + \frac{2\pi D}{(\Delta z)^2} c_{i,p+1} + \frac{2\pi D}{(\Delta z)^2} c_{i,p-1}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} + \frac{2\pi D}{2\Delta r \left[ r_i + f \log \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p+M}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} - \frac{2\pi D}{2\Delta r \left[ r_i + f \log \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p-M}$$

$$(4.71)$$

floor((p-1)/M) rounds p/M to the next smaller integer.

The central difference approach does not work for left/right boundary because there is no neighboring nod in one direction. Thus, two time forward/backward Taylor series expansion

was applied for the left and right boundary since no boundary condition is given for the boundaries at z=0 and z=L except for the inner membrane phase (eqs. 4.72 & 4.73).

$$0 = 2\pi D \left[ \frac{c_{i,m,n+1} - c_{i,m,n-1}}{2r_n \Delta r} + \frac{c_{i,m,n+1} - 2c_{i,m,n} + c_{i,m,n-1}}{(\Delta r)^2} + \frac{c_{i,m+2,n} - 2c_{i,m+1,n} + c_{i,m,n}}{(\Delta z)^2} \right] + k_{i,j}c_{i,m,n}$$

$$0 = \left[ \left( \frac{-2 * 2\pi D}{(\Delta r)^2} + \frac{2\pi D}{(\Delta z)^2} \right) + k_{i,j} \right] c_{i,p} - \frac{2 * 2\pi D}{(\Delta z)^2} c_{i,p+1} + \frac{2\pi D}{(\Delta z)^2} c_{i,p+2}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} + \frac{2\pi D}{2\Delta r \left[ r_i + f \log r \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p+M}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} - \frac{2\pi D}{2\Delta r \left[ r_i + f \log r \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p-M}$$

$$(4.72)$$

$$0 = 2\pi D \left[ \frac{c_{i,m,n+1} - c_{i,m,n-1}}{2r_n \Delta r} + \frac{c_{i,m,n+1} - 2c_{i,m,n} + c_{i,m,n-1}}{(\Delta r)^2} + \frac{c_{i,m-2,n} - 2c_{i,m-1,n} + c_{i,m,n}}{(\Delta z)^2} \right] + k_{i,j}c_{i,m,n}$$

$$0 = \left[ \left( \frac{-2 * 2\pi D}{(\Delta r)^2} + \frac{2\pi D}{(\Delta z)^2} \right) + k_{i,j} \right] c_{i,p} - \frac{2 * 2\pi D}{(\Delta z)^2} c_{i,p-1} + \frac{2\pi D}{(\Delta z)^2} c_{i,p-2}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} + \frac{2\pi D}{2\Delta r \left[ r_i + f \log \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p+M}$$

$$+ \left( \frac{2\pi D}{(\Delta r)^2} - \frac{2\pi D}{2\Delta r \left[ r_i + f \log \left( \frac{p-1}{M} \right) \Delta r \right]} \right) c_{i,p-M}$$

$$(4.73)$$

All equations presented in the "set up of model equations" subsection were discretized accordingly. Also, the above-mentioned boundary conditions were discretized accordingly. However, the obtained set of discretized governing equations and discretized boundary conditions cannot be solved directly due to interdepences of the equations. For example, the oxygen uptake rate of T. reesei for maintenance metabolism influences the local oxygen concentration and depends on the concentration of fungal biomass, which itself depends on the local oxygen concentration. Thus, the system is solved by means of iteration. For each species, the arithmetic mean between initial bulk concentration and initial concentration in the inner membrane is chosen as initial value for the oxygen concentration of every volume element. Each run of the iteration gives a new solution for the local concentration of species i in each volume element. The solution vector is used as initial value set for the next iteration and then is overwritten by the new solution. The termination criterion for the iteration is a certain relative error threshold. To compute the relative error, the solutions of all included neighboring elements  $c_{k-1}$ ,  $c_{k+1}$ ,  $c_{k-M}$  and  $c_{k+M}$  of the examined cell  $c_k$  are plugged into the discretized equation of cell k. This gives a solution for  $c_k$ , which is different from the solution  $c_k$  in the solution vector. A relative error is calculated from these two values of  $c_k$ . As soon as the relative error comes under a certain threshold (0.1 % rel. error in this work), the termination criterion for the iteration is fulfilled. Since the convergence of the iteration is limited by the grid resolution, a suitable

grid resolution is needed for the corresponding iteration termination criterion (a 183x180 mesh converged to 0.1 % rel. error with 833 iterations).

#### Model simulations

Fig. 4.8 shows the 2D concentration profile for oxygen for the steady-state condition depicted in Fig. 3.7. The two discontinuities reflect the equilibrium at the phase boundaries gas-PDMS & PDMS-liquid defined by the partition coefficients of oxygen. The mass transfer limitation of the convective boundary layer at the inner membrane wall and the outer biofilm was found to be negligible, since large variations of the Reynolds number did not affect the convective mass transfer.

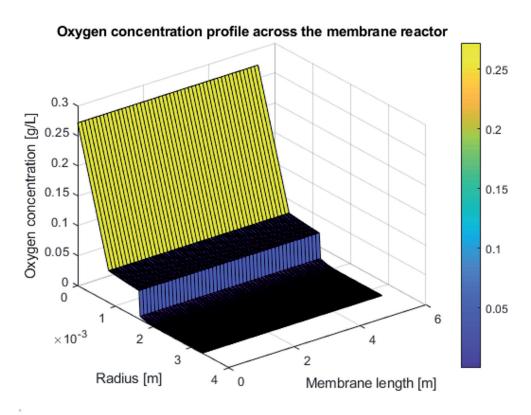


Figure 4.8: Simulated oxygen profile for the standard membrane ( $d_i$ = 1.58 mm,  $d_o$ = 3.18 mm, L= 5.6 m). Even at low Reynolds numbers in the membrane (Re= 306.5), z-gradient of the system is almost negligible. The two discontinuities reflect the partition coefficients of oxygen for gas, PDMS and water.

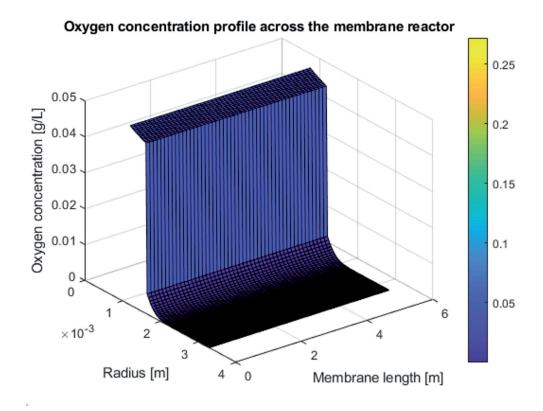


Figure 4.9: Oxygen profile within the biofilm for the standard membrane ( $d_i$ = 1.58 mm,  $d_o$ = 3.18 mm, L= 5.6 m). The detailed view demonstrates the curvature of the oxygen profile as a result of the tubular system.

The logarithmic curvature due to the cylindrical membrane reflected by  $\frac{c_{i,m,n+1}-c_{i,m,n-1}}{2r_n\Delta r}$  in the discretization equation becomes clearly visible in the detailed view (Fig. 4.9). Furthermore, the z-gradient is almost negligible for the validation procedure. Oxygen shows the highest variance in z with a maximum of 0.3 % over the membrane length (Fig. 4.10), which is lower than the maximum numerical error of the model. Thus, the following graphs will be shown in 2D at z=0 for illustration purposes.

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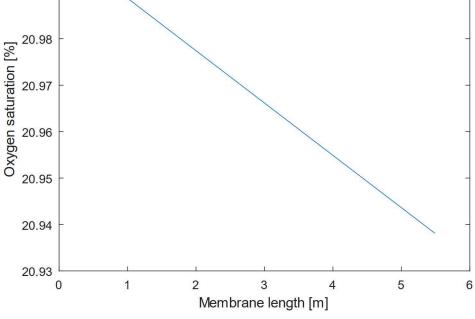


Figure 4.10: Oxygen profile along z-axis for the standard membrane ( $d_i$ = 1.58 mm,  $d_o$ = 3.18 mm, L=5.6 m). The oxygen saturation within the membrane changes by 0.3 % over the length, which is lower than the maximum numerical error of the model.

In order to fit the simulation outcome with the experiments of continuous CBP (chapter 3), the enzyme synthesis constant of *T. reesei* and the effective diffusivity of  $\beta$  – *glucosidase* were fitted within a range of 20 % - 100 % of the reported literature values (Fig. B.1). [10,124,125] It was assumed that these two parameters were affected the most by the change of bubble aerated batch suspension to immobilized membrane aerated biofilm formation during continuous operation. [10] Best agreement with the continuous results could be achieved by reduction of ca. 40 % (0.67  $\frac{FPU}{mL*d}$  vs 1.152  $\frac{FPU}{mL*d}$  ) in enzyme production rate and a ca. 20 % reduced diffusivity of  $\beta$ -glucosidase compared to endoglucanase and cellobiohydrolase. The reduced diffusivity of  $\beta$ -glucosidase results in higher  $\beta$ -glucosidase concentrations in the biofilm ans thus, accounts for the affinity of  $\beta$ -glucosidase to attach to the cell wall. The cell wall attachement of  $\beta$ -glucosidase could not be modeled with an adsorption equilibrium due to a lack of available data for the adsorption constants. The modeled ethanol concentration across all layers in the  $1^{st}$  reactor of the steady-state presented in 3.7 shows a deviation of 3.5 % compared to the validation parameter (Fig. 4.11).

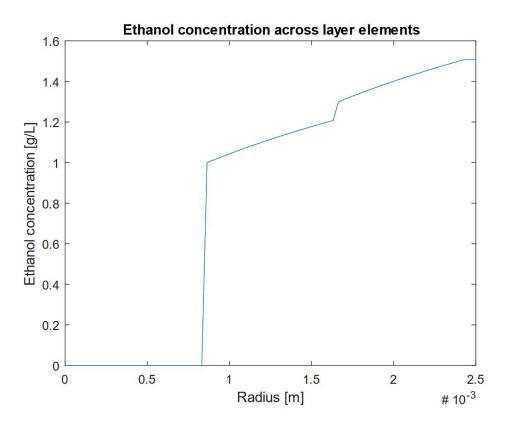


Figure 4.11: Ethanol profile along r-axis (z=0) over all layer elements for the standard membrane ( $d_i$ = 1.58 mm,  $d_o$ = 3.18 mm, L= 5.6 m). The ethanol concentration at the right corresponds to the modeled bulk ethanol concentration of 1.51  $\frac{g}{L}$ , which has a 3.5 % deviation from the experimental value.

Having the model fitted to the continuous experiments at lab scale allows to examine low yields of the continuous experiments although  $k_L$ a was kept constant or even increased. Fig. 4.12 & 4.13 show the microbial growth rate as function of the radial coordinate in the fungal biofilm for 21 % and 42 % oxygen concentration. Since T. reesei growth is either limited by glucose or by oxygen, the optimum growth rate is achieved, where both limitations are equal. Given a higher mass transfer of oxygen per membrane area allows to grow a thicker biofilm (Fig. 4.12), which is not per se beneficial. On the one hand, there is more volume and thus, more production capacity. On the other hand, a thicker biofilm would extend the distance between glucose saturation and oxygen saturation (the dashed line from Fig. 4.12 moves to the right in Fig. 4.13). Thus, the activity decreases. Furthermore, thicker biofilms cause the problem of glucose-depleted, but oxygen-enriched zones (red circles in Fig. 4.13), where ethanol degradation by T. reesei increases by a factor of ca. 3, which was already discussed (section 3).

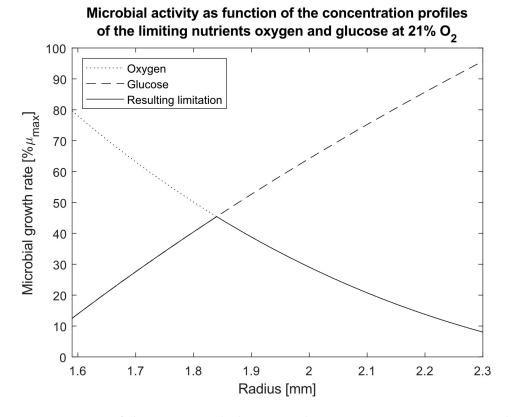


Figure 4.12: Projection of the oxygen and glucose gradient at z=0 as projection in the z-plane. Depending on the position in the fungal biofilm, either glucose or oxygen is the limiting nutrient. The maximum growth rate of ca. 45 %  $\mu_{\text{max}}$  is reached at a distance of ca. 0.25 mm from the membrane surface for the standard membrane ( $d_i$ = 1.58 mm, $d_o$ = 3.18 mm,L= 2.8 m) at an oxygen concentration of 21 %.

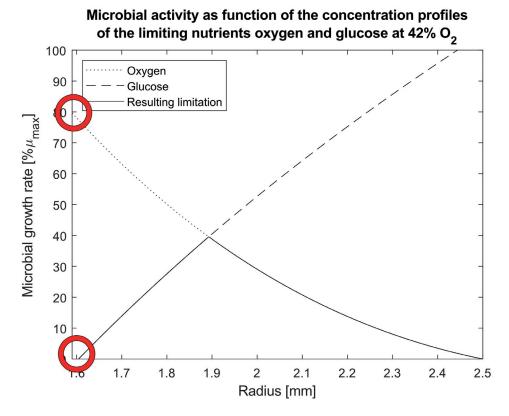


Figure 4.13: Projection of the oxygen and glucose gradient at z=0 as projection in the z-plane. Depending on the position in the fungal biofilm, either glucose or oxygen is the limiting nutrient. The maximum growth rate of ca. 40 %  $\mu_{\rm max}$  is reached at a distance of ca. 0.32 mm from the membrane surface for the standard membrane ( $d_i$ = 1.58 mm, $d_o$ = 3.18 mm,L= 2.8 m) at an oxygen concentration of 42 %. The red circles denote glucose-depletd, but oxygen-enriched zones in the fungal biofilm, where T. resei degrades high amounts of ethanol (Fig. 3.6)

Fig. 4.14 summarizes the optimization problem. Increasing the fungal biofilm thickness (e.g. by a higher oxygen gradient or by a thinner membrane) causes a squared increase of the volume of the fungal biofilm (dashed line in Fig. 4.14). The microbial performance is proportional to the volume of the fungal biofilm (eq. 4.74).

$$P \propto V_f \propto \delta_f^2 \tag{4.74}$$

However, the shortage of the nutrient supply due to longer diffusion paths increases logarithmically due to the cylindrical geometry of the membrane (dotted line in Fig. 4.14) (eq. 4.75)

$$P \propto \frac{1}{\ln\left(\delta_f\right)} \tag{4.75}$$

As the logarithm outweighs the polynome for high  $\delta_f$ , but not for short  $\delta_f$ , an optimum fungal biofilm thickness of 1.5 mm is found for the standard membrane ( $d_i$ = 1.58 mm,  $d_o$ = 3.18 mm, L= 2.8 m) (solid line Fig. 4.14). Since  $\delta_f$  contains information about the benefits of high-volume biofilms as well as the disadvantages of long diffusion paths, it seems to be a promising scale-up parameter.

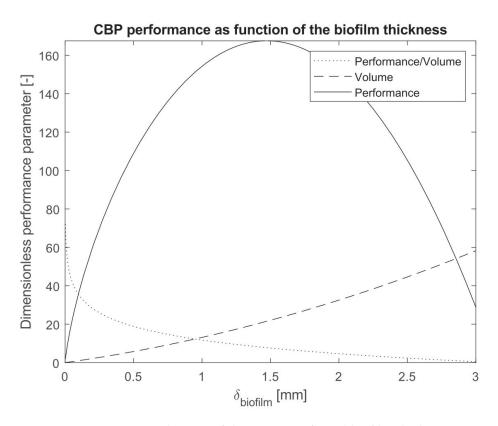


Figure 4.14: Evaluation of the optimum fungal biofilm thickness

#### Biofilm measurement

As the fungal biofilm thickness was identified as critical parameter for the CBP performance, but did not belong the set of validation parameters, a batch experiment at the same conditions was conducted to grow a biofilm of comparable thickness. After 9 d of batch CBP operation, the reactor was harvested and the biofilm thickness was measured. The membrane support was mounted on a CNC apparatus (Fig. 4.15) and and the biofilm was punctuated with a needle (Fig. 4.16), which was connected to a multimeter measuring the resistance at the needle tip. As the conductivity is the reciprocal of the resistance, the needle showed low conductivity & high resistance in the air and in the membrane, but high conductivity and low resistance within the biofilm, which consists of 85 % water with dissolved salts.

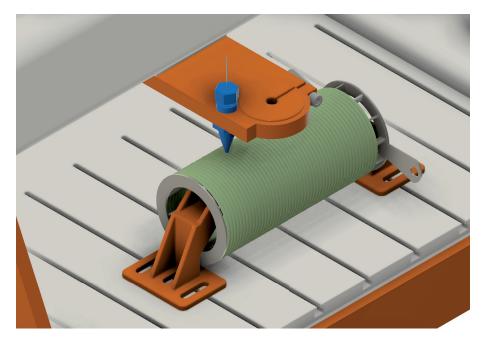


Figure 4.15: 3D view of the experimental apparatus to measure the biofilm thickness by measuring the conductivity at the tip of a needle punctuating the biofilm. (CAD created by S. Bowald)

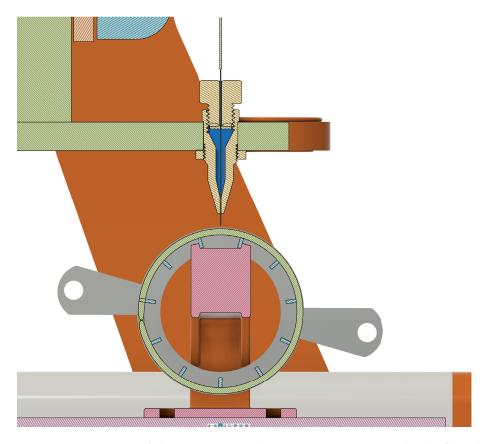


Figure 4.16: Cross-section view of the experimental apparatus to measure the biofilm thickness by measuring the conductivity at the tip of a needle punctuating the biofilm. (CAD created by S. Bowald)

The decrease in resistance from air to biofilm is discontinuous, whereas the increase in resistance from the biofilm to the membrane occurs slowly due to slight membrane deformation by the needle pressure (Fig. 4.17). In order to determine the boundary between the biofilm and the membrane properly, the biofilm was considered to end at that point, where the resistance is beyond a  $4\sigma$  confidence interval around the average resistance of the biofilm. Since a  $4\sigma$  confidence interval captures 99.4 % of the Gaussian normal distribution, the probability is sufficiently high, that a resistance outside of the confidence interval is rather due to membrane deformation than statistical uncertainty.

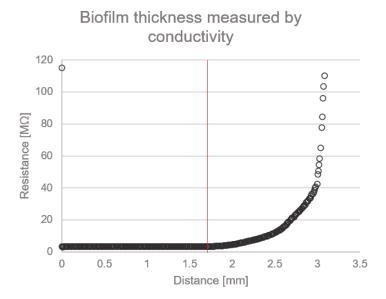


Figure 4.17: Resistance at the needle tip over the distance of punctuation. The decrease in resistance from air to biofilm is discontinuous, whereas the increase in resistance from the biofilm to the membrane occurs slowly due to slight membrane deformation by the needle pressure. The red line marks the end of the  $4\sigma$  confidence interval of the average biofilm resistance

The measured biofilm thickness (triangle markers in Fig. 4.18) of  $\delta_f = 1.7 \pm 0.35$  mm on average (solid line in Fig. 4.18) shows a deviation of ca. 12% to the model result (dashed line in Fig. 4.18). Given the difference in the setup (eg. batch vs. continuous), the model results regarding the biofilm thickness may be regarded as plausible.

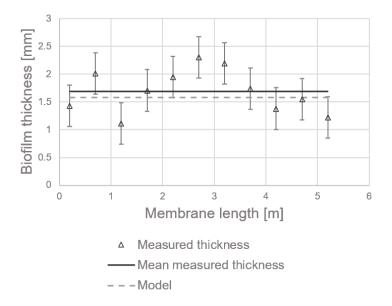


Figure 4.18: The measured biofilm thickness (triangle markers) of  $\delta_f = 1.7 \pm 0.35$  mm on average (solid line) shows a deviation of ca. 12% to the model result (dashed line)

### 4.4 Conclusion

A rigorous process model was developed for continuously operated consolidated bioprocessing of cellulose to ethanol. 9 species were considered (oxygen, glucose, T. reesei, secondary mycelia of T. reesei, enzymes, cellulose, cellobiose, yeast density and ethanol). 8 of these 9 species (each except cellulose) are present in the biofilm and thus, needed to be modelled spatially resolved in order to account properly for mass transfer limitations. The fungal biofilm thickness  $\delta_f$  was found to be a critical parameter with an optimum for every membrane configuration. Smaller  $\delta_f$  reduced the fungal biofilm volume and thus, the enzyme production unnecessarily and larger  $\delta_f$  increased the diffusion path length and caused shortage in nutrient supply as well as lower enzyme concentrations in the bulk. The results of the model were able to explain the different productivities observed in the continuous experiments. The enzyme synthesis rate of the secondary mycelia and the effective diffusivity of  $\beta$ -glucosidase  $D_{BG,eff}$  were used as fitting parameter of the model. A reduction of ca. 40 % (0.67  $\frac{FPU}{mL*d}$  vs 1.152  $\frac{FPU}{mL*d}$ ) in enzyme activity and ca. 20 % (5\*10<sup>-11</sup>  $\frac{m^2}{s}$  vs 4\*10<sup>-11</sup>  $\frac{m^2}{s}$ ) reduced effective diffusivity of  $\beta$ -glucosidase compared to batch models yielded agreement with the continuous experiments. The fitting of these two parameters allowed for less than 0.5 % numerical error of model iterations and less than 15 % deviation of experimental results (validation parameters) and model results. Furthermore, an experimental proof-of-concept for the plausibility of the model results regarding the fungal

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biofilm thickness  $\delta_f$  was conducted. The fully validated rigorous process models allows to run optimization simulation for the best performing experimental setup at higher scales.

# CHAPTER 5

Scale-up of a 2.7 L laboratory scale consortium-based consolidated bioprocess to 130 L pilot scale

#### 5.1 Abstract

The scale-up of innovative reactor concepts, which could enable bio-based bulk chemicals to replace their fossil-based counterparts, progresses slowly. The heterogeneity of the biological system often causes performance decrease at higher scales and thus, accentuate the lack of economic competitiveness against fossil-based pendants. It was aimed to combine the systematic scale-up approach of non-dimensionalizing the mathematical problem and requesting non-dimensional similarity with the simulation outcome of a rigorous process model in order to scale up a membrane aerated biofilm reactor to produce lignocellulosic ethanol employing consolidated processing. It became clear, that the simulation effort may be reduced significantly by identifying design trade-offs with a basic, systematic approach such as non-dimensionalizing the problem and resolving only the critical design constraints with a highly differentiated model. Whenever the the design constraints were overspecified, the minimum selling price was used as optimization criterion to minimize production costs. Regarding the final results, it was distinguished between an industrial favorable solution and an academically feasible solution to experimentally prove the scale-invariance of the model at 130 *L* pilot scale.

## 5.2 Introduction

The scale-up of bioprocesses is gaining attention as governments around the globe realize the urgent need to promote industrial biotechnology as sustainable alternative to the fossil-based industry in the framework of a bio-based economy. [8,126] However, especially for low-margin

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products such as bulk chemicals, the obstacles of scaling up a bioprocess (heterogeneity of microbial and plant biomass, mechanical and chemical sensitivity of cells etc.) paired with a lack of economic competitiveness of the bioprocess hinder wide-range implementation. [127–129] Ethanol, being produced from biomass to a large extent (share of bioethanol was 95 % in 2007 and increasing ever since [130, 131]), is an exception in this context. However, the production of bioethanol from direct fermentation of sugar crops or the cleavage of starch with amylases and subsequent fermentation is very "scale-up-friendly". The fermentation of sugars to ethanol with S. cerevisiae is known for several thousands of years and conducted under reproducible conditions at large scale since the 1930s. [132] Besides the advantage through extensive experience, the fermentation occurs under anoxic conditions resp. the respiratory genes of a Crabtree-positive yeast such as S. cerevisiae are repressed by the high glucose concentrations, and thus, the most difficult challenge in most bioprocesses, the oxygen supply of the microbes, is not an issue. [133] However, the above-mentioned scale-up obstacles become relevant again, when replacing 1<sup>st</sup> generation bioethanol resources such as corn and sugar crops with non-edible 2<sup>nd</sup> generation bioethanol resources like lignocellulose, the most abundant organic carbon source in world, in order to avoid ethical conflicts as well as the hidden CO<sub>2</sub> footprint of 1st generation bioethanol resources due to land clearing measures or the use of fertilizers. [29, 134, 135] The economic competitiveness of 2<sup>nd</sup> generation bioethanol was addressed by many researches and CBP was identified as largest lever to reduce costs. [3,33] CBP denotes the highest degree of process intensification, where enzyme production, enzymatic hydrolysis of the cellulose and fermentation of the sugars to ethanol is conducted in one process step. [4]

In chapter 2, it was shown, that the cost savings by continuously operated CBP allow for profitable 2<sup>nd</sup> generation biofuel production in the EU, but not in the US without applying an additional cost saving approach such as calculating with slightly lower returns on capital investment. [33] However, the cost savings of 27.5 % by applying continuously operated CBP are unmatched making it the most promising concept for large-scale production of  $2^{nd}$  generation bioethanol. [33] Since continuous operation demands long-term stability and robustness, a CBP approach with an industrial microbial consortium was preferred over a genetically modified "super-bug". [34] In chapter 3 the proof-of-concept was delivered, that continuous CBP may be operated with a consortium of industrial microbes. The microbial community consisting of an aerobic enzyme producing filamentous fungus T. reesei and a facultative anaerobic single-celled fermenting organism S. cerevisiae is kept stable by assigning a niche for each species. The oxygen-enriched layer around a tubular, aerated membrane is the niche for *T. reesei*, whereas the oxygen-depleted zones in the reactor (outer biofilm layer and bulk suspension) are populated by S. cerevisiae. [4] Theoretically, S. cerevisiae could invade the niche of T. reesei and does likely to a minor extent (Chapter 4). However, the system stabilizes itself according to mechanisms of a "cheater-cooperator"-community. [34] S. cerevisiae, which cannot digest

cellulose, relies on the enzyme production of T. reesei to depolymerize cellulose and thus, an equilibrium is formed. It becomes clear, that mass transfer between the two niches is of central importance for the process. Therefore, a detailed rigorous process model was developed (Chapter 4) to enable model-based scale-up. However, the process model does not give direct insight about the relevance of certain design trade-offs, which have to be resolved at higher scales (e.g. maintaining the solid-liquid mixing behavior vs. maintaining the flow field and thus, the boundary layer thickness). Only extensive simulation efforts of all design trade-offs would reveal the critical constraints. Therefore, the starting point of scale-up consideration is the similarity-paradigm. [136] According to the Buckingham-Π theorem, all relevant design parameters can be reduced to a set of dimensionless numbers, which needs to be kept constant for similar performance at model scale and technical scale. [136,137] As the similarity paradigm has known weaknesses (e.g. for surface-related processes [8,127]), the critical constraints are not solved by simply requesting similarity, but are addressed with simulations of the rigorous process model. Concluding, it can be stated, that the similarity paradigm is used as systematic approach to classify the severeness of the different design constraints, which reduces the computational effort. The critical parameters are scaled-up with the help of a rigorous process model.

With this procedure, the presented work aims to provide a reliable scale-up guideline for continuously operated, consortium-based CBP based on both, general scale-up laws and the simulation results of the rigorous process model, which was adjusted to any necessary design changes. A continuous experiment at 130 L pilot scale should confirm the results obtained from scale-up laws and the process model to validate both, the scale-up laws and the adjustments of the process model. Furthermore, implications with the techno-economic model have to be considered since the overall goal is to deliver a case for profitable  $2^{nd}$  generation ethanol production from lignocellulose at large scales.

#### 5.3 Results and Discussion

The goal of a scale-up design in general is to maintain the process performance (yield, titer, residence time) while increasing the size of the apparatus. [138] However, this principle assumes a perfectly optimized small scale system, which does not hold for the laboratory scale setup presented in section 3.3. On the one hand this is due to limited resources in a lab environment and most important, on the other hand continuous CBP operation is a time-consuming and challenging task (Chapter 3). The design of the continuous CBP apparatus was designed to minimize the risk of failure instead of aiming at maximum productivities. Therefore, the state of optimization of laboratory scale CBP needs to be discussed before advancing to the scale-up considerations. pH and temperature were optimized regarding the enzyme production of *T*.

reesei. [4] The volume flow rate within the membrane was optimized with respect to a minimum convective mass transfer limitation. [89] However, the membrane dimensions with respect to the liquid reactor volume (inner diameter  $d_i$ , outer diameter  $d_o$  & length L), the oxygen concentration within the membrane  $c_{ox}$ , the feed cellulose concentration  $c_{in}$  and the residence time  $\tau$  were not optimized towards maximum ethanol output. These six parameters form the degrees of freedom (DoF) for the scale up since there is no point in demanding similarity of non-optimized parameters from the laboratory setup. In section 4.3, it was found that there is an optimum biofilm thickness  $\delta_f$  for each pair of oxygen concentration at the outer membrane surface and glucose concentration within the bulk. Designing the scaled-up system for an optimum biofilm thickness reduces the number of DoFs by two: The oxygen concentration at the outer membrane surface depends on the oxygen concentration within the membrane and the membrane surface depends on the oxygen concentration within the membrane and the membrane thickness. Thus, only two parameters of  $d_i$ ,  $d_o$  &  $c_{ox}$  can be chosen freely. The third is given by  $\delta_f$ .

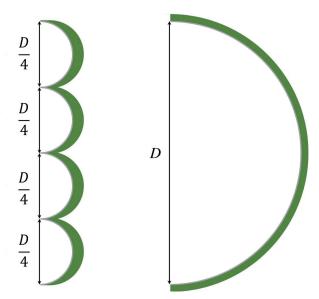


Figure 5.1: Schematic representation of the the biofilm growth (green) on one large membrane (right) and n multiple small membranes (left). n = 4 was chosen solely for illustration purposes.

Fig. 5.1 depicts the different setup of a membrane with small diameter versus a membrane with a large diameter. Given a certain space available for the membrane winding, the membrane surface per winding height  $h_w = D$  is independent of the membrane (eq. 5.1) or rather in favor of the large membrane, where less membrane area is lost due to contact of the upper and lower membrane in the winding. However, the biofilm volume growing on the small membrane with a certain thickness  $\delta$  is always larger than the biofilm volume growing on a large membrane (eq. 5.2). Theoretically  $\lim_{n \to \infty} n \to \infty$  would be the optimum solution. However, other factors

such as pressure loss and the oxygen gradient along the membrane shift the optimum towards lower n.

$$A_{\rm m} = L\frac{\pi}{2}D = nL\frac{\pi}{2}\frac{D}{n} \tag{5.1}$$

$$V_{bf,D} = L\pi \left[ \left( \frac{D}{2} + \delta \right)^2 - \frac{D^2}{2} \right] = L\pi \left( \delta^2 + D\delta \right) < V_{bf,D/n} = nL\pi \left[ \left( \frac{D}{2n} + \delta \right)^2 - \frac{D^2}{2n} \right] = L\pi \left( n \times \delta^2 + D\delta \right)$$
(5.2)

The same reduction of DoFs holds for the glucose bulk concentration, which depends on the cellulose conversion. The membrane length L influences the enzyme loading in the bulk and thus, the speed of cellulose conversion to glucose as well as the titer, by determining the total biofilm volume.  $\tau$  defines the time for cellulose conversion and  $c_{in}$  determines the maximum available substrate for conversion. Again, only two of the parameters may be chosen freely, whereas the third is given by the optimization for  $\delta_f$ . With respect to the glucose concentration, it makes sense to define L and  $c_{in}$  instead of  $\tau$  as it was shown in chapter 2, that  $\tau$  has a very low impact on the production costs.

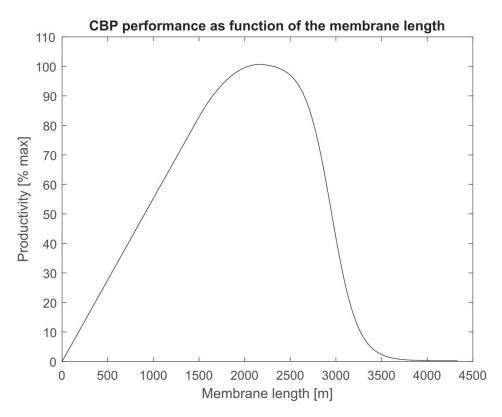


Figure 5.2: Model results of the productivity  $\frac{g_{EtOH}}{h}$  as function of the membrane length at standard conditions (membrane inner diameter  $d_i$ = 1.58 mm, membrane outer diameter, 21 % oxygen fraction within the membrane, 17.5  $\frac{g}{L}$  cellulose feed concentration the residence time  $\tau$  was 130 h) in the pilot scale system. The linear increase at the beginning is caused by the higher enzyme loading in the bulk as consequence of more biofilm volume without affecting the biofilm thickness  $\delta_f$  (chapter 4). The flattening of the curve with the subsequent strong decline in productivity is a result of the reduced bulk volume since a large fraction of the reactor is occupied with the membrane and the biofilm. Consequently, two factors are responsible for the decreasing productivity: First, a large fraction of the fed cellulose is necessary to maintain the biofilm. Second, the Dilution rate  $D = \tau^{-1}$  is defined by the nominal reactor volume. Therefore, the effective dilution rate of the bulk is higher, if a large fraction of the reactor is occupied by the immobilized biofilm. The higher dilution rate reduces the effective residence time of substrate and enzymes and thus, the cellulose conversion. The productivity reaches zero, when the whole reactor system is completely filled with the membrane and the biofilm and no bulk phase is left. Note: The presented calculations assume infinite available cellulose without any substrate inhibition effects in order to evaluate only the effect of the membrane length. At low solid loadings, the optimum is reached with less membrane length as there is no more cellulose to hydrolyze in the bulk. However, this "optimum" arises from a solid loading limitation (a parameter, which could be changed easily) instead of from reactor geometry constraints (parameters, which are difficult to change)

Given a experimentally confirmed yield of 40.3 % (section 3.4),  $c_{in}$  is not a limiting factor of the current setup. Evaluating the simulated ethanol productivity as function of the membrane

length (Fig. 5.2) reveals an optimum membrane length at around 2.2 km for the pilot scale reactor. At membrane lengths larger than 2.2 km, the model predicts lower productivities as a result of the reduced bulk volume since a large fraction of the reactor is occupied with the biofilm. Two factors are responsible for the decreasing productivity: First, a large fraction of the fed cellulose is necessary to maintain the biofilm. Second, the Dilution rate  $D = \tau^{-1}$  is defined by the nominal reactor volume. Therefore, the effective dilution rate of the bulk is higher, if a large fraction of the reactor is occupied by the immobilized biofilm. The higher dilution rate reduces the effective residence time and thus, the cellulose conversion. The productivity reaches zero, when the whole reactor system is occupied with biofilm and no bulk phase is left. However, this optimum of 2.2 km membrane length within a 130 L reactor is not feasible. Within a technically feasible range (e.g. 0-50 m), the productivity increases quasi-linear with the membrane length. The linear increase results from the linear increase in biofilm volume and thus, enzyme loading of the system, without affecting the biofilm thickness  $\delta_f$ .

Concluding, it can be stated that the available DoFs resulting from the not fully optimized laboratory scale cannot be resolved by optimizing the biofilm since the optima are found at the boundaries. As the optimization of whole system is too complex for an assessment with 4 DoFs, a classic approach of scale-up-theory is chosen to identify the critical design parameters for adjusting the DoFs: The scale-up is conducted by requiring similarity of all optimized parameters by aiming at geometric similarity, process similarity and physical similarity between small scale and large scale, respectively model scale and pilot scale in this work (see Tab. 5.1 for size comparison). [136] In order to properly account for the biology within the system, additionally the physical similarity is introduced. [136] Given this adjustment, the similarity concept promises good results because a lack of reproducibility at larger scale is mostly a consequence of cell sensitivity to poorly adjusted external parameters (e.g. mixing behavior) instead of the internal stochastic nature of gene expression. [8,139]

Table 5.1: Overview of the laboratory scale reactor and the pilot scale reactor dimensions

	Laboratory scale	Pilot scale
Reactor	Infors Labfors 5	Bioengineering P130
Volume	2.7 L	130 L
Height	0.18 m	0.975 m
Diameter	$0.14 \ m$	$0.412 \ m$

Since both reactors, the Labfors 5 (model scale; V = 2.7 L) and the Bioengineering P130 (pilot scale; V = 130 L), are cylindrical shaped, CSTRs, geometric similarity was achieved by installing the same type of stirrer and membrane support at pilot scale. Thus, the installed propeller mixer was replaced with a helical ribbon impeller at pilot scale and a membrane support

structure was installed allowing to wind a tubular membrane in helical shape. The exact design of the stirrer and the membrane support was defined by process similarity, which is discussed in the following. Process similarity is not as straightforward as geometric similarity because the reactor has three different zones (inside of the membrane, membrane & biofilm and the bulk phase), which underly different process conditions. The high degree of process integration with CBP yields exceptional cost savings but comes at the cost of much more difficulties when scaling the process. Universal optimization (e.g. saving the costs with an equally simplistic process design for scale-up) is not possible according to the "no free lunch"-theorem. [140] Process similarity in each of the reactor zones is achieved by keeping a certain set of dimensionless parameters, which reflect the process conditions, constant. This set of dimensionless parameters is obtained by applying the Buckingham-II—theorem. [137] By doing so, all relevant process parameters are grouped. The number of needed dimensionless parameters is equal to the number of relevant parameters subtracted by the number basic SI-units of the relevant parameter. For the inside of the membrane, the following group of dimensionless parameters is obtained (eq. 5.3):

$$\left\{p_{abs}\left[Pa = \frac{kg}{m * s^{2}}\right]; p_{O_{2}, \text{ wall }}\left[\frac{kg}{m * s^{2}}\right]; \dot{V}\left[\frac{m^{3}}{s}\right]; L[m]; d_{i}[m]; D_{O_{2}, m}\left[\frac{m^{2}}{s}\right]; \rho\left[\frac{kg}{m^{3}}\right]; \nu\left[\frac{m^{2}}{s}\right]\right\} - \left\{kg; m; s\right\}$$

$$= \begin{cases}
Re \\
Pe' = Re * Sc \\
Sh \\
\zeta \\
n_{O_{2}, \text{ wall}}
\end{cases} (5.3)$$

8 relevant parameters (absolute pressure, partial pressure of oxygen at the membrane wall, volumetric flow, length and inner diameter of the membrane, oxygen diffusivity in the membrane, density and kinematic viscosity of the fluid) minus 3 basic SI units (mass, length and time) yields 5 dimensionless parameters. Since the problems of pressure loss in a pipe, heat transfer from the inside of a hollow cylinder to its outside and the analogy between heat and mass transfer are well known, the obtained 5 dimensionless parameters are well-known and have given definitions (Tab. 5.2). Process similarity in the inside of the membrane is given, if all these 5 dimensionless parameters are kept constant. Note, that the temperature within the whole reactor system (incl. the membrane) is kept constant, which allows to omit the temperature as basic SI unit. Of course, the temperature could be used to vary parameters like  $D_{O_2,m}$  or  $\nu$  in order to achieve process similarity. However, the resulting heat transfer would directly affect the physical similarity, which is discussed later.

Table 5.2: Overview of the 5 necessary dimensionless numbers (Reynolds number, modified Péclet number, Sherwood number, pressure loss coefficient, mole fraction of oxygen at the membrane wall) to obtain process similarity in the inside of the membrane.

Dimensionless number	Definition	Comment
Reynolds number <i>Re</i>	$\frac{4\dot{V}}{\pi d_i \nu}$	The ratio of inertial forces caused by the flow to viscous forces represents the flow behavior and thus, defines the boundary layer thickness at the membrane wall.
Modified Péclet number <i>Pe'</i> [21]	$rac{4\dot{V}}{\pi d_i D_{O_2,m}}$	Pe' = Re * Sc is the product of $Re$ and the Schmidt number $Sc$ . It is the mass transfer equivalent to the original Péclet number $Pe = Re * Pr$ . Since $Re$ is already part of the solution, $Pe'$ could be replaced by $Sc$ without any effect. However, as $Pe'$ directly relates the fraction of oxygen diffusing through the membrane to the whole amount of fluid flowing by, it represents the problem in this work better.
Sherwood number <i>Sh</i>	$\frac{k_{conv,O_2,m}d_i}{D_{O_2,m}} = f(Re,Sc)$	Sh relates convective mass transfer to diffusive mass transfer at the membrane wall
Pressure loss coefficient ζ	$\frac{\Delta p}{\frac{\rho}{2} \left(\frac{4\dot{V}}{\pi d_i^2}\right)^2 \frac{L}{d_i}} = \frac{p_{abs} _{z=L} - p_{abs} _{z=0}}{\frac{8\rho L\dot{V}^2}{\pi^2 d_i^5}}$	Note: In other non-dimensional analyses, the Euler number $Eu=2*\zeta$ is used. However, the calculations are not affected by choosing $\zeta$ over Eu or vice versa.
Oxygen mole fraction at membrane wall $n_{{\it O}_{2,wall}}$	$n_{O_2,wall} = \frac{p_{O_2,wall}}{p_{abs}}$	$n_{O_2,wall}$ is of great relevance as it denotes the driving force for oxygen diffusion through the membrane to feed the microbes in the biofilm

One might consider the  $k_L$ a value to be missing, since many researchers pronounce its crucial significance for any biotechnological scale-up design. [139] The  $k_L$ a value relates the oxygen transfer rate to the reactor volume. In this work, the bulk reactor volume is meant to be anoxic in order to avoid respiration of ethanol to  $CO_2$  by S. cerevisiae. Therefore, the  $k_L$ a value is not a relevant parameter in this context, because the oxygen transfer to the biofilm, which is reflected by the above-mentioned set of dimensionless parameters, and not to the bulk defines the process performance. Nevertheless, the enzymes, which are produced by T. reesei in the biofilm and released to the bulk, become more and more diluted, if the reactor volume is simply increased. Therefore, the volume ratio of the biofilm and the reactor volume  $V_{bf}/V_{reac}$  is a critical parameter (eq. 5.4 & Tab. 5.3). It becomes clear that the  $k_L$ a value -although being a valuable parameter in other experimental setups- is an improper simplification by merging oxygen transfer characteristics with reaction kinetics in the biofilm (as already described in

chapter 3).

Besides the relevant process parameters for the inner membrane compartment of the reactor, it is necessary to define the critical parameters in the biofilm compartment and bulk compartment as well. As the biofilm layer and the bulk volume strongly interact with each other, the process similarity concept is developed for both phases simultaneously. In total, the system is governed by 13 relevant parameters, the inlet concentration, reactor volume, biofilm volume, reaction rate, residence time, rotational speed of the stirrer, stirrer power, stirrer diameter, bulk fluid density, viscosity, the yeast cell diameter, viscosity of the fluid fraction in the biofilm and diffusivity (eq. 5.4):

$$c_{\text{in}}\left[\frac{kg}{m^{3}}\right]; V_{\text{reac}}\left[m^{3}\right]; V_{bf}\left[m^{3}\right]; r\left[\frac{kg}{m^{3}s}\right]; \tau[s]; N\left[s^{-1}\right]; P\left[\frac{kg*m^{2}}{s^{3}}\right]; d_{\text{stirrer}}\left[m\right]; \rho\left[\frac{kg}{m^{3}}\right]; v\left[\frac{m^{2}}{s}\right]; d_{\text{yeast}}\left[m\right]; v_{bf}\left[\frac{m^{2}}{s}\right]; D\left[\frac{m^{2}}{s}\right]$$

$$(5.4)$$

Subtracting the 3 basic unit results in 10 dimensionless parameters (Tab. 5.3):

Table 5.3: Overview of the 10 necessary dimensionless parameters to ensure process similarity in the bulk phase.

Dimensionless number	Definition	Comment
Sherwood number <i>Sh</i>	$\frac{k_{conv,b}\sqrt[3]{V_{bf}}}{D} = f(Re_b, Sc_b)$	To ensure the same mass transfer rate
	$\frac{1}{D} = f(Re_b, Sc_b)$	for every species <i>i</i> across the biofilm-
		bulk boundary layer, Sh needs to be
		kept constant
Schmidt number <i>Sc</i>	$v_{bf}$	Sc relates diffusive momentum transfer
Semmat namber be	$\frac{v_{bf}}{D}$	to diffusive mass transfer
Reynolds number <i>Re</i>	$Nd^2$ .	In a stirred vessel, the inertial forces of
Reynolds number Re	$\frac{Nd_{stirrer}^2}{dt}$	The state of the s
	V	Re are defined by the rotational speed
	P	and the stirrer diameter. [117]
Newton number <i>Ne</i>	$\frac{r}{\rho N^3 d_{stirrer}^5}$	Ne relates the stirrer power to the
	$\rho N^3 d_{stirrer}^3$	available hydrodynamic power in the
	7 th 7 (	vessel
Yield $\eta$	$\frac{r * \tau}{c_{in}} \left( = \frac{c_{out}}{c_{in}} \right)$	The yield denotes the process efficiency
	$c_{in} \setminus c_{in}$	by relating the output to the input.
Dimensionless number $c_1$	$\frac{r * \tau}{\rho} \left( = \frac{r * V_{reac}}{\rho \dot{V}} \right)$	$C_1$ relates the productivity $r * V_{reac}$ to the
	${\rho} \left( = {\rho \dot{V}} \right)$	solid content $\rho \dot{V}$ , which becomes clear,
		if the fraction is not reduced by $V_{reac}$ .
Dimensionless number C2	$V_{bf}$	$C_2$ relates the biofilm volume to the
2	$\frac{V_{bf}}{V_{reac}}$	total reactor volume and thus, accounts
	7.000	for the dilution of biofilm products such
		as enzymes in the bulk.
Dimensionless number $\mathcal{C}_3$	Turbulent flow:	For turbulent flow, $C_3$ relates the mixing
Dimensionless number C <sub>3</sub>		
	$\frac{\Theta}{\tau} = \frac{\lambda^2}{D\tau} = \frac{\left(\frac{V^3}{\varepsilon}\right)^{1/2}}{D\tau}$ $= \frac{\left(\frac{\rho V_{reac} v^3}{P}\right)^{1/2}}{D\tau}$	time $\theta$ of a solid-liquid suspension to
	$\frac{\sigma}{\sigma} = \frac{\kappa}{R\sigma} = \frac{\kappa}{R\sigma}$	the residence time in order to ensure
	t Dt Dt	proper mixing in the bulk. As mixing is
	$\left(\frac{\rho v_{reac} v^{2}}{\rho}\right)$	rate-limited by the diffusion within the
	$=\frac{\langle T \rangle}{D\tau}$	smallest-scale vortices, the mixing time
		is a function of $D$ and the Kolmogorov
	Laminar flow:	scale $\lambda$ .
		For laminar flow, $C_3$ relates the
	$\frac{t_c}{\tau} = \frac{V_{reac}}{K_O N d_{stirrer}^3 \tau}$	circulation time of a fluid particle to its
	QStirrer	residence time. The circulation time
		depends on the reactor volume, the
		stirrer design and a constant, the
		circulation number $K_0$ . [128]
Dimensionless number $C_4$	$D\sqrt[3]{V_{bf}}\tau$ ( $D\sqrt[3]{V_{bf}}$ )	$C_4$ relates the rate-limiting diffusive
	$\frac{\sqrt{y}}{V_{2,2,2,2}} \left( = \frac{\sqrt{y}}{\dot{V}} \right)$	mass transfer through the biofilm with
	reac ( V )	the wash-out by the reactor outflow. $C_4$
		may be viewed as product of the
		productivity $C_1$ and the $2^{nd}$ order
		Damköhler number $Da_{II}$ , which relates
Dimensionless number 6	Turbulant flavor	reaction speed to diffusive speed.
Dimensionless number $C_5$	Turbulent flow :	$C_5$ reflects the mechanical sensitivity of
	$\left(\frac{v^3}{2}\right)^{1/2}$	the cells by relating the Kolmogorov
	$\frac{n}{d} = \frac{\langle \mathcal{E} \rangle}{1}$	length scale to the yeast cell diameter
	$a_{yeast}$ $a_{yeast}$	in the case of turbulent flow. The yeast
	$-\left(\frac{\rho V_{reac} v^3}{P}\right)^{1/4}$	cell diameter needs to be smaller ( $C_5$ >
	$=\frac{P}{I}$	1) in order to neglect any negative shea
	$a_{yeast}$	stress influence on the cells. [120]
	Laminar flow:	For laminar flow, the shear tension
	$\frac{\tau\sqrt{\dot{\gamma}\nu}}{2} = \frac{\tau\sqrt{kN\nu}}{2}$	defined by the viscosity and the shear
	$\frac{1}{d_{yeast}} - \frac{1}{d_{yeast}}$	rate $\dot{\gamma} = kN$ is related to the exposed
		surface of the yeast cells. According to
		Metzner & Otto, $k$ is a constant
		depending on the stirrer type and

To achieve process similarity, it is crucial, that, besides the above mentioned parameters (Tab. 5.3), the reaction kinetics in the biofilm and the bulk phase should be the same in order to maintain productivity and yield. The similarity of substrate and inhibitor concentrations in the biofilm is considered by the above-mentioned dimensionless numbers (Tab. 5.3). Thus, the last missing criterion is the reaction temperature, which is reflected by the Arrhenius number  $\gamma$ , which is basically the exponential argument of the Arrhenius law (eq. 5.5):

$$\gamma = \frac{E_A}{RT} = \text{const} \tag{5.5}$$

Since  $E_A$  and R are constant, one could just set the temperature constant, which is the reason, why it does not appear in Tab. 5.3. However,  $\gamma$  is used here to keep the dimensionless approach consistent. It is important to note, that the fluid properties in the biofilm are not affected by the rheology of the bulk fluid, because the particles, which define the bulk rheology cannot diffuse into the biofilm. Thus, the biofilm always consists of a Newtonian fluid making the diffusivity within the biofilm only a function of the fluid composition and temperature (given the moderate pressures of any bioprocess). As both, composition and temperature similarity, are reflected by the two above-mentioned dimensionless parameters  $\gamma$  and  $C_2$ , the mass transfer similarity within the biofilm is automatically given. Furthermore, the hydrostatic pressure is not included in the similarity analysis for 2 reasons: First, the hydrostatic pressure at pilot scale is negligible. The reactor filling height of 0.975 m yields a maximum hydrostatic pressure of less than 0.1 bar. Second, it was shown, that S. cerevisiae reacts to higher pressures according to the Le Chatelier principle of least resistance and reduces any volume increasing biochemical activity such as fermentation, where one mole of soluble glucose is digested to two moles of soluble ethanol and two mol of dissolved CO<sub>2</sub>. [141] However, it is still at 60 % productivity when the pressure is increased by factor of 70 to 7 MPa. [142] Thus, it may be assumed, that any fungal cell can withstand higher pressures and operate closely to the optimum at reasonable hydrostatic pressure increases (especially given the fact, that S. cerevisiae is not always exposed to the full hydrostatic pressure due to mixing of the vessel.

In this work, the physical similarity is not reflected by equations as the other similarities, but by the choice of materials. To ensure the same biological activity at large scales, the biological system should face the same environment at large scale as at small scale. Therefore, all materials should be the same or at least biocompatible according to ISO 10993-1. The choice of the membrane is particularly important: On the one hand, changing the membrane material is a powerful lever to adjust the diffusion coefficient and thus, all related dimensionless numbers. On the other hand, a change of the membrane material introduces many uncertainties because little quantitative information is available on phenomena like the degradation rate of different materials by the biofilms or adhesion affinity of biofilms to different surface structures although

their existence is proven. [143,144] Thus, all materials were the same at small scale & large scale with two exceptions: First, the reactor wall at lab scale is made of glass, whereas it is EN 1.4401 stainless steel at pilot scale. Since both materials are biocompatible, no impact is expected from this change. Second the substrate was changed. The experiments at small scale were conducted with pure microcrystalline cellulose (Avicel®PH-101) to omit the influence of any inhibiting substances and thus, guarantee reproducibility, whereas the pilot plant will be fed with steam pretreated beech wood. Pretreated beech wood introduces new chemicals to the system such as lignin and small residues of inhibitors (acetic acid, furfural etc.) from the pretreatment. Therefore, it is only possible to keep either the solid loading or the cellulose concentration of the inlet stream constant. In terms of dimensionless parameters, ratio of the cellulose feed stream to the total feed stream is not kept constant (eq. 5.6).

$$C_6 = \frac{\dot{m}_{C,feed}}{\dot{m}_{tot,feed}} \neq \text{const}$$
 (5.6)

Obviously, this is a harsh violation of the similarity paradigm for scale-up, but it is unequivocal since microcrystalline cellulose is valuable for facilitated reproducibility at lab scale, but the process needs to work with plant biomass at pilot and industrial scale.

The usual procedure of scale-up would be to derive all relevant parameters at large scale from an optimized small-scale model sticking to the similarity paradigm. [136] However, besides having already violated the similarity paradigm, the small-scale model cannot be regarded as fully optimized as shown in the beginning of this section. The impossibility to maintain similarity for all dimensionless parameters results in the importance of the rigorous process model, which can be used to simulate the change in CBP performance when violating the similarity paradigm. Besides  $C_6$ , the following dimensionless parameter cannot be maintained for different reasons (Tab. 5.4): The pressure loss coefficient  $\zeta$  may increase marginally due to longer membranes. However, as long as the membrane's stability is not affected and the pressure gradient along the membrane is still negligible, the process similarity may be considered as fullfilled. The oxygen concentration at the membrane wall is one of the DoFs mentioned earlier and thus, subject to optimization. The same holds for the dimensionless parameters reflecting the productivity ( $C_1$ , Tab. 5.3) and the biofilm volume ( $C_2$ , Tab. 5.3). Re<sub>v</sub>, Ne, C<sub>3</sub> & C<sub>5</sub> all refer to the stirring of the tank and thus, only one can be kept constant. The stirring has to be similar with respect to either the flow field  $(Re_v)$ , the necessary stirring power (Ne), the mixing time ( $C_3$ ) or the mechanical stresses on the cells ( $C_5$ ). Since the stirring affect the most dimensionless parameter and is affected itself by the change in feed cellulose concentration ( $C_6$ ), it is worth disucssing the stirrer design in the following:

Table 5.4: Overview of the scaled dimensionless parameters

Parameter	Similarity paradigm fullfilled
$Re_m$	$\checkmark$
Pe'	$\checkmark$
$Sh_m$	$\checkmark$
ζ	<b>(</b> √)
$n_{O_2,wall}$	×
$Sh_v$	$\checkmark$
$Sc_v$	$\checkmark$
$Re_v$	?
Ne	?
η	$\checkmark$
$\gamma$	$\checkmark$
$C_1$	×
$C_2$	×
$C_3$	?
$C_4$	$\checkmark$
$C_5$	?
$C_6$	×

Besides the influence of lignin on the reaction kinetics, the change of substrate mainly implies one of the following consequences: Either, the rheology of the bulk will be considerably influenced by the higher solid loading at equal cellulose concentration or the titer, which already is critically low, would be reduced further by 50-60 % as a result of lower cellulose concentrations in the reactor at an identical solid loading and thus, identical rheological properties. [30] Second, the lignin in the feed will cause enzyme deactivation by adsorption, which has to be included in the model. If inhibitors are present in relevant concentration, their inhibition terms have to be included in the model as well. The influence of Lignin on the reaction kinetics is rather irrelevant for stirring, but the change in rheology is of crucial importance. There is little information about the rheology of pretreated beech wood slurries. However, the rheology of beech wood and corn stover with the same solid content should be comparable given the fact, that even different substrates with different pretreatment methods show viscosities in the same order of magnitude, if the solid content is equal. [145] Corn stover with 5 % solid content behaves like a Newtonian fluid over a wide range of shear rates with a viscosity higher by a factor of ca. 120 compared to water, whereas 10 % solid content and more

result in non-Newtonian fluid behavior (Fig. 5.3). [15] Since the pilot scale should be able to handle both, the 1.75 % cellulose content from lab scale (equivalent to 3.5 % solid content [30]) and the needed 15-20 % solid content to obtain ca. 4 wt% ethanol titer for feasible distillation afterwards, the stirrer needs to be able to handle a vast range of fluid properties. Extrapolating the viscosity of a 1.75 % solid content solution from data of Pimenova. et al. (2004) gives 0.059 *Pas* (Fig. 5.3). 2 % solid content result in a viscosity of ca. 20 *Pas* in a reasonable range of shear rates, which will be discussed later (Fig. 5.3).

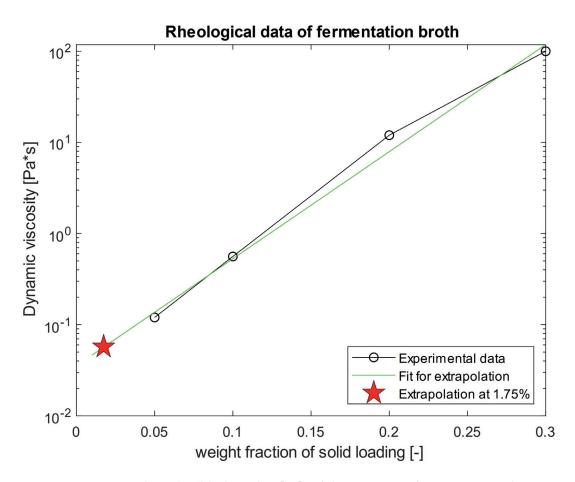


Figure 5.3: Experimental results (black circles; [15]) of the viscosity of a corn stover slurry at a shear rate of  $\dot{\gamma} = 9s^{-1}$  were fitted with an exponential function (green curve; coefficient of determination R<sup>2</sup>=0.997) to extrapolate the data for 1.75 % solid loading.

The upper viscosity limit demands a helical ribbon impeller as stirrer, because at such high viscosities, the mass and heat transfer from the reactor wall becomes crucial in order to ensure proper mixing quality. [146] Based on computational fluid dynamics, it is proposed to aim at minimal "clearance" (gap between helical blade and reactor wall, Fig. 5.4) when designing a helical ribbon impeller with optimum mixing properties. [146] In order to account

for manufacturing tolerance, a Clearance  $C = 0.03 \ d_{\rm vessel}$  was chosen, which is higher than the ideal value of  $0.01 d_{vessel}$ , but below the critical value of  $0.1 \ d_{vessel}$ . [146] The clearance defines the stirrer diameter:  $d_{\rm stirrer} = d_{\rm vessel} - 2 * C = 0.94 \ d_{\rm vessel}$ . Based on the stirrer diameter, the remaining design parameters, which are the pitch S=  $d_{stirrer}$  and the blade width W=  $0.2 \ d_{stirrer}$ , are derived according to Tsui et al. [146]

The membrane is winded helically around a membrane support structure at the outer boundary of the stationary frame (Fig. 5.4) because it maximizes the possible membrane area at the given design and the region is characterized by good mixing. [146]

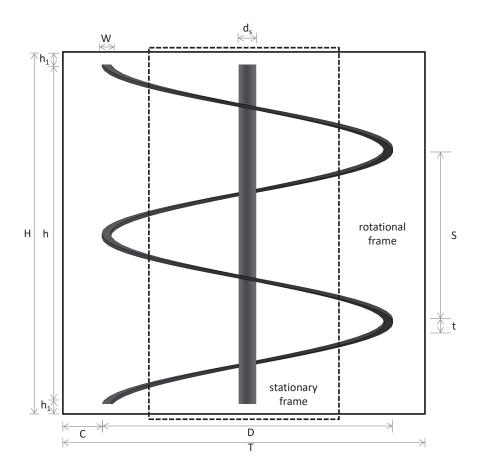


Figure 5.4: Design geometry of a helical ribbon impeller

However, the membrane support with the membrane occupies the full stirrer height  $h_{stirrer}$  likely leading to poor mixing in the inside at high viscosities. Thus, the inside of the membrane support was regarded as an own vessel and a central screw was designed for proper mixing within this virtual inner vessel. [147,148] The central screw clearance was again set to  $C_{cs}$ =0.03  $d_{pseudo-vessel}$ ). The pitch of the central screw is slightly higher as for the helical ribbon impeller  $S_{cs} = \frac{2}{3}d_{cs}$  for improved mixing in the virtual vessel at reasonable power

consumption. [148] The blade width is defined by the clearance  $W_{cs} = \frac{d_{pseudo-vessel} - 2C_{cs} - d_{shaft}}{2}$ . The blade of the central screw is winded opposite to the helical ribbon impeller to support the axial flow regime within the reactor. [146, 147] The complete configuration of helical ribbon impeller, membrane support and central screw is shown in Fig. 5.5. An overview of the design parameters and their calculation is given in Tab. 5.5.

Table 5.5:	Overview	of the	design	parameter	for the	stirrer	of the reactor
iubic o.o.	CVCIVICV	or tric	acoign	parameter	TOT LITE	Duile	or tric reactor

Parameter	Helical ribbon impeller	Central screw	Reference
Vessel diameter	$d_{\mathrm{vessel}} = 412 \; \mathrm{mm}$	$d_{\text{pseudo-vessel}} = d_{i, \text{ membrane support}}$ = 120 mm	-
Vessel filling height	$h_{\rm filling} = 975 \; \mathrm{mm}$	$h_{\text{filling}} = 975 \text{ mm}$	-
Shaft diameter	$d_{\rm shaft} = 56.6 \text{ mm}$	$d_{\rm shaft} = 56.6 \; \rm mm$	-
Shaft height	$h_{ m shaft}=740~{ m mm}$	$h_{\mathrm{shaft}} = 740 \; \mathrm{mm}$	-
Stirrer height	$h_{\text{stirrer}} = 1.1 * h_{\text{filling}}$ = 1072.5 mm	$h_{cs} = h_{\text{shaft}} = 740 \text{ mm}$	-
Clearance	$C = 0.03d_{\text{mrol}} = 11.67 \text{ mm}$	$C_{cs} = 0.03 d_{\text{vseudo-vessel}} = 3.6 \text{ mm}$	[107]
Impeller diameter	$d_{\text{stirrer}} = \frac{d_{\text{vessel}}}{1.06} = 389 \text{ mm}$	$d_{cs} = \frac{u_{\text{pseudo-vessel}}}{106} = 113.2 \text{ mm}$	-
Pitch	$S = d_{\text{stirrer}} = 389 \text{ mm}$	$S_{cs} = \frac{2}{3} d_{\text{vessel}} = 274.6 \text{ mm}$	[107,108]
Blade width	$W = 0.2d_{\rm stirrer} = 77.8 \text{ mm}$	$W_{cs} = \frac{d_{cs} - d_{shaft}}{2} = 28.6 \text{ mm}$	[107]

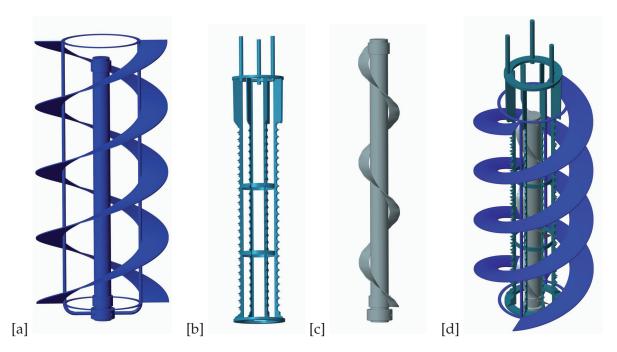


Figure 5.5: Configuration of helical ribbon impeller ([a], blue), membrane support ([b], turquoise) and central screw ([c], grey) for optimum mixing behavior over a large range of fluid viscosities [d].

Despite putting an unsolvable design constraint on the scale-up The stirrer design is consistent with the dimensionless analysis. The design parameter d<sub>stirrer</sub> needed to be chosen in favor of proper mixing over a large range of viscosities and the dimensionless number for mixing quality  $C_3$  contains  $d_{stirrer}$  in case of laminar flow (laminar flow is expected as consequence of the high viscosities and the absence of any baffles [136]). The process similarity in terms of minimized mixing time is achieved by the stirrer design and reflected by  $C_3$ . Since the mixing time  $C_3$  was kept constant, the stirrer will need more power (higher Ne), which is in agreement with the no-free-lunch theorem. The higher stirring power will slightly increase the mechanical stresses  $(C_5)$ , whereas (Re) decreases by the power of 2/3 (cf. exponents of  $d_{stirrer}$  in Tab.5.3) leading to a larger boundary layer at the biofilm. However, as long as the changes Ne, C<sub>5</sub> and Re are still below certain thresholds (no considerable convective mass transfer limitaion at the biofilm-bulk boundary and no harming of the cells), these dimensionless parameters may be considered similar. These thresholds are defined by model simulations, where the possible parameter variation without altering the model outcome significantly is evaluated. Due to the increased importance of the clearance at higher viscosity, the similarity paradigm needed to be violated in that sense, that  $d_{stirrer}$  cannot be adjusted anymore for other dimensionless parameters such as  $C_2$  to optimize the available space for the membrane. These additional design constraints make the set of equations overspecified. An overspecified set of equations does not allow for an exact solution. By applying an optimization criterion, the given equations may be solved by maximizing/minimizing the optimization criterion. [149] The minimum selling price, which can be related to every possible calculation outcome by the techno-economic model presented in chapter 2, is a predestined optimization criterion. [150] The calculations of the corresponding MESPs are conducted with the sensitivity data of the process parameters presented in chapter 2.1. However, the pilot scale reactor is still in an academic environment with utilities different from industry. Thus, regarding some design specifications it will be distinguished between an industrial favorable solution and a feasible solution for pilot scale since the overall goal of this work is to demonstrate the proper functioning of the given scale-up design framework. For example, the stirrer was scaled-up with respect to the pilot scale setup available at site since the process model strongly relies on the assumption of a perfectly mixed bulk. The economic impact of poor mixing is hard to quantify without extensive CFD simulations. Therefore, it was decided to prioritize the mixing performance of the reactor over process economics in order to achieve the above-mentioned proof that the given scale-up framework is reliable.

Given the stirrer design, the membrane area is determined by the space on the cylindrical shell of the membrane support. In other words, the 2 DoFs of the membrane dimensions were sacrificed to ensure proper mixing. In terms of industrial scale-up, it is not favorable to put such a hard constraint on the membrane design by designing the stirrer, but from an academic point of view, proper mixing is unequivocal for the model validation at higher scales.

The membrane is scaled up by means of the fungal biofilm thickness  $\delta_f$ , which is a function of

the bulk glucose concentration and the oxygen concentration at the outer membrane surface. Regarding the oxygen concentration in the membrane, it would be economically favorable to do the oxygen make-up with air instead of expensive pure oxygen. Replacing the lost oxygen with air leads to an equilibrium within the membrane, which is reached as soon as 0.79/0.21 times as much nitrogen diffuses through the membrane meaning, that the gas diffusing through the membrane has exactly the composition of air. Since nitrogen is inert, it leaves the system only through the reactor outlet (eq. 5.7).

$$J_{N_{2}} = H_{cp}^{N_{2}} p_{v} \dot{V}_{out} = \frac{0.79}{0.21} J_{O_{2}} \approx \frac{0.79}{0.21} \frac{2\pi D_{O_{2},m} L \left( H_{cp}^{o_{2}} p_{O_{2},m} - 0 \right)}{\ln \left( r_{i,m} / r_{o,m} + \delta_{bf} \right)}$$

$$\Leftrightarrow p_{o_{2},m} \approx \frac{0.21 M_{N_{2}} H_{cp}^{N_{2}} p_{v} \dot{V}_{out} \ln \left( r_{i,m} / r_{o,m} + \delta_{bf} \right)}{1.58 \pi D_{O_{2},m} L H_{cp}^{o_{2}} M_{O_{2}}} = 0.01 \text{ bar at small scale}$$

$$(5.7)$$

Due to the low nitrogen removal from the system, a high amount of  $N_2$  accumulates in the membrane. The optimum fungal biofilm thickness for a partial oxygen pressure of  $10\ mbar$  would require a membrane thickness in the nanometer range, which is not feasible, of course. Thus, industrial oxygen needs to be purchased at  $8.35\ \text{/Nm}^3$  (price adjusted to 2020 with the US producer price index, published by the US Bureau of Labor Statistics). [148,151] Using pure oxygen to feed T. reesei would yield a US MESP increase of  $6.12\ \text{/L}$  Ethanol (+15%). [33] However, feeding T. reesei with pure oxygen allows any oxygen concentration within the membrane an thus, the degree of freedom regarding the membrane dimension is maintained (cf. beginning of this chapter), which is important since the membrane dimensions underlie other constraints as shown above. Since the performance of the bioreactor increases linearly with the membrane length at a given membrane diameter and a sufficiently high Reynolds number, the best membrane configuration will be the smallest available membrane, which could be winded the maximum number of times. The membrane should be segmented and connected to gas distributors in order to keep the pressure loss below  $0.3\ bar$ .

The highest ethanol titers, which were 40 % lower compared to the laboratory scale titers, were simulated with the standard membrane (membrane inner diameter  $d_i$ = 1.58 mm, membrane outer diameter) at the maximum possible length of L=116 m with 26 % oxygen concentration in the membrane, 17.5  $\frac{g}{L}$  cellulose feed concentration and a residence time of  $\tau=120$  h.

Concluding, it can be stated that the majority of the given non-dimensional parameters can be kept constant (all membrane parameters except  $n_{O_2,wall}$  and all bulk parameters except Ne,  $C_1$  and  $C_2$ ) thanks to an elongated residence time  $\tau$ , which compensates for the lower cellulose conversion rate (smaller  $C_1$ ) as result of less enzyme loading in the bulk (smaller  $C_2$ ). The higher energy demand for stirring (higher Ne) is subtracted from the excess electricity, which is sold to the grid. The model simulations with the fungal biofilm thickness  $\delta_f$  should ensure proper outcome when the similarity paradigm was violated, and the techno-economic model

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may be used to optimize different outcomes with respect to minimizing the costs at higher scales. However, extensive model simulation runs at pilot scale could not yet be conducted due to a diverging algorithm in Matlab. It is assumed that the solving algorith cannot handle the fast converging reaction kinetics of the bulk with the slow converging mass transfer equations in the biofilm.

## 5.4 Conclusions

A scale-up framework consisting of a rigorous process model and a set of non-dimensional parameters was developed to scale up consortium-based consolidated bioprocessing of cellulosic substrates from 2.7 L laboratory scale to 130 L pilot scale. The majority of the non-dimensional parameters could be kept constant during scale-up as requested by the similarity paradigm. Necessary changes were aimed to simulate with the model. Again, the fungal biofilm thickness  $\delta_f$  served as a relevant parameter for scale-up considerations. In general, the relative loss of biofilm volume is compensated by longer residence times since the residence time has by far the least impact on the process economics. [33] However, an experimental confirmation of the presented calculations remains still to be done. The synergy of a classic trade-off identifying approach such as the similarity paradigm and the rigorous model, which delivers precise information on any set of process condistions is designed to overcome the reported typical performance decreases of 10 %- 30 % at industrial scale. [8,127,139] Applying the economics as optimization criterion allowed to minimize the effect of increasing costs at higher scales, as process involving a surface  $A \propto L^2$  and reactor volume  $V \propto L^3$ , where the similarity paradigm cannot be maintained by definition. The expected price increase of ca. 15 % at industrial scale due to the need of pure oxygen could be reduced by exploiting synergies with other bioprocesses in the framework of a biorefinery. [152] E.g., algae produce oxygen in purity, which is by far sufficient to feed the membrane with the optimum concentration of 26 %. [153]

# CHAPTER 6

# Evaluation of *in-situ* product removal strategies to improve the productivity and economics of consolidated bioprocessing

#### 6.1 Abstract

Popular rate-controlled separation techniques in biotechnology, such as adsorption, liquid-liquid extraction, steam stripping, CO<sub>2</sub> stripping, vapor permeation and pervaporation, were investigated regarding their potential to replace distillation as industrial standard for ethanol separation from a fermentation broth. It was focused on *in-situ* and slip stream separation setups in order to reduce yeast inhibition by ethanol additional to the general advantages of rate-controlled separations such as avoiding limitations by an azeotrope or the unfavorable vapor-liquid equilibrium of highly diluted ethanol-water mixtures.

However, except from CO<sub>2</sub> stripping and pervaporation, all mechanisms fail to handle the solids of the fermentation broth. CO<sub>2</sub> stripping is limited by a poor ethanol recovery due to the trade-off between bubble residence time and stable bubble flow regime. Pervaporation, being the most promising concept for *in-situ* product removal, would be a cost-saving alternative to distillation for batch operation, but is limited by an unfavorable vapor-liquid equilibrium due to low bulk concentrations during continuous operations.

# 6.2 Introduction

The current industrial standard for ethanol separation from a fermentation broth is distillation followed by an adsorption dehydration step with a molecular sieve disregarding whether it is  $1^{st}$  generation ethanol from edible biomass or  $2^{nd}$  generation ethanol from lignocellulose. [2,64] The advantages of distillation are high ethanol recovery, reasonable efficiency already at titers

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of 4 wt.% ethanol as well as extensive scale-up experience. [64] The main disadvantages are the high costs for titers below 4 wt.% ethanol and the separation limit by the azeotrope of ethanol and water, which results in the need of a second dehydration step. [64] Both disadvantages could be overcome by a rate-controlled separation mechanism as it is shown in the following. Distillation is an equilibrium-controlled separation mechanism, because each distillation stage exploits the higher volatility of ethanol in the vapor-liquid equilibrium of an ethanol-water mixture. [154] Thus, given a certain scale, the only parameter, which influences the separation efficiency and the costs, is the initial ethanol concentration of the fermentation broth, i.e. the titer of the fermentation. [154] Rate-controlled separations also rely on a concentration gradient as driving force, but equilibrium is never reached (e.g., by withdrawing the ethanol vapor from the permeate in a pervaporation process). As the name suggests, they are rate-controlled and the rate is always a product of the driving force and a rate constant. [154]

$$J_{\text{diff}} = D \frac{\partial c}{\partial x} \tag{6.1}$$

Given the Fick law of diffusion as example (eq. 6.1), the diffusion rate, called the flux  $J_{\text{diff}}$ , is equal to the product of the rate constant, the diffusivity D, and the concentration gradient  $\frac{\partial c}{\partial x}$  as driving force. [155] A membrane, which is very permeable for a species i (leading to a high D), theoretically could give better results at lower concentrations of the substance i than another membrane with poor permeability for i. Generally spoken, a setup with a high rate constant allows a margin for poor concentration gradients. Furthermore, any rate-controlled separation is not subject to equilibrium-related phenomena such as an azeotrope. [154] Adjusting the rate of separation to be much higher than the rate of ethanol loss by the reactor outflow would also allow to remove ethanol during the fermentation process (eq. 6.2).

$$r_{\text{separation}} \gg r_{\text{outlet}} = \dot{V}c_{\text{out}}$$
 (6.2)

A so-called slip-stream or *in-situ* separation setup (Fig. 6.1) for a rate-controlled separation technique has the possibility to increase the productivity by avoiding yeast inhibition by toxicity of ethanol above a certain threshold (Fig. 6.2) and additionally, in the case of *in-situ* separations, the possibility to reduce the capital expenses by reducing the number of apparatus for separation. [156,157]

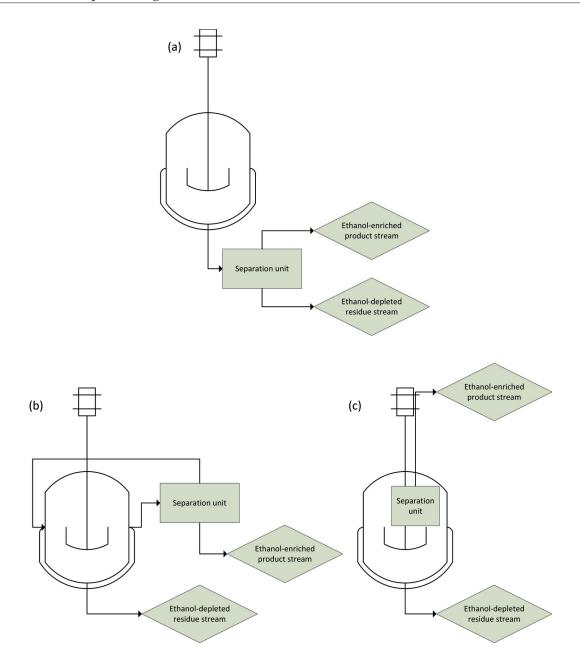


Figure 6.1: Illustration of the different separation setups: End-of-pipe separation (a), slip stream separation (b) and *in-situ* separation (c). With end-of-pipe separation, the whole reactor outlet is sent to the separation unit and there is no interaction with the bioreactor anymore. With slip stream separation, a circulating stream between the separation unit and the bioreactor is established. The reactor outlet is already ethanol-depleted and no further ethanol is recovererd. *In-situ* separation works identically to slip-stream separation with the only difference, that the separation unit is installed within the bioreactor. Note: The inlet streams for the reactors are removed for illustration purposes

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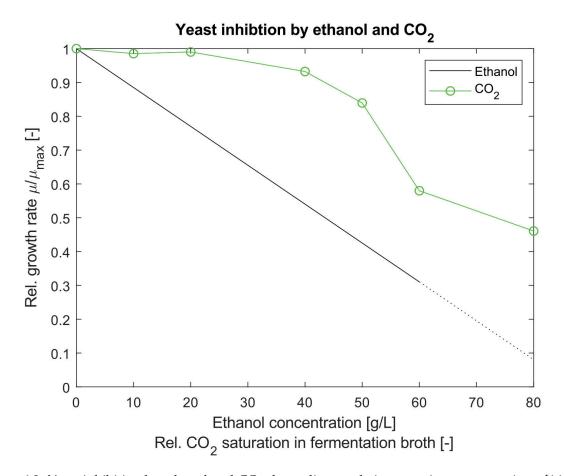


Figure 6.2: Yeast inhibition by ethanol and  $CO_2$  depending on their respective concentrations. [16,17] The modeled ethanol data is experimentally validated for ethanol concentrations up to  $60 \frac{g}{L}$ . [16] For concentrations above  $60 \frac{g}{L}$ , the data is extrapolated, but in agreement with the experimental findings of other published studies. [16,18]

The possibility to cope with low titers, to decrease capital costs and to increase the productivity is a promising feature for continuously operated CBP. As previously shown (chapter 2), CBP costs are dominated by the CAPEX with a share of 58 %. [10] Thus, even small reductions of the CAPEX due to *in-situ* product removal (ISPR) would impact the MESP. Moreover, continuous ethanol production from lignocellulose by means of CBP lacks in productivity compared to  $1^{st}$  generation bioethanol (ca.  $0.07 \frac{g}{L*h}$  vs.  $4 \frac{g}{L*h}$ ). [4,33,98] Given a conservative approach by assuming, that the CBP productivity cannot be further increased, the necessary residence time to obtain a titer of 4 wt.% would be ca.  $24 \, days$ . In terms of costs, this is doable as the residence time has a small impact on the total costs. However, the start-up phase to reach steady-state after the yearly maintenance would increase by a factor of 3 to 5 resulting in start-up durations of 72-120 days, which is not feasible. [33,83] Thus, ISPR could help to cope with both of the major drawbacks of CBP by increasing the productivity through decreasing inhibitory effects

and by obtaining dehydrated ethanol efficiently from lower titers.

This work aims to investigate different rate-controlled *in-situ* or slip stream ethanol separation techniques as alternative to the classic distillation-adsorption approach regarding their potential to address the weaknesses of continuous CBP (high capital costs, lack of productivity and titer) in order to make  $2^{nd}$  generation bioethanol economically competitive with  $1^{st}$  generation ethanol.

#### 6.3 Results and Discussion

The state-of-the-art procedure of ethanol purification, distillation followed by adsorption, is an established industrial process yielding 99.5 % ethanol at arbitrary scale within the projected limits (chapter 2) and costs of 3.39  $\phi$ /annual L ethanol at a throughput of 2000 dry tons per day.

The following rate-controlled separation techniques, which are subject to biotechnology research, are investigated regarding their potential to outperform the economics of the state-of-the-art at the given specifications [64]:

- Adsorption
- Liquid-liquid extraction
- Steam stripping
- CO<sub>2</sub> stripping
- Vapor permeation
- Pervaporation

Adsorption is conducted in a column packed with nano-porous material, which chemical composition allows for selective surface adsorption of the desired component. [158] It is well established to purify ethanol from 90-93 wt.% to 99.5 wt.% after distillation. [2,64] However, it is inappropriate as main separation technology disregarding whether it is and-of-pipe or slip stream separation setup. This is due to the following issues: First, the traditional adsorption approach (removing water from ethanol) would require huge capacities at titers of 4 wt.% or even lower causing an increase in CAPEX. Thus, an adsorption material, which is selective towards ethanol, would be necessary. Research is conducted to find suitable materials, but industrial maturity is not yet reached. [159,160] However, the main issue is the solid loading. The fermentation broth has a considerable solid loading, which would immediately clog the

adsorption column. Therefore, a solid-liquid separation step prior to adsorption would be necessary. One option for solid-liquid separation is evaporation in a column, but such a beer tower is operated at 103 °C to avoid ethanol losses through the liquid-solid outlet. [2] Thus, adsorption would require almost the same heat energy as distillation at much higher apparatus costs due to the adsorption packing [60], which is economically not favorable. Other options for solid-liquid separation such as a hydrocyclone or filtration are not feasible as well. A single hydrocyclone separates only ca. 60 % of the solids due to the low difference in density between water and yeast cells. [161] In order to achieve sufficiently high solids removal, a series of hydrocyclones is necessary, which again causes too large CAPEX. [62,161] Filtration faces the same problems as membrane separation, which are discussed later on.

Liquid-liquid extraction involves a second fluid, which most importantly has a high selectivity  $\beta$  towards ethanol and immiscible with the fermentation broth. [64] In a slip stream or end-of pipe application, the fermentation broth is mixed with the extractant, usually a long-chain alkane such as n-dodecane. [64, 162] Ethanol is transferred to the extractant due to higher solubility.  $\beta$  defines the ethanol recovery, whereas the equilibrium distribution coefficient  $K_D$  defines the separation rate. High ethanol recoveries due to  $\beta > 100$  are possible, but unfortunately  $\beta$  is inversely proportional to  $K_D$  for most fluids. Therefore, the process is either selective and slow or fast and unselective. [64] Due to the immiscibility, the two fluids separate after the mixing unit by buoyancy and ethanol may be separated from the extractant by any separation technique. Apart from productivity-limiting interferences between the alkane and the fermentation product, which are discussed later, liquid-liquid extraction is suitable for a slip-stream separation approach. In a slip-stream separation, the reactor outlet is not further separated and thus, any ethanol in the reactor outlet is lost. In a CSTR, the reactor concentration is equal to its outlet concentration. [83] Given a required ethanol recovery of 99 % (distillation standard [2]) would result in an ethanol concentration of 0.01\*4  $\frac{g}{l}$ =0.04  $\frac{g}{l}$ in the bioreactor. Even with a high selectivity  $\beta$  [64], liquid-liquid extraction with an ethanol concentration of 0.04  $\frac{g}{L}$  would require roughly twice as much energy as distillation. At 4  $\frac{g}{L}$ ethanol concentration, liquid-liquid extraction may be performed with only ca. 4 % of the energy demand of distillation making it an interesting option for end-of-pipe separation. [64] However, again the solid content is a problem, because the extractant tends to emulsify with solids such as yeast cells, cellulose and lignin. [162-164] Apart from ecological issues, the costs to replace the loss of extractant (12 \$/kg resp. 70.45 \$/mol [165]) outweigh the savings in energy demand. A prior solid-liquid separation is not possible for the reasons mentioned above regarding adsorption.

Steam stripping and vapor permeation involve heating up the fermentation broth to vapor formation or the exposure of the fermentation broth to steam at low pressures or high temperatures. [64] Both is lethal to the microorganisms in the bioreactor making steam stripping and

vapor permeation unfeasible for *in-situ* or slip stream separation. Applying steam stripping as end-of-pipe separation mechanism does not make sense, because the process is very similar to distillation. [64] One would sacrifice the industrial maturity of distillation for comparable costs and process performance. Also, there is no point in replacing distillation with vapor permeation as end-of-pipe separation. The demand of thermal energy is comparable since the reactor outflow needs to be vaporized, but the membrane will be exposed to a high risk of membrane fouling due to the high loading of organics in the reactor outflow. [64,166] Exchanging the membrane more frequent than on a yearly basis will increase the MESP only by less than 0.5 % per additional membrane exchange. [33] However, the plant downtime is not included in the MESP increase and again, the industrial maturity of distillation is sacrificed to overcome the azeotrope in one separation step at comparable costs.

CO<sub>2</sub> stripping seems promising on the first look: Purging bioreactors and thus, an *in-situ* implementation, as well as the condensation of gas stripping streams are well-established processes, the CO<sub>2</sub> gassing ensures anerobic conditions in the bulk phase, CO<sub>2</sub> stripping works properly at the moderate temperature levels in the fermenter, ethanol inhibition of the yeast is avoided, and the CO<sub>2</sub> lost by imperfections of the stripping cycle could be compensated by the CO<sub>2</sub> production of the yeast. [18] However, there are drawbacks, which outweigh these advantages: CO<sub>2</sub> stripping would cause high dissolved CO<sub>2</sub> concentrations in the fermentation broth of an open system. Apart from unfavorable consequences of a pH-drop as consequence of high dissolved CO<sub>2</sub> concentrations, the yeast will be strongly inhibited (ca. 50 % less productivity, Fig. 6.2) by the high dissolved CO<sub>2</sub> concentrations. [17] Furthermore, the above-mentioned equilibrium of 0.04  $\frac{g}{L}$  ethanol concentration in the bioreactor will become an issue again, if *in-situ* stripping with a recovery of 99 % is conducted. However, the maximum stripping recovery is much lower, since a certain bubble residence time is necessary for the ethanol mass transfer to the gas phase, which corresponds to a minimum reactor height ( $h_{\rm reactor,min} = au_{
m bubble,min} * v_{
m bubble}$ ), and the bubble flow regime is necessary to obtain a sufficient mass transfer rate. To establish a stable bubble flow regime, a minimum diameter of the reactor is required, which allows a maximum reactor height at a given reactor volume  $\left(h_{\text{reactor,max}} = \frac{V_{\text{reactor}}}{0.25\pi * d_{\text{reactor,min}}^2}\right)$ . [167] At the given reactor volume, the maximum possible ethanol recovery is 30 %, where the two height requirements match each other (Fig. 6.3). Note, that the influence of the stirring speed is discussed controversially, but the low stirring speed of 50 rpm will not improve the result anyway. [168, 169] A maximum ethanol recovery of 3 %, when applying CO<sub>2</sub> stripping *in-situ* obviously is economically not favorable.

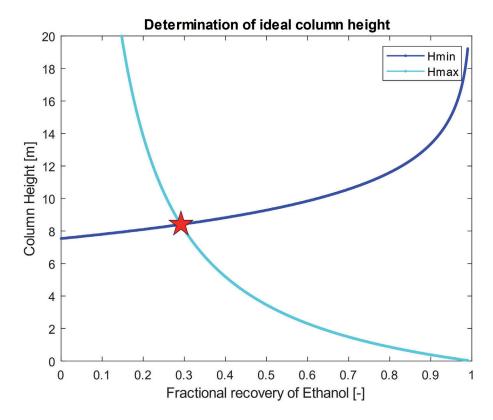


Figure 6.3: Determination of the maximum possible ethanol recovery of 30 % (red asterisks) by applying the reactor height requirements for bubble flow ( $h_{min}$ , blue line) and the bubble residence time ( $h_{max}$ , cyan line)

 $CO_2$  stripping as end-of-pipe separation mechanism is not feasible either considering the amount of  $CO_2$ , which is necessary to achieve the required recovery of 99 % (Fig. 6.4). Even for a poor ethanol recovery of 90 %, almost 5 t  $CO_2/s$  are theoretically needed at industrial scale (chapter 2 according to published, experimentally validated partition coefficients (cf. section C.1). [168] Besides the gas amount, which could be recycled, none of the apparatus (compressor e.g.) could handle these dimensions. A titer of 4 wt.% at such high volume flows makes  $CO_2$  stripping impossible.

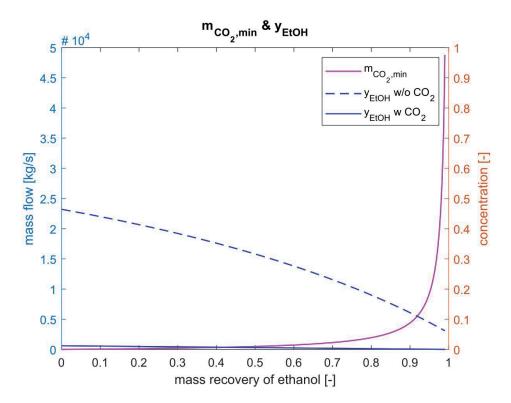


Figure 6.4: Necessary CO<sub>2</sub> mass flow (magenta line) and ethanol concentrations as weight fraction in the gas stream (blue line) and the residual stream (blue dashed line) as function of the ethanol recovery.

Pervaporation is a membrane separation mechanism, where the permeate evaporates due to low pressures on the permeate side (or less common, is withdrawn with a gas purge). [64] The mass transfer rate across the dense membrane may be described with the solution-diffusion model (eq. 6.3). [170,171]

$$J_{EtOH} = Q_{EtoH} \left( p_{EtOH,sat} x_{EtOH,bulk} - p_p y_{EtOH,p} \right)$$
(6.3)

The rate constant  $Q_{EtOH}$  denotes the permeance  $[\frac{mol}{Pa*s}]$  of ethanol for the given membrane and is a function of the diffusivity of ethanol in the membrane  $D_{EtOH}$ , the membrane thickness  $\delta_m$  and the gas phase sorption coefficient  $K_{EtOH}$ . The ethanol vapor pressure  $p_{EtOH,sat}$  reflects the volatility of ethanol.

 $x_{EtOH,bulk}$  and  $y_{EtOH,p}$  represent the ethanol mole fractions in liquid bulk side and the gaseous permeate side, respectively.  $p_p$  denotes the pressure on the permeate side. Given the flux equation, it becomes clear, that pervaporation is the most promising *in-situ* separation concept, because the low mole fraction of ethanol in the liquid phase may be compensated by other design parameters such as the permeate pressure, membrane thickness, a suitable membrane material with high diffusivity for ethanol etc. [64] Furthermore, a PDMS membrane, which was

reported to show good separation characteristics for ethanol [172], is already installed in the bioreactor. However, a second membrane would have to be installed, but this is not an option for two reasons: First, space in the reactor is limited and maintaining a necessary membrane surface during scale-up is very challenging (chapter 5). Thus, a second membrane would put a highly unfavorable design constraint on any scale-up procedure. Second, the additional membrane would be exposed to membrane fouling due to the high concentration of microbial biomass in the bioreactor. [166,173] The additional mass transfer resistance would accentuate membrane separation problems such as temperature and concentration polarization. [170] Concluding, it can be stated, that an additional membrane decreases the net performance of CBP as valuable space for biofilm formation is sacrificed only for a moderate increase in separation efficiency compared to a design with only one membrane. However, using the already installed membrane for two purposes, oxygen supply for the microbes and in-situ product removal, would further integrate the process and thus, perfectly fit the concept of CBP. [4,52] In order to examine the potential of pervaporation for *in-situ* product removal of CBP, the design constraints for the membrane setup are formulated in the following: Ensuring an optimum fungal biofilm thickness  $\delta_f$ , the partial pressure of oxygen within the membrane must be 0.26 bar (Chapter 5) (mechanical stability of the PDMS membrane is assumed). Operating the membrane with pure oxygen would result in the theoretical minimum possible permeate pressure of 0.26 bar. The aimed ethanol recovery of 9 % results in an ethanol bulk concentration of 0.04  $\frac{g}{L}$  as mentioned above. The required mass flux across the biofilm and the membrane calculates as follows (eq. 6.4):

$$J_{\min,EtOH} = 99 * J_{\text{EtOH,outlet}} = 99 * c_{EtOH,bulk} * \dot{V} = 99 * 0.04 \frac{g}{L} * \frac{2.7 L}{5 * 24 h} = 89.1 \frac{mg}{h}$$
 (6.4)

For this estimation, lab scale parameters were chosen in order to evaluate the pervaporation potential at sufficient membrane area, which corresponds to an ideal case. Considering the mass transfer resistance of the biofilm bulk boundary layer and the biofilm itself as well as ethanol degradation by *T. reesei*, this mass transfer rate is feasible as long as equilibrium is not reached (Chapter 3 & 4). However, equilibrium is reached very fast given the fact, that ethanol has a Henry constant of  $H_{CP}^{EtOH} = 1.9 \frac{\text{mol}}{m^3 \text{ Pa}}$  (eq. 6.5) [174]:

$$p_{EtOH,eq} = \frac{c_{EtOH, \text{ bulk}}}{H_{CP}^{EtOH}} = 0.457 \text{ Pa} = 0.046 \text{ mbar}$$
 (6.5)

As soon, as the partial pressure of ethanol in the permeate reaches 0.046 *mbar*, equilibrium is reached, and no further mass transfer occurs. To avoid equilibrium, high volume flow rates within the membrane would be necessary to withdraw and dilute the ethanol concentration.

The ethanol dilution will cause higher costs for separation from the gas phase and the high volume flow rates will cause a large pressure loss over the membrane, which increases the cost of compression for gas recirculation besides threatening the mechanical integrity of the membrane. Concluding, it can be said, that pervaporation is a promising *in-situ* product removal strategy for batch operation of bioprocesses with diluted volatile organics as product as stated elsewhere in literature. [64,170,172] However, at continuous operation, pervaporation is not feasible at any scale.

#### 6.4 Conclusion

Popular rate-controlled separation techniques were investigated regarding their potential to outperform distillation as industrial standard, since they offer the potential to reduce yeast inhibition by ethanol, to avoid separation limitations by the azeotrope and they are not bound to the vapor-liquid-equilibrium of highly diluted ethanol-water mixtures. However, except from CO<sub>2</sub> stripping and pervaporation, all mechanism fail to handle the solids of the fermentation broth. CO<sub>2</sub> stripping is limited by a poor ethanol recovery due to the trade-off between bubble residence time and stable bubble flow regime. Pervaporation, being the most promising concept for *in-situ* product removal, would be a cost-saving alternative to distillation for batch operation, but is limited by an unfavorable vapor-liquid equilibrium due to low bulk concentrations during continuous operations.

Distillation as industrial standard for ethanol separation from the fermentation broth remains untouched because there is too little incentive to change the separation design apart from economic savings. At the given titer of 4 wt.% or lower, yeast inhibition by ethanol is almost negligible. *In-situ* product removal strategies exploit their full potential, if the fermentation product is highly toxic, such as butanol, where the productivity increase is significant, when butanol is removed *in-situ*. [64,175]

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## CHAPTER 7

### Summary and conclusions

This work demonstrated that consolidated bioprocessing is a promising concept for conversion of lignocellulose to ethanol at industrial scale. CBP offers a great cost saving potential, is feasible to be operated continuously and may be scaled up due to extensive knowledge of the process from a chemical engineering point of view. The main findings and conclusions of the discussed topics are given in the following.

Cost savings of up to 27.5 % of the total costs compared to conventional bioethanol production from lignocellulose, as stated by a techno-economic assessment, make continuous CBP the strongest lever to reduce processing costs of lignocellulosic ethanol. In the EU, applying CBP offers a sufficient margin for profitable production or the possibility to decrease the plant size to 15 % and thus decentralize the biomass valorization. However, in the US where 56.2 % of the world's ethanol is currently consumed, the market situation is tense (31 % price drop for ethanol since 2007 whereas prices for chemical plants increased by 16 %). A cost sensitivity analysis of several process parameters (scale, titer, yield and residence time) and investment parameters (feedstock price, price level in the country of the plant location and costs of capital) show that scale and yield are the main cost-pushers from a process point of view, whereas the price level of the plant location has the highest impact on the investment conditions. Since outsourcing  $2^{nd}$  generation bioethanol production to third world countries with low price levels leaves valuable biomass potential unused and hinders economic growth in rural areas, it should be aimed at meeting the current ethanol market price by taking advantage of the cost levers of multiple process and/or investment parameters if necessary, such as utilizing cheaper waste feedstocks at comparable yields and reducing the costs of capital by accepting lower returns on equity. Alternatively, exploiting the added-value through sustainable production as well as local market disparities such as tariff barriers or tax exemptions may lead to profitable production of lignocellulosic bioethanol. In the short term, retrofitting of depreciated existing

corn ethanol plants to CBP operation, might be an interesting approach to reduce the CAPEX in order to meet the world market price of ethanol with lignocellulosic ethanol.

In order to prove the feasibility of continuous CBP, and therefore the mentioned cost savings of 27.5 %, and to validate a rigorous process model, continuous experiments were successfully conducted. The known obstacles of developing continuous processes could be avoided by adjusting the experimental setup. A maximum titer of  $3.258\pm0.007 \frac{g}{L}$ , a productivity of  $0.025 \frac{g}{L*h}$ and constant enzyme production over 750 h were achieved. Furthermore, it was proven that the continuous co-cultivation of two competitors, T. reesei & A. phoenicis, is possible, if the process conditions are adjusted to the identical growth rate. The adding of A. phoenicis targeted the better utilization of the inhibiting intermediate cellobiose by balancing the fungal enzyme cocktail in terms of higher  $\beta$ -G concentrations. This goal was achieved, but however did not result in higher yields or productivities. Furthermore, the continuous experiments showed that the oxygen flux per membrane area is a critical parameter for the process. Setups with identical volumetric oxygen transfer rate  $k_L$ a, but different oxygen fluxes per membrane area (large area & low concentration gradient vs. small area and high concentration gradient) showed titer differences of ca. 80 % (1.83  $\frac{g}{L}$  vs 3.26  $\frac{g}{L}$ ) in favor of setups with the large membrane surface. The difference was attributed to long diffusion paths in thicker biofilms and thus, shortage in nutrient supply.

A rigorous process model was developed for continuously operated consolidated bioprocessing of cellulose to ethanol to quantitatively describe the phenomena of lower titers at higher  $k_L$ a for optimization purposes . 9 species were considered (oxygen, glucose, T. reesei, secondary mycelia of T. reesei, enzymes, cellulose, cellobiose, yeast density and ethanol). 8 of these 9 species (all except cellulose) are present in the biofilm and thus, needed to be modelled spatially resolved in order to account properly for mass transfer limitations. The enzyme synthesis rate of the secondary mycelia and the effectivie diffusivity of  $\beta$ -glucosidase were used as fitting parameter of the model. Compared to literature data of suspended cultures in a batch process [10,124,125], a reduction in enzyme synthesis rate of ca. 40 % (0.67  $\frac{FPU}{mL*d}$  vs 1.152  $\frac{FPU}{mL*d}$ ) and a ca. 20 %  $(5*10^{-11} \frac{m^2}{s} \text{ vs } 4*10^{-11} \frac{m^2}{s})$  reduced effective diffusivity accounting for the affinity of  $\beta$ -G to attach to the cell walls yielded agreement with the continuous experiments within a 15 % confidence interval. The results of the model were able to explain the different productivities observed in the continuous experiments. The fungal biofilm thickness  $\delta_f$  was found to be a critical parameter with an optimum for every membrane configuration. Smaller  $\delta_f$  reduced the fungal biofilm volume and thus, the enzyme production unnecessarily and larger  $\delta_f$  increased the diffusion path length and caused shortage in nutrient supply as well as lower enzyme concentrations in the bulk. The agreement between the model data and the experiments also confirmed the non-proportionality of the fungal growth and enzyme production.

With the process model as centerpiece, a scale-up framework consisting of the model and a set of non-dimensional parameters was developed to scale up consortium-based consolidated bioprocessing of cellulosic substrates from 2.7 L laboratory scale to 130 L pilot scale. The majority of the non-dimensional parameters could be kept constant during scale-up as requested by the similarity paradigm. Necessary changes were simulated with the model. Again, the fungal biofilm thickness  $\delta_f$  served as a relevant parameter for scale-up considerations. In general, the relative loss of biofilm volume should be compensated by longer residence times since the residence time has by far the least impact on the process economics. However, an experimental confirmation of the presented calculations remains still to be done. The expected price increase of ca. 15 % at industrial scale due to the need of pure oxygen could be reduced by exploiting synergies with other bioprocesses in the framework of a biorefinery, where oxygen might be a byproduct of another process.

Finally, popular rate-controlled separation techniques were investigated regarding their potential to outperform distillation as industrial standard, since they offer the potential to reduce yeast inhibition by ethanol, to avoid separation limitations by the azeotrope and they are not bound to the vapor-liquid-equilibrium of highly diluted ethanol-water mixtures. However, except from CO<sub>2</sub> stripping and pervaporation, all mechanism fail to handle the solids of the fermentation broth. CO<sub>2</sub> stripping is limited by a poor ethanol recovery due to the trade-off between bubble residence time and stable bubble flow regime. Pervaporation, being the most promising concept for *in-situ* product removal, would be a cost-saving alternative to distillation for batch operation, but is limited by an unfavorable vapor-liquid equilibrium due to low bulk concentrations during continuous operations. *In-situ* product removal strategies do not exploit their full potential with ethanol, because ethanol is not toxic enough to cause considerable increases in productivity when withdrawn *in-situ*.

Further research should target the conduction of the CBP experiment at pilot scale to prove the scale-invariance rigorous model and thus, the reliability of the scale-up guideline. Other potential obstacles, which need to be overcome for industrial implementation of CBP, might be limited space for the membrane in the reactor and the low productivity. Therefore, investigations regarding other mixing mechanisms such as recirculation by pumping or the development of a stable thermophile consortium to accelerate hydrolysis with higher reactor temperatures might be valuable.

Recalling the urgent need to reduce GHG emissions to keep global warming below 1.5 °C, cost-efficient CBP of non-edible resources is a unique opportunity to secure the supply of chemicals such as ethanol, which must be seized as soon as possible since the technology maturity level is a crucial factor for ubiquitous implementation. When CBP of lignocellulose reaches industrial stage, further improvements should target the efficient conversion of the

substrate's carbon. Given the stoichiometric conversion of glucose to ethanol (7.1), it becomes clear that at least 1/3 of the available carbon is lost as  $CO_2$ .

$$C_6H_{12}O_6 \rightarrow 2 \cdot C_2H_6O + 2 \cdot CO_2$$
 (7.1)

Recalling the high water content of lignocellulosic biomass and the transport costs, a more efficient use of the carbon is unequivocal. The industrial potential of promising concepts such as the lactate platform could be evaluated in depth at moderate costs by adjusting the presented models to the biological pathways of other microorganisms.

# APPENDIX A

Supplementary material for chapter 2: Techno-economic assessment of consolidated bioprocessing of lignocellulose to ethanol at industrial scale

## A.1 Calculations for redimensioning

Calculation of the CAPEX and OPEX savings by CBP

In the base case, 2000 dry tons of corn stover per day are converted to ethanol. The costs per dry ton of feedstock are 48.53 \$ (31.75 \$ for the collection, transport and handling; 21.32 \$ for the feedstock itself). The pretreatment is a dilute acid-catalyzed steam explosion pretreatment. The pretreated slurry is conditioned with ammonia. After a residence time of 5 *days* for hydrolysis and fermentation, 271.3 *L* ethanol per dry ton feedstock are obtained (76 % yield). The final product concentration is 5.4 wt.% ethanol. The enzymes are produced by *T. reesei* and the fermentation is carried out by *Zymomonas mobilis*. The ethanol is recovered by means of a rectification (beer tower and a second distillation column) and adsorption. The beer stillage is separated from the lignin and sent to a wastewater treatment plant (WWT) together with the other waste streams of the process. Lignin and biogas from the anaerobic digestion in the WWT are burned to generate heat and electricity for the process. 0.48 kWh/annual L ethanol of excess electricity is sold to the grid. The calculated annual cost of capital account for 13.1 % of the CAPEX.

Applying the highest degree of process intensification, CBP, by merging enzyme production, hydrolysis and fermentation in one process step as well as the change in pretreatment yield cost savings in capital expenditure (CAPEX) as well as in OPEX. In this work, the saved costs are allocated either to CBP or to steam pretreatment. In general, CAPEX and variable OPEX underlie considerable changes when applying CBP and steam pretreatment whereas

the change of fixed OPEX is almost negligible. The change to CBP mostly affects the areas of enzyme production, hydrolysis and fermentation. CAPEX are saved due to a reduced need of apparatuses as a result of the process integration. Variable OPEX are reduced since no glucose is needed for enzyme production as the fungus metabolizes sugars released from the hydrolyzed feedstock. An experimentally confirmed cellulose-to-ethanol yield of 73 % including the fact that a fraction of the feedstock is consumed for the enzyme production was adapted to 76 % to ensure comparability given the uncertainty of different operation modes (batch vs. continuous), substrates (corn stover vs. pure cellulose), resources for enzyme-production (*in-situ* vs. *ex-situ*) and maturity levels of the technologies. Single yields of the pretreatment (yields of xyloses and glucan) and hydrolysis unit (pentose yield) were taken from the base case. Furthermore, the residence time of 5 *days* for hydrolysis and fermentation was kept constant. Since the enzyme concentration in a steady-state continuous operation stays constant over time (enzyme production equals the wash-out during steady-state), the residence time for enzyme growth in A 400 may be neglected.

The change from dilute acid-catalyzed steam pretreatment to pure steam pretreatment increases the CAPEX of the pretreatment area, because the apparatuses must withstand higher pressures. Variable OPEX are saved due to a strongly reduced use of chemicals, which results in a lower salt concentration in the downstream processing. Thus, the beer stillage is not sent directly to anaerobic digestion like in the base case, but to an evaporator cascade and a subsequent combustion of the obtained solids. Therefore, more electricity can be generated and sold, which reduced variable OPEX as well. An overview of the CAPEX changes presented in Tab. A.1.

The totals correspond to the total installed costs of each unit (next section for further details). The costs of a warehouse, site development and additional piping were determined as percentage of the inside battery limit (ISBL) costs according to the base case. ISBL denotes the total installed costs of the areas, where the actual process happens (A 200, 300, 400 and 500). The sum of the total installed costs and the costs for a warehouse, site development and additional piping give the total direct costs (TDC). Proratable expenses (includes fringe benefits, burdens, and insurance of the construction contractor), field expenses, home office & construction fee (includes engineering plus incidentals, purchasing, and construction), project contingency and other costs for start-up, permits etc. are functions of the TDC and were calculated according to the base case. Their sum plus the TDC yields the fixed capital investment (FCI). The total capital investment (TCI or CAPEX) consists of the FCI and the costs for land and working capital, which were calculated according to the base case as well.

Table A.1: Total Capital Investment (TCI) of the base case and consortium-based CBP derived from the total installed costs of all apparatuses.

table A.1.: Jotal Capital investment (1C1) of the base case and consortium-based CDF derived from the total installed costs of all apparate	the base case	e and consol	rtium-based (	br derived	rrom the total installe	ed costs of al	ı apparaı
	Base Case	Change due	Change due to pretreatment	Change due	Change due to consortium-based CBP	Sum of changes	anges
	abs. [ MM\$]	abs. [MM\$]	rel. [%]	abs. [MM\$]	rel. [%]	abs. [MM\$]	rel. [%]
Totals (excl. A 100)	232.22	34.50	14.86	-22.07	-9.50	244.65	5.35
ISBL (A 200- A 500)	105.28	19.60	18.62	-22.07	-20.96	102.81	-2.35
Warehouse (4 % ISBL)	4.21	0.78		-0.88		4.11	
Site Development (9 % of ISBL)	9.48	1.76		-1.99		9.25	
Additional Piping (4.5 % of ISBL)	4.74	0.88		-0.99		4.63	
Total Direct Costs (TDC)	250.64	37.93	15.13	-25.93	-10.35	262.64	4.79
Proratable Expenses (10 % TDC)	25.06	3.79		-2.59		26.26	
Field Expenses (10 % TDC)	25.06	3.79		-2.59		26.26	
Home Office & Construction Fee (20 % TDC)	50.13	7.59		-5.19		52.53	
Project Contingency (10 % TDC)	25.06	3.79		-2.59		26.26	
Other Costs (Start-Up, Permits, etc.) (10 % TDC)	25.06	3.79		-2.59		26.26	
Total Indirect Costs (TIC)	150.39	22.76	15.13	-15.56	-10.35	157.58	4.79
Fixed Capital Investment (FCI)	401.03	69.09	15.13	-41.49	-10.35	420.23	4.79
Land	1.85	0.00		0.00		1.85	
Working Capital (5% FCI)	20.05	3.03	15.13	-2.07	-10.35	21.01	4.79
Total Capital Investment (TCI/CAPEX)	422.93	63.72	15.07	-43.57	-10.30	443.09	4.77

Change in CAPEX for each unit of the base case scenario

This chapter covers the changes of the process layout for each apparatus in the single process areas. The base case is subdivided into 9 areas (Tab. A.2), which are referred to in the following.

Table A.2: Areas and their functions in the base case

A 100 Feedstock storage & handling

A 200 Pretreatment & conditioning

A 300 Enzymatic hydrolysis & fermentation

A 400 Cellulase enzyme production

A 500 Product, solids & water recovery

A 600 Wastewater treatment

A 700 Product & feed chemical storage

A 800 Combustor, boiler & turbogenerator

A 900 Utilities

**Area A 100: Feedstock storage & handling:** No changes were applied to the feedstock storage and handling since the same amount of feedstock is used and the composition of the corn stover is assumed to be identical. Furthermore, the apparatus of A 100 are not included in the CAPEX calculations identical to the base case. Feedstock purchase, storage and handling are pooled in a price of 48.53 \$/dry ton. [2]

Area A 200: Pretreatment & conditioning: The change from dilute acid catalyzed steam pretreatment to pure steam pretreatment results in changes of CAPEX and OPEX of A 200: All equipment for the addition of sulfuric acid and the conditioning of the pretreated slurry with ammonia were removed, resulting in cost savings of 1.87 % of the installed costs of A 200. The pH change due to autohydrolysis and its consequences will be discussed in the hydrolysis and fermentation unit (A300). However, to reach a similar pretreatment severity without adding sulfuric acid, the temperature must be increased from 158 °C to 180 °C (10 bar) in the first stage and 230 °C (28 bar) in the second stage, respectively. [58] To evaluate the cost of a high pressure apparatus based on the costs for low pressure apparatuses, Ulrich et al. proposed the multiplication of the installed costs with a pressure factor  $F_P$ =1.4 for pressures up to 11 bar and  $F_P$ = 2.5 for pressures up to 31 bar. [61] Thus, the change from 158 °C to 180 °C can be neglected in terms of installed costs since the vapor pressures of water at 158 °C and 180 °C

are in the same  $F_P$  range. However, the installed costs of the second stage pretreatment need to be increased by a factor of 1.79:

$$\frac{F_{P,CBP}}{F_{P,base\ case}} = \frac{2.5}{1.4} = 1.79\tag{A.1}$$

Applying this factor to the second stage pretreatment reactor, leads to higher installed costs of 7.9 MM\$. Subtracting the above-mentioned savings yields a net increase in total installed costs for A 200 of 7.26 MM\$ (+22 %), which corresponds to an 3.1 % increase of plant's total installed costs.

Area A 300: Enzymatic hydrolysis & fermentation: Since enzymatic hydrolysis and fermentation are conducted in the same reactor, the hydrolysis tank and the transfer pump from the hydrolysis tank to the fermenters are omitted. Furthermore, CBP is carried out continuously in contrast to the batch operation in the base case. Therefore, only 7 fermenters are needed instead of 12, since the batch-inherent downtime is avoided (The volumetric flow after the pretreatment of 221  $m^3/h$  multiplied with the residence time of 5 days gives a total necessary reactor volume of 26'500  $m^3$ , which corresponds to 7 fermenters with 3'785  $m^3$  each). This leads to cost savings of 14.9 MM\$ (47.7 %) of installed costs. The only extra equipment needed is the membrane and its support. The membrane support is modelled with the cost function of stainless-steel internal heating coil as the geometry and the mounting is comparable. [61] Each of the 7 membrane supports has a purchased equipment cost of 10'000 \$ based on the CEPCI from 2004. Applying the CEPCI from 2007 and an installation factor of 1.5 leads to installed costs of 138'000 \$ for the membrane support. Applying the specific membrane surface of 10  $m^{-1}$ , the total reactor volume of 26′500  $m^3$  demands 265′000  $m^2$  of membrane surface. Ulrich et al. propose 30-50  $\$/m^2$  total installed costs for membranes (based on CEPCI from 2004). [61] Since the membrane is made from PDMS,  $30 \text{ } \text{$^{/}m^2$}$  are assumed leading to total installed costs of 10.44 MM\$ for the membrane in 2007. The resulting net savings of total installed costs of A 300 are 4.31 MM\$ (13.8 %), which corresponds to 1.9 % savings of the plant's total installed costs.

Area A 400: Cellulase enzyme production: The cellulolytic enzyme cocktail is produced in-situ in the membrane reactor. Thus, all apparatus of A 400 can be omitted except the air compressor package and the nutrient pump, because these apparatuses are needed for CBP as well to supply the cellulolytic fungus with oxygen and nutrients. The resulting net savings of total installed costs of A 400 are 17.76 MM\$ (-97 %), which corresponds to 7.6 % savings of the plant's total installed costs.

**Area A 500: Product, solids & water recovery:** No changes were applied to the ethanol distillation and dehydration. However, the beer stillage (bottom of the first distillation column)

is new sent to a cascade of three evaporators, where the top outlet consists of recycling water and the bottom outlet consists of a combustible paste, which is sent to A 800, as it was proposed in the earlier NREL lignocellulosic bioethanol report from 2002. [63] In the base case, the beer stillage needs to be sent to anaerobic digestion of the wastewater treatment due to the high salt concentration resulting from the dilute acid pretreatment and the necessary pH adjustment. Since the salt concentration after the CBP will be much lower due to the pure steam explosion pretreatment, an earlier design case for a cellulosic ethanol plant published by NREL can be adopted. [63] All apparatuses dealing with the beer stillage are removed leading to savings on total installed costs of 6.84 MM\$. They are replaced with the beer stillage processing described in the previous base case leading to total installed costs (CEPCI from 2007) of 18.9 MM\$. The net increase of total installed costs for A 500 is 12 MM\$ (+54 %), which corresponds to 5.2 % savings of the plant's total installed costs.

**Area A 600: Wastewater treatment:** Because of the different processing of the beer stillage in A 500, the wastewater treatment (WWT) inlet flow is reduced to only 13.7 % of the base case. The WWT has a size exponent of 0.6. Thus, 13.7 % of the base case size lead to 30.3 % of the total installed costs, a reduction of 34.4 MM\$ (-69.7 %). This corresponds to 14.8 % savings of the plant's total installed costs.

Area A 700: Product & feed chemical storage: No changes were applied to A 700. The tanks for sulfuric acid and ammonia are not used for the pretreatment and conditioning, but for the pH regulation of the reactors. Thus, they might be oversized, but in the light of their negligible fraction of the total CAPEX it was decided to keep them at the current size.

Area A 800: Combustor, boiler & turbogenerator: Due to the pure steam explosion pretreatment, the sulfur concentration in the flue gas of the combustor is below the limit demanding flue gas desulfurization (FGD). [63] The costs for the FGD are however included in the combustion package in the base case. Therefore, cost functions from Turton (baghouse filter) [60] and Garrett (spray dryer absorber) [62] were taken to determine these costs without FGD. The equipment costs of the baghouse amount to 290'000 \$ with a CEPCI of 542 (2016). Considering an installation factor of 1.9, the installed costs are 534'000 \$ (CEPCI from 2007). The spray dryer absorber has purchased costs of 290'000 \$ with a CEPCI of 355 and an installation factor of 1.64 leading to installed costs of 703'888 \$ (CEPCI from 2007). Thus, the total installed costs reduction due to removal of the FGD apparatuses is 1.24 MM\$ (CEPCI from 2007). The remaining apparatuses of the combustion unit A 800 (64.72 MM\$) have to be scaled up by a factor of 2.8 since a larger fraction of the beer stillage is sent to combustion (cf. changes in A 500) resulting in an inlet flow, which is 2.8 times higher than in the base case. A size exponent of 0.6 is given for the combustion package in the base case. Scaling the combustion package up by a factor of 2.8 leads to an installed cost increase by a factor of 1.9. Thus, the net increase in

installed costs is 54.42 MM\$ (+82.5 %), which corresponds to a 23.4 % increase of the plant's total installed costs.

**Area A 900: Utilities:** The cooling tower system has a size exponent of 0.6 and needs to be scaled up by the same factor 2.8 as the combustor and boiler system due to the additional heat production. Apart from that, no changes were applied to A 900, since the same utilities are needed. This leads to an increase in total installed costs of 1.88 MM\$ (+27.3 %) for A 900, which corresponds to an 0.8 % increase of the plant's total installed costs.

Changes of OPEX

#### **Fixed OPEX**

The fixed OPEX consist of labor costs, maintenance, property insurance and tax. Maintenance (3 % of the inside battery limits (ISBL; Tab. A.1)) as well as property insurance and tax (0.7 % CAPEX are determined by the CAPEX and account for 6 MM\$, which corresponds to  $4.67 \, \varphi$ /annual L ethanol and an increase of 1 % compared to the base case.

The total labor costs account for 2.04 ¢/annual L ethanol in the base case. However, the base case provides little information about the allocation of workers to areas or apparatuses. Only the workers responsible for enzyme production are explicitly mentioned. Since A 400 could be omitted completely (the only exception is the compressor package and the pump), the costs for the shift operators for the enzyme production were not included in the present design. Despite massive apparatus reductions in A 300 and A 600, no further reductions of labor costs were applied, since it cannot be ensured that the increased number and size of apparatus in A 500 and A 800 do not compensate the reduced need of shift operators in A 300 and A 600. The cost per employed worker was kept constant. Thus, the total labor costs amount to 4.12 MM\$ per year, which corresponds to 1.78 ¢/annual L ethanol and a reduction of 12.5 %.

#### Variable OPEX

The variable OPEX consist of the costs for raw materials and disposal of waste streams minus the revenue for selling by-products. Since they are not projected over the lifetime of the plant, they can be directly expressed as costs per liter of ethanol as it is shown in Tab. A.3.

The greatest savings in variable costs come from the integration of the enzyme production in the main fermenter, as this allows the addition of glucose for enzyme production to be omitted. Furthermore, the change from acid-catalyzed steam pretreatment to pure steam explosion pretreatment avoids the use of chemicals during the pretreatment, which contributes substantially to the total raw material cost savings as well. Additional costs result from the need to exchange the membrane on a yearly base. [61] Pure steam pretreatment results in a higher steam demand of  $1'460 \ kg/h$  ( $800 \ kW$ ), which is provided at no additional OPEX, because the

Table A.3: Comparison of the raw material costs between the base case and the case employing consortium-based CBP with steam explosion pretreatment.

picar	or carrier.			
Unit	Raw material/ feed chemical	Costs Base case $\lceil \epsilon / \text{annual } L \text{ ethanol} \rceil$	Costs This work $\lceil \varphi / \text{annual } L \text{ ethanol} \rceil$	Note
				21.32 \$/ton feedstock price
A 100	Feedstock	19.57	19.57	31.75 \$/dry ton total costs for collection,
				processing, storage and transportation
A 200	Sulfuric acid	0.65	0.00	No need for chemicals during steam
				exprosion pretreatment The reduced amount of ammonia necessary to
	Ammonia	1.72	0.00	condition the steam pretreated slurry due to autohydrolysis is negligible
				$(0.00172  \epsilon/\text{annual}  L  \text{ethanol})$
A 300	CSL	0.24	0.24	The same media consumption for the fermenting microorganism is assumed
	Diammonia phosphate	0.51	0.51	
	Sorbitol	0.18	0.00	Sorbitol is used to accelerate the metabolism of Z mobilis it is not necessary for S. coronisiae [176]
	Membrane	0.00	0.05	The membrane is assumed to be exchanged every year at 30 $\%/m^2$ [61]
				Glucose is not needed for enzyme production
A 400	Glucose	5.11	0.02	since the enzyme producer consumes part of the hydrolyzed feedstock during CBP. 0.02 $\epsilon$ /annual $L$ ethanol reflect the additional substrate costs
				for growing the microbial biomass after yearly maintenance
	CSL	0.03	0.03	Other media consumption of the enzyme producer is assumed to be the same as in the base case
	Ammonia	0.19	0.19	
	Host nutrients	0.20	0.20	
	Sulfur dioxide	0.02	0.02	
A 600	NaOH	1.23	0.00	NaOH is used in the base case to flush the fermenters between each batch, which becomes needless for continuous CRP A little amount of NaOH is
				necessary for sterilization after yearly maintenance
A800	Boiler chemicals	0.00	0.01	The scale-up by a factor of 2.8 affects linearly the raw material consumption in A 800 (2.8*0.0045)
	Feedstock	0.00	0.00	No feedstock needs to be added for stable combustion
	FGD lime	0.65	0.00	No lime is used since FGD is not needed
A900	Cooling tower chemicals	0.03	0.03	
	Makeup water	0.14	0.14	
Total		30.46	21.02	The reduction of 31.1 % of the total var. OPEX is achieved by the change in pretreatment (10.1 %) and the switch to consortium-based CBP (21 %)

up-scaled combustor and boiler system delivers 2.8 times the heat energy  $(46'000 \ kW)$  of the base case, which is sufficient to supply the additional steam needs.

The only waste stream in the base case, which must be landfilled, is the ash from FGD. As FGD can be omitted, these  $0.66 \ \epsilon/\text{annual} \ L$  ethanol are saved in this case due to the change in pretreatment.

One-third of the total reduction of variable OPEX of 31.1 % comes from the switch of the pretreatment and two-thirds from the use of consortium-based CBP. The excess electricity generated by the combustion of lignin (8.8 % of the corn stover's LHV) is a by-product, which is sold to the grid. In the base case, 12'814~kW of excess electricity are produced. The scale-up of the combustor will lead to an excess electric power of 36'000~kW, leading to revenues of 7.32~c/annual L ethanol. The unused heat (44 % of the corn stover's LHV) is released to the atmosphere due to the remote location of the plant analogous to the base case. 6.8~% and 0.9~% of the corn stover's LHV are used for process electricity and process heat, respectively. 39.5~% of the corn stover's LHV are stored in the produced ethanol.

Concluding, the total variable OPEX per annual liter of ethanol for CBP amount to 13.84  $\phi$ /annual L ethanol instead of 28.46  $\phi$ /annual L ethanol in the base case, which corresponds to a reduction of 51.37 %.

#### Additional remarks regarding the calculations of the sensitivity analysis:

- Change of the process layout at small scales:
  - 1. The size exponent of the hydrolysis and fermentation unit A 300 was changed from 1 to 0.6. Above 10 % of the base case scale, the fermenters are scaled up by parallelizing, which gives a size exponent close to 1. Below 10 %, the remaining reactors become smaller, which can be scaled with a size exponent of 0.6. [60]
  - 2. Also, below 10 % the costs for combustion and boiler unit reach their minimum size. Further downsizing is not possible with the fuel, i.e. moist lignin, given by the process. [62] Thus, the installed costs of these apparatuses are kept constant for smaller scales.
  - 3. Below 5 % of the base case scale, the WWT unit cannot be further downscaled [177] and it becomes economically favorable to send the whole beer slurry to the WWT. Thus, the WWT works to capacity and the CAPEX savings of omitting the combustion and boiler unit overcompensate the loss of electricity revenues assuming, that steam and disposal of waste can be purchased at market prices (60 \$/ton steam and 31  $e/m^3$  waste water). [61–63]
- Change of feedstock costs with scale:

Assuming, that the feedstock is collected in a circle around the production site, leads to a linear relationship between the plant size and the areal size of the circle, where the feedstock is collected. But the transport distance (directly proportional to the radius of the circle) scales with a factor of  $1/\sqrt{2}$  to the area. Thus, a half-sized plant would require a half-sized circular area for the collection of feedstock, but the transportation distance would only be reduced to 71 %.

• Correlation of yield and feedstock price:

Neglecting the resizing of apparatus in the units A100-400 due changes in yield for a moment, a yield of 96 % and 56 % instead of 76 % corresponds to 79 % and 136 %, respectively, of the total feedstock costs. Recalling the 30 % MESP share of the feedstock costs explains the strong sensitivity towards the yield.

• Assumptions concerning the MESP sensitivity with the PPP:

It is assumed, that the CAPEX are not affected by the PPP although the possibility of considerable CAPEX differences depending on the plant location is reported in literature. [178] However, the assumption is justified by three reasons:

- 1. There is little price index data from other countries (only from the Netherlands, Germany, South Africa and Canada)
- 2. Some of the needed apparatus (i.e. the steam pretreatment unit A 200) are manufactured only by a very limited number of companies worldwide (and thus they are not object to local trading)
- 3. A conversion of currencies, which is said to be the most important factor of local CAPEX differences, is not necessary in this work due to the dominance of the US\$ as international currency in apparatus pricing. [179,180]

#### Calculation of cost changes with varying titer, yield, residence time and capital charge rate

• Ethanol titer 5 (7) wt.% vs. 5.4 wt.%:

The titer influences only the purification unit A 700. Cysewski et al. reported the distillation costs at different weight fractions of sugar in the fermentation feed for a total ethanol production of 90'000 L ethanol/d. [181] Considering a fermentation yield of 95 % of the theoretical limit (0.51 g ethanol/g glucose) leads to 14.5 wt.% glucose concentration for 7 wt.% ethanol titer and 11.1 wt.% glucose concentration for 5.4 wt.% ethanol titer resulting in 0.79  $\phi/L$  ethanol and 0.71  $\phi/L$  ethanol separation costs, respectively. Applying the size exponent of 0.67 for distillation columns [60] and the CEPCI from 2007, a cost difference of 0.8  $\phi/L$  ethanol is found. The difference in distillation costs per liter ethanol

corresponds to a total cost (MESP) difference of 1.39 %. Furthermore, the cascade of the three evaporators for the beer stillage can be smaller for higher titers since less water leaves the beer tower bottom. The difference in titer causes a 1.84 % lower flow inlet. This results in 1.51 % lower total installed costs based on the size exponent of 0.68 for the evaporators. [63] 1.51 % lower total installed costs result in 2.98 % TCI reduction, which corresponds to a 1.26 % MESP reduction. Furthermore, the TCI reduction results in lower fixed OPEX (reduction of maintenance, insurance and tax expenses). The 2.98 % lower TCI lead to a 0.22 % MESP reduction due to lower fixed OPEX.

Concluding, it can be stated, that 1.26 %+1.39 %+0.22 %=2.87 % of additional cost savings can be realized if the titer is increased from 5.4 wt.% to 7 wt.%. Analogue it can be stated that the titer reduction from 5.4 wt.% to 5 wt.% reduces the cost savings by 0.72 %. Thus, the cost savings reported by Lynd et al. exclude 0.72 % of cost savings due to a higher titer in the base case. [3]

#### • Yield 398.6 *L* ethanol/dry US ton vs. 299 *L* ethanol/dry US ton:

A higher yield with constant ethanol titer demands less feedstock. Thus, feedstock costs can be saved and all apparatuses in A 200 and 300 become cheaper because they are smaller since less inlet flow is necessary for the same ethanol titer. Due to better conversion of the feedstock, less revenues are gained with excess electricity since less feedstock is consumed in general and thus, less lignin is available for combustion.

A yield increase by a factor of 1.3291 (=398.6 L ethanol/299 L ethanol) leads to the same ethanol output with 75.24 % of the feedstock. 24.73 % feedstock reduction results in 8.52 % MESP reduction as a consequence of lower feedstock and handling cost. The cost saving due to smaller apparatuses are calculated with weighted size exponents for A 200 and 300. The weighted size exponents were obtained by averaging the size exponents of one unit weighing the with the total installed cost of the corresponding equipment (eq. A.2).

weighted size exp. 
$$\bar{n} = \frac{\sum_{i} n_{i} * \text{ installed costs }_{i}}{\sum_{i} \text{ installed costs }_{i}} = \begin{cases} 0.608 \text{ for } A200 \\ 0.856 \text{ for } A300 \end{cases}$$
 (A.2)

A flow reduction of 24.73 % of the processing stream due to higher yield leads to an FCI reduction of 2.85 %, which corresponds to a MESP reduction of 1.20 %. Furthermore, changes of the fixed OPEX savings (because the fixed OPEX are coupled with the CAPEX) due to lower maintenance, insurance and tax costs as well as the lost revenue from excess electricity have to be considered. The flow reduction causes an MESP increase of 1.24 % due to less electricity whereas the fixed OPEX savings yield a MESP decrease of 0.23 %. Concluding, it can be stated, that 8.52 %+1.20 %-1.24 %+0.23 %=8.71 % of the cost savings reported by Lynd et al. are due to the higher yield. [3]

#### • Residence time 1.5 *d* vs. 5 *d*:

The reduction of the residence time during hydrolysis and fermentation only affect the CAPEX of A 300 as neither the pretreatment nor the post-processing is affected by faster reaction rates. The reduction of the residence time by 70 % yields a size reduction of 70 % for all apparatuses in A 300. Considering the weighted size exponent of 0.856 for A 300, a size reduction of 70 % leads to a reduction of installed costs of 64.3 %, which corresponds to 20.08 MM\$, a TCI reduction of 7.98 % and a MESP reduction of 3.37 %. 0.6 % of fixed OPEX (maintenance, insurance and taxes) are reduced due to the lower CAPEX requirements.

Concluding, it can be stated, that 3.37 % + 0.6 % = 3.97 % of the cost savings reported by Lynd et al. are due to the lower residence time. [3]

• Capital charge rate 16.7 % vs. 13.1 %:

Due to varying equity shares, interests on equity and debts, Lynd et al. calculate with a capital charge rate of 16.7 % whereas the base case assumes 13.1 %. The capital charge rate of Lynd et al. is higher by a factor of 1.2748 (= 16.7 %/13.1 %) and affects the capital costs, which account for 42.2 % of the total costs.

Thus, it can be stated that the cost savings reported by Lynd et al. exclude 11.6 % of cost savings due to a lower capital charge rate in the base case [3]

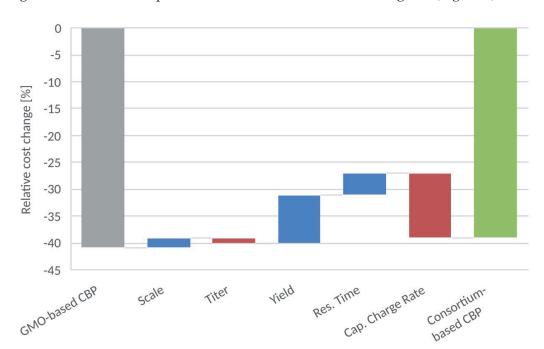
#### A.2 Calculations GMO-based CBP

#### Adaption of published GMO-based CBP cost data to input parameters of the base case

The published data of GMO-based CBP normalized to the same feedstock and the same process condition as in the base case. The different input parameters are depicted in Tab. A.4.

Table A.4: Differences between the process assumptions of Lynd et al., the base case and this work. Values in brackets denote values of different scenarios published by Lynd et al. [3]

Parameter	Lynd et al. [3]	Base case	This work
Scale [dry ton feedstock/d]	4536 (2000)	2000	2000
Ethanol titer [wt.%]	5 (7)	5.4	5.4
Yield	439.4	329.6	329.6
[L ethanol/dry ton feedstock]	137.1	32).0	327.0
Residence time [d]	1.5	5	5
Pretreatment	AFEX	Dilute acid catalyzed	Steam explosion
Tetreatment	THEA	steam explosion	Steam explosion
Capital charge rate [%]	16.7	13.1	13.1



The single normalization steps are illustrated with a waterfall diagram (Fig. A.1).

Figure A.1: Waterfall diagram depicting the normalized cost savings through GMO-based CBP published by Lynd et al. [3] The grey bar represents the published cost savings. The red and blue bars represent extra cost savings or reduced cost savings due to adapted titer, yield, residence time and capital charge rate, respectively. The green bar represents the resulting cost saving after applying the adaptions.

Lynd et al. published cost savings of 41 % when GMO-based CBP is applied (grey bar in Fig. A.1). [3] The titer is lower and the capital charge rate is higher than in the base case. Increasing the titer and lowering the capital charge rate to match the base case conditions leads to higher cost savings than published (red bars in Fig. A.1). In contrast, lowering scale as well as yield and increasing the residence time to match base case conditions reduce the published cost savings (blue bars in Fig. A.1). In conclusion, the beneficial and disadvantageous effects almost compensate each other so that the final cost savings of GMO-based CBP (green bar in Fig. A.1) at base case conditions account for 39 % (Supplementary material A.1). The pretreatment was excluded from this calculation, because detailed cost data for the ammonia fiber expansion (AFEX) pretreatment at industrial scale with the conditions assumed by Lynd et al. are not available. However, it seems unlikely, that part of the reported cost savings are realized with the different pretreatment method used given the necessity to use elevated pressures and the use of ammonia. [31]

Furthermore, Lynd et al. report cost savings of 5.5 % when increasing the ethanol titer from 5 wt.% to 7 wt.%. This work obtains cost savings of 3.6 % for the same titer increase

(Supplementary material A.1). 25 % total cost savings are reported by omitting the pretreatment, whereas in the base case 13.4 % of the total costs are allocated to the pretreatment. [3] Thus, levelling the cost savings of 39 % published by Lynd et al. with the ratio 3.6 %/5.5 % or the ratio 13.4 %/25 % in order to have equal impact on the costs by equal technological advance (i.e. applying CBP) yields cost savings of 25.5 % and 21 %, respectively.

## A.3 Apparatus list of the base and CBP

Year of Quote         Scaling Variable         Scaling Exp         Inst Factor         Size Ratio         Scaled Purch           2009 Mass flow         0.6         1,7         1,1         \$5,5           2009 Mass flow         0.6         1,7         1,1         \$6,5           2009 Mass flow         0.6         1,7         1,1         \$8,5           2009 Mass flow         0.6         1,7         1,1         \$8,4           2009 Mass flow         0.6         1,7         1,1         \$8,4           2009 Mass flow         0.6         1,7         1,1         \$1,4           2009 Mass flow         0.6         1,7         1,1         \$1,4           2009 Mass flow         0.6         1,5         1,1         \$1,4           2009 Mass flow         0.6         1,5         1,1         \$1,4           2009 Mass flow         0.6         1,5         1,1         \$1,4           2009 Mass flow         0.6         1,	Scaled Purch Cost \$5,714,628 \$3,225,265 \$316,474	Purch Cost in Proj year Inst Cost in Proj year \$8,752,952 \$92	Inst Cost in Proj year (CBP) \$9.780.018	
Transfer Conveyor   2   85,85700    2009  Mass flow   0.6   1.7   1.1   55	<b>ж</b>			
MACHICIDED   Mass flow   0.6   1.7   1.1   5.5	₩ ₩			
Interpretate   1	<i>8</i>			
Figure   F	iii			
Transfer Conveyor		\$3,246,895 \$5,519,721	21,819,721	
Transient Conveyor   1   INCLUDED				
Percentage   Per				
Strong				
Percentage   Contemporary   Contem		\$117.255	33	
Secretarian				
Section   Storage Dame   2   \$5,500.00   \$2000   Mass flow   0.6   1.7   1.1   \$5.5				
Second Parison   Control Par	8	S	Š	
Comparison   Com				
NUM RECO    Sealed tris tabled   Scaling Variable   Scaling Exp   Inst Factor   Size Ratio   Scaled Purc   Size Ratio	0,		13 \$507,213	
Scaled Instituted   Scaling Instituted   Scaling Variable   Scaling Exp   Inst Factor   Size Ratio   Scaled Pure   Section	\$14,114,178	\$14,208,831 \$24,155,013	\$24,155,013	no changes were applied in A-100
NUM REQD   Scaled Installed   Scaling Variable   Scaling Fac   Scaling Pack   S				
NUM REQD   \$   Vear of Oducte   Scaling Variable   Scaling Perp   Inst Factor   State Part   Scaled Purc   Scale			Adjustments due to CBP	Comments regarding adjustments
1   SSC 000   All Ass flow   0.5   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   1   0.28   0.28   1	Scaled Purch Cost	Purch Cost in Proj year Inst Cost in Proj year	Inst Cost in Proj year (CBP)	
1 NOLLUDED   2009 Mass flow   0.5   1.5   1.11	0.28 \$3,202	\$3,223		\$0 Omitted since no acid is used in the pretreatment
3         \$80,000         2009 Mass flow         0.5         1.5         1.1           1         \$82,000         2009 Mass flow         0.5         1.5         1.15           1         \$82,000         2009 Mass flow         0.5         1.5         1.05           2         INCLUDED         2009 Mass flow         0.5         1.5         1.05           2         INCLUDED         2009 Mass flow         0.5         1.5         1.05           1         INCLUDED         1.0         1.0         1.0         1.0           1         INCLUDED         2.0         1.0         2.2         1.15         1.15           1         INCLUDED         2.0         1.0         2.2         1.15         1.0         1.0           2         INCLUDED         2.0         1.0         2.0         1.0         2.2         1.15         1.0           2         INCLUDED         2.0         1.0         2.0         1.0         2.2         2.2         2.3         1.0           2         INCLUDED         2.0         2.0         2.0         2.0         2.0         2.0         2.0         2.0         2.0         2.0         2.0         <				
1   \$80,000   \$2009 Mass flow   0.5   1.5   1.11     1   \$8,000   \$2009 Mass flow   0.5   1.5   1.05     1   \$8,000   \$2009 Mass flow   0.5   1.5   1.05     2			\$142	
1   \$5,000   \$2,000   Mass flow   0.5   1.5   1.05     1   \$6,000   \$2,000   Mass flow   0.5   1.5   1.05     2   NOLLUDED		\$95,276 \$142,914	\$142,914	
1 SS,000				Omitted since no acid is used in the pretreatment
1 NOLLUDED   NOLLUDE		2,2		\$0 Omitted since no acid is used in the pretreatment
NOLLUDED		80	80	
MINITIDED   MINI				
1   NOLLUDED   NOLLU				
1   NOLLUDED   NOLLU				
1 NOLLUDED   1 NOLLUDED   1 SE2200   1 SE2				
1   NiCLUDED   2010   Heatt duty   0.7   2.2   1.15     1   \$\$4,000   2009   Heatt duty   0.7   2.2   3.98     2   NiCLUDED   2009   Heatt duty   0.7   2.2   3.98     2   NiCLUDED   2009   Misss flow   0.8   1.5     3   \$\$19,812,400   2009   Misss flow   0.8   2.3   0.51     1   \$\$2,500   2009   Misss flow   0.8   2.3   1.36     1   \$\$2,500   2009   Misss flow   0.8   2.3   1.36     1   \$\$2,500   2009   Misss flow   0.8   2.3   1.36     1   \$\$2,500   2009   Misss flow   0.8   2.3   1.07     1   \$\$2,500   2009   Misss flow   0.8   2.3   1.07     1   \$\$35,000,000   2009   Misss flow   0.8   2.3   1.07     1   \$\$35,000,000   2009   Misss flow   0.8   2.3   1.07     1   \$\$35,000,000   2009   Misss flow   0.7   3   1.3     1   \$\$35,000,000   2000				
1   \$\$2,000   \$2.00				
1   1   1   23,000   2,000		\$97,091 \$213,600		
2   INCLUDED		\$89,946	80 8197,880	
1				
INCLUDED   INCLUDED   INCLUDED   INC				
2         INCLUDED         NACUUED         NACUUED         NACUUED         1         \$1 </td <td></td> <td></td> <td></td> <td></td>				
2         INCLUDED         2009 Mass flow         0.6         1.5         1         \$19           1         \$519502400         2009 Mass flow         0.8         2.3         0.53         1           1         \$5500         2009 Mass flow         0.8         2.3         1.1           1         \$5500         2009 Mass flow         0.8         2.3         1.3           1         \$52,00         2009 Mass flow         0.8         2.3         1.0           1         \$22,00         2009 Mass flow         0.8         2.3         1.0           1         \$500,000         2009 Mass flow         0.8         2.3         1.07           1         \$500,000         2009 Mass flow         0.8         2.3         1.07           1         \$500,000         2001 Mass flow         0.7         1.7         0           1         \$6,000         2001 Mass flow         0.7         3         1				
3   \$19.812,400   2000  Musse flow   0.6   1.5				
1 \$8,000 2009 Mass flow 0 0.8 2.3 0.53     1 \$25,000 2009 Mass flow 0.8 2.3 1.36     1 \$25,000 2009 Mass flow 0.8 2.3 1.36     1 \$5,000 2009 Mass flow 0.8 2.3 1.07     1 \$5,000 2009 Mass flow 0.8 2.3 1.07     1 \$5,000,000 2009 Mass flow 0.8 2.3 1.07     1 \$5,000,000 2009 Mass flow 0.7 3 1.07     1 \$6,000 2009 Mass flow 0.7 3 1.07     1 \$6,000 2009 Mass flow 0.7 3 1.00     1 \$6,000 2009 Mass flow 0.00	\$18	\$29	\$37,817973	\$37,817973 Increased price due to higher pressure duty
1   \$5,000,000   \$2,000   Mass flow   0.0   2.3   1.36			\$000	Omitted since no acid is used in the pretreatment
1 SYSTATION   2010   Marse frow   0.0   2.3   1.30   1.3				
1   \$52,500   2009 Mass flow   0.8   2.3   1.07		\$30,049 \$16,630 \$18,346	360,092	
1   SS.000.000   2009 Mass flow   0.8   2.3   1.07   1.07   1.17   0.9   1.07   1.17   0.9   1.07   1.17   0.9   1.07   1.17   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9   1.07   0.9			2,000	\$0 Omitted since no acid is used in the pretreatment
\$35,000,000 2009 Mass flow 0.7 1.7 0 86,210 20.10 Mass flow 0.7 3 1 \$66,210				
1 \$6,210 2010 Mass flow 0.7 3 1 56,				
	1 \$6,209	\$5,937 \$17,810		\$0 Omitted since no acid is used in the pretreatment
1 INCLUDED Tank				
1 \$511,000 2009 Mass flow 0.7 2 1.11	1.11 \$548,271	\$551,948 \$1,103,895	\$1,103	
nk 1 \$203,000 2000 Mass flow 0.7 2 1.11			\$438,6	
Administration and 1 \$2.26,000 2.009 Mass flow 0.7 2 1.05 \$243,670 0.000 Mass flow 0.000 Mass		\$245,304 \$490,609		SU Omitted since no acid is used in the pretreatment
COLI Z I.U Wass now Oct II.	0.00	06 100 000	170 07 4	

Mechanical Equipment List Area			Scaled Installed								Adjustments due to CBP	Comments regarding adjustments
EQUIPMENT TITLE	NUM REQD \$		Year of Quote	Scaling Variable	Scaling Exp	Inst Factor S	ize Ratio Sc.	aled Purch Cost	Purch Cost in Proj year	Inst Cost in Proj year	uote Scaling Variable   Scaling Exp   Inst Factor   Size Ratio   Scaled Purch Cost   Purch Cost in Proj year   Inst Cost in Proj year (CBP)	
Ethanol Fermentor Agitator	-	\$52,500	2009	2009 Size fermenter	-	1.5	12	\$630,000	\$634,225	5 \$951,337		\$554,947 7/12 of the size due to reduced number of fermentors
Seed Hold Tank Agitator	- 1	\$31,800		2009 Mass flow	0.5	1.5	1.05	\$32,651	\$32,870	0 \$49,305	\$49,306	
4th Seed Vessel Agitator	2	\$26,000		2009 Size fermenter	0.5	1.5	-	\$26,000	\$26,174	\$39,262	\$39,263	
5th Seed Vessel Agitator	2	\$43,000		2009 Size fermenter	0.5	1.5	+	\$43,000	\$43,286	8 \$64,933	\$64,934	
Beer Surge Tank Agitator	2	\$68,300		2009 Mass flow	0.5	1.5	1.06	\$70,265	\$70,737	\$106,105	\$106,106	
Enzyme-Hydrolysate Mixer	-	\$109,000		2009 Mass flow	0.5	1.7	1.17	\$117,751	\$118,540	0 \$201,519	\$201,520	
Ethanol Fermentor	12	\$10,128,000	2009	2009 Mass flow/Scale	-	1.5	+	\$10,128,000	\$10,195,921	1 \$15,293,882		\$8,921,432 Continuous operation allows 7 instead of 12 fermentor
Membrane	7			Size fermenter							\$138,000	
Membrane support construction	7			Size fermenter							\$10,440,000	
1st Seed Fermentor	2	\$75,400	2009	2009 Size fermenter	0.7	1.8	1	\$75,400	\$75,906	\$136,630	\$136,631	
2nd Seed Fermentor	2	\$116,600		2009 Size fermenter	0.7	1.8	-	\$116,600	\$117,382	2 \$211,288	\$211,289	
3rd Seed Fermentor	2	\$157,600		2009 Size fermenter	0.7	1.8	+	\$157,600	\$158,657	7 \$285,582	\$285,583	
4th Seed Fermentor	2	\$352,000	2009	2009 Size fermenter	7.0	2	1	\$352,000	\$354,361	1 \$708,721	\$708,722	
5th Seed Fermentor	2	\$1,180,000		2009 Size fermenter	0.7	2	-	\$1,180,000	\$1,187,913	3 \$2,375,827	\$2,375,828	

Table A.5: Apparatus list of the base and CBP

r-ermentation Cooler	7.	\$26,928		Z009 Heat duty	-	7.7	-	\$26,928	LLC'/8\$	\$2,524 \$192,524	\$26,281\$	
Hydrolyzate Cooler	-	\$85,000		2010 Heat duty	0.7	2.2	1.3	\$101,972	897,500	\$214,500	\$214,501	
4th Seed Fermentor Coil	-	INCLUDED										
5th Seed Fermentor Coil	-	INCLUDED										
Fermentor Batch Cooler	F	\$23,900	L	2009 Heat duty	0.7	1.8	0	0\$	0\$	0\$	\$1	
Fermentation Recirc/Transfer Pump	5	\$47,200		2009 Size fermenter	8.0	2.3	-	\$47,200	\$47,517	\$109,288	\$109,289	
Seed Hold Transfer Pump	-	\$8,200		2009 Mass flow	8.0	2.3	66.0	\$8,117	\$8,172	\$18,795	\$18,796	
Seed Transfer Pump	2	\$24,300		2009 Mass flow	8:0	2.3	66.0	\$24,055	\$24,217	\$55,698	\$55,699	
Beer Transfer Pump	1	\$26,800		2009 Mass flow	8.0	2.3	0.92	\$25,120	\$25,289	\$58,165	\$58,166	
Saccharification Transfer Pump	2	\$47,200		2009 Mass flow	8.0	2.3	1.05	\$49,125	\$49,455	\$113,746	0\$	\$0 Omitted due to CBP
Seed Hold Tank	-	\$439,000		2009 Mass flow	7.0	1.8	1.05	\$455,540	\$458,595	\$825,471	\$825,472	
Beer Storage Tank	1	\$636,000		2009 Mass flow	2.0	1.8	1.06	\$661,768	\$666,206	\$1,199,170	\$1,199,171	
Saccharification Tank	8	\$3,840,000		2009 Mass flow	7.0	2	1.05	\$3,976,717	\$4,003,386		0\$	\$0 Omitted due to CBP
			Area 300 Totals					\$18,365,811	\$18,484,821	\$31,218,520	\$26,908,520	
Mechanical Equipment List Area			Scaled Installed							_	Adjustments due to CBP	Comments regarding adjustments
EQUIPMENT TITLE	NUM REQD \$		Year of Quote	ote Scaling Variable	Scaling Exp	nst Factor Size	e Ratio Sc.	aled Purch Cost	Scaling Exp Inst Factor Size Ratio Scaled Purch Cost Purch Cost in Proj year	Inst Cost in Proj year In	آ ا	
Cellulase Fermentor Agitators	-	\$580,000		2009 Size fermenter	-	1.5	6	\$5,220,000	\$5,255,007	\$7,882,510	0\$	\$0 Omitted due to CBP
Cellulase Fermentor Agitators	1	\$3,420		2009 Size fermenter	1	1.5	4	\$13,680	\$13,772	\$20,658	0\$	\$0 Omitted due to CBP
Cellulase Fermentor Agitators	-	\$63,000		2009 Size fermenter	1	1.5	4	\$252,000	\$253,690	\$380,535	0\$	\$0 Omitted due to CBP
Cellulase Fermentor Agitators	-	\$11,000		2009 Size fermenter	-	1.5	4	\$44,000	\$44,295	\$66,443	0\$	\$0 Omitted due to CBP
Media-Prep Tank Agitator	-	\$8,500		2009 Mass flow	9:0	1.5	0	0\$	0\$	0\$	0\$	\$0 Omitted due to CBP
Cellulase Nutrient Mix Tank Agitator	1	\$4,800		2009 Mass flow	0.5	1.6	1.29	\$5,446	\$5,482	\$8,772	0\$	\$0 Omitted due to CBP
Cellulase Hold Tank Agitator	1	\$26,900		2009 Mass flow	0.5	1.5	1.27	\$30,266	\$30,469		\$0	\$0 Omitted due to CBP
Cellulase Fermentor	-	\$400,500		2009 Scale	-	2	6	\$3,604,500	\$3,628,673	\$7,257,345	0\$	\$0 Omitted due to CBP
1st Cellulase Seed Fermentor	1	\$46,000		2009 Scale	1	1.8	4	\$184,000	\$185,234	\$333,421	0\$	\$0 Omitted due to CBP
2nd Cellulase Seed Fermentor	1	\$57,500		2009 Scale	1	1.8	4	\$230,000	\$231,542	\$416,776	0\$	\$0 Omitted due to CBP
3rd Cellulase Seed Fermentor	1	\$95,400		2009 Scale	1	1.8	4	\$381,600	\$384,159	\$691,486	0\$	\$0 Omitted due to CBP
Cellulase Fermentation Cooler	-	INCLUDED										Omitted due to CBP
Media Prep Tank Cooler	-	INCLUDED										Omitted due to CBP
Fermenter Air Compressor Package	2	\$350,000		2009 Mass flow	9.0	1.6	0.98	\$346,282	\$	\$557,767	\$557,768	\$557,768 Kept for air circulation in A300
Cellulase Transfer Pump	1	\$7,357		2010 Mass flow	0.8	2.3	1.03	\$7,549	\$7,218		\$0	\$0 Omitted due to CBP
Cellulase Seed Pump	4	\$29,972	2010	2010 Mass flow	8:0	2.3	1.13	\$33,045	\$31,596	\$72,670	0\$	\$0 Omitted due to CBP
Media Pump	1	\$7,357		2010 Mass flow	8.0	2.3	0	\$0	0\$	0\$	0\$	\$0 Omitted due to CBP
Cellulase Nutrient Transfer Pump	-	\$1,500		2009 Mass flow	8:0	2.3	0.49	\$852	\$858	\$1,974	\$1,974	\$1'974 Kept for nutrient addition in A300
Cellulase Feed Pump	-	\$1,500		2009 Mass flow	8.0	2.3	0.76	\$4,584		09	0\$	\$0 Omitted due to CBP
Anti-foam Pump	-	\$1,500		2009 Mass flow	8.0	2.3	1.26	\$1,805	\$1,817	\$4,179	\$0	\$0 Omitted due to CBP
SO2 Storage Tank	1	\$0										Omitted due to CBP
Media-Prep Tank	-	\$176,000		2009 Mass flow	0.7	1.8	0	\$0	0\$	0\$	\$0	\$0 Omitted due to CBP
Cellulase Nutrient Mix Tank	-	000'6\$		2010 Mass flow	0.7	3	-	\$9,000			\$0	\$0 Omitted due to CBP
Cellulase Hold Tank	-	\$248,070		2009 Mass flow	0.7	1.8	1.27	\$292,589	\$294,551	\$530,192	\$0	\$0 Omitted due to CBP
			- 400 T-4-1-					540,000 407	007 001 070	001 000 010	771 0440	_

Mechanical Equipment List Area			Scaled Installed								Adjustments due to CBP	Comments regarding adjustments
EQUIPMENT TITLE	NUM REQD			Scaling Variable	Scaling Exp	Inst Factor	Size Ratio St	Inst Factor Size Ratio Scaled Purch Cost F	Purch Cost in Proj year	Inst Cost in Proj year	Inst Cost in Proj year (CBP)	
Filtrate Tank Agitator	1	\$26,000	2009	2009 Mass flow	9.0	1.5	1.05	\$26,669	\$26,848	\$40,272	78	\$0 Replaced by NREL 2002 water recovery
Lignin Wet Cake Conveyor	-	\$70,000	2009	2009 Mass flow	8.0	1.7	1.28	\$85,082	\$85,653	\$145,610		\$0 Replaced by NREL 2002 water recovery
Lignin Wet Cake Screw	-	\$20,000	2009	2009 Mass flow	8.0	1.7	1.28	\$24,309	\$24,472	\$41,603		\$0 Replaced by NREL 2002 water recovery
Beer Column	-	\$3,407,000	2009	2009 Mass flow	9.0	2.4	96.0	\$3,327,914	\$3,350,232	\$8,040,557	\$8,040,5	
Rectification Column	-	INCLUDED										
Beer Column Reboiler	1	INCLUDED										
Rectification Column Reboiler	1	INCLUDED										
Beer Column Condenser	-	INCLUDED										
Rectification Column Condenser	-	\$487,000	2010	2010 Mass flow	9.0	2.8	-	\$486,746	\$465,399	\$1,303,116	\$1,303,117	
Beer Column Feed Interchanger	-	INCLUDED										
Molecular Sieve Package (9 pieces)	-	\$2,601,000	2009	2009 Mass flow	9.0	1.8	96'0	\$2,540,057	\$2,557,091	\$4,602,764	\$4,602,765	
Pressure Filter Pressing Compr	1	\$75,200		2009 Mass flow	9'0	1.6	1	\$75,245	\$75,750	\$121,199	\$121,200	
Pressure Filter Drying Compr	2	\$405,000	2009	2009 Mass flow	9.0	1.6	66.0	\$402,453	\$405,152	\$648,243	\$648,244	
Beer Column Bottoms Recirc Pump	-	INCLUDED										
Beer Column Reflux Pump	1	INCLUDED										
Rectification Column Btms Pump	1	INCLUDED										
Rectification Column Reflux Pump	-	INCLUDED										
Beer Column Stillage Pump	1	INCLUDED										
Scrubber Bottoms Pump	-	\$6,300	2009	2009 Mass flow	8'0	2.3	1.11	\$6,843	688'9\$	\$15,844	\$15,845	
Filtrate Tank Discharge Pump	1	\$13,040	2010	2010 Mass flow	8.0	2.3	1.15	\$14,567	\$13,928	\$32,035	\$32,036	
Feed Pump	1	\$18,173		2010 Mass flow	8'0	2.3	1.15	\$20,301	\$19,411	\$44,645		\$0 Replaced by NREL 2002 water recovery
Manifold Flush Pump	-	\$17,057		2010 Mass flow	8.0	2.3	1.15	\$19,054	\$18,219	\$41,903	\$41,904	
Cloth Wash Pump	-	\$29,154	2010	2010 Mass flow	9.0	2.3	1.15	\$32,568	\$31,140	\$71,621	\$71,622	
Filtrate Discharge Pump	1	\$13,040	2010	2010 Mass flow	8'0	2.3	1.15	\$14,567	\$13,928	\$32,035	\$32,036	
Pressure Filter	2	\$3,294,700	2010	2010 Mass flow	9:0	1.7	1.15	\$3,680,519	\$3,519,098	\$5,982,467	38	
Beer Column Reflux Drum	1	INCLUDED		Mass flow								
Rectification Column Reflux Drum	1	INCLUDED		Mass flow								
Vent Scrubber	1	\$215,000	2009	2009 Mass flow	9.0	2.4	0.96	\$210,121	\$211,530	\$507,673	\$507,6	
Filtrate Tank	,	\$103,000	2010	2010 Mass flow	0.7	2	1.15	\$113,480	\$108,503			\$0 Replaced by NREL 2002 water recovery
Feed Tank	1	\$174,800	2010	2010 Mass flow	0.7	2	1.15	\$192,585	\$184,139	\$368,278		\$0 Replaced by NREL 2002 water recovery
Recycled Water Tank	1	\$1,520	2010	2010 Mass flow	0.7	3	1.15	\$1,675	\$1,601	\$4,804	\$4,805	

Table A.5: Apparatus list of the base and CBP (continued)

Pressing Air Compressor Receiver Drying Air Compressor Receiver	2 4	\$8,000	2010 Mass flow 2010 Mass flow	0.7	3.1	1.15	\$8,814	\$8,427	\$26,125 \$55,516	\$26,126	
Water recycling system from 2002 NREL report										\$18,900,000	NREL 2002 water recovery possible due to lower salt concentration
1st Effect Evaporation	2	INCLUDED	2002 Area	0.68		2.1					
ration	-	INCLUDED	2002 Area	0.68		2.1					
3rd Effect Evaporation	2	INCLUDED	2002 Area	0.68		2.1					
	7 -	NCLUDED	2002 Mass flow	0.79		2.8					
	- 2	INCLUDED	2002 Mass flow	0.79		2.8					
Evaporator Condensate Pump		INCLUDED	2002 Mass flow	0.79		2.8					
Evaporator Condenser	-	INCLUDED	2002 Heat Duty	0.68		2.1					
Evaporator Condensate Drum	-	INCLUDED	2002 Mass flow	0.93		2.1					
Recycled Water Tank	-	INCLUDED	2002 Mass flow	0.745		1.4					
Pneumapress Filter	4	INCLUDED	2002 Mass flow	9.0		1.04					
Lignin Wet Cake Screw	-	INCLUDED	Area 500 Totals	0.78		1.4	\$11.302.300	\$11.145.318	\$22.343.314	\$34.343.314	
							200120011		10000		
							ŀ				
Mechanical Equipment List Area		Э	8	$\neg$				Т		Adjustments due to CBP	Comments regarding adjustments
EQUIPMENT III LE	NOW KEGD	NCHIDED	Year of Quote Scaling Variable	Die Scaling Exp	Inst Factor	Size Ratio Scaled	Scaled Purch Cost	Purch Cost in Proj year	inst cost in Proj year	inst cost in Proj year (CBP)	
Aprohip Director Blower	- 00	\$1 033 750	2010 Mass flow	90		105	\$1 086 R27	\$1 800 408			
Aerobic Studge Screw	,-	\$25,000	2010 Mass flow	90	-	105	\$25,684	\$24.557	\$24.557		
stor Feed Cooler	-	\$83,863	2010 Mass flow	9.0	-	1.05	\$86,156	\$82,378			
Biogas Emergency Flare	4	\$32,955	2010 Mass flow	9.0	-	1.05	\$33,856	\$32,371	\$32,371		
Polymer Addition System	-	\$9,300	2010 Mass flow	9.0	-	1.05	\$9,554	\$9,135			
Caustic Feed System	3	\$22,800	2010 Mass flow	9.0	-	1.05	\$23,423	\$22,396			
Evaporator System		\$3,801,095	2010 Mass flow	0.¢	-	1.05	\$3,905,034	\$3,733,767	S		
Anaerobic Reactor Feed Pump	4	\$231,488	2010 Mass flow	9.0	-	1.05	\$237,818	\$227,388	\$227,388		
stor Recirc Pump	4	INCLUDED	Mass flow								
Waste Anaerobic Sludge Pump	9	\$93,300	2010 Mass flow	9.0	,	1.05	\$95,851	\$91,647	\$91,647		
Leed Pump	4 0	\$64,000	ZO TO INDES IIOW	0.0	- ,	1.05	\$60,297	\$62,012			
Reverse Osmosis Food Burn	-	OPC. 1718	Mass flow	0.0		00.	\$102,140	001,4,100	9174,100		
Centrifice Feed Pilmp	- 6	\$61.200	2010 Mass flow	90	-	105	\$62.873	\$60 116			
	2	\$70,800	2010 Mass flow	9.0	-	1.05	\$72,736	\$69,546	\$69,546		
reated Water Pump	1	INCLUDED	Mass flow								
Membrane Bioreactor	3	\$5,248,750	2010 Mass flow	9.0	1 1	1.05	\$5,392,274	\$5,155,780			
Reverse Osmosis System	-	\$2,210,979	2010 Mass flow	9.0	-	1.05	\$2,271,437	\$2,171,816	\$2,171,816		
		\$6,493,500	2010 Mass flow	0.6	-	1.05	\$6,671,062	\$6,378,482			
Anaerobic Basin	4 0	\$27,000,000	ZO 10 Mass flow	9.0		1.05	\$27,738,302	\$20,122,028			
Aeration Digester Sludge Holding Tank	, -	\$2,700,000 INCLUDED	ZOTO Mass flow	Oit	-	GU.T	\$2,773,830	\$2,052,175			
		4	Area 600 Totals				\$51,654,964	\$49,389,478	\$49,389,478	\$14,389,478	Only 13.7% of the original size due to adapted water
											B. III.
Mechanical Equipment List Area		38	Scaled Installed			-				Adjustments due to CBP	Comments regarding adjustments
EQUIPMENT TITLE	NUM REQD \$			ble Scaling Exp	Inst Factor	Size Ratio Scaled Purch Cost	d Purch Cost F			Inst Cost in Proj year (C	
Denaturant In-line Mixer	-		2009 Mass flow	3:0		96:0	\$3,776	\$3,801	\$3,801		
ink Agitator		\$21,200	2009 Mass flow	0.5		0.95	\$20,660	\$20,798			
DAP Make-up lank Agitator	  -  -	29,800	2009 Mass flow	6.0	9.1	0.87	\$9,152	\$9,214	\$13,820	\$13,820	
DAP bulk bag Unloader	- 0	\$30,000	Woll stand good	0.0		0.00	\$27,030	\$21,622			
Sufferio Acid Person	7-	\$9,200	2010 Mass flow	0.0	23	0.90	\$0,910	67 163	\$21,024		
Firewater Pimp		\$15,000	2009 Mass flow	0.0		0 0	C14 F36	£14 633			
	-	\$3,000	2009 Mass flow	0.8		0.98	\$2,959	\$2,979			
	-	\$3,000	2009 Mass flow	8.0		0.95	\$2.879	\$2,898		\$8,984	
	-	\$3,000	2009 Mass flow	9.0		0.87	\$2,689	\$2,707			
Ethanol Product Storage Tank	2	\$1,340,000	2009 Mass flow	7.0	1.7	96:0	\$1,303,683	\$1,312,426			
Sulfuric Acid Storage Tank	-	000'96\$	2010 Mass flow	7.0	L	-	\$95,987	\$91,777			
Firewater Storage Tank	-	\$803,000	2009 Mass flow	0.7	7.1.7	96.0	\$781,201	\$786,440		S	
Ammonia Storage Tank	2	\$196,000	2010 Mass flow	0.7		- 000	\$195,389	\$186,820			
Gasoline Storage Tank		\$200,000	2009 Mass flow	0.7		0.98	\$197,602	\$198,927			
nk Selder	+	\$70,000	2009 Mass flow	0.7	5.6	0.95	\$67,516	867,969	\$176,720	\$176,720	
DAP Make-up Tank	<u></u>	\$102,000	2009 Mass flow	7.0	1.8	0.72	\$81,192	\$81,737			
1		A	Area 700 Totals				\$2,823,265	\$2,827,086	\$4,953,786	\$4.953.787	
							1002,020,20	10001120120			

Table A.5: Apparatus list of the base and CBP (continued)

Table A.5: Apparatus list of the base and CBP (continued)

	\$8.770.517	6 890 517	\$3.984.635	\$4.114.396			Totals	Area 900		
		\$474,476	\$279,104		1.7	0.7	2009 Mass flow	\$250,000	-	
	\$49,934	\$49,933	\$16,107		3.1	9.0	2009 Mass flow	\$16,000	1	
	\$27,182	\$27,181	\$15,101		1.8	9.0	2009 Mass flow	\$15,000	-	
	\$45,644	\$45,643	\$14,724		3.1	8.0	2010 Mass flow	\$15,292	-	cess Water Circulating Pump
	\$19,460	\$19,459	\$6,277		3.1	0.8	2010 Mass flow	\$6,864	1	
	\$897,990	\$897,989	\$289,674	31	3.1	8.0	2010 Mass flow	\$283,671	3	
	\$1,257,981	\$1,257,980	\$698,878		1.8	9.0	2009 Mass flow	\$421,000	-	
	\$1,888,349	\$1,888,348	\$1,180,217	7.	1.6	9.0	2010 Heat duty	\$1,275,750	1	
	\$42,836	\$42,835	\$26,772		1.6	9.0	2010 Mass flow	\$28,000	1	
\$4,066,673 Cooling duty increases with larger combustor unit	\$4,066,673	\$2,186,673	\$1,457,782	1.19 \$1,524,650	1.5	9.0	2010 Mass flow	\$1,375,000	-	
	Inst Cost in Proj year (CBP)	Inst Cost in Proj year	t in Proj year	ch Cost	st Factor Size	Scaling Exp   Ir	ariable	Year of	NUM REQD  \$	
Comments regarding adjustments	Adjustments due to CBP						nstalled	Scaled I		chanical Equipment List Area
St20,379,573 Base case -\$1,240,000 because the FGD is not necessary anymore due to kwer salt concentrations, but stage,573 all remaining apparatus need to be acceled up by a factor of 2.8 since more solids are sent to combustion.		\$65,959,573	\$36,441,604	\$38,111,118			Totals	Area 700 Totals		
								INCLUDED	1	,
								INCLUDED	1	
		\$872,600	\$290,867	1 \$304,209	3	9.0	2010 Mass flow	\$305,000	-	
								INCLUDED	-	
								INCLODED	+	ille Iransier Pump
						Ī		INCLUDED	2 ,	
								INCLUDED	2	
								INCLUDED	2	
								INCLUDED	2	bine Condensate Pump
								INCLUDED	2	
								INCLUDED	1	
								INCLUDED	-	
		\$68,842	\$38,246	1 \$40,000	1.8	0	2010 Mass flow	\$40,000	-	
		\$133,894	\$74,386	1 \$77,798	1.8	9.0	2010 Mass flow	\$78,000	-	Process Water Softener System
		\$16,145,591	\$8,969,773	0.98 \$9,381,215	1.8	9.0	2010 Heat duty	\$9,500,000	-	
Omitted since no rou is needed								INCLUDED		noustion cas bagnouse

## APPENDIX B

Supplementary material for chapter 4: Set-up and validation of a rigorous, spatially resolved model of the kinetics and mass transfer limitations of consortium-based consolidated bioprocessing for ethanol production

### Overview of the validation of the model

Table B.1: Overview of the experimentally obtained validation parameters and the model results

Substance	Run	Reactor	Experiment	Model
Ethanol	1	1	$1.45 \ g/L$	$1.49 \ g/L$
	1	2	3.26  g/L	3.30  g/L
	2	1	$0.70 \; g/L$	0.68  g/L
	2	2	$1.82 \ g/L$	$1.79 \ g/L$
	3	1	$0.69 \ g/L$	0.71  g/L
	3	2	2.63  g/L	2.75  g/L
Cellobiose	1	1	0~g/L	0.12  g/L
	1	2	0.18  g/L	$0.20 \ g/L$
	2	1	$0.37 \ g/L$	0.33  g/L
	2	2	0.51  g/L	0.55  g/L
	3	1	0.11  g/L	0.13  g/L
	3	2	0.24  g/L	0.19  g/L
Glucose	1	1	0 g/L	0.15  g/L
	1	2	0 g/L	0.23  g/L
	2	1	0 g/L	0.09  g/L
	2	2	0 g/L	0.14  g/L
	3	1	0 g/L	0.16  g/L
	3	2	0 g/L	0.19  g/L
Endoglucanase	1	1	5.01~IU/mL	5.76 IU/mL
	1	2	9.47~IU/mL	$9.06\ IU/mL$
	2	1	8.33 IU/mL	7.65~IU/mL
	2	2	11.09 IU/mL	$10.65\ IU/mL$
	3	1	$4.50\ IU/mL$	$4.59\ IU/mL$
	3	2	$8.98\ IU/mL$	9.32~IU/mL
Cellobiohydrolase	1	1	0.08 IU/mL	0.10~IU/mL
Cellobiohydrolase	1	2	$0.14\ IU/mL$	$0.14\ IU/mL$
	2	1	$0.12\ IU/mL$	0.10~IU/mL
	2	2	0.18 IU/mL	0.20~IU/mL
	3	1	$0.06\ IU/mL$	0.07~IU/mL
	3	2	0.11~IU/mL	0.11~IU/mL
β-Glucosidase	1	1	0.01~IU/mL	0.01~IU/mL
	1	2	$0.02\ IU/mL$	$0.02\ IU/mL$
	2	1	$0.02\ IU/mL$	$0.02\ IU/mL$
	2	2	$0.02\ IU/mL$	$0.02\ IU/mL$
	3	1	$0.00\ IU/mL$	$0.02\ IU/mL$
	3	2	0.02 <i>IU/mL</i>	0.02 <i>IU/mL</i>

## **B.2** Matlab programming files

```
1 %% Design and set parameters
2 % Enter all design and set parameters in the corresponding blocks below
4 % *Temperature for temperature dependence of the following parameters \star
5 param.T_m_C=28; % temperature within membrane [ C ]
6 % needs to be between 0 C and 70 C!
7 param.T_m_K = param.T_m_C+273.15; % Temperature within membrane [K]
8 param.T_v_C = 28; % bulk temperature [ C ]
9 param.T_v=param.T_v_C+273.15; % bulk temperature [K]
10 param.titer_EtOH = 0.003; % starting value for ethanol titer [kg/m^3]
12 % *Reactor geometry*
13 geo.d_t_i = 1.58e-03; % tube membrane inner diameter [m]
14 geo.r_t_i = 0.5*geo.d_t_i; % tube membrane inner radius [m]
15 geo.d_t_o = 3.18e-03; % tube membrane outer diameter [m]
16 geo.r_t_o = 0.5*geo.d_t_o; % tube membrane outer radius [m]
17 geo.\Delta_m = geo.r_t_o-geo.r_t_i;
18 geo.l_t = 5.6; % tube membrane length [m]
19 geo.A_m_cross = pi*(geo.r_t_i^2); % Cross-sectional area [m^2]
20 % of the tube membrane
21 geo.A_t_i = pi*geo.d_t_i*geo.l_t; % tube membrane inner wall area [m^2]
22 \text{qeo.A\_t\_o} = \text{pi*qeo.d\_t\_o*qeo.l\_t}; % tube membrane outer wall area [m^2]
23 geo.h_wind = geo.d_t_o; % height of membrane winding [m]
24 geo.d_wind = 0.07; % diameter of membrane winding [m]
25 geo.d_curv = geo.d_wind*(1+((geo.h_wind/(pi*geo.d_wind))^2));
26 % curvature diameter according to VDI heat atlas chapter G3
27 geo.d_v = 0.2; % vessel diameter [m]
28 geo.d_stirrer = 0.15; % stirrer diameter [m]
29 geo.V_v = 0.0027; % reactor working volume [m^3]
30 geo.h_fill = geo.V_v/(0.25*pi*(geo.d_v^2)); % reactor filling height [m]
31 %%
32 % *Chemicals*
33 chem.R_gas = 8.31446261815324; % Universal gas constant [J/(mol*K)]
34 chem.M_ox = 0.031998; % Molar mass oxygen [kg/mol]
35 chem.M_air = 0.02896; % Molar mass air [kg/mol]
36 chem.M_m_n = 0.0280134; % Molar mass nitrogen [kg/mol]
37 chem.M_EtOH = 0.04607; % Molar mass ethanol [kg/mol]
38 chem.M_G = 0.180156; % Molar mass glucose [kg/mol]
39 chem.M_CO2 = 0.04401; %Molar mass CO2 [kg/mol]
40 chem.D_m_ox = 3.4 \times (10^{(-9)});
41 % Diffusivity of oxygen in PDMS [m^2/s] (@35 C) Merkel et al. 2000
42 chem.D_m_n = 3.4*(10^{(-9)});
43 % Diffusivity of nitrogen in PDMS [m^2/s] (@35 C) Merkel et al. 2000
```

```
44 chem.D_m_CO2 = 2.2*(10^{(-9)});
45 % Diffusivity of CO2 in PDMS [m^2/s] (@35 C) Merkel et al. 2000
46 chem.D_m_EtOH = 1.338*(10^{(-6)})*exp((-27760)/(chem.R_gas*param.T_m_K));
47 % Diffusivity of ethanol in PDMS membrane [m^2/s] Xia et al. 2015
48 chem.sol_m_ox = ((10^{(-5)})/1.013)*0.18*((chem.M_ox*(10^5))/...
       (chem.R_gas*273.15)); % Solubility oxygen in PDMS membrane
50 \% [kg/(m^3*Pa)] (@35 C) Merkel et al. 2000
51 chem.sol_m_n = ((10^{(-5)})/1.013)*0.09*((chem.M_m_n*(10^5))/...
52 (chem.R_gas*273.15)); % Solubility nitrogen in PDMS membrane
8[kg/(m^3*Pa)] (@35 C) Merkel et al. 2000
54 chem.sol_m_CO2 = ((10^{(-5)})/1.013) \times 1.29 \times ((chem.M_CO2 \times (10^{5}))/...
       (chem.R_gas*273.15)); % Solubility CO2 in PDMS membrane
\frac{1}{2} %[kg/(m<sup>3</sup>*Pa)] (@35 C) Merkel et al. 2000
57 chem.sol_m_EtOH = chem.M_EtOH\star2.67\star(10^{\circ}(-11))/chem.D_m_EtOH;
58 % Solubility ethanol in PDMS membrane [kg/(m^3*Pa)] Lue et al. 2015
59 chem.H_EtOH = 1.9*chem.M_EtOH; %Henry coefficient for ethanol in water
60 \% [kg/(m^3*Pa)] Sander et al. 2015
61 chem.D_w_ox = 2e-9;
62 % Oxygen diffusivity in water [m^2/s] (Stewart et al. 2003)
63 chem.D_w_n = 1.88e-9;
64 chem.D w CO2 = 1.92e-9;
65 chem.D_w_G = 0.698e-9;
66 % glucose diffusivity in water [m^2/s] (Suhaimi et al. 2015)
67 chem.D_w_Cb = 0.59e-9;
68 % Cellobiose diffusivity in water [m^2/s]
69 %(Traving et al. 2015; Hardy et al. 1993)
70 chem.D_w_E = 0.05e-9;
71 % Enzyme diffusivity in water [m^2/s] (Traving et al. 2015)
72 % 0.14e-9 (Kim et al. 1996)
73 chem.D_w_EtOH = (1e-9)*(1/((5-0)*(30-25)))*...
       [5-param.titer_EtOH param.titer_EtOH-0] * [1.24 1.41; 0.91 1.13] * ...
       [30-param.T_v_C; param.T_v_C-25];
76 % 2D interpolation for EtOH diffusivity [m^2/s]
77 %(data from Pratt et al. 1974)
78 chem.P_ox = 0.12; %Partition coefficient for oxygen between PDMS and H20
79 %PhD thesis Michael Hanspeter Studer ETHZ
80 %%
81 % *Membrane*
82 param.n_ox_m=0.21; % oxygen fraction in gas within membrane [-]
83 param.dVdt_m_Lmin = 0.368; % volumetric flow within membrane [L/min]
84 param.dVdt_m = param.dVdt_m_Lmin/(1000*60); %
85 % volumetric flow within membrane [m^3/s]
86 param.visc_m = 1e-7*(((0.0010714286)*(param.T_m_C^2))+...
       (0.8895238095*param.T_m_C)+134.9916666667);
88 % Kinematic viscosity [m^2/s] of the fluid within the membrane
89 % approximated with fitted air data from VDI heat atlas (chapter D2.2)
90 param.visc_ox = (0.0011170100*(param.T_m_C^2))+...
```

```
(0.9077425018*param.T_m_C)+135.7002517027;
92 % Kinematic viscosity [m^2/s] of oxygen
93 % (fitted data from VDI heat atlas (chapter D2.5)
94 param.Re_m = (geo.d_t_i*param.dVdt_m/geo.A_m_cross)/param.visc_m;
95 % Reynolds number [-] within membrane
96 param.Re_m_crit=2300*(1+(8.6*((geo.d_t_i/geo.d_curv)^0.45)));
97 % critical Reynolds number
98 % in a helical coil according to VDI heat atlas chapter G3
99 param.Pr_m = ((5e-7)*param.T_m_C^2)-(param.T_m_C*0.000155)+0.711;
100 % Prandtl number [-] of the fluid within the membrane
101 % approximated with fitted air data from VDI heat atlas (chapter D2.2)
102 param.Sc_ox = param.visc_ox/chem.D_w_ox;
103 % Schmidt number of oxygen in the inner membrane phase
105 % _The following parameters are calculated based on the entries_
106
107
108 rho_m=1.149; % starting value for density of air
   % at given tmeperature [m^2/s] (VDI heat atlas D 2.2)
110
111 H_cp_ox=1.2e-5; % Henry constant for oxygen [mol/(m^3/Pa] R. Sander 2015
113 % *Biofilm*
114 param.mu_max_tr = 2.3/(24*3600); % max. growth rate T. reesei [1/s]
param.K_ox_tr = 0.001; % half-saturation constant
116 % of T. reesei for oxygen [kg/m^3]
param.K_G_tr = 4.0/(24*3600); % half-saturation constant
118 % of T. reesei for glucose [kg/m^3]
119 param.K_tr_ps = 2.2/(24*3600); % rate constant [1/s] for T. reesei
120 % conversion of primary mycelia to secondary mycelia
121 param.K_tr_dec = 0.09/(24*3600); % rate constant [1/s] of T. reesei
122 % secondary mycelia decay
123 param.K_tr_synth = (1/32) *19.8*0.45/(24*3600);
124 % enzyme synthesis rate constant
125 % [g enzymes/(g secondary mycelium * s) ]
126 param.K_E_dec = 0.0092/(24*3600); % enzyme decay rate [1/s]
127 %all above mentioned data is from Velkovska et al. 1997
128 param.Y_ox_tr = 0.0323/chem.M_ox; % kg biomass/kg 02
129 param.Y_G_tr = 0.44; % kg biomass/kg glucose
130 param.M_ox_tr = chem.M_ox*(1000/3600)*0.85e-3; % kg 02/(kg biomass*s)
131 param.M_G_tr = chem.M_G*(1000/3600)*0.14e-3; % kg glucose/(kg biomass*s)
132 param.mean_rho_tr = 50.1; % mean fungal biofilm density [kg/m^3]
133 % Ercan et al. 2015 & Lecault et al. 2009
134 param.mean_rho_Y = 0.15*1100; % mean yeast density [kg/m<sup>3</sup>]
135 % Ercan et al. 2015; Baldwin et al. 1984; Bryan et al. 2010
136 param.K_y_{dec} = 6.48e-5*5*24/3600; %decay rate S. cerevisiae
137 % Fan et al. 2015
```

```
138 param.K_DEGR_EtOH = 0.0306/(5*3600); %ethanol degradation constant of
139 %T. reesei if no substrate is present (own experiments)
140 param.K_degr_EtOH = 0.01183/(5*3600); %ethanol degradation constant of
141 %T. reesei if another substarte is present (own experiments)
142
143 %
144 %%
145 % *Reactor bulk & hydrolysis*
146 param.T_v_C = 28; % bulk temperature [ C ]
147 param.T_v=param.T_v_C+273.15; % bulk temperature [K]
148 param.tau = 5*24*3600; %Residence time [s]
149 param.sol_load_feed = 17.5; % solid loading of the feed stream [kg/m^3]
150 param.feed_frac_s = 1; % cellulose fraction of feed solid content [-]
151 param.c_C_in = param.sol_load_feed*param.feed_frac_s;
152 %cellulose feed stream
153 param.sol_load = 17.5; % solid loading of the bulk [kg/m^3]
param.c_EtOH_max = param.sol_load_feed*param.feed_frac_s*...
      (360/324)*(2*chem.M_EtOH/chem.M_G);
156 % stoichiometric conversion of cellulose to glucose to ethanol
157 param.N_stirrer = 50/60; % Rotational speed stirrer [1/s]
158 param.visc_v = 0.03539435*exp(27.0464373*0.001*param.sol_load);
159 %fitted curve for data from Pimenova et al. 2003
160 param.Re_v = param.N_stirrer*(geo.d_stirrer^2)/param.visc_v;%(0.8335e-6);
161 % Reynolds number for stirred vessels
162 param.Sc_v_E=chem.D_w_E/param.visc_v;
163 param.c_ox_b = 1e-6; %oxygen concentration in the bulk [kg/m^3]
164
165 param.frac_E_endo_Tr = 0.9899; % fraction of endoglucanase activity
166 % of total enzyme activity [-] (Xiros et al, 2017)
167 param.frac_E_exo_Tr = 0.0085; % fraction of exoglucanase (=CBH) activity
168 % of total enzyme activity [-] (Xiros et al, 2017)
169 param.frac_E_betaG_Tr = 0.0016; % fraction of beta-glucosidase activity
170 % of total enzyme activity [-] (Xiros et al, 2017)
171 param.frac_exo_sites_C_in = 0.0033; %fraction of active sites for
172 %exoglucanase of Avicel [-] (Zhang et al. 2004)
173 param.k_endo = 0.110/3600; hydrolysis rate constant of endoglucanase [1/s]
174 % van Zyl et al. 2010
175 param.k_exo = 0.07/3600; %hydrolysis rate constant of exoglucanase [1/s]
176 % van Zyl et al. 2010
177 param.K_C_Cb = 5.85; % Inhibition constant of cellobiose on
178 %cellulose conversion [kg/m^3]
179 % van Zyl et al. 2010
180 param.K_C_EtOH = 50.35; % Inhibition constant of ethanol on
181 %cellulose conversion [kg/m^3]
182 % van Zyl et al. 2010
183 param.sigma_endo = 0.084; % endoglucanase capacity on Avicel [-]
184 % van Zyl et al. 2010
```

```
185 param.sigma_exo = 0.084; % exoglucanase capacity on Avicel [-]
186 % van Zyl et al. 2010
187 param.k_fc = 1.8366/3600; % enzyme adsorption constant
188 % on Avicel [m^3/(kg*s)]
189 % van Zyl et al. 2010
190 param.K_endo = 1.84; % equilibrium constant for endoglucanase [m^3/kg]
191 % van Zyl et al. 2010
192 param.K_exo = 55; % equilibrium constant for exoglucanase [m^3/kg]
193 % van Zyl et al. 2010
194 param.K_Cb = 0.02/3600; % rate constant of cellobiose hydrolysis [1/s]
195 % van Zyl et al. 2010
196 param.K_m = 10.56; %Michael constant of beta-G for cellobiose [kg/m^3]
197 % van Zyl et al. 2010
198 param.K_Cb_G = 0.62; %inhibition constant of glucose on cellobiose
199 %conversion [kg/m^3]
200 % van Zyl et al. 2010
201 param.Y_X_Y_G = 0.12; %yield coefficient of yeast biomass from glucose [-]
202 % van Zyl et al. 2010
203 param.mu_max_Y = 0.4/3600; %maximum anaerobic growth rate S. cerevisiae
204 %[1/s]
205 % van Zvl et al. 2010
206 param.K_G = 0.476; % Half-saturation glucose [kg/m^3]
207 % van Zyl et al. 2010
208 param.K_X_EtOH = 87; %inhibition constant of ethanol on yeast growth
209 %[kg/m^3]
210 % van Zyl et al. 2010
211 param.Y_EtOH_G = 0.419; %yield coefficient of ethanol from glucose [-]
212 % van Zyl et al. 2010
213
214 %
216 % _The following parameters are calculated based on the entries_
217 % rho_w_v=((T_v_C^3)*0.000033603)+((T_v_C^2)*(- 0.0349738131))+...
         (T_v_C*11.6350223258)-253.6172523896;
219 % % density of pure liquid water in vessel between 0 C and 50 C [kg/m^3]
220 % visc_w_v = (10^-6) * (((T_v_C^3) * (-0.0000079042)) + ...
         ((T_v_C^2)*(0.0075055404))+(T_v_C*(-2.3873231021))+254.9613281728);
222 % %kinematic viscosity of liquid water between 0 C and 50 C [m^2/s]
223
224 응응
225 % % *Discretization grid*
226 geo.n=25; % grid resolution for each layer
227 % (membrane, fungal biofilm and yeast biofilm)
228 %including inner membrane and bulk boundary condition
229 geo.M=50; %grid resolution in Z-direction
230 geo.N=3*geo.n+4; % total grid resolution in R-direction including inner
231 % membrane and bulk boundary condition as well as the bulk itself
```

```
232 geo.dz=geo.l_t/geo.M; %axial length of discretized element [m]
233 geo.dr=(geo.r_t_o-geo.r_t_i)/geo.n;
234 % radial length of discretized element [m]
235 geo.r = zeros (1, geo.M*geo.N); %radius at position i in the grid [m]
236 for i = 1 : geo.M
       geo.r(i)=0;
238 end
239 for i = \text{geo.M+1}: \text{geo.N*geo.M}
       geo.r(i) = geo.r_t_i + (geo.dr * floor((i - (geo.M+1))/geo.M));
241 end
242 geo.dV = zeros (1, geo.M*geo.N); %volume at position i in the grid [m^3]
243 for i = 1 : geo.M
       geo.dV(i) = pi*(geo.r_t_i^2)*geo.dz;
244
245 end
246 for i = \text{geo.M+1}: (\text{geo.N-1}) * \text{geo.M}
       geo.dV(i) = pi*geo.dz*((geo.r(i+geo.M)^2)-(geo.r(i)^2));
248 end
249 for i = (geo.M*(geo.N-1))+1 : geo.N*geo.M
        geo.dV(i) = (geo.V_v-sum(geo.dV(1:geo.N*(geo.M-1))))/geo.M;
251 end
252 응응
253 % % *Temporary values*
254 geo.r_f = geo.r_t_o+(geo.n*geo.dr);
255 %starting value for fungal biofilm thickness
```

```
1 errvec = zeros(geo.M*geo.N,1);
2 maxerrvec = zeros(geo.M*geo.N,1);
3 error = zeros(8*geo.N*geo.M,1);
4 param.last_iter = zeros(geo.M*geo.N,1);
5 solvec=solvec_0;
6 hydrosolvec_0=[0.99*param.c_C_in , 0 , 10 , -1.4e-5 ,
      6, 6, 6, 6, 6, 0, 6, 0, 6, 0.5, 7, 1e-5, 3, 3];
8 param.max_rel_error_EtOH=1;
9 itercount=0;
10 param.max_rel_error_ox=1;
11 %maximum relative error oxygen concentration [%]
while itercount<1500 || param.max_rel_error_EtOH>0.5 ||
      param.max_rel_error_ox>0.5%
13
14 % Concentration profiles oxygen, fungal biomass & enzymes
      % oxygen inner membrane phase
16 for i= 1: geo.M
         solvec(i) = (chem.M_ox*param.n_ox_m*
          (1/(chem.R_gas*param.T_m_K))*param.p_m(i));
          %(chem.sol_m_ox*param.p_m(i)*param.n_ox_m);
20 end
21 %oxygen at membrane wall (neglecting convective boundary layer)
```

```
22 for i = \text{geo.M+1}
                  solvec(i) = (chem.sol_m_ox*param.p_m(i-qeo.M)*param.n_ox_m);
24 end
     for i = geo.M+2 : 2*geo.M
25
                  solvec(i) = solvec(i-1) + (2*pi*chem.D_m_ox*geo.dz*(solvec(i-1) - ox*geo.dz*(solvec(i-1) - ox*
26
                   solvec(i+geo.M-1))/(param.dVdt_m*log(geo.r_t_i/(geo.r_t_i+geo.dr))));
27
28 end
29 %oxygen in membrane
      for i = (2*geo.M) + 1 : (1+geo.n)*geo.M
                  n = floor((i-1)/geo.M)-1;
                   solvec(i) = sqrt((((solvec(i-(n*qeo.M))*log(qeo.r_t_o/qeo.r(i)))+
32
                   (solvec(i+((geo.n-n)*geo.M))*log(geo.r(i)/geo.r_t_i)))/
33
                   log(geo.r_t_i/geo.r_t_o))^2);
34
35
     end
       for i = ((1+geo.n) * geo.M) + 1 : (2+geo.n) * geo.M
                   solvec(i) = (1/((chem.D_w_ox*chem.P_ox/log(geo.r_t_o/geo.r_f))+
37
                   (chem.D_m_ox/log(geo.r_t_i/geo.r_t_o))))*((solvec(i-(geo.n*geo.M)))*(
38
                   chem.D_m_ox/log(qeo.r_t_i/qeo.r_t_o)) + (solvec(i+(qeo.n*qeo.M)) *
39
                   chem.D_w_ox/log(geo.r_t_o/geo.r_f)));
41 end
     %oxygen in fungal biofilm
      for i = ((2+\text{geo.n}) * \text{geo.M}) + 1 : ((3+\text{geo.n}) * \text{geo.M})
                  solvec(i) = 0.12*solvec(i-geo.M);
44
45
     end
       for i = ((3+geo.n)*geo.M)+1 : ((2+(2*geo.n))*geo.M)
                   if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) && i/(geo.M) \neq floor(i/(geo.M))
47
                   solvec(i) = sqrt(((1/((-4*pi*chem.D_w_ox/(geo.dr^2))+
48
                    (-4*pi*chem.D_w_ox/(geo.dz^2))+(0)))*(((solvec(i+1)*
49
                   50
                   (geo.dz^2)))+(solvec(i+geo.M)*((2*pi*chem.D_w_ox/(geo.dr^2))+
51
                   (2*pi*chem.D_w_ox/(2*geo.dr*geo.r(i)))))+(solvec(i-geo.M)*
                   ((2*pi*chem.D_w_ox/(geo.dr^2))-(2*pi*chem.D_w_ox/
53
                   (2*geo.dr*geo.r(i))))))+((-param.mu_max_tr/param.Y_ox_tr)*
54
55
                   min((solvec(i+(5*geo.N*geo.M)))/(param.K_G+solvec(i+(5*geo.N*geo.M)))))
                   (solvec(i)/(param.K_ox_tr+solvec(i))))*(param.K_tr_dec/
56
                   ((param.mu_max_tr*min((solvec(i+(5*geo.N*geo.M)))/(param.K_G+
57
                   solvec(i+(5*qeo.N*qeo.M)))),(solvec(i)/(param.K_ox_tr+solvec(i)))))+
58
                   param.K_tr_dec))*solvec(i+(geo.N*geo.M)))+(-param.M_ox_tr*
                   solvec(i+(geo.M*geo.N)))))^2);
60
                   elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
61
                   solvec (i) = sqrt(((1/((-4*pi*chem.D_w_ox/(geo.dr^2))+
62
                   (2*pi*chem.D_w_ox/(geo.dz^2))+(0)))*(((solvec(i+1)*(-4*pi*chem.D_w_ox/(geo.dz^2)))))))
                   (geo.dz^2)) + (solvec(i+2) * (2*pi*chem.D_w_ox/(geo.dz^2))) +
64
                   (solvec(i+geo.M)*((2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_o
                   (2*geo.dr*geo.r(i)))))+(solvec(i-geo.M)*((2*pi*chem.D_w_ox/(geo.dr^2))
                   -(2*pi*chem.D_w_ox/(2*qeo.dr*qeo.r(i))))))+((-param.mu_max_tr/
67
                  param.Y_ox_tr) *min((solvec(i+(5*geo.N*geo.M))/(param.K_G+
68
```

```
solvec(i+(5*geo.N*geo.M)))),(solvec(i)/(param.K_ox_tr+solvec(i))))*
69
 70
               (param.K_tr_dec/((param.mu_max_tr*min((solvec(i+(5*geo.N*geo.M))/
               (param.K_G+solvec(i+(5*geo.N*geo.M)))),(solvec(i)/(param.K_ox_tr+
72
               solvec(i)))))+param.K_tr_dec))*solvec(i+(geo.N*geo.M)))+
               (-param.M_ox_tr*solvec(i+(geo.M*geo.N))))^2);
 73
               elseif i/(geo.M) ==floor(i/(geo.M))
74
               solvec (i) = sqrt(((1/((-4*pi*chem.D_w_ox/(geo.dr^2)))+
75
               (2*pi*chem.D_w_ox/(geo.dz^2))+(0)))*(((solvec(i-1)*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D_w_ox/(solvec(i-1))*(-4*pi*chem.D
76
               (geo.dz^2)) + (solvec(i-2)*(2*pi*chem.D_w_ox/(geo.dz^2))) +
               (solvec(i+geo.M) * ((2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/
               (2*geo.dr*geo.r(i)))))+(solvec(i-geo.M)*((2*pi*chem.D_w_ox/(geo.dr^2))
 79
               -(2*pi*chem.D_w_ox/(2*geo.dr*geo.r(i))))))+((-param.mu_max_tr/
 80
               param.Y_ox_tr) *min((solvec(i+(5*geo.N*geo.M))/(param.K_G+
 81
               solvec(i+(5*geo.N*geo.M)))), (solvec(i)/(param.K_ox_tr+solvec(i))))*
 82
               (param.K_tr_dec/((param.mu_max_tr*min((solvec(i+(5*geo.N*geo.M))/
 83
 84
               (param.K_G+solvec(i+(5*geo.N*geo.M)))),(solvec(i)/(param.K_ox_tr+
               solvec(i)))))+param.K_tr_dec))*solvec(i+(geo.N*geo.M)))+
 85
               (-param.M_ox_tr*solvec(i+(geo.M*geo.N))))^2);
 86
               end
 88
     end
      %oxygen in yeast biofilm
89
      for i = ((2+(2*geo.n))*geo.M)+1 : ((2+(3*geo.n))*geo.M)
               solvec(i) = param.c_ox_b;
91
92 end
      %oxygen at biofilm boundary layer
94 for i = ((2+(3*geo.n))*geo.M)+1 : ((3+(3*geo.n))*geo.M)
               solvec(i) = param.c_ox_b;
     end
 97 %oxygen within bulk
     for i = ((3+(3*geo.n))*geo.M)+1
               solvec(i) = param.c_ox_b;
100 end
     for i = ((3+(3*geo.n))*geo.M)+2 : geo.N*geo.M
101
102
               solvec(i) = solvec(i-1);
103 end
104
105
106 %Fungal biomass
107 %average growth rate
108 ox_lim=zeros(geo.n*geo.M,1);
109 for i = ((2+geo.n)*geo.M)+1 : ((2+(2*geo.n))*geo.M)
              ox_lim (i-((2+geo.n)*geo.M)) = solvec(i)/(param.K_ox_tr+solvec(i));
110
111 end
112 param.avg_ox_lim=mean(ox_lim);
113 %fungal biomass inner membrane phase, membrane boundary layer & membrane
114 for i = (\text{geo.N*geo.M}) + 1 : ((\text{geo.N*geo.M}) + (2+\text{geo.n}) *\text{geo.M})
              solvec(i) = 0;
115
```

```
116 end
   %fungal biomass in fungal/yeast biofiolm
   for i = ((qeo.N*qeo.M) + (2+qeo.n)*qeo.M) + 1 :
        ((geo.N*geo.M) + ((2+(2*geo.n))*geo.M))
119
        if solvec(i-(geo.M*geo.N))≤param.c_ox_b
120
            solvec(i) = 0;
121
       else
122
       solvec(i) = ((param.mean_rho_tr*min((1),(solvec(i-(geo.M*geo.N)))/
123
        (param.K_ox_tr+solvec(i-(geo.M*geo.N)))))))param.avg_ox_lim);
          (min((1), (mean(solvec((((2+geo.n)*geo.M)+1) : ((2+(2*geo.n))*geo.M)))
125
          /(param.K_ox_tr+mean(solvec((((2+geo.n)*geo.M)+1) :
126
          ((2+(2*geo.n))*geo.M))))));
       end
128
129
  end
   %fungal biomass in fungal/yeast biofilm, biofilm boundary layer and bulk
130
   for i = ((qeo.N*qeo.M) + ((2+(2*qeo.n))*qeo.M)) + 1 : (2*qeo.N*qeo.M)
       if solvec(i-(geo.M*geo.N))≤param.c_ox_b
132
133
            solvec(i) = 0;
134
       else
       solvec(i) = ((param.mean_rho_tr*min((1),(solvec(i-(geo.M*geo.N)))/
135
        (param.K ox tr+solvec(i-(geo.M*geo.N)))))/param.avg ox lim);
136
137
          (\min((1), (\max(solvec((((2+qeo.n)*qeo.M)+1) : ((2+(2*qeo.n))*qeo.M))))
          /(param.K_ox_tr+mean(solvec((((2+geo.n)*geo.M)+1) :
138
139
          ((2+(2*geo.n))*geo.M))))));
       end
141
  end
   %secondary mycelia in the system
142
   for i = (2*geo.N*geo.M) + 1 : (3*geo.N*geo.M)
143
144
       solvec(i) = solvec(i-(geo.M*geo.N))*param.mu_max_tr*
        (solvec(i-(2*geo.M*geo.N))/(param.K_ox_tr+solvec(i-(2*geo.M*geo.N))))/
145
        ((param.mu_max_tr*(solvec(i-(2*geo.M*geo.N)))/(param.K_ox_tr+
        solvec(i-(2*geo.M*geo.N)))))+param.K_tr_dec);
147
148 end
149
   %enzyme concentration in the inner membrane phase & membrane
   for i = (3*geo.N*geo.M) + 1 : (3*geo.N*geo.M) + ((2+geo.n)*geo.M)
       solvec(i)=0:
151
152
  end
   %enzyme concentration in the fungal/yeast biofilm
   for i = (3*geo.N*geo.M) + ((2+geo.n)*geo.M) + 1
154
       solvec(i) = (1/((chem.D_w_E/(geo.dz^2)) + (2*pi*chem.D_w_E*geo.dz/
155
       \log(\text{geo.r}(i-(3*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(3*\text{geo.N*geo.M})))
156
       param.K_E_dec)))*((chem.D_w_E*solvec(i+1)/(geo.dz^2))+
157
        (2*pi*chem.D_w_E*qeo.dz*solvec(i+qeo.M)/log(qeo.r(i-(3*qeo.N*qeo.M))/
158
       geo.r(geo.M+i-(3*geo.N*geo.M))))+(param.K_tr_synth*
       solvec(i-(geo.N*geo.M)));
160
161 end
  for i = (3*geo.N*geo.M) + ((2+geo.n)*geo.M) + 2:
```

```
163
        ((3*geo.N*geo.M) + ((3+geo.n)*geo.M)) - 1
        solvec(i) = (1/((2*chem.D_w_E/(geo.dz^2)) +
164
        (2*pi*chem.D_w_E*geo.dz/log(geo.r(i-(3*geo.N*geo.M))/
        geo.r(geo.M+i-(3*geo.N*geo.M)))+param.K_E_dec)))*((chem.D_w_E*
166
        (solvec(i-1)+solvec(i+1))/(geo.dz^2))+(2*pi*chem.D_w_E*geo.dz*
167
        solvec(i+geo.M)/log(geo.r(i-(3*geo.N*geo.M))/
168
        geo.r(geo.M+i-(3*geo.N*geo.M))))+(param.K_tr_synth*
169
        solvec(i-(geo.N*geo.M))));
170
   for i = ((3*geo.N*geo.M) + ((3+geo.n)*geo.M))
172
        solvec(i) = (1/((chem.D_w_E/(geo.dz^2)) + (2*pi*chem.D_w_E*geo.dz/
173
        \log(\text{geo.r}(i-(3*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(3*\text{geo.N*geo.M})))
174
        param.K_E_dec)))*((chem.D_w_E*solvec(i-1)/(geo.dz^2))+
175
        (2*pi*chem.D_w_E*geo.dz*solvec(i+geo.M)/log(geo.r(i-(3*geo.N*geo.M))/
176
        geo.r(geo.M+i-(3*geo.N*geo.M))))+(param.K_tr_synth*
177
178
        solvec(i-(geo.N*geo.M))));
   end
179
180
   for i = (3*qeo.N*qeo.M) + ((3+qeo.n)*qeo.M) + 1:
181
        ((3*geo.N*geo.M) + ((2+(3*geo.n))*geo.M))
        if solvec(i-(3*geo.M*geo.N))>param.c_ox_b
182
            if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) & &
183
                i/(geo.M) \( floor(i/(geo.M)) \)
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_E/(geo.dr^2))+
185
186
            (-4*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i+1)*
            (2*pi*chem.D_w_E/(geo.dz^2)))+(solvec(i-1)*(2*pi*chem.D_w_E/
187
            (geo.dz^2)) + (solvec(i+geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))+
188
            (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))+
189
            (solvec(i-qeo.M)*((2*pi*chem.D_w_E/(geo.dr^2))-(2*pi*chem.D_w_E/
190
191
            (2*geo.dr*geo.r(i-(3*geo.N*geo.M)))))))+(param.K_tr_synth*
            solvec(i-(geo.N*geo.M)))))^2);
192
            elseif (i-1)/(qeo.M) == floor((i-1)/(qeo.M))
193
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_E/(geo.dr^2))+
194
            (2*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i+1)*i))
195
196
            (-4*pi*chem.D_w_E/(geo.dz^2))) + (solvec(i+2)*(2*pi*chem.D_w_E/
            (geo.dz^2)))+(solvec(i+geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))+
197
            (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))+
198
            (solvec(i-geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))-(2*pi*chem.D_w_E/
199
            (2*geo.dr*geo.r(i-(3*geo.N*geo.M)))))))+(param.K_tr_synth*
            solvec(i-(geo.N*geo.M)))))^2);
201
202
            elseif i/(geo.M) ==floor(i/(geo.M))
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_E/(geo.dr^2))+
203
            (2*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i-1)*
204
            (-4*pi*chem.D_w_E/(geo.dz^2)))+(solvec(i-2)*(2*pi*chem.D_w_E/
205
206
            (geo.dz^2)) + (solvec(i+geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))+
            (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.M*geo.N))))))+
207
            (solvec(i-geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))-(2*pi*chem.D_w_E/
208
            (2*geo.dr*geo.r(i-(3*geo.N*geo.M)))))))+(param.K_tr_synth*
209
```

```
210
             solvec(i-(geo.N*geo.M)))))^2);
211
        elseif solvec(i-(3*geo.M*geo.N)) ≤ param.c_ox_b
212
             if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) &&
213
                  i/(geo.M) \( floor(i/(geo.M)) \)
214
             solvec (i) = \operatorname{sqrt}((((1/((-4*\operatorname{pi*chem.D} \text{ w E}/(\operatorname{qeo.dr}^2)))+
215
             (-4*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i+1)*
216
             (2*pi*chem.D w E/(geo.dz^2)))+(solvec(i-1)*(2*pi*chem.D w E/
217
             (geo.dz^2)) + (solvec(i+geo.M) * ((2*pi*chem.D_w_E/(geo.dr^2)) +
             (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))+
219
             (solvec(i-qeo.M)*((2*pi*chem.D_w_E/(qeo.dr^2))-(2*pi*chem.D_w_E/
220
             (2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))))))))))))
221
             elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
222
             solvec (i) = sqrt((((1/((-4*pi*chem.D_w_E/(geo.dr^2))+
223
             (2*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i+1)*
             (-4 * pi * chem.D_w_E/(geo.dz^2))) + (solvec(i+2) * (2 * pi * chem.D_w_E/
225
             (\text{geo.dz}^2)) + (\text{solvec}(i+\text{geo.M}) * ((2*\text{pi*chem.D}_w_E/(\text{geo.dr}^2)) +
226
227
             (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))
             (solvec(i-geo.M)*((2*pi*chem.D_w_E/(geo.dr^2))-(2*pi*chem.D_w_E/
             (2*geo.dr*geo.r(i-(3*geo.N*geo.M)))))))))))))))))
229
             elseif i/(geo.M) ==floor(i/(geo.M))
230
231
             solvec (i) = \operatorname{sqrt}((((1/((-4 \cdot \operatorname{pi} \cdot \operatorname{chem.D_w_E}/(\operatorname{geo.dr^2})) +
             (2*pi*chem.D_w_E/(geo.dz^2))+(-param.K_E_dec)))*(((solvec(i-1)*
232
233
             (-4 * pi * chem.D_w_E/(geo.dz^2))) + (solvec(i-2) * (2 * pi * chem.D_w_E/
             (\text{geo.dz}^2)) + (\text{solvec}(i+\text{geo.M}) * ((2*\text{pi*chem.D}_w_E/(\text{geo.dr}^2)) +
             (2*pi*chem.D_w_E/(2*geo.dr*geo.r(i-(3*geo.M*geo.N))))))+
235
             (solvec(i-qeo.M)*((2*pi*chem.D_w_E/(geo.dr^2))-(2*pi*chem.D_w_E/
236
             (2*geo.dr*geo.r(i-(3*geo.N*geo.M))))))))))))))))
237
238
             end
239
        end
240
    %enzyme concentration in biofilm boundary layer
241
    for i = ((3*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1:
242
243
        ((3*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
        %no mass transfer limiting convective boundary layer is assumed
244
           solvec (i) = ((chem.D_w_E*solvec(i-qeo.M)/log(qeo.r(i-(3*qeo.N*qeo.M))
245
   %/(geo.r(i-(3*geo.N*geo.M))-geo.dr)))-(param.k_conv_E_v*geo.r(i-(3*geo.N*geo.M))*
246
   solvec(i+qeo.M))/((chem.D_w_E/log(qeo.r(i-(3*qeo.N*qeo.M))/(qeo.r))
   %(i-(3*geo.N*geo.M)))-geo.dr))))-(param.k_conv_E_v*geo.r(i-(3*geo.N*geo.M))));
248
249
250
   %enzyme concentration in the bulk
251
    for i = ((3*geo.N*geo.M) + ((3+(3*geo.n))*geo.M)) + 1
252
253
        solvec(i) = sqrt(((1/((param.K_E_dec+(1/param.tau))*geo.M*
        geo.dV(i-(3*geo.N*geo.M))))*((param.K_tr_synth*
254
255
        sum((solvec(((2*qeo.N*qeo.M)+1):(3*qeo.N*qeo.M)).*(qeo.dV.'))))-
        (param.K_E_dec*sum((solvec(((3*geo.N*geo.M)+1):((3*geo.N*geo.M)+
256
```

```
257
       ((2+(3*geo.n))*geo.M))).*((geo.dV(1:((2+(3*geo.n))*geo.M))).')))))))))
         solvec (i) = (param.k_conv_E_v*2*pi*geo.dz*geo.r(i-(3*geo.N*geo.M))*
  % solvec(i-geo.M))/(((geo.V_v/geo.M)*(param.K_E_dec+(1/param.tau)))+
260 % (param.k_conv_E_v*2*pi*geo.dz*geo.r(i-(3*geo.N*geo.M))));
261 end
262 for i = ((3*qeo.N*qeo.M) + ((3+(3*qeo.n))*qeo.M)) + 2 : (4*qeo.N*qeo.M)
       solvec(i) = solvec(i-1);
264 end
266 %% Hydrolysis network
267 param.c_E_b = solvec(4*geo.N*geo.M);
268 param.c_E_b_endo = param.frac_E_endo_Tr*param.c_E_b;
269 param.c_E_b_exo = param.frac_E_exo_Tr*param.c_E_b;
270 param.c_E_b_BG = param.frac_E_betaG_Tr*param.c_E_b;
271 if itercount==0
272 hydrosolvec_0(9) = 0.5*param.c_E_b_endo;
273 hydrosolvec_0(11) = 0.5*param.c_E_b_exo;
274 end
276 % call fsolve to solve the hydrolysis reaction network
277 opt = optimset('LargeScale','off','Jacobian','off','TolX',1.0e-15,
278 'TolFun', 1.0e-15); %'TolX', 1.0e-15, 'TolFun', 1.0e-15);
279 [hydrosolvec, fval, exitflag] =
280 fsolve(@fsolve_bulk_reactions, hydrosolvec_0, opt, param);
281 hydrosolvec_0=hydrosolvec;
282
283 param.c_C_in_endo = abs(hydrosolvec(1));
284 param.c_C_b = abs(hydrosolvec(3));
285 param.r_C = hydrosolvec(4);
286 param.c_EC_endo = abs(hydrosolvec(5));
287 param.c_EC_exo = abs(hydrosolvec(6));
288 param.c_C_endo = abs(hydrosolvec(7));
289 param.c_C_exo = abs(hydrosolvec(8));
290 param.c_E_f_endo = abs(hydrosolvec(9));
291 param.c_C_f_endo = abs(hydrosolvec(10));
292 param.c_E_f_exo = abs(hydrosolvec(11));
293 param.c_C_f_exo = abs(hydrosolvec(12));
param.c_Cb_b = abs(hydrosolvec(13));
param.c_G_b = abs(hydrosolvec(14));
296 param.r_y_b = hydrosolvec(15);
297 param.c_X_y_b = abs(hydrosolvec(16));
298 param.c_EtOH_b = abs(hydrosolvec(17));
299
300 %% Concentration profiles cellobiose, glucose, yeast & ethanol
301
302 %cellobiose concentration in the inner membrane phase & membrane
303 for i = (4*qeo.N*qeo.M) + 1 : (4*qeo.N*qeo.M) + ((2+qeo.n)*qeo.M)
```

```
solvec(i) = 0;
304
305
   %cellobiose concentration in the fungal/yeast biofilm
306
   for i = (4 \times \text{geo.N} \times \text{geo.M}) + ((2 + \text{geo.n}) \times \text{geo.M}) + 1
307
        solvec(i) = (1/((chem.D_w_Cb/(geo.dz^2))+(2*pi*chem.D_w_Cb*geo.dz/
308
        \log(\text{geo.r}(i-(4*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(4*\text{geo.N*geo.M})))
309
        (param.K_Cb*param.frac_E_betaG_Tr*solvec(i-(geo.N*geo.M))/
310
        ((param.K m*(1+(solvec(i+(geo.N*geo.M)))))+(solvec(i)))))))*
311
        ((chem.D_w_Cb*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_Cb*geo.dz*)
312
        solvec(i+geo.M)/log(geo.r(i-(4*geo.N*geo.M))/
313
        geo.r(geo.M+i-(4*geo.N*geo.M))));
314
315
   end
   for i = (4*geo.N*geo.M) + ((2+geo.n)*geo.M) + 2:
316
        ((4*qeo.N*qeo.M) + ((3+qeo.n)*qeo.M)) - 1
317
        solvec(i) = (1/((2*chem.D_w_Cb/(geo.dz^2)) +
318
        (2*pi*chem.D_w_Cb*qeo.dz/log(qeo.r(i-(4*qeo.N*qeo.M))/
319
        geo.r(geo.M+i-(4*geo.N*geo.M)))+(param.K_Cb*param.frac_E_betaG_Tr*
320
321
        solvec(i-(qeo.N*qeo.M))/((param.K_m*(1+(solvec(i+(qeo.N*qeo.M))))))
        (solvec(i)))))))*((chem.D_w_Cb*(solvec(i-1)+solvec(i+1))/(geo.dz^2))+
        (2*pi*chem.D_w_Cb*geo.dz*solvec(i+geo.M)/log(geo.r(i-(4*geo.N*geo.M))/
323
        geo.r(geo.M+i-(4*geo.N*geo.M))));
324
   end
325
   for i = ((4*geo.N*geo.M) + ((3+geo.n)*geo.M))
326
327
        solvec(i) = (1/((chem.D_w_Cb/(geo.dz^2)) + (2*pi*chem.D_w_Cb*geo.dz/
        \log(\text{geo.r}(i-(4*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(4*\text{geo.N*geo.M})))
        (param.K_Cb*param.frac_E_betaG_Tr*solvec(i-(geo.N*geo.M))/((param.K_m*
329
        (1+(solvec(i+(geo.N*geo.M)))))+(solvec(i))))))*((chem.D w Cb*
330
        solvec(i-1)/(geo.dz^2)) + (2*pi*chem.D_w_Cb*geo.dz*solvec(i+geo.M)/
331
332
        log(geo.r(i-(4*geo.N*geo.M))/geo.r(geo.M+i-(4*geo.N*geo.M)))));
   end
333
   for i = (4*qeo.N*qeo.M) + ((3+qeo.n)*qeo.M) + 1:
334
        ((4*geo.N*geo.M) + ((2+(3*geo.n))*geo.M))
335
             if (i-1)/(geo.M) \( floor((i-1)/(geo.M)) \( && \)
336
337
                 i/(geo.M) \( floor(i/(geo.M)) \)
             solvec (i) = sqrt(((1/((-4*pi*chem.D_w_Cb/(geo.dr^2))+
338
             (-4*pi*chem.D w Cb/(geo.dz^2)) + (-(param.K Cb*
339
             param.frac_E_betaG_Tr*solvec(i-(geo.N*geo.M))/
340
             ((param.K_m*(1+(solvec(i+(geo.N*geo.M)))))+(solvec(i)))))))*
341
             (((solvec(i+1)*(2*pi*chem.D_w_Cb/(geo.dz^2)))+(solvec(i-1)*)
342
343
             (2*pi*chem.D_w_Cb/(geo.dz^2))) + (solvec(i+geo.M)*((2*pi*chem.D_w_Cb/
             (\text{geo.dr}^2)) + (2 \cdot \text{pi} \cdot \text{chem.D}_w_E / (2 \cdot \text{geo.dr} \cdot \text{geo.r} (i - (4 \cdot \text{geo.N} \cdot \text{geo.M}))))))
344
             + (solvec(i-geo.M)*((2*pi*chem.D_w_Cb/(geo.dr^2))-(2*pi*chem.D_w_E/
345
             (2*geo.dr*geo.r(i-(4*geo.N*geo.M)))))))))))))))
346
347
             elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
             solvec (i) = sqrt(((1/((-4*pi*chem.D_w_Cb/(geo.dr^2))+
348
             (2*pi*chem.D_w_Cb/(geo.dz^2))+(-(param.K_Cb*param.frac_E_betaG_Tr*
349
             solvec(i-(geo.N*geo.M))/((param.K_m*(1+(solvec(i+(geo.N*geo.M))))))
350
```

```
351
                        (solvec(i))))))*(((solvec(i+1)*(-4*pi*chem.D_w_Cb/(geo.dz^2)))+
                        (solvec(i+2)*(2*pi*chem.D_w_Cb/(qeo.dz^2)))+(solvec(i+qeo.M)*
352
                        ((2*pi*chem.D_w_Cb/(geo.dr^2))+(2*pi*chem.D_w_E/(2*geo.dr*
353
                       geo.r(i-(4*geo.N*geo.M))))))+(solvec(i-geo.M)*((2*pi*chem.D_w_Cb/Seo.M))))))
354
                        (geo.dr^2))-(2*pi*chem.D_w_E/(2*geo.dr*
355
                       geo.r(i-(4*geo.N*geo.M))))))))))));
356
                       elseif i/(geo.M) ==floor(i/(geo.M))
357
                       solvec (i) = sqrt(((1/((-4*pi*chem.D_w_Cb/(geo.dr^2))+
358
                        (2*pi*chem.D_w_Cb/(geo.dz^2))+(-(param.K_Cb*param.frac_E_betaG_Tr*
359
                       solvec(i-(geo.N*geo.M))/((param.K_m*(1+(solvec(i+(geo.N*geo.M)))))+
360
                        (solvec(i))))))*(((solvec(i-1)*(-4*pi*chem.D_w_Cb/(geo.dz^2)))+
361
                        (solvec(i-2)*(2*pi*chem.D_w_Cb/(geo.dz^2)))+(solvec(i+geo.M)*
362
                        ((2*pi*chem.D_w_Cb/(geo.dr^2))+(2*pi*chem.D_w_E/(2*geo.dr*
363
                       geo.r(i-(4*geo.M*geo.N))))))+(solvec(i-geo.M)*((2*pi*chem.D_w_Cb/M)))))
364
                        (geo.dr^2))-(2*pi*chem.D_w_E/(2*geo.dr*
365
                       geo.r(i-(4*geo.N*geo.M)))))))))))));
                       end
367
368
       %cellobiose concentration in biofilm boundary layer
       for i = ((4*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1 :
               ((4*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
371
372
               solvec(i) = solvec(i+geo.M);
               %no mass transfer limiting convective boundary layer is assumed
373
374
375
      end
376
      %cellobiose concentration in the bulk
      for i = ((4 \times \text{geo.N} \times \text{geo.M}) + ((3 + (3 \times \text{geo.M})) \times \text{geo.M})) + 1 : (5 \times \text{geo.N} \times \text{geo.M})
377
               solvec(i) = param.c_Cb_b;
378
379
      end
380
      %glucose concentration in the inner membrane phase & membrane
381
       for i = (5*qeo.N*qeo.M) + 1 : (5*qeo.N*qeo.M) + ((2+qeo.n)*qeo.M)
               solvec(i) = 0;
383
384
      end
      %glucose concentration in the fungal/yeast biofilm
       for i = (5*geo.N*geo.M) + ((2+geo.n)*geo.M) + 1
386
               solvec(i) = (1/((chem.D_w_E/(geo.dz^2)) + (2*pi*chem.D_w_G*geo.dz/
387
               log(geo.r(i-(5*geo.N*geo.M))/geo.r(geo.M+i-(5*geo.N*geo.M)))+
               param.K\_E\_dec)))*((chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_G*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w*solvec(i+1)/(geo.dz^2))+(2*pi
389
               geo.dz*solvec(i+geo.M)/log(geo.r(i-(5*geo.N*geo.M))/
390
               , geo.r(geo.M+i-(5*geo.N*geo.M))))+(param.K_tr_synth*
391
               solvec(i-(geo.N*geo.M))));
392
393
      end
394
       for i = (5*geo.N*geo.M) + ((2+geo.n)*geo.M) + 2:
               ((5*geo.N*geo.M) + ((3+geo.n)*geo.M)) - 1
395
               solvec(i) = (1/((2*chem.D_w_E/(geo.dz^2)))+(2*pi*chem.D_w_G*geo.dz/
396
               \log(\text{geo.r}(i-(5*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(5*\text{geo.N*geo.M})))
397
```

```
398
             param.K_E_dec)))*((chem.D_w_G*(solvec(i-1)+solvec(i+1))/(geo.dz^2))+
              (2*pi*chem.D_w_G*qeo.dz*solvec(i+qeo.M)/log(qeo.r(i-(5*qeo.N*qeo.M))/
              geo.r(geo.M+i-(5*geo.N*geo.M))))+(param.K_tr_synth*
400
              solvec(i-(geo.N*geo.M))));
401
     end
402
      for i = ((5*qeo.N*qeo.M) + ((3+qeo.n)*qeo.M))
403
              solvec(i) = (1/((chem.D_w_E/(geo.dz^2)) + (2*pi*chem.D_w_G*geo.dz/
404
              \log(\text{geo.r}(i-(5*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(5*\text{geo.N*geo.M})))
405
              param.K\_E\_dec)))*((chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D\_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solvec(i-1)/(geo.dz^2))+(2*pi*chem.D_w\_G*solve
              geo.dz*solvec(i+geo.M)/log(geo.r(i-(5*geo.N*geo.M))/
407
              geo.r(geo.M+i-(5*geo.N*geo.M))))+(param.K_tr_synth*
408
              solvec(i-(geo.N*geo.M)));
409
410
     end
      for i = (5*qeo.N*qeo.M) + ((3+qeo.n)*qeo.M) + 1:
411
              ((5*geo.N*geo.M) + ((2+(3*geo.n))*geo.M))
              if solvec(i-(5*geo.M*geo.N))>param.c_ox_b
413
                     if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) &&
414
415
                             i/(geo.M) \( floor(i/(geo.M)) \)
                     solvec (i) = \operatorname{sqrt}((((1/((-4*pi*chem.D_w_G/(geo.dr^2))+
                      (-4*pi*chem.D_w_G/(geo.dz^2))+((360/342)*param.K_Cb*
417
                     solvec(i-(geo.N*geo.M))*param.frac E betaG Tr*
418
                     solvec(i-(2*qeo.N*qeo.M))/((param.K_m*(1+(solvec(i))))+
                      (solvec(i-(geo.N*geo.M))))))))(((solvec(i+1)*(2*pi*chem.D_w_G/
420
421
                      (\text{geo.dz}^2)) + (\text{solvec}(i-1) * (2*pi*chem.D_w_G/(\text{geo.dz}^2))) +
                      (solvec(i+geo.M)*((2*pi*chem.D_w_G/(geo.dr^2))+(2*pi*chem.D_w_G/
                      (2*geo.dr*geo.r(i-(5*geo.N*geo.M))))))+(solvec(i-geo.M)*
423
                      ((2*pi*chem.D w G/(geo.dr^2)) - (2*pi*chem.D w G/(2*geo.dr*))
424
                     geo.r(i-(5*geo.N*geo.M)))))))+(((-param.mu_max_tr/param.Y_G_tr)*
425
426
                     min((solvec(i)/(param.K_G+solvec(i))), (solvec(i-(5*geo.M*geo.N))/
                      (param.K_ox_tr+solvec(i-(5*geo.N*geo.M))))) * (param.K_tr_dec/
427
                      ((param.mu_max_tr*min((solvec(i)/(param.K_G+solvec(i)))),
                      (solvec(i-(5*geo.M*geo.N))/(param.K_ox_tr+
429
                     solvec(i-(5*geo.N*geo.M))))))+param.K_tr_dec))*
430
431
                     solvec(i-(4*geo.N*geo.M)))+(-param.M_G_tr*
432
                     solvec(i-(4*geo.M*geo.N))))))))));
                     elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
433
                     solvec (i) = sqrt((((1/((-4*pi*chem.D_w_G/(geo.dr^2))+
434
                      (2*pi*chem.D_w_G/(geo.dz^2)) + ((360/342)*param.K_Cb*
435
                     solvec(i-(geo.N*geo.M))*param.frac_E_betaG_Tr*
436
437
                     solvec(i-(2*geo.N*geo.M))/((param.K_m*(1+(solvec(i))))+
                      (solvec(i-(geo.N*geo.M))))))*(((solvec(i+1)*(-4*pi*chem.D_w_G/
438
                      (geo.dz^2)))+(solvec(i+2)*(2*pi*chem.D_w_G/(geo.dz^2)))+
439
                      (solvec(i+geo.M)*((2*pi*chem.D_w_G/(geo.dr^2))+(2*pi*chem.D_w_G/
440
                      (2*geo.dr*geo.r(i-(5*geo.N*geo.M))))))+(solvec(i-geo.M)*
                      ((2*pi*chem.D_w_G/(geo.dr^2))-(2*pi*chem.D_w_G/(2*geo.dr*
442
                     qeo.r(i-(5*qeo.N*qeo.M)))))))+(((-param.mu_max_tr/param.Y_G_tr)*
443
                     min((solvec(i)/(param.K_G+solvec(i))), (solvec(i-(5*geo.M*geo.N))/
444
```

```
445
            (param.K_ox_tr+solvec(i-(5*geo.N*geo.M))))) * (param.K_tr_dec/
446
            ((param.mu_max_tr*min((solvec(i)/(param.K_G+solvec(i)))),
            (solvec(i-(5*geo.M*geo.N))/(param.K_ox_tr+
447
            solvec(i-(5*geo.N*geo.M))))))+param.K_tr_dec))*
448
            solvec(i-(4*geo.N*geo.M)))+(-param.M_G_tr*
449
            solvec(i-(4*geo.M*geo.N))))))))));
450
            elseif i/(geo.M) ==floor(i/(geo.M))
451
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_G/(geo.dr^2))+
452
            (2*pi*chem.D_w_G/(geo.dz^2))+((360/342)*param.K_Cb*
453
            solvec(i-(geo.N*geo.M))*param.frac_E_betaG_Tr*
454
            solvec(i-(2*geo.N*geo.M))/((param.K_m*(1+(solvec(i))))+
455
            (solvec(i-(geo.N*geo.M))))))*(((solvec(i-1)*
456
            (-4*pi*chem.D_w_G/(geo.dz^2)))+(solvec(i-2)*(2*pi*chem.D_w_G/(geo.dz^2)))
457
            (geo.dz^2))) + (solvec(i+geo.M) * ((2*pi*chem.D_w_G/(geo.dr^2)) +
458
            (2*pi*chem.D_w_G/(2*geo.dr*geo.r(i-(5*geo.M*geo.N)))))))+
459
            (solvec(i-qeo.M)*((2*pi*chem.D_w_G/(qeo.dr^2))-(2*pi*chem.D_w_G/
            (2*geo.dr*geo.r(i-(5*geo.N*geo.M)))))))+
461
            (((-param.mu_max_tr/param.Y_G_tr) *min((solvec(i)/
462
            (param.K_G+solvec(i))), (solvec(i-(5*geo.M*geo.N))/
            (param.K_ox_tr+solvec(i-(5*geo.N*geo.M)))))*(param.K_tr_dec/
464
            ((param.mu_max_tr*min((solvec(i)/(param.K_G+solvec(i))),
465
            (solvec(i-(5*geo.M*geo.N))/(param.K_ox_tr+
            solvec(i-(5*geo.N*geo.M))))))+param.K_tr_dec))*
467
            solvec(i-(4*geo.N*geo.M)))+(-param.M_G_tr*
468
            solvec(i-(4*geo.M*geo.N)))))))))));
469
470
            end
       elseif solvec(i-(5*geo.M*geo.N)) ≤ param.c_ox_b
471
            if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) & &
472
473
                i/(geo.M) \( floor(i/(geo.M)) \)
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_G/(geo.dr^2)))+(-4*pi*
474
            chem.D_w_G/(qeo.dz^2))+((360/342)*param.K_Cb*
475
            solvec(i-(geo.N*geo.M))*param.frac_E_betaG_Tr*
476
            solvec(i-(2*geo.N*geo.M))/((param.K_m*(1+(solvec(i))))+
477
478
            (solvec(i-(geo.N*geo.M)))))-((1/param.Y_X_Y_G)*
            (param.mu_max_Y*solvec(i+(geo.N*geo.M))/(solvec(i)+param.K_G))*
479
            (1-(solvec(i+(2*geo.M*geo.N))))))))))))))))))
480
            (\text{geo.dz}^2)) + (\text{solvec}(i-1) * (2*pi*chem.D_w_G/(\text{geo.dz}^2))) +
481
            (solvec(i+geo.M)*((2*pi*chem.D_w_G/(geo.dr^2))+(2*pi*chem.D_w_G/(geo.dr^2)))
            (2*geo.dr*geo.r(i-(5*geo.N*geo.M))))))+(solvec(i-geo.M)*
483
            ((2*pi*chem.D_w_G/(geo.dr^2))-(2*pi*chem.D_w_G/(2*geo.dr*
484
            geo.r(i-(5*geo.N*geo.M))))))))))));
485
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
486
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_G/(geo.dr^2))+
487
488
            (2*pi*chem.D_w_G/(geo.dz^2))+((360/342)*param.K_Cb*
            solvec(i-(geo.N*geo.M))*param.frac_E_betaG_Tr*
489
            solvec(i-(2*geo.N*geo.M))/((param.K_m*(1+(solvec(i))))+
490
            (solvec(i-(geo.N*geo.M)))))-((1/param.Y_X_Y_G)*
491
```

```
492
            (param.mu_max_Y*solvec(i+(geo.N*geo.M))/(solvec(i)+param.K_G))*
            (1-(solvec(i+(2*qeo.M*qeo.N))))))*(((solvec(i+1)*
            (-4 * pi * chem.D_w_G/(geo.dz^2))) + (solvec(i+2) * (2 * pi * chem.D_w_G/
            (geo.dz^2)) + (solvec(i+geo.M) * ((2*pi*chem.D_w_G/(geo.dr^2)) +
495
            (2*pi*chem.D_w_G/(2*geo.dr*geo.r(i-(5*geo.N*geo.M))))))+
496
            (solvec(i-qeo.M)*((2*pi*chem.D_w_G/(qeo.dr^2))-(2*pi*chem.D_w_G/
            (2*geo.dr*geo.r(i-(5*geo.N*geo.M))))))))))))))))
498
           elseif i/(geo.M) ==floor(i/(geo.M))
499
           solvec (i) = sqrt((((1/((-4*pi*chem.D_w_G/(geo.dr^2))+
500
            (2*pi*chem.D_w_G/(geo.dz^2))+((360/342)*param.K_Cb*
501
           solvec(i-(geo.N*geo.M))*param.frac_E_betaG_Tr*
502
           solvec(i-(2*geo.N*geo.M))/((param.K_m*(1+(solvec(i))))+
503
            (solvec(i-(geo.N*geo.M)))))-((1/param.Y_X_Y_G)*
504
            (param.mu_max_Y*solvec(i+(geo.N*geo.M))/(solvec(i)+param.K_G))*
505
            506
           chem.D_w_G/(qeo.dz^2))+(solvec(i-2)*(2*pi*chem.D_w_G/(qeo.dz^2)))+
507
            (solvec(i+geo.M)*((2*pi*chem.D_w_G/(geo.dr^2))+(2*pi*chem.D_w_G/
508
509
            (2*qeo.dr*qeo.r(i-(5*qeo.M*qeo.N)))))+(solvec(i-qeo.M)*
            ((2*pi*chem.D_w_G/(geo.dr^2))-(2*pi*chem.D_w_G/(2*geo.dr*
           geo.r(i-(5*geo.N*geo.M))))))))))))))))
511
512
           end
       end
514
  end
515
   %glucose concentration in biofilm boundary layer
   for i = ((5*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1 :
       ((5*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
517
       solvec(i) = solvec(i+geo.M);
518
       %no mass transfer limiting convective boundary layer is assumed
519
  end
520
  %glucose concentration in the bulk
521
   for i = ((5*qeo.N*qeo.M) + ((3+(3*qeo.n))*qeo.M)) + 1 : (6*qeo.N*qeo.M)
       solvec(i) = param.c_G_b;
523
  end
524
525
   %yeast concentration in the inner membrane phase & membrane
   for i = (6*geo.N*geo.M) + 1 : (6*geo.N*geo.M) + ((2+geo.n)*geo.M)
527
       solvec(i) = 0;
528
529
  end
   %yeast concentration in the fungal/yeast biofilm
530
531
   for i = (6*geo.N*geo.M) + ((2+geo.n)*geo.M) + 1:
       ((6*geo.N*geo.M) + ((2+(3*geo.n))*geo.M))
532
       if solvec(i-(6*geo.M*geo.N))>param.c_ox_b
533
           solvec(i) = 0;
534
535
       elseif solvec(i-(6*geo.M*geo.N)) ≤ param.c_ox_b
536
           solvec(i) = param.mean_rho_Y*solvec(i-(geo.N*geo.M))/
537
            (sum(solvec(((5*qeo.N*qeo.M)+((2+qeo.n)*qeo.M)+1):((5*qeo.N*qeo.M)+
            ((2+(3*geo.n))*geo.M))))/nnz(solvec(((5*geo.N*geo.M)+
538
```

```
539
             ((2+\text{geo.n}) * \text{geo.M}) + 1) : ((5*\text{geo.N}* \text{geo.M}) + ((2+(3*\text{geo.n})) * \text{geo.M})))));
540
        end
   end
   %yeast concentration in biofilm boundary layer
   for i = ((6*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1 :
        ((6*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
        solvec(i) = solvec(i+geo.M);
545
        %no mass transfer limiting convective boundary layer is assumed
546
   %yeast concentration in the bulk
   for i = ((6 \cdot qeo.N \cdot qeo.M) + ((3 + (3 \cdot qeo.M)) \cdot qeo.M)) + 1 : (7 \cdot qeo.N \cdot qeo.M)
549
        solvec(i) = param.c_X_y_b;
550
551
   end
552
553 param.last_iter =solvec(((7*geo.N*geo.M)+1):(8*geo.N*geo.M));
   %ethanol concentration in the inner membrane phase & inner membrane wall
   for i = (7*geo.N*geo.M) + 1 : (7*geo.N*geo.M) + (2*geo.M)
555
        solvec(i) = (param.c_EtOH_b/chem.H_EtOH) *chem.M_EtOH/
556
        (chem.R_gas*param.T_m_K);
        %no mass transfer limiting convective boundary layer is assumed
558
559
   end
   %ethanol concentration within the membrane
   for i = (7*geo.N*geo.M) + (2*geo.M) + 1 : (7*geo.N*geo.M) + ((2+geo.n)*geo.M)
562
        solvec(i) = (param.c_EtOH_b/chem.H_EtOH) *chem.sol_m_EtOH;
563
   end
   %ethanol concentration in the fungal/yeast biofilm
564
   for i = (7*geo.N*geo.M) + ((2+geo.n)*geo.M) + 1
565
        if solvec(i-(2*geo.N*geo.M))\leq0.05
566
        solvec(i) = (1/((chem.D_w_EtOH/(geo.dz^2))+(2*pi*chem.D_w_EtOH*geo.dz/
567
       log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))+
568
        param.K_DEGR_EtOH)))*((chem.D_w_EtOH*solvec(i+1)/(geo.dz^2))+
569
       (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
570
        log(geo.r(i-(7*geo.N*geo.M)))/geo.r(geo.M+i-(7*geo.N*geo.M)))));
571
572
        if solvec(i-(2*geo.N*geo.M))\geq0.05
573
        solvec(i) = (1/((chem.D_w_EtOH/(geo.dz^2)) + (2*pi*chem.D_w_EtOH*)
574
        qeo.dz/log(qeo.r(i-(7*qeo.N*qeo.M))/qeo.r(qeo.M+i-(7*qeo.N*qeo.M)))+
575
        param.K_degr_EtOH))) * ((chem.D_w_EtOH*solvec(i+1)/(geo.dz^2))+
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
577
578
        log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))));
579
580
   end
   for i = (7*geo.N*geo.M) + ((2+geo.n)*geo.M) + 2:
581
582
        ((5*geo.N*geo.M) + ((3+geo.n)*geo.M)) - 1
        if solvec(i-(2*geo.N*geo.M)) \le 0.05
583
        solvec(i) = (1/((2*chem.D_w_EtOH/(geo.dz^2))+(2*pi*chem.D_w_EtOH*)
584
        geo.dz/log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))+
585
```

```
586
       param.K_DEGR_EtOH))) * ((chem.D_w_EtOH* (solvec(i-1)+solvec(i+1))/
587
        (geo.dz^2))+(2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
        log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))));
588
589
        if solvec(i-(2*geo.N*geo.M))\geq0.05
590
        solvec(i) = (1/((2*chem.D_w_EtOH/(geo.dz^2))+(2*pi*chem.D_w_EtOH*
591
       geo.dz/log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))+
502
       param.K_degr_EtOH)))*((chem.D_w_EtOH*(solvec(i-1)+solvec(i+1))/
593
        (geo.dz^2))+(2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
594
        log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))));
595
       end
596
597
   end
598
   for i = ((7*geo.N*geo.M) + ((3+geo.n)*geo.M))
        if solvec(i-(2*geo.N*geo.M))<0.05
599
        solvec(i) = (1/((chem.D_w_EtOH/(geo.dz^2)) + (2*pi*chem.D_w_EtOH*)
600
       qeo.dz/log(qeo.r(i-(7*qeo.N*qeo.M))/qeo.r(qeo.M+i-(7*qeo.N*qeo.M)))+
601
       param.K_DEGR_EtOH))) * ((chem.D_w_EtOH*solvec(i-1)/(geo.dz^2))+
602
603
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
604
       \log(\text{geo.r}(i-(7*\text{geo.N*geo.M}))/\text{geo.r}(\text{geo.M+i-}(7*\text{geo.N*geo.M})))));
       end
605
        if solvec(i-(2*geo.N*geo.M))>0.05
606
        solvec(i) = (1/((chem.D_w_EtOH/(geo.dz^2))) + (2*pi*chem.D_w_EtOH*)
       \text{geo.dz/log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))}
608
609
       param.K_degr_EtOH)))*((chem.D_w_EtOH*solvec(i-1)/(geo.dz^2))+
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
        \log(\text{qeo.r(i-(7*qeo.N*qeo.M))/qeo.r(qeo.M+i-(7*qeo.N*qeo.M))))};
611
612
   end
613
614
   for i = (7*geo.N*geo.M) + ((3+geo.n)*geo.M) + 1:
        ((7*geo.N*geo.M) + ((2+(3*geo.n))*geo.M))
615
        if solvec(i-(7*geo.M*geo.N))>param.c_ox_b
616
            if solvec(i-(2*geo.N*geo.M))\leq0.05
617
            if (i-1)/(geo.M) \( floor((i-1)/(geo.M)) \( && \)
618
619
                i/(geo.M) \( floor(i/(geo.M)) \)
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
620
            (-4*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
621
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*
            (2*pi*chem.D_w_EtOH/(geo.dz^2))) + (solvec(i+geo.M)*
623
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
624
625
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
626
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))))))
627
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
628
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
630
            (((solvec(i+1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+2)*
631
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
632
```

```
633
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
634
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
635
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))))))))))))
636
            elseif i/(geo.M) ==floor(i/(geo.M))
637
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
638
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
639
            (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2))))+(solvec(i-2)*
640
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
642
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
643
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
644
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))))))
645
            end
646
            end
647
            if solvec(i-(2*geo.N*geo.M))\geq0.05
648
            if (i-1)/(geo.M) \( \)floor((i-1)/(geo.M)) &&
649
650
                i/(geo.M) \( floor(i/(geo.M)) \)
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
            (-4*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
652
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*
653
654
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
655
656
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))))))
658
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
659
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
660
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
661
            (((solvec(i+1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+2)*)
662
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
663
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
664
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
665
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
666
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))))))
667
            elseif i/(geo.M) ==floor(i/(geo.M))
668
            solvec (i) = sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
669
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
670
            (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-2)*)
671
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
672
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
673
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
674
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
675
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))))))
            end
677
678
            end
679
       elseif solvec(i-(7*geo.M*geo.N)) ≤ param.c_ox_b
```

```
if (i-1)/(geo.M) \( \)floor((i-1)/(geo.M)) &&
680
                 i/(geo.M) \( floor(i/(geo.M)) \)
681
            solvec (i) = sqrt((((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
682
            (-4*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
683
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*
684
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
685
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
686
            (2 \times \text{geo.dr} \times \text{geo.r}(i - (7 \times \text{geo.N} \times \text{geo.M}))))) + (\text{solvec}(i - \text{geo.M}) \times
687
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))+
            ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N))/
690
            (param.K_G+solvec(i-(2*geo.M*geo.N)))) *
691
            (1-(solvec(i)/param.K_X_EtOH))))^2);
692
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
693
            solvec (i) = sqrt(((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
694
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
            (((solvec(i+1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+2)*
696
697
            (2*pi*chem.D_w_EtOH/(geo.dz^2))) + (solvec(i+geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
699
            ((2*pi*chem.D w EtOH/(geo.dr^2))-(2*pi*chem.D w EtOH/
700
701
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))+
            ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N)))/
702
703
            (param.K_G+solvec(i-(2*geo.M*geo.N)))) *
            (1-(solvec(i)/param.K_X_EtOH))))^2);
            elseif i/(geo.M) ==floor(i/(geo.M))
705
            solvec (i) = sqrt(((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
706
707
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
708
            (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+
            (solvec(i-2)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
709
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
711
            (2*geo.dr*geo.r(i-(7*geo.M*geo.N))))))+(solvec(i-geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
712
713
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))))+
714
            ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N))/
715
            (param.K G+solvec(i-(2*geo.M*geo.N))))*
            (1-(solvec(i)/param.K_X_EtOH))))^2);
716
            end
717
        end
718
719
   end
   %ethanol concentration in biofilm boundary layer
720
   for i = ((7*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1:
721
        ((7*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
722
723
        solvec(i) = solvec(i+geo.M);
        %no mass transfer limiting convective boundary layer is assumed
724
725
  end
   %ethanol concentration in the bulk
```

```
727 for i = ((7*qeo.N*qeo.M) + ((3+(3*qeo.n))*qeo.M)) + 1 : (8*qeo.N*qeo.M)
              solvec(i) = param.c_EtOH_b;
728
729
      end
730
731 %% error calculation oxygen
732 % oxygen inner membrane phase
     for i= 1: geo.M
                      errvec(i) = (chem.sol_m_ox*param.p_m(i)*param.n_ox_m);
734
      %oxygen at membrane wall (neglecting convective boundary layer)
      for i = geo.M+1 : 2*geo.M
737
738
              errvec(i) = (chem.sol_m_ox*param.p_m(i-geo.M)*param.n_ox_m);
739
      end
740
      %oxygen in membrane
      for i = (2*geo.M) + 1 : (2+geo.n)*geo.M
              if (i-1)/(qeo.M) \neq floor((i-1)/(qeo.M)) & i/(qeo.M) \neq floor(i/(qeo.M))
742
              errvec(i) = (1/((-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/
743
744
              (geo.dz^2))+(0)))*((solvec(i+1)*(2*pi*chem.D_m_ox/(geo.dz^2)))+
               (solvec(i-1)*(2*pi*chem.D_m_ox/(geo.dz^2)))+(solvec(i+geo.M)*
              ((2*pi*chem.D_m_ox/(geo.dr^2))+(2*pi*chem.D_m_ox/(2*geo.dr*geo.r(i)))))
746
              +(solvec(i-geo.M)*((2*pi*chem.D_m_ox/(geo.dr^2))-(2*pi*chem.D_m_ox/
747
              (2*geo.dr*geo.r(i)))));
              elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
749
750
              errvec (i) = (1/((-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.D_m_ox/(geo.dr^2))+(-4*pi*chem.
              (geo.dz^2))+(0)))*((solvec(i+1)*(-4*pi*chem.D_m_ox/(geo.dz^2)))+
751
              (solvec(i+2)*(2*pi*chem.D_m_ox/(geo.dz^2)))+(solvec(i+geo.M)*
752
              ((2*pi*chem.D_m_ox/(geo.dr^2))+(2*pi*chem.D_m_ox/(2*geo.dr*geo.r(i)))))
753
              + (solvec(i-geo.M) * ((2*pi*chem.D_m_ox/(geo.dr^2)) - (2*pi*chem.D_m_ox/
754
              (2*geo.dr*geo.r(i)))));
755
              elseif i/(geo.M) ==floor(i/(geo.M))
756
              errvec (i) = (1/((-4*pi*chem.D_m_ox/(qeo.dr^2))+(-4*pi*chem.D_m_ox/
757
              (\text{geo.dz}^2) + (0)) \times ((\text{solvec}(i-1) \times (-4 \times \text{pi} \times \text{chem.D_m_ox}/(\text{geo.dz}^2))) +
              (solvec(i-2)*(2*pi*chem.D_m_ox/(geo.dz^2)))+(solvec(i+geo.M)*
759
760
               ((2*pi*chem.D_m_ox/(geo.dr^2))+(2*pi*chem.D_m_ox/(2*geo.dr*geo.r(i)))))
              +(solvec(i-geo.M)*((2*pi*chem.D_m_ox/(geo.dr^2))-(2*pi*chem.D_m_ox/(geo.dr^2)))
762
               (2*geo.dr*geo.r(i)))));
763
              end
      %oxygen in fungal biofilm
765
      for i = ((2+geo.n)*geo.M)+1 : ((2+(2*geo.n))*geo.M)
766
              if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) && i/(geo.M) \neq floor(i/(geo.M))
767
              errvec(i) = (1/((-4*pi*chem.D_w_ox/(geo.dr^2))+(-4*pi*chem.D_w_ox/(geo.dr^2)))
768
              (geo.dz^2))+(0)))*(((solvec(i+1)*(2*pi*chem.D_w_ox/(geo.dz^2)))+
769
770
              (solvec(i-1)*(2*pi*chem.D_w_ox/(geo.dz^2)))+(solvec(i+geo.M)*
              ((2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(2*geo.dr*geo.r(i)))))
771
772
              +(solvec(i-geo.M)*((2*pi*chem.D_w_ox/(geo.dr^2))-(2*pi*chem.D_w_ox/(geo.dr^2)))
773
              (2*geo.dr*geo.r(i))))))+((-param.mu_max_tr/param.Y_ox_tr)*
```

```
774
              min((1),(solvec(i)/(param.K_ox_tr+solvec(i))))*(param.K_tr_dec/
775
               ((param.mu_max_tr*min((1),(solvec(i)/(param.K_ox_tr+solvec(i)))))+
              param.K_tr_dec))*solvec(i+(geo.N*geo.M)))+(-param.M_ox_tr*
776
              solvec(i+(geo.M*geo.N)));
777
              elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
778
              errvec (i) = (1/((-4*pi*chem.D_w_ox/(geo.dr^2))+
779
               (2*pi*chem.D_w_ox/(geo.dz^2))+(0)))*(((solvec(i+1)*
780
               (-4*pi*chem.D_w_ox/(geo.dz^2)))+(solvec(i+2)*
781
               (2*pi*chem.D_w_ox/(geo.dz^2)))+(solvec(i+geo.M)*
782
               ((2*pi*chem.D_w_ox/(geo.dr^2))+(2*pi*chem.D_w_ox/(2*geo.dr*geo.r(i)))))
783
               + (solvec(i-qeo.M) * ((2*pi*chem.D_w_ox/(qeo.dr^2)) - (2*pi*chem.D_w_ox/(qeo.dr^2)) - (2*pi*
784
               (2*geo.dr*geo.r(i))))))+((-param.mu_max_tr/param.Y_ox_tr)*
785
              min((1),(solvec(i)/(param.K_ox_tr+solvec(i))))*(param.K_tr_dec/
786
               ((param.mu_max_tr*min((1),(solvec(i)/(param.K_ox_tr*solvec(i)))))+
787
              param.K_tr_dec)) *solvec(i+(geo.N*geo.M)))+(-param.M_ox_tr*
788
789
              solvec(i+(geo.M*geo.N))));
              elseif i/(geo.M) ==floor(i/(geo.M))
790
791
              errvec (i) = (1/((-4*pi*chem.D_w_ox/(geo.dr^2))+
               (2*pi*chem.D_w_ox/(geo.dz^2))+(0)))*(((solvec(i-1)*
               (-4*pi*chem.D_w_ox/(geo.dz^2)))+(solvec(i-2)*(2*pi*chem.D_w_ox/
793
794
               (\text{geo.dz}^2)) + (\text{solvec}(i+\text{geo.M}) * ((2*\text{pi*chem.D} \text{ w ox}/(\text{geo.dr}^2)) +
795
               (2*pi*chem.D_w_ox/(2*qeo.dr*qeo.r(i)))))+(solvec(i-qeo.M)*
               ((2*pi*chem.D_w_ox/(geo.dr^2))-(2*pi*chem.D_w_ox/
796
797
               (2*qeo.dr*qeo.r(i))))))+((-param.mu_max_tr/param.Y_ox_tr)*
              min((1),(solvec(i)/(param.K_ox_tr+solvec(i))))*(param.K_tr_dec/
799
               ((param.mu_max_tr*min((1),(solvec(i)/(param.K_ox_tr+solvec(i))))))
               +param.K_tr_dec)) *solvec(i+(geo.N*geo.M)))+(-param.M_ox_tr*
800
              solvec(i+(geo.M*geo.N)));
801
802
              end
803 end
      %oxygen in yeast biofilm
804
      for i = ((2+(2*geo.n))*geo.M)+1 : ((2+(3*geo.n))*geo.M)
              errvec(i) = param.c_ox_b;
806
807
      %oxygen at biofilm boundary layer
      for i = ((2+(3*geo.n))*geo.M)+1 : ((3+(3*geo.n))*geo.M)
809
              errvec(i) = param.c_ox_b;
810
     end
    %oxygen within bulk
812
813
      for i = ((3+(3*geo.n))*geo.M)+1 : geo.N*geo.M
              errvec(i) = param.c_ox_b;
814
815 end
      for i = 1 : geo.N*geo.M
816
              maxerrvec(i) = (errvec(i) - solvec(i)) / solvec(i);
818 end
819
     %ethanol concentration in the inner membrane phase & inner membrane wall
```

```
for i = (7*\text{geo.N*geo.M}) + 1 : (7*\text{geo.N*geo.M}) + (2*\text{geo.M})
        error(i)=solvec(i)-((param.c_EtOH_b/chem.H_EtOH)*chem.M_EtOH/
822
        (chem.R_gas*param.T_m_K));
823
824
        %no mass transfer limiting convective boundary layer is assumed
825 end
   %ethanol concentration within the membrane
   for i = (7*geo.N*geo.M) + (2*geo.M) + 1 : (7*geo.N*geo.M) + ((2*geo.m) *geo.M)
        error(i) = solvec(i) - ((param.c_EtOH_b/chem.H_EtOH) *chem.sol_m_EtOH);
828
   %ethanol concentration in the fungal/yeast biofilm
830
   for i = (7*qeo.N*qeo.M) + ((2+qeo.n)*qeo.M) + 1
831
        if solvec(i-(2*geo.N*geo.M))\leq0.05
832
       error(i) = solvec(i) - ((1/((chem.D_w_EtOH/(geo.dz^2)) +
833
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
834
        geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_DEGR_EtOH)))*
835
        ((chem.D_w_EtOH*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_EtOH*
       geo.dz*solvec(i+geo.M)/log(geo.r(i-(7*geo.N*geo.M))/
837
       geo.r(geo.M+i-(7*geo.N*geo.M)))));
838
       if solvec(i-(2*geo.N*geo.M))\geq0.05
840
       error(i) = solvec(i) - ((1/((chem.D w EtOH/(geo.dz^2)) +
841
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
       geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_degr_EtOH)))*
843
844
        ((chem.D_w_EtOH*solvec(i+1)/(geo.dz^2))+(2*pi*chem.D_w_EtOH*geo.dz*)
        solvec(i+geo.M)/log(geo.r(i-(7*geo.N*geo.M))/
        geo.r(geo.M+i-(7*geo.N*geo.M)))));
846
        end
847
   end
848
   for i = (7*geo.N*geo.M) + ((2+geo.n)*geo.M) + 2:
849
        ((5*geo.N*geo.M)+((3+geo.n)*geo.M))-1
850
        if solvec(i-(2*geo.N*geo.M))\leq0.05
851
        error(i) = solvec(i) - ((1/((2*chem.D_w_EtOH/(geo.dz^2))) +
852
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
853
        geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_DEGR_EtOH)))*
854
        ((chem.D_w_EtOH*(solvec(i-1)+solvec(i+1))/(geo.dz^2))+
855
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
856
        log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M))))));
857
       end
       if solvec(i-(2*geo.N*geo.M))\geq0.05
859
        error(i) = solvec(i) - ((1/((2*chem.D_w_EtOH/(geo.dz^2))) +
860
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
861
        geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_degr_EtOH)))*
862
        ((chem.D_w_EtOH*(solvec(i-1)+solvec(i+1))/(geo.dz^2))+
863
864
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
       log(geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M))))));
865
        end
866
867
   end
```

```
for i = ((7*geo.N*geo.M) + ((3+geo.n)*geo.M))
868
        if solvec(i-(2*geo.N*geo.M))\leq0.05
869
        error(i) = solvec(i) - ((1/((chem.D_w_EtOH/(geo.dz^2))) +
870
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
871
        geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_DEGR_EtOH)))*
872
        ((chem.D w EtOH*solvec(i-1)/(geo.dz^2))+
873
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
874
        \log(\text{geo.r(i-(7*geo.N*geo.M))/geo.r(geo.M+i-(7*geo.N*geo.M)))))};
875
876
        if solvec(i-(2*geo.N*geo.M))\geq0.05
877
        error(i) = solvec(i) - ((1/((chem.D_w_EtOH/(geo.dz^2))) +
878
        (2*pi*chem.D_w_EtOH*geo.dz/log(geo.r(i-(7*geo.N*geo.M))/
879
        geo.r(geo.M+i-(7*geo.N*geo.M)))+param.K_degr_EtOH)))*
880
        ((chem.D_w_EtOH*solvec(i-1)/(geo.dz^2))+
881
        (2*pi*chem.D_w_EtOH*geo.dz*solvec(i+geo.M)/
882
        \log(\text{qeo.r}(i-(7*\text{qeo.N}*\text{qeo.M}))/\text{qeo.r}(\text{qeo.M}+i-(7*\text{qeo.N}*\text{qeo.M}))))));
        end
884
885
   end
   for i = (7*geo.N*geo.M) + ((3+geo.n)*geo.M) + 1:
        ((7*geo.N*geo.M)+((2+(3*geo.n))*geo.M))
887
        if solvec(i-(7*geo.M*geo.N))>param.c ox b
888
            if solvec(i-(2*geo.N*geo.M))\leq0.05
            if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) & &
890
891
                i/(geo.M) \( floor(i/(geo.M)) \)
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2)))
            +(-4*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
893
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*)
894
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
895
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
896
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))+(solvec(i-geo.M)*
897
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
898
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))));
899
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
900
901
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2)))+
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
902
            (((solvec(i+1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+2)*
903
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
904
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
905
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
906
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
907
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))));
908
            elseif i/(geo.M) ==floor(i/(geo.M))
909
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2)))+
910
911
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_DEGR_EtOH)))*
            (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-2)*
912
913
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/(2*geo.dr*
914
```

```
915
            qeo.r(i-(7*qeo.N*qeo.M))))))+(solvec(i-qeo.M)*((2*pi*chem.D_w_EtOH/
            (geo.dr^2))-(2*pi*chem.D_w_EtOH/(2*geo.dr*
916
917
            geo.r(i-(7*geo.N*geo.M))))))))))));
            end
918
            end
919
            if solvec(i-(2*geo.N*geo.M))\geq0.05
920
            if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) &&
921
                i/(geo.M) \( floor(i/(geo.M)) \)
922
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2)))+
923
            (-4*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
924
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*
925
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
926
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
927
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
928
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
929
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))))))))));
930
            elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
931
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(qeo.dr^2)))+
932
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
            (((solvec(i+1) * (-4*pi*chem.D_w_EtOH/(geo.dz^2)))+
934
            (solvec(i+2)*(2*pi*chem.D w EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
935
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
937
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
938
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))));
            elseif i/(geo.M) ==floor(i/(geo.M))
940
            error (i) = solvec(i) - (sqrt((((1/((-4*pi*chem.D_w_EtOH/(geo.dr^2))+
941
            (2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
942
943
            (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-2)*
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
944
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
945
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
946
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
947
948
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))))));
            end
949
            end
950
        elseif solvec(i-(7*geo.M*geo.N)) ≤ param.c_ox_b
951
            if (i-1)/(geo.M) \neq floor((i-1)/(geo.M)) & &
952
                i/(geo.M) \( floor(i/(geo.M)) \)
953
954
            error (i) = solvec(i) - (sqrt(((((1/((-4*pi*chem.D_w_EtOH/
            (\text{geo.dr}^2)) + (-4 * \text{pi*chem.D_w_EtOH}/(\text{geo.dz}^2)) - \text{param.K_degr_EtOH}))) *
955
            (((solvec(i+1)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i-1)*)
956
            (2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
957
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))+(solvec(i-geo.M)*
959
            ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
960
            (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))))+
961
```

```
962
             ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N))/
             (param.K_G+solvec(i-(2*geo.M*geo.N))))*
963
             (1-(solvec(i)/param.K_X_EtOH))))^2));
             elseif (i-1)/(geo.M) == floor((i-1)/(geo.M))
965
             error (i) = solvec(i) - (sqrt((((((/(-4*pi*chem.D_w_EtOH/
966
             (geo.dr^2))+(2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
             (((solvec(i+1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+2)*
968
             (2*pi*chem.D w EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
969
             ((2*pi*chem.D_w_EtOH/(geo.dr^2))+(2*pi*chem.D_w_EtOH/
970
             (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))+(solvec(i-geo.M)*
971
             ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
972
             (2*geo.dr*geo.r(i-(7*geo.N*geo.M))))))))+
973
             ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N))/
974
             (param.K_G+solvec(i-(2*geo.M*geo.N)))) *
975
             (1-(solvec(i)/param.K_X_EtOH))))^2));
             elseif i/(geo.M) ==floor(i/(geo.M))
977
             error (i) = solvec(i) - (sqrt(((((1/((-4*pi*chem.D_w_EtOH/(qeo.dr^2)))
978
             +(2*pi*chem.D_w_EtOH/(geo.dz^2))-param.K_degr_EtOH)))*
979
             (((solvec(i-1)*(-4*pi*chem.D_w_EtOH/(geo.dz^2)))+
             (solvec(i-2)*(2*pi*chem.D_w_EtOH/(geo.dz^2)))+(solvec(i+geo.M)*
981
             ((2*pi*chem.D w EtOH/(geo.dr^2))+(2*pi*chem.D w EtOH/
982
             (2 \times \text{geo.dr} \times \text{geo.r}(i - (7 \times \text{geo.M} \times \text{geo.N}))))) + (\text{solvec}(i - \text{geo.M}) \times (1 \times \text{geo.M}))
             ((2*pi*chem.D_w_EtOH/(geo.dr^2))-(2*pi*chem.D_w_EtOH/
984
985
             (2*geo.dr*geo.r(i-(7*geo.N*geo.M)))))))))+
             ((param.Y_EtOH_G/param.Y_X_Y_G) * (solvec(i-(2*geo.M*geo.N))/
             (param.K_G+solvec(i-(2*geo.M*geo.N))))*
987
             (1-(solvec(i)/param.K X EtOH))))^2));
988
             end
989
990
        end
   end
991
   %ethanol concentration in biofilm boundary layer
    for i = ((7*geo.N*geo.M) + ((2+(3*geo.n))*geo.M)) + 1:
993
        ((7*geo.N*geo.M) + ((3+(3*geo.n))*geo.M))
994
995
        error(i) = solvec(i)-solvec(i+geo.M);
        %no mass transfer limiting convective boundary layer is assumed
996
   end
997
   %ethanol concentration in the bulk
    for i = ((7*geo.N*geo.M) + ((3+(3*geo.n))*geo.M)) + 1 : (8*geo.N*geo.M)
        error(i) = solvec(i) -param.c_EtOH_b;
1000
1001
   end
1002
   param.max_rel_error_ox = 100*max(maxerrvec);
1003
   param.max_rel_error_EtOH = 100 \times max(error(((7 \times geo.N \times geo.M) + 1)))
1004
    (8*geo.N*geo.M))./solvec(((7*geo.N*geo.M)+1):(8*geo.N*geo.M)));
   itercount=itercount+1;
1006
1007
   end
```

```
1 function sol = fsolve_bulk_reactions(hydrosolvec,param)
sol = zeros(12,1);
4 % 12 unknowns:
5 % hydrosolvec(1) = c_C_in_endo
6 % hydrosolvec(2) = c_C_in_exo = param.frac_exo_sites_C_in*param.c_C_in
7 % not included in the equation solving
8 \% \text{ hydrosolvec(3)} = c_C
9 \% \text{ hydrosolvec(4)} = r_C
10 % hydrosolvec(5) = c_EC_{endo}
11 % hydrosolvec(6) = c_EC_exo
12 % hydrosolvec(7) = c_C_endo
13 % hydrosolvec(8) = c_C_exo
14 % hydrosolvec(9) = c_E_f_endo
15 % hydrosolvec(10) = c_C_f_endo
16 % hydrosolvec(11) = c_E_f_exo
17 % hydrosolvec(12) = c_C_f_exo
18 % hydrosolvec(13) = c_Cb_b
19 % hydrosolvec(14) = c_G_b
20 % hydrosolvec(15) = r_y_b
21 % hydrosolvec(16) = c_X_y_b
22 % hydrosolvec(17) = c_EtOH_b
24 % 12 equations:
25 sol(1) = sqrt((hydrosolvec(1))^2)+(param.frac_exo_sites_C_in*
26 param.c_C_in)-param.c_C_in;
27 sol(2) = param.c_C_in+((hydrosolvec(4)*param.tau)+
28 sqrt((hydrosolvec(3))^2));
29 sol(3) = ((-1)*param.k_endo*(sqrt((hydrosolvec(5))^2)/
30 (1+param.sigma_endo)) * (param.K_C_Cb/(sqrt((hydrosolvec(13))^2)+
31 param.K_C_C) * (param.K_C_EtOH/(sqrt((hydrosolvec(17))^2)+param.K_C_EtOH)))
32 +((1/param.tau)*(sqrt((hydrosolvec(1))^2)-sqrt((hydrosolvec(7))^2)));
33 sol(4) = ((-1)*param.k_exo*(sqrt((hydrosolvec(6))^2)/(1+param.sigma_exo))*
34 (param.K_C_Cb/(sqrt((hydrosolvec(13))^2)+param.K_C_Cb))*(param.K_C_EtOH/Cb)
35 (sqrt((hydrosolvec(13))^2)+param.K_C_EtOH)))+((1/param.tau)*
36 ((param.frac_exo_sites_C_in*param.c_C_in)-sqrt((hydrosolvec(8))^2)));
sol(5) = sqrt((hydrosolvec(7))^2) + sqrt((hydrosolvec(8))^2) -
38 sqrt((hydrosolvec(3))^2);
39 sol(6) = (param.k_fc*sqrt((hydrosolvec(9))^2)*sqrt((hydrosolvec(10))^2)*
40 (1+param.sigma_endo))-(sqrt((hydrosolvec(5))^2)*((param.k_fc/param.K_endo)+
41 (1/param.tau)));
42 sol(7) = (param.k_fc*sqrt((hydrosolvec(11))^2)*sqrt((hydrosolvec(12))^2)*
43 (1+param.sigma_exo))-(sqrt((hydrosolvec(6))^2)*((param.k_fc/param.K_exo)+
44 (1/param.tau)));
45 sol(8) = param.c_E_b_endo-((sqrt((hydrosolvec(5))^2)*)
46 param.sigma_endo/(1+param.sigma_endo))+sqrt((hydrosolvec(9))^2));
```

```
47 sol(9) = param.c_E_b_exo-((sqrt((hydrosolvec(6))^2) *
48 param.sigma_exo/(1+param.sigma_exo))+sgrt((hydrosolvec(11))^2));
49 sol(10) = sqrt((hydrosolvec(7))^2) - ((sqrt((hydrosolvec(5))^2)/
50 (1+param.sigma_endo))+sqrt((hydrosolvec(10))^2));
51 sol(11) = sqrt((hydrosolvec(8))^2)-((sqrt((hydrosolvec(6))^2)/
52 (1+param.sigma_endo))+sqrt((hydrosolvec(12))^2));
sol(12) = ((342/324) * sqrt((hydrosolvec(4))^2)) + ((param.K_Cb*)
54 sqrt((hydrosolvec(13))^2)*param.c_E_b_BG/((param.K_m*
55 (1+(sqrt((hydrosolvec(14))^2)/param.K_Cb_G)))+(sqrt((hydrosolvec(13))^2))))
56 - (sqrt((hydrosolvec(13))^2)/param.tau));
57 sol(13) = ((360/342) * (param.K_Cb*sqrt((hydrosolvec(13))^2) *
58 param.c_E_b_BG/((param.K_m*(1+(sqrt((hydrosolvec(14))^2)/param.K_Cb_G)))+
59 sqrt((hydrosolvec(13))^2))))-((sqrt((hydrosolvec(15))^2)/param.Y_X_Y_G)+
60 (sqrt((hydrosolvec(14))^2)/param.tau));
61 sol(14) = ((param.mu_max_Y*sqrt((hydrosolvec(14))^2)/(param.K_G+
62 sgrt((hydrosolvec(14))^2)))*sgrt((hydrosolvec(16))^2)*
63 (1-(sqrt((hydrosolvec(17))^2)/param.K_X_EtOH)))-sqrt((hydrosolvec(15))^2);
64 sol(15) = sqrt((hydrosolvec(15))^2)-(sqrt((hydrosolvec(16))^2)/param.tau);
65 sol(16) = ((param.Y_EtOH_G/param.Y_X_Y_G) * sqrt((hydrosolvec(15))^2))-
66 (sqrt((hydrosolvec(17))^2)/param.tau);
67
68 end
```

```
1 %% Plot commands
2 figure()
3 surf(z_axis,r_axis,02);
4 colorbar;
5 axis ij;
6 % set(gca,'zscale','log')
7 title('Oxygen concentration profile across the membrane reactor');
8 xlabel('Membrane length [m]');
9 vlabel('Radius [m]');
10 zlabel('Oxygen concentration [g/L]');
12 figure()
13 surf(z_axis,r_axis,X_tr);
14 colorbar;
15 axis ij;
16 %set(gca,'zscale','log')
17 title...
      ('Fungal biomass concentration profile across the membrane reactor');
19 xlabel('Membrane length [m]');
20 ylabel('Radius [m]');
21 zlabel('Fungal biomass concentration [g/L]');
22
23 figure()
```

```
24 surf(z_axis,r_axis,X_tr_sec);
25 colorbar;
26 axis ij;
27 %set(gca,'zscale','log')
28 title...
29 ('Secondary mycelia concentration profile across the membrane reactor');
30 xlabel('Membrane length [m]');
31 ylabel('Radius [m]');
32 zlabel('Secondary mycelia concentration [g/L]');
34 figure()
35 surf(z_axis,r_axis,E);
36 colorbar;
37 axis ij;
38 %set(gca,'zscale','log')
39 title('Enzyme concentration profile across the membrane reactor');
40 xlabel('Membrane length [m]');
41 ylabel('Radius [m]');
42 zlabel('Enzyme concentration [g/L]');
43
44 figure()
45 surf(z_axis,r_axis,Cb);
46 colorbar;
47 axis ij;
48 %set(gca,'zscale','log')
49 title('Cellobiose concentration profile across the membrane reactor');
50 xlabel('Membrane length [m]');
51 ylabel('Radius [m]');
52 zlabel('Cellobiose concentration [g/L]');
53
54 figure()
55 surf(z_axis,r_axis,G);
56 colorbar;
57 axis ij;
58 %set(gca,'zscale','log')
59 title('Glucose concentration profile across the membrane reactor');
60 xlabel('Membrane length [m]');
61 ylabel('Radius [m]');
62 zlabel('Glucose concentration [g/L]');
63
64 figure()
65 surf(z_axis,r_axis,X_y);
66 colorbar;
67 axis ij;
68 %set(gca,'zscale','log')
69 title('Yeast concentration profile across the membrane reactor');
70 xlabel('Membrane length [m]');
```

```
71 ylabel('Radius [m]');
72 zlabel('Yeast concentration [g/L]');
73
74 figure()
75 surf(z_axis,r_axis,EtOH);
76 colorbar;
77 axis ij;
78 %set(gca,'zscale','log')
79 title('Ethanol concentration profile across the membrane reactor');
80 xlabel('Membrane length [m]');
81 ylabel('Radius [m]');
82 zlabel('Ethanol concentration [g/L]');
84 % figure()
85 % plot(r_axis, mu_tr, 'o')
86 % % plot(r_axis,c_02_z_L,'-')
87 x1=zeros(geo.M,1);
88 for i=1:qeo.M
89 x1(i) = (i-1) * geo.dz;
90 end
y1=100*02(2,:)./((1/param.n_ox_m)*02(2,1));
92 figure()
93 plot(x1,y1,'-')
94 title('Oxygen saturation in PDMS over membrane length');
95 xlabel('Membrane length [m]');
96 ylabel('Oxygen saturation [%]');
```

```
1 if param.Re_m≥param.Re_crit
      disp('Fully developed turbulent flow!')
      disp('Corresponding Nusselt/Sherwood correlations are applied')
4 end
5 if param.Re_m≤2300
      disp('Fully developed laminar flow! Corresponding Nusselt/')
      disp('Sherwood correlations are applied')
8 end
9 if param.Re_m>2300 && param.Re_m<param.Re_crit
      disp('Transient flow! All quantities are calculated by')
      disp('interpolation between laminar flow at Re_m=2300')
11
      disp('and turbulent flow at Re_m=Re_crit')
13 end
14 if param.Re_m>10^5 || param.Re_m<1</pre>
      disp('Expression for pressure loss not valid!')
      disp('Nusselt/Sherwood correlations for turbulent flow are valid')
17 end
18
19 if param.Re_m≥param.Re_crit
```

```
zeta=(0.3164/(param.Re_m^0.25)) * ...
20
21
           (1+(0.095*sqrt(geo.d_t_i/geo.d_curv)*(param.Re_m^0.25)));
       %friction factor for helical coils
23
   end
  if param.Re_m≤2300
24
       zeta=(64/param.Re_m)*(1+(0.033*...
           (((log10(param.Re_m*sqrt(geo.d_t_i/geo.d_curv)))^4))));
       %friction factor for helical coils [-]
27
  end
  if Re_m>2300 && Re_m<Re_crit
29
      p_loss=(((Re_m-2300)/(Re_crit-2300))*(((((0.3164/(Re_crit^0.25)))*...
30
           (1+(0.095*sqrt(di_m/d_curv)*(Re_crit^0.25))))*(l_m/di_m)*...
31
           (0.5*rho_w_m*(u_m^2))))-...
32
       ((((64/2300)*(1+(0.033*(((log10(2300*sqrt(di_m/d_curv)))^4)))))...
33
       34
       (((log10(2300*sqrt...
35
       (di_m/d_curv)))^4)))) * (L/di_m) * (0.5*rho_m*(u_m^2)));
36
37
  %interpolated pressure loss [Pa]
39
40
  % Nusselt correlations according to VDI heat atlas chapter G1
42
43
   if param.Re_m>param.Re_crit
      Xi = ((1.8 * log10 (param.Re_m)) - 1.5)^(-2);
45
       %factor for Nusselt correlation [-]
46
      Nu_m = ((0.125*Xi*param.Re_m*param.Pr_m)/(1+(12.7*sqrt(0.125*Xi)*...
47
           ((param.Pr_m^(2/3))-1))))*(1+((geo.d_t_i/geo.l_t)^(2/3)));
      %Nusselt number for inner memrane flow & medium [-]
49
       Sh_m=((0.125*Xi*param.Re_m*param.Sc_m)/(1+(12.7*sgrt(0.125*Xi)*...
50
           ((param.Sc_m^(2/3))-1)))*(1+((geo.d_t_i/geo.l_t)^(2/3)));
       %Sherwood number for inner memrane flow & medium [-]
52
53
  end
54
  if param.Re_m≤2300
55
       Nu_m = ((3.66^3) + 0.343 + (((1.615*((param.Re_m*param.Pr_m*...
56
           (geo.d_t_i/geo.l_t))^(1/3))-0.7)^3))^(1/3);
       %Nusselt number for inner memrane flow & medium [-]
58
59
       % (under asumption of a long pipe)
       Sh_m = ((3.66^3) + 0.343 + (((1.615 * ((param.Re_m*param.Sc_m*...
60
           (geo.d_t_i/geo.l_t))^(1/3))-0.7)^3))^(1/3);
61
       %Sherwood number for inner memrane flow & medium [-]
62
63
       %(under asumption of a long pipe
64
  end
65
  if param.Re_m>2300 && param.Re_m<param.Re_crit
```

```
Nu_m=(((param.Re_m-2300)/(param.Re_crit-2300))*...
67
           ((((0.125*(((1.8*log10(param.Re_crit))-1.5)^(-2))*...
68
           param.Re_crit*param.Pr_m)/(1+(12.7*sqrt(0.125*(((1.8*...
           log10 (param.Re\_crit))-1.5)^(-2)))*((param.Pr\_m^(2/3))-1)))*...
           (1+((geo.d_t_i/geo.l_t)^(2/3)))-4.364)+4.364;
71
      %Nusselt number for inner memrane flow & medium [-]
       Sh_m=(((param.Re_m-2300)/(param.Re_crit-2300))*...
           ((((0.125*(((1.8*log10(param.Re_crit))-1.5)^(-2))*...
74
           param.Re_crit*param.Sc_m)/(1+(12.7*sqrt(0.125*(((1.8*...
           log10(param.Re\_crit))-1.5)^(-2)))*((param.Sc\_m^(2/3))-1))))*...
           (1+((geo.d_t_i/geo.l_t)^(2/3)))-4.364)+4.364;
77
       %Sherwood number for inner memrane flow & medium [-]
79 end
80
 % Chilton-Colburn mass transfer analogy
81
82 %Sh_m=Nu_m*((Sc_m/Pr_m)^(1/3));
83 k_conv_ox_m=Sh_m*param.D_O2_m/geo.d_t_i;
84 k_conv_E=6e-6;
86
  %Sherwood correlation for enzymes biofilm bulk boundary layer
87
88 Sh_v_lam_E=0.664*sqrt(param.Re_v)*(param.Sc_v_E^(1/3));
89 Sh_v_turb_E=0.037*(param.Re_v^0.8)*param.Sc_v_E/(1+(2.443*...
       (param.Re_v^{(-0.1)}) * ((param.Sc_v_E^{(2/3)}) - 1)));
91 Sh_v_E=0.3+sqrt((Sh_v_lam_E^2)+(Sh_v_turb_E^2));
92 char_L_v=geo.h_wind*geo.l_t/(pi*geo.d_wind);
93 k_conv_E_v=Sh_v_E*chem.D_w_E/char_L_v;
```

## APPENDIX C

Supplementary material for chapter 6: Evaluation of *in-situ* product removal strategies to improve the productivity and economics of consolidated bioprocessing

## C.1 Calculations for CO<sub>2</sub> stripping

```
2 % Name: CO2stripping.m
3 % Author: Philipp Stampfli
 % E-Mail: stamphil@student.ethz.ch
 % Date: 11. July 2018
 % Update: 06.08.18
 % Purpose: Calculating the needed CO2-gas flow for stripping out the EtOH
           from the fermentation broth. In a 2nd step the design criteria
           for the bioreactor to reach the desired stripping effect
           (residence time of bubbles in the liquid)
12 % Notes:
13 % References: -...
 16 clear all
17 clc
19 %% Properties incoming stream and reactor volume
21 m_EtOH=21941/3600;%31.907/3600; % [kg/s], mass stream of EtOH generated
_{22} m_H2O=378525/3600;%234.594/3600; %[kg/s], mass stream of H2O total leaving
m_{CO2}=20955/3600;%33.833/3600; %[kg/s], mass stream of CO2 generated
```

```
24 \text{ m\_in}=450740/3600; %368.506/3600; %[kg/s], mass stream in reactor
26 p_reac=1.013; %[bar], pressure in reactor
27 T_reac=28+273; %50+273; %[K], temperature in reactor
28 V_reac=7*3785.411;%44.221; %[m3], total volume of reactors
29 V_ves=V_reac/7;%V_reac/5; %[m3], volume of each reactor vessel
31 %% specifications
33 FRg_EtOH=0.0001:0.0001:0.99; % mass recovery of EtOH in gas stream
34 lFR=length(FRq_EtOH);
35 %% conversion in moleflows and fractions
36 n_EtOH=m_EtOH/0.046; %[mol/s], mole flow of EtOh generated
37 n_CO2=m_CO2/0.044; %[mol/s], mole flow of CO2 generated
m_H20=m_H20/0.018; %[mol/s], mole flow of H2O total leaving
40 L=m_EtOH+m_H2O;
41 Ln=n_EtOH+n_H2O;
43 z_EtOH=m_EtOH/L;
44 z_H2O=m_H2O/L;
46 zn_EtOH=n_EtOH/Ln;
47 zn_H2O=n_H2O/Ln;
49 %% physiochemical constants
50 H_EtOH=4.7*exp(13/(1.9872*10^(-3))*(1/T_reac-1/298))*1000;
51 %Henry constant of Ethanol in water according to Snider et Dawson, 1985
52 KH_CO2=HenryCO2(zn_EtOH, T_reac);
54 %density of fluid: assumption all density same as the one for water
55 %density of vanillin (assumption for lignin from NREL) is 1060 kg7m3
56 %so all can be assumed as same density as water
57 rho_l=1000; %[kg/m3]
59 % density CO2
60 rho_g=0.044*p_reac*10^5/(8314*T_reac);
61 %surface tension of EtOH/water mixture (Khattab et al., 2012)
62 sigma_1=48.37+(zn_EtOH-0.033)*(38.77-48.37)/(0.072-0.033);
63
64 % shear rate according to NV Pimenove et al., 2004
65 % shear=K*N, where N [rps] of mixer
66 shear (1) = 10.8 \times 300/60;
shear (2) = 10.8 * 500/60;
shear(3)=10.8\times1100/60;
69 % viscosity of slurry (non-newtonian) from NV Pimenova et al., 2004
70 % mu_l=Tau/shear=K2*shear^(n-1)
```

```
71 mu_1(1)=1.87*shear(1)^(0.91-1);
mu_1(2) = 1.87 * shear(2) ^ (0.91-1);
73 mu_1(3)=1.87*shear(3)^(0.91-1);
75 % gravity constant
76 q=9.81; %[m/s]
77 %% CO2 absorbed in liquid phase
78 xn_CO2=p_reac/KH_CO2;
79 absn_CO2=xn_CO2*Ln;
80 absm_CO2=absn_CO2*0.044;
81 x_CO2=absm_CO2/L;
82 %% Partition Ceofficient K_pLG acc. to Loser et al. 2005
84 % Loser et al. are calculating in their paper the partition coefficent as
85 % follows:
87 % K_pLG= (p0*T_G*rho_wL*v0)/(pvapEtOH*T0*gam_EtOHL*Mw);
89 % unit of partition coefficent is: [-]
90 % where:
91 % T G=T reac
93 p0=1.01325; %[bar], used same as for Loser et al.
94 T0=273; %[K], acc. to Loser et al.
95 v0=22.41; %[L/mole], acc. to Loser et al.
96 Mw=18; %[g/mole], MW of water
97 \mbox{rho\_wL=1000; } %[g/1], \mbox{density of water, same as used by Loser et al.}
98 pvapEtOH=pvapEtOH(T_reac); %[bar], saturation pressure @T_reac
99 [gamEtOH,gamH2O]=unifac(zn_EtOH,T_reac); %activity coefficients
100
101 K_pLG=p0*T_reac*rho_wL*v0/(pvapEtOH*T0*gamEtOH*Mw);
102
103 %% gas stream needed Fg needed to remove the ETOH
104 Fg=zeros(3,1FR);
105 ng_CO2=zeros(3,1FR);
106 mg_CO2=zeros(3,1FR);
108 Fg_avg=zeros(1, 1FR);
ngavg_CO2=zeros(1,1FR);
mgavg_CO2=zeros(1,1FR);
112 % massbalance acc. Ponce et al. 2016:
113 %
114 % dP/dt = r_p-r_ps (1), where it is for a batch process
115 % P=concentration of EtOH inside vessel, [kg/m3]
116 % r_p: produced EtOH
117 % r_ps: removed EtOH by stripping with CO2
```

```
118 %
119 % since a continuous process is at steady state and the concentration
120 % inside the vessel is always equal the final concentration (assumption of
121 % perfect mixing), the production rate times the volume
122 % (r_p*V_reac/t) is equal to the total produced ethanol
124 \% dP/dt=0=r_p-r_ps-r_pL (2)
125 % r_pL= rate of EtOH leaving with the liquid stream
127 % Loser et al. fromulated the eqn (2) in dependendcy of stripping rate and
128 % dilution rate:
130 % dP/dt = -[r_ps/P+D] *P+r_p (3)
131 % where D is the dilution rate: D=F1/V_reac
132 % and Fl is the incoming liquid stream (Fl=L/rho_in)
133 Fl=L/rho_l;
134 D=F1/V_reac;
135 %
136 % Loser et al. brought the definitions for the stripping rate:
137 %
138 % r_ps=[(Fq*k_pla)/(Fq+V_reac*k_pla*K_pLG)]*P (4)
140 % we can now combine eq (3) and (4) resulting in:
141 %
142 % dP/dt=-[(Fg*k_pla)/(Fg+V_reac*k_pla*K_pLG)+D]*P+r_p
143 %
144 % the fractional recovery is defined as:
145
146 % FR=m_eg/(m_eg+m_el)=m_eg/m_EtOH
147 응
148 % with m=F*C and C_eq=r_ps we get:
149 %
150 % FR=1/(1+D*[1/k_pla+V_reac*K_pLG/Fg]) (5)
152 % For checking, if a desired recovery is feasible, one need so to take the
153 % limit for infinit gasstream. We then get:
155 % FR=1/(1+D/k_Pla), the dilution rate is give, so we can calculate the
156 % minimum masstransfer coefficient:
157 for i=1:1FR
158 k_plamin=D*FRq_EtOH(i)/(1-FRq_EtOH(i));
159 %
160 % the only unknown in this eq. is the variable of k\_pla. This can be
161 % calculated by the empirical correlation of Truong et Blackburn (1984)
162 % for volatile organic components:
163 %
164 % k_pla*V_reac/Fq=b*(H_c)^m, with b=0.0093 and m=0.872
```

```
165 % k_pla=(Fg/V_reac) *0.0093 * (H_c)^0.872 = (Fg/V_reac) *H_tild (9)
166 % H_tild=0.0093*(H_c)^0.872;
167 H_tild=0.0093*(H_EtOH)^0.872;
169 % H_c is the dimensionless solubility of the
170 % organic compount (EtOH) in water and can be
171 % calculated by the approach of Snider et al (cf. calculation of H_EtOH)
172 % We can plug eq (9) in eq(8) and then by rearranging we get a dependency
173 % of the variable Fg:
174 %
175 % Fq=V_reac*(1/H_tild+K_pLG)/((1-FRq_EtOH)*1/(FRq_EtOH*D));
176 Fg(1,i) = V_reac*(1/H_tild+K_pLG)/((1-FRq_EtOH(i))*1/(FRq_EtOH(i)*D));
177
178 % ALternatively, the mass transfer coefficient (MTC)
179 % can be calculated according
180 % to the calculations of Loser et al. They determined the mass transfer
181 % coefficient for O2 for different stirring rates and stated that the
182 % MTC is only dependent on the
183 % diffusion coefficient of the component.
184 %
185 % k elA=k O2a*D EtOH/D O2
187 % The diffusion coefficient for ethanol can be calculated for another
188 % temperature according to the Einstein law:
189 % D_iT2=D_iT1*(T2/T1)
190 D_02=2.6*10^{(-9)}; %[m2/s]
191 D_EtOH=1.3*10^(-9)*T_reac/303; %[m2/s]
192 k_ela500=130/3600*D_EtOH/D_02; %[1/s]
193 k_ela1100=350/3600*D_EtOH/D_O2; %[1/s]
194
195 if k_ela500<k_plamin
       warning('mass transfer coefficient k_ela500 lower than the minimum')
       warning('mass transfer coefficient! The specifications cannot be met,')
197
198
       warning('please adjust specs or conditions')
199 end
200 if k_ela1100<k_plamin
       warning('mass transfer coefficient k_ela1100 lower than the minimum')
201
       warning ('mass transfer coefficient! The specifications cannot be met,')
203
       warning('please adjust specs or conditions')
204 end
205 % Using these MTCs, we can rearrange eqn (5):
206 % Fg2=V_reac*K_pLG/((1-FR)*1/(FR*D)-1/k_pla)
207 Fg(2,i)=V_reac*K_pLG/((1-FRg_EtOH(i))*1/(FRg_EtOH(i)*D)-1/k_ela500);
208 Fg(3,i)=V_reac*K_pLG/((1-FRg_EtOH(i))*1/(FRg_EtOH(i)*D)-1/k_ela1100);
209 % calculation of required mass stream by applying the ideal gas law with
210 % V=Fa
211 ng_CO2(1,i) = p_reac*10^5*Fg(1,i)/(8.312*T_reac)-n_CO2; %[mole/s],
```

```
212 % mole stream required of CO2
213 mq_CO2(1,i) = nq_CO2(1,i) *0.044; %[kg/s], mass stream required of CO2
214
ng_CO2(2,i) = p_reac*10^5*Fg(2,i)/(8.312*T_reac)-n_CO2; %[mole/s],
216 % mole stream required of CO2
217 mq_CO2(2,i) = nq_CO2(2,i) *0.044; %[kg/s], mass stream required of CO2
218
p_{col} = p_{c
220 % mole stream required of CO2
221 mg_CO2(3,i)=ng_CO2(3,i)*0.044; %[kg/s], mass stream required of CO2
222
223 %averaged
224 Fg_avg(i) = (Fg(1,i) + Fg(2,i) + Fg(3,i))/3;
225 ngavg_CO2(i) = p_reac*10^5*Fg_avg(i)/(8.312*T_reac); %-n_CO2; %[mole/s],
226 % mole stream required of CO2
227 mgavg_CO2(i) = ngavg_CO2(i) *0.044; %[kg/s], mass stream required of CO2
228 end
229 %% amount of water stripped off
230 % applying same steps as for EtOH, we result in same eqns.
231
232 pvapH2O=pvapH2O(T_reac);
233 % partition coefficient for water
234 K_HLG=p0*T_reac*rho_wL*v0/(pvapH2O*T0*gamH2O*Mw);
235
 236 % mass transfer coefficient
237 DH2O=3.89310^{-9}; %[m2/s]
238 \text{ k\_hla500=130/3600*DH20/D\_02; } [1/s]
239 k_hla1100=350/3600*DH2O/D_O2; %[1/s]
240
241 %fractional recoveries
242 FRqH2O=zeros(2,1FR);
243 % mass recovered
244 mg_H2O=zeros(2, 1FR);
245 mgavg_H2O=zeros(1, 1FR);
246
      for i=1:1FR
247
                 FRgH2O(1,i)=1/(1+D*(1/k_hla500+V_reac*K_HLG/Fg(2,i)));
248
                 mg_H2O(1,i) = m_H2O*FRgH2O(1,i);
249
250
                 FRgH2O(2,i)=1/(1+D*(1/k_hla1100+V_reac*K_HLG/Fg(3,i)));
251
                 mg_H20(2,i) = m_H20 * FRgH20(2,i);
252
253
                 mgavg_H2O(i) = (mg_H2O(1,i) + mg_H2O(2,i))/2;
254
255 end
256
257 %% plot the results for the gasstream
258 figure
```

```
259 yyaxis left
260 plot (FRq_EtOH, mgavg_CO2, 'm-', 'LineWidth', 1)
261 xlabel('mass recovery of ethanol [-]')
262 ylabel('CO2 mass flow required [kg/s]')
263 axis([0 1 0 16])
265 yyaxis right
266 plot(FRg_EtOH, mgavg_H2O, 'c--', 'LineWidth', 1)
267 ylabel('recovered water mass flow [kg/s]')
269 title('required gasstream and recovered water in gas phase')
270 legend('CO2', 'water in gas recovered')
271
272 %% concentration of EtOH in gas stream w & w/o CO2
273 y_EtOH=zeros(3,1FR); %mass(1&2,:) and mole fraction (3,:)
274 % fraction of water in gasstream
y_{H20}=zeros(3,1FR); %mass(1&2,:) and mole(3,:)
276 % fraction of EtOH on gasstream
277 for i=1:1FR
       y_EtOH(1,i)=FRg_EtOH(i)*m_EtOH/(FRg_EtOH(i)*m_EtOH+mgavg_H2O(i));
278
       y_EtOH(2,i)=FRq_EtOH(i) *m_EtOH/(FRq_EtOH(i) *m_EtOH+mgavq_H2O(i)...
279
           +mgavg_CO2(i));
       y_EtOH(3,i)=FRg_EtOH(i)*m_EtOH*0.046/(FRg_EtOH(i)*m_EtOH*0.046+...
281
282
           mgavg_H20(i) *0.018 + mgavg_C02(i) *0.044);
       y_H2O(1,i)=mgavg_H2O(i)/(FRg_EtOH(i)*m_EtOH+mgavg_H2O(i));
       y_H2O(2,i)=mgavg_H2O(i)/(FRg_EtOH(i)*m_EtOH+mgavg_H2O(i)+mgavg_CO2(i));
284
       y_{H20}(3,i) = mgavg_{H20}(i) *0.018/(FRq_EtOH(i) *m_EtOH*0.046+...
285
            mgavg_H20(i) *0.018 + mgavg_C02(i) *0.044);
286
287 end
288
289 %% plot of concentration vs. fractional recovery
290 figure
291 yyaxis left
292 plot (FRg_EtOH, mgavg_CO2, 'm-', 'LineWidth', 1)
293 ylabel('mass flow [kg/s]')
294 yyaxis right
295 plot(FRg_EtOH, y_EtOH(1,:), 'b--', 'LineWidth', 1)
296 hold on
297 plot(FRg_EtOH,y_EtOH(2,:),'b-','LineWidth',1)
298 hold off
299 xlabel('mass recovery of ethanol [-]')
300 ylabel('concentration [-]')
301 axis([0 1 0 1])
302 title('m_{CO_{2}, min} & y_{EtOH}')
303 legend('m_{CO_{2},min}','y_{EtOH} w/o CO_2','y_{EtOH} w CO_2')
304
305 figure
```

```
306 yyaxis left
307 plot (FRq_EtOH, mgavg_CO2, 'm-', 'LineWidth', 1)
308 ylabel('mass flow [kg/s]')
309 yyaxis right
310 plot (FRg_EtOH, y_EtOH(1,:), 'b--', 'LineWidth', 1.5)
311
312 xlabel('mass recovery of ethanol [-]')
313 ylabel('concentration [-]')
315 title('m_{CO_{2}, min} & y_{EtOH}')
316 legend('m_{CO_{2}, min}', 'y_{EtOH}')
317 %% max. mole fraction in gasphase
318 y_H2Osat=pvapH2O/p_reac;
319 y_EtOHsat=pvapEtOH/p_reac;
320 y_CO2sat=1-y_H2Osat-y_EtOHsat;
321 y_CO2=zeros(1,1FR);
322 for i=1:1FR
       if y_EtOH(3,i)≥y_EtOHsat %check if calculated concentrations
323
324
              are lower than saturated
            warning('mole fraction of EtOH above saturated mole fraction!')
325
            disp('this element is above:')
326
327
328
            y_EtOH(3,i)
            disp('For the desired fractional recovery:')
329
330
            FRg_EtOH(i)
331
       end
332
333
       if y_H2O(3,i) ≥y_H2Osat %check if calculated concentrations
334 %
              are lower than saturated
            warning('mole fraction of H2O above saturated mole fraction!')
335
            disp('this element is above:')
336
337
            i
            y_{H20}(3,i)
338
339
            disp('For the desired fractional recovery:')
            FRg_EtOH(i)
340
341
       end
       y_CO2(i) = 1 - y_EtOH(3, i) - y_H2O(3, i);
342
343 end
344
345 %% gas and bubble characteristics
346 wg_max=0.05; %[m/s], max superficial gas velocity for
347 % bubbly flow regime (Kantarci et al, 2005)
348 epsg=zeros(1,3); %[], gas hold up
349 w0g=zeros(1,3); %[m/s], interstitial gas velocity
350 wb=zeros(1,3); %[m/s], bubble rise velocity
351 Db=zeros(1,3); %[m], bubble diameter
352
```

```
353 for n=1:3
       epsg(n) = (2.25+0.379/wq_max*(rho_1/72)^0.31*mu_1(n)^.016)^(-1);
       %gas holdup correlation acc. to smith et al.
        for aqn alcohol with solids
356
       w0g(n) = epsg(n) * wg_max;
357
       wb (n) = wq_max*(1-epsq(n))^1.75;
358
       %bubble velocity according to Ishii and Zuber (1979) where \mu_{-}1>>\mu_{-}g
359
360
       %iteration for bubble diameter calculation via direct
       %substitution method and function call
362
       Db(n) = bubDia2(wb(n), rho_q, rho_l, mu_l(n), sigma_l);
363
         DbH(1)=10^{(-3)}; %help variable for diameter [m]
364 %
365 %
         Re=wb(n)*rho_l*DbH(1)/mu_l(n); %Reynolds number for bubble
366
         %calculation of drag coefficient according to lecture
         %multiphase flow
         if Re<2.2 % rigid sphere (stokes)
369
370 %
             cD=24/Re;
371 %
         end
372 %
         if Re>2.2 && Re<4.02*(rho_l*sigma_l^3/(g*mu_l(n)^4))^.214
373 %internal circulation
             cD=18.7/Re^0.68;
375 %
         end
376 %
         if Re>4.02*(rho_l*sigma_l^3/(g*mu_l(n)^4))^.214 && Re<3.1*...
  % (rho_l*sigma_l^3/(g*mu_l(n+1)^4))^.25 %flattening
              cD=0.366*g*rho_l*DbH(1)^2/(sigma_l);
378
         end
379
         if Re>3.1*(rho_1*sigma_1^3/(g*mu_1(n)^4))^.25 %cap shaped bubbles
380
381 %
             cD=2.61;
382 %
         end
         DbH(2) = 3 * rho_1 * wb(n)^2 * cD/(4 * (rho_1 - rho_g) * g);
385 %help variable no2 for bubble diameter [m]
386
         diffD=abs(DbH(1)-DbH(2));
387 %
         while abs(diffD)>10^{(-6)}
388 %
             DbH(1) = DbH(2);
389
             Re=wb(n)*rho_l*DbH(1)/mu_l(n); %Reynolds number for bubble
391 %
             %calculation of drag coefficient according to lecture
392 %
              %multiphase flow
394 %
             if Re<2.2 % rigid sphere (stokes)
395 %
                  cD=24/Re;
             end
             if Re>2.2 && Re<4.02*(rho_1*sigma_1^3/(g*mu_1(n)^4))^.214
397 %
398 %internal circulation
          cD=18.7/Re^0.68;
```

```
400 %
              end
              if Re>4.02*(rho_1*sigma_1^3/(g*mu_1(n)^4))^.214 && ...
   % Re<3.1*(rho_1*sigma_1^3/(g*mu_1(n)^4))^.25 %flattening</pre>
                  cD=0.366*g*rho_l*DbH(1)^2/(sigma_l);
403
   응
404
              end
              if Re>3.1*(rho_1*sigma_1^3/(g*mu_1(n)^4))^.25 %cap shaped bubbles
                  cD=2.61;
406
407
   00
              end
              DbH(2) = 3 * rho_1 * wb(n)^2 * cD/(4 * (rho_1 - rho_g) * g);
409
              diffD=abs(DbH(2)-DbH(1));
410
         end % while diffD>10^-6
411
         Db(n) = DbH(2);
412
   9
413
       %Volume of the bubble [m3]
       Vb(n) = 4/3 * pi * (Db(n)/2)^3;
416 end %for n=0:2
417
418 %% Masstransfer
419
  for n=1:3
420
421
       ng_C02(n) = p_reac*Vb(n)/(8.314*T_reac);
       %total amount of CO2 moles in bubble
422
423
       n_sat(n) = ng_co2(n)/y_co2sat; %total amount of moles at saturation
       ng_EtOHsat(n)=y_EtOHsat*n_sat(n);
       %total amount of EtOH moles at saturation
425
       Vbsat(n) = Vb(n) / (1-y_EtOHsat-y_H2Osat); %volume of bubble at saturation
426
       Csat(n) = ng_EtOHsat/Vbsat; %[mole/m3], EtOH concentration at saturation
427
428 end
429
430 t=zeros(3,1FR); %[s], time required to reach desired concentration
431 ng_EtOH=zeros(3,1FR); %moles of EtOH at end of column
432 n_reac=zeros(3,1FR); %final amount of moles
433 Vb_reac=zeros(3,1FR); %final volume of bubble
434 C=zeros(3,1FR); %[mole/m3], final concentration of EtOH
435 for i=1:1FR
       for n=1:3
436
437
            n_{eq}(n,i) = ng_{eq}(n) / y_{eq}(i);
            ng_EtOH(n,i) = y_EtOH(3,i) *n_reac(n,i);
438
            Vb_{reac}(n,i) = Vb(n) / (1-y_EtOH(3,i)-y_H2O(3,i));
439
            C(n,i) = nq_EtOH(n,i) / Vb_reac(n,i);
440
            if n==1
441
                kla=Fg_avg(i)/V_reac*H_tild;
442
            end
            if n==2
444
445
                kla=k_ela500;
446
            end
```

```
447
            if n==3
448
                kla=k_ela1100;
450
            t(n,i)=1/kla*(1-log(C(n,i)/Csat(n)));
       end
451
453
454 %% column sizing
455 Hmin=zeros(3,1FR);
456 %[m], minimum height of column according to mass transfer
457 Hmax=zeros(3,1FR);
458 %[m], maximum height of column according towards volume specifications
459 Amin=zeros(3,1FR);
460 %[m2], minimum crosssectional area according to flow regime limitations
461 Dmin=zeros(3,1FR); %[m], minimum diameter
463 max=zeros(1,3);
464 maxH=zeros(1,3);
   for i=1:1FR
         for n=1:3
466
             Amin(n,i)=Fg_avg(i)/(5*wg_max);
467
              Dmin(n,i)=2*sqrt(Amin(n,i)/pi);
             Hmax(n,i) = V_ves/Amin(n,i);
469
           % Hmin1(n,i)=t(n,i)*w0g(n);
470
              Hmin(n,i)=t(n,i)*wb(n);
              deltH=abs(Hmax(n,i)-Hmin(n,i));
472
              if deltH<10^{-3}
473
474
                  max(n) = FRq_EtOH(i);
475
                  maxH(n) = Hmax(n,i);
476
              end
         end
478 end
479
480
  %% plotting sizing results
481
482 figure
483 subplot (3, 1, 1)
484 yyaxis left
485 plot(FRg_EtOH, Dmin(1,:),'--g','LineWidth',1)
486 title('column sizes for 300 rpm')
487 xlabel('Fractional recovery of Ethanol')
488 ylabel('Column Diameter [m]')
489 axis([0 1 0 20])
490 yyaxis right
491 plot(FRg_EtOH, Hmin(1,:),':b','LineWidth',1.5)
492 hold on
493 plot (FRg_EtOH, Hmax(1,:),':c','LineWidth',1.5)
```

```
494 plot (max(1), maxH(1), '-rh', 'LineWidth', 1)
495 ylabel ('Column Height [m]')
496 legend('Diameter', 'Min. Height', 'Max Height', 'Max possible')
497 axis([0 1 0 20])
498 hold off
500 subplot (3, 1, 2)
501 yyaxis left
502 plot(FRg_EtOH, Dmin(2,:),'--g','LineWidth',1)
503 title('column sizes for 500 rpm')
504 xlabel('Fractional recovery of Ethanol')
505 ylabel('Column Diameter [m]')
506 axis([0 1 0 20])
507 yyaxis right
508 plot(FRg_EtOH, Hmin(2,:),':b','LineWidth',1.5)
509 hold on
510 plot(FRg_EtOH, Hmax(2,:),':c','LineWidth',1.5)
511 plot (max (2), maxH (2), '-rh', 'LineWidth', 1)
512 ylabel('Column Height [m]')
13 legend('Diameter', 'Min. Height', 'Max Height', 'Max possible')
514 axis([0 1 0 20])
515 hold off
516
517 subplot (3, 1, 3)
518 yyaxis left
plot(FRg_EtOH, Dmin(3,:),'--g','LineWidth',1)
520 title('column sizes for 1100 rpm')
521 xlabel('Fractional recovery of Ethanol')
522 ylabel('Column Diameter [m]')
523 axis([0 1 0 20])
524 yyaxis right
525 plot(FRg_EtOH, Hmin(3,:),':b','LineWidth',1.5)
526 hold on
527 plot (FRq_EtOH, Hmax(3,:),':c','LineWidth',1.5)
528 plot (max(3), maxH(3), '-rh', 'LineWidth', 1)
529 ylabel('Column Height [m]')
530 legend('Diameter', 'Min. Height', 'Max Height', 'Max possible')
531 axis([0 1 0 20])
532 hold off
533
534 figure
plot(FRg_EtOH, Hmin(3,:),'--r','LineWidth',1)
536 hold on
537 plot(FRg_EtOH, Hmax(3,:),'--m','LineWidth',1)
538 plot(max(3), maxH(3), '-ro', 'LineWidth', 1)
539 plot(FRg_EtOH, Hmin(2,:),'.-b','LineWidth',1)
540 plot(FRq_EtOH, Hmax(2,:),'.-c','LineWidth',1)
```

```
541 plot (max(2), maxH(2), '-rp', 'LineWidth', 1)
542 plot(FRg_EtOH, Hmin(1,:),':g','LineWidth',2)
543 plot(FRg_EtOH, Hmax(1,:),':k','LineWidth',1.5)
544 plot(max(1), maxH(1), '-rh', 'LineWidth', 1)
545 title('influence of mixer speed on column size')
546 xlabel('Fractional recovery of Ethanol')
547 ylabel('Column Height [m]')
100 legend('Hmin 1100rpm', 'Hmax 1100rpm', 'Max Possible 1100rpm',...
       'Hmin 500rpm', 'Hmax 500rpm', 'Max Possible 500rpm', 'Hmin 300rpm',...
       'Hmax 300rpm', 'Max Possible 300rpm')
551 axis([0 1 0 20])
552 hold off
553
554 % figure
555 % plot(FRg_EtOH, Hmin(2,:),'.-b','LineWidth',1)
556 % hold on
557 % plot(FRg_EtOH, Hmax(2,:),'.-c','LineWidth',1)
558 % plot(max(2), maxH(2), '-rp', 'LineWidth', 1)
560 % title('influence of mixer speed on column size')
561 % xlabel('Fractional recovery of Ethanol')
562 % ylabel('Column Height [m]')
563 % legend('Hmin 500rpm', 'Hmax 500rpm', 'Max Possible 500rpm')
564 % axis([0 1 0 20])
565 % hold off
566 figure
567 plot(FRg_EtOH, Hmin(2,:),'.-b','LineWidth',1)
569 plot (FRg_EtOH, Hmax(2,:),'.-c','LineWidth',1)
570 % plot(max(2), maxH(2), '-rp', 'LineWidth', 1)
572 title('Determination of ideal column height')
573 xlabel('Fractional recovery of Ethanol')
574 ylabel('Column Height [m]')
575 legend('Hmin','Hmax', 'Max Possible 500rpm')
576 axis([0 1 0 20])
577 hold off
```

# APPENDIX D

### References

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# APPENDIX E

## List of publications

#### **Publications**

to be submitted

Scale-up of consolidated bioprocessing from 2.7 L laboratory scale to 130 L pilot scale based on arigorous model

D. Dempfle, P. Bühler, S. Bowald, D. Blaser, O. Kröcher, M. H. Studer

to be submitted

Continuous consolidated bioprocessing of cellulosic ethanol based on a microbial consortium in a membrane aerated biofilm reactor to validate a rigorous spatially resolved model

D. Dempfle, C. Wagner, O. Kröcher, M. H. Studer

2021

Techno-economic assessment of bioethanol production from lignocellulose by consortium-based consolidated bioprocessing at industrial scale

D. Dempfle, O. Kröcher, M. H. Studer

New Biotechnology. 65 (2021) 53-60, doi: 10.1016/j.nbt.2021.07.005

2018

External mass transfer in a laser sintered structured reactor for continuous hydrogenation of alkynes

S. Vernuccio, D. Dempfle, Roman Goy, J. Medlock, P. Rudolf von Rohr Chemical Engineering and Processing. doi: 10.1016/j.cep.2018.02.005.

### **Conference contributions**

04/2020 42nd Symposium on Biomaterials, Fuels and Chemicals, New Orleans,

United States of America

Techno-economic assessment of bioethanol production from lignocellulose by consortium-based consolidated bioprocessing at industrial scale

D. Dempfle, O. Kröcher, M. H. Studer

# APPENDIX F

### Curriculum vitae

Name David Beat Dempfle

Date of birth 22<sup>th</sup> June 1992

Nationality German

**Education** 

09/2017 - 11/2021 Doctoral student

École Polytechnique Fédérale de Lausanne, Group of Catalysis for Biofuels and Bern University of Applied Sciences, Laboratory of Biofuels and

Biochemicals

PhD thesis Model-based scale-up of a continuously operated consolidated bioprocess based on

a microbial consortium to produce ethanol from lignocellulose

Prof. Dr. Oliver Kröcher & Dr. Michael Studer

09/2011 - 05/2017 Master of Science ETH in Process Engineering

Swiss Federal Institute of Technology Zurich

Specialization Process Engineering

Master thesis Continuous hydrogenation of 2-methyl-3-butyn-2-ol in a structured reactor

Swiss Federal Institute of Technology Zurich, Institute for Process

Engineering

Prof. Dr. Philipp Rudolf von Rohr

Semester thesis Scale-up of microfluidic devices and effect of water evaporation on droplet volume

distribution and shape

Swiss Federal Institute of Technology Zurich

Prof. Dr. Marco Mazotti & Prof. Dr. Philipp Rudolf von Rohr

chemical vapor deposition

Swiss Federal Institute of Technology Zurich

Prof. Dr. Philipp Rudolf von Rohr

08/2005 - 07/2011 High school student (Abitur)

Gymnasium Aloisiuskolleg, Bonn

Professional experience

04/2017 - 07/2017 Research assistant

Swiss Federal Institute of Technology Zurich

Research topic Reactive multiphase flows in porous structures & Development of a business case

for ethanol production in Switzerland

Prof. Dr. Philipp Rudolf von Rohr

04/2015 - 07/2015 Intern

ThyssenKrupp Industrial Solutions

Department Process Engineering

06/2011 - 07/2011 Intern

Bayer Technology Services

Scope Basic knowledge of machining, joining and forming production processes