

DORI Reveals the Influence of Noncovalent Interactions on Covalent Bonding Patterns in Molecular Crystals Under Pressure

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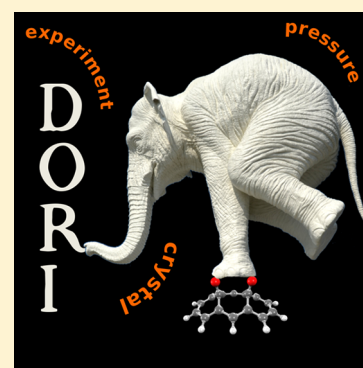
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Supporting Information

ABSTRACT: The study of organic molecular crystals under high pressure provides fundamental insight into crystal packing distortions and reveals mechanisms of phase transitions and the crystallization of polymorphs. These solid-state transformations can be monitored directly by analyzing electron charge densities that are experimentally obtained at high pressure. However, restricting the analysis to the featureless electron density does not reveal the chemical bonding nature and the existence of intermolecular interactions. This shortcoming can be resolved by the use of the DORI (density overlap region indicator) descriptor, which is capable of simultaneously detecting both covalent patterns and noncovalent interactions from electron density and its derivatives. Using the biscarbonyl[14]annulene crystal under pressure as an example, we demonstrate how DORI can be exploited on experimental electron densities to reveal and monitor changes in electronic structure patterns resulting from molecular compression. A novel approach based on a flood-fill-type algorithm is proposed for analyzing the topology of the DORI isosurface. This approach avoids the arbitrary selection of DORI isovalues and provides an intuitive way to assess how compression packing affects covalent bonding in organic solids.



Studies of matter under high pressure have long been the realm of geoscientists, solid-state physicists, and astro-physicists who examine the extreme conditions of Earth¹ and extraterrestrial environments.² In materials science, pressure is also exploited to control the properties of materials, for instance, by reducing interatomic or intramolecular distances.^{3–6} This leads to a host of interesting applications, ranging from superhard^{7,8} and high-energy density materials⁹ to hydrogen storage.¹⁰ We are interested in the behavior of molecular organic and metal–organic crystals under pressure.^{11–13} Such an understanding provides deep insight into the pressure-induced distortions of crystal packing, the switching of molecular conformations, and the exploration of new polymorphic forms (e.g., chemisorption in metal–organic frameworks,^{14,15} piezochromic switches,^{16,17} photovoltaic hybrid perovskites,^{18,19} the crystal engineering of pharmaceuticals,²⁰ as well as amino acids^{21,22} and sugars^{23,24}).

During variable pressure experiments, changes appear in the molecular geometries²⁵ (e.g., interatomic distances and angles) due to the compression of molecular packing.^{26–28} But these geometrical changes do not directly allow the deduction of

changes in the electronic structure, which represents perhaps the most appealing and sensitive way of examining inter- and intramolecular interactions of compressed molecular crystals. The ability to experimentally observe electronic structure modifications under pressure is relatively recent.^{29–32} Macchi's work on *syn*-1,6:8,13-biscarbonyl[14]annulene (BCA) (see Figure 1) represents a major breakthrough.³³ This BCA crystal was chosen to be studied because its charge density at ambient pressure revealed an unusual bond path that links the two bridgehead carbonyl groups in almost C_{2v} molecular symmetry but shifts toward one of the resonant forms³⁴ of an ideal aromatic system when high pressure is applied, as shown in Figure 1. Applying pressure weakens the electron delocalization in the double bonds of the annulene ring that is observed at ambient pressure, distorting the systems to the C_s subsymmetry point group of C_{2v} . As for the packing, BCA crystallizes with four molecules in the unit cell, with no change

Received: January 24, 2019

Accepted: March 13, 2019

Published: March 13, 2019

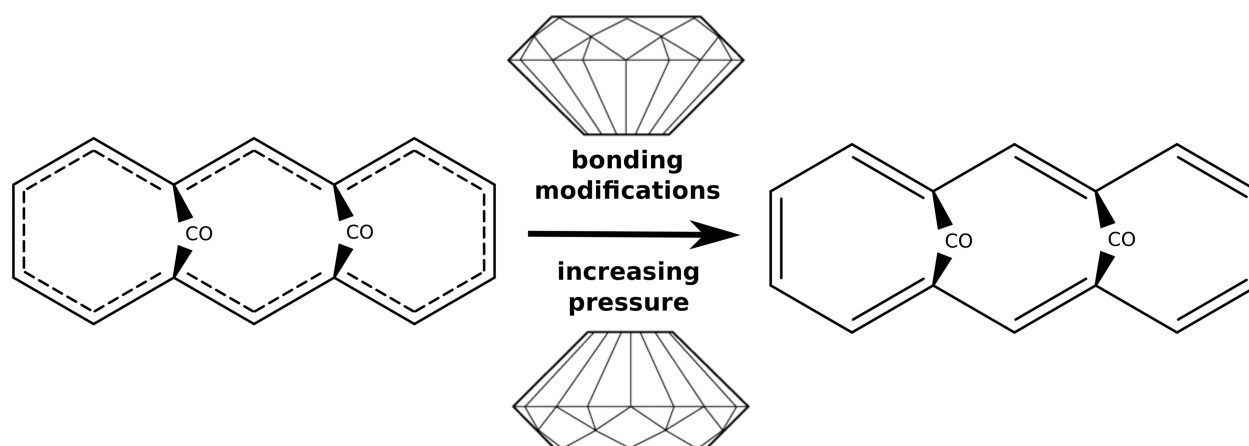


Figure 1. Ideal aromatic representation (left) and resonance structure (right) for the *syn*-1,6:8,13-biscarbonyl[14]annulene (BCA) molecule.

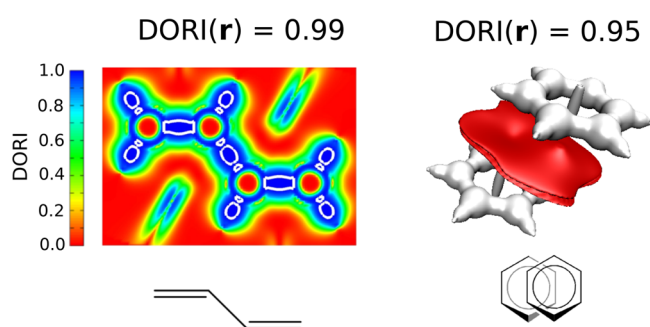


Figure 2. 2D DORI maps ($\text{DORI}(\mathbf{r}) = f$) in the σ_h plane of butadiene with $f = 0.99$ isocontour in white (left). 3D representation of the parallel-displaced benzene dimer for $f = 0.95$ (right) with covalent and noncovalent DORI [f] domains depicted in white and red, respectively. These examples are adapted and reprinted with permission from ref43.

in space group (monoclinic $P2_1/n$) detected when increasing the pressure up to 7.7 GPa.

Whereas the geometric perturbations caused by placing the BCA crystal under pressure are easy to observe, a subtle computational analysis is required to determine the bond type and to illuminate the interplay between chemical bonds and the crystal packing²⁵ from the experimental electron density.³⁵ Several methods for analyzing electron charge densities have been proposed in the literature: topological analysis,³⁶ quantum crystallography,³⁷ and the use of molecular scalar fields.^{38–40} Among the latter, the density overlap region indicator (DORI)⁴¹ (derived from the single exponential decay detector (SEDD)⁴²) is a specific and ideally suited example because it reveals both covalent and noncovalent interactions directly from the charge density, $\rho(\mathbf{r})$, (and its derivatives) that is accessible from experiment. DORI is defined as

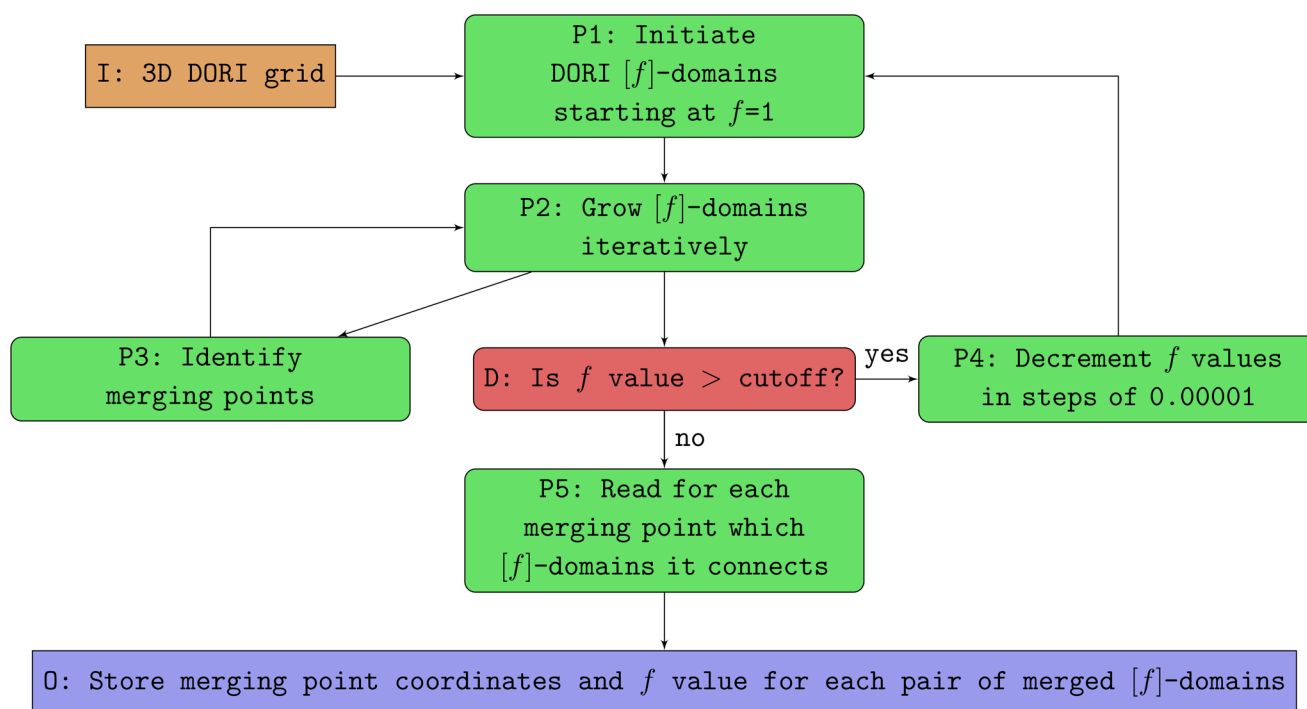


Figure 3. Schematic outline of the search for merging points. The boxes are colored as orange = input (I), blue = output (O), green = processes (P1–P5), and red = decision (D).

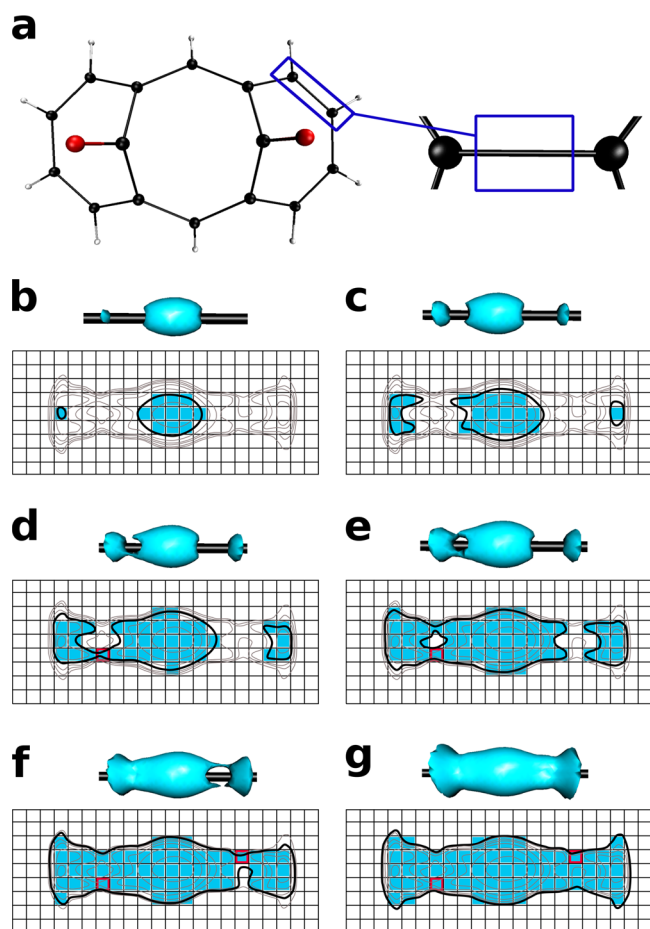


Figure 4. 3D illustration and its schematic 2D analogue of DORI $[f]$ domains for a given C–C bond (a) of BCA at ambient pressure with $f = 0.9990$ (b), $f = 0.9984$ (c), $f = 0.9980$ (d), $f = 0.9978$ (e), $f = 0.9966$ (f), and $f = 0.9940$ (g). The gray lines represent DORI isocontours for each step. For each step, the grid points (in black) with DORI values higher than f are shown in blue. Red encircled grid points correspond to the basin merging points (e.g., three basins merged in two points in panels d and f).

$$\text{DORI}(\mathbf{r}) = \frac{\theta(\mathbf{r})}{1 + \theta(\mathbf{r})} \quad (1)$$

where

$$\theta(\mathbf{r}) = \frac{\left(\nabla \left(\frac{\nabla \rho(\mathbf{r})}{\rho(\mathbf{r})} \right)^2 \right)}{\left(\frac{\nabla \rho(\mathbf{r})}{\rho(\mathbf{r})} \right)^6} \quad (2)$$

Intuitively, DORI captures the deviations from the single-exponential behavior of the density in real space and reveals density overlaps between atomic shells, atoms, or molecules.⁴¹ The regions of these overlapping charge densities can be directly interpreted as covalent bonds (if the regions lie between atoms) or noncovalent interactions (if the regions lie between molecules).⁴¹ Plotting the DORI values on the 0 to 1 scale leads to unambiguous representations of these overlaps, as shown in Figure 2.

Like any other scalar field on a 3D domain, the representation of DORI requires a fourth dimension (three dimensions for \mathbb{R}^3 and one for the value of the function). To

visualize the essential features of DORI in three dimensions, one selects a meaningful function value f and displays the closed isosurfaces for f . These surfaces are the boundaries of the $[f]$ domains (i.e., the points with $\text{DORI}(\mathbf{r}) = f$), where $[f]$ domains are all points in space with the DORI value greater than or equal to the chosen isovalue f (i.e., the points with $\text{DORI}(\mathbf{r}) \geq f$). The DORI basins correspond to chemical interactions, which can be quantified by integrating the electron density that is enclosed in each basin

$$\text{DORI}(\mathbf{r})_{\text{int}}(V_{[f]}) = \int_{V_{[f]}} \rho(\mathbf{r}) \, d\mathbf{r} \quad (3)$$

Noncovalent interactions and bonding patterns are then directly compared using the integral of the electron density ($\text{DORI}(\mathbf{r})_{\text{int}}$) and the volume of the DORI basins ($V_{[f]}$). However, as evident from eq 3, the size and even the number of DORI basins directly depends on the chosen f value. Lowering f , for instance, results in the merging of previously distinct domains. This type of behavior has been rationalized by Savin and Marx,⁴⁴ who used bifurcation diagrams to depict maxima and saddle points (the points where basins occur and merge) for the electron localization function (ELF). Heuristic examinations of these bifurcation diagrams have led to a more comprehensive picture of covalent bonding in alkene,⁴⁵ aromatic,⁴⁶ and biologically relevant⁴⁷ systems. However, the bifurcation points (of ELF) were never automatically detected using an algorithmic approach.

Up to now, we generally considered two or three distinct f values to ensure the robustness of any observation of trends associated with DORI fingerprints.^{41,43} Such arbitrary choices are, in the best case, nonideal and, in the worst case, may lead to inaccurate conclusions. Picking a single DORI- f value would be especially inconsistent when the experimentally measured electron density is obtained under different thermodynamic conditions (e.g., pressure and temperature) and is therefore not one-to-one comparable. Here we overcome the arbitrariness of selecting DORI isovalues by exploiting an algorithm that continuously and automatically monitors the DORI basins and the positions of their merging points while decreasing the f value. Taking the average of the DORI- f values of all of the bond merging points gives a meaningful and unique choice of the f value at which the covalent bonds are analyzed. This uniqueness together with the ability of DORI to simultaneously reveal covalent and noncovalent regions provides a breakthrough in assessing how high pressure affects the peculiar interplay between bonding patterns and compression packing.

Inspired by the idea of the bifurcation diagram but adopting an algorithmic approach, we analyzed the BCA covalent bonding pattern under ambient and high pressure using a connected component search algorithm⁴⁸ (see Figure 3). The algorithm performs a topological analysis of the DORI function based on 3-manifold decomposition theory and identifies its critical points (e.g., maxima and saddle point; see the details in the Supporting Information). A similar algorithm has recently been applied to study methane diffusion in nanoporous materials from a potential energy field.⁴⁸ In short, while decreasing the DORI values, the connected component search algorithm lists the coordinates of the grid points belonging to the growing DORI $[f]$ domains and detects the merging points (i.e., both their DORI values and their coordinates) between any pair of different basins.

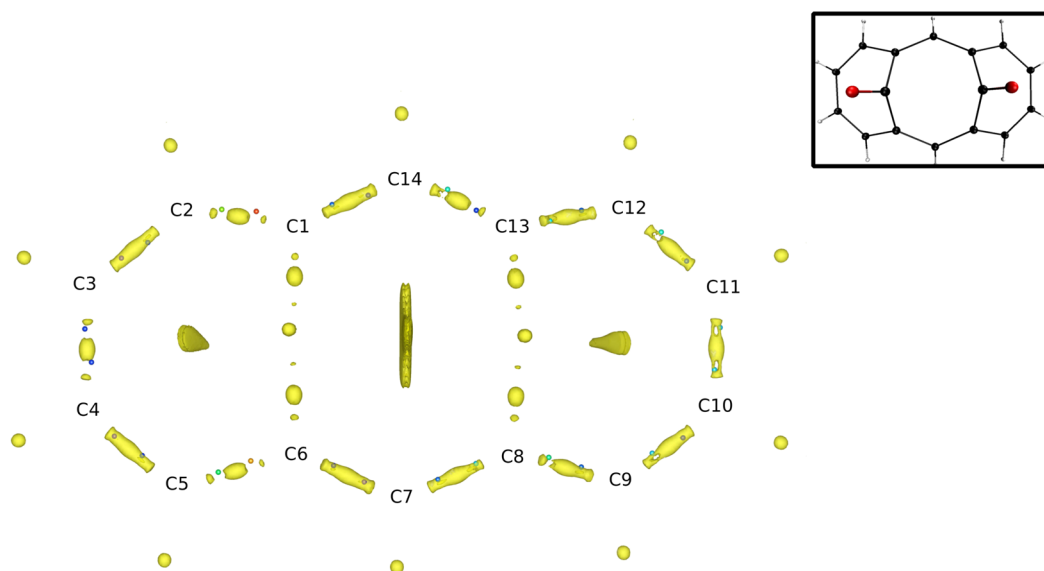


Figure 5. DORI isosurface ($\text{DORI}(\mathbf{r}) = f$) of BCA at high pressure is shown for $f = 0.999$ with 28 detected merging points associated with the 14 covalent C–C bonds. Each carbon–carbon bond can be assimilated to three growing basins (e.g., between C1 and C2) that merge into one (e.g., between C10 and C11). The first point that connects two basins is selected as their merging point. The top-right corner is a reminder of the underlying BCA molecule.

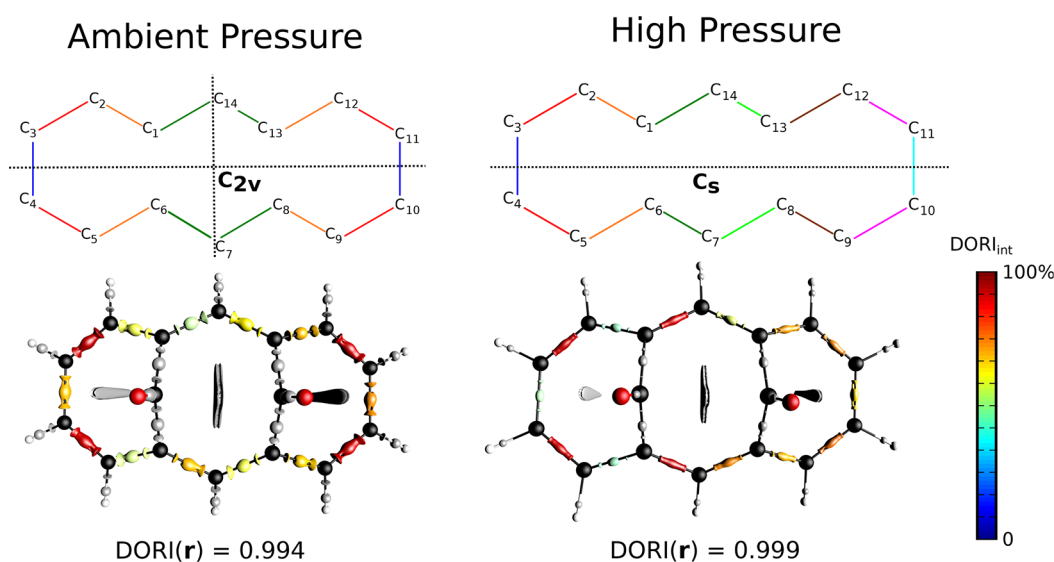


Figure 6. Annulene skeleton at the experimental symmetries: C_{2v} very close to the configuration at ambient pressure (top left) and one of the C_s subsymmetry close to the molecule in the crystal at high pressure (top right). DORI basins of each C–C bond are color-coded to represent the relative percentage of the electron density integrals (DORI_{int}) within the basins (relative to the maximum found) at ambient (bottom left) and high pressure (bottom right). All integral values (DORI_{int}) and volumes of the basins (DORI_{vol}) are given in the [Supporting Information](#).

Figure 4 provides a schematic illustration of the algorithm on a BCA C–C bond. The volume of the DORI domains (in blue) associated with the bond increases with decreasing DORI- f until the merging occurs (visible in red). This covalent bond is properly captured at DORI- f values, for which the three basins defining this bond are merged into one basin. Because the annulene ring of the BCA is composed of 14 C–C bonds, the value used to study the pressure-induced bonding modifications corresponds to the average f value of the 28 merging points (see Figure 5, $\text{DORI}(\mathbf{r}) = 0.994$ and $\text{DORI}(\mathbf{r}) = 0.999$ isovalues for the ambient and the high-pressure conditions; all merging point's DORI- f values are provided in the [Supporting Information](#)).

With 14 conjugated carbon atoms, the BCA annulene backbone is pseudo-Hückel aromatic ($4n+2 \pi$ electrons) with a distortion from planarity imposed by the two carbonyl bridges.⁴⁹ Under ambient conditions, BCA has an experimentally verified C_{2v} symmetry.⁵⁰ In Figure 6 (where the basins are colored proportionally to the maximum DORI_{int} found under each condition), the insight obtained from the DORI domains goes beyond geometrical effects. DORI captures the “electronic” equivalence of the bonds that is imposed by the symmetry. At high pressure, the additional stress perturbs the BCA electron delocalization and distorts the electron density of the annulene electron skeleton. This results in an inhomogeneous contraction of the C–C bonds reflected by the drastic changes in the DORI covalent patterns. (All

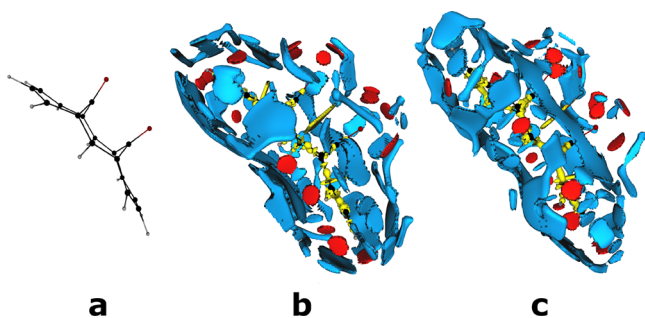


Figure 7. (a) BCA geometry. Noncovalent ($\text{DORI}(r) = f$) domains of a single BCA molecule in (b) an ambient and (c) a high-pressure crystal environment. van der Waals interactions are colored in blue, $\text{CH}\cdots\text{O}$ in red, and covalent bonds in yellow. $f = 0.994$ and 0.999 for ambient and high pressure, respectively.

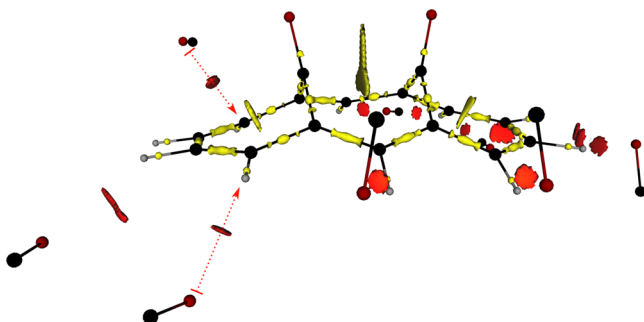


Figure 8. $\text{DORI} = 0.999$ isosurfaces associated with the $\text{CH}\cdots\text{O}$ interactions of a BCA molecule in a crystal environment at high pressure. Red arrows indicate out-of-plane interactions.

DORI_{int} and DORI_{vol} are given in the Supporting Information.) In particular, as attested by the electron density integrated within the $\text{DORI} [f]$ domains (i.e., DORI_{int}), the left side of the molecule shows an alternation between compressed (e.g., C1–C14, C2–C3, C4–C5, C6–C7) and loose (e.g., C2–C1, C5–C6) bonds, whereas the right side maintains a partial electron delocalization and smaller electronic compression of the C–C bonds (see Figure 6). Those observations are in line with other indicators (e.g., electron density at the bond critical points,³⁶ delocalization indices,⁵¹ and extremely localized molecular orbitals⁵²) and with quantum-chemical computations (see comparisons with gas-phase and periodic density functional theory (DFT) computations in the Supporting Information). The electron density measured at high pressure integrated within the $\text{DORI} [f]$ domains attests to the charge density accumulation in specific bonds of the annulene ring (see Figure 6), which desymmetrizes the molecule. DORI , however, has the advantage of giving a more intuitive visual picture of the pressure-induced modifications of the covalent pattern using an experimental electron density as the sole ingredient.

More relevantly, DORI not only captures the symmetry break and the charge-density accumulation but also identifies their cause, which lies in the distinct packing environment on the left and right sides of the BCA. Whereas the fact that high-pressure crystal packing would somehow induce an anisotropy within the π -conjugation covalent pattern is rather intuitive,^{25,53} only indirect measurements of this phenomenon based on two-photon spectroscopy^{54,55} or geometrical parameters^{23,24,56,57} have been observed. The cause and effects are here revealed directly and unambiguously.

At ambient pressure, DORI captures a rich network of noncovalent interactions around a single BCA molecule (see Figure 7) and distinguishes between $\text{CH}\cdots\text{O}$ interactions, pseudo π - π stacks, and hydrogen contacts. The seven nonredundant $\text{CH}\cdots\text{O}$ interactions experimentally characterized in the BCA crystal⁵⁰ are reflected by the directional DORI domains (see red basins in Figure 7), typical for hydrogen bonding.⁴¹ (Integral values, DORI_{int} , and volume of the basins, DORI_{vol} are given in the Supporting Information.) Many nondirectional van der Waals regions that span all around each BCA at ambient and high pressure are also clearly visible in blue. The monitoring of this noncovalent network upon compression discloses which interactions cause the largest changes in the covalent bonding patterns.

The rearrangement of directional interactions (e.g., $\text{OH}\cdots\text{O}$, $\text{NH}\cdots\text{O}$, and $\text{CH}\cdots\text{O}$ bonds or $\text{O}\cdots\text{O}$ contacts) is especially essential to interpret the modifications of compressed molecular crystals.^{23,24,56,57} From the DORI viewpoint, the $\text{CH}\cdots\text{O}$ bridges are the key to rationalize the BCA covalent pattern. As pressure is applied, several $\text{CH}\cdots\text{O}$ DORI domains

slide from the typical $\text{CH}\cdots\text{O}$ to the unconventional $\begin{array}{c} \text{C} \\ | \\ \text{H}\cdots\text{O} \end{array}$

contact, where the interacting basin now points to the carbon–hydrogen bond. In particular, two of these interactions occur out of the pseudoplane of BCA, pushing the neighboring carbon atom forward (see Figure 8). The C2 and C5 carbon atoms involved in those noncovalent contacts are both located in the same seven-membered ring (C1–C2–C3–C4–C5–C6–C15), explaining the stronger bond length alternation in the left part of the molecule. The right side of the BCA molecule is involved in strong $\text{CH}\cdots\text{O}$ contacts that remain in the annulene plane, disturbing the C–C covalent patterns to a lesser extent. At even higher pressure, we can expect those interactions to slide out of the pseudoplane, disturbing the symmetry on both sides.

In summary, we analyzed the experimental electron densities of the BCA crystal under high pressure and demonstrated how DORI intuitively captures the dramatic effects of noncovalent interactions on bonding patterns. Our approach relies on a connected component search algorithm, which avoids the arbitrary selection of the DORI isovalue and provides a general framework for the cause–effect analysis of electronic structure patterns in molecular crystals under pressure or under any distinct (e.g., temperature, condensed environment) conditions.

■ ASSOCIATED CONTENT

📄 Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcl.9b00220.

Details of the electron density refinement and of the flood-fill-type algorithm, all merging points of covalent $[f]$ domains, volume and integral of the electron density within covalent and noncovalent $\text{DORI} [f]$ domains, and additional 2D and 3D DORI representations (PDF)

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Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

This work has been supported by EPFL and the National Centre of Competence in Research (NCCR) Materials Revolution: Computational Design and Discovery of Novel Materials (MARVEL) of the Swiss National Science Foundation (SNSF). S.B. and B.S. are supported by the European Research Council (ERC) under the European Unions Horizon 2020 research and innovation program (grant agreement no. 666983, MaGic). A.M. thanks the Swedish Council (VR) for financing (project number 2015-06320). This work was supported by a grant from the Swiss National Supercomputing Centre (CSCS) under project ID s761. We thank Ganna Gryn'ova for the graphical content. We thank Piotr de Silva for his past contribution and discussions associated with DORI.

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