

Analysis of Photocarrier Dynamics at Interfaces in Perovskite Solar Cells by Time-Resolved Photoluminescence

Ahmer A.B. Baloch, Fahhad H. Alharbi, Giulia Grancini, Mohammad I. Hossain, Md. K. Nazeeruddin,
Nouar Tabet

Abstract

The power conversion efficiency of perovskite solar cells is drastically affected by the carrier dynamics at the interfaces. Experimental measurements under continuous excitation show a quenching of the photoluminescence (CW-PL) signal from the perovskite layer when it is capped with a hole transport medium (HTM). Furthermore, time resolved photoluminescence (TRPL) data show a faster decay of the PL signal in presence of perovskite/HTM interface. The experimental decay is usually fitted using one or two exponential functions with incomplete physical picture. In this work, we calculate the decay of the PL signal in presence of both defect assisted recombination (SRH) and band-to-band radiative recombination. The carrier extraction/recombination at the interfaces is described by the interface recombination velocity. The proposed model captures the temporal and spatial distribution of TRPL signal by fitting the experimental data and extracting the key physical parameters characterizing the carrier dynamics in the bulk as well as at the interfaces of the studied films. Notably, the inclusion of diffusion, doping density and surface recombination velocity at interfaces allow to accurately capture the physics of TRPL kinetics by improving the conformity of fits to experiments. This method of deconvoluting physical parameters from standard TRPL measurements can assist engineers and scientists to assess and improve the device parameters and process techniques.

1. Introduction

Since their discovery, perovskite solar cells (PSC) unleashed a great deal of enthusiasm in the PV community because of their technological promises and the open questions raised concerning the physical processes occurring in the device. The nature of the gap (direct/indirect)¹⁻³, the values of the carrier mobilities and diffusion length⁴⁻⁶, the charge transport mechanism⁷⁻¹¹, the role of point defects^{12,13}, and the recombination mechanisms responsible of the carrier losses¹⁴⁻¹⁸ have been the subject of intensive debates. In the standard configuration, a PSC consists of a thin perovskite absorbing layer sandwiched between an electron transport medium (ETM) and a hole transport medium (HTM). Under light excitation, the photocarriers are generated in the perovskite absorbing layer and diffuse towards the interfaces. Because of the appropriate band alignment at the interfaces, electrons are extracted at the ETM/perovskite interface while holes are extracted at the perovskite /HTM interface¹⁹. The carrier extraction at these interfaces occurs within picosecond range after excitation^{20,21}. The radiative band to band recombination leading to Photoluminescence (PL) occurs in the nanosecond range^{22,23}. The photocarriers generated close to the interfaces are extracted before contributing to the PL signal leading to the PL quenching. The drastic reduction of PL signal in presence of HTM /perovskite interface has been assigned by many authors to carrier extraction at the selective electrodes²⁴.

Time resolved Photoluminescence (TRPL) has been used extensively to investigate the carrier extraction at the interfaces of perovskite solar cells^{9,25-29}. The contactless nature and its application for both complete and non-complete device makes it an ideal tool for characterizing limitations in PSC. Careful physical examination of TRPL measurements can provide us with an understanding of the complex attributes of charge dynamics and extraction mechanism in mixed halide PSC. In a typical TRPL experiment, the sample is excited by a very short laser pulse leading to the generation of an initial excess carrier density $n(0)$ which subsequently decays as a

result of the recombination and carrier extraction at the interfaces as illustrated by Figure 1a. Figure 1 shows the TRPL schematic along with conventional curve fitting and charge dynamics fitting method for PL measurements. Conventionally, TRPL curves are analyzed by performing curve-fitting to the PL transients and extracting the associated lifetimes. Due to the complex quasi-exponential shape of the TRPL; one exponent, two exponent and stretched exponential functions for fitting have often been employed as shown in Figure 1b. The main limitation arising from this method is the extraction of arbitrary life time constants without consistent consideration of the physical processes involved in TRPL decay dynamics. Moreover, as the diffusion and varied recombination pathways in bulk are occurring at comparable time scales, there is a high likelihood that the extracted parameters may be convoluted with other properties. To understand the opto-electronic properties and obtain meaningful insights, charge transport for analyzing PL transients must be taken into consideration. This assists in unraveling the physical factors governing the PL decay under different time scale and conditions.

The determination of the PL decay requires solving the continuity equation taking into account the generation, transport, recombination and extraction of the carriers.²⁹⁻³¹ In the practical experimental setup, the incident light penetrates into the cell through the transparent glass, FTO and ETM layers and gets absorbed exponentially in the perovskite layer according to Lambert law. Therefore, a diffusion term needs to be included in the continuity equation which governs the charge dynamics after a pulsed excitation. The effect of doping concentration, intentional or unintentional, must be considered as well to study the collective impact of doping and radiative recombination on TRPL kinetics^{8,32}. More importantly, the addition of surface recombination velocity and diffusion provides detailed insight of the complex kinetics occurring at initial PL decay. This can equip us with the true quality of absorbers coupled with HTM or ETM. We describe in this work, such approach along with the boundary conditions and optimization algorithm to consider the carrier extraction or/and recombination at the interfaces. This fundamental work can benefit in understanding the details of the transport and extraction kinetics by dismembering the effect of individual parameters contributing to TRPL in PSC. By coupling this comprehensive model with the experimental measurements, the aim is to go beyond the conventional fitting parameters of life times and extract the parameters with physical significance such as surface recombination/interface recombination velocity (S_L and S_R), monomolecular recombination constant (k_1), bi-molecular recombination constant (k_2), mobility (μ) and doping density (N_D) as shown in Figure 1c.

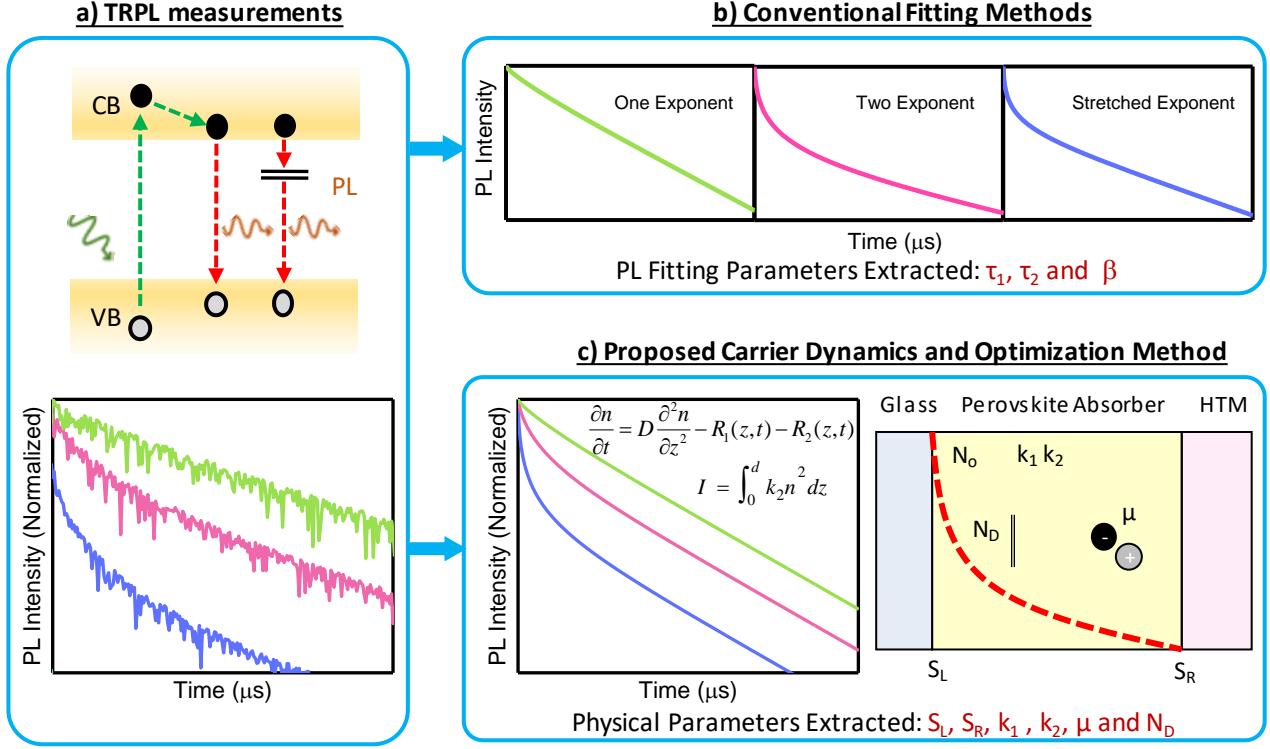


Figure 1 a) TRPL signals arising from recombination pathways b) Conventional fitting method of TRPL measurements for fitting constants. PL curves are often fitted by one, two and stretched exponential functions. Here τ_1, τ_2 and β show lifetimes and stretched constant, respectively. c) The proposed charge dynamics method predicts physical parameters by solving rate equation with appropriate boundary conditions based on the geometry. By numerical optimization, it deduces the opto-electronic properties from measurements. Here, surface recombination/interface recombination velocity (S_L and S_R), monomolecular recombination constant (k_1), bi-molecular recombination constant (k_2), mobility (μ) and doping density (N_D) are the physical parameters extracted.

2. Time Resolved Photoluminescence modeling

Let us consider the case of a perovskite layer deposited on a glass substrate and covered by a thin HTM layer as displayed in Fig. 2 a) and 2b).

The continuity equation in the perovskite layer can be written on the following form:

$$\frac{\partial n}{\partial t} = D \frac{\partial^2 n}{\partial z^2} - R_1(z,t) - R_2(z,t) \quad (1)$$

where n is the minority excess carrier density, D is the carrier diffusion constant, z is the distance from the origin taken at the location of the interface HTL/perovskite, R_1 is the recombination constant associated to Shockley Read Hall (SRH) recombination, and R_2 is the recombination rate associated with the band to band recombination (bimolecular process). The Auger recombination is negligible under the normal working condition of solar cells (below an excess carrier density of 10^{17}cm^{-3})³³. The end of the excitation laser pulse is taken as the time origin (i.e. at $t = 0$).

The SRH recombination rate is a function of the photocarrier density, the energy level of the trap (E_t), its cross section σ and density N_t ³⁴.

$$R_1 = \frac{(n_0 + n)(p_0 + p) - n_i^2}{(n_0 + n) + (p_0 + p) + 2n_i \cosh\left(\frac{E_i - E_t}{kT}\right)} \sigma v_{th} N_t \quad (2)$$

Where n_0 and p_0 are the equilibrium carrier densities of electrons and holes respectively, n and p are the densities of photogenerated carriers ($n = p$), E_i is the mid gap and E_t is the trap energy level.

Under low injection level conditions, the photocarrier density n is much lower than the equilibrium density of the majority carriers, R_1 can be expressed as linear function of the photocarrier density $n(z, t)$

$$R_1(z, t) \approx k_1 n(z, t) \quad (3)$$

where k_1 is the SRH recombination frequency. For n -type absorber, k_1 is given by:

$$k_1 = \frac{\sigma v_{th} N_t}{1 + 2 \frac{n_i}{n} \cosh\left(\frac{E_i - E_t}{kT}\right)} \quad (4)$$

R_2 is given by :

$$R_2(z, t) = k_2 \left[(n_0 + n)(p_0 + p) - n_i^2 \right] \quad (5)$$

where k_2 is the band-to-band recombination constant which is a characteristics of the material. It is clear from Eq. 2 that R_1 has some radiative part as in Eq. (5).

Assuming n -type absorber, and considering the low injection condition. $n = p \ll n_0 = N_D$, the term R_2 becomes also a linear function of the photocarrier density:

$$R_2(z, t) \approx k_2 N_D n \quad (6)$$

Therefore Eq. (1) can be rewritten under low injection conditions as follows:

$$\frac{\partial n}{\partial t} = D \frac{\partial^2 n}{\partial z^2} - (k_1 + k_2 N_D) n \quad (7)$$

Notice that the term $k_2 N_D$ is non negligible only if the absorbing layer is highly doped (for typical values of $k_1 = 10^7 \text{ s}^{-1}$ and $k_2 = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $N_D > 10^{17} \text{ cm}^{-3}$). Therefore, under low injection level conditions, and low doping concentration, the decay of the photogenerated carriers is mainly controlled by the SRH recombination rate k_1 .

Under high injection levels, Eq. (1) takes the following form

$$\frac{\partial n}{\partial t} = D \frac{\partial^2 n}{\partial z^2} - (k'_1 + k_2 N_D) n - k_2 n^2 \quad (8)$$

where k'_1 is given by

$$k'_1 = \frac{\sigma v_{th} N_t}{2 \left\{ 1 + \frac{n_i}{n} \cosh \left(\frac{E_i - E_t}{kT} \right) \right\}} \quad (9)$$

Note that the variation of k'_1 on the injection level depends upon the level of the trap. For deep level, that is $E_i - E_t \gg kT$, k'_1 is half of its value under low injection conditions, that is

$$k'_1 = \frac{\sigma v_{th} N_t}{2} \quad (10)$$

However, for shallow levels, k'_1 increases as the density of photocarriers n increases.

As shallow level contributes very little to the recombination process under low injection levels, we will consider only the deep levels in our analysis. Therefore, in the presence of deep levels, Eq. (1) can be rewritten in the following form for all injection levels:

$$\frac{\partial n}{\partial t} = D \frac{\partial^2 n}{\partial z^2} - (k'_1 + k_2 N_D) n - k_2 n^2 \quad (11)$$

Where the constant k'_1 varies from k_1 to $\frac{k_1}{2}$ as the injection is increased from low to high levels.

Considering the experimental configuration shown in Fig. 2, the photoluminescence signal is then obtained by integrating the radiative term over the absorber as follows

$$I_{PL} = \int_0^d k_2 n^2 dz \quad (12)$$

In order to obtain the PL signal decay versus time, we need to specify the boundary conditions of the problem and determine the function $n(z, t)$ by solving Eq. (11). These boundary conditions can be expressed at the ends of the absorbing materials by introducing a surface /interface recombination velocity, S . The inclusion of surface recombination velocity along with diffusion term provides an accurate assessment of the complicated kinetics at the initial PL signal.

In the case of an absorbing layer deposited on glass:

$$J(0, t) = S_L n(0, t)$$

and

$$J(d, t) = S_R n(d, t)$$

where J is the carrier flux and S is the surface/interface recombination velocity.

Note that, in absence of HTM layer (Fig. 2a), S_R characterizes the surface recombination at the free surface of the absorber. However, in presence of HTM layer (Fig. 2b), S_R integrates both the carrier extraction from the absorber to the HTM layer as well as a possible SRH recombination due to defects at the interface. S_L highlights the recombination velocity at the excited side of the substrate/sample film.

Radiative Efficiency or Photoluminescence Efficiency (PLE) provides an upper limit for solar cell where the main motivation is to decrease the trap assisted recombination³⁵. It is a fraction of the radiative recombination to the total radiative and non-radiative SRH recombination³⁶. Since this is a measure of emission and absorption of photons, PLE provides a direct figure of merit of material quality by linking the parameters such as N_0 , k_1 , k_2 and N_D as given by Eq. (13). Care must be taken when comparing PLE as it is governed by nature of the bandgap, direct or indirect.

$$PLE = \frac{k_2(N_D + n)}{k_1 + k_2(N_D + n)} \quad (13)$$

The initial distribution of carriers is given by

$$n(z, t_0) = N_0 e^{(\alpha z)} \quad (14)$$

where α is the linear coefficient of absorption of the absorbing material and N_0 is the initial photocarrier concentration at the glass/absorber interface.

The rate equation, Eq. (11), can be solved numerically to determine the carrier distribution $n(z, t)$. Considering the stiff nature of the problem, an implicit solver must be used.

Two observations can be pointed out:

1) The effect of carrier extraction is expected to become measurable only when the carrier diffusion length $L = \sqrt{D\tau}$ is comparable or larger than the thickness (d) of the absorbing layer.

2) The extraction of the carriers at the interface may lead to a charge build up at the interface which, in return, would affect the carrier extraction thus the parameter, S . Such possible effect would induce more complexity in the problem and is neglected in the current analysis.

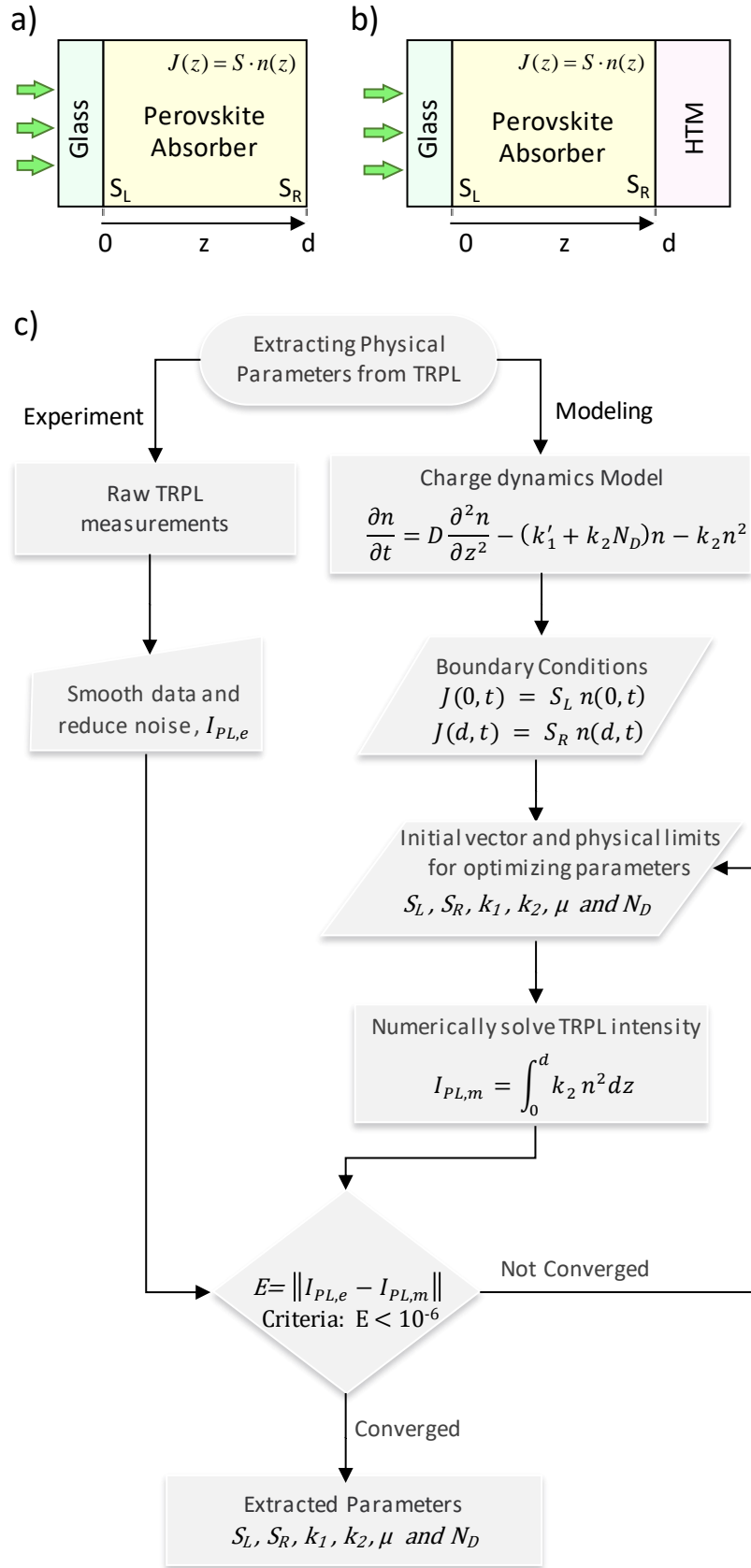


Figure 2 Schematic for samples and methodology for TRPL analysis for PSC. a) Perovskite deposited on glass (no carrier extraction), b) Glass structure/Perovskite/HTM with carrier extraction at Perovskite/HTL interface. c) Flow chart

describing the TRPL numerical modeling and charge dynamics based optimization method. The proposed solver is capable for simultaneously extracting physical parameters from device such as $S_L, S_R, k_1, k_2, \mu, N_D$.

3. Numerical Methodology

Figure 2c shows the flowchart for the numerical modeling and charge dynamics based optimization method. The experimentally obtained normalized TRPL signal, $I_{PL}/I_{PL,max}$, is smoothed first by reducing the machine associated noise. Poor signal-to-noise ratio associated with long decay tails with weak PL emission may hinder proper extraction of $n(t)$ resulting in unreliable parameters. In addition, care must be taken while selecting the time scale for the PL decay to be considered as this may overestimate or underestimate the processes occurring at different time regimes such as trap assisted recombination k_1 at longer time scales and radiative recombination k_2 at short time scale. For the extraction of parameters from TRPL curves, a gradient based multi-start optimization algorithm was developed and employed for an objective function of error between measured PL and modeled PL decay as given by Eq. (15).

$$\|E_{PL}\| = \|I_{PL,measured}(z,t) - I_{PL,modeled}(S_L, S_R, k_1, k_2, \mu, N_D)\| \quad (15)$$

where $\|\bullet\|$ is the 2nd norm.

The numerically modeled PL decay is capable of tracing temporal variation of optoelectronic properties along with the transport of minority carriers spatially. The collective reconstruction of spatial and temporal profile of PL makes it a robust model for precise determination of surface recombination (S_L and S_R), SRH recombination frequency (k_1), Band-to-band radiative recombination (k_2), carrier mobility (μ) and doping density (N_D). Numerically, higher order finite difference based scheme with Neumann boundary condition for surface recombination is employed for spatial discretization and the resulted rate equation of the system is solved using fully implicit ODE solver for calculating the PL signal in Eq. (12). Shorter time steps are used at the early time regimes to effectively capture the charge carrier physics with step size ($\sim 10^{-12}$). The fitting procedure is provided with an initial vector for optimizing parameters of $S_L, S_R, k_1, k_2, \mu, N_D$ and is iteratively solved until the stopping criteria of $\|E_{PL}\| < 10^{-6}$ between experimental and PL modeled decay is satisfied.

4. Results and Discussion

4.1 TRPL modeling analysis

In the following section, we generate a series of plots showing the effect of various physical parameters such as $S_L, S_R, k_1, k_2, \mu, N_D, N_0$ on the PL signal decay. This enables us to assess the sensitivity of the curves to these parameter changes and the possibility to extract these parameters from the experiment using an optimization fitting procedure. Then we will illustrate the methodology by using it for the analysis of PL curves obtained on perovskite thin films (sample on glass with and without an HTM layer) and single crystals.

Figure 3 shows typical PL curves for various values of surface recombination velocity: S_L and S_R , where S_L is at the glass, ETM or FTO interface and S_R is at the interface with HTM. Qualitatively, surface recombination

velocity, at interface results in quenching of PL decay showing a reduction in PL signal³⁷. Figure 3a and 3b shows the effect of S_R on PL kinetics due to varying recombination at sample/HTM interface. Here, two values for S_L are considered (10^1 cm/s and 10^5 cm/s). The PL signal quenching is due to the efficient carrier transfer to the interface which may include both carrier extraction from the absorber to HTM and possible SRH recombination due to interfacial defects³¹. Note that, in absence of HTM, S_R describes the recombination at the free surface. If the recombination is negligible at the free surface, then the presence of HTM is expected to increase S_R due to the extraction process. With higher S_L , i.e. more extraction from the photo-excited side, the quenching of PL curve is larger as the overall impact of trap assisted recombination is significant. At a longer time scale, both curves follow mono-exponential decay where k_1 becomes dominant over k_2N_0 .

Figure3c shows the effect of S_L on the PL signal. The initial decay signifies the carrier quenching to the adjacent glass/absorber interface. It is evident that PL decays more rapidly for injections near the sample-substrate interface for both S_R and S_L cases. Therefore, for curve fitting of PL measurements, it is important to decouple both surface recombination velocity and diffusion to assess the quality of each interface with the absorber²⁹. The key advantage of analyzing surface recombination is its direct relation with device performance and process parameters for fabricating PSC³⁸. This in turn can provide design guidelines for optimal device performance such as indicating the requirements for surface layer passivation³⁹.

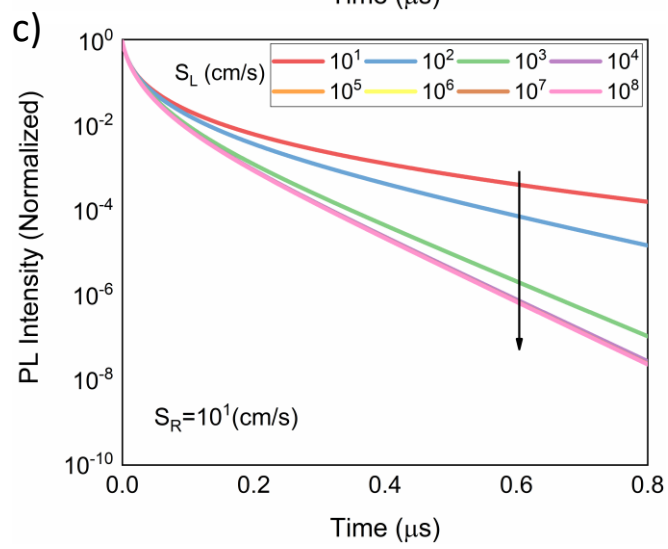
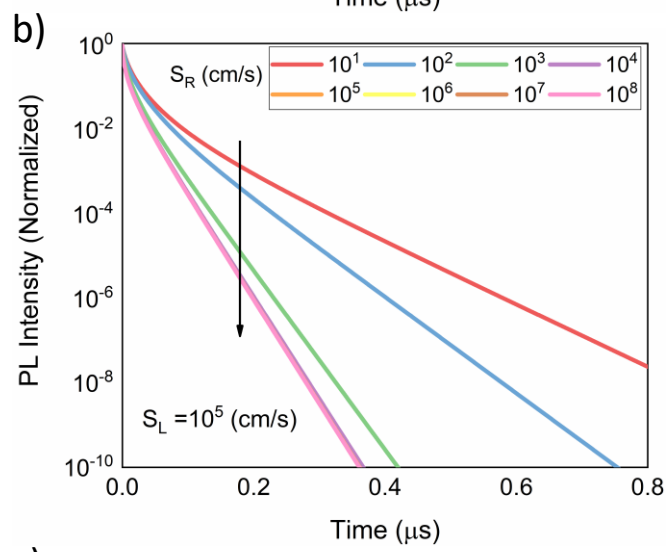
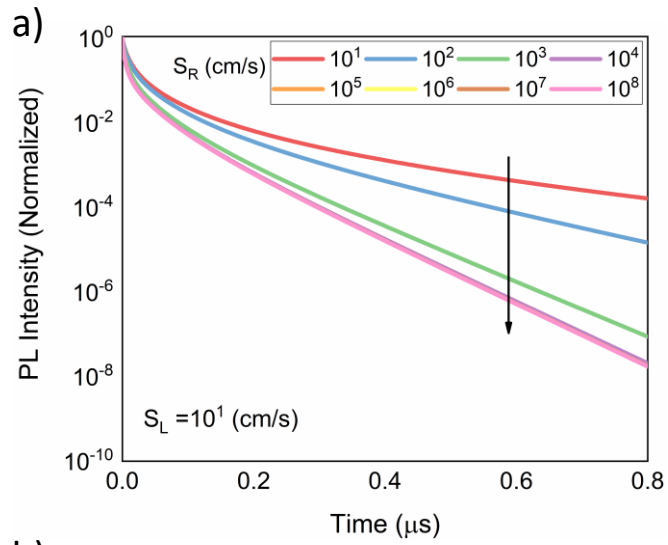


Figure 3 Effect of surface recombination velocity: Calculated surface /interface recombination velocity, S_L and S_R , for perovskite films. Here S_L and S_R characterizes the surface recombination at the glass/absorber interface and free surface of the absorber, respectively. In the presence of HTM layer, S_R integrates both the carrier extraction from the absorber to the HTM layer as well as a possible SRH recombination due to defects at the interface. Calculations are based on $d=0.3\mu\text{m}$, $\mu=0.1\text{cm}^2/\text{Vs}$, $k_1=10^6\text{ s}^{-1}$, $k_2=10^{-12}\text{ cm}^3/\text{s}$, $N_D=10^{10}\text{ cm}^{-3}$, $N_0=10^{15}\text{ cm}^{-3}$. Respective S_L and S_R are indicated in the figures with arrows indicating the increase in parameter.

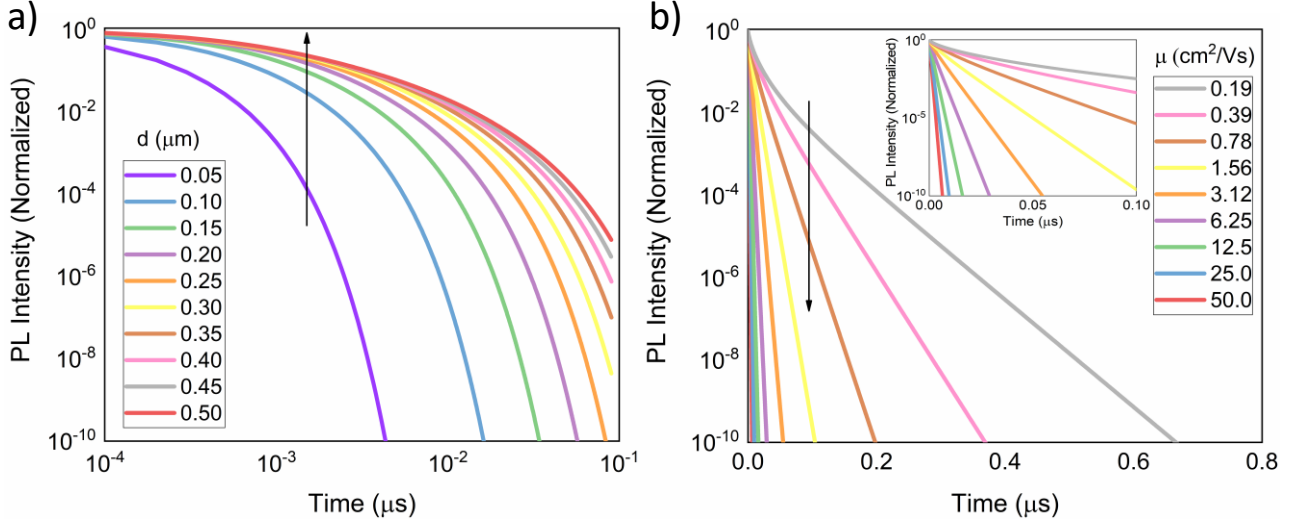


Figure 4 Effect of a) absorber thickness (d) and b) charge carrier mobility (μ): Calculations are based on $S_L=10^1\text{ cm/s}$, $S_R=10^5\text{ cm/s}$, $k_1=10^6\text{ s}^{-1}$, $k_2=10^{-12}\text{ cm}^3/\text{s}$, $N_D=10^{10}\text{ cm}^{-3}$ and $N_0=10^{15}\text{ cm}^{-3}$. Fig 4a has fixed carrier mobility of $0.1\text{ cm}^2/\text{Vs}$ whereas 4b assumes $d=0.3\mu\text{m}$. The inset in Fig. 4b shows the zoomed PL at shorter time scale. The effect of both thickness (d) and minority carrier mobility (μ) can be better described by carrier diffusion length through $L = \sqrt{D\tau}$ where $D = \frac{kT}{q}\mu$ and τ represents the effective lifetimes from radiative and non-radiative SRH recombination³⁴. Notably, the effect of carrier extraction is significant only when the width (d) of the absorber is comparable or smaller than the diffusion length ($L \approx 0.5\mu\text{m}$ in this case with k_1 as limiting recombination mechanism).

Figure 4a and 4b shows the effect of PL on carrier dynamics as a result of varying thickness and minority carrier mobility. The effect of both thickness (d) and minority carrier mobility (μ) can be described by carrier

diffusion length through $L = \sqrt{D\tau}$ where $D = \frac{kT}{q}\mu$ and τ represents the effective lifetimes from radiative and

non-radiative SRH recombination³⁴. Diffusion length, L , is the average distance an excess carrier travels before it recombines whereas D is the diffusion constant of the material at specific temperature T . It is dependent on the mobility and life time of the material which characterizes the quality of the material. For a constant mobility of $0.1\text{ cm}^2/\text{Vs}$, increasing the absorber thickness reduces the PL signal as a result of lesser recombination due to the interface shown in Fig.4a . For thinner absorbers, photo-generated charge carriers have a higher chance to reach the HTM interface thereby leading to faster PL quenching. Particularly, the effect of carrier extraction is significant only when the diffusion length is comparable or larger than the thickness of the absorber i.e $L \geq d$. By considering SRH to be the dominant recombination mechanism, $k_1 \gg k_2$, diffusion length was found to be $0.5\mu\text{m}$ in this case. Moreover, combination of the thickness dependency on PL with surface recombination velocity at interface can assist in decoupling the bulk and surface recombination lifetime^{40,41}.

Charge carrier mobility (μ) plays a crucial role in determining the shape of PL signal as displayed in Fig. 4b. The initial decay of the PL curve is governed by diffusion for the carriers especially for higher injection regime

where the quadratic dependence of injection on the recombination is significant [Please see Eq. (11)]. Therefore, minority carriers with high mobility diffuses faster to the interface thereby producing a sharper PL decay. However, as the carrier mobility decreases, extraction at the interfaces is slowed down due to the possible recombination of the carrier in the bulk resulting in lower PL signal. It should be noted that charge carrier dynamics and consequently the PL signal is found to be extremely sensitive to the carrier mobility especially at the first few ns after excitation⁴².

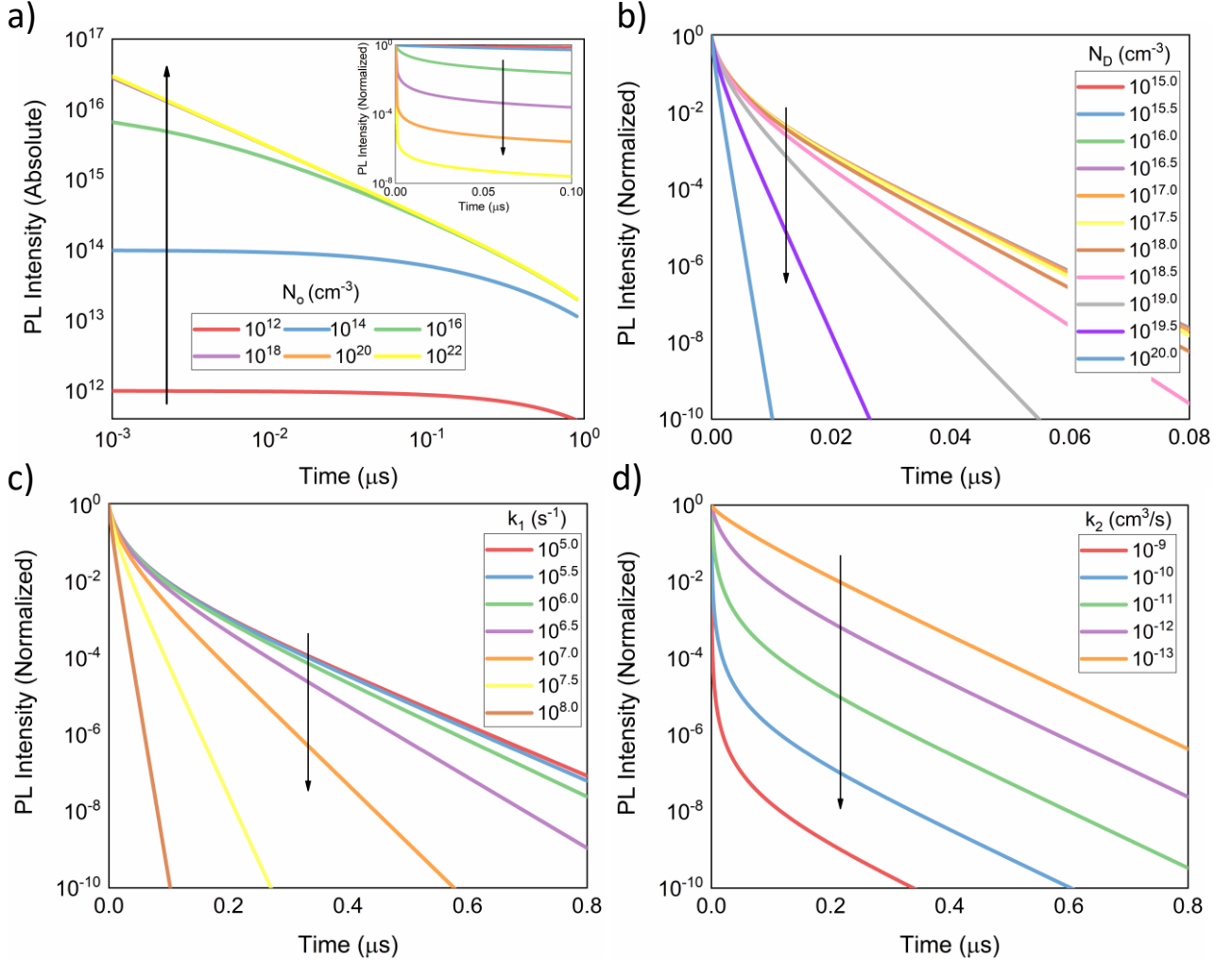


Figure 5 TRPL dependence of initial carrier concentration (N_0), doping density (N_D), SRH recombination frequency (k_1) and Band-to-band recombination (k_2). Calculations are based on $d=0.3 \mu\text{m}$, $\mu=0.1 \text{ cm}^2/\text{Vs}$, $S_L=10^1 \text{ cm/s}$ and $S_R=10^5 \text{ cm/s}$ with parameters for a) $k_1=10^6 \text{ s}^{-1}$, $k_2=10^{-12} \text{ cm}^3/\text{s}$, $N_D=10^{10} \text{ cm}^{-3}$; b) $k_1=10^6 \text{ s}^{-1}$, $k_2=10^{-12} \text{ cm}^3/\text{s}$, $N_0=10^{15} \text{ cm}^{-3}$; c) $k_2=10^{-12} \text{ cm}^3/\text{s}$, $N_D=10^{10} \text{ cm}^{-3}$, $N_0=10^{15} \text{ cm}^{-3}$; d) $k_1=10^6 \text{ s}^{-1}$, $N_D=10^{10} \text{ cm}^{-3}$, $N_0=10^{15} \text{ cm}^{-3}$. The arrows indicate the increase in material parameter analyzed. Fig 5a contains the absolute and normalized (inset) for TRPL decay for better visualization of injection effect.

Figure 5a presents the curves for injection dependent PL kinetics. These TRPL curves can provide a detailed insight into various recombination pathways^{31,33,36}. The PL transients and recombination kinetics is a function of injection level, $n(t)$. For better understanding, the effect of injection is discussed in conjunction with k_1 and

k_2 . SRH recombination rate, k_1 , signifies the defect assisted recombination in the material. Therefore, from the device and fabrication point of view, the contribution from non-radiative SRH recombination should be lower than its radiative counterpart for a pure material and better crystallinity⁴³. In TRPL decays as shown by Fig 5c, SRH follows the mono-exponential decay essentially where the effect of k_1 becomes dominant over $k_2 N_D$, i.e. $k_1 \gg k_2 N_D$. Under such condition, $n \propto \exp(-k_1 t)$ and a linear relation is observed at longer time scales. As k_1 increases, the PL quenching increases due to reduced carrier lifetime and higher recombination. It is important to understand that the variation of SRH recombination upon the injection level depends on the trap level. From shallow to midgap deep level traps (i.e. at $E_g/2$), the constant k_1' varies from k_1' to $\frac{k_1'}{2}$ as the injection is increased from low to high. This behavior is caused by the saturation of trap states by the carriers^{44,45}. Thus, SRH recombination is a dominant mechanism at low level injection where it is mainly governed by single charge carrier specie. The decay of the photogenerated carriers is mainly controlled by the SRH recombination frequency k_1' under low injection condition whereas k_2 is dominant for high level injection (HLI) condition at initial time scale. Physically, higher injection results in more radiative recombination ($I_{PL} \propto n^2$) and carrier extraction at the excited side thereby leading to more quenching at short time scale. Once the carrier moves away from the excited interface, the normalized PL curves results in similar shape with an offset between each other when the effect of $k_2 N_0$ becomes comparable to k_1 . The behavior can be seen clearly from absolute PL curves in Fig. 5a where the effect of injection is proportional to PL signal. One key benefit of using different injection levels is the possibility to acquire better signal-to-noise ratio at larger time scale where the PL emission is weak. This is extremely valuable in capturing the effect of k_1 from long decay tails³⁷.

The effect of doping density (N_D) on TRPL is an effective measure of a material quality^{46,47}. Figure 5b shows the effect of doping on the PL kinetics. The transient PL curves at different time scales is either limited by SRH recombination frequency k_1 or the product of doping density and radiative band to band recombination, $k_2 N_D$ ³¹. Generally, the presence of doping, intentional or unintentional, will decrease the carrier life time. The effect of the term $k_2 N_D$ becomes important for a highly doped absorbing layer or very low SRH values (for typical values of $k_1 = 10^7 \text{ s}^{-1}$ and $k_2 = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $N_D > 10^{17} \text{ cm}^{-3}$). Consequently, under low injection level (LLI) and low doping concentration, the decay of the photogenerated carriers is mainly controlled by the SRH trap mediated recombination, k_1 ⁴⁸.

Radiative band-to-band recombination, R_2 , is an intrinsic property of the material which characterizes the reciprocal relation between absorption and emission of photon. TRPL is, therefore, a direct measure of radiative recombination. Under LLI ($n = p \ll n_0$), R_2 becomes a linear function of the photocarrier density, $R_2 \propto n(t)$. Contrarily, HLI shows quadratic dependence of recombination rates on the photocarrier density, $R_2 \propto n(t)^2$. Figure 5d shows the effect of variable k_2 on the PL decay. Under HLI, the effect of k_2 is dominant which explains the initial decay in the Figure5b. The effect of k_2 is dominant when $k_2 N_D \gg k_1$. It can be observed that as k_2 decreases to $10^{-13} \text{ cm}^3 \text{ s}^{-1}$, the contribution from k_1 (i.e. mono-exponent behavior) is significantly increased.

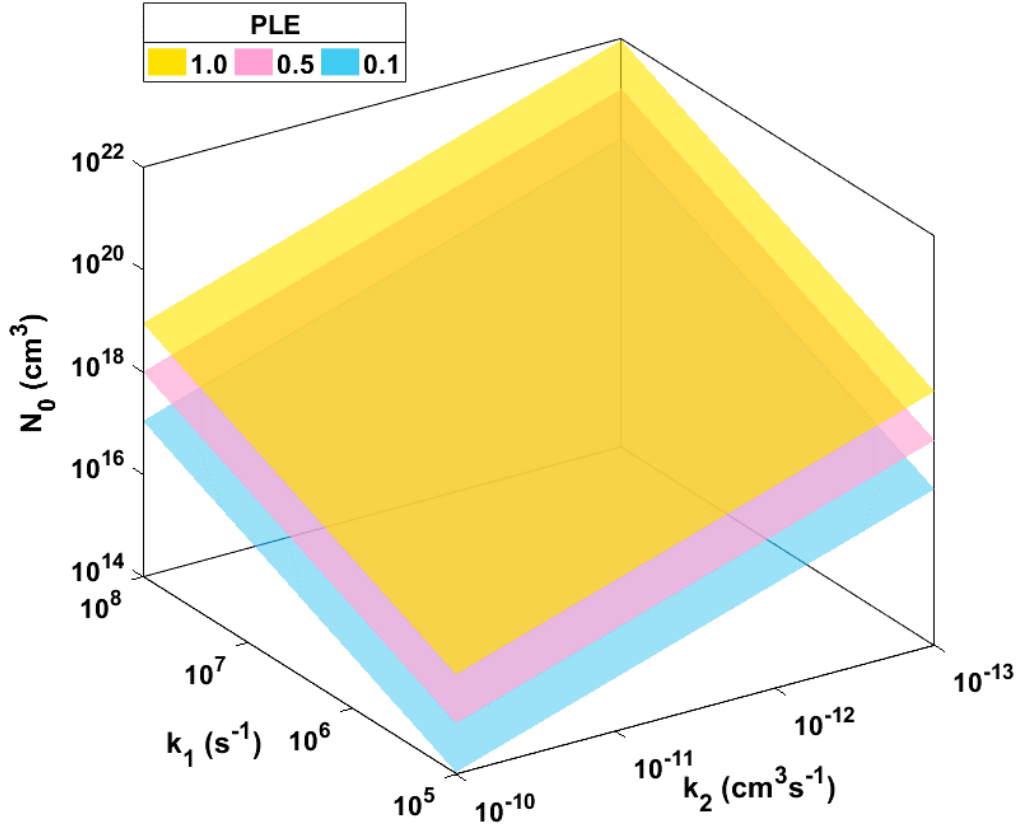


Figure 6 Photoluminescence Efficiency (PLE) trend for injection level (N_0), SRH recombination frequency (k_1) and band-to-band radiative recombination (k_2). The iso-surfaces represent the PLE at specific values of 1.0, 0.5 and 0.1 for different combinations of k_1 , k_2 and N_0 with constant doping density ($N_D=10^{10} \text{ cm}^{-3}$). PLE is a fraction of the radiative recombination to the total (radiative and non-radiative) recombination.

Figure 6 presents the calculated PLE as function of k_1 , k_2 , and N_0 with N_D as 10^{10} cm^{-3} . For PLE to be high, $k_1 \ll k_2(N_D + N_0)$ under high injection level needs to be satisfied whereas under low injection level this condition reduces to $k_1 \ll k_2(N_D)$. PLE provides an upper limit for solar cell where the motivation is to decrease the trap assisted recombination³⁵. However, it should be noted that since PL is a measure of band-to-band recombination, PLE is dependent on the nature of band gap of the material. PLE has been used extensively as a performance indicator in light emitting applications such as LED and lasers⁹.

4.2 Analysis of experiment

Experiments were carried out to analyze the robustness of the developed method and extract physical parameters from TRPL optimization algorithm. For better assessment, thin films (TF) and single crystal (SC) based devices were examined. Thin films for PSC were fabricated with and without HTM whereas single crystal device transients were obtained from Ref. ²⁹. Figure 7 a) and 7b) shows the PL signal decay obtained on two samples fabricated for thin films. The first one corresponds to a thin film of Methylammonium lead iodide deposited on glass and the second deposited on a similar glass substrate and covered by a thin layer of OMeTAD as hole transport material. TRPL decay for thin films was monitored at excitation powers of 0.466 mW, 0.585 mW and 1.115 mW with an excitation pulse of 405 nm and absorber thickness of 0.3 μm . The fitting is done collectively

where only N_0 and k_2 (to allow for photon recycling) are varied for different excitation levels while all the other parameters are kept common. For single crystal, Fig. 8 shows the measurements which were performed on $10 \mu\text{m}$ thick absorber with an excitation of 447 nm ²⁹.

Generally, the type of TRPL decays shown in Fig. 7 and Fig. 8 are fitted by one or two exponential functions as follows ^{49–52}

$$I_{PL} = A_1 e\left(-\frac{t}{\tau_1}\right) + A_2 e\left(-\frac{t}{\tau_2}\right) \quad (16)$$

or using a stretched exponential function ^{25–28}

$$I_{PL} = A_1 e\left(-\frac{t}{\tau_1}\right) + A_2 e\left(-\frac{t}{\tau_2}\right)^\beta \quad (17)$$

The constants τ_1 and τ_2 are expected to be related to the physical parameters of the absorbing layer such as k_1 , k_2 and μ but also to the photocarrier extraction and /or recombination at the interfaces. However, this relation is not straightforward. Here, we show that the physical parameters of the problem such as k_1 , k_2 and the interface recombination velocity, S , can be extracted by fitting the experimental data to thin films with and without HTM and Single Crystal of perovskite

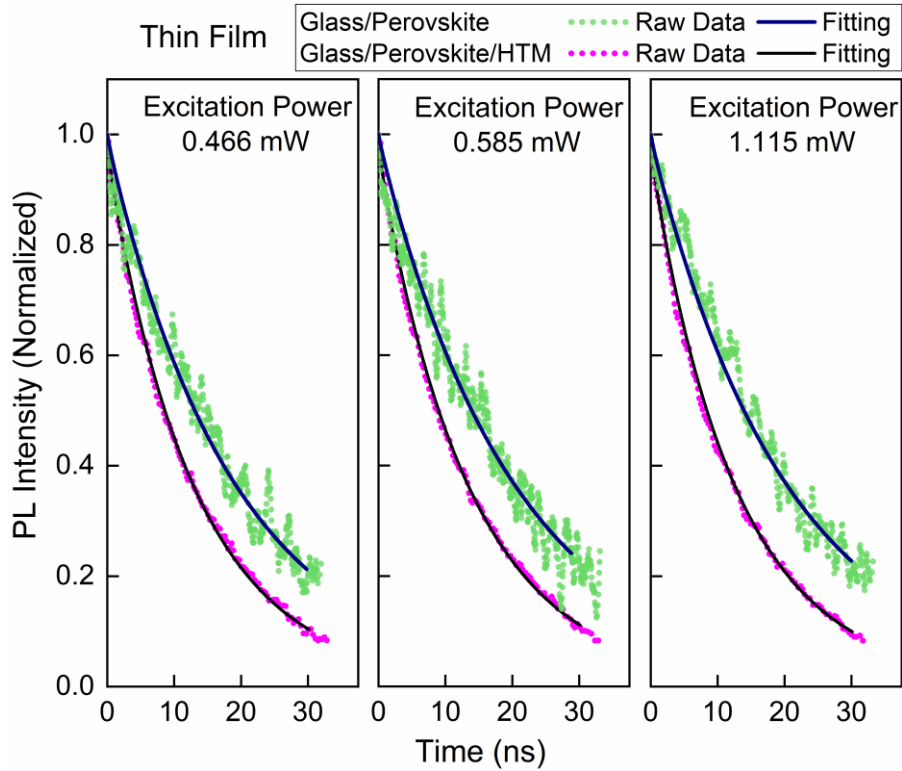


Figure 7 Evaluation of the TRPL fitting on the experimental measurements for perovskite thin films. Samples prepared were Glass/Perovskite and Glass/Perovskite/HTM with sample thickness (d) of $0.3 \mu\text{m}$. Three measurements at excitation power of 0.466 mW , 0.585 mW and 1.115 mW were carried out with an excitation pulse of 405 nm and beam size of $800 \mu\text{m}^2$.

Table 1 shows the resulted fitting parameters from the proposed charge dynamics and optimization method. Importantly, the inclusion of μ , N_D , S_L and S_R at both interfaces allowed to accurately capture the physics of TRPL kinetics by improving the conformity of fits to experimental measurements. The decay was found to be higher for thin films in Glass/perovskite/HTM due to the higher rate of extraction at the HTM interface than pure perovskite film. This is also substantiated by the increase in surface recombination velocity from 5.89×10^4 to $8.91 \times 10^5 \text{ cm s}^{-1}$ when we employ HTM for quenching. Interestingly, S_R estimated here for thin films is in the same order of magnitude for several unpassivated optoelectronic materials such as GaAs ($\sim 10^5 \text{ cm s}^{-1}$)⁵³ and n-type Si ($\sim 10^6 \text{ cm s}^{-1}$)⁵⁴. The higher surface recombination velocity, therefore, advocates the usage of surface passivation techniques for PSC⁵⁵. The initial time decay component is also affected by the surface recombination from the glass/absorber interface i.e. the excited side S_L . It was found to be lower around 24.54 and 5.75 cm s^{-1} for TF and SC, respectively. This can be attributed to the trap filling process due to carrier injection from the excited interface leading to lower interfacial recombination.

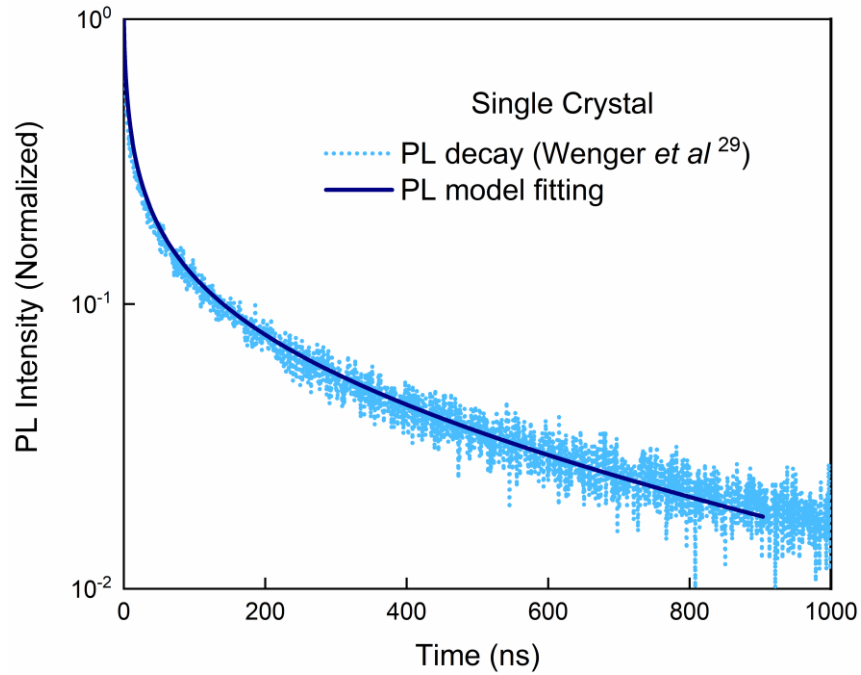


Figure 8 TRPL curve fitting for perovskite single crystal data ($10 \mu\text{m}$ thick) obtained from Ref: Wenger *et al*²⁹. Excitation was carried out at 447 nm with $N_0 = 7.8 \times 10^{16} \text{ cm}^{-3}$.

SC showed a long decay tail up to 1000 ns whereas TF exhibited shorter PL decay lasting up to $\sim 30 \text{ ns}$. Qualitatively, this short decay in TF implies that the defect concentration is higher in TF than SC. In Fig. 8 after 1000 ns , the signal to noise ratio was found to be poor for suitable extraction of SRH based parameter. The SRH recombination rate, k_1 , was found to be $7.47 \times 10^6 \text{ s}^{-1}$ ($\tau_{TF,SRH} = 134 \text{ ns}$) for thin film whereas in single crystal it was found to be $4.07 \times 10^5 \text{ s}^{-1}$ ($\tau_{SC,SRH} = 2511 \text{ ns}$). The results agree well with earlier reports where the

range of k_1 is from 10^6 to 10^9 s^{-1} . Furthermore, it is expected due to the better quality of SC over TF as $k_{1,SC} < k_{1,TF}$. Remarkably, doping density was estimated to be 1.38×10^8 to $2.01 \times 10^{13} \text{ cm}^{-3}$ for SC and TF, respectively. Again, this is due to the better quality of SC than TF. The low concentration demonstrates the possible unintentional photodoping arising from acoustic phonon scattering^{56,57} or by trapped charge carriers from subgap states⁵⁸. However, for accurate analysis, $k_2 N_D$ should be compared with k_1 under low injection whereas under high injection the effect of N_0 also becomes significant.

Thin films exhibited higher band to band recombination, k_2 , than single crystals ($k_{2,TF} = 9.55 \times 10^{-12} \text{ cm}^3/\text{s}$ and $k_{2,SC} = 1.05 \times 10^{-13} \text{ cm}^3/\text{s}$). The increase in k_2 in thin films can be attributed to the presence of small grain boundaries which redshifts the bandgap of the material resulting in higher radiative recombination^{59,60}. Manser and Kamat have reported a value of $2 \times 10^{-9} \text{ cm}^3/\text{s}$ for organometal halide perovskites⁶¹ while Johnston and Herz reported values ranging from 6×10^{-11} to $9.2 \times 10^{-10} \text{ cm}^3/\text{s}$ for different hybrid perovskite materials⁹. The relatively higher k_2 in TF than SC is due to the additional localized radiative recombination from small grain boundaries⁵⁹.

Table 1 Comparison of extracted parameters from TRPL for thin films and single crystal of perovskites.

Parameter	Unit	Thin Film	Single Crystal
k_1	s^{-1}	7.47×10^6	4.07×10^5
k_2	cm^3/s	9.55×10^{-12}	1.05×10^{-13}
N_D	cm^3	2.01×10^{13}	1.38×10^8
μ	cm^2/Vs	0.18	2.04
S_L (Glass/Absorber)	cm/s	24.54	5.75
S_R (Absorber)	cm/s	5.89×10^4	1.00
S_R (Absorber/HTM)	cm/s	8.91×10^5	-
PLE	-	3.16×10^{-5}	1.62×10^{-4}

Extraction of carrier mobility from TRPL transients resulted in values of $0.18 \text{ cm}^2/\text{Vs}$ for TF which was increased to $2.04 \text{ cm}^2/\text{Vs}$ for SC. For the same SC, minority carrier mobility was estimated as 10 by Wenger et al²⁹. Similar mobilities have been reported by earlier works on SC such as $2.5 \text{ cm}^2/\text{Vs}$ for PSC using space-charge-limited current technique by Shi et al^{6,62}. On the other hand, mobilities for thin film PSC covers a large span from 10^{-4} to $10 \text{ cm}^2/\text{Vs}$ ⁶³. The difference between the thin films and single crystals in PSC suggests that the grain morphology and boundaries is a huge factor in determining the carrier mobility in these materials. Herz⁶² has showed recently that there exists a wide range of charge carrier mobility arising due to experimental uncertainties from different experiments even for the same stoichiometric material. Although it is expected for the carrier mobilities for SC to be higher than TF, the difference is not found to be huge in the literature⁶².

PLE for the SC and TF was calculated to be 3.16×10^{-5} and 1.62×10^{-4} , respectively. PLE in this order of 10^{-4} to 10^{-5} shows a good potential for PSC when compared with previous generation solar cells⁶⁴. It is vital to understand that PL as a result of radiative recombination is dependent on the nature of the bandgap, direct or

indirect. This could be observed from Green's consolidated list of both direct and indirect band semiconductors for PLE which has a huge span ranging from 2.25×10^{-1} for GaAs to 2.7×10^{-9} for OPV cell⁶⁴. Even in the same direct band family, thin film with the localized grain boundaries may yield higher recombination⁶⁵ as observed in PL results (Table 1) than its counterpart SC with higher crystallinity.

Conclusion

A comprehensive TRPL analysis has been carried out to assess the carrier dynamics due to bulk and interfacial recombination in perovskite films. The work herein provides insight into the transport and extraction kinetics by decoupling the effect of different processes contributing to TRPL signal. By linking this rate model with the experimental measurements, the purpose is to go beyond the conventional fitting life times and extract the physical parameters such as S_L , S_R , k_1 , k_2 , μ and N_D . An excellent conformity of fits to experimental data is found by including the effect of diffusion, doping density and surface recombination velocity at interfaces for accurate representation of TRPL kinetics. The resulted physical parameters from thin films and single crystals of perovskites clarified the distinct nature of both materials and provided hints for possible improvements. The PL signal quenching is found to be due to the efficient carrier transfer to the interface which included both the carrier extraction from the absorber to HTM and SRH recombination due to interfacial defects. Under low injection level and low doping concentration, the decay of the photogenerated carriers is mainly controlled by the SRH recombination rate, k_1 , whereas radiative recombination, R_2 , becomes significant under high injection level leading to higher PL efficiency. For accurate assessment and identification of the dominant recombination from PL decay, it is recommended to compare k_1 with $k_2(N_D + N_0)$. The ability of the proposed charge dynamics model to swiftly extract meaningful optoelectronic parameters from TRPL signal makes it a standard characterization tool for acquiring in-depth knowledge of the material.

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