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Performance Potential of Gas Foil Thrust Bearings Enhanced with Spiral Grooves

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Abstract

The upscaling of turbomachinery using gas foil thrust bearings is limited because of their limited load capacity and the thermal issues linked with very thin film thickness. The improvement potential of spiral grooves manufactured on the top-foil of such bearings is investigated in terms of load capacity and drag torque for a wide range of ramp depth, compressibility number and bearing compliance. Multi-objective optimization of grooves parameters allows to identify a trade-off between the drag reduction and the load capacity improvement. In some cases, load capacity improvements reach nearly 70% or drag torque at equal load diminishes by 40%. However, the results suggest that the ultimate load capacity of the bearing is reduced compared to plain gas foil thrust bearings.

Keywords: Gas Lubrication, Foil Bearings, Axial thrust bearing, Simulation

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Roman symbols

a	Groove length (m)
b	Ridge length (m)
c_s	NGT coefficient (-)
e	Eccentricity (m)
f	NGT coefficient (-)
g	NGT coefficient (-)
h	Clearance (m)
h_0	Nominal clearance (m)
h_g	Groove clearance (m)
h_r	Ridge clearance (m)
h_R	Ramp depth (m)
K	Foil stiffness (Nm^{-3})
P	Pressure (Pa)
R	Radius (m)
r	Radial coordinate (m)
s	Bump foil pitch (m)
T	Drag torque (Nm)
T_r	Drag torque ratio (-)
W	Load capacity (N)
W_r	Load capacity ratio (-)

Greek symbols

α	Groove aspect ratio, compliance (-)
$\hat{\beta}$	Groove angle ($^\circ$)
δ	Groove depth (m)
ϵ	Eccentricity ratio (-)
θ	Circumferential coordinate (-)
Λ	Compressibility number (-)
μ	Dynamic viscosity (Pa s)
ω	Angular velocity (rad s^{-1})

Superscripts

—	Non-dimensional
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Subscripts

<i>a</i>	Ambient condition
<i>F</i>	Foil
<i>g</i>	Groove
<i>i</i>	Inner
<i>o</i>	Outer
<i>R</i>	Ramp
<i>r</i>	Ridge, ratio

Acronyms

<i>GFSGTB</i>	Gas foil spiral groove thrust bearing
<i>GFTB</i>	Gas foil thrust bearing
<i>NGT</i>	Narrow groove theory
<i>SGTB</i>	Spiral groove thrust bearing

1. Introduction

Gas Foil Thrust Bearings (GFTB) are widely used in oil-free airborne applications such as microturbomachinery. While the first applications of this technology were small-scale with modest loads, global research efforts are being made toward the application of the compliant gas bearing technology to upscaled systems, with larger loads, in order to broaden the scope of application of GFTB and oil-free bearings in general.

1.1. Nature of the issue

Heshmat [1] proposed a model of GFTB considering the compliant bump foil as a simple elastic foundation and performed a parametric study to identify the geometry maximizing the load capacity. A considerable effort was spent by the community on the refinement of this model, implementing more complex foundation models or refining the method for the computation of the compliance coefficient. The layout of GFTB studied by Heshmat is a widely used design in oil-free turbomachinery applications such as supercritical CO₂ compressors [2] or turbochargers [3]. Moreover, the model developed decades ago by Heshmat is still of use in the recent literature, showing a reasonable agreement with experimental data [2, 3, 4]. The upscaling trend in size of rotors supported on foil bearings is limited by their load capacity and drag losses, which may lead to a delicate thermal management [5]. Scaling laws do not play in favor of larger applications, as showed by Prasad [6] and Dellacorte [7]. To overcome this intrinsic limitation, researchers have investigated numerous possibilities to further increase the load capacity of GFTB. **The clearance distribution was optimized by Lehn [8] to maximize the load capacity using a gradient-based optimization.** A hybrid foil thrust bearings was investigated by Lee et Kim [9], where compressed air is supplied to the bearing fluid film in order to sustain a thin lubricating gas film even at high load. Magnetic bearings can also be a solution to relieve the aerodynamic bearing, as suggested by Heshmat et al. [10]. Both alternatives imply the use of auxiliaries, which is costly in terms of space, investment and power and reduces the reliability.

In the meantime, the development of rigid spiral groove thrust bearings (SGTB) followed a parallel path, starting with Malanoski and Pan [11] who applied the Narrow Groove Theory (NGT) to model grooved thrust bearings. However, this technology is limited to very small-scale machines because of the tight manufacturing tolerances required. The recent literature brought

37 an promising improvement potential in terms of static stiffness and dynamic
38 stability for SGB with non-constant groove parameters, with the work of
39 Hashimoto et al. [12] and Schiffmann [13].

40 Despite the progress accomplished, the two technologies remain isolated
41 one from another. An early attempt to combine the SGTB with a compliant
42 structure was realized by Licht in 1981 [14] with a full bearing based on
43 Malanoski's rigid design. The compliant structure was designed such that
44 the top foil remains parallel to the runner under load in order to preserve the
45 validity of Malanoski's performance predictions. Unfortunately, no model
46 was proposed and the improvement potential was not assessed. Based on
47 this work it is hypothesized that the addition of spiral grooves on a GFTB's
48 top foil can be of practical interest in the quest of enhanced load capacities
49 and eased thermal management. Moreover, the manufacturing of grooves is
50 inexpensive and could even be retrofited on existing GFTBs.

51 *1.2. Goals and objectives*

52 The present work investigates the use of spiral grooves manufactured
53 on the GFTB's top foil to improve the load capacity and/or to reduce the
54 drag losses. The objective are to: (1) develop a model for Gas Foil Sprial
55 Groove Thrust Bearings (GFSGTB), (2) investigate the static performance
56 of such bearings in comparison to their ungrooved equivalent in terms of load
57 capacity and losses and (3) devise design guidelines.

58 *1.3. Scope of the Paper*

59 The GFTB model of Heshmat, including a simple foundation model for
60 the compliant structure, is combined with the modified Reynolds equation of
61 the NGT to model the pumping action of logarithmic grooves manufactured
62 on the top foil of the bearing. Multi-objective optimizations are performed for
63 various geometries (ramp depth) and operating conditions in order to identify
64 trade-offs in terms of load capacity and losses. Compressibility numbers up to
65 1000 are evaluated. The potential of the new bearing geometry is highlighted,
66 as well as its limitations. Based on these results, a set of design guidelines is
67 suggested to take advantage of the new layout.

68 **2. Theory**

69 The layout under investigation consists in an inward-pumping spiral groove
70 thrust bearing, where grooves are located on the outer diameter (Fig.2). Ini-
71 tially, the section covering the angle θ_R , referred as *ramp*, is converging (Fig.

72 1) with a depth h_R and a nominal clearance h_0 . The Narrow Groove The-
73 ory is employed to predict the overall pressure in the grooved region of the
74 bearing, assuming a infinite number of groove-ridge pairs, so the pressure
75 variation over a groove-ridge pair vanishes globally, while varying linearly
76 between a groove and the following ridge locally. This hypothesis is equiv-
77 alent to a local incompressibility of the lubricant. It allows an efficient and
78 effective modelling of groove patterns without the need of fine grid size to
79 capture the grooves individually. The first use of this theory to analyze SGTB
80 was done by Malanoski and Pan [11]. The analysis was later supported by
81 Zirkelback and San Andres [15] with the finite element method. Only the
82 resulting differential equation, as developed in [16] for an isothermal ideal
83 gas for steady state operation is displayed here:

$$\begin{aligned} \partial_\theta \left[\bar{P} \left(\frac{1}{\bar{r}} f_1 \partial_\theta \bar{P} + f_2 \partial_z \bar{P} \right) \right] + \partial_{\bar{r}} \left[\bar{P} (f_2 \partial_\theta \bar{P} + f_3 \bar{r} \partial_{\bar{r}} \bar{P}) \right] \\ + c_s (\bar{r} \sin \beta \partial_\theta (f_4 \bar{P}) - \cos \beta \partial_{\bar{r}} (\bar{r}^2 f_4 \bar{P})) = \Lambda \bar{r} \partial_\theta (f_5 \bar{P}) \end{aligned} \quad (1)$$

84 where the geometry is presented in Figures 2 and 1 and functions f_i are
85 summarized in the Appendix. This equations applies to the entire bearing
86 domain, reducing to the normal Reynolds equation in the land region, where
87 $\bar{h}_g = \bar{h}_r = \bar{h}$.

88 The modeling is based on the work by Heshmat [1] using a simple foun-
89 dation model for the compliant structure. The non-dimensionalization of the
90 governing equation is performed as follows:

$$\bar{P} = P/P_a \quad \bar{r} = r/R_o \quad \bar{h}_{r/g} = h_{r/g}/h_0 \quad \Lambda = \frac{6\mu\omega R_o^2}{P_a h_0^2} \quad (2)$$

91 The non-dimensional ridge and groove clearances are expressed as a func-
92 tion of the position and local pressure :

$$\begin{aligned} \bar{h}_r &= 1 - \epsilon + g(\theta) + \alpha_F (\bar{P} - 1) \\ \bar{h}_g &= \bar{h}_r + \bar{\delta} \end{aligned} \quad (3)$$

93 where the compliance α_F is expressed as follows:

$$\alpha_F = \frac{P_a s}{K_f h_0} \quad (4)$$

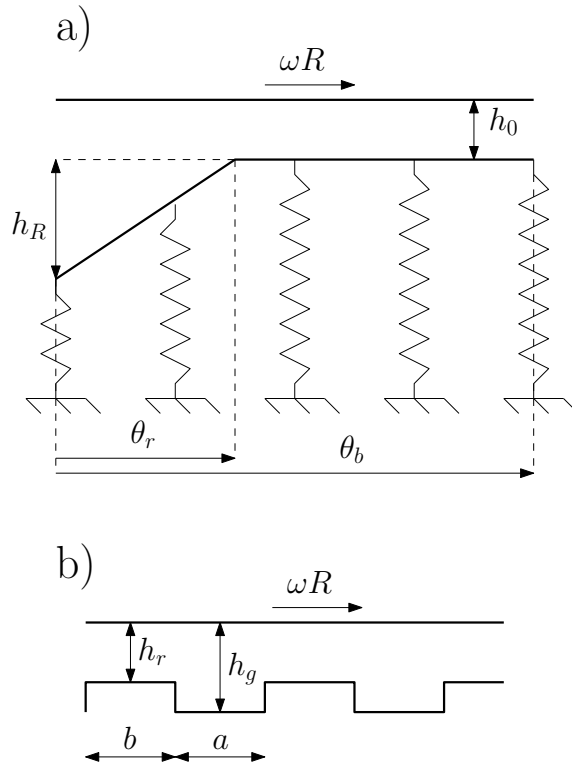


Figure 1: Geometry and nomenclature of GFSGTB

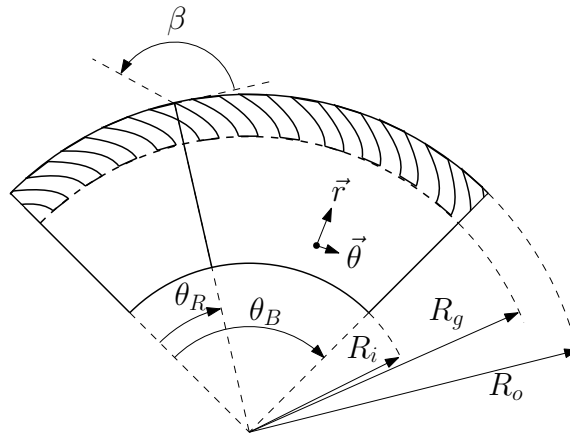


Figure 2: Geometry and nomenclature of inward-pumping GFSGTB

94 $g(\theta)$ expresses the change in clearance in the converging sector of the fluid
 95 film domain:

$$g(\theta) = \max [\bar{h}_R (1 - \theta/\theta_R), 0] \quad (5)$$

96 The term ϵ is the eccentricity ratio, defined as $\epsilon = e/h_0$, with e being the
 97 axial displacement of the rotating smooth disk from its nominal position.
 98 The boundary conditions of Eq. 1 are ambient pressure at $\bar{r} = R_i/R_o$, $\bar{r} = 1$,
 99 $\theta = 0$, $\theta = \theta_B$. On the line $\bar{r} = R_g/R_o$, the continuity of the radial mass flow
 100 rate across the land and grooved region is imposed:

$$\dot{m}_{r,groove} = \dot{m}_{r,land} \quad (\bar{r} = R_g/R_o) \quad (6)$$

101 which leads to the following expression:

$$c_s f_4 \bar{r} \cos \beta - f_2 \frac{1}{\bar{r}} \partial_\theta \bar{P} - f_3 \partial_{\bar{r}} \bar{P} = -\bar{h}^3 \partial_{\bar{r}} \bar{P} \quad (7)$$

102 The non-linear modified Reynolds equation is discretized using a finite
 103 difference scheme and iteratively solved with a successive approximation
 104 method [17]. The field of local clearance (Eq.3) is updated based on the
 105 previously computed local pressure. The iterative procedure is stopped when
 106 the maximum relative error between two successive pressure fields pass below
 107 a convergence threshold of 10^{-4} . After a grid sensitivity analysis was per-
 108 formed on the bearing model, a grid of 100 points in the radial direction and
 109 250 in the circumferential direction was selected, which leads to a satisfying
 110 convergence.

111 Because it limits the wider application of the technology, the static per-
 112 formance is of primary importance in the design of gas thrust bearings. It
 113 appears more relevant than the dynamic behavior in a first study. Therefore,
 114 the performance metrics compare the investigated grooved and smooth lay-
 115 outs are the non-dimensional load capacity \bar{W} and the non-dimensional drag
 116 torque \bar{T} :

$$\bar{W} = \int_{R_i/R_o}^1 \int_0^{\theta_B} (\bar{P} - 1) \bar{r} d\theta d\bar{r} \quad (8)$$

$$\bar{T} = \int_{R_i/R_o}^1 \int_0^{\theta_B} \left(\frac{\alpha \bar{h}_g + (1 - \alpha) \bar{h}_r}{2} \bar{r} \partial_\theta \bar{P} + \frac{\Lambda}{6} \bar{r}^3 \left(\frac{\alpha}{\bar{h}_g} + \frac{1 - \alpha}{\bar{h}_r} \right) \right) d\theta d\bar{r} \quad (9)$$

117 They are linked to their dimensional counterparts as follows:

$$W = P_a R_o^2 \bar{W} \quad (10)$$

$$T = P_a h_0 R_o^2 \bar{T} \quad (11)$$

It is useful to define the load capacity and drag torque of the grooved design normalized by the plain GFTB:

$$\bar{W}_r = \frac{\bar{W}_{grooved}}{\bar{W}_{plain}} \quad (12)$$

$$\bar{T}_r = \frac{\bar{T}_{grooved}}{\bar{T}_{plain}} \quad (13)$$

118 The outputs of the implemented model are compared to the results of Hesh-
 119 mat [1] as a sanity check for $\bar{h}_R = 1$, $\alpha = 1$, $\theta_B = 45^\circ$ and $\theta_R/\theta_B = 0.5$,
 120 $R_o/R_i = 2$, suggesting a good agreement with the experimentally validated
 121 model (Figure 3). The largest relative deviation between the two models
 122 occurs at $\Lambda = 40$ and reaches 1.9%.

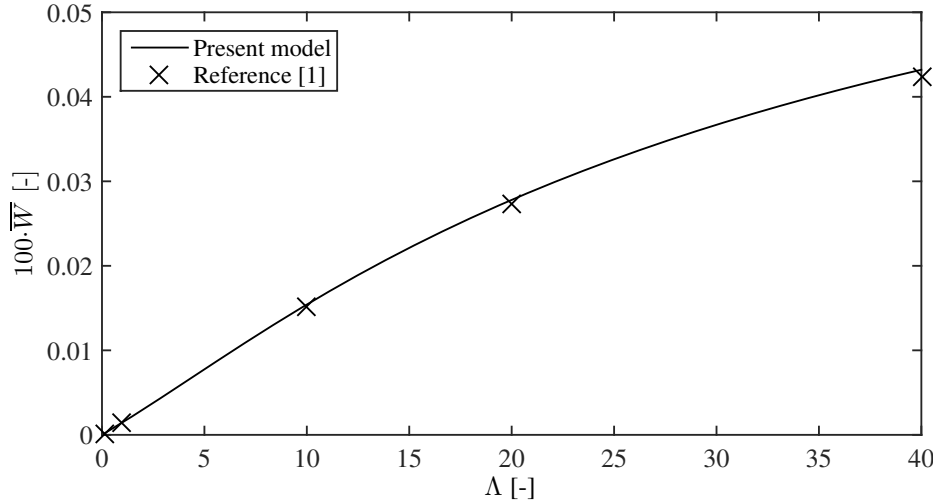


Figure 3: Comparison of the present model with reference [1]

123 3. Numerical computations and results

124 The main geometrical parameters of the studied bearings follow the con-
 125 clusion of Heshmat who identified the layout maximizing the load capacity

126 for GFTB as being $R_o/R_i = 2$, $\theta_B = 45^\circ$ and $\theta_R/\theta_B = 0.5$. The relative
 127 ramp height \bar{h}_R is varied from low values ($\bar{h}_R = 1$) to values in the range
 128 recommended by Heshmat for maximum load capacity ($\bar{h}_R > 10$). Unless
 129 specified differently, the compliance is set to $\alpha_F = 1$ and the eccentricity
 130 ratio ϵ to 0.

131 3.1. Effect of logarithmic grooves on the bearing performance

In order to investigate the effect of grooved top foils on the defined performance indicators and to identify the optimum groove geometries, multi-objective optimizations were performed for different bearing geometries (\bar{h}_R) and operating conditions (Λ) simultaneously maximizing the load capacity and minimizing the drag torque. The decision variables are the 4 geometrical parameters describing the grooved region, namely:

$$\bar{h}_g \in [1, 4] \quad (14)$$

$$\alpha = \frac{a}{a+b} \in [0.3, 0.7] \quad (15)$$

$$\beta \in [0, \pi] \quad (16)$$

$$\gamma = \frac{R_g - R_i}{R_o - R_i} \in [0.1, 0.9] \quad (17)$$

132 The optimizations were performed using a genetic algorithm [18] with 10^4
 133 evaluations to obtain a satisfying convergence. The outputs of the optimization are Pareto fronts representing the optimal trade-offs between load capacity and drag torque. An example is given in Figure 4, for the case $\Lambda = 0.1$ and four different values of \bar{h}_R . The results clearly suggest the existence of regions with a positive effect of the spiral grooves on the drag torque and on the load capacity compared to plain GFTB. Depending on the constraints of a particular design problem, designers may either choose a solution favoring a high load capacity ratio or a low drag torque ratio. The Pareto fronts obtained for large ranges of h_R and Λ are processed to highlight two metrics of practical interest: (1) the maximum value of \bar{W}_r and (2) the value of \bar{T}_r corresponding to the point where $\bar{W}_r = 1$, which corresponds to (1) maximizing gain in load capacity without considering the drag and (2) minimizing the drag torque without losing load capacity compared to the plain GFTB design, respectively.

147 Figure 5 represents the maximum \bar{W}_r as a function of the compressibility
 148 number for various ramp depth ratios and a constant compliance $\alpha_F = 1$.

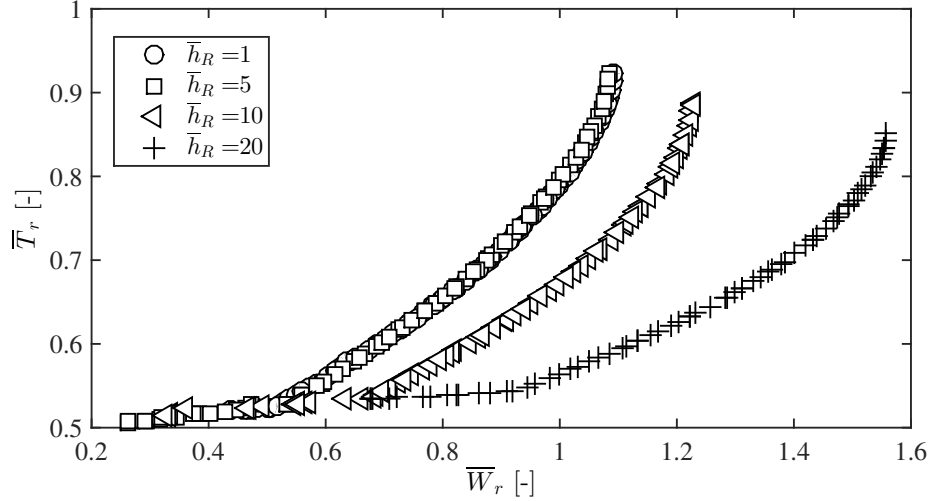


Figure 4: Pareto fronts for $\Lambda = 0.1$ and different ramp depth ratios.

149 There is a strong influence of the relative ramp depth \bar{h}_R on the potential
150 performance gain. Low values exhibit stronger improvements at high values
151 of Λ and inversely for large \bar{h}_R . This behavior can be explained by the absence
152 of a limiting solution for $\Lambda \rightarrow \infty$ for rigid grooved bearings modeled with the
153 NGT [19], which limits the performance of the smooth thrust bearings [20].
154 Ultimately, the results suggest that the maximum \bar{W}_r for grooved thrust
155 bearings is well above 1 for all values of \bar{h}_R . Although not captured by
156 the NGT, a limiting solution does exist at very high compressibility in the
157 case of grooved bearings. However, it is shifted to higher compressibility
158 numbers [19], which maintains the interest of using the NGT even at such
159 high values of Λ . For every investigated value of \bar{h}_R , a minimum in \bar{W}_r
160 is observed at intermediate values of Λ , where the optimal grooved case is
161 close to the performance of a smooth design. The location of this minimum
162 is shifted toward higher compressibility numbers as \bar{h}_R increases. This is
163 a consequence of the limiting solution at high compressibility numbers: a
164 larger value of \bar{h}_R leads to a limiting solution in pressure rise, which becomes
165 more difficult to overcome by the pumping effect of grooves.

166 Figure 6 represents the drag loss ratio \bar{T}_r as a function of the compress-
167 ibility and for various ramp depth ratios at $\bar{W}_r = 1$. The curves show that
168 at equal load capacity, the grooved design can reduce the losses significantly
169 depending on the geometry and the operating conditions. The most promis-

170 ing solutions maximizing the load capacity ratio in Figure 5 are also the most
 171 interesting ones regarding the drag reduction in drag torque in Figure 6. In
 172 these cases, the whole Pareto front happens to be partially or totally shifted
 173 in the domain $\bar{W}_r > 1$, allowing a significant performance in the two met-
 174 rics. Depending on the case, the reduction of drag torque can exceed 40%. In
 175 addition, two optimizations performed at high compressibility numbers (500
 176 and 1000), both with $\bar{h}_R = 1$, only provide Pareto fronts with $\bar{W}_r > 1$. As a
 177 consequence, the point of lowest \bar{W}_r (and therefore lowest \bar{T}_r) was displayed
 and the actual value of the load capacity ratio indicated.

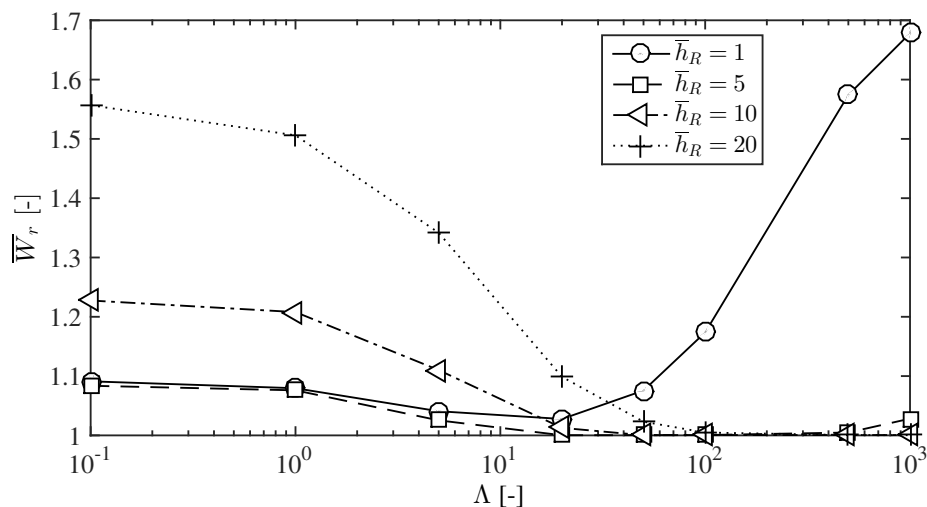


Figure 5: Solutions of maximum \bar{W}_r for a compliance $\alpha_F = 1$

178 The groove parameters of the solutions for maximum load capacity shown
 179 in Figure 5 are displayed in Figure 7. Increasing the value of the ramp depth
 180 \bar{h}_R tends to increase the optimum values of \bar{h}_g and α , and decrease β and
 181 γ . At very high compressibility numbers Λ , the grooves tend to be deeper
 182 and occupy a larger area (higher α and lower γ), in particular for the cases
 183 $\bar{h}_R = 1$ and 5. It is important to note that for some cases the optimal
 184 design yield $\bar{h}_g = 1$, which corresponds to a plain design, where the other
 185 parameter have no influence on the bearing performance, thus explaining
 186 their swinging values for these particular cases. The optimal groove geometry
 187 does not evolve significantly for $\Lambda < 10$, which is a indicator for good off-
 188 design performance, as it will be shown below.

189 The points corresponding to $\Lambda = 5$ in Figure 5 have their pressure field

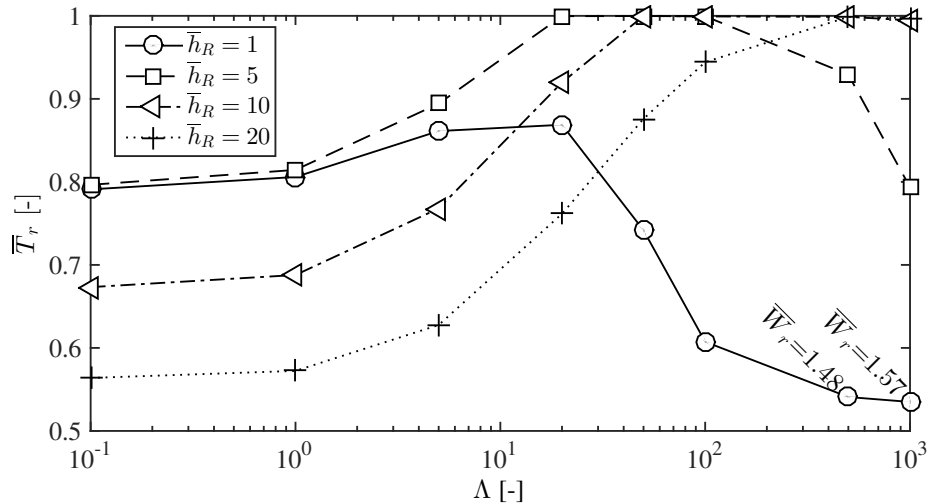


Figure 6: Values of \bar{T}_r for solutions with $\bar{W}_r = 1$ for a compliance $\alpha_F = 1$

191 represented in Figures 8 and 9. The pressure gradient in t is much stronger
 192 along the radial direction in the grooved zone for $\bar{r}_g < \bar{r} < 1$ than in the
 193 smooth zone, because of the pumping action of the grooved pattern. As the
 194 relative ramp depth increases, the zone of maximum pressure shifts from the
 195 center of the bearing toward the plateau, with a zone of maximum pressure
 196 bordered by the groove zone. In the ramp zone, the grooves tend to loose
 197 their pumping effect and become locally ineffective at building pressure or
 198 acting as a radial seal.

199 Since the presented results correspond to cases with a compliance $\alpha_F = 1$,
 200 the influence of this choice on the results is investigated. Figure 10 shows
 201 the influence of the foil compliance on the maximum load capacity ratio at
 202 a high compressibility number, resulting from an optimization performed at
 203 discrete values of α_F . Because of the low pressure build-up in the bearing at
 204 low values of Λ , the compliance has little effect on the performance metric
 205 because the resulting deflection of the top foil is not significant. \bar{W}_r exhibits
 206 a minimum at $\alpha_F \approx 0.35$ and increases approximately linearly at high compli-
 207 ance. However, the relative variation of \bar{W}_r over the considered domain is
 208 low. It is therefore suggested that the compliance has little influence on the
 209 potential of the GFSTB over the plain GFTB.

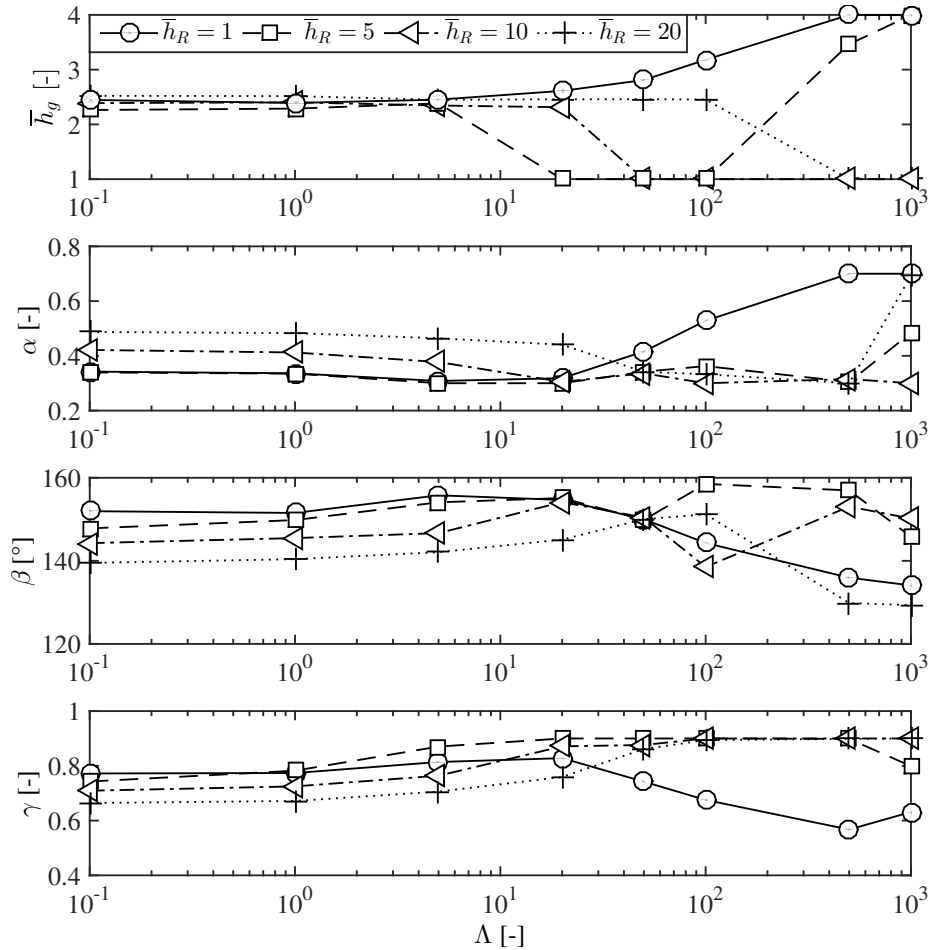


Figure 7: Groove parameters corresponding to solutions in Figure 5

210 *3.2. Off-design operation*

211 Figure 11 represents the off-design performance in terms of compressibil-
 212 ity number of two geometries with $\bar{h}_R = 20$ maximizing \bar{W}_r at $\Lambda = 0.1$ and
 213 50 respectively, for a compliance $\alpha_F = 1$. Since the optimal groove geometry
 214 does not evolve much for the case $\Lambda = 0.1$, the performance remains close
 215 to the optimum at low compressibility number, until $\Lambda \approx 20$. \bar{W}_r drops be-
 216 low 1 for higher compressibility numbers. The design optimized for $\Lambda = 50$
 217 maintains its performance close to 1 at high values of Λ with an appreciable
 218 gain at low compressibility, although it performs significantly lower than the
 219 local optimal geometry.

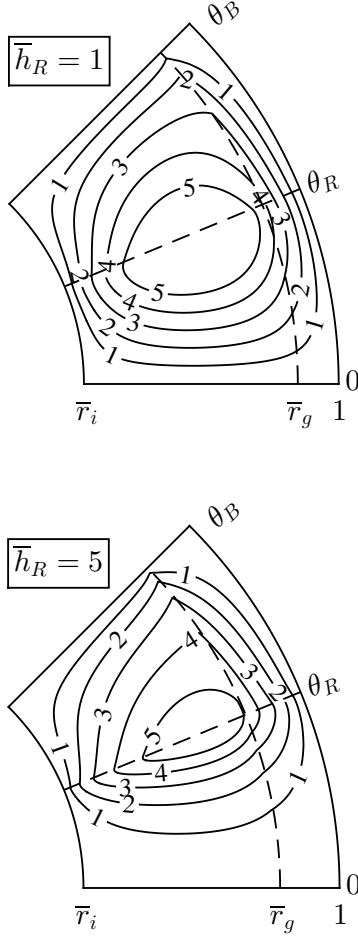


Figure 8: Contour of $100 \cdot (\bar{P} - 1)$ for the geometries maximizing the load capacity at $\Lambda = 5$ and ramp depth $\bar{h}_R = 1$ and 5

220 Figures 12 and 13 extend this analysis with \bar{h}_R as a second variable, ex-
 221 ploring the performance of the geometry optimized for $\Lambda = 0.1$ and $\Lambda = 50$
 222 respectively, with $\bar{h}_R = 20$. The domain of interest with $\bar{W}_r > 1$ is nar-
 223 rowed further in Λ as \bar{h}_R departs from the design value. A local minimum
 224 in \bar{W}_r is visible, however with a reduction of less than 15% compared to
 225 the design value. The performance increases sharply for low operating \bar{h}_R at

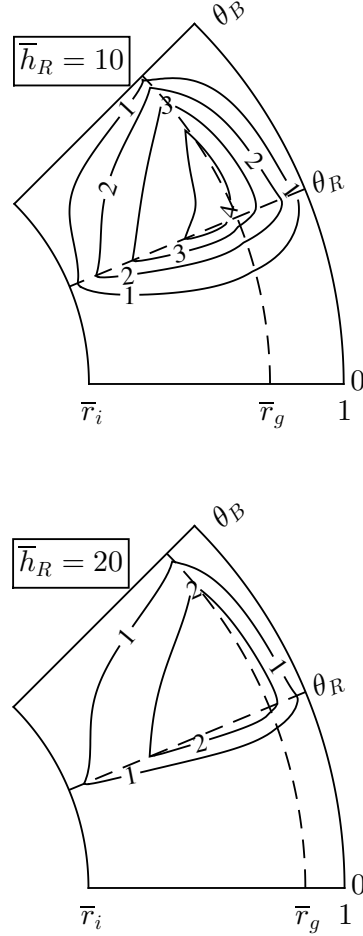


Figure 9: Contour of $100 \cdot (\bar{P} - 1)$ for the geometries maximizing the load capacity at $\Lambda = 5$ and ramp depth $\bar{h}_R = 10$ and 20

226 high compressibility, which corroborates with the results in Figure 5. It is
 227 important to note that for a given off-design value of \bar{h}_R , the performance
 228 passes through a minimum before increasing again. It supports the men-
 229 tioned conjecture that an optimal groove design with $\bar{W}_r > 1$ exists at very
 230 high values of compressibility number Λ for any value of ramp depth ratio
 231 \bar{h}_R , as long as the local incompressibility assumption of the NGT is verified

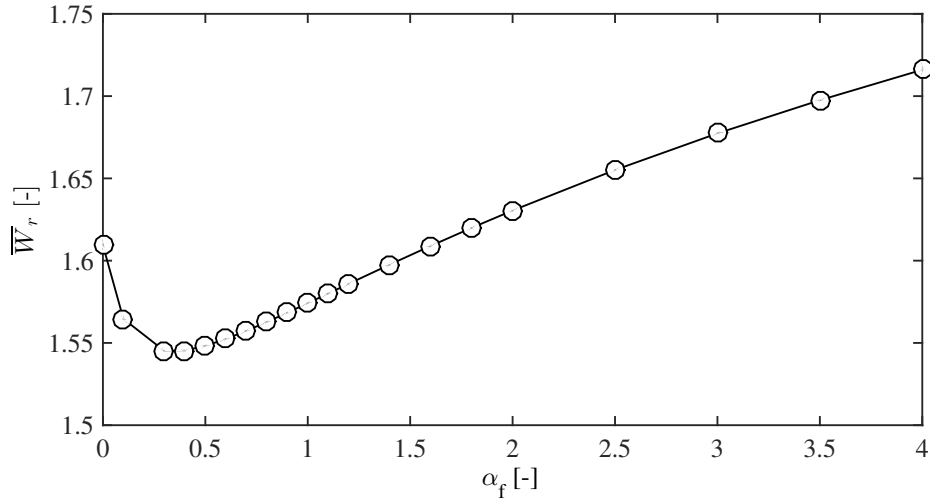


Figure 10: Evolution of the load capacity ratio against the bearing compliance at $\Lambda = 500$ and $\bar{h}_R = 1$

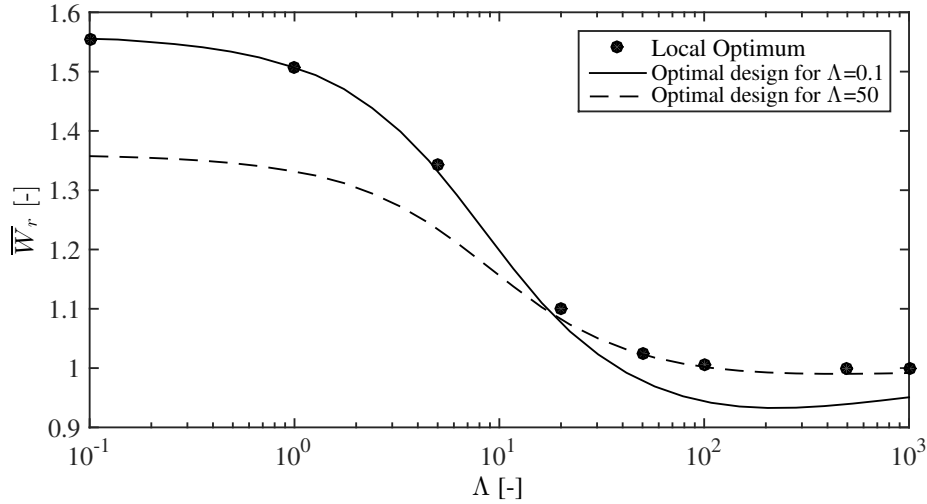


Figure 11: Off-design performance ($\bar{h}_R = 20$) in terms of \bar{W}_r of geometries optimized for $\Lambda = 0.1$ and 50

232 [19]. A qualitatively similar observation can be made for the performance
 233 along the variable \bar{h}_R at constant Λ . In both investigated cases, \bar{W}_r passes
 234 through a minimum at $\bar{h}_R \approx 2$ for $\Lambda < 10$. The value of relative ramp height
 235 associated with this minimum increases at higher compressibility numbers.
 236 Note that cases close to $\bar{h}_R = 0$ represent two parallel surfaces, which are

237 unable to build-up pressure if grooves are absent. Therefore, \overline{W}_r becomes
 238 asymptotically large in these cases.

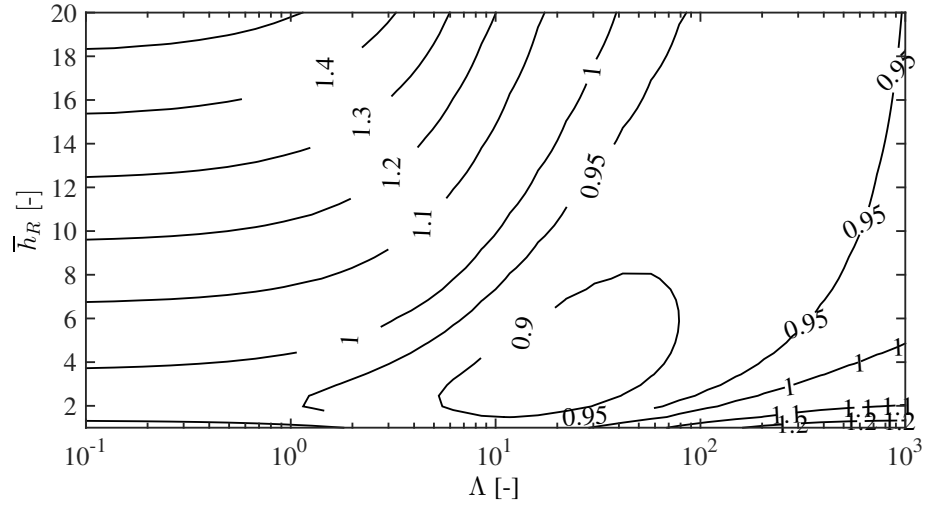


Figure 12: Off-design performance in terms of \overline{W}_r of the geometry optimized for $\Lambda = 0.1$ and $\overline{h}_R = 20$

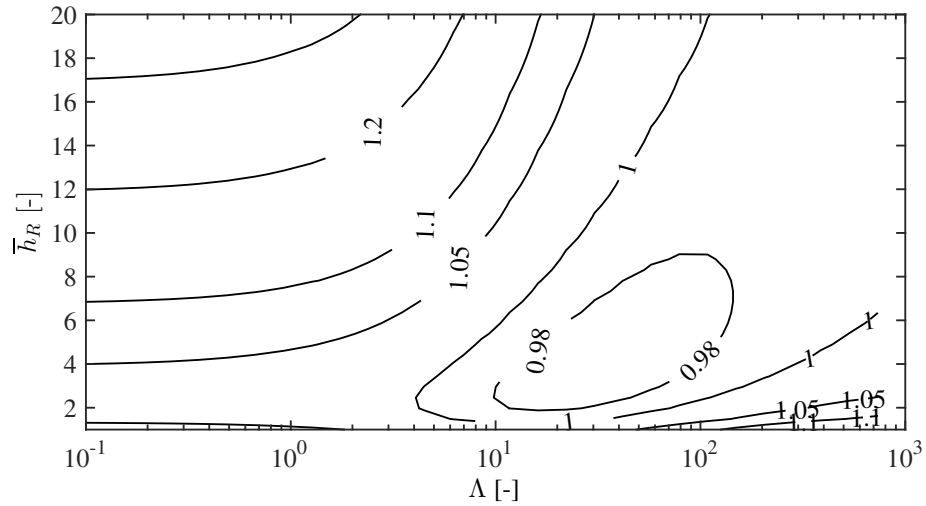


Figure 13: Off-design performance in terms of \overline{W}_r of the geometry optimized for $\Lambda = 50$ and $\overline{h}_R = 20$

239 The evolution of \overline{W}_r with the eccentricity ratio ϵ is shown in Figure 14.
 240 The geometry of the four represented cases maximizes \overline{W}_r at $\epsilon = 0$ and a

241 nominal compliance $\alpha_F = 1$ evaluated at zero eccentricity. Note that for ob-
 242 taining these results the stiffness of the elastic foundation is kept constant,
 243 which, according to Eq.4, leads to a compliance that evolves with eccentricity.
 244 All grooved geometries show an improved load capacity in nominal conditions
 245 but exhibit a lower performance than the plain GFTB design at high eccen-
 246 tricity ratios, with a loss of nearly 25%. \bar{W}_r reaches a local maximum a high
 247 values of \bar{h}_R , which is not present for $\bar{h}_R=1$, where it decreases steadily with
 248 an increasing eccentricity ratio. Theses results suggest that GFSTB do not
 249 provide a higher ultimate load capacity compared to the plain design. They
 250 allow though, to achieve higher load capacities at moderate eccentricities,
 251 which can be beneficial for the thermal management.

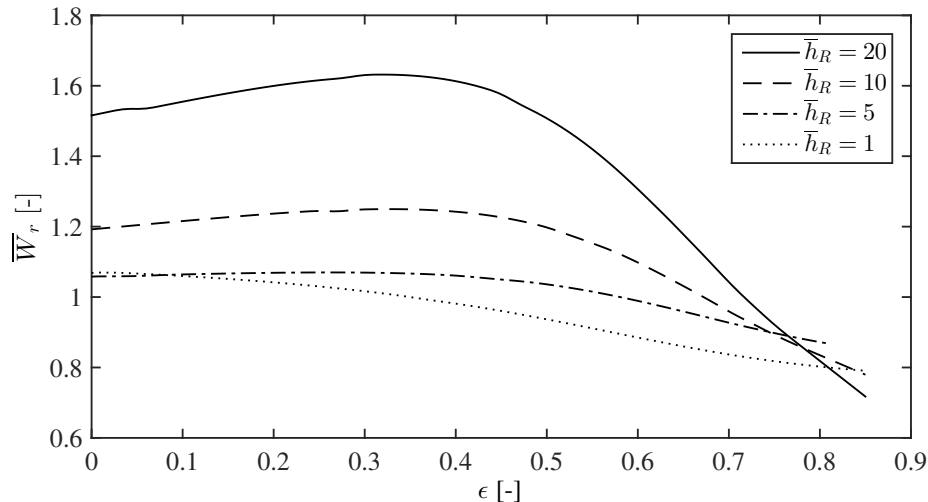


Figure 14: Off-design performance in terms of \bar{W}_r of the geometry optimized for $\Lambda = 1$

252 4. Conclusions

253 Based on Heshmat's work [1], a model of gas foil thrust bearing enhanced
 254 with logarithmic spiral grooves is developed using the Narrow Groove Theory.
 255 The improvement potential is evaluated in terms of load capacity and drag
 256 torque for a large range of compressibility numbers, relative ramp depth
 257 and bearing compliance. A multi-objective optimization for identifying the
 258 optimal groove geometries to maximize the load capacity while minimizing
 259 the drag torque leads to the following observations:

- 260 • The improvement potential of a grooved bearing compared to a plain
261 one is the highest at low compressibility numbers and large relative
262 ramp depth or inversely at high compressibility numbers and low ramp
263 depths.
- 264 • Optimum groove geometries allow to improve the load capacity by
265 nearly 70%.
- 266 • Optimum groove geometries allow to decrease the drag torque (losses)
267 of the thrust bearing by up to 40% compared to a plain Gas Foil Thrust
268 Bearing, in cases where the specific load capacity between the two
269 bearing types is the same.
- 270 • An assessment on off-design operation suggests that groove geometries
271 optimized for low compressibility numbers negatively impact the load
272 capacity at higher values (i.e. higher rotor speed and smaller clear-
273 ance). However, a design optimized for high compressibility numbers
274 still present a significant gain at lower compressibility numbers com-
275 pared to plain gas foil thrust bearing.
- 276 • The presence of grooves negatively impacts the ultimate load capacity
277 of the thrust bearings compared to the plain GFTB.

278 It follows that the addition of spiral grooves on the GFTB's top foil can be an
279 interesting solution to improve the load capacity and/or relieve the thermal
280 management of plain gas foil thrust bearings. Due to the simplicity of the
281 added manufacturing step, the proposed bearing layout is applicable to both
282 new and commissioned bearings (retrofit).

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350 **AppendixA. NGT**

351 The terms composing equation 1 are developed here.

$$\bar{h}_r = \frac{h_r}{h_0} = \frac{h_r}{h_r(\theta_R < \theta < \theta_B)} \quad (\text{A.1})$$

$$\bar{h}_g = \frac{h_g}{h_0} \quad (\text{A.2})$$

$$\bar{\delta} = \frac{h_g - h_r}{h_0} \quad (\text{A.3})$$

$$g_1 = \bar{h}_g^3 \bar{h}_r^3 \quad (\text{A.4})$$

$$g_2 = (\bar{h}_g^3 - \bar{h}_r^3)^2 \alpha (1 - \alpha) \quad (\text{A.5})$$

$$g_3 = (1 - \alpha) \bar{h}_g^3 + \alpha \bar{h}_r^3 \quad (\text{A.6})$$

$$c_s = \frac{6\mu\omega R^2}{p_a h_0^2} \alpha (1 - \alpha) \bar{\delta} \sin \hat{\beta} \quad (\text{A.7})$$

$$f_1 = \frac{g_1 + g_2 \sin^2 \hat{\beta}}{g_3} \quad (\text{A.8})$$

$$f_2 = \frac{g_2 \sin \hat{\beta} \cos \hat{\beta}}{g_3} \quad (\text{A.9})$$

$$f_3 = \frac{g_1 + g_2 \cos^2 \hat{\beta}}{g_3} \quad (\text{A.10})$$

$$f_4 = \frac{\bar{h}_g^3 - \bar{h}_r^3}{g_3} \quad (\text{A.11})$$

$$f_5 = \alpha \bar{h}_g + (1 - \alpha) \bar{h}_r \quad (\text{A.12})$$