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# New insights on scrape-off layer plasma turbulence

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What are the properties of SOL plasma and how can we simulate it?

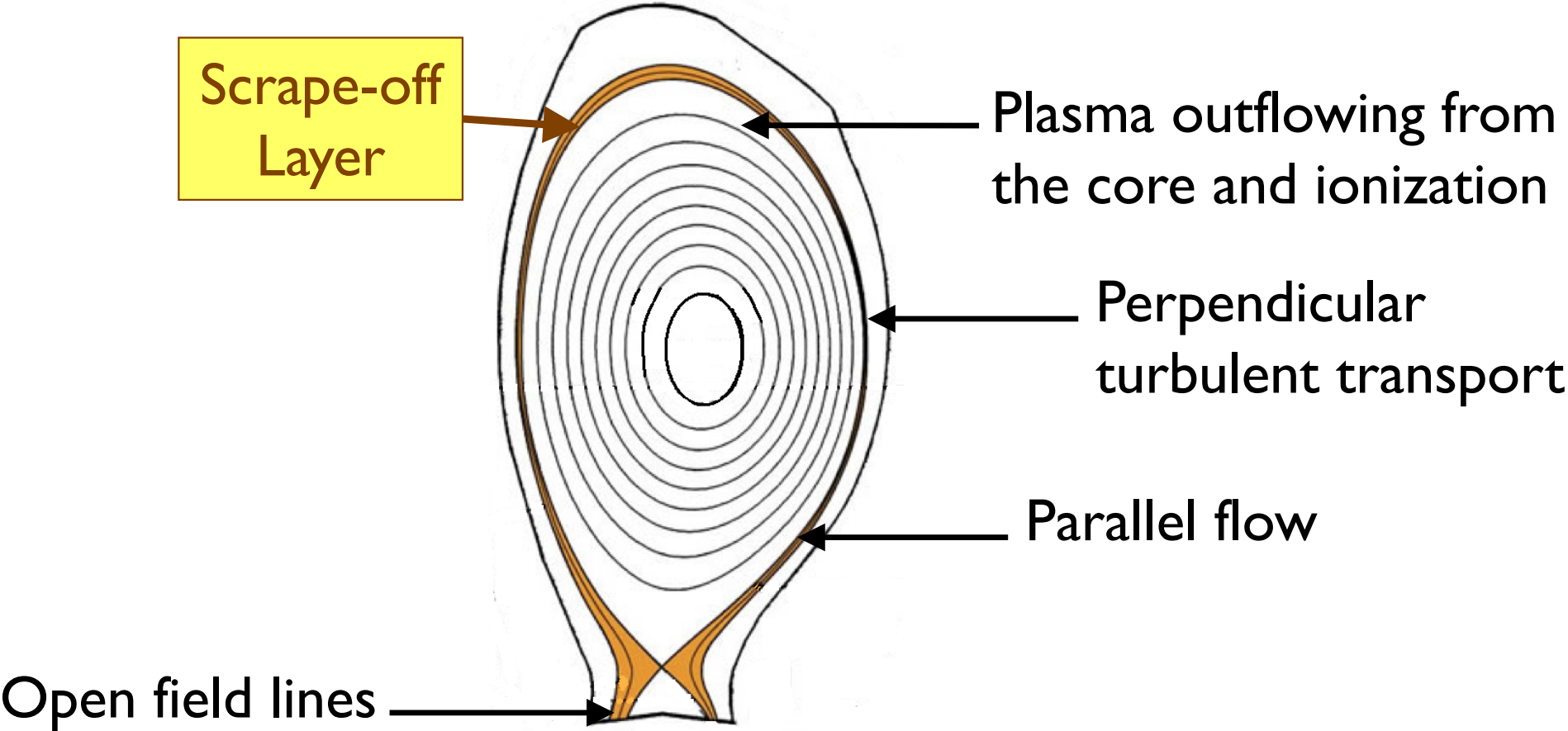
Mechanisms setting the SOL width? ES potential? Toroidal rotation?

How do our simulations compare with experiments?

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# SOL channels particles and heat to the wall

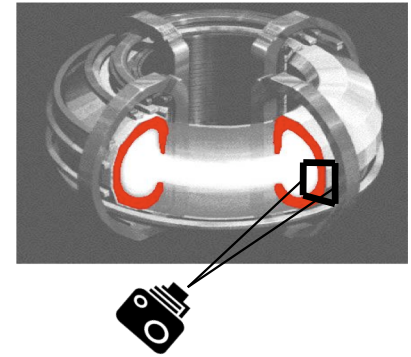
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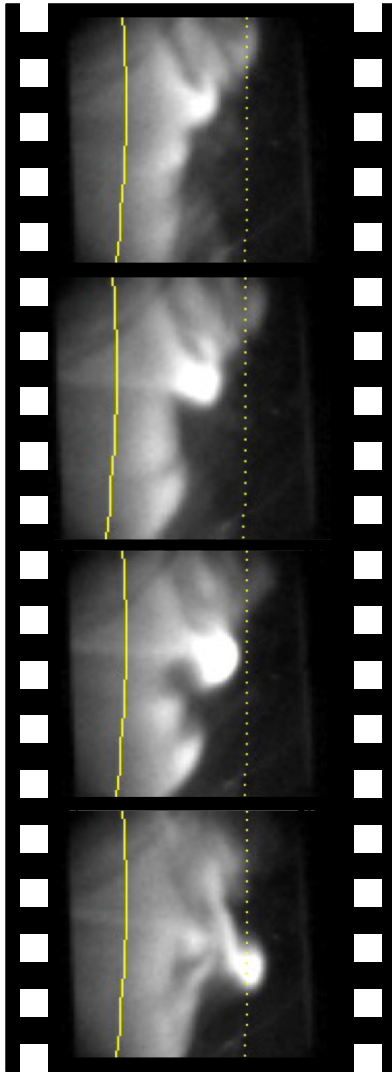


# SOL plasma properties

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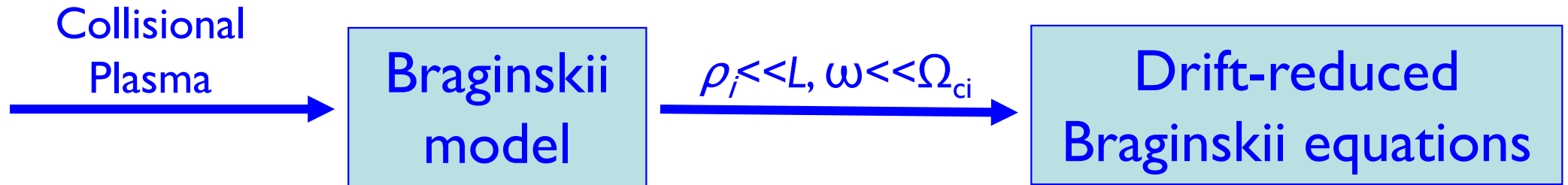


Courtesy of R. Maqueda, typical L-mode SOL



- $n_{fluc} \sim n_{eq}$
- $L_{fluc} \sim L_{eq}$
- Fairly cold ( $< 100$  eV,  $n_e \sim 10^{19} \text{ m}^{-3}$ ) magnetized plasma
- Role of neutrals
- Sheath physics

# A model to evolve plasma turbulence in the SOL



$$\frac{\partial n}{\partial t} + \underbrace{[\phi, n]}_{\substack{\text{E} \times \text{B} \\ \text{CONVECTION}}} = \underbrace{\hat{C}(nT_e) - n\hat{C}(\phi)}_{\text{MAGNETIC CURVATURE}} - \underbrace{\nabla_{\parallel}(nV_{\parallel e})}_{\substack{\text{PARALLEL} \\ \text{DYNAMICS}}} + \underbrace{n_n\nu_{\text{ion}}}_{\text{IONIZATION}} - \underbrace{n\nu_{\text{rec}}}_{\text{RECOMBINATION}} + \underbrace{S_n}_{\substack{\text{OUTFLOW} \\ \text{FROM CORE}}}$$

$T_e, T_i, \Omega$  (vorticity) → similar equations

$V_{\parallel e}, V_{\parallel i}$  → parallel momentum balance

$$\nabla \cdot (n \nabla_{\perp} \phi) = \Omega - \tau \nabla_{\perp}^2 p_i$$

$$\nabla_{\perp}^2 \psi = j_{\parallel}$$

# A model to evolve plasma turbulence in the SOL

+ coupling with neutrals

$$\frac{\partial f_n}{\partial t} + \mathbf{v} \cdot \frac{\partial f_n}{\partial \mathbf{x}} = -\nu_{\text{ion}} f_n - \nu_{\text{CX}} (f_n - n_n f_i / n_i) + \nu_{\text{rec}} f_i$$

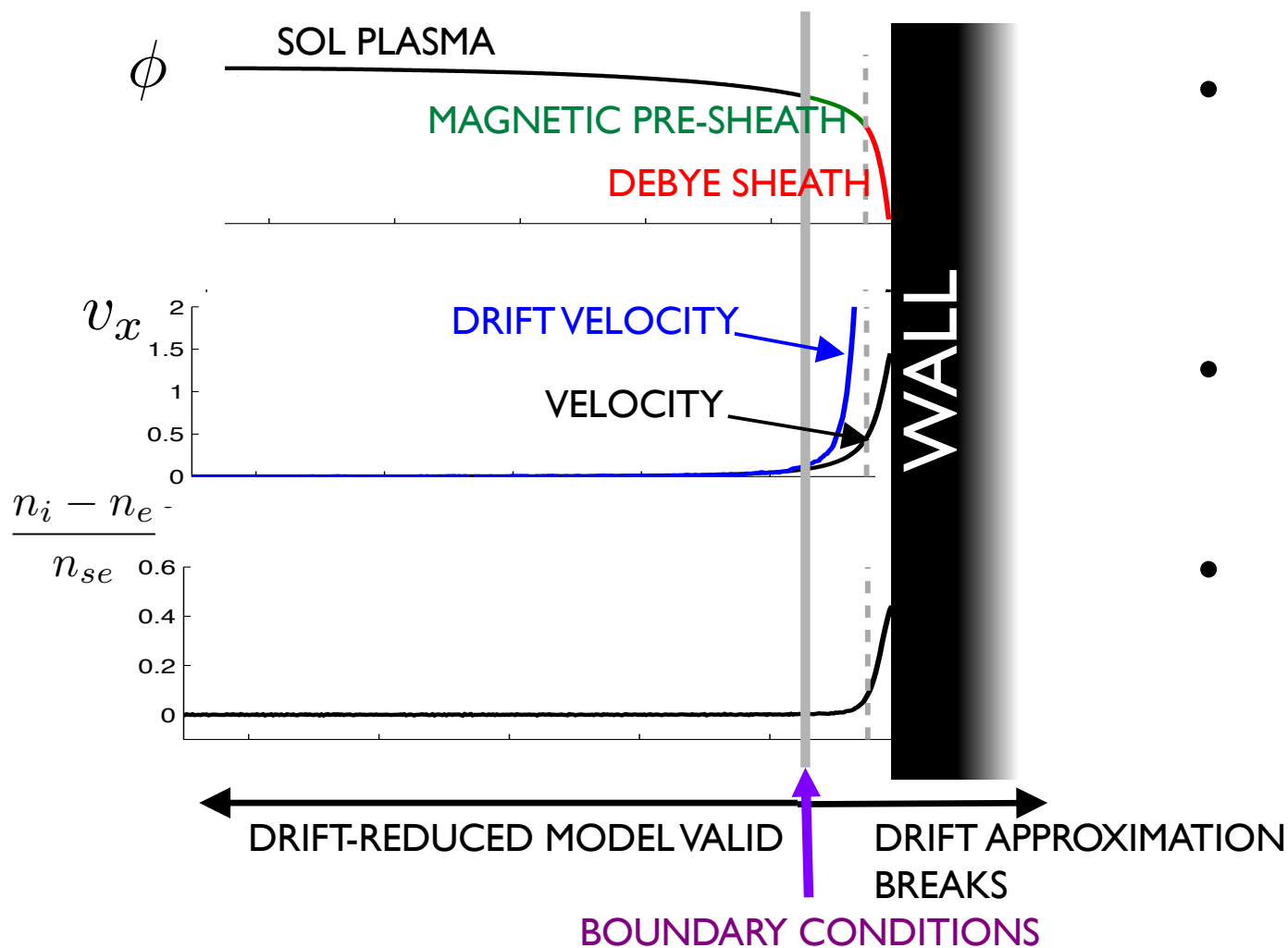
STREAMING      IONIZATION      CHARGE EXCHANGE      RECOMBINATION

$\nu_{\text{ion}} = n \langle v_e \sigma_{\text{ion}} \rangle$        $\nu_{\text{CX}} = n \langle v_{\text{rel}} \sigma_{\text{CX}}(v_{\text{rel}}) \rangle$        $\nu_{\text{rec}} = n \langle v_e \sigma_{\text{rec}} \rangle$

Wersal & Ricci, NF 2015

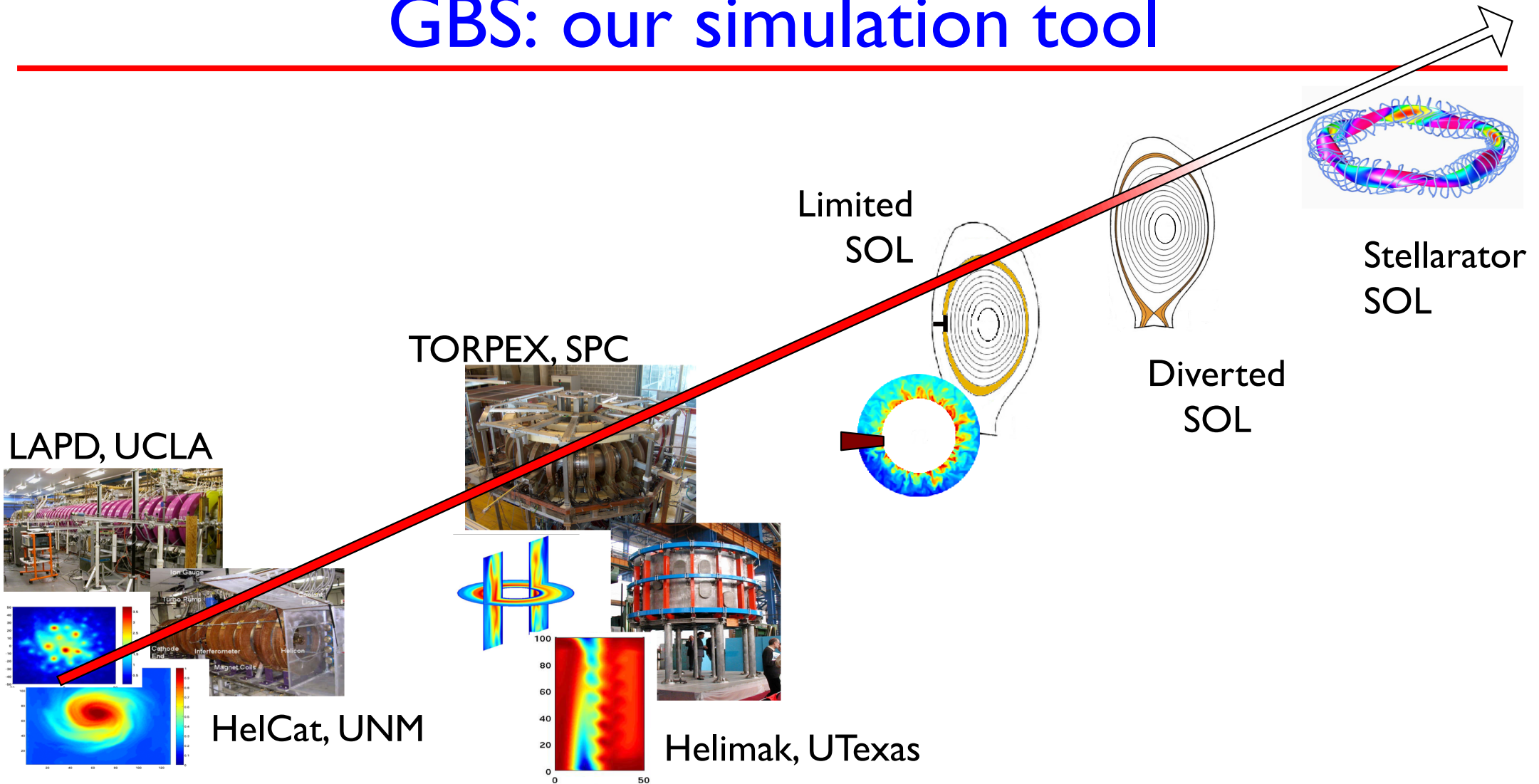
We solve in 3D geometry, taking into account plasma outflow from the core, turbulent transport, ionization and charge exchange processes, and losses at the vessel

# Boundary conditions at the plasma-wall interface



- Set of b.c. for all quantities, generalizing Bohm-Chodura
- Checked agreement with PIC kinetic simulations
- Neutrals: reflection and re-emission with cosine distribution

# GBS: our simulation tool



Ricci et al., PPCF 2012; Halpern et al., JCP 2016

# How do you make sure there are no bugs in your code?

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- 1) Simple tests
  - 2) Code-to-code comparisons (benchmarking)
  - 3) Discretization error quantification
  - 4) Convergence tests
  - 5) Order-of-accuracy tests
- NOT SUFFICIENT
- RIGOROUS,  
requires  
analytical  
solution

Only verification ensuring  
convergence and correct  
numerical implementation

# Order-of-accuracy tests, method of manufactured solution

Our model:  $A(f) = 0$ ,  $f$  unknown  
We solve  $A_n(f_n) = 0$ , but  $\epsilon_n = f_n - f = ?$

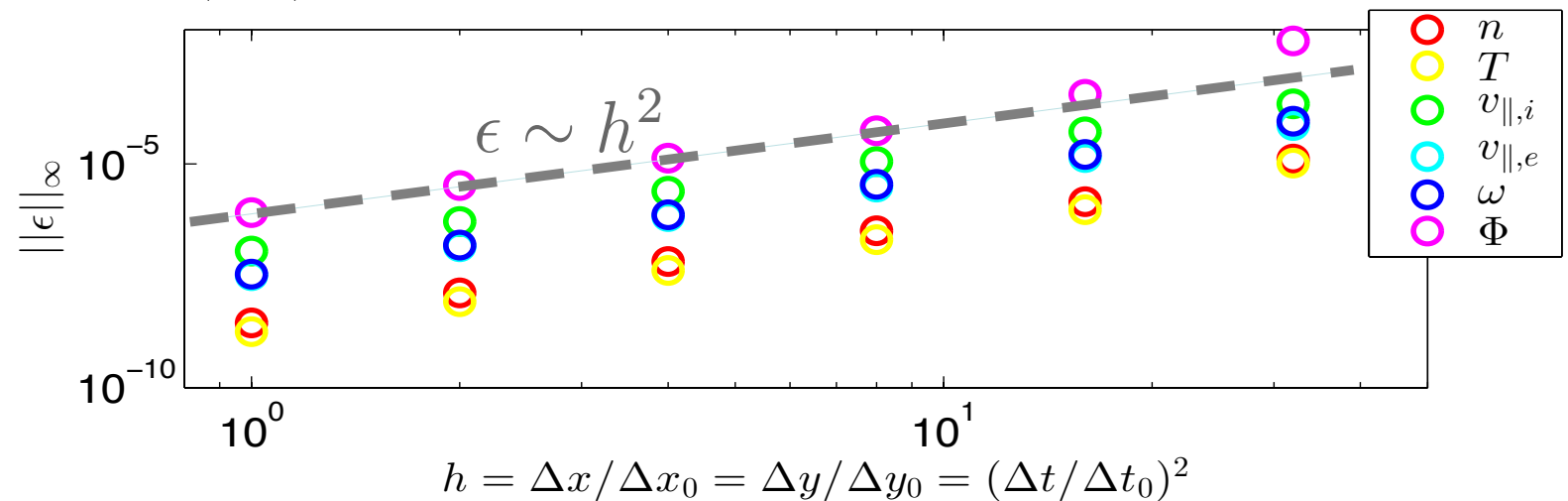
## Method of manufactured solution:

1) we choose  $g$ , then  $S = A(g)$

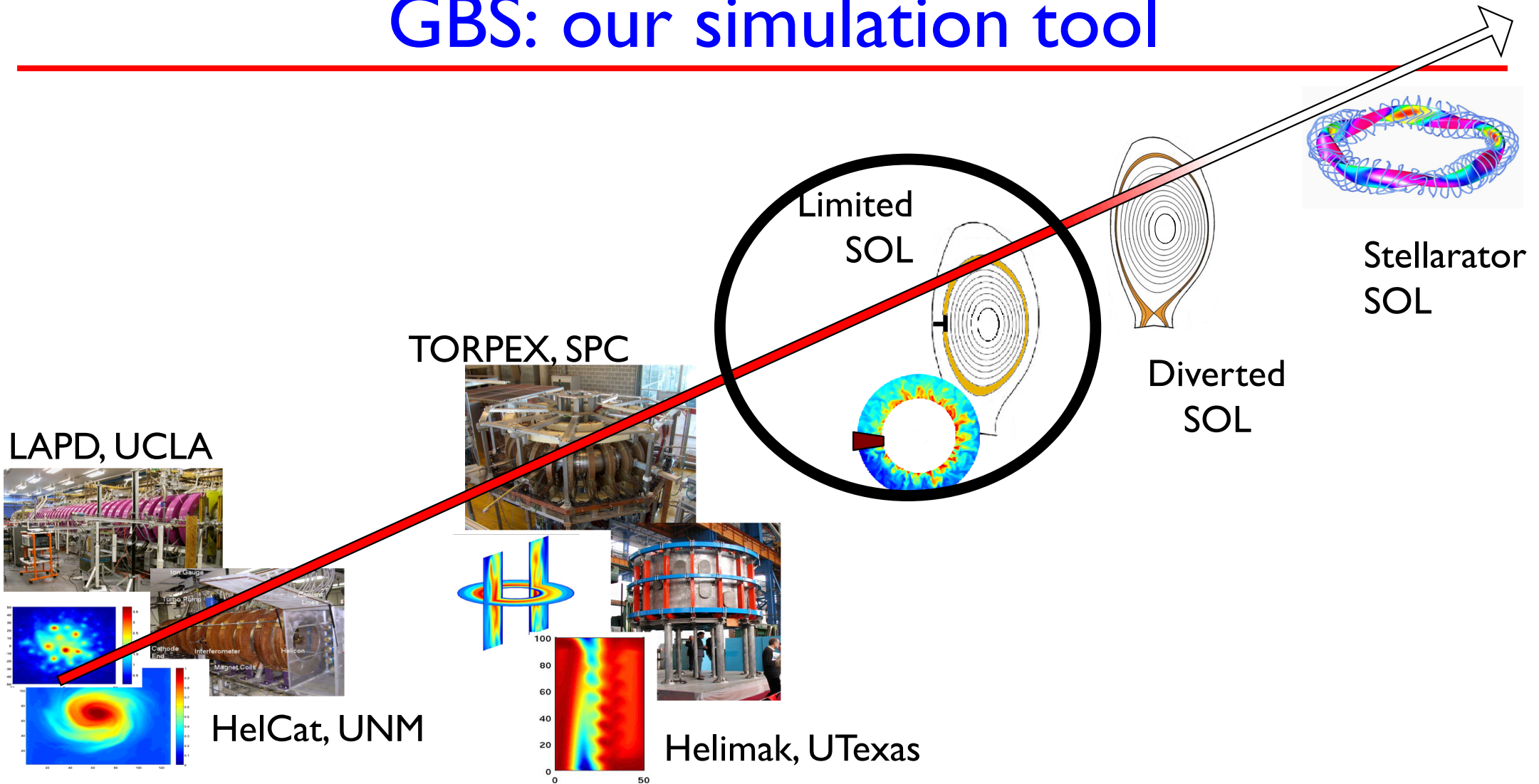
2) we solve:  $A_n(g_n) - S = 0$

$$\epsilon_n = g_n - g$$

For GBS:



# GBS: our simulation tool

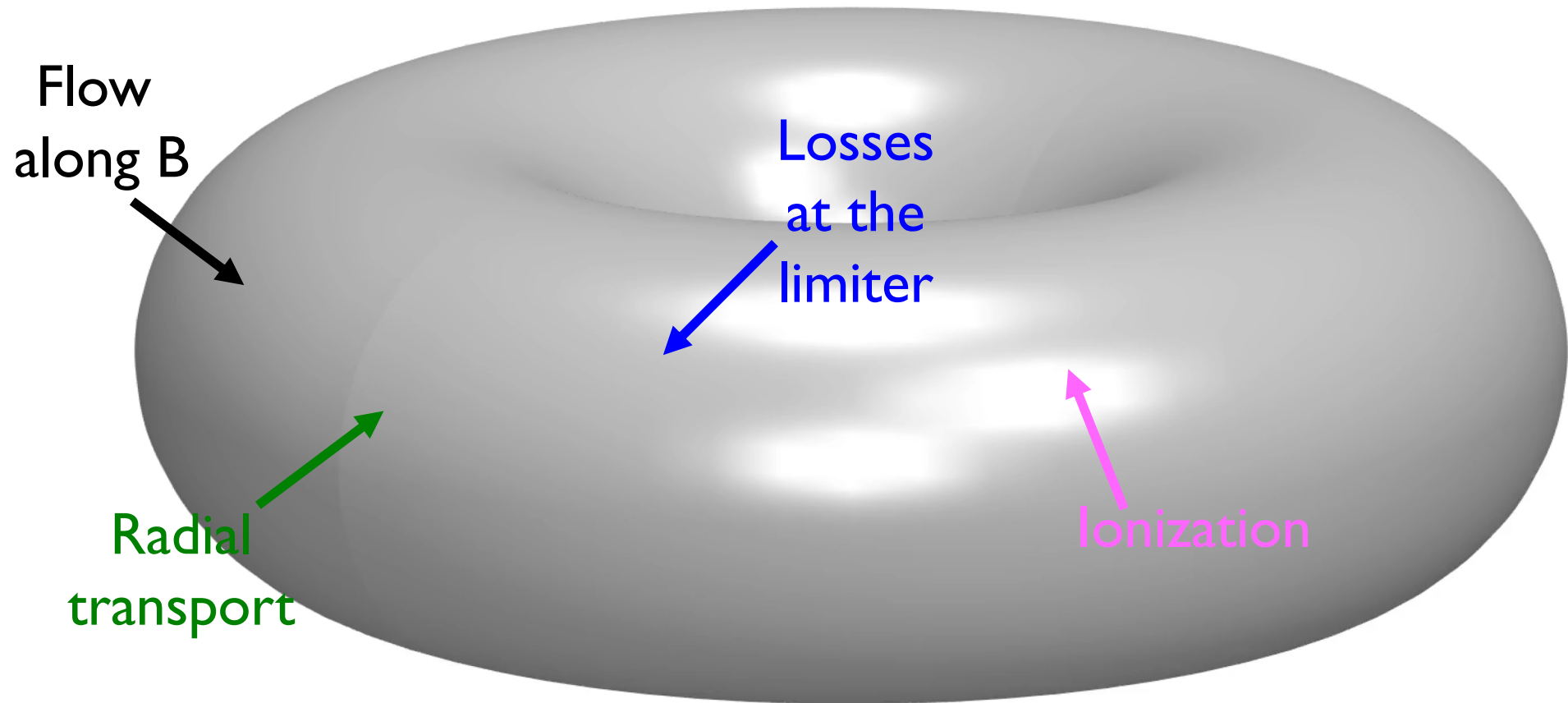


Ricci et al., PPCF 2012; Halpern et al., JCP 2016



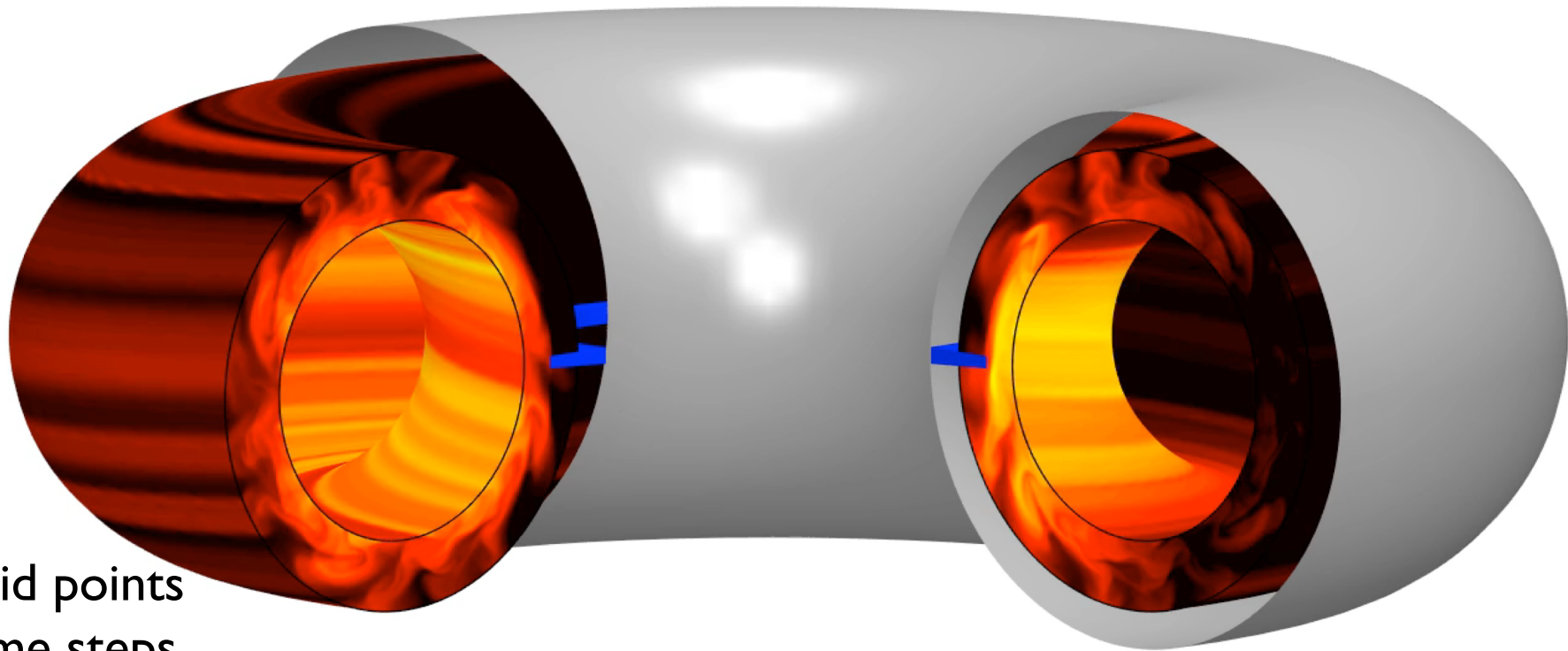
# GBS evolves plasma and neutrals self-consistently

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# GBS evolves plasma and neutrals self-consistently

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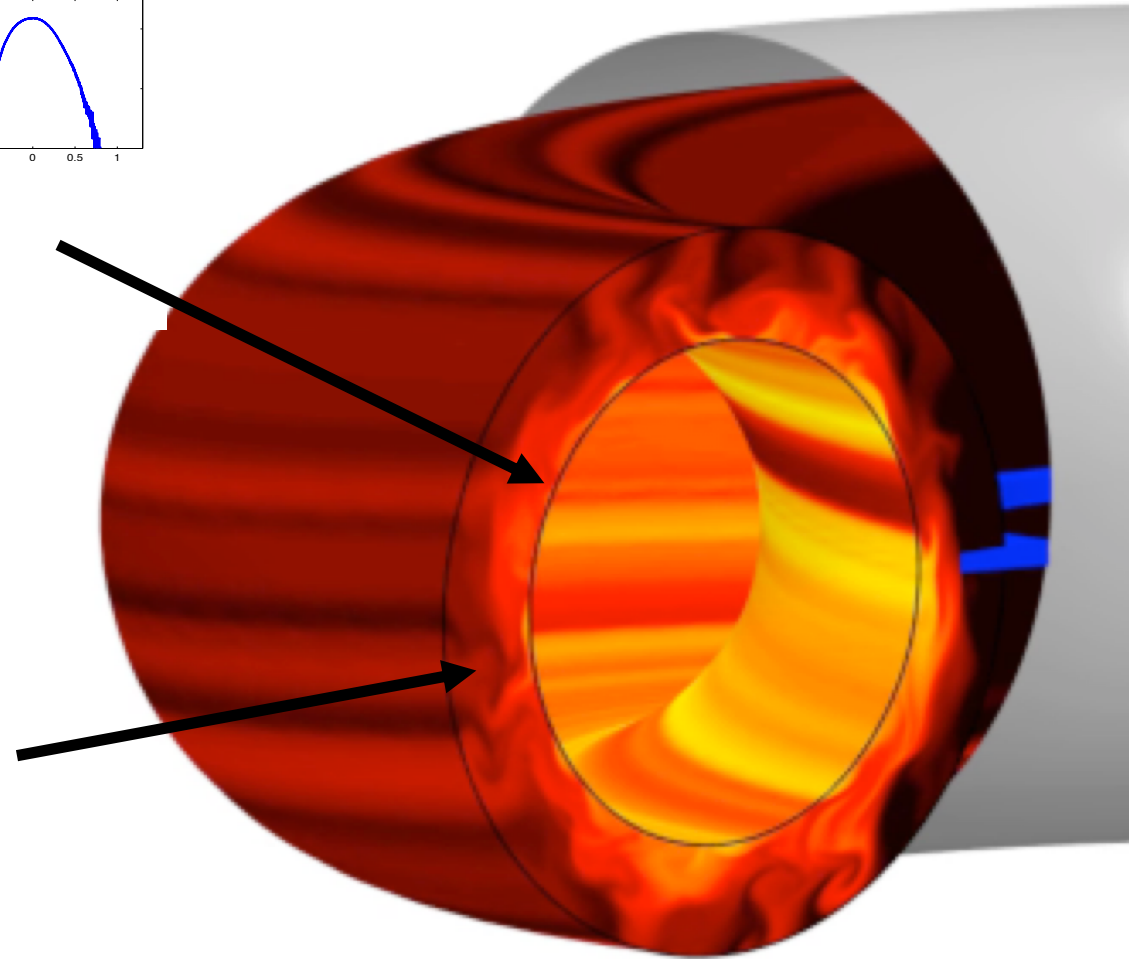
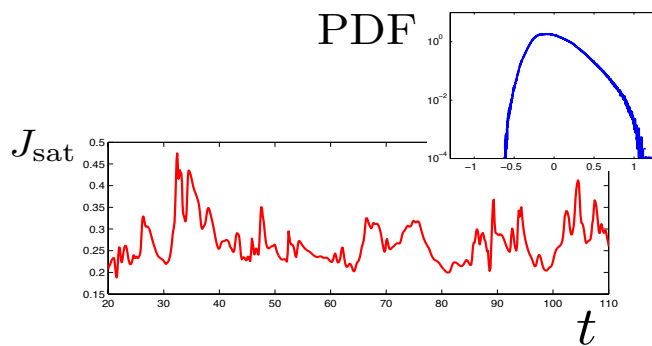
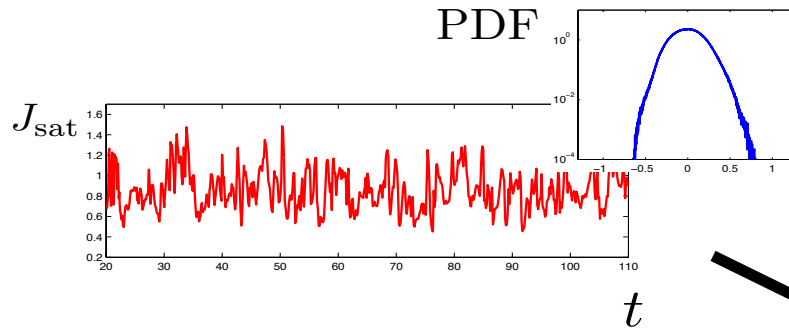
$\log(p_e)$

$\log(S_{iz})$

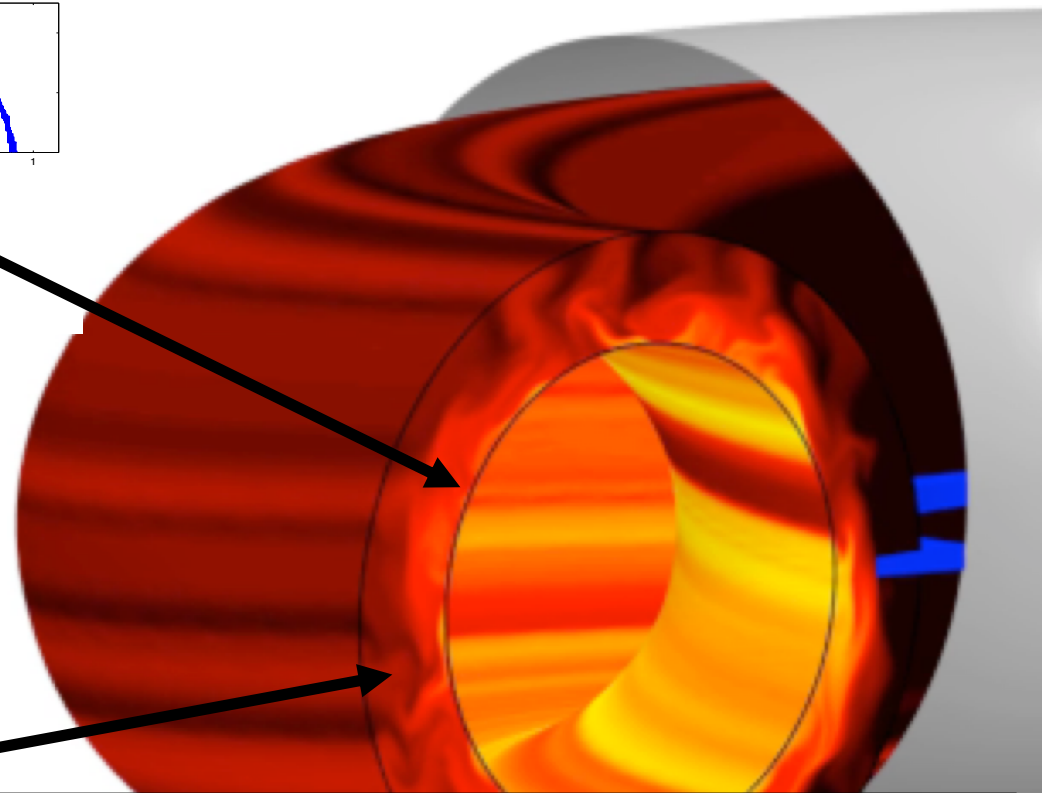
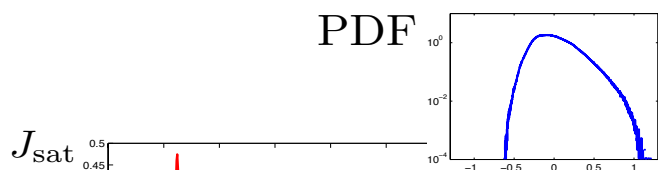
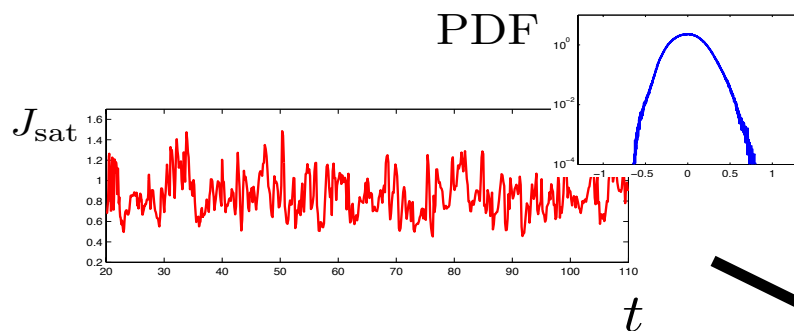
- $10^7$  grid points
- $10^6$  time steps
- $10^4$  CPUs
- $10^5$  CPU hours

# Main experimental features retrieved

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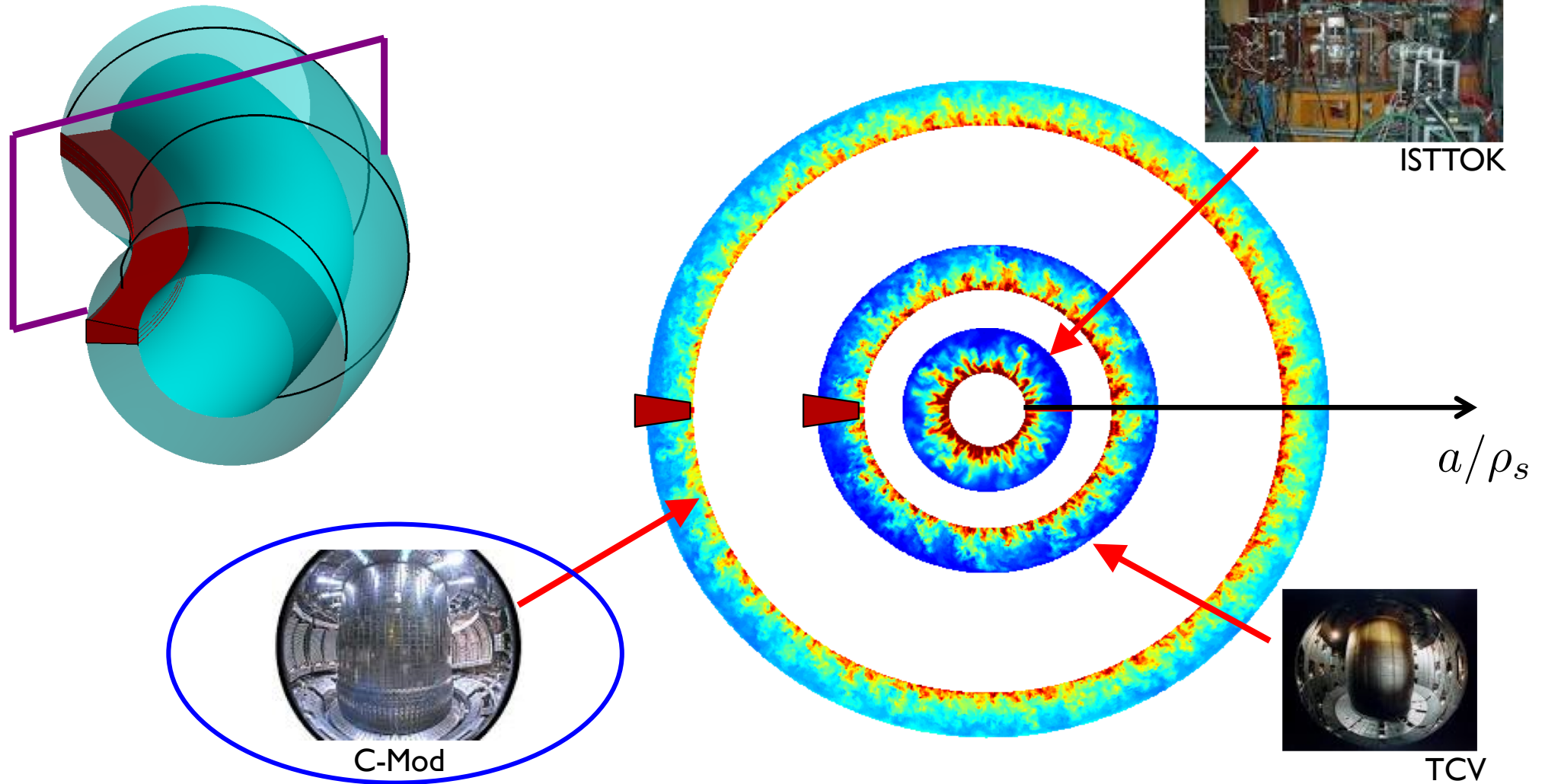


# Main experimental features retrieved

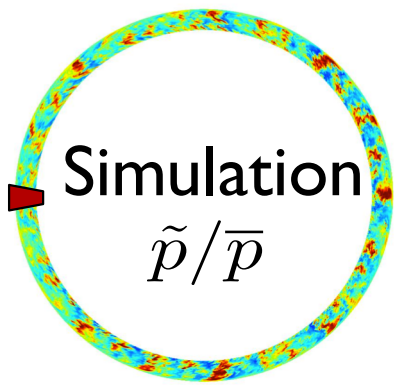
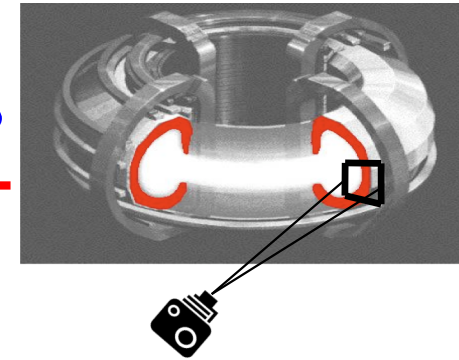


Simulations contain physics of ballooning modes, drift waves, Kelvin-Helmholtz, blobs, parallel flows, sheath losses...

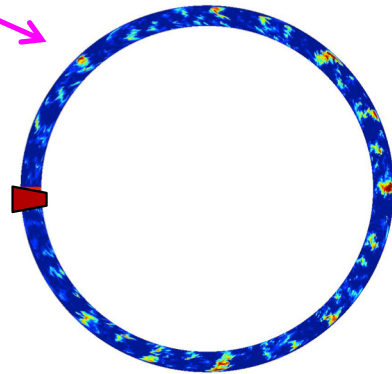
# A large validation effort



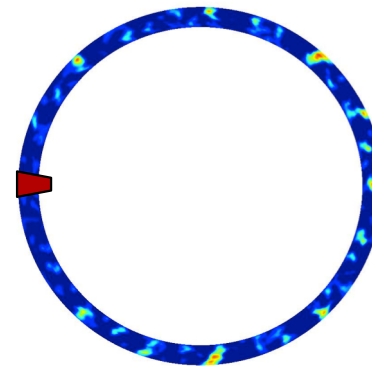
# Gas puff imaging diagnostics



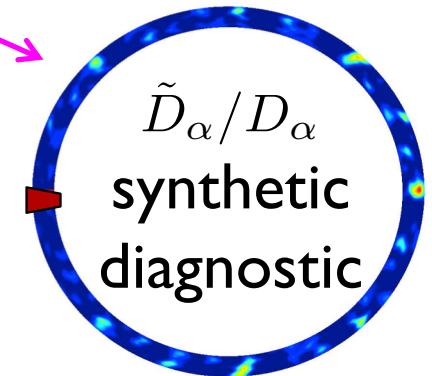
Emission



Photodiode

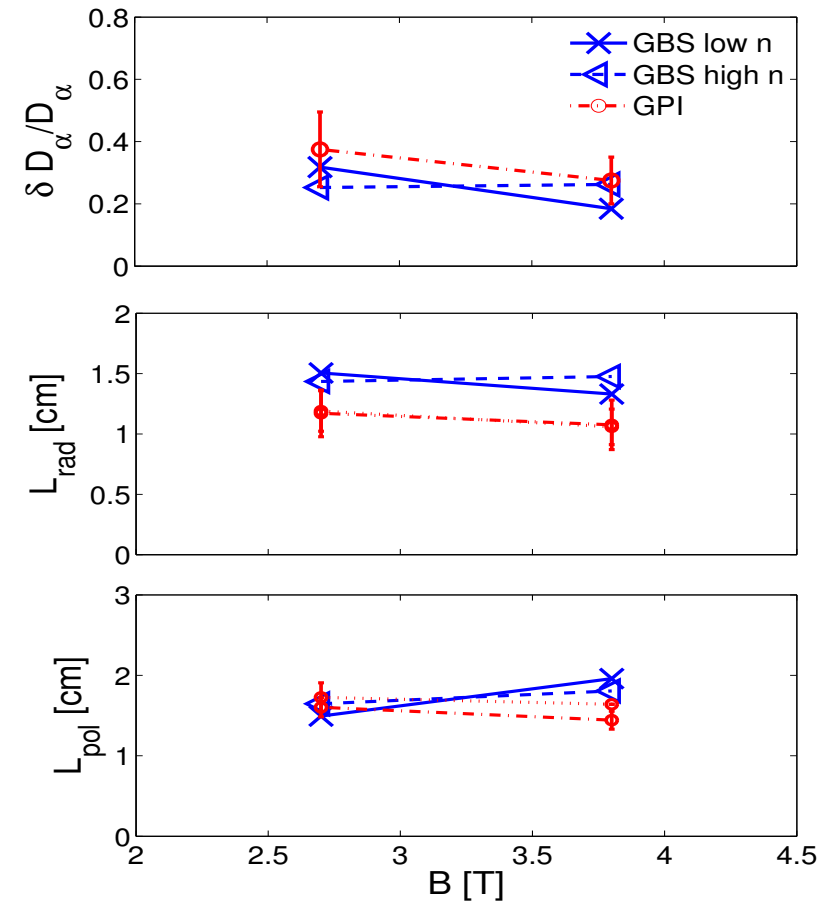
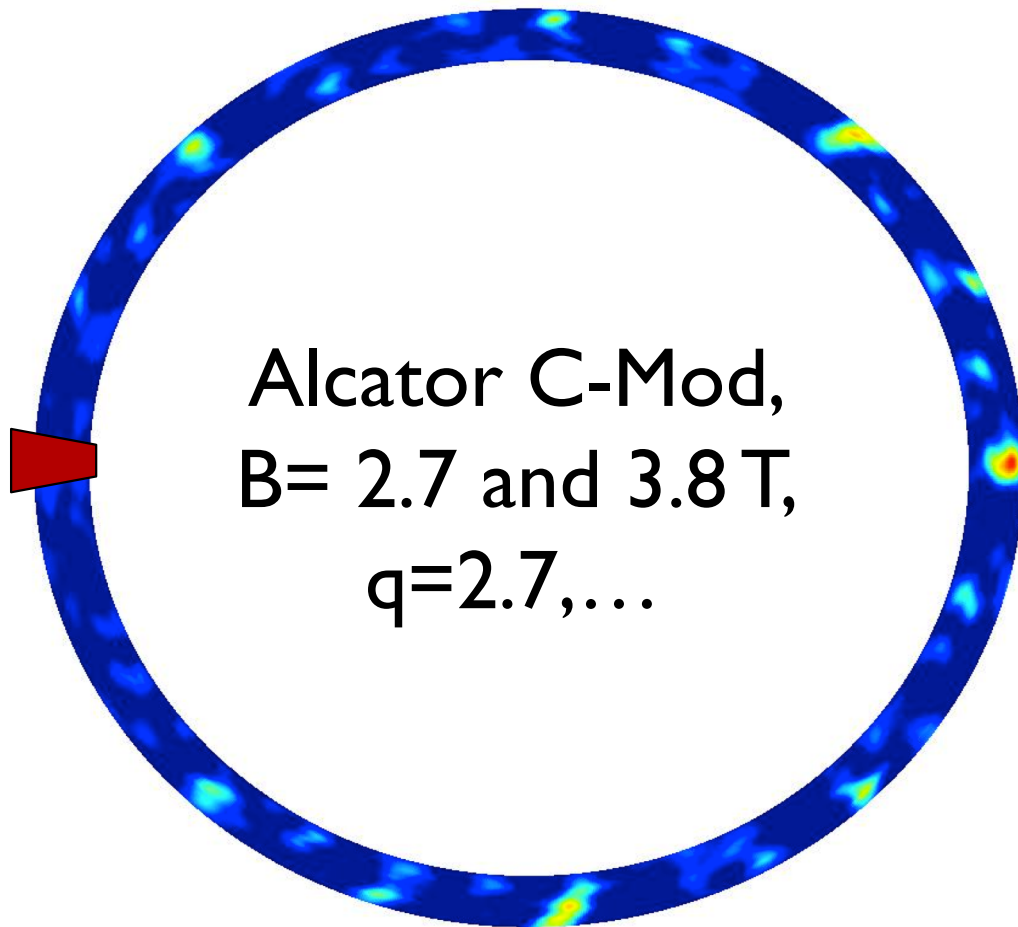


Geometry



Halpern et al, PPCF 2015  
Wersal & Ricci, NF 2017

# C-Mod fluctuation properties well captured





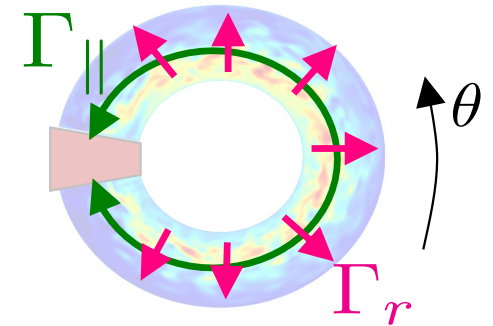
# A few of the key questions we addressed

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- How is the SOL width established?
- Why is there a difference between near and far SOL?
- What determines the SOL electrostatic potential?
- Are there mechanisms to generate toroidal rotation in the SOL?



# SOL width – analytical estimate



$$\begin{aligned}
 & \sim \frac{1}{L_p} \quad \sim \frac{1}{qR} \quad \sim c_s p \text{ Bohm's} \\
 & \nabla_r \Gamma_r \sim \nabla_{||} \Gamma_{||} \\
 & = \langle \tilde{p} \tilde{v}_{E \times B, r} \rangle_t = \frac{1}{B} \left\langle \tilde{p} \frac{\partial \tilde{\phi}}{\partial \theta} \right\rangle_t \sim \frac{\gamma \bar{p}}{L_p k_r^2} \sim \frac{\gamma \bar{p}}{k_\theta}
 \end{aligned}$$

$$\frac{\partial p}{\partial t} + \nabla \cdot (p \mathbf{v}_{E \times B}) \simeq 0$$

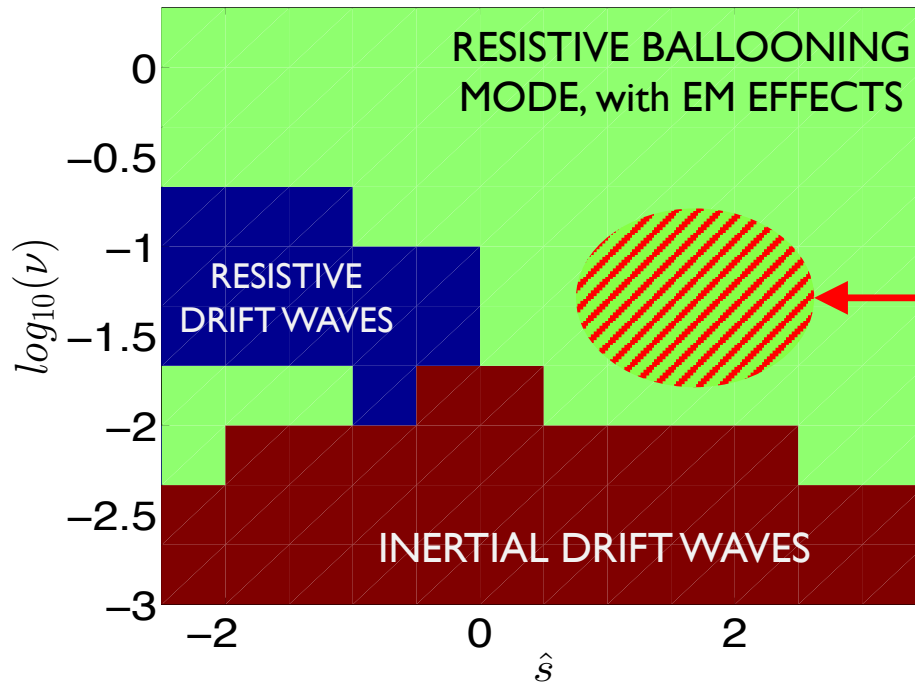
Removal of driving gradient  
Nonlocal

$$\frac{\partial \tilde{p}}{\partial r} \sim \frac{\partial \bar{p}}{\partial r}$$

$$L_p \simeq \frac{qR}{c_s} \left( \frac{\gamma}{k_\theta} \right)_{\max}$$

# SOL turbulent regimes

Instability driving turbulence depends mainly on  $q, \nu, \hat{s}$ .



TYPICAL LIMITED SOL OPERATIONAL PARAMETERS

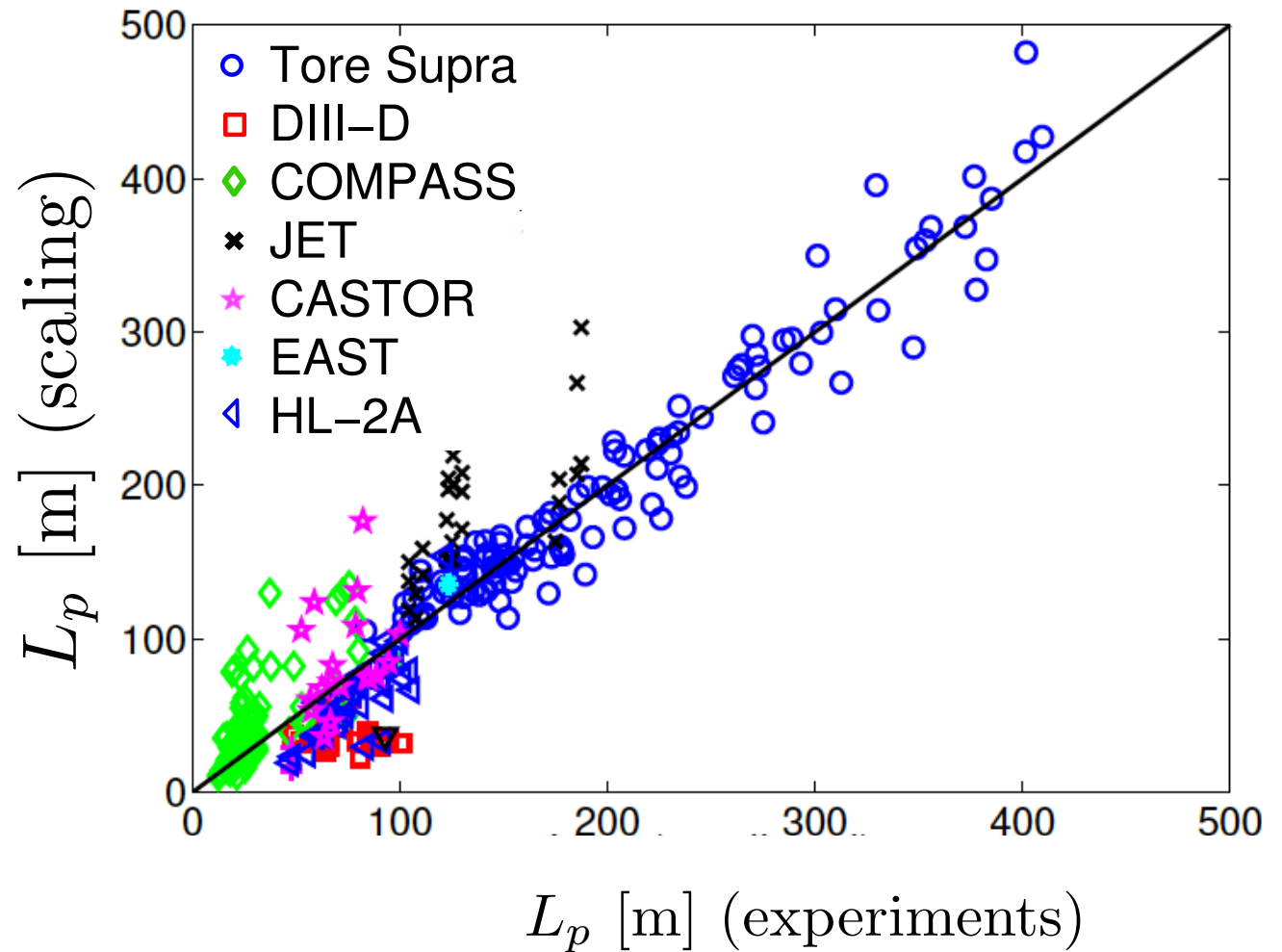
$$L_p = \frac{qR}{c_s} \begin{pmatrix} \gamma \\ k_\theta \end{pmatrix}$$

BM  $\gamma \sim \gamma_b = c_s \sqrt{\frac{2}{RL_p}}$

max BM  $k_\theta \sim \sqrt{\frac{\mu_0 \sigma_{\parallel} c_A^2}{q^2 R^2 \gamma_b}}$

# Successful validation of ballooning scaling

Good agreement with simulation results and ITPA database



Halpern et al., NF 2013;  
NF 2014, PPCF 2016

# A few of the key questions we addressed

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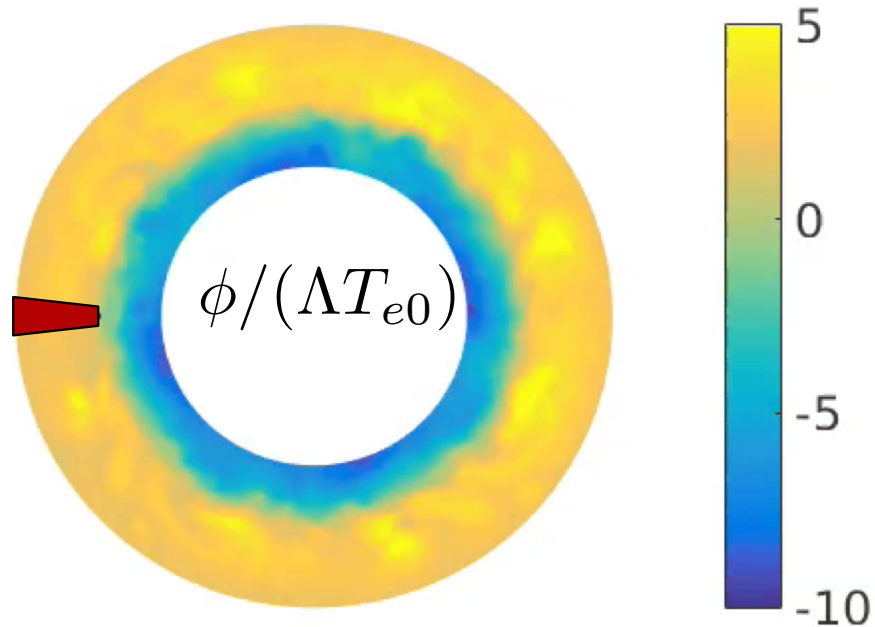
- How is the SOL width established?

- Why is there a difference between near and far SOL?

- What determines the SOL electrostatic potential?

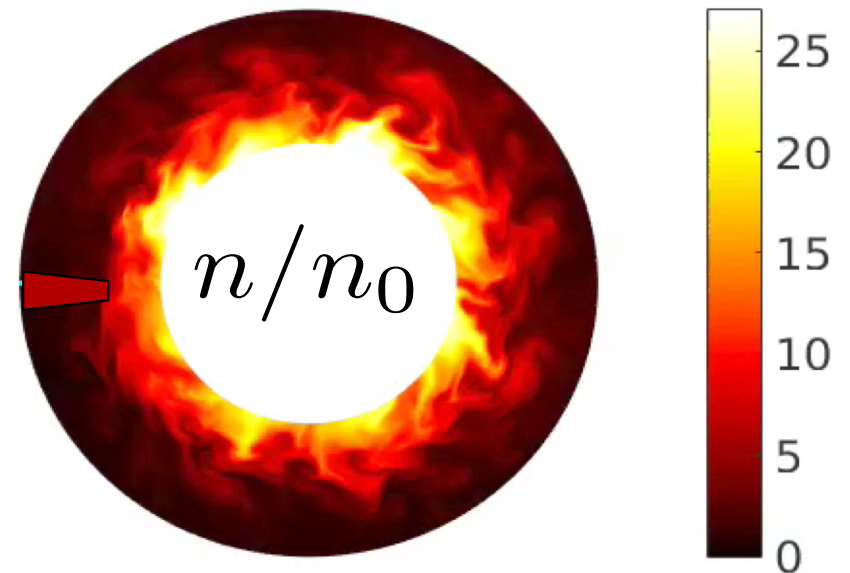
- Are there mechanisms to generate toroidal rotation in the SOL?

# Different turbulent properties in near and far SOL



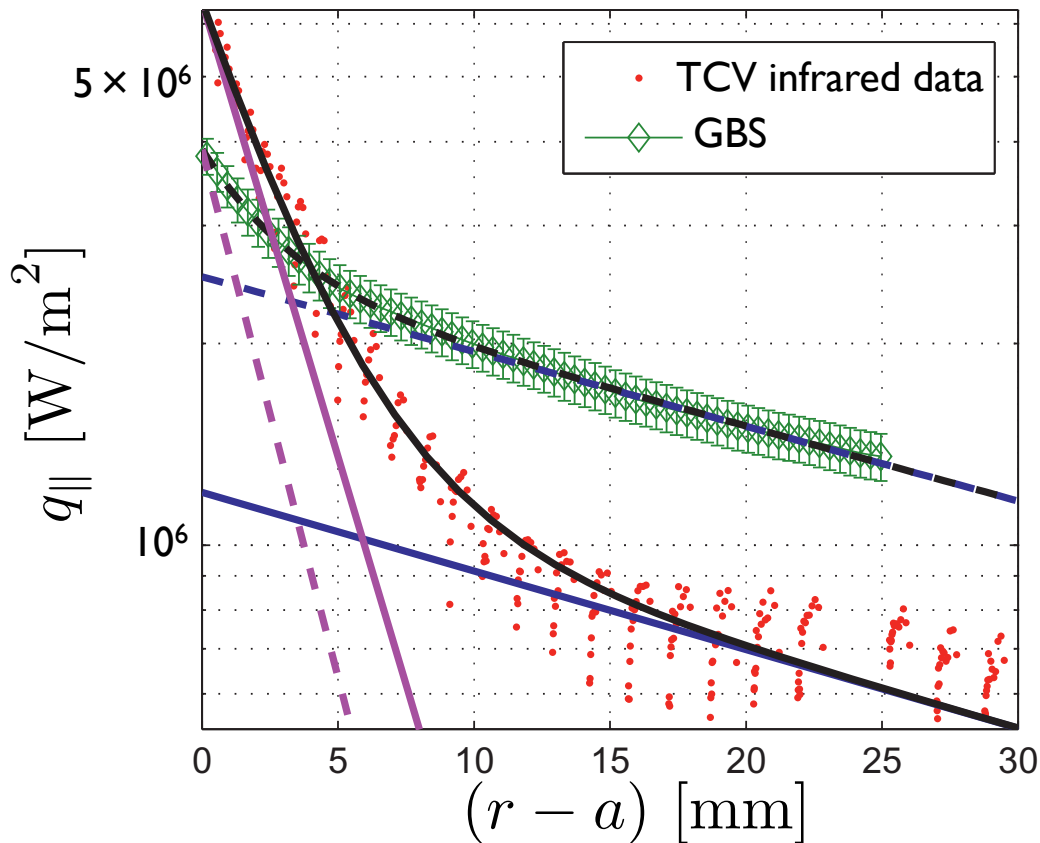
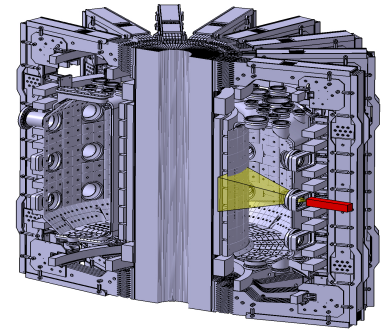
Strong shear flow at the LCFS...

... resulting into a strong density gradient



Halpern & Ricci, NF 2017

# Narrow feature at LCFS, long decay in far SOL



- TCV comparison: similar scale lengths, reduced heat flux in narrow feature
- Short scale: turbulence correlation length

Nespoli et al., JNM 2017  
Halpern & Ricci, NF 2017

ITER inner wall was redesigned

# A few of the key questions we addressed

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- How is the SOL width established?
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# Potential in the SOL set by sheath and electron adiabaticity

Typical estimate: at the sheath

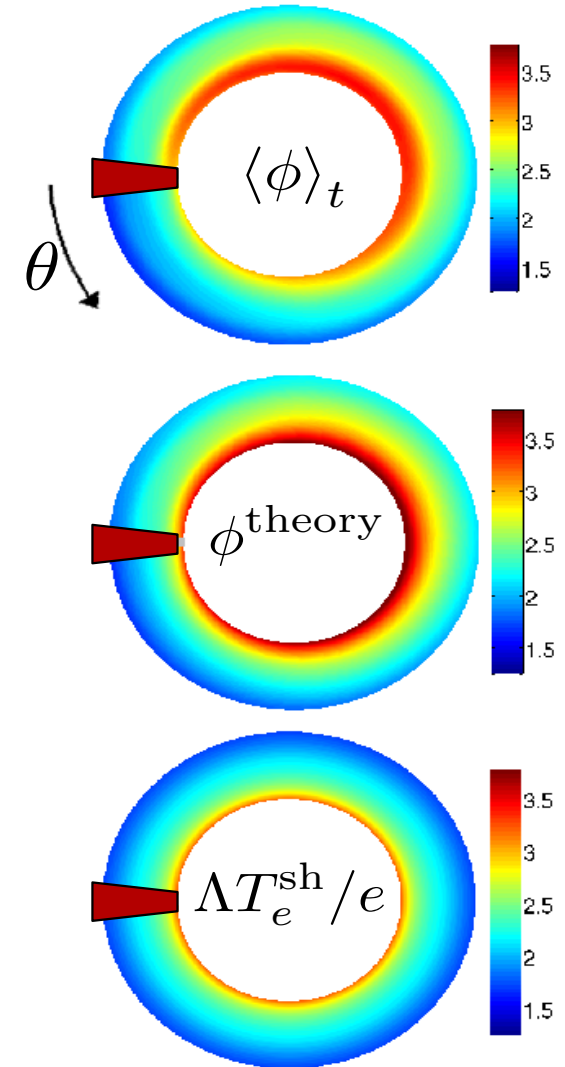
$$v_{\parallel i} = c_s \quad v_{\parallel e} = c_s \exp(\Lambda - e\phi/T_e^{\text{sh}})$$

to have ambipolar flows,  $v_{\parallel i} = v_{\parallel e}$

$$\phi = \Lambda T_e^{\text{sh}}/e \simeq 3T_e^{\text{sh}}/e$$

$$\phi = \underbrace{\Lambda T_e^{\text{sh}}/e}_{\text{Sheath}} + \underbrace{2.71(T_e - T_e^{\text{sh}})/e}_{\text{Adiabaticity}}$$

Our more rigorous treatment, from  $v_{\parallel e}$  equation





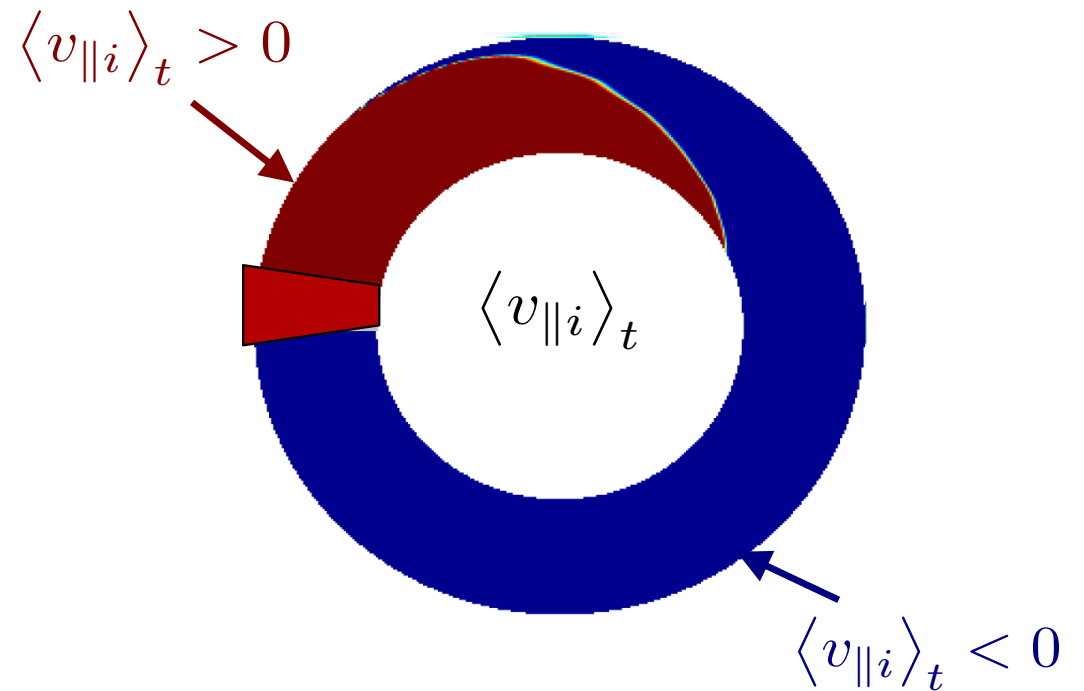
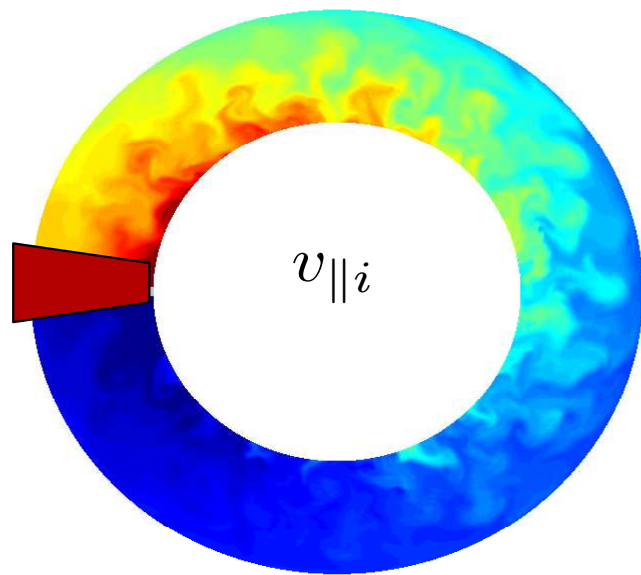
# A few of the key questions we addressed

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# GBS simulations show intrinsic toroidal rotation

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# 2D equation for the equilibrium flow

$$\underbrace{-\frac{\partial}{\partial r} \left( D_T \frac{\partial \bar{v}_{\parallel i}}{\partial r} \right)}_{\text{Turbulent driven radial transport, gradient-removal estimate}} + \underbrace{\frac{\sigma_\varphi}{|B_\varphi|} \frac{\partial \phi}{\partial r} \frac{\partial \bar{v}_{\parallel i}}{\partial \theta}}_{\text{Poloidal convection}} + \underbrace{\alpha \sigma_\theta \bar{v}_{\parallel i} \frac{\partial \bar{v}_{\parallel i}}{\partial \theta}}_{\text{Parallel convection}} + \underbrace{\frac{\alpha \sigma_\theta}{m_i \bar{n}} \frac{\partial \bar{p}}{\partial \theta}}_{\text{Pressure poloidal asymmetry}} = 0$$

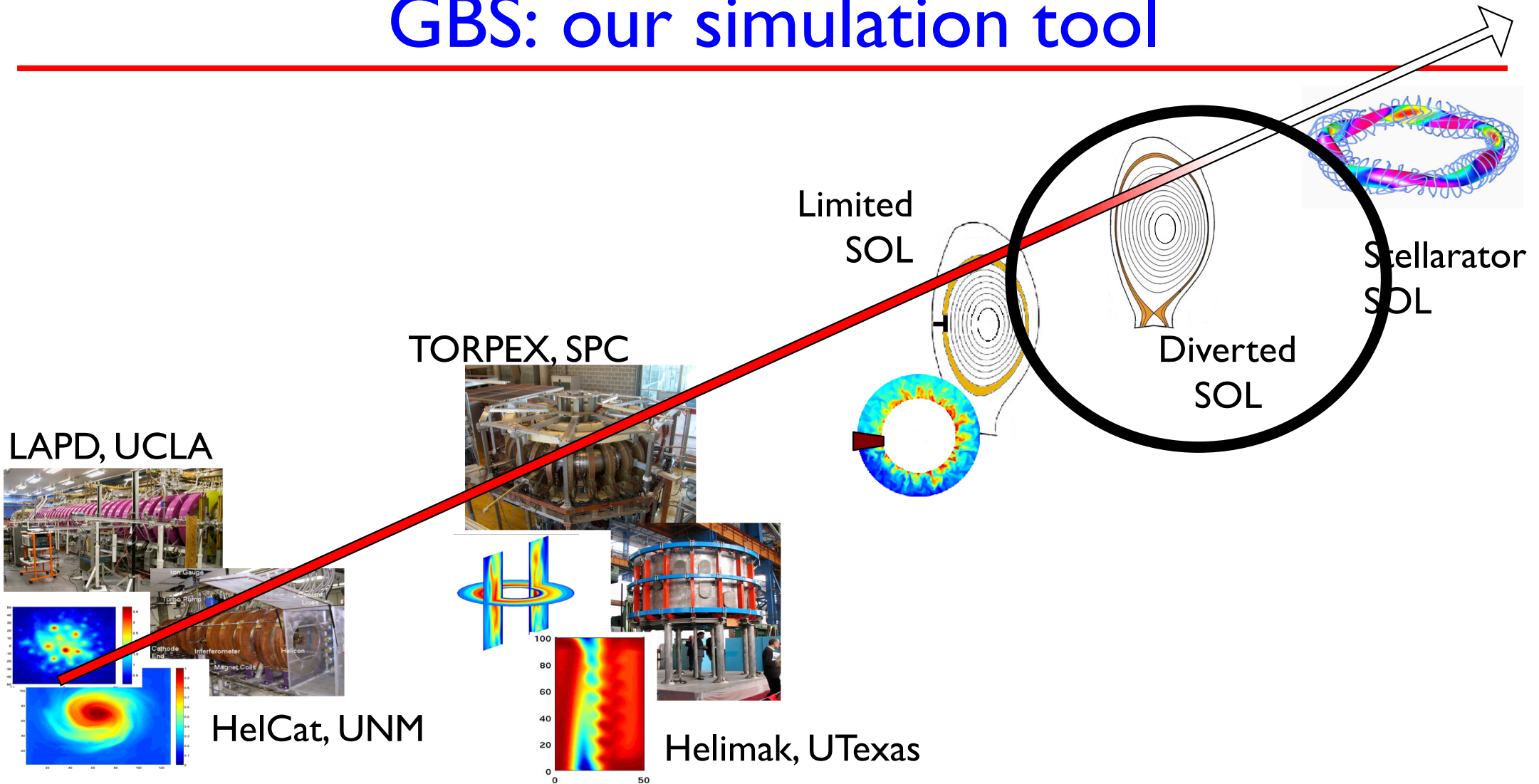
with boundary conditions:

$$\bar{v}_{\parallel i} \Big|_{se} = \underbrace{\pm c_s}_{\text{Bohm's criterion}} - \underbrace{\frac{q}{\epsilon} \frac{\partial \phi}{\partial r}}_{\text{ExB correction}}$$

Sources of toroidal rotation

Agreement with C-Mod observations

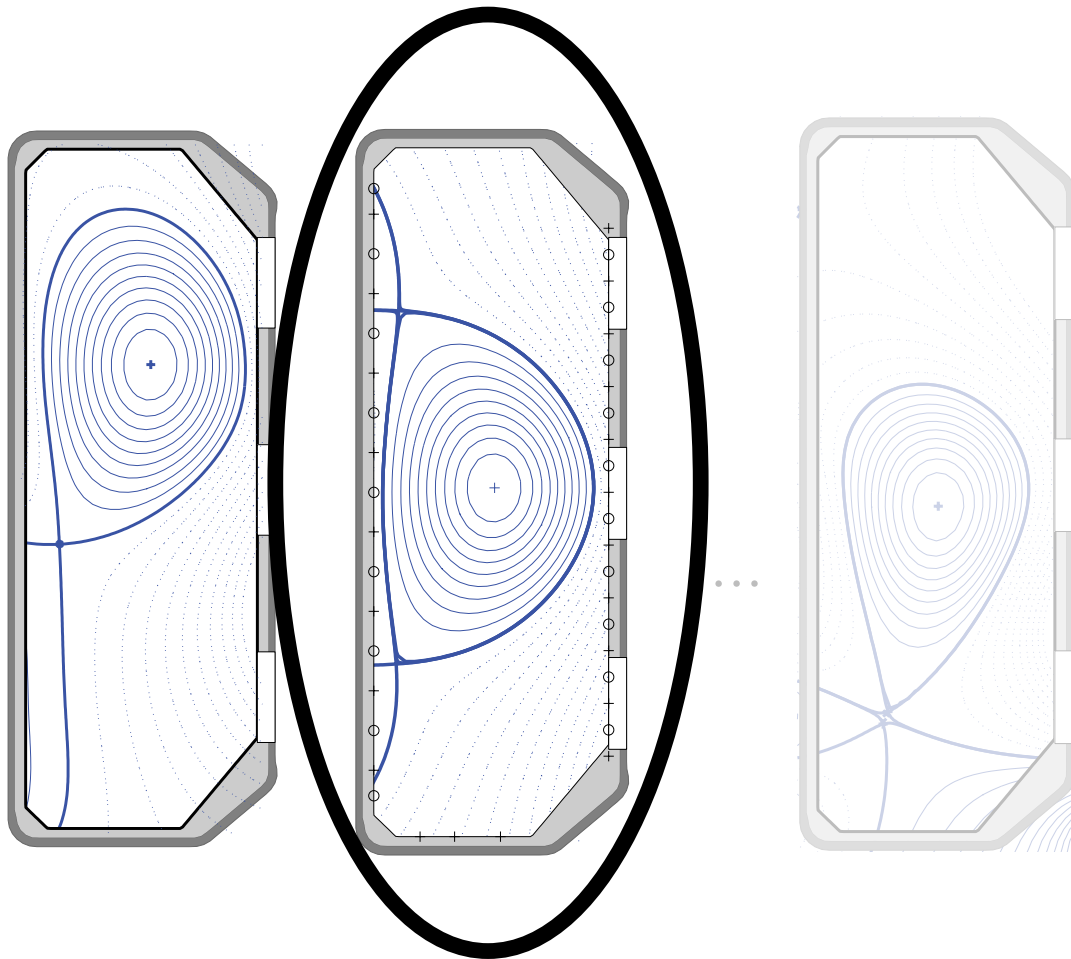
# GBS: our simulation tool



Ricci et al., PPCF 2012; Halpern et al., JCP 2016

# Flexible non-field aligned algorithm for diverted geometries

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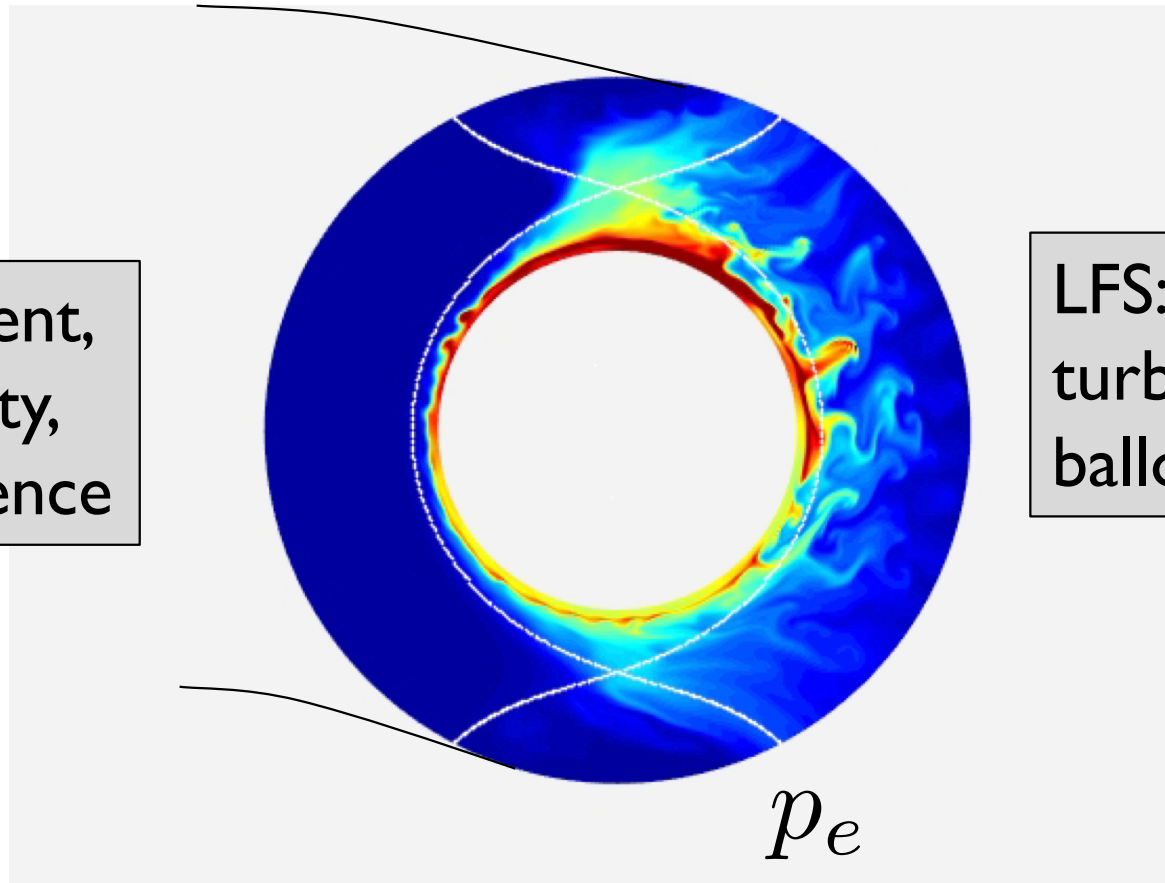
Double null:

- Possible heat exhaust solution
- High and low field sides separated

# GBS simulations of double-null configurations

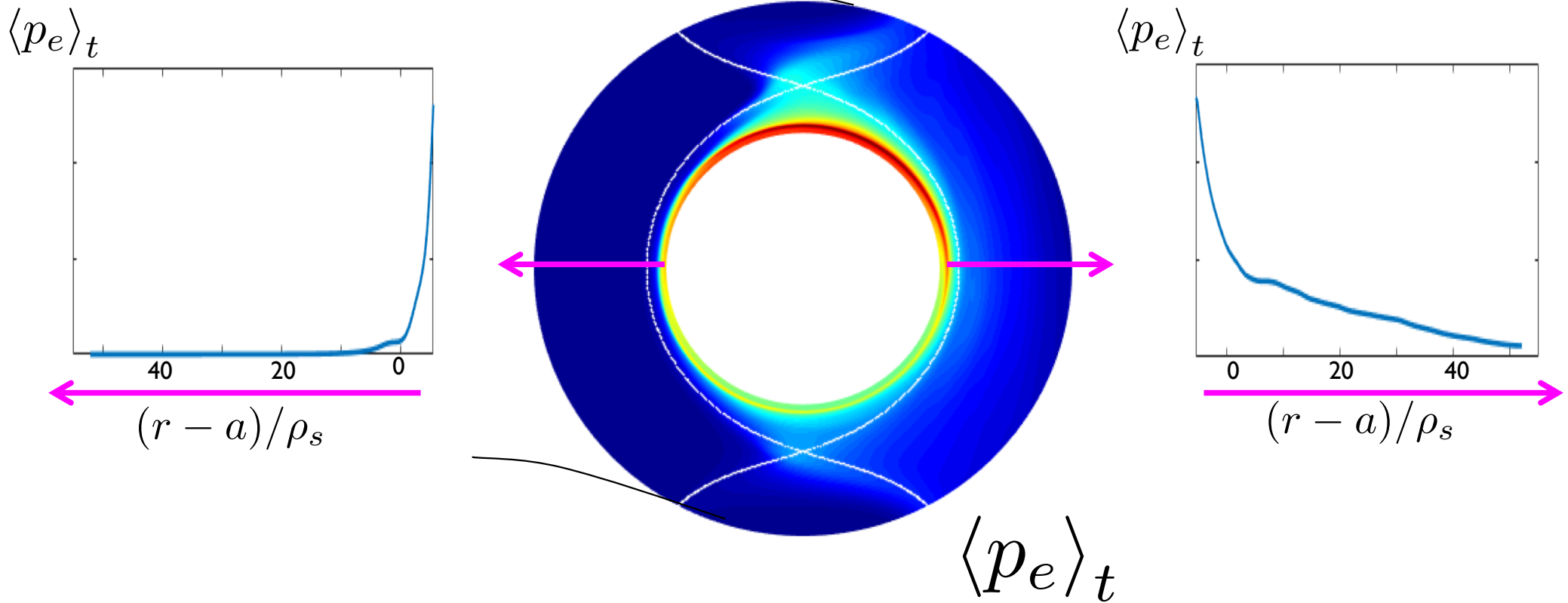
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HFS: quiescent,  
almost empty,  
K-H turbulence

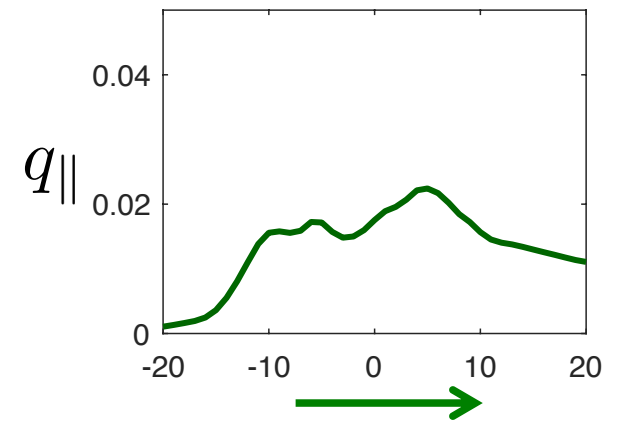
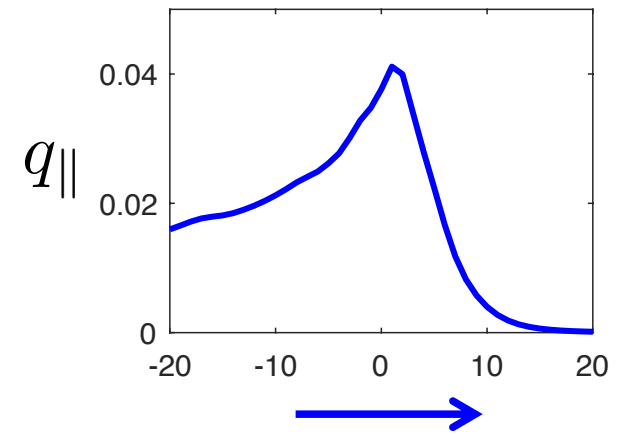
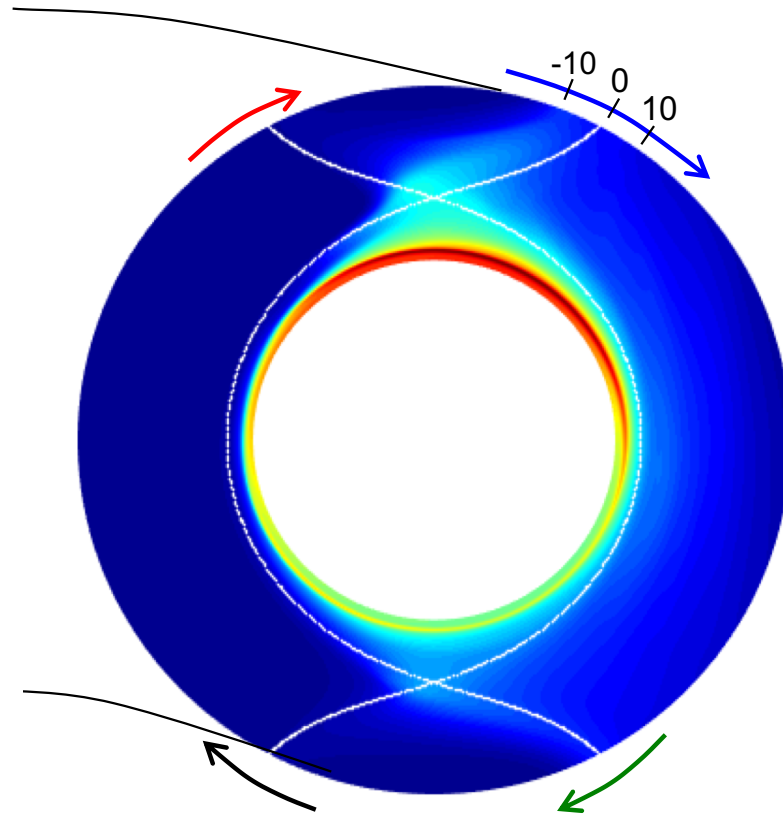
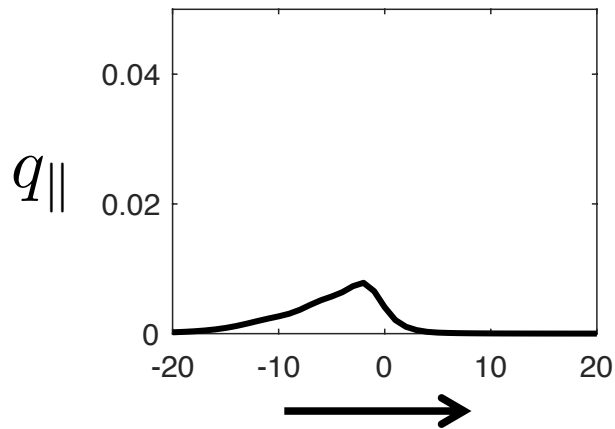
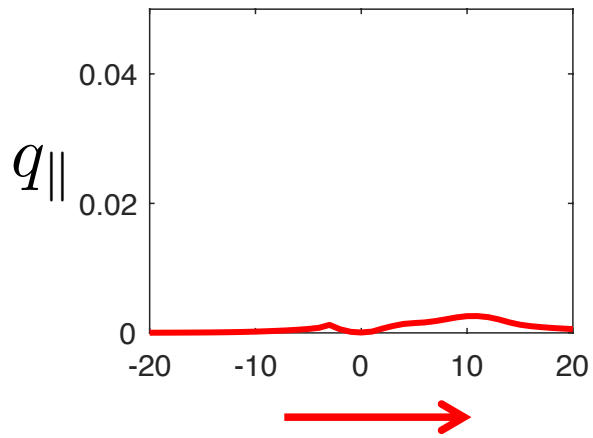


LFS: blobs, strong  
turbulence,  
ballooning drive...

# Steep gradient at HFS, 2 scale lengths at LFS



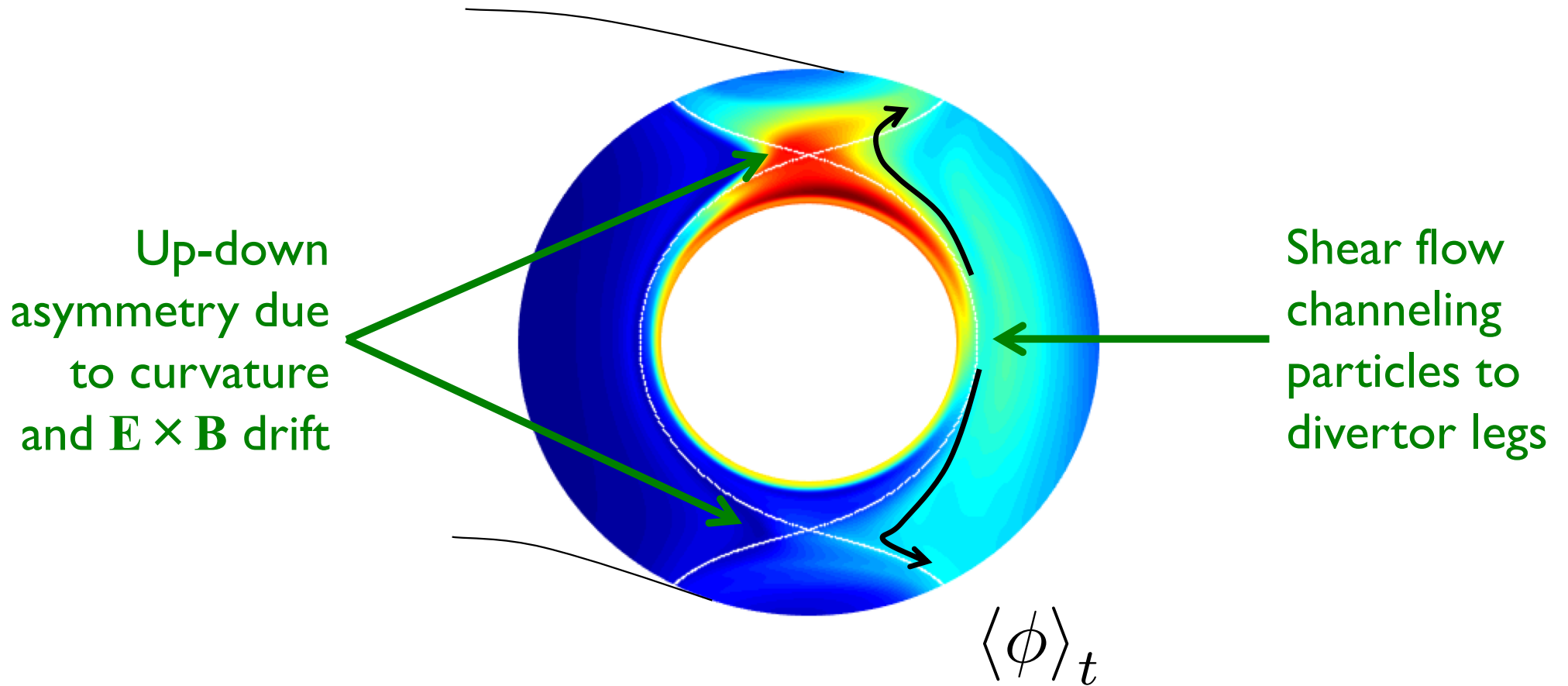
# Very different heat fluxes along 4 legs





# Complex circulation pattern

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# What are we learning on SOL dynamics?

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- The use first-principles simulations and analysis to investigate SOL plasma dynamics
- Progressive approach to complexity
- Results in limited configuration:
  - SOL width set by resistive ballooning-driven turbulence saturated by the gradient removal mechanism in good agreement with multi-machine database
  - Presence of strong shear flow at the LCFS, resulting into 2 scale lengths
  - Mechanisms setting electrostatic potential and toroidal rotation
- Diverted configurations, complex flow patterns

<http://people.epfl.ch/paolo.ricci>

Extra slides

# The complete set of equations

$$\frac{\partial n}{\partial t} = -\rho_\star^{-1} [\phi, n] + \frac{2}{B} [C(p_e) - nC(\phi)] - \nabla_{\parallel} (nv_{\parallel e}) + \mathcal{D}_n(n) + S_n + n_n n r_{iz} - n^2 r_{rec} \quad (1)$$

$$\frac{\partial \tilde{\omega}}{\partial t} = -\rho_\star^{-1} [\phi, \tilde{\omega}] - v_{\parallel i} \nabla_{\parallel} \tilde{\omega} + \frac{B^2}{n} \nabla_{\parallel} j_{\parallel} + \frac{2B}{n} C(p) + \mathcal{D}_{\tilde{\omega}}(\tilde{\omega}) \quad (2)$$

$$\frac{\partial v_{\parallel e}}{\partial t} + \frac{m_j}{m_e} \frac{\beta_e}{2} \frac{\partial \Psi}{\partial t} = -\rho_\star^{-1} [\phi, v_{\parallel e}] - v_{\parallel e} \nabla_{\parallel} v_{\parallel e} + \frac{m_j}{m_e} \left( v \frac{j_{\parallel}}{n} + \nabla_{\parallel} \phi - \frac{1}{n} \nabla_{\parallel} p_e - 0.71 \nabla_{\parallel} T_e \right) + \mathcal{D}_{v_{\parallel e}}(v_{\parallel e}) \quad (3)$$

$$\frac{\partial v_{\parallel i}}{\partial t} = -\rho_\star^{-1} [\phi, v_{\parallel i}] - v_{\parallel i} \nabla_{\parallel} v_{\parallel i} - \frac{1}{n} \nabla_{\parallel} p + \mathcal{D}_{v_{\parallel i}}(v_{\parallel i}) + n_n (r_{iz} + r_{cx})(v_{\parallel n} - v_{\parallel i}) \quad (4)$$

$$\frac{\partial T_e}{\partial t} = -\rho_\star^{-1} [\phi, T_e] - v_{\parallel e} \nabla_{\parallel} T_e + \frac{4T_e}{3B} \left[ \frac{1}{n} C(p_e) + \frac{5}{2} C(T_e) - C(\phi) \right] + \frac{2T_e}{3} \left[ \frac{0.71}{n} \nabla_{\parallel} j_{\parallel} - \nabla_{\parallel} v_{\parallel e} \right] \quad (5)$$

$$+ \mathcal{D}_{T_e}(T_e) + \mathcal{D}_{T_e}^{\parallel}(T_e) + S_{T_e} - n_n r_{iz} E_{iz}$$

$$\frac{\partial T_i}{\partial t} = -\rho_\star^{-1} [\phi, T_i] - v_{\parallel i} \nabla_{\parallel} T_i + \frac{4T_i}{3B} \left[ \frac{1}{n} C(p_e) - \tau \frac{5}{2} C(T_i) - C(\phi) \right] + \frac{2T_i}{3} \left[ (v_{\parallel i} - v_{\parallel e}) \frac{\nabla_{\parallel} n}{n} - \nabla_{\parallel} v_{\parallel e} \right] \quad (6)$$

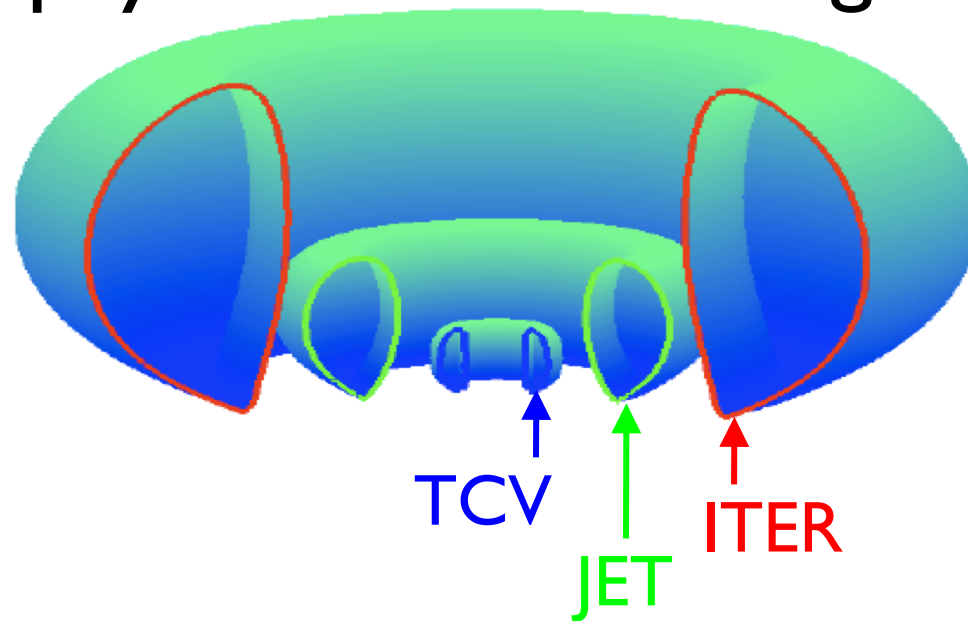
$$+ \mathcal{D}_{T_i}(T_i) + \mathcal{D}_{T_i}^{\parallel}(T_i) + S_{T_i} + n_n (r_{iz} + r_{cx})(T_n - T_i + (v_{\parallel n} - v_{\parallel i})^2)$$

$$\nabla_{\perp}^2 \phi = \omega, \quad \nabla_{\perp}^2 \Psi = j_{\parallel}, \quad \rho_\star = \rho_s / R, \quad \nabla_{\parallel} f = \mathbf{b}_0 \cdot \nabla f + \frac{\beta_e}{2} \rho_\star^{-1} [\Psi, f], \quad \tilde{\omega} = \omega + \tau \nabla_{\perp}^2 T_i, \quad p = n(T_e + \tau T_i)$$

# ITER design based on scaling law

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SOL basic physics understanding is still missing



Simulations of SOL turbulence are crucial

# The full set of GBS equations

$$\begin{aligned}
 \partial_t n &= -\frac{R}{B} [\phi, n] + \frac{2}{B} [\hat{C}(p_e) - n\hat{C}(\phi)] - \nabla_{\parallel} (nv_{\parallel e}) + S_n \\
 \partial_t \nabla_{\perp}^2 \phi &= -\frac{R}{B} [\phi, \nabla_{\perp}^2 \phi] + \frac{2B}{n} \hat{C}(p_e) - v_{\parallel i} \nabla_{\parallel} \nabla_{\perp}^2 \phi + \frac{B^2}{n} \nabla_{\parallel} j_{\parallel} \\
 \partial_t \left( v_{\parallel e} + \frac{m_i \beta_e}{m_e 2} \psi \right) &= -\frac{R}{B} [\phi, v_{\parallel e}] - v_{\parallel e} \nabla_{\parallel} v_{\parallel e} \\
 &\quad + \frac{m_i}{m_e} \left\{ -\nu \frac{j_{\parallel}}{n} + \nabla_{\parallel} \phi - \frac{1}{n} \nabla_{\parallel} p_e - 0.71 \nabla_{\parallel} T_e - \frac{2}{3n} \nabla_{\parallel} G_e \right\} \\
 \partial_t v_{\parallel i} &= -\frac{R}{B} [\phi, v_{\parallel i}] - v_{\parallel i} \nabla_{\parallel} v_{\parallel i} - \frac{1}{n} \nabla_{\parallel} p_e \\
 \partial_t T_e &= -\frac{R}{B} [\phi, T_e] - v_{\parallel e} \nabla_{\parallel} T_e + \frac{4}{3} \frac{T_e}{B} \left[ \frac{7}{2} \hat{C}(T_e) + \frac{T_e}{n} \hat{C}(n) - \hat{C}(\phi) \right] + S_{T_e} \\
 &\quad + \frac{2}{3} T_e \left[ 0.71 \nabla_{\parallel} v_{\parallel i} - 1.71 \nabla_{\parallel} v_{\parallel e} + 0.71 \left( \frac{v_{\parallel i} - v_{\parallel e}}{n} \right) \nabla_{\parallel} n \right]
 \end{aligned}$$

Need boundary conditions for:  
 $n, v_{\parallel e}, v_{\parallel i}, T_e, \nabla_{\perp}^2 \phi, \psi, \phi$

# Gradient-removal estimate of ExB velocity transport

$$\Gamma_{v,r} \sim \left\langle \tilde{v}_{\parallel i} \frac{\partial \tilde{\phi}}{\partial \theta} \right\rangle_t \left\langle \left( \frac{\partial \tilde{\phi}}{\partial \theta} \right)^2 \right\rangle_t \frac{\partial \bar{v}_{\parallel i}}{\partial r}$$

↑  
Parallel momentum  
 $\gamma \tilde{v}_{\parallel i} \sim \partial_r \bar{v}_{\parallel i} \partial_\theta \tilde{\phi}$

$$\left\langle \tilde{p}^2 \right\rangle_t \frac{\partial \bar{v}_{\parallel i}}{\partial r} - \frac{\gamma}{k_\theta} L_p \frac{\partial \bar{v}_{\parallel i}}{\partial r}$$

↑ Continuity  $\gamma \tilde{p} \sim \partial_r \bar{p} \partial_\theta \tilde{\phi}$       ↑ Grad removal  $\partial_r \tilde{p} \sim \partial_r \bar{p}$

$$-\frac{L_p^2 c_s}{qR} \frac{\partial \bar{v}_{\parallel i}}{\partial r}$$

↑ Lp estimate  
 $L_p \sim qR\gamma / (c_s k_\theta)$

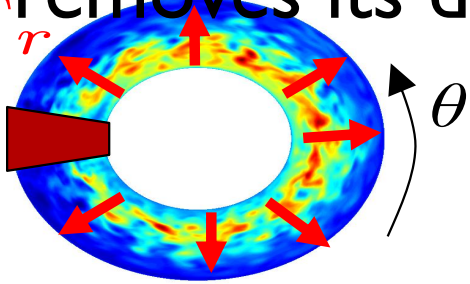
➔

$$\Gamma_{v,r} = -D_T \frac{\partial \bar{v}_{\parallel i}}{\partial r}, \quad D_T = \frac{L_p^2 c_s}{qR}$$

# Turbulent transport with gradient removal (GR) saturation

Turbulence saturates when it  $\rightarrow \frac{\partial \tilde{p}}{\partial r} \sim \frac{\partial \bar{p}}{\partial r} \rightarrow k_r \tilde{p} \sim \bar{p} / L_p$

$\Gamma_r$  removes its drive



$$\frac{\partial p}{\partial t} \simeq [p, \phi]$$

$$\Gamma_r = \left\langle \tilde{p} \frac{\partial \phi}{\partial \theta} \right\rangle_t$$

GR hypothesis

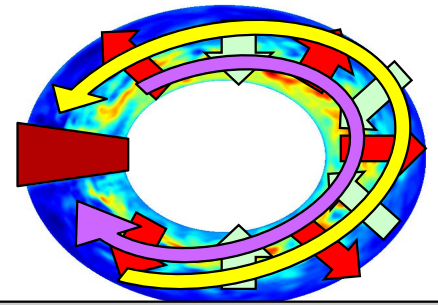
Nonlocal linear theory,  $\uparrow k_r \sim \sqrt{k_\theta / L_p}$



$$D_{GR} = \frac{\Gamma_r}{\bar{p} / L_p} \sim \frac{\gamma L_p}{k_\theta}$$



# Turbulence saturation due to ~~Kelvin-Helmholtz instability (KH)~~



Primary instability grows until it causes KH

$$\rightarrow \frac{\partial \Omega}{\partial t} \sim [\phi, \Omega] \rightarrow \tilde{\phi} \sim \frac{\gamma}{k_\theta^2}$$

unstable shear flow

$$\Gamma_r = \left\langle \tilde{p} \frac{\partial \tilde{\phi}}{\partial \theta} \right\rangle_t \sim \frac{\gamma \bar{p}}{L_p k_\theta^2} \rightarrow D_{KH} \sim \frac{\gamma}{k_\theta^2}$$

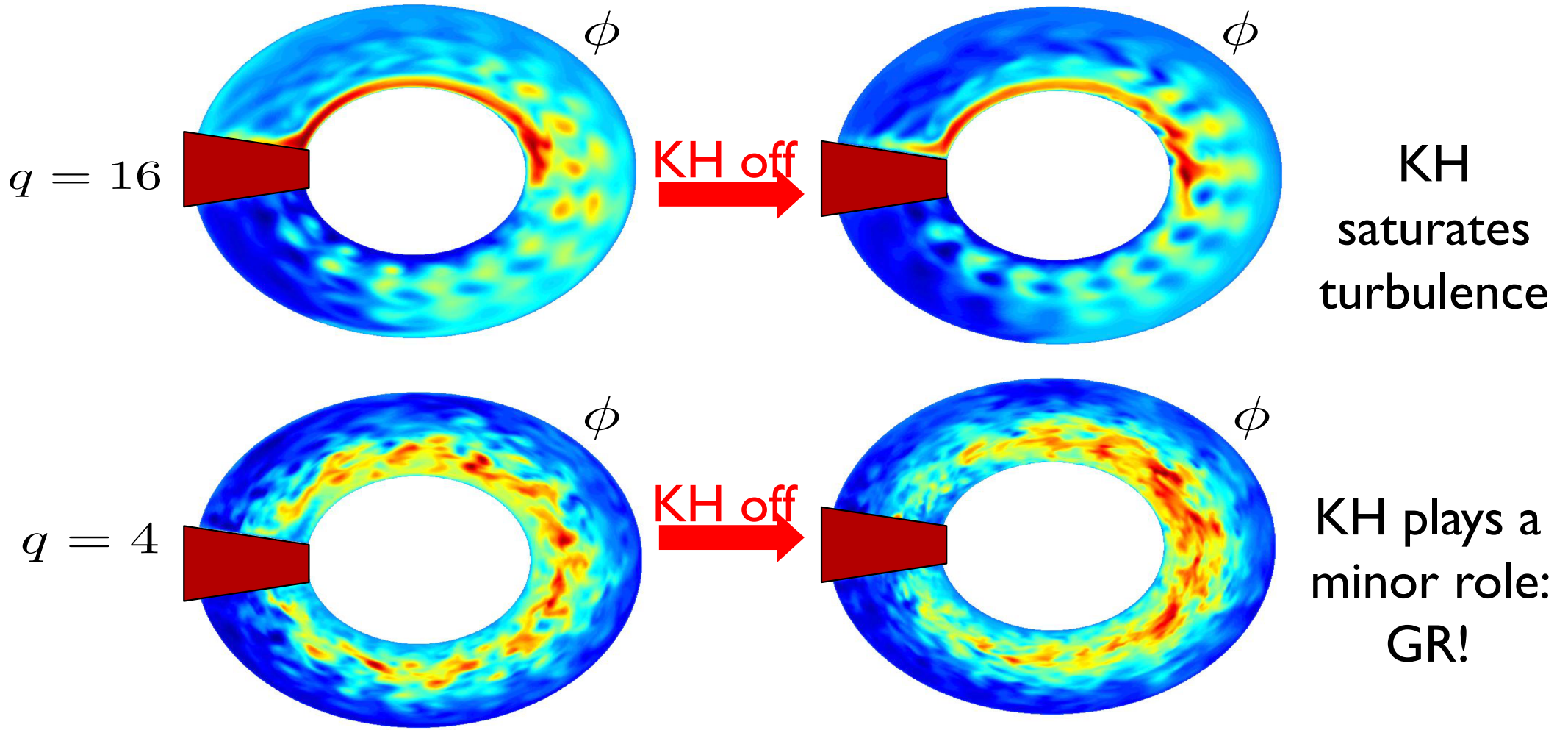
## KH vs GR mechanism:

$$\frac{D_{KH}}{D_{GR}} \sim \frac{1}{k_\theta L_p} < 1$$

We expect KH to limit the transport, provided that KH is unstable!

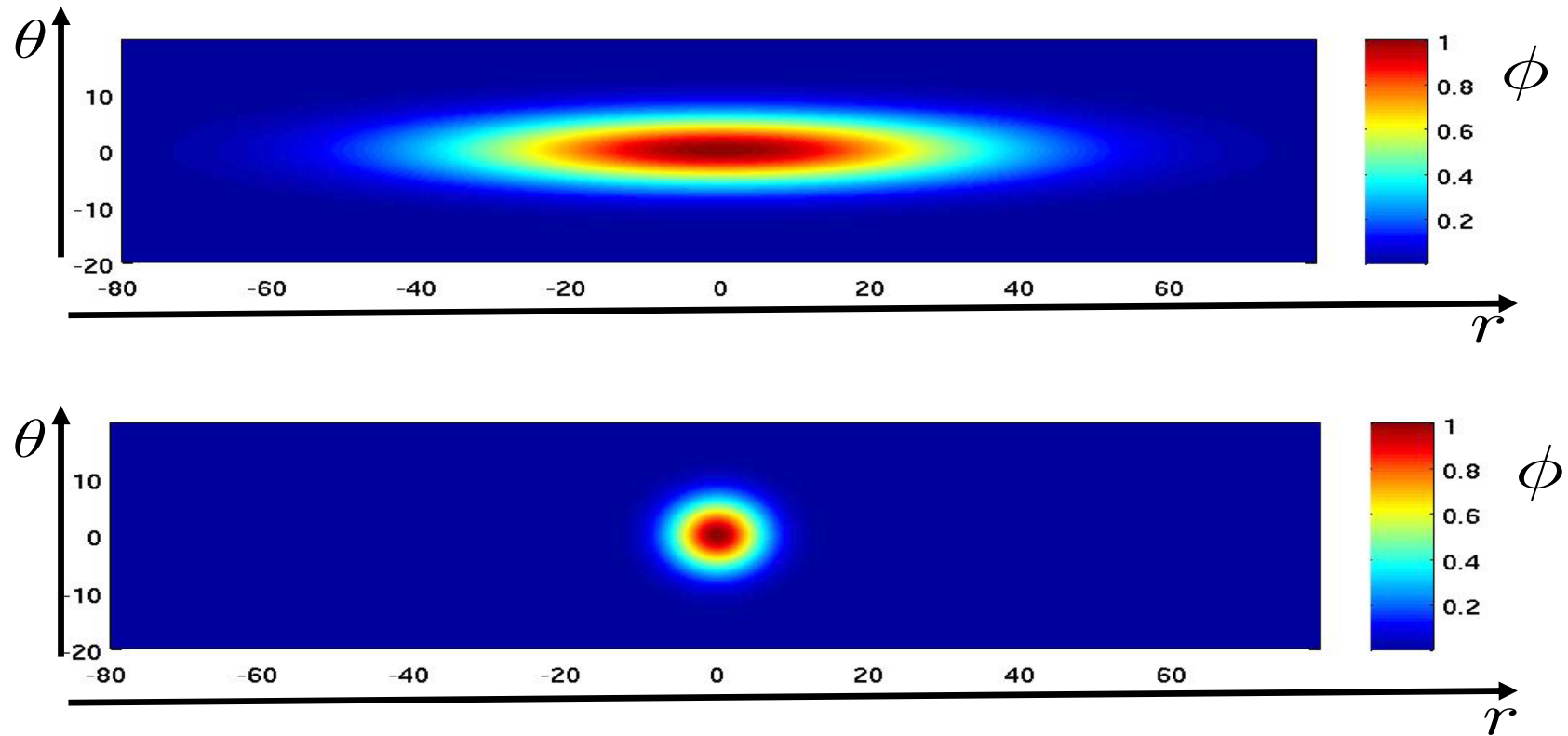
# Is KH really setting transport?

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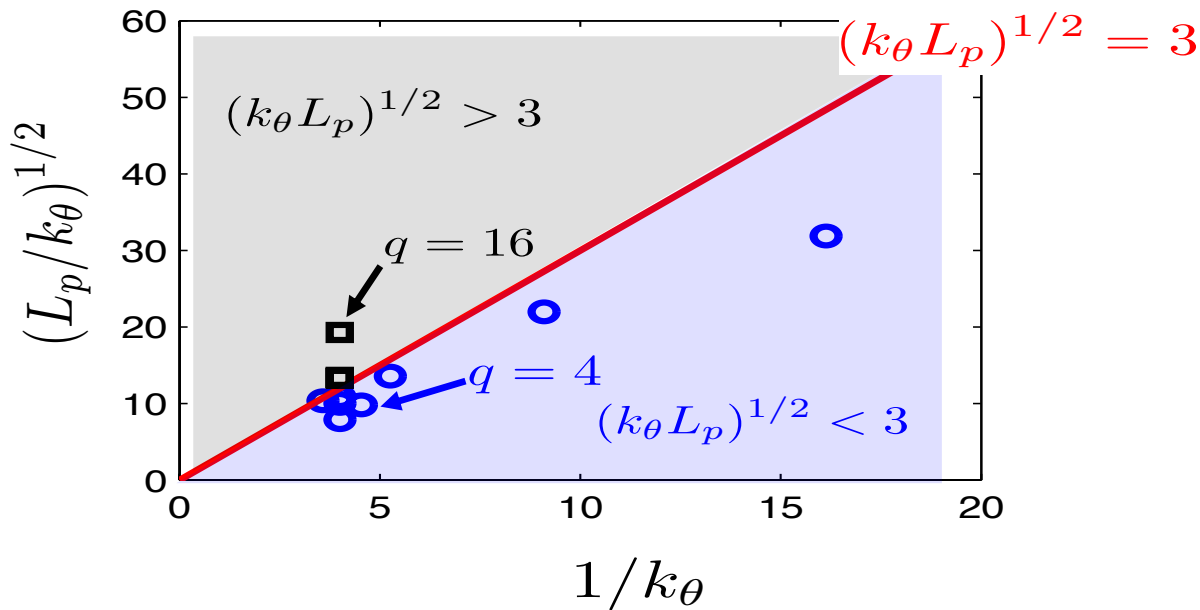
# Why is KH stable at low $q$ but not higher $q$ ?

Only elongated eddies are KH unstable



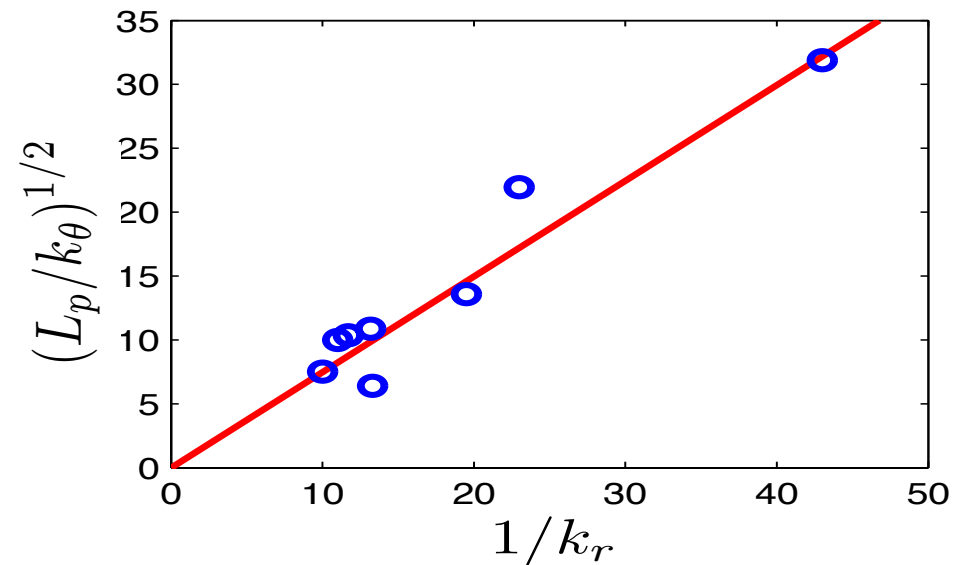
By comparing eddy turn over time and KH growth rate,  
KH unstable if:  $\sqrt{k_\theta L_p} > 3$

# Why is KH stable at low $q$ but not higher $q$ ?



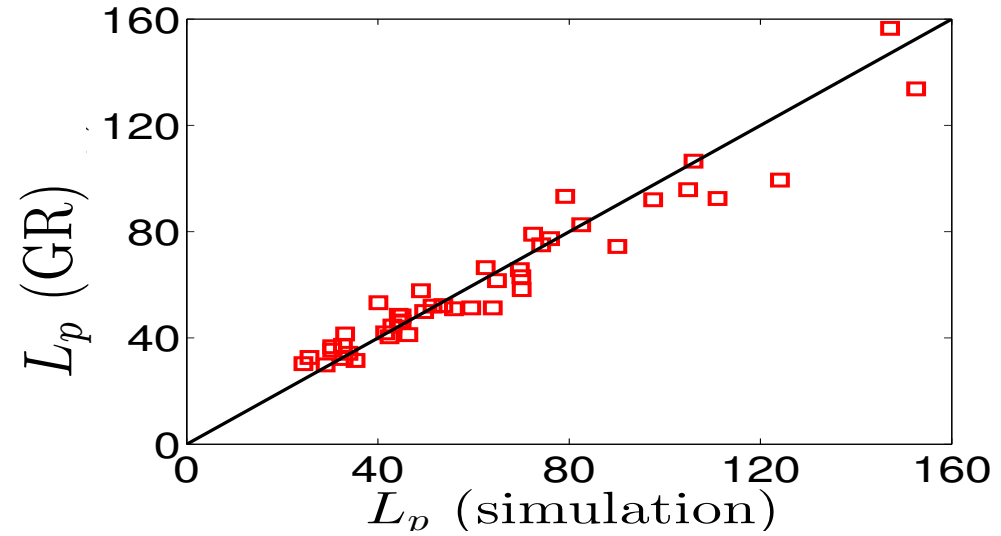
$q=4$  simulations are in the KH stable region

The eddies show the GR scaling properties

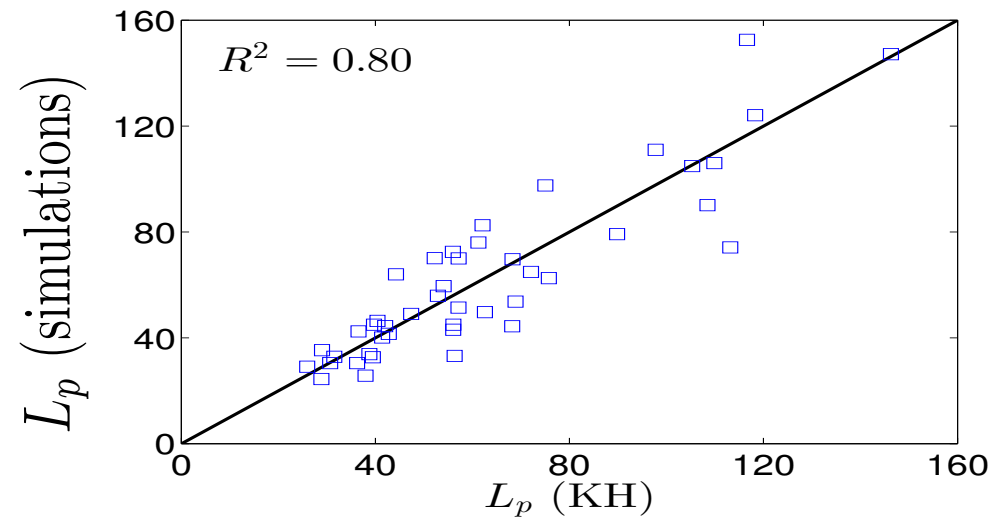


# KH vs GR scaling?

$$R^2 = 93\%$$

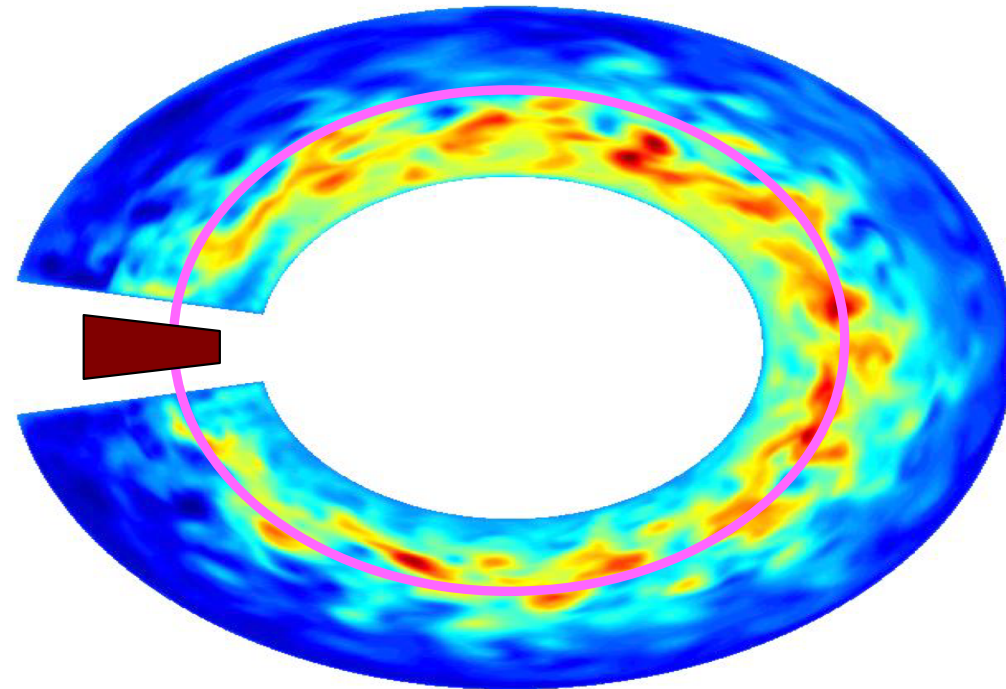


$$R^2 = 80\%$$



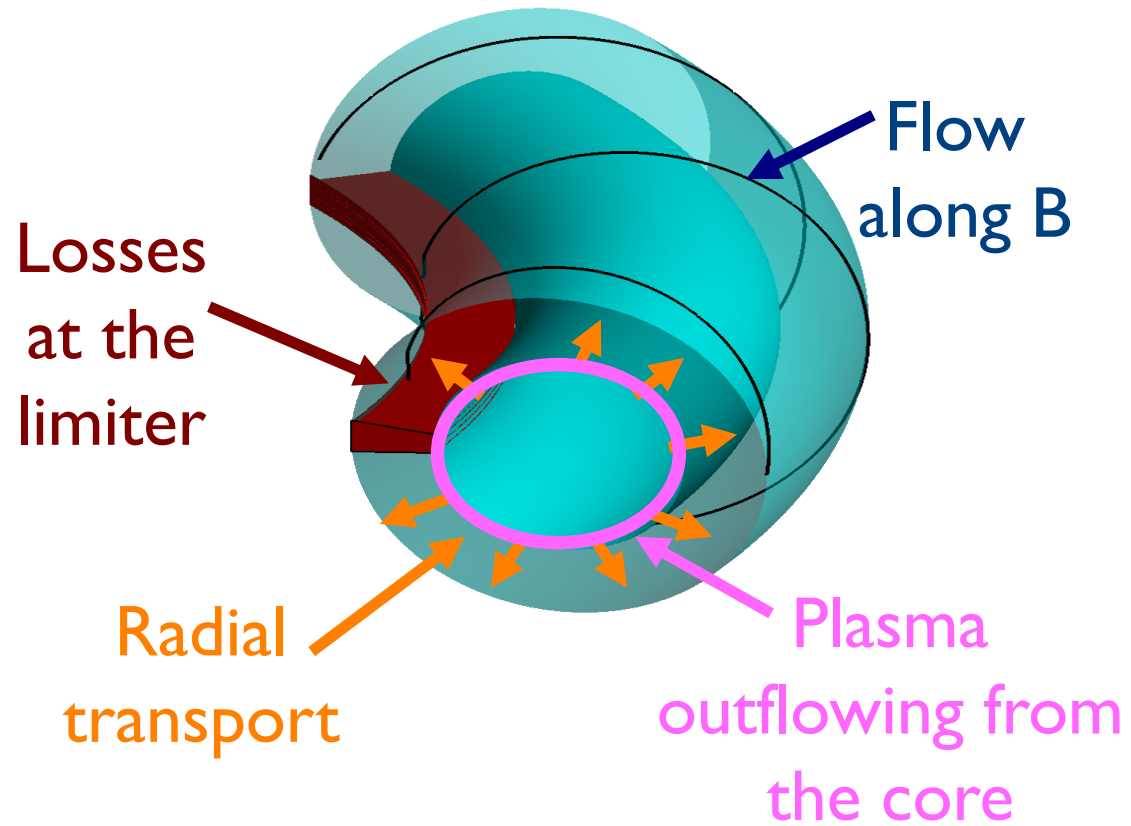
# Details of the source

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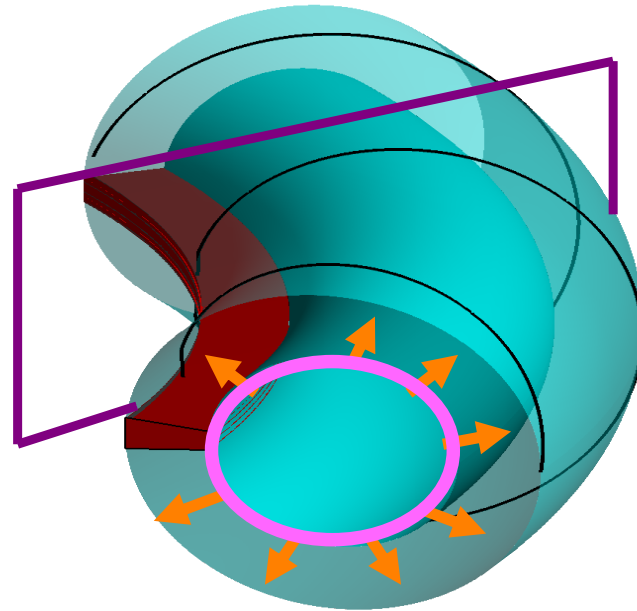
# Tokamak SOL simulations

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# Tokamak SOL simulations

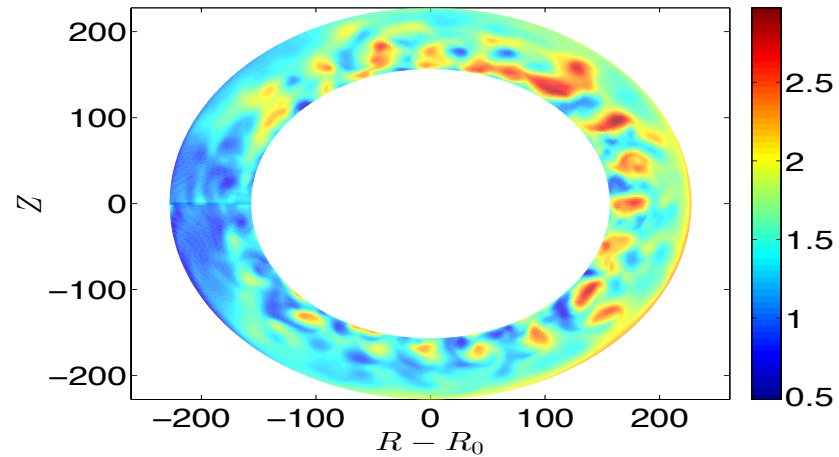
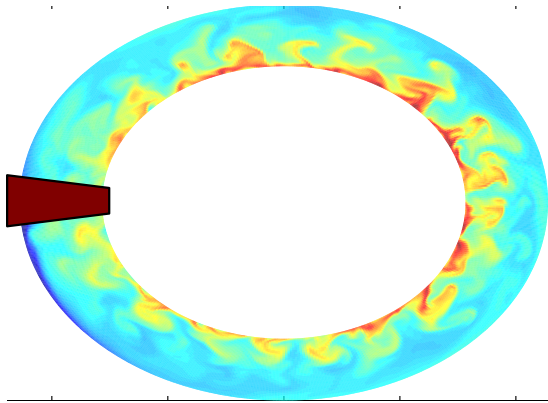
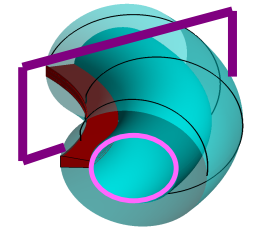
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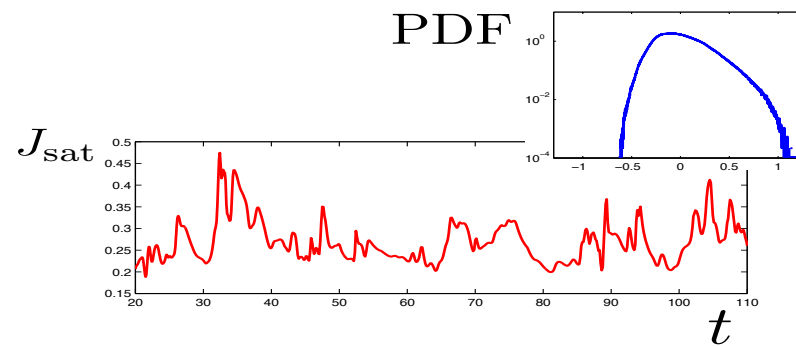
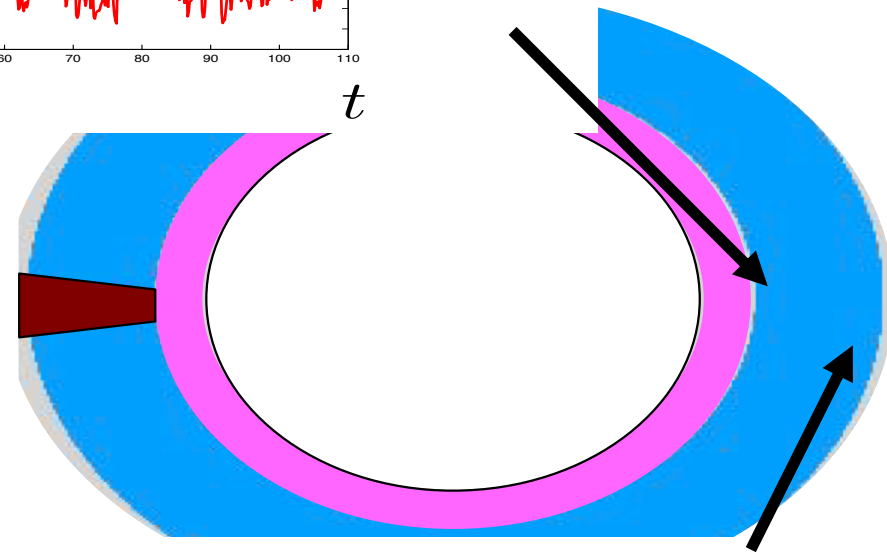
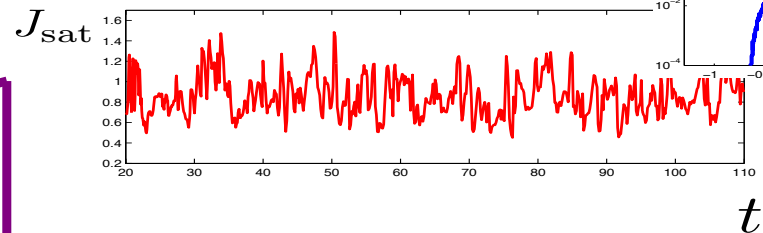
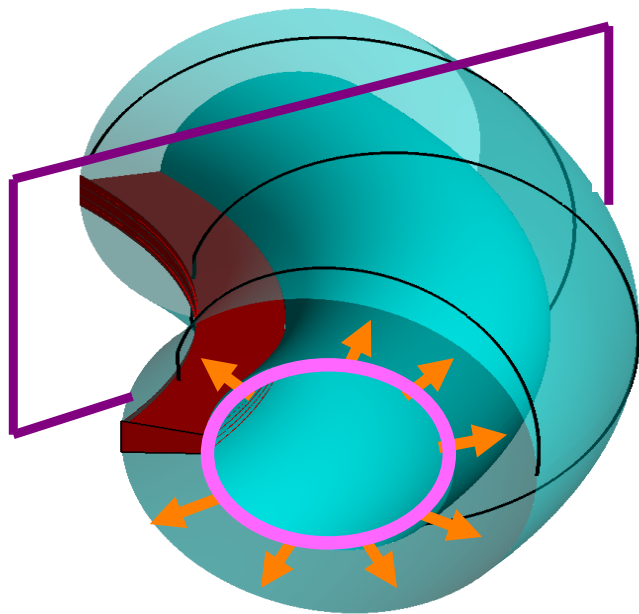


# Tokamak SOL simulations

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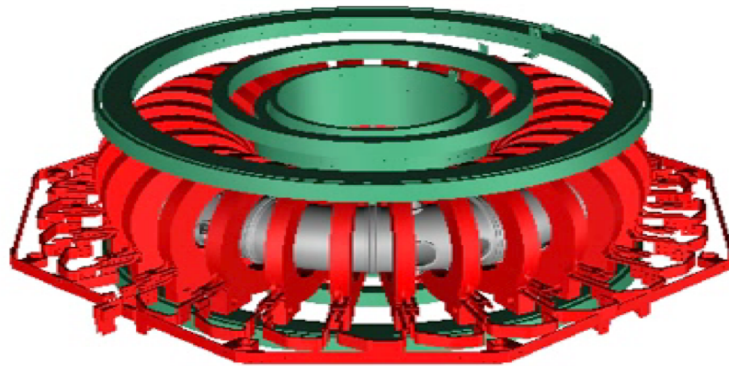


# Tokamak



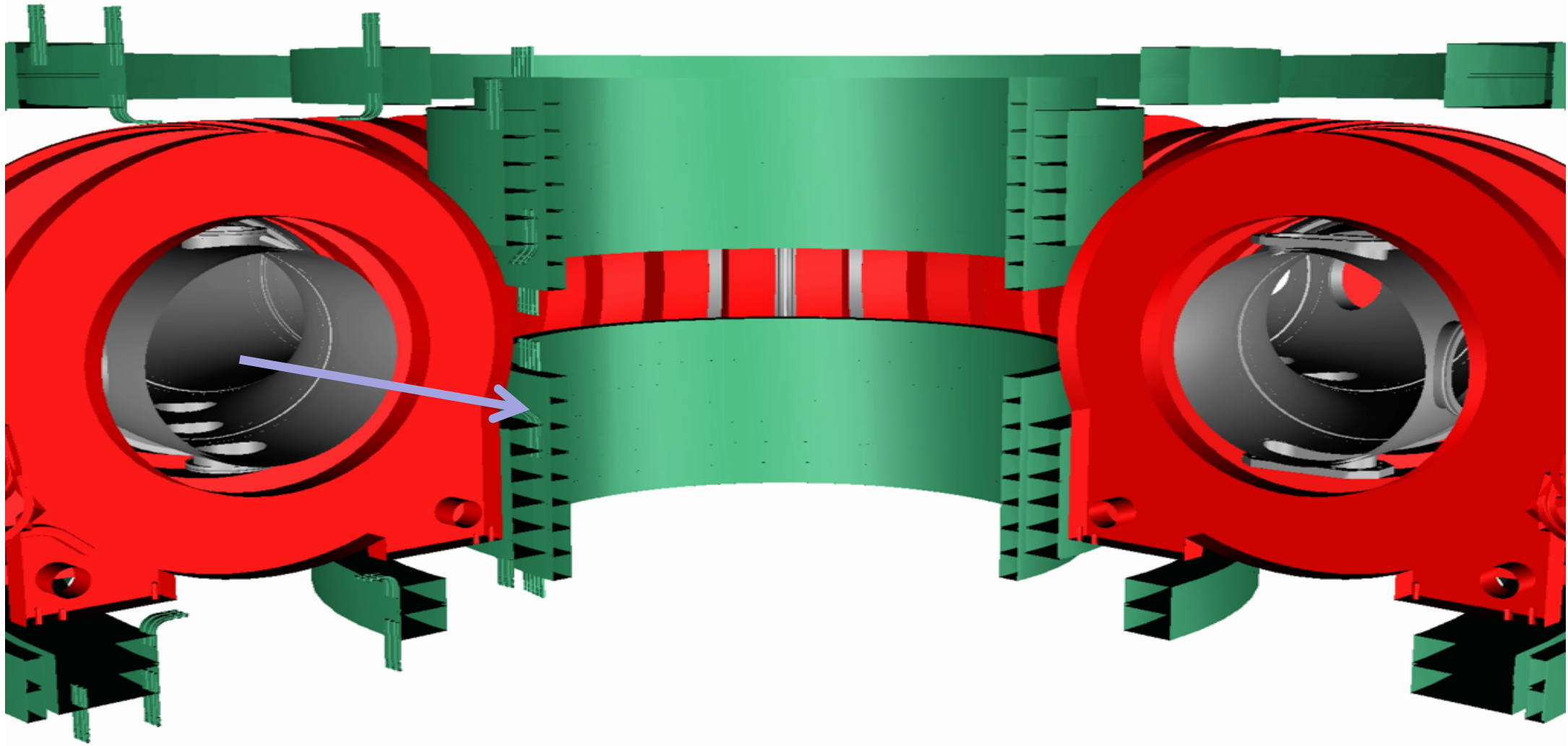
# The TORPEX device

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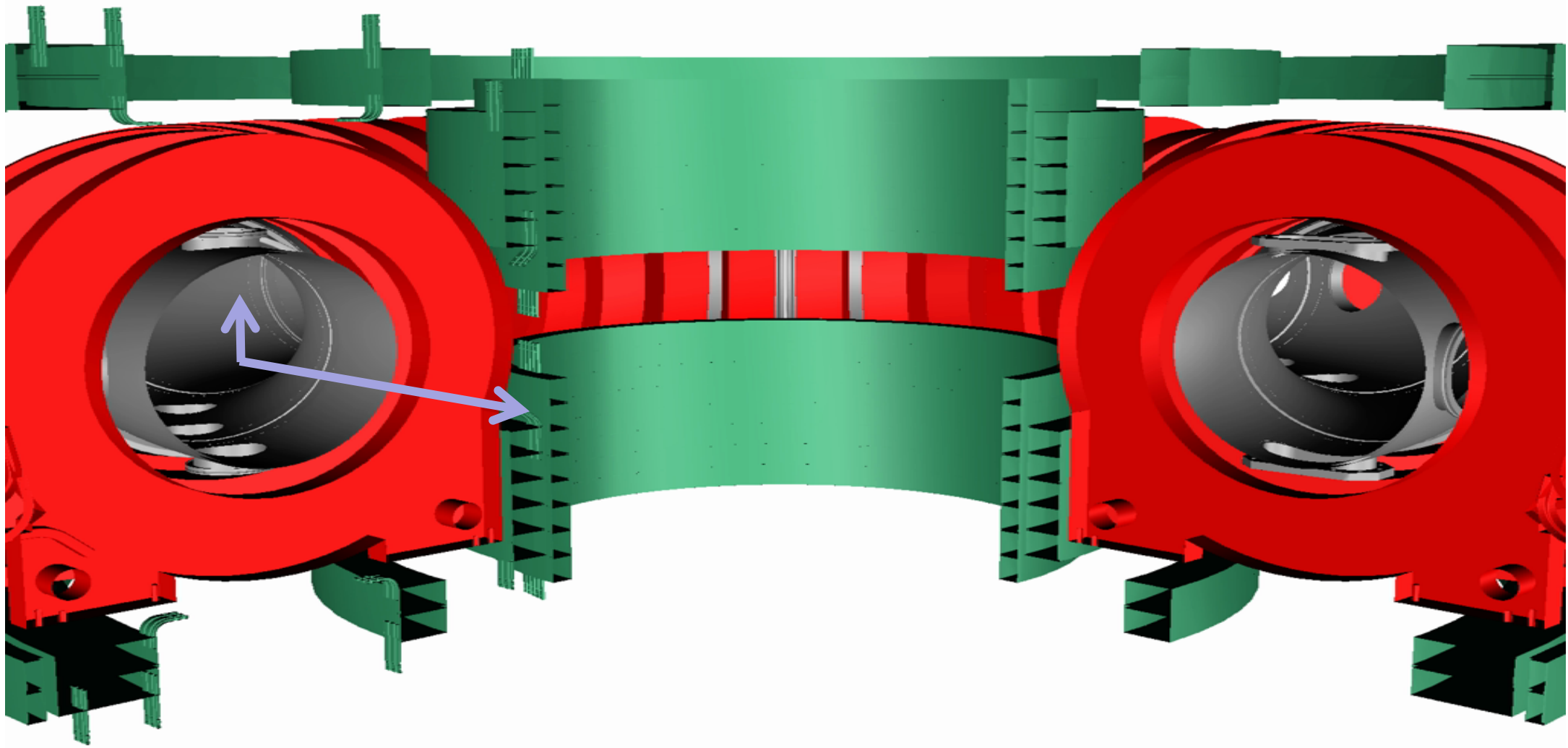
# The TORPEX device

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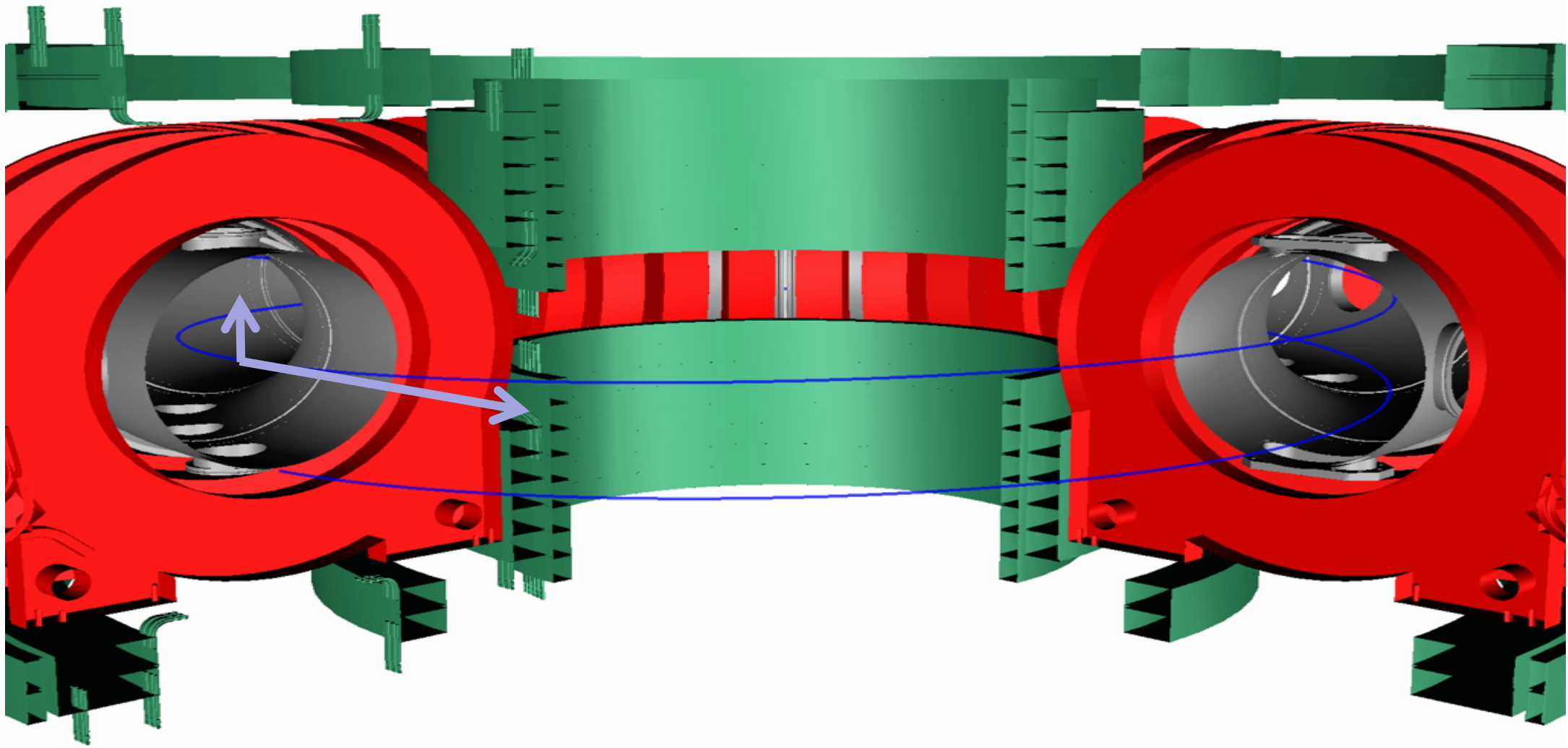
# The TORPEX device

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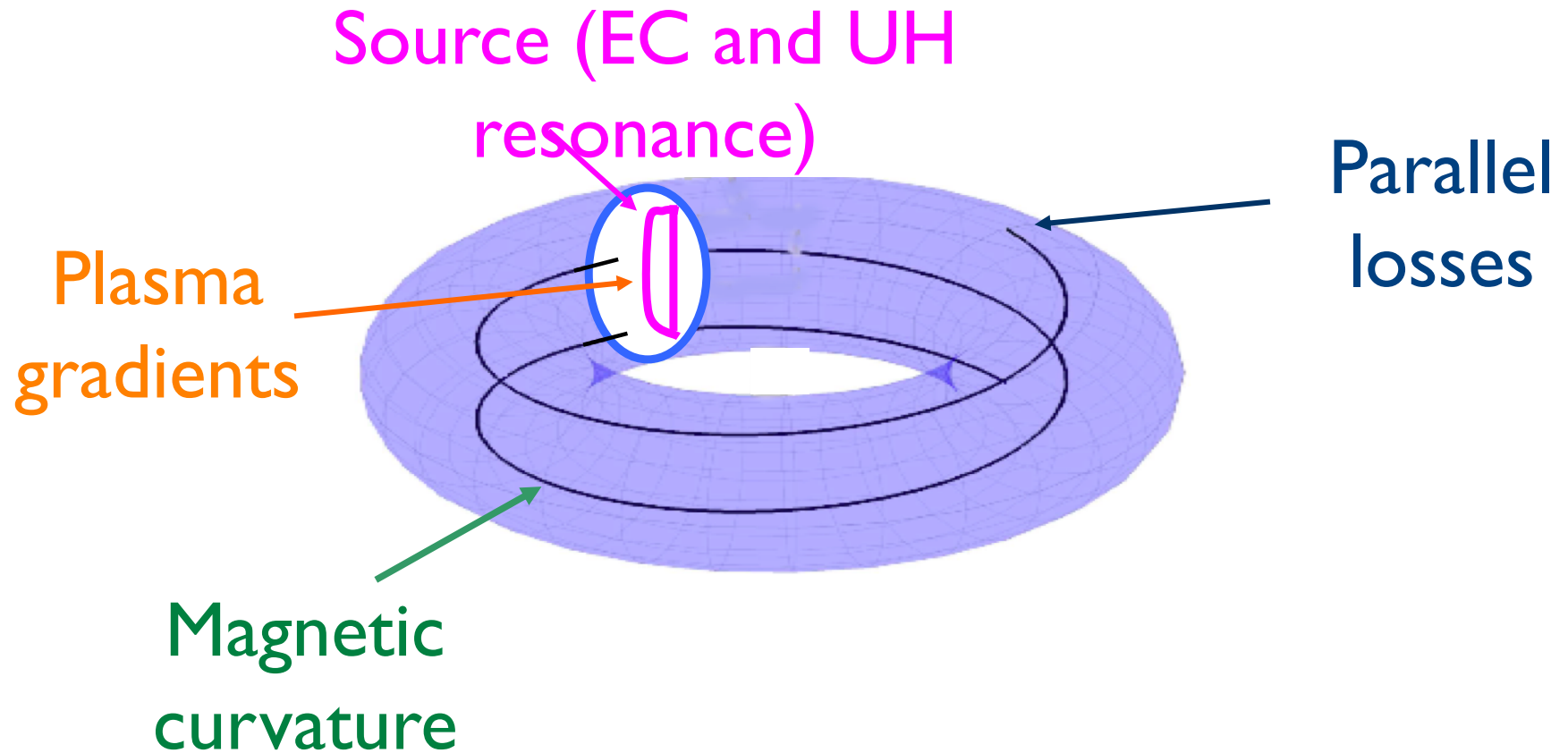
# The TORPEX device

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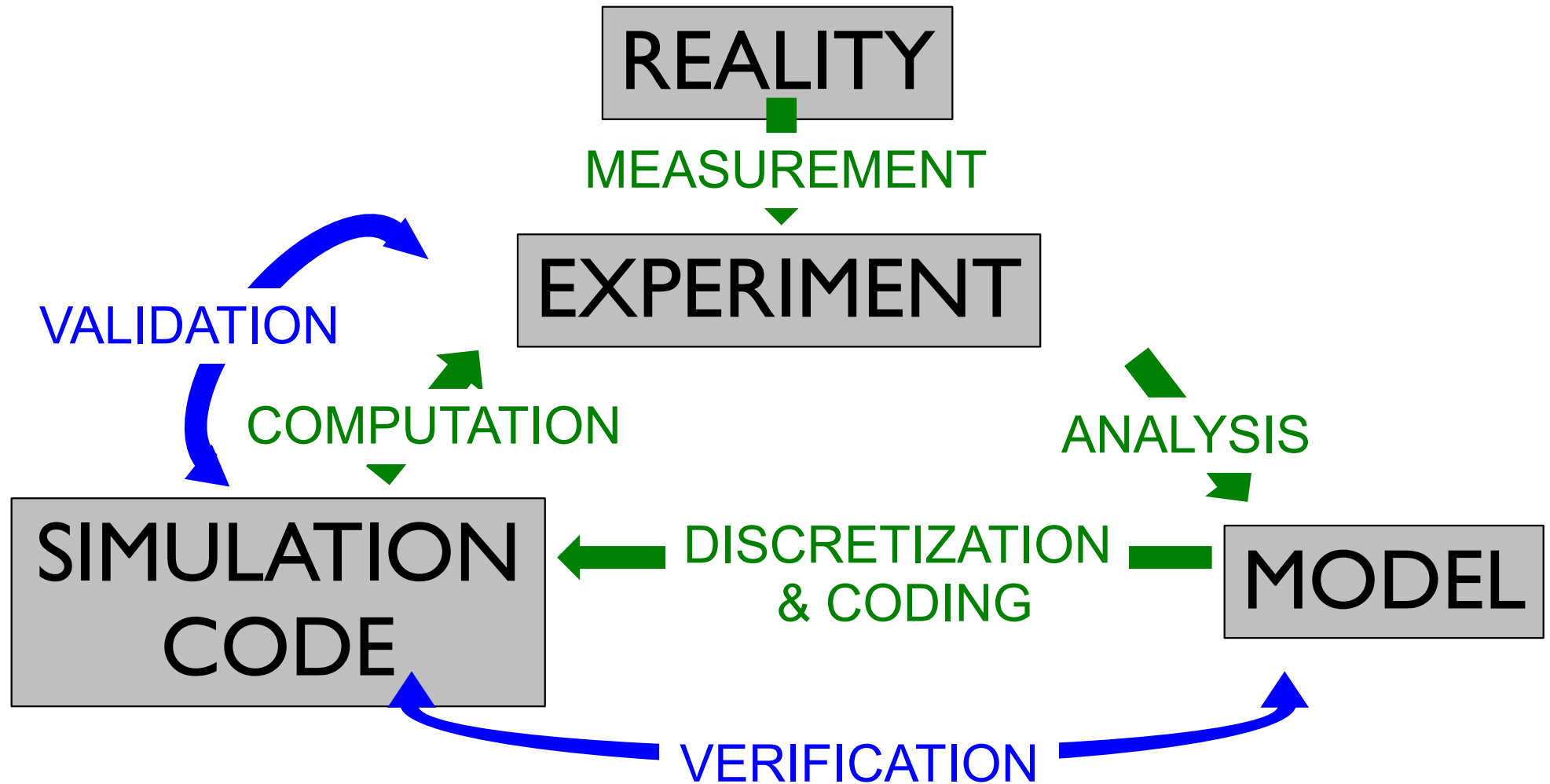


# Key elements of the TORPEX device

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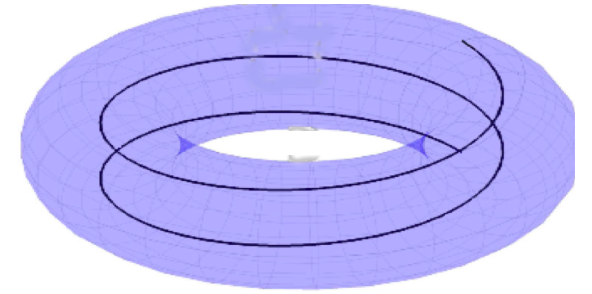


# Verification & Validation

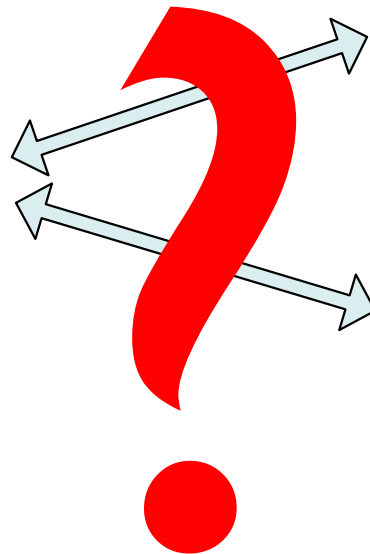




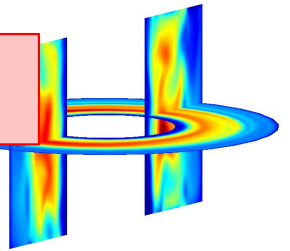
# Our project, paradigm of turbulence code validation



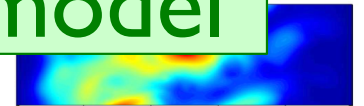
TORPEX



3D GBS model



2D reduced model



What is the agreement of experiment and simulations as a function of  $N$  (number of field line turns)? Is 3D necessary?

What is the agreement of experiment and simulations as a function of  $N$  (number of field line turns)? Is 3D necessary?

# The validation methodology

[Based on ideas of Terry et al., PoP 2008; Greenwald, PoP 2010]

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*What quantities can we use for validation? The more, the better...*

- **Definition & evaluation of the validation observables**

*What are the uncertainties affecting measured and simulation data?*

- **Uncertainty analysis**

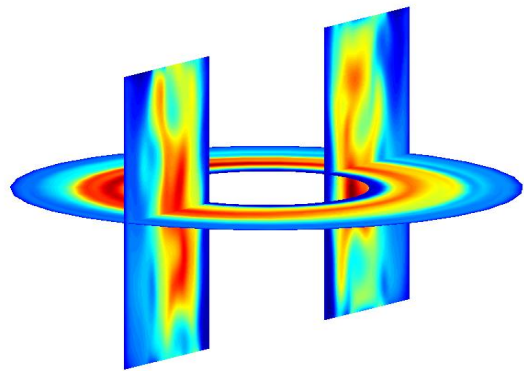
*For one observable, within its uncertainties, what is the level of agreement?*

- **Level of agreement for an individual observable**

*How directly can an observable be extracted from simulation and experimental data? How worthy is it, i.e. what should be its weight in a composite metric?*

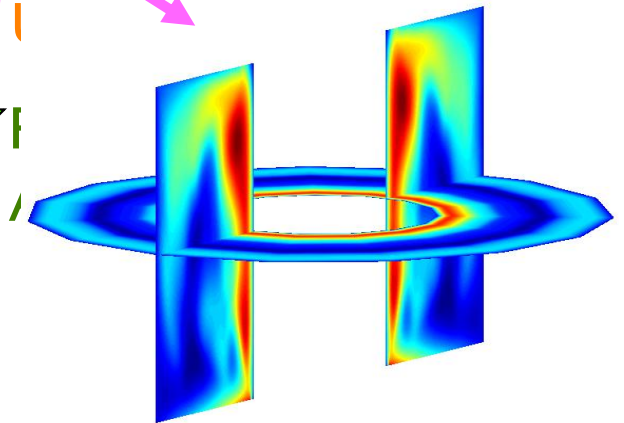
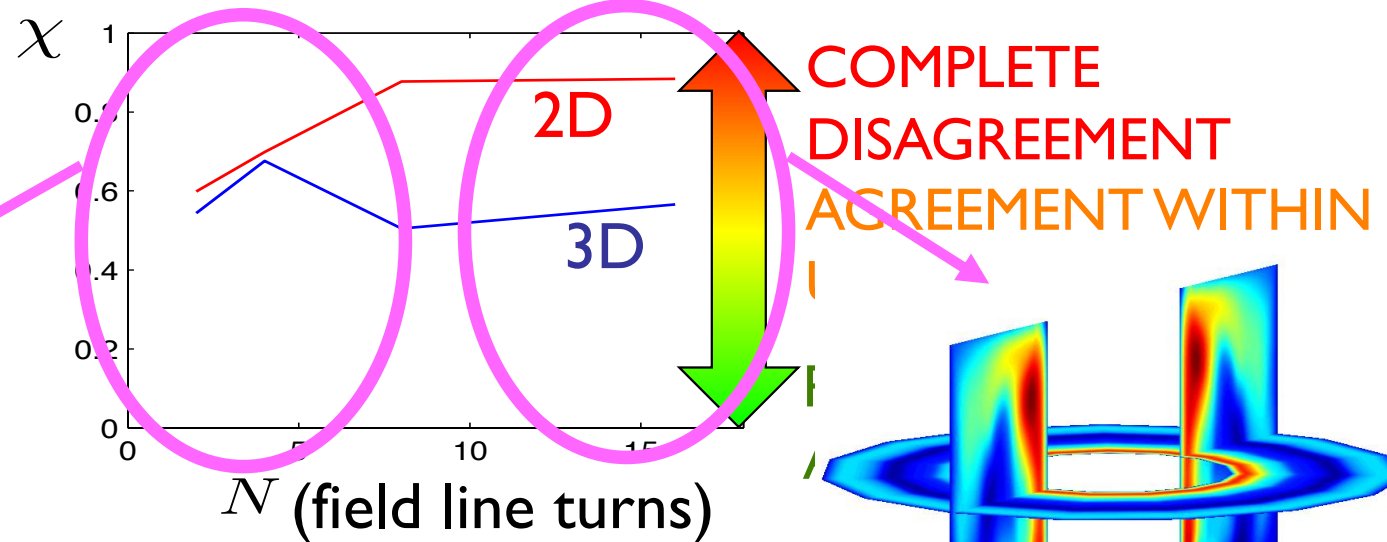
- **The observable hierarchy**

# Interpretation of the validation results



$$k_{\parallel} = 0$$

- Ideal interchange turbulence
- 2D model appropriate

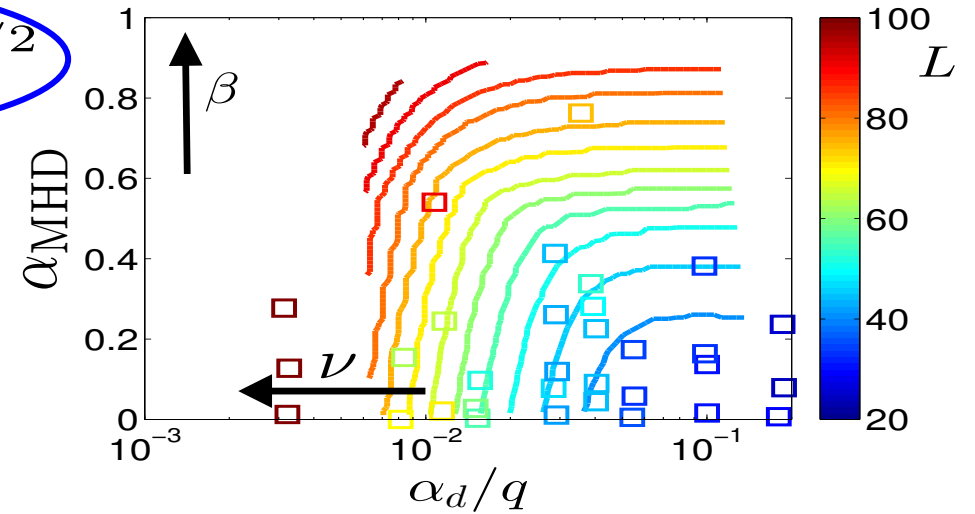


$$k_{\parallel} \neq 0$$

- Resistive interchange turbulence
- 2D model not

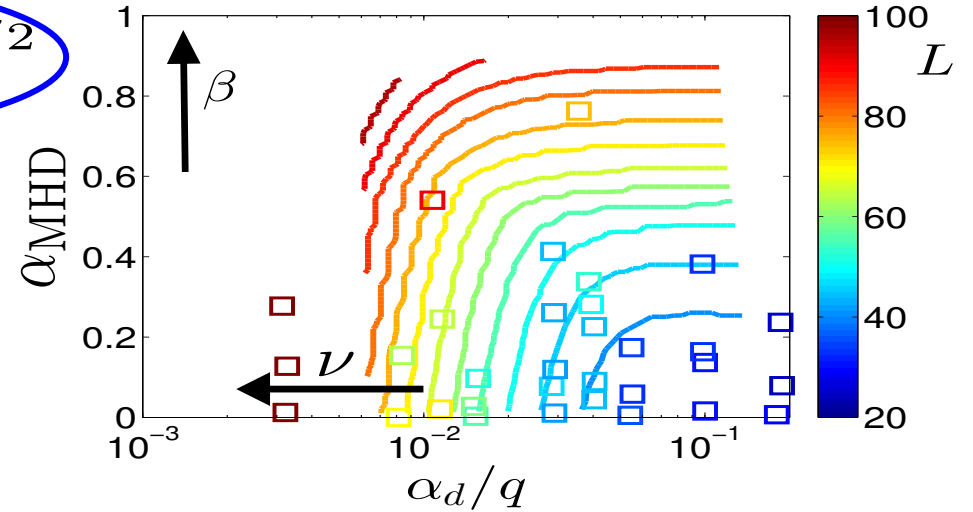
# Limited SOL transport increases with $\beta$ and $\nu$

$$L_p = R^{1/2} [2\pi(1 - \alpha_{\text{MHD}})\alpha_d/q]^{-1/2}$$



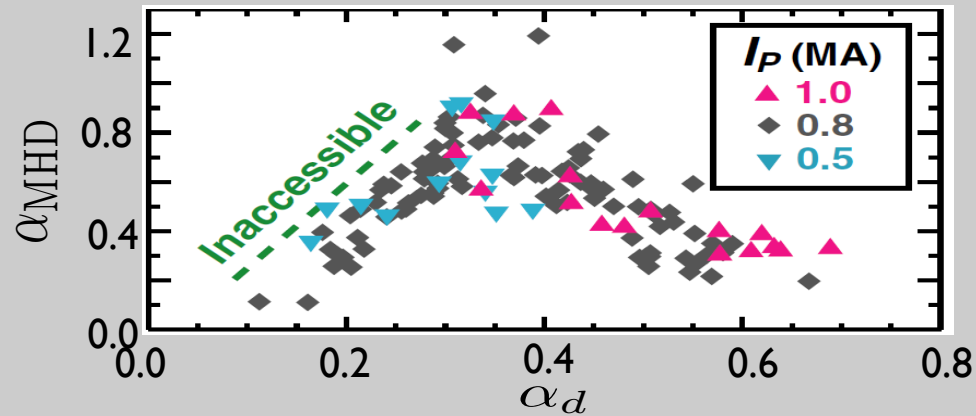
# Limited SOL transport increases with $\beta$ and $\nu$

$$L_p = R^{1/2} [2\pi(1 - \alpha_{\text{MHD}})\alpha_d/q]^{-1/2}$$



Maybe related to the density limit?

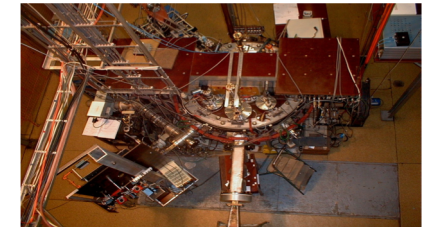
Coupling with core physics needs be



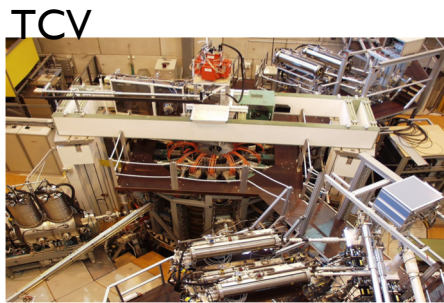
LaBombard, NF 2005

# Limited SOL width widens with $R$

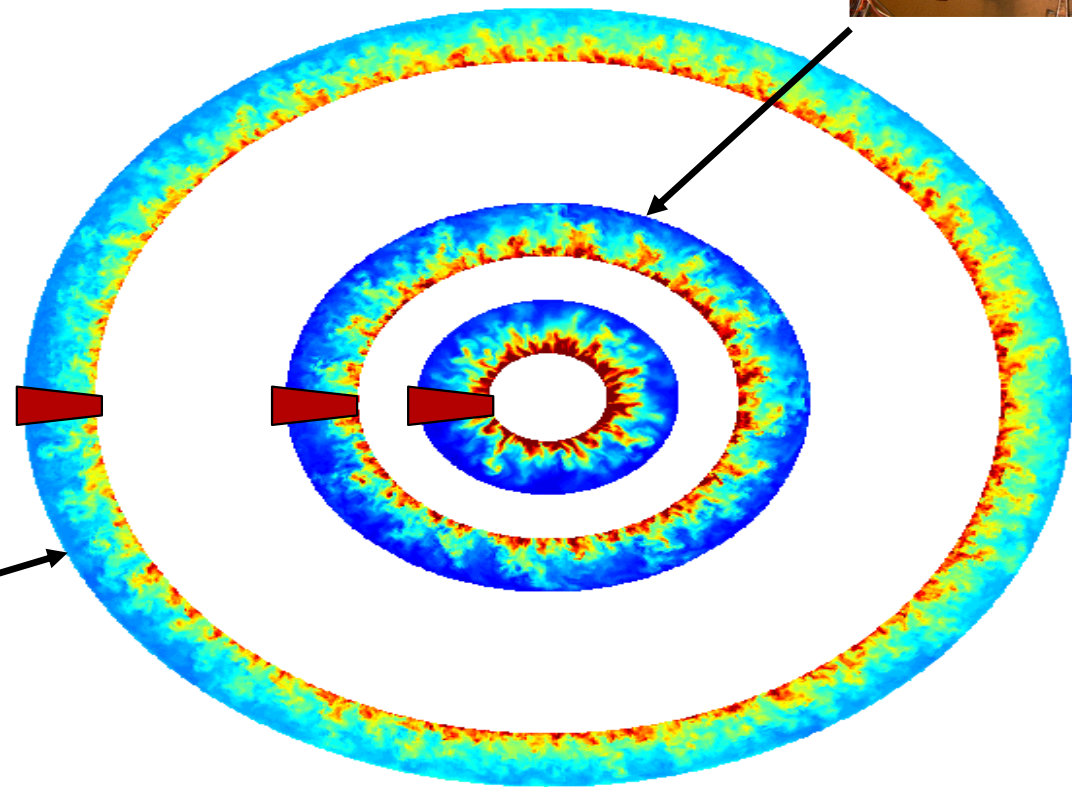
$$L_p = R^{1/2} [2\pi(1 - \alpha_{\text{MHD}})\alpha_d/q]^{-1/2}$$



CASTOR

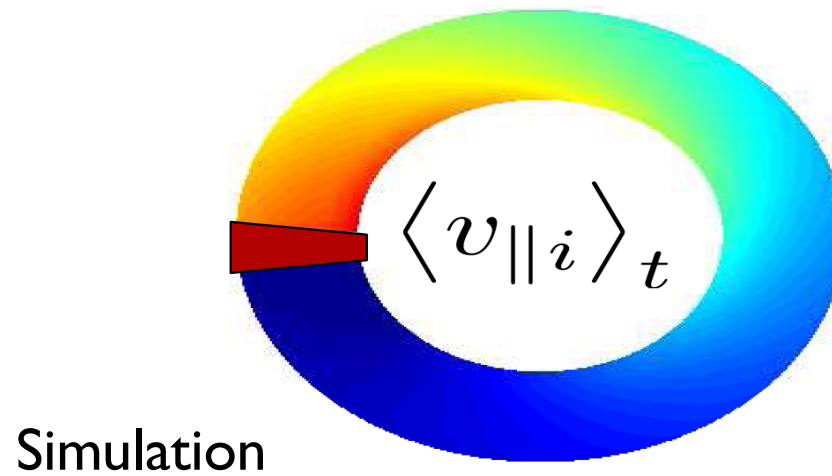
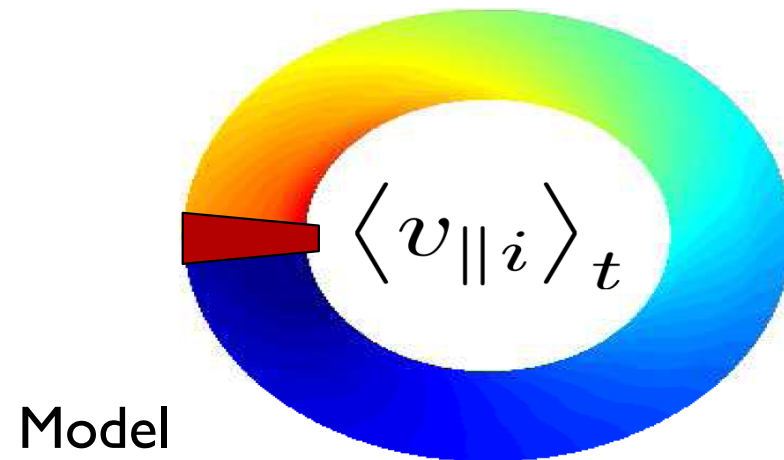


TCV



# Our model well describes simulation results...

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## ... and experimental trends

Analytical solution, far from limiter:

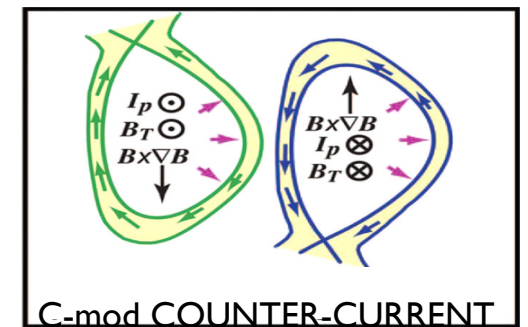
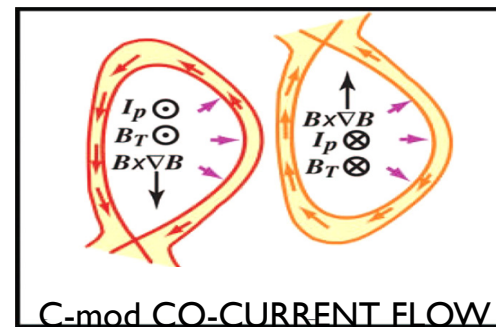
$$M = M_s e^{-r/l} + \left[ \frac{\Lambda}{2\alpha} \frac{\rho_s}{L_T} e^{-r/L_T} - \frac{\sigma_\varphi}{2} \left( \frac{\delta n}{n} + \frac{\delta T}{T} \right) \right] (1 - e^{-r/l})$$

Core  
coupling

Sheath  
contribution,  
co-current

Pressure poloidal asymmetry  
at divertor plates,  
due to ballooning transport,  
direction: depends

- $M_{||} \lesssim 1$
- Typically co-current
- Can become counter-current by reversing **B** or divertor position



Loizu et al., PoP 2014