

1 Estimates for the stiffness, strength and drift capacity of stone masonry walls based on 2 123 quasi-static cyclic tests reported in the literature

3 Francesco Vanin¹⁾, Dario Zaganelli¹⁾, Andrea Penna²⁾, Katrin Beyer¹⁾

4 Abstract

5 This paper summarises 123 existing quasi-static shear-compression tests on stone masonry walls and evaluates the results to
6 provide the input required for the displacement-based assessment of stone masonry buildings. Based on the collected data, existing
7 criteria for estimating lateral strength and stiffness of stone masonry walls are reviewed and improvements proposed. The drift
8 capacity of stone masonry walls is evaluated at six different limit states that characterise the response from the onset of cracking
9 to the collapse of the wall. To provide input data for probabilistic assessments of stone masonry buildings, not only median values
10 but also the corresponding coefficients of variation are determined. In addition, analytical expressions that estimate the ultimate
11 drift capacity either as a function of masonry typology and failure mode or as a function of masonry typology, shear span and axial
12 load ratio are proposed. The paper provides also estimates of the uncertainty related to the natural variability of stone masonry by
13 analysing repeated tests and investigates the effect of mortar injections and the effect of the loading history (monotonic vs cyclic)
14 on stiffness, strength and drift capacities. The data set is made publicly available.

15 **Keywords:** Stone masonry, in-plane behaviour, drift capacity, shear strength, wall stiffness, wall database

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27 1 Introduction

28 Many buildings that are part of the European cultural heritage are stone masonry buildings. Furthermore, stone masonry
29 construction is still used today in several developing countries. Due to the low tensile strength of the mortar and the often poor
30 interlock between stones, stone masonry buildings are among the most vulnerable buildings when subjected to seismic loading
31 (Grünthal 1998). Buildings with stone masonry walls can fail due to in-plane loading, out-of-plane loading or a combination of the
32 two failure modes (Fig. 1). Out-of-plane failure modes are promoted by the large mass of stone masonry walls, the small restraint
33 provided by timber floors and the poor interlock between the stones (D'Ayala and Speranza 2003). They are the most frequent
34 cause for the partial or complete collapse of existing stone masonry buildings during earthquakes and their assessment is therefore
35 of high importance (e.g. Costa et al. 2015). If out-of-plane failures are prevented by appropriate structural details such as anchors
36 and ties, the structure can develop a global response that is governed by the in-plane behaviour of the walls and the diaphragm
37 stiffness (Penna 2015). In-plane failure modes include the failure of piers and spandrels. While the failure of spandrels causes local
38 failures and a global decrease in stiffness and strength, the failure of piers can lead to the collapse of the building (Beyer and
39 Mangalathu 2012). The deformation capacity of the piers is therefore essential when assessing the ultimate limit state of stone
40 masonry buildings.

1 Current codes do not distinguish between different masonry typologies when assessing the drift capacity (for a review of drift
2 capacity models in codes, see Petry and Beyer 2014). Eurocode 8, Part 3 (EC8-3, CEN 2005a) assigns the drift capacity based on
3 the failure mode (shear vs flexure) and the shear span ratio H_0/L where H_0 is the height of zero moment and L the wall length:

Shear failure:
$$\delta_{SD} = 0.4\% \quad (1a)$$

Flexural failure:
$$\delta_{SD} = 0.8\% \cdot \frac{H_0}{L} \quad (1b)$$

4 Although the current version of EC8-3 is limited to concrete and brick masonry (CEN 2005a), due to the lack of alternative values
5 for other masonry typologies, in engineering practice these values are often also applied to stone masonry. Equation (1) gives the
6 drift capacities for the limit state “Significant Damage” (SD). To obtain the drift capacity at 20% strength loss (defined as near
7 collapse limit state, NC), the drift capacities of Eq. (1a) are multiplied by a factor 4/3 (CEN 2005a). Recent works investigated the
8 correlation of these drift capacity models with tests on clay block masonry walls (Pfyl-Lang et al. 2011; Petry and Beyer 2014a).
9 However, the proposed models cannot be applied directly to stone masonry since stone masonry differs from block masonry with
10 regard to the material properties, the shape of the stones, the fabric of the masonry and the number of leaves. Kržan et al. (2014)
11 provide on the basis of three test series minimum and maximum values of drift capacity at the SD and NC limit state but do not
12 differentiate between different types of stone masonry.

13 The objective of this paper is to provide the input data for the wall limit states that is required for the probabilistic displacement-
14 based assessment of stone masonry buildings. While the framework of probabilistic assessment procedures are established (e.g.
15 Dolsek 2009; Vamvatsikos and Fragiadakis 2010), their application to stone masonry buildings is at the moment limited by the
16 lack of information on the distribution of drift capacities. To provide this information, this paper evaluates median values and
17 coefficients of variations of drifts for the following six element limit states:

- 18 - Drift at the onset of cracking δ_{cr}
- 19 - Drift at yield δ_y
- 20 - Drift limit “Significant damage” which is defined as $\delta_{SD} = \min(3\delta_{cr}, \delta_{max})$
- 21 - Drift at maximum force δ_{max}
- 22 - Drift at ultimate LS (20% strength drop) δ_u
- 23 - Drift at collapse (50% strength drop) δ_c

24 The drift at the onset of cracking is the drift for which first cracks were reported. The yield drift results from the bilinear
25 approximation of the force-displacement response (see Section 2.1). The drift at maximum force δ_{max} is relevant as it marks the
26 onset of damage concentration in few cracks (Petry and Beyer 2014b). The definition of the drift limit state “Significant damage”
27 is slightly modified criterion from Tomaževič (2007). For the data set analysed here, the drift limit SD is governed in approximately
28 half of the cases by the limit $3\delta_{cr}$ and in the other half by δ_{max} . The ultimate drift δ_u is defined as the drift at which the strength has
29 dropped to 80% of the peak strength. This is a common definition of the ultimate deformation capacity, which is used for many
30 different structural elements and materials. The definition of collapse, on the other hand, is more subjective. Ideally, it would be
31 related to the loss of axial load bearing capacity. Since this state was not attained by most tests a definition related to the loss in
32 lateral strength was chosen. It is expected that the drift at axial load bearing collapse is only marginally larger given that the strength
33 loss is rapid and shear and axial failures strongly coupled.

34 To determine the probability distributions of these drift capacities and investigate on which parameters the drift capacities depend,
35 this paper collects the results of 123 in-situ and laboratory shear-compression tests on stone masonry walls (Section 2) and evaluates
36 for these the stiffness, the strength and drift capacities (Sections 6-8). The analysis of the test data showed—as it had also been
37 observed for clay block masonry walls (Petry and Beyer 2014a)—that monotonic tests lead to significantly larger drift capacities
38 than cyclic tests while the load history has only little influence on stiffness and strength (Section 4). Since drift capacities are
39 typically used for seismic assessments and therefore cyclic loads, monotonic tests are disregarded when calculating drift capacities
40 (Section 8). All tests are quasi-static tests, i.e., the effect of strain rates on the response of stone masonry walls are beyond the
41 scope of this study.

42 The effect of the variability of stone masonry properties on the seismic assessment of stone masonry buildings can be analysed by
43 means of Monte-Carlo simulations, which assign each building model a different drift capacity for the stone masonry walls (Rota
44 et al. 2014). However, also the walls within a building have different drift capacities due to the natural variability of the stone

1 masonry. To evaluate this aleatoric uncertainty, tests of identical wall configurations are analysed with regard to the variability of
2 stiffness, strength and deformation capacity (Section 3). Seismic assessments often also investigate the effect of a strengthening
3 measures on the performance of a building. The database contains few pairs of strengthened and unstrengthened walls. The
4 strengthening measures aim at improving the integrity of the stone masonry walls by mortar injections or horizontal reinforcements
5 through the wall thickness in order to improve the connection between leaves. Section 5 reviews pairs of unstrengthened and
6 strengthened wall tests and computes ratios for stiffness, strength and drift capacities of strengthened to unstrengthened walls. The
7 paper closes with a discussion of the obtained results. Based on these, future research needs are outlined that aim at improving the
8 understanding of the various parameters that influence the in-plane properties of stone masonry walls.



9

10 **Fig. 1 Stone masonry buildings after the 2009 L'Aquila earthquake that failed due to an out-of-plane mechanism (a, Photo:**
11 **A. Dazio) and an in-plane mechanisms (b, Photo: A. Penna).**

12 2 Database of tests on stone masonry walls

13 The database contains 123 shear-compression tests on stone masonry walls from 16 test campaigns (Table 1). Collected were all
14 shear-compression tests on stone masonry walls that were sufficiently documented in the literature. The database contains both
15 laboratory and in-situ tests. Tests other than shear-compression tests, such as for example diagonal compression tests, were not
16 included. All typologies of stone masonry were considered. However, test units that featured unrepresentatively few stones along
17 the wall length were excluded (Devaux 2008). Furthermore, panels strengthened with intrusive interventions that change
18 consistently their structural behaviour (for example, application of fibre reinforced polymers or jacketing) were not included in the
19 database. For this reason, only tests on walls that were strengthened or retrofitted by injections with lime grouts or by improving
20 the local connections between the wall leaves were considered.

21 The database can be downloaded from the web repository [10.5281/zenodo.812146^a](https://zenodo.org/record/812146). It comprises:

- 22 • A table with
 - 23 ○ characteristic data of the test units (test campaign, type of test, geometry and masonry typology of test units,
24 material properties, Masonry Quality Index as defined in Section 2.2, failure mode).
 - 25 ○ the bilinear approximations of the force-displacement response. The procedure for determining the bilinear
26 approximation is outlined in Section 2.1. - 27 ○ drift capacities for six different limit states. The limit states were defined in Section 1.
- 28 • Cyclic force-displacement curves and envelopes are provided as CSV files; these were available for 110 tests. The data
- 29 was digitised from the test reports using vector graphics software. For one test campaign (Magenes et al. 2010),30 experimental data were directly provided by the authors.

31 The masonry typologies of the test units in the database were classified according to the Italian code (MIT 2009), which
32 distinguishes between five types of stone masonry:

- 33 - Class A: irregular stone masonry, with pebbles, erratic and irregular stone units;
34 - Class B: uncut stone masonry, with external leaves of limited thickness and infill core (three-leaf stone masonry)

^a This database will be part of the European Masonry Database, which the authors are currently establishing in collaboration with Matija Gams (University of Ljubljana).

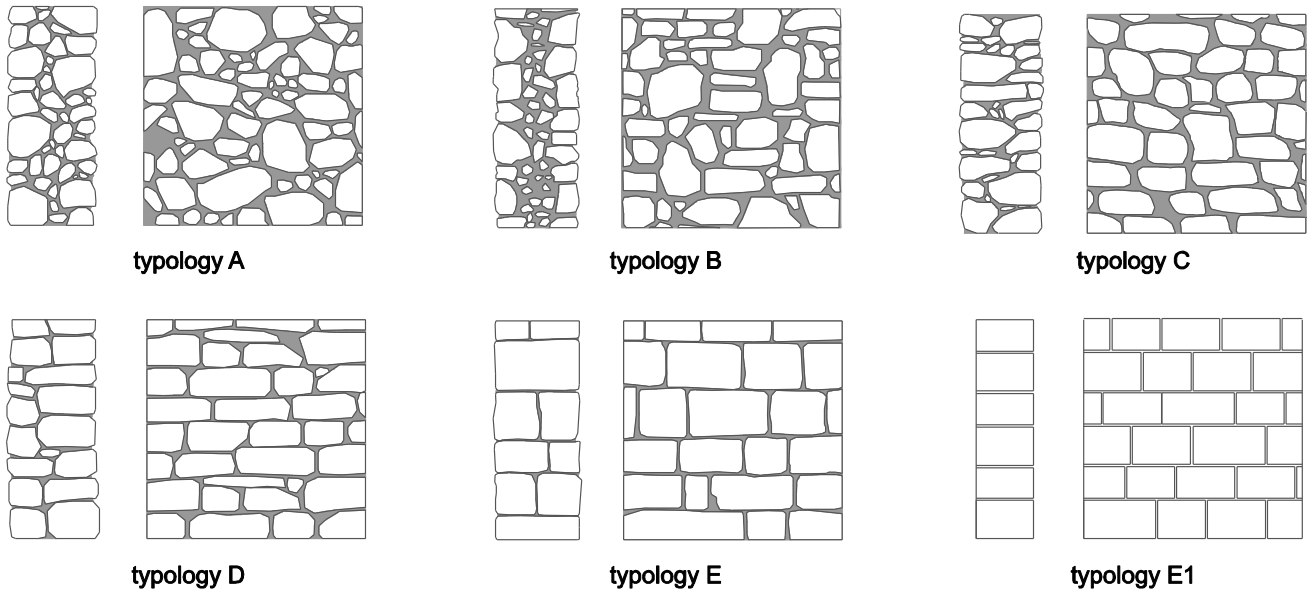
- 1 - Class C: cut stone masonry with good bond
- 2 - Class D: soft stone regular masonry (built with tuff or sandstone blocks)
- 3 - Class E: Ashlar masonry, built with sufficiently resistant blocks (i.e. blocks with higher resistance than those of class D).
- 4 This class was further subdivided into regular squared block masonry with mortar joints (E) and dry-joint ashlar masonry
- 5 (E1).

6 Typical cross-sections of these masonry typologies are shown in Fig. 2.

7 **Table 1 Database with shear-compression tests on stone masonry walls: List of test campaigns.**

Series	References	No. of units	Masonry typology	Test type	Lab./ In-situ
S1	Vasconcelos (2005); Vasconcelos and Lourenço (2009)	28	E1, C	Cyclic, Monotonic	Laboratory
S2	Silva et al. (2014)	16	B	Cyclic	Laboratory
S3	Mazzon (2010)	6	B	Cyclic	Laboratory
S4	Magenes et al. (2010)	5	C	Cyclic	Laboratory
S5	Almeida et al. (2012)	2	E	Cyclic	Laboratory
S6	Borri et al. (2001)	3	A	Monotonic	In-situ
S7	Borri et al. (2012)	10	A	Monotonic	In-situ
S8	Corradi et al. (2014)	2	A	Monotonic	In-situ
S9	Marcari et al. (2007)	4	D	Monotonic	Laboratory
S10	Costa et al. (2011)	1	A	Cyclic	In-situ
S11	Pinho et al. (2012)	6	A	Cyclic, Monotonic	Laboratory
S12	Lourenço et al. (2005)	7	E1	Monotonic	Laboratory
S13	Almeida et al. (2014)	12	E1, C	Cyclic	Laboratory
S14	Kržan et al. (2014)	14	E	Cyclic	Laboratory
S15	Silva et al. (2012)	1	C	Cyclic	Laboratory
S16	Faella et al. (1992)	6	D	Cyclic	Laboratory
	Total	123			

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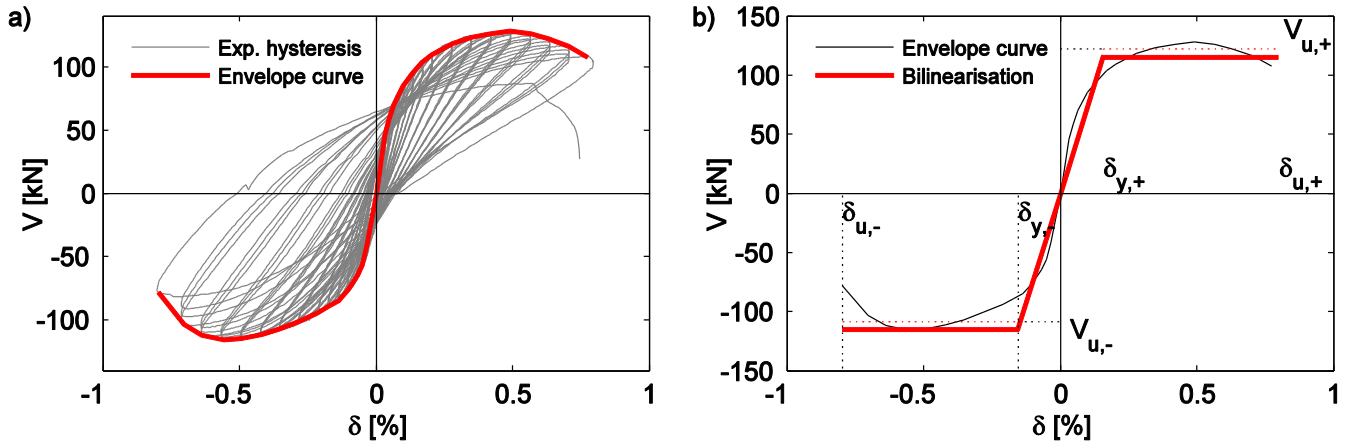
10 **Fig. 2 Stone masonry typologies: sketches of typical textures and cross sections**

11 2.1 Bilinear approximation of the force-displacement curve

12 In shear-compression tests, the axial force is kept constant while the applied horizontal displacement is varied. The loading
 13 protocols for the horizontal displacement differed between the various campaigns and included monotonic tests and reversed cyclic

1 tests. For the monotonic tests (35 tests, for 22 of which the load-displacement curve is available) no processing was required to
 2 obtain the envelope curve. For the reversed cyclic tests with one or three repeated cycles (24 and 57 tests, respectively), the
 3 envelope curves were derived from the digitised force-displacement hysteretic curves by connecting the points at displacement
 4 peaks. When more than one cycle was imposed per displacement amplitude, the first cycle was considered for constructing the
 5 envelope, in order to make results from different loading protocols as comparable as possible. This approach also accounts for the
 6 finding that masonry piers that are part of a building, which is subjected to a real earthquake, are not likely to be subjected to more
 7 than one or two cycles at the highest drift demand (Mergos and Beyer 2014).

8 The bilinear approximation of the envelope curves was computed as described in Fig. 3. First, the maximum recorded strength V_{max}
 9 was identified. The effective stiffness was then defined as the secant stiffness at 70% V_{max} . The ultimate drift δ_u was determined as
 10 the drift at which the strength had dropped to 80% V_{max} . If such a large drop was not attained, the largest drift that was reached
 11 during the test was taken as δ_u . The ultimate strength V_u was defined as the strength that yields for the bilinear approximation the
 12 same area below the curve as the actual envelope up to δ_u . For cyclic tests, bilinear approximations were computed for the envelopes
 13 in the positive and negative loading direction. The final envelope curve was derived as follows: The final effective stiffness and
 14 ultimate strength correspond to the average of the values for the two directions. For the ultimate drift, however, the minimum value
 15 of the ultimate drift in the positive and negative direction was taken. When the force drop was only attained in one direction, the
 16 corresponding ultimate drift was considered for the final envelope. This procedure is similar to the one adopted by Frumento et al.
 17 (2009); unlike by Frumento et al., the envelope of the first cycles was used and not the average of envelopes corresponding to
 18 repeated cycles.



19
 20 **Fig. 3 Example of a force-displacement response curve (a) and definition of effective stiffness, strength and drift capacity**
 21 **based on the envelope of the response (b).**

22
 23 **2.2 Distribution of properties of test units contained within the database**

24 The collected experimental data spans a wide range of test unit configurations (Fig. 4). Most tests were laboratory tests (111 test
 25 units, 90%); in addition, the database contains also 12 in-situ tests on walls that were isolated in an existing building. Of the
 26 laboratory tests, 87 (78%) were cyclic tests and 24 (22%) monotonic tests while 11 out of the 12 in-situ tests were monotonic tests
 27 and only one was a cyclic test. For nine in-situ tests and four laboratory tests only the peak force but not the complete force-
 28 displacement curve was reported (in total 13 tests, i.e., 11%). These tests could therefore only be used for the strength model but
 29 not when evaluating the stiffness and deformation capacity of the walls.

30 Fig. 4a shows the number of tests that is available for each masonry typology. It further shows the portion of monotonic and cyclic
 31 tests. The colour code introduced in this figure with regard to the masonry typology is employed throughout the article. A large
 32 majority of the tests were carried out on relatively small test units with heights between 0.9-1.25 m and only very few tests on
 33 storey-high units (Fig. 4b). The shear span ratio H_0/L varies between 0.5 and 2.0 (Fig. 4c). Most of the masonry typologies that
 34 were tested had a compressive strength less than 5 MPa while few tests of dry stone masonry (E1) had a strength larger than 50 MPa
 35 (Fig. 4d); note that the latter value was obtained from tests on masonry prisms rather than masonry walls or wallettes. The
 36 compressive strength was in 53% of the tests determined from compression tests on walls or wallettes, in 28% of the tests from
 37 prism tests; in 7% of the tests it was assumed based on code provisions (MIT 2009). In 12% of the tests, there was no information

1 on the compression strength available and code guidelines could not be applied because a photo of the test unit was missing. The
2 mortar strength was for all test units, for which this information was available, smaller than 6 MPa (Fig. 4e). The axial stress ratio
3 varies between 0 and 0.6 (Fig. 4f).

4 To account for the individual mechanical characteristics of the stone masonry, Binda and co-workers developed a procedure for
5 assessing the quality of the stone masonry and its compliance to the “rules of the art”, which is based on a visual inspection and
6 the evaluation of local geometric parameters (Binda et al. 2009; Cardani and Binda 2015). Based on these characteristics, Borri
7 and co-workers developed a quantitative quality index (Borri and De Maria 2009; Borri et al. 2015), named Masonry Quality Index
8 (MQI), which has been correlated to the masonry strength (Borri et al. 2011). It accounts for the texture of the masonry by
9 considering the following criteria: i) mechanical properties and conservation state of the stone units, ii) the dimensions of the
10 stones, iii) the shape of the stones, iv) the characteristics of the wall section, including the connection of leaves, v) the horizontality
11 of the bed-joints, vi) the staggering of the vertical joints, vii) the quality and conservation of the mortar joints. These characteristics
12 are evaluated largely qualitatively, according to criteria specified in Borri et al. (2015). One parameter that can be determined
13 quantitatively is the interlock of the units, both in the in-plane and out-of-plane directions, which can be described using the concept
14 of the length of the minimum trace (LMT), as proposed by Doglioni et al. (2009). It is defined as the minimum length of a line
15 passing only through mortar joints, between two points that are vertically aligned and at a distance h_v , generally taken equal to
16 100 cm:

$$\text{LMT} = \frac{\text{Min. trace through joints}}{h_v} \quad (2)$$

17 For the test units in the database, the length of the minimum trace has been determined from photos and is tabulated in the database.
18 The MQI assigns to each criterion a value dependent on whether the criterion is satisfied, partially satisfied or not satisfied. The
19 resulting MQI value varies between 0 and 10. The method differentiates between the behaviour under vertical loads, out-of-plane
20 loading and in-plane loading by assigning different coefficients to the different parameters. The MQI is evaluated for all walls that
21 are included in the database. Fig. 4g shows the distribution of the masonry quality index for in-plane loading that are obtained for
22 the tests in the database. Masonry walls of very good quality are somewhat overrepresented in the database due to the large number
23 of tests on walls that belong to typology E or E1. For masonry strengths smaller than 10 MPa, the MQI correlates well with the
24 masonry compressive strength (Fig. 4g; note that this correlation does not improve if the vertical MQI is plotted). Fig. 4h shows
25 the axial load ratio against the MQI for in-plane loading. These two quantities are not directly related. The figure shows, however,
26 that the test designs resulted in a rather strong correlation between these two variables, i.e., the higher the MQI, the smaller was in
27 general the applied axial load ratio. The dataset constitutes itself out of 16 different test programs that were carried out in different
28 laboratories. As a result, the parameters were not varied in a systematic manner, which will need to be taken into account when
29 interpreting any trends in the data. Since all walls were subjected to relatively small axial stresses in a narrow range ($\sigma_0=0-2$ MPa),
30 the axial stress ratio σ_0/f_c essentially depends on f_c and therefore σ_0/f_c varies strongly with MQI. It will therefore be difficult
31 to distinguish between the influence of MQI and the influence of axial stress ratio σ_0/f_c .

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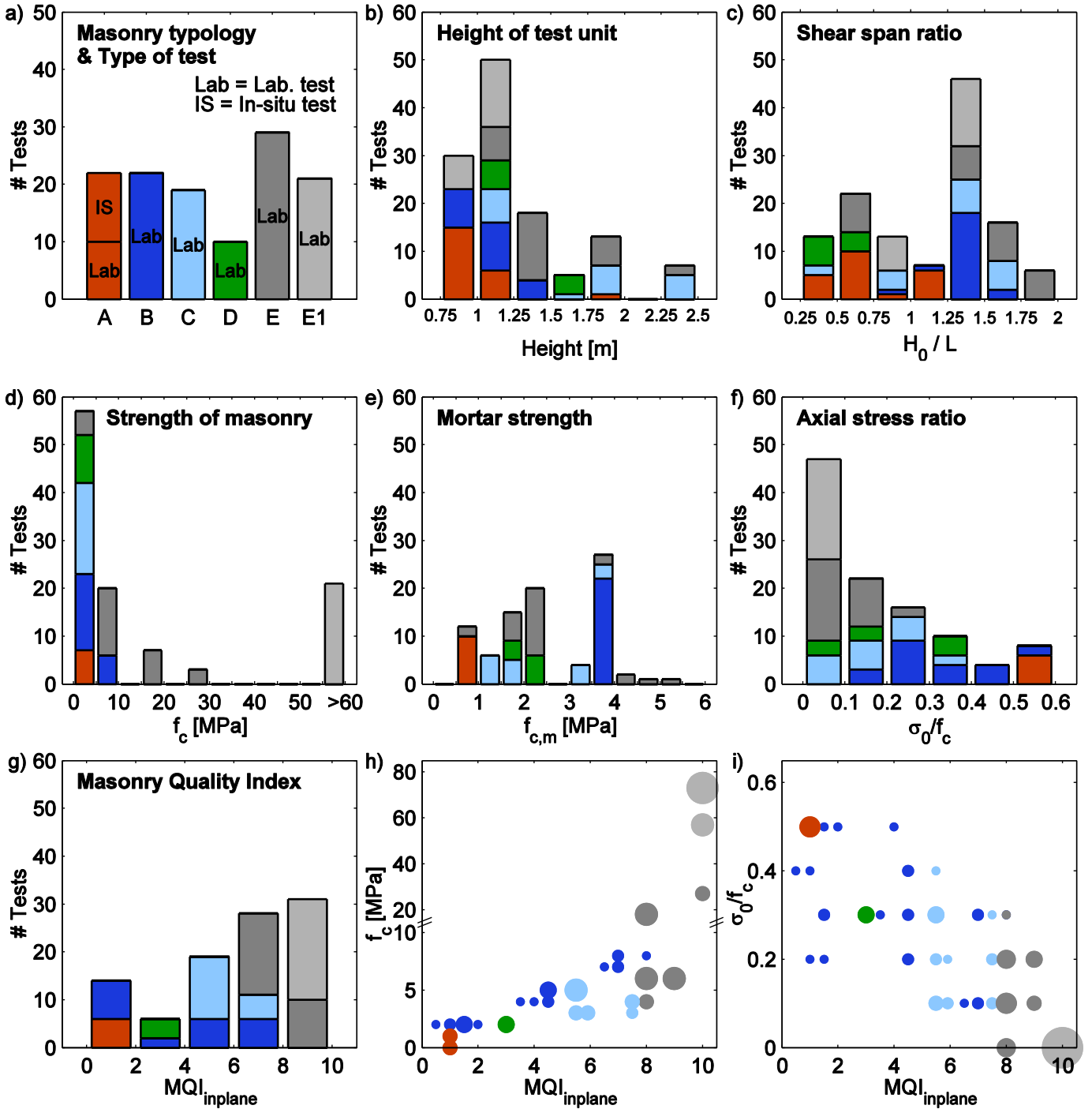


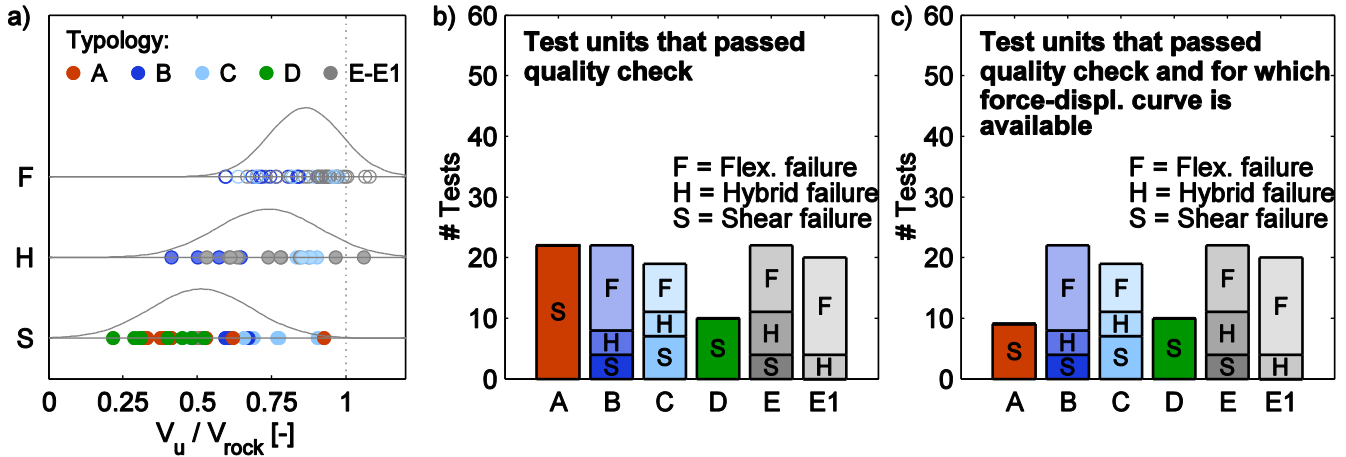
Fig. 4 Database of shear-compression tests on stone masonry walls: Distribution with regard to various parameters. The colours refer to the masonry typology (see plot a). For plots h) and i), the size of the marker relates to the number of test units with the corresponding parameter combination.

2.3 Quality control of measured peak strength

The 16 test series were performed by various research groups using different test setups, which might lead to slightly different boundary conditions. As a quality check of the applied boundary conditions, the peak strength obtained in the tests was compared to the theoretical rocking strength of an infinitely strong rigid body with the same dimensions of the masonry wall:

$$V_{rock} = \frac{NL}{2H_0} \quad (3)$$

1 where N is the axial force, L the wall length and H_0 the shear span. In order to compute an upper limit of the rocking strength, N is
 2 taken as the sum of the applied axial load $\sigma_0 L t$ and an estimate of the self-weight of the test unit. The latter is computed assuming
 3 a specific weight of 20 kN/m^3 for all test units. Fig. 5a shows for all test units the ratio of the ultimate strength V_u , which was
 4 derived from the bilinearisation of the envelope curves, to the rocking strength. Theoretically, the peak strength V_{peak} of masonry
 5 walls let alone the ultimate strength V_u should not be larger than V_{rock} . To allow for small imperfections in the applied boundary
 6 conditions, all tests with ultimate strengths less than 1.10 times V_{rock} are considered when evaluating stiffness, strength and drifts
 7 in the following sections. Eight of the 123 tests do not pass this quality check and are in the following disregarded. Of the 115
 8 retained tests, about half of the test units failed in flexure and half in shear or a hybrid mode. The distribution of the failure modes
 9 with regard to the masonry typologies are shown in Fig. 5b. For masonry typologies A and D only shear failures were observed
 10 while for the other four typologies at least two out of the three failure modes were observed. Fig. 5c shows the tests that passed the
 11 quality check and for which the force-displacement curve is available



12 **Fig. 5 Quality check of shear-compression tests on stone masonry walls: Ratio of maximum shear strength to rocking**
 13 **strength (a), distribution of all tests that passed the quality check (b), distribution of all tests that passed the quality check**
 14 **and for which the force-displacement curve is available.**
 15

16 3 Aleatoric variability of stiffness, strength and drift limits

17 Stone masonry is made of the constituents stone and—unless it is dry masonry—mortar. The properties of both constituents are
 18 subject to a certain natural variability and so is the fabric of stones and mortar that is created by the mason. The properties of stone
 19 masonry walls are therefore associated with an aleatoric uncertainty, which will be estimated in the following. The data set contains
 20 19 groups of replicate tests, i.e., groups of tests in a test series that have been conducted with the same set of parameters (Table 2).
 21 This section evaluates for each of these groups of replicate tests the variability of stiffness, strength and deformation capacity. All
 22 but one of these groups are laboratory tests; for in-situ tests only one group of replicates was available. The number of tests per
 23 group varies between 2 and 4. These group sizes are of course rather small for computing coefficients of variations. The reported
 24 values should therefore be taken as a first estimate of the scatter among replicate tests until results of replicate tests on larger groups
 25 are available.

26 Vasconcelos and Lourenço (2009) tested nine groups of replicates. Fig. 6 shows the force-displacement curves of three groups of
 27 replicates from three different masonry typologies (C, E, E1). The plots show the positive and negative envelopes of each tests,
 28 which confirm that stiffness, strength and deformation capacity vary between the replicate tests. In the following, all 19 groups are
 29 analysed. For the tests shown in Fig. 6, the strength in the negative direction tends to be slightly larger than the strength in the
 30 positive direction indicating that there might have been a slight asymmetry in the test setup. This highlights that even replicate tests
 31 might not yield an estimate of the aleatoric variability that is related to the variability of the material properties and the fabric alone
 32 but that some variability might also be related to imprecisions of the test setup.

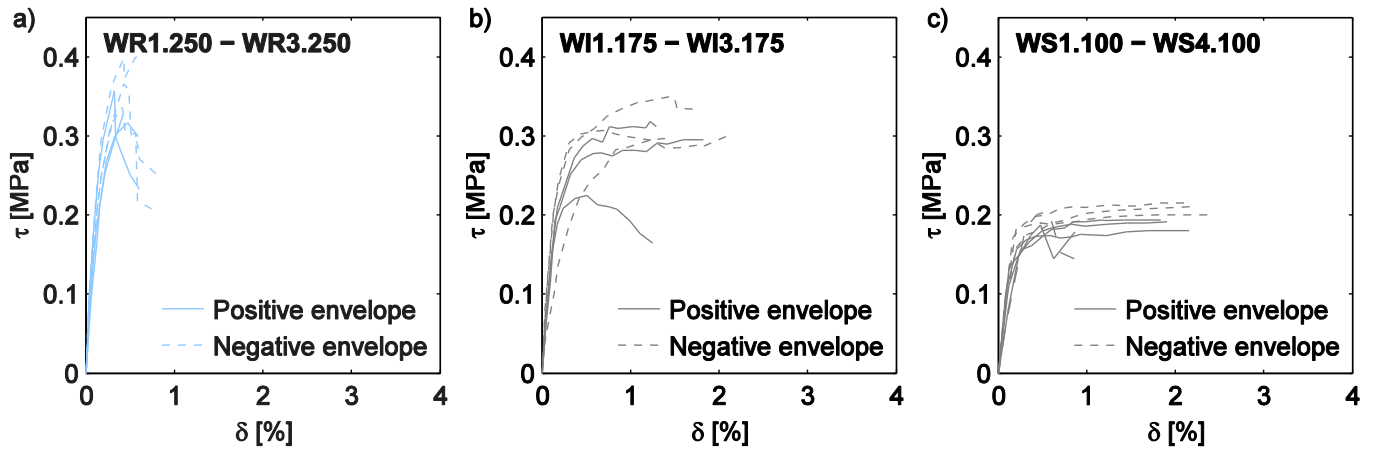
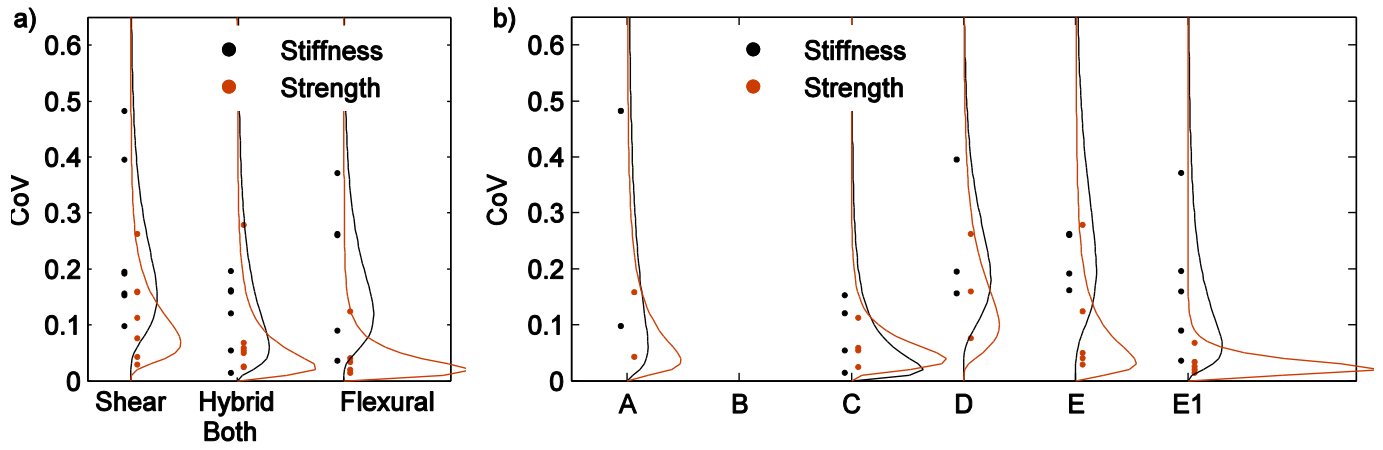


Fig. 6 Force-displacement envelopes of repeated tests by Vasconcelos and Lourenço (2009): Walls of masonry typology C (a), E (b) and E1 (c).

Table 2 summarises the coefficients of variation (CoVs) for all groups of replicates with regard to stiffness, strength and five deformation limits (δ_{cr} , δ_y , δ_{max} , δ_u , δ_c). Fig. 7 and Fig. 8 visualise the distributions of these CoVs by grouping the values according to failure mode and masonry typology. Only one group of replicate tests was carried out as in-situ tests. The obtained values are larger than those obtained from most laboratory tests but not larger than the maximum values obtained from laboratory tests and therefore laboratory and in-situ tests will be treated together. The CoVs of each group of replicates are plotted as a dot. In addition, for each bin the lognormal distribution fitted to these CoVs is plotted. The scatter of the CoVs is rather large but some trends can be identified. Fig. 7a show the CoVs of stiffness and strength as a function of the failure mode. The CoV of the strength is slightly larger for walls that fail in shear than for walls that fail in flexure. For the stiffness, however, both failure types lead to similar CoVs.

The CoVs obtained for the drift limits δ_{max} and δ_u (Fig. 8) tend to be larger than CoVs for stiffness and strength while δ_{cr} leads to a similar CoV. All but two of the replicate groups stem from masonry typologies that have relatively regularly shaped stones and a regular bond pattern (C, D, E, E1). For typologies A and B, the stone pattern is more irregular and therefore one might expect a larger aleatoric variability. The data shows, however, that the masonry typology does not seem to have a significant influence on the aleatoric variability of the drift values. The data base for the irregular masonry typologies A and B is very scarce (A: two groups of replicate tests, B: none) and therefore the influence of the masonry typology on the aleatoric variability cannot be conclusively answered with the available data. If estimates of the aleatoric variability of stiffness, strength and deformation limits are sought for the computation of fragility curves of a class of buildings or the probabilistic seismic assessment of a specific building, it is suggested to use the values given in Table 3. These values are based on the mean values of the CoVs and rounded to the next 0.10. Note also that no test data is available for characterising the aleatoric variability of the drift at collapse since none of the tests was continued up to a 50% drop in strength.

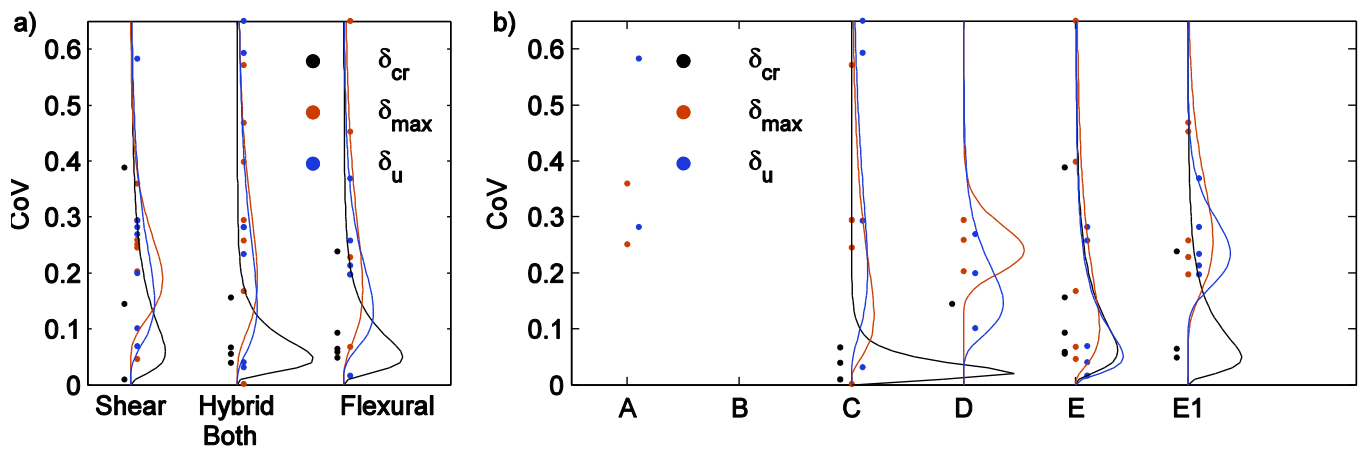


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Fig. 7 Coefficients of variation of replicate tests for effective stiffness K_{eff} ultimate strength V_u as a function of the failure mode (a) and the masonry typology (b).



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Fig. 8 Coefficients of variation of replicate tests for the drift at the onset of cracking δ_{cr} , the drift at maximum strength δ_{max} and the ultimate drift δ_u as a function of the failure mode (a) and the masonry typology (b).

1 **Table 2 Coefficients of variation of replicated tests for effective stiffness, strength and drift values at five limit states (δ_{cr} -**
 2 **δ_u).**

Reference	Test units	Typ.	Units	Type of test	Failure modes	CoV K_{eff}	CoV V_u	CoV δ_{cr}	CoV δ_y	CoV δ_{SD}	CoV δ_{max}	CoV δ_u
Borri et al. (2001)	B-T-04-OR, P-T-15-OR	A	2	In-situ	S	0.48	0.16	-	0.34	0.36	0.36	0.58
Pinho et al. (2012)	M5, M12, M20	A	3	Lab.	S	0.10	0.04	-	0.07	0.25	0.25	0.28
Vasconcelos and Lourenço (2009)	WR1.100, WR2.100	C	2	Lab.	F, H	0.01	0.05	0.07	0.04	0.57	0.57	0.59
Vasconcelos and Lourenço (2009)	WR1.175, WR2.175	C	2	Lab.	F, H	0.05	0.06	0.04	0.00	0.00	0.00	0.03
Vasconcelos and Lourenço (2009)	WR1.250 - WR3.250	C	3	Lab.	S	0.15	0.11	0.01	0.17	0.24	0.24	0.29
Magenes et al. (2010)	CS00, CS02 ¹	C	2	Lab.	F, H	0.12	0.02		0.10	0.29	0.29	0.65
Faella et al. (1992)	T1-1, T1-2, T2-1	D	3	Lab.	S	0.16	0.08	0.00	0.12	0.20	0.20	0.20
Marcari et al. (2007)	P#1 - P#4	D	4	Lab.	S	0.40	0.26	0.14	0.15	0.29	0.29	0.27
Vasconcelos and Lourenço (2009)	WI1.100, WI2.100	E	2	Lab.	F	0.26	0.04	0.09	0.30	0.07	0.07	0.02
Vasconcelos and Lourenço (2009)	WI1.175 - WI3.175	E	3	Lab.	F	0.26	0.12	0.06	0.19	0.65	0.65	0.26
Vasconcelos and Lourenço (2009)	WI1.250, WI2.250	E	2	Lab.	F, H	0.16	0.05	0.06	0.11	0.17	0.17	0.04
Krzan et al. (2015)	test 3 - test 6 ²	E	4	Lab.	H	0.69	0.28	0.16	0.56	0.40	0.40	0.28
Krzan et al. (2015)	test 7 - test 10 ²	E	4	Lab.	S	0.19	0.03	0.39	0.16	0.05	0.05	0.07
Lourenço et al. (2005)	SW.100.1, SW.100.2	E1	2	Lab.	F, H	0.20	0.07	-	0.13	0.26	0.26	0.28
Lourenço et al. (2005)	SW.200.1, SW.200.2	E1	2	Lab.	H	0.16	0.03	-	0.13	0.47	0.47	0.23
Vasconcelos and Lourenço (2009)	WS1.100 - WS4.100	E1	4	Lab.	F	0.37	0.03	0.24	0.42	0.45	0.45	0.37
Vasconcelos and Lourenço (2009)	WS1.175 - WS3.175	E1	3	Lab.	F	0.09	0.02	0.07	0.10	0.23	0.23	0.21
Vasconcelos and Lourenço (2009)	WS1.250 - WS3.250	E1	3	Lab.	F	0.04	0.01	0.05	0.05	0.20	0.20	0.20
Min.			2			0.01	0.01	0.00	0.00	0.00	0.00	0.02
Max.			4			0.69	0.28	0.39	0.56	0.65	0.65	0.65
Mean						0.22	0.08	0.11	0.17	0.29	0.29	0.27
Median						0.16	0.05	0.07	0.13	0.26	0.26	0.27
Standard deviation						0.79	0.99	0.97	0.84	0.60	0.60	0.69

3 ¹Masonry strength differed between the two test units (internal information; not reported in Magenes et al. (2010).

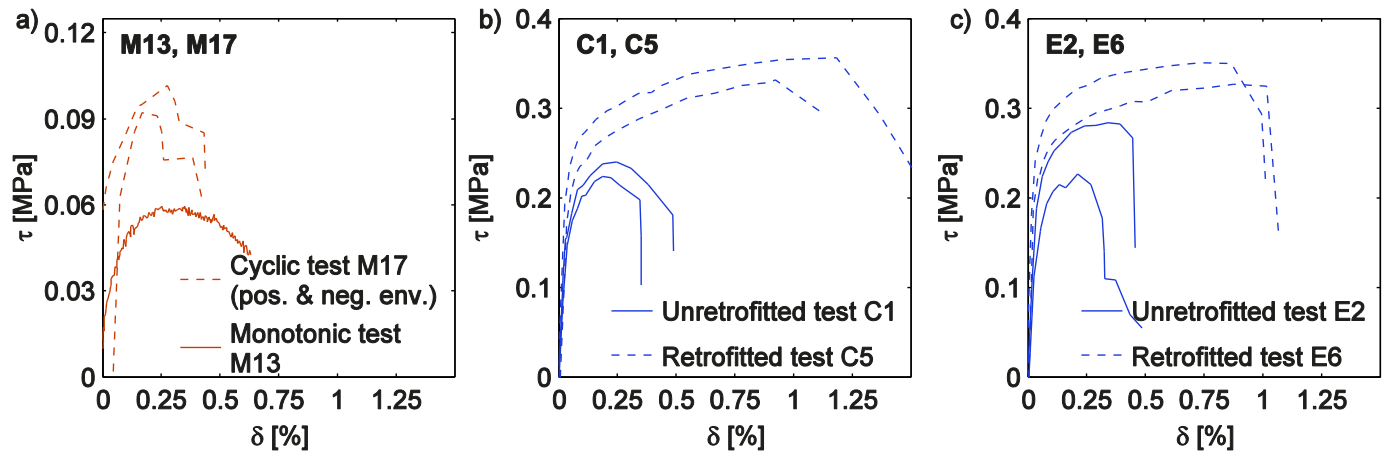
4 ²Two out of the four test units were constructed with through-stones, the other two without. Since the through-stones did not seem
 5 to influence the force-displacement response significantly the four tests are treated as one group of replicates.

1 **Table 3 Recommended values for coefficient of variations for effective stiffness, strength and drift limits.**

Masonry typology & Failure mode	CoV K_{eff}	CoV V_u	CoV δ_{cr}	CoV δ_y	CoV δ_{SD}	CoV δ_{max}	CoV δ_u	CoV δ_c
A – E1	0.20	0.10	0.10	0.20	0.30	0.30	0.30	-

2 **4 Effect of load history on stiffness, strength and drift limits**

3 Among the 115 tests that passed the quality check there is only one pair of monotonic and cyclic tests (M13 and M17 by Pinho et
 4 al. 2012). Fig. 9a shows the force-displacement relationships of these two tests. It shows that test units subjected to cyclic loads
 5 tend to be stiffer and exhibit a smaller drift capacity—trends that were also confirmed by tests on clay block masonry walls, for
 6 which three pairs of monotonic and cyclic tests are reported in the literature (Petry and Beyer 2014a). For clay block masonry
 7 walls, however, the strength of walls subjected to cyclic loads was similar to that subjected to monotonic loading while for the
 8 stone masonry pair the cyclic test led to a significantly larger strength than the monotonic test. At present, a systematic study on
 9 the influence of the loading history on unreinforced masonry wall response is missing. Not only a comparison of monotonic and
 10 cyclic response would be of interest, but also the influence of the number of cycles as there is evidence that most quasi-static cyclic
 11 tests on masonry walls were carried out with more cycles than what would be representative of moderate or even high seismicity
 12 (Beyer et al. 2014; Mergos and Beyer 2014).



13
 14 **Fig. 9 Comparison of force-displacement relationship of monotonic and cyclic tests (a) and strengthened and**
 15 **unstrengthened test units (b, c).**

16 **5 Effect of strengthening interventions on stiffness, strength and drift limits**

17 The dataset comprises 19 test units that were strengthened. For four of these, a non-strengthened counterpart was tested applying
 18 the same axial load and shear span (Silva et al. 2012; Silva 2012). All of these four test units were strengthened by injecting a
 19 hydraulic lime-based grout into the voids of the wall section, which was a three-leaf wall with rubble core. The strengthening
 20 interventions were performed on the undamaged test units. Table 4 shows the ratios of properties of the strengthened to the
 21 unstrengthened test units. The number of pairs is too small to draw any statistically significant conclusions and the results are also
 22 expected to vary significantly with the retrofit intervention. The available results show that retrofitting through grout injections has
 23 the largest impact on the deformation capacity and it is particularly significant if the failure mode changes from shear to flexure.
 24 Note that while the applied axial load was the same for each pair, the axial load ratio was smaller for the strengthened specimens
 25 since their compressive strength was larger.

26

1 **Table 4 Pairs of strengthened and unstrengthened test units: Ratio of properties of strengthened to unstrengthened test**
 2 **unit.**

Reference	Labels of unstrengthened and strengthened test units		Typ.	Failure mode of unstrengthened and strengthened test units		Intervention	Ratio of properties of strengthened to unstrengthened test unit					
	Unstr.	Str.		Unstr.	Str.		f_c	K_{eff}	V_u	δ_{cr}	δ_{max}	δ_u
Silva (2012)	C1	C5	B	Shear	Flex.	Injected	1.7	0.8	1.5	3.5	6.3	4.3
Silva (2012)	C2	C7	B	Shear	Flex.	Injected	1.7	1.7	2.0	2.6	5.8	6.2
Silva (2012)	E2	E6	B	Flex.	Flex.	Injected	2.0	1.5	1.3	1.9	3.5	3.2
Silva (2012)	E4	E5	B	Flex.	Flex.	Injected	2.0	1.0	1.4	1.8	2.5	2.6
Mean values				Shear	Flex.		1.7	1.3	1.8	3.0	6.0	5.3
Mean values				Flex.	Flex.		2.0	1.3	1.3	1.8	3.0	2.9
Italian code: Ratios for typology B (MIT 2009)						Injected	1.7	1.7	1.7	-	-	-

3 **6 Stiffness of stone masonry walls**

4 Force-based and displacement-based assessment procedures require as input an estimate of the horizontal stiffness of structural
 5 walls. The stiffness is needed to compute the dynamic properties of a building as well as its force-displacement response. The
 6 initial uncracked stiffness is only of interest in engineering practice if nonlinear structural models can account explicitly for the
 7 stiffness degradation after cracking of the element. In all other cases, i.e. for simplified structural models (bilinear models for each
 8 structural element) or force-based assessment procedures, the effective stiffness is of interest. However, in the absence of better
 9 models, current codes suggest to estimate the effective stiffness as a ratio of the elastic uncracked stiffness (e.g. CEN 2005b) which,
 10 therefore, should be determined with sufficient accuracy.

11 This section computes from the force-displacement envelopes the ratio of effective to uncracked stiffness and compares the
 12 obtained values to code estimates (Section 6.1). The remainder of the section evaluates different methods of estimating the E-
 13 modulus. First, the median values and CoVs of the E-modulus are computed for the various masonry typologies (Section 6.2).
 14 Second, the E-modulus is computed from results of compression tests and dynamic identification tests that were carried out as part
 15 of the experimental campaigns (Section 6.3). The so obtained E-moduli are compared to compute the horizontal stiffness of the
 16 walls and conclusions drawn on which kind of tests are suitable for obtaining estimates of E-moduli. When assessing a masonry
 17 building, in-situ tests to determine the elastic properties, such as flat-jack tests, are often not available and their use can be
 18 questionable for multiple-leaves stone masonry. It can be necessary, hence, to estimate the E-modulus from the compressive
 19 strength of the masonry, which is often the first material parameter that is determined from tests or assumed based on code values.
 20 Section 6.4 proposes such an expression, which also accounts for the effect of the axial load ratio on the effective stiffness. The
 21 last section compares the different approaches for estimating the stiffness with regard to the bias and coefficient of variations
 22 (Section 6.5).

23 **6.1 Ratio of effective to uncracked stiffness**

24 Current codes estimate the effective stiffness postulating a constant ratio between initial uncracked stiffness and effective stiffness;
 25 EC8-3 recommends a ratio of 0.5 (CEN 2005b) and the Swiss guidelines SIA D0237 a ratio of 0.3 (Pfyl-Lang et al. 2011). To
 26 check the applicability of these assumptions, the experimental initial uncracked stiffness was calculated from the envelopes as the
 27 secant stiffness at 15% of the maximum force; for cyclic tests, the average of the stiffness derived from the positive and negative
 28 envelopes is considered. Similarly, the effective stiffness was defined as the secant stiffness at 70% of the maximum force. Fig.
 29 10a shows the ratios of effective to elastic stiffness that were obtained from the wall tests. The variation is rather large for all failure
 30 modes and slightly larger for walls failing in shear or a hybrid mode than for walls failing in flexure. Clear differences between
 31 masonry typologies could not be identified. Table 5 summarises the experimentally determined ratios; despite the large uncertainty,
 32 a value of 0.5, as suggested by EC8, is close to a mean estimate for all failure modes.

1 **Table 5 Experimental determination of effective to elastic stiffness ratio.**

Experimental ratio of effective to elastic stiffness	Experimental failure mode		
	Shear	Hybrid	Flexure
Average $K_{eff}^{exp}/K_{el}^{exp}$	0.59	0.50	0.53
CoV	0.51	0.45	0.41

2

3 **6.2 E-modulus as a function of the masonry typology**

4 For all tests, for which the force-displacement curve was reported, the E-modulus of the masonry can be back-calculated from the
5 horizontal stiffness of the wall. Generally, the stiffness of masonry walls is computed by means of Timoshenko beam models,
6 which account for both flexural and shear deformability with the latter being particularly relevant for the typical slenderness ratios
7 of masonry piers. Applying the Timoshenko beam theory, the elastic stiffness K_{el} of a wall with a rectangular cross section with a
8 height H and shear span H_0 that is subjected to a horizontal force at its top is:

$$K_{el} = \frac{1}{\frac{H^3}{2EI} \left(\frac{H_0}{H} - \frac{1}{3} \right) + \frac{6H}{5GLt}} \quad (4)$$

9 where E and G are the Young modulus and the shear modulus of the masonry, which is idealised as a homogeneous continuum.
10 For back-calculating the E-modulus from the measured stiffness, it was necessary to assume a ratio of the G- to E-modulus.
11 Eurocode 6 (CEN 2005b) recommends a ratio G/E of 0.4 for all types of masonry if a better estimate is not available. Much lower
12 G/E -ratios, in the range 0.06-0.25, are reported in the literature (e.g. Tomažević 1999). According to the elasticity theory of
13 homogenous isotropic materials the maximum Poisson ratio is 0.5 and therefore the minimum G/E -ratio 0.33. Considering the
14 composite anisotropic nature of the masonry material, smaller G/E -ratios are, however, possible. The Italian code (MIT 2009)
15 assumes for most stone masonry typologies a ratio of G/E equal to 0.33 and this ratio was also adopted here. Based on this
16 assumption, the E-modulus can be computed from the experimental stiffness of the wall:

$$E_{exp} = K_{exp} \frac{6/5 H \cdot \left[1 + 5 \left(\frac{H_0}{H} - 1/3 \right) \cdot G/E \cdot \left(\frac{H}{L} \right)^2 \right]}{G/E \cdot Lt} \quad (5)$$

17 Average values of the elastic and the effective stiffness and standard deviation derived for each masonry typology are reported in
18 Table 6. The effective stiffness values are compared to the ranges indicated by the Italian code in Fig. 12a. For typologies A, C
19 and D the reference values proposed in the Italian code provide a reasonable estimate in terms of mean values, while the error of
20 the predicted stiffness is considerable for the other typologies. In order to make the code ranges representative of 16th-84th fractiles
21 of a probability distribution, as suggested in CNR (2013), the variance of the stiffness should be significantly increased for all
22 stone masonry typologies. However, if one considers the modification factors proposed in the code for considering various mortar
23 qualities, the code ranges for stiffness and strength would be enlarged and the variance of the distribution, therefore, increased.
24 Nonetheless, given that a large part of the tests considered for this study are laboratory tests on panels built with good quality
25 mortar, the variability of the stiffness and strength properties seems to be related to an aleatoric variability rather than to the quality
26 of the materials.

27

1

2

Table 6 Elastic and effective stiffness ranges for the various masonry typologies.

	Masonry typology					
	A	B	C	D	E	E1
Italian code ¹⁾ , E_{el} [MPa]	870	1230	1740	1080	2800	2800
CoV	0.21	0.17	0.14	0.17	0.14	0.14
Italian code ¹⁾ , G_{el} [MPa]	290	410	580	360	860	860
CoV	0.21	0.17	0.14	0.17	0.09	0.09
Number of tests	10	7	18	10	20	22
Elastic stiffness, E_{el}						
Median [MPa]	1110	(3650) ²⁾	1900	510	1460	1000
CoV	0.63	(0.39) ²⁾	0.69	0.48	0.61	0.43
Effective stiffness, E_{eff}						
Median [MPa]	320	(2240) ²⁾	900	430	550	630
CoV	0.49	(0.22) ²⁾	0.38	0.42	0.57	0.42
$(E_{eff}/f_c)_{ref}$	400	(700) ²⁾	300	250	200	250

3

1 - The Italian code (MIT 2009) gives an upper and lower bound value. According to CNR (2013), they can be interpreted as the 16th and 84th percentile values.

4

The mean value given here is computed as the average of the upper and lower bound value and the CoV, assuming a lognormal distribution, as $\sqrt{e^{\beta^2} - 1}$,

5

where β is the logarithmic standard deviation computed as $1/2 (\ln E_{84\%} - \ln E_{16\%})$

6

2 - The values of stiffness for typology B are derived from a single test campaign.

7

8

6.3 Determining the E-modulus from compression tests or dynamic identification tests

9

Most test campaigns with shear-compression tests on stone masonry walls also comprised some material tests from which the elastic properties of the masonry can be estimated. Different types of tests were carried out for this purpose. Most common are compression tests on wallets or masonry prisms. The wallets had typically dimensions of approximately 1 m by 1 m while the prisms were much smaller and comprised just a vertical stack of 3-5 stones. In addition to compression tests, some research groups determined the elastic properties from dynamic identification tests or from the deformation measured when applying the vertical load to the wall. The G-modulus is more difficult to determine than the E-modulus, and test reports do often not report estimates for the G-modulus and such values are therefore also not included in the database.

16

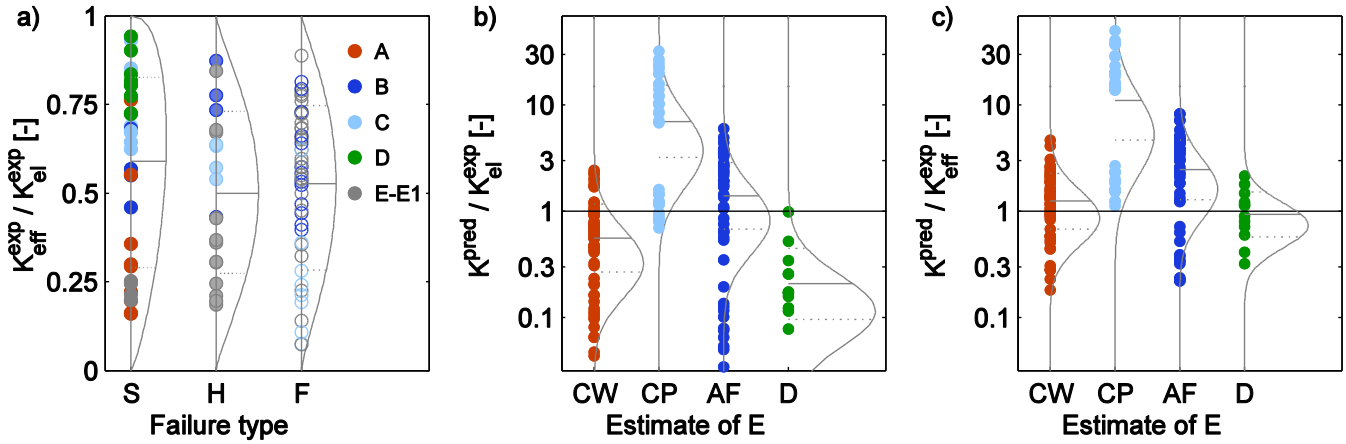
Fig. 10b and c show the distributions of errors in predicting the elastic and effective wall stiffness when determining the E-modulus from compression tests on wallets (CW), compression tests on prisms (P), from deformations measured when applying the axial force at the beginning of the shear-compression tests (AF) and from dynamic identification tests (D) on the walls that are later used for shear-compression tests. The estimate of the effective stiffness is in general characterised by a smaller dispersion, compared to the elastic stiffness. The results show that the elastic properties should not be derived from compression tests on prisms (Lourenço 1996; Oliveira 2003), but that the compression tests should be carried out on wallets. Compression tests on prisms tend to overestimate the E-modulus, most likely because the texture of prisms is typically much more uniform than that of larger masonry walls.

24

As presented in more detail in Fig. 11, the test that leads to the smallest bias and uncertainty is the compression test on masonry wallets and this is therefore the preferred test for estimating the E-modulus. The stiffness derived from the axial force load stage is affected by a larger uncertainty than compression tests on masonry wallets, most likely because the walls are only loaded to relatively small axial load ratios where the stress-strain relationship can be nonlinear. Dynamic identification tests were used only for few tests and therefore conclusions on the reliability of the properties obtained from such tests cannot be derived.

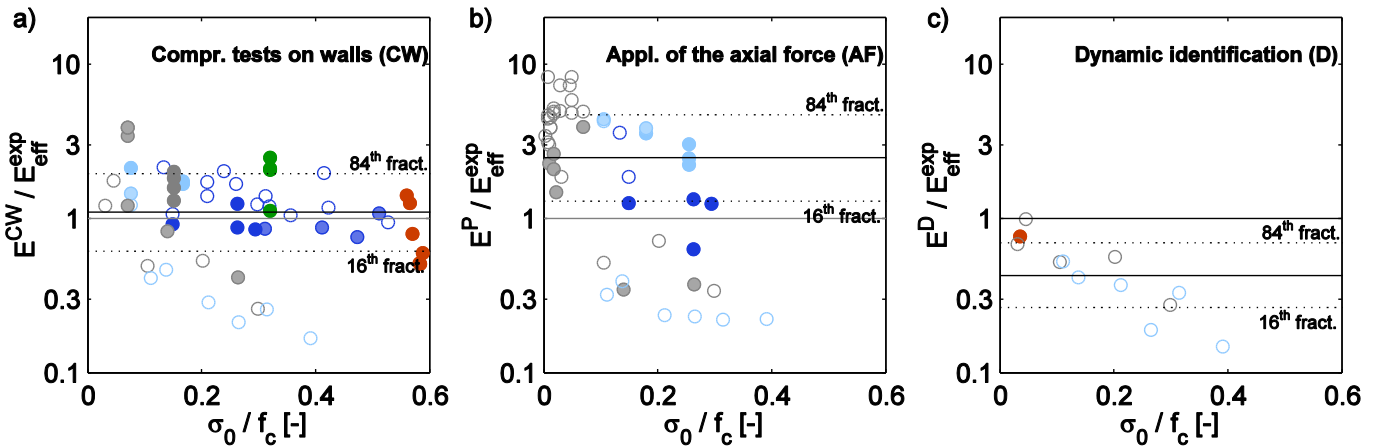
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1 Based on the three more reliable estimates of the elastic properties—compression tests on walls, axial force load stage, dynamic
 2 identification tests—the effective stiffness can be estimated by assuming a ratio of effective to elastic stiffness and a G/E -ratio.
 3 Fig. 10 shows the distribution of the errors of predicted effective stiffness if one assumes for all typologies and failure modes a
 4 ratio of effective to elastic stiffness equal to 0.5 and the ratio of G/E as 0.33. Standard deviations of the errors are in general smaller
 5 than for the elastic stiffness (Table 6); this might be related to the fact that the effective stiffness is a more robust measure when
 6 determined from experimental envelopes than the elastic stiffness.



7

8 **Fig. 10 Stiffness of walls subjected to horizontal loads: Effective to elastic wall stiffness ratios for different failure types and**
 9 **masonry typologies (a); estimate of the experimental elastic wall stiffness (b) and effective wall stiffness (c) from different**
 10 **types of tests (CW- compression tests on walls; CP – compression tests on prisms; AF – stiffness measured when applying**
 11 **the axial force at the beginning of the shear-compression test; D – dynamic identification tests).**



12

13 **Fig. 11 Estimate of the effective stiffness for different experimental test: compression test on walls (a), stiffness measured**
 14 **during the application of the axial force before the shear-compression test (b), and dynamic identification tests (c).**

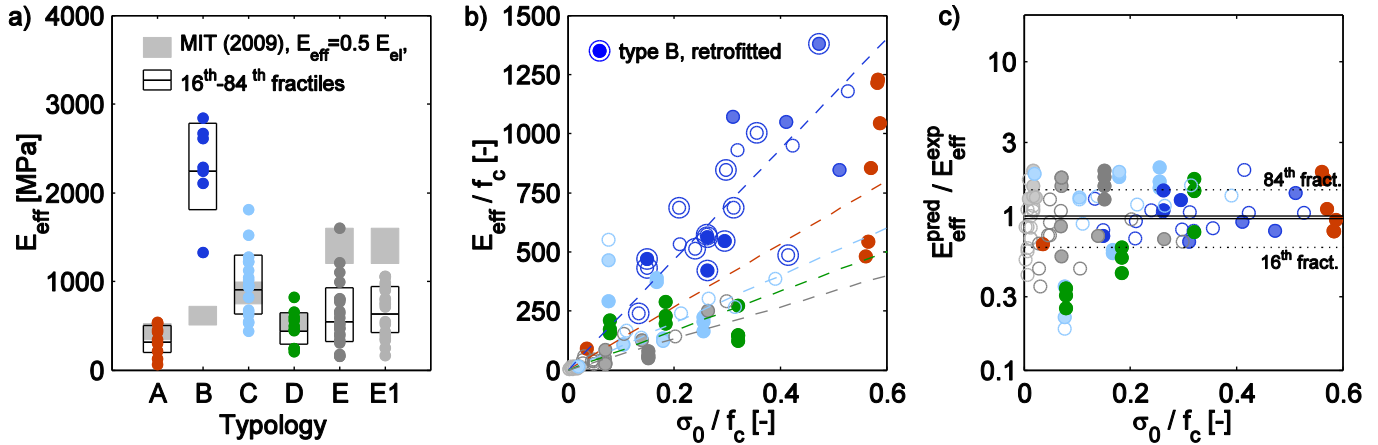
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16 **6.4 Determining the E-modulus from the compression strength**

17 In engineering practice, compression or dynamic identification tests can often not be conducted and reference values have to be
 18 obtained from the literature or from code provisions. Many codes only tabulate the compressive strength and estimate the E-
 19 modulus as $1000f_c$, a value suggested also by Eurocode 6 (CEN 2005b). However, such ratio has been shown to be highly variable
 20 when determined from experimental tests, as pointed out by Tomažević (1999), who reported for this ratio values between 200 and
 21 2000. On average, in the collected sample of tests, the ratio between the experimental effective stiffness and the compressive
 22 strength of masonry tends to increase with the axial load ratio, as shown in Fig. 12b. An increase of the effective stiffness with
 23 applied axial load had already been reported by a few authors (Vasconcelos 2005; Bosiljkov et al. 2005). However, not all test
 24 campaigns show a clear trend in this regard (for example, Magenes et al., 2010). Assuming that an increase of stiffness is related
 25 to the axial load ratio, the experimental effective stiffness can be estimated through an empirical relation of the type:

$$E_{eff} = \left(\frac{E}{f_c}\right)_{ref} \cdot f_c \cdot \frac{\sigma_0/f_c}{0.30} \quad (6)$$

1 This simple linear formula has limits when applied to axial stresses close to zero. However, the available data and the significant
 2 scatter did not justify a more complex relationship between stiffness and axial load ratio (Fig. 12b). Reference values of the
 3 expected ratio between effective stiffness and compressive strength refer to an axial load ratio of 30%. They are derived from the
 4 database and are tabulated for the various typologies in Table 6. The ratio of experimental stiffness to the stiffness predicted by
 5 Eq. (6) is shown in Fig. 12c.



6
 7 **Fig. 12 Comparison between the experimental effective stiffness and the ranges proposed in the Italian code; b) relation**
 8 **between effective stiffness and axial load, normalized to the compressive strength f_c ; c) prediction of the effective stiffness**
 9 **through Eq. (6).**

6.5 Comparison of various approaches for estimating the stiffness

12 The accuracy of the various approaches for estimating the effective stiffness is compared in Table 7. Estimating the effective
 13 stiffness from E-moduli that were determined experimentally from compression tests on walls or prisms, dynamic identification
 14 tests or computed from the shortening of the wall when applying the axial load leads to large uncertainties (CoV=0.5-0.7) and
 15 considerable bias. Surprisingly none of these results led to an improved estimate of the horizontal wall stiffness when compared to
 16 the Italian code values.

17 The use of median E_{eff} -values obtained from the collected tests reduces obviously the bias but not much the coefficient of variation.
 18 Moreover, it should be considered that in Fig. 12 and in Table 6 typology B represents solely unstrengthened panels, which are
 19 derived from a single test campaign, hence their use for assessment is not recommended but a larger number of tests from different
 20 campaigns would be required to derive reliable reference values. Strengthened panels were excluded from the sample relative to
 21 typology B since their elastic properties are significantly affected by the intervention, and they are therefore not directly comparable
 22 to the unstrengthened ones. The formulation in Eq. (6), with the reference parameters calibrated on the collected sample of tests,
 23 can reduce both the bias and the coefficient of variation of the estimate of the stiffness. In this case strengthened panels were also
 24 included in the analysis, since the ratio between elastic modulus and compressive strength, which is the main parameter of the
 25 formulation, does not appear to be strongly affected by the intervention (Fig. 12b).

26 **Table 7 Comparison of different methods for estimating the effective stiffness of the shear-compression tests.**

	Compression test, walls (CW)	Compression test, prisms (CP)	Axial force application (AF)	Dynamic identification (D)	MIT (2009a), mean values	Experimental median values (Table 6)	Eq. (6) (Table 6)
Number of tests	57	34	49	12	84	84	99
$E_{eff}^{pred}/E_{eff}^{exp}$, median	1.25	11.1	2.46	0.93	1.31	1.00	0.92
CoV	0.67	1.06	0.73	0.52	0.91	0.69	0.45

7 Strength of stone masonry walls

The in-plane shear force capacity of stone masonry walls is typically evaluated from equations that model the different failure modes of the wall, namely rocking failure with crushing of the compressed toe and shear failure with diagonal cracking or sliding along the bed joints (Magenes and Calvi 1997). Expressions to evaluate the strength capacity relative to these different failure modes are available in the literature and in the codes (CEN 2005a; MIT 2009).

7.1 Strength equations in Eurocode 8, Part 3

The force capacity of a pier failing in flexure can be evaluated neglecting the tensile strength given that the tensile strength of masonry is normally very small and that horizontal cracking due to cyclic loading is expected at ultimate limit state. Eurocode 8, Part 3 (EC8-3) computes the flexural strength as follows:

$$V_{fl} = \frac{L^2 t}{2H_0} \sigma_{0,tot} \left(1 - 1/\kappa \frac{\sigma_{0,tot}}{f_c} \right) \quad (7)$$

where $\sigma_{0,tot}$ is the mean vertical stress acting at the base of the pier and f_c is the compressive strength of masonry. EC8-sets the factor $1/\kappa$ equal to 1.15, which corresponds to a rectangular stress block in which the maximum stress is equal to $\kappa f_c = 0.87 f_c$. A linear stress distribution at the wall toe would lead to a factor $1/\kappa = 1.33$, while a value equal to 0 can be assumed if the compressive strength is considered infinite, for which the expression in Eq. (7) is equivalent to the rocking capacity in Eq. (3). For assessment purposes, EC8-3 suggests to use design values for f_c that are multiplied by a confidence factor to account for the uncertainty, which depends on the knowledge that is available on that particular structure. However, for the scope of this study, no confidence factor is applied and the compressive strength derived from compression tests are employed.

Shear failure is modelled by EC8-3 by means of a Mohr-Coulomb criterion to be applied to the portion of the wall that is subjected to compression stresses. Although EC8-3 refers only to brick or concrete block masonry, the application of the approach was checked also for stone masonry walls. This criterion is meant to describe failure due to the interaction of flexural cracking and shear at the base of a masonry pier. The uncracked length of the wall L_c can be estimated adopting a suitable stress distribution and considering the axial force acting at the base of the wall. If the tensile strength is disregarded and a triangular stress distribution is adopted, one can write the Mohr-Coulomb criterion as follows:

$$V_{MC} = L_c t c + \mu L t \sigma_{0,tot} = L t \left(\frac{3/2 c + \mu \sigma_{0,tot}}{1 + 3 c H_0 / \sigma_{0,tot} L} \right) \quad (8)$$

where c and μ are the cohesion and the friction coefficient of masonry. The parameters c and μ should be interpreted as global strength parameters and should not be derived directly from interface tests on joint interfaces, in order to account for the non-uniform stress distribution along the compression zone. EC8-3 indicates for the friction coefficient a value equal to 0.4, while reference values for the cohesive contribution in stone masonry walls should be assumed from the literature. As an additional condition accounting indirectly for tensile cracking in the units, EC8-3 prescribes that the average shear stress in the uncracked length of the wall should be less than the 6.5% of the compressive strength of the units. However, this latter criterion is meant to be applied to brick/block masonry to account for possible shear cracking through the units. In the case of stone masonry piers, due to the typically high strength of stone units, this condition is seldom the governing criterion and alternative formulations should be used to consider the possible activation of shear failures involving sub-diagonal cracking (e.g. Turnšek and Čačovič).

7.2 Application of strength equations to database

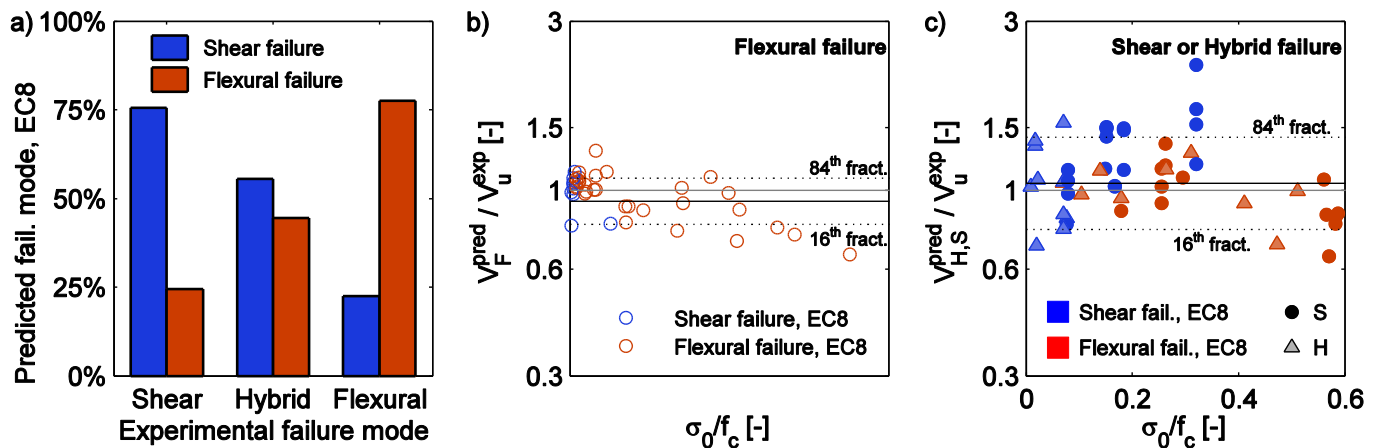
The criteria proposed in EC8-3 (CEN 2005a) were applied to the tests collected in the database and the effectiveness of standard code formulations in predicting correctly the experimental failure mode and force capacity was evaluated. Mechanical properties documented in the test reports do not include the shear strength parameters c and μ . The friction coefficient value suggested in EC8-3 is applied ($\mu=0.4$). The cohesion was estimated assuming a parabolic tension cut-off as $c = 2\mu f_t$, where the tensile strength f_t can be derived from code provisions (MIT 2009). The force capacity is defined as the ultimate shear capacity derived from the bilinear idealisation of the envelope curves. For 15 tests, the load displacement curve is not available and the maximum force capacity reported by the authors was used instead. The average ratio of maximum to ultimate force capacities is 1.04, and it exceeds

1 the value 1.10 in less than 2% of the cases. The failure mode that was attributed to each test is based on the information provided
 2 in test reports, which assess the failure modes based on the observed damage (diagonal or horizontal cracking, sliding, crushing at
 3 the toe). However, this attribution can be somehow subjective, and mixed or hybrid failure modes are frequently observed.

4 EC8-3 predicts the failure mode based on the force capacities computed for flexural and shear failure: the smaller force capacity is
 5 assumed to control the failure mode. Fig. 13a compares the experimentally observed failure mode to the failure mode predicted by
 6 EC8-3. The failure mode is well predicted for walls failing in flexure. For some walls failing in shear, EC8-3 predicts also a flexural
 7 failure. However, this does not necessarily mean that the prediction of the force capacity is wrong, since also walls developing
 8 large shear cracks might fail due to the crushing of the compressed corner. Moreover, shear and flexural capacity equations might
 9 lead to rather similar results and while the failure mode might be incorrectly predicted the shear strength might be rather well
 10 estimated. An incorrect prediction of the failure mode can have, however, a significant influence on the estimate of the deformation
 11 capacity. Most of today's codes assign the displacement capacity based on the failure mode and assume that walls failing in flexure
 12 have roughly twice the displacement capacity of walls failing in shear. The fact that a part of the observed shear and hybrid failures
 13 are predicted to be flexural failures might therefore lead to unconservative estimates of the deformation capacity (see next section).

14 For flexure-dominated walls the prediction of the force capacity is fairly good (Fig. 13b), since it depends mainly on geometrical
 15 dimensions and loading conditions, and only to a minor extent on material properties. The ratio of predicted to experimental force
 16 capacity, for flexural walls, has a median of 0.93 and a coefficient of variation (CoV) of 15%. The prediction is less accurate for
 17 higher axial load ratios, indicating that the assumption of a stress block with $\kappa=0.87$ at the corner of the wall is probably rather
 18 conservative. The best prediction of the force capacity, with a mean of 1.00 and a CoV of 12%, is obtained for $\kappa=1.20$, which
 19 would correspond to a local increase of the compressive strength at the base of the wall. A physical justification of this could be
 20 the presence of relatively large stones in the wall corners, which increase local strength properties. For brick masonry, also a
 21 confinement of the lowest brick row due to the foundation was observed (Petry and Beyer 2015). However, the refinement of the
 22 assumptions with regard to the stress block does not seem warranted, as the shift of the predicted force capacity is rather small and
 23 the coefficient of variation does not reduce consistently.

24 The predicted force capacity of walls showing hybrid or shear failure is affected by a larger uncertainty, related primarily to the
 25 estimation of the mechanical parameters, which play for these failure modes a significant role. The force capacity is on average
 26 overestimated, in a more evident manner for walls subjected to high axial load ratios (Fig. 13c). This can be related to the
 27 assumptions on the friction coefficient, for which a value of 0.4 is adopted in the Eurocode, regardless of the type of masonry.
 28 Angelillo et al. (2014) indicate different reference values for stone masonry, ranging from 0.2 for rubble masonry, 0.3 for irregular
 29 masonry, to 0.4 for dry joints stone masonry.



30
 31 **Fig. 13 a) Failure mode predicted by Eurocode 8 part 3; b) Estimate of the flexural capacity; c) Estimate of the shear**
 32 **capacity according to EC8-3 (Mohr-Coulomb criterion on the uncracked length of the section).**

33 If a Mohr-Coulomb formulation is adopted for the assessment of the shear capacity, results are strongly affected by the choice of
 34 a suitable value for the friction coefficient. In this study, the cohesive term was assumed to be dependent on the tensile strength,
 35 which was derived from code provisions. The friction coefficient, and the uncertainty related to its determination, were hence

1 derived from a linear regression, as shown in Fig. 14c. Only panels showing shear or hybrid failure modes were considered.
2 Depending on the masonry typology, the so obtained friction coefficient varies between 0.2 and 0.4 (Table 8).

3 The mean values and coefficient of variation of the ratio of predicted to experimental force capacity for the different material
4 properties and models for shear capacity are summarised in Table 9.

5 **7.3 Turnšek-Čačovič criteria and calibration of the tensile strength**

6 The Mohr-Coulomb criterion in EC8-3 is suitable for cases in which shear failure is associated with bed joint sliding and the
7 opening of head joints. For irregular masonry typologies, however, the physical significance of such criterion can be questionable.
8 An alternative formulation, proposed originally by Turnšek and Čačovič (1971), relates the shear force capacity to the onset of
9 diagonal cracking. The opening of a diagonal crack can be modelled through a tensile criterion, applied to an idealised biaxial
10 stress condition in the middle of the masonry panel, obtaining the formulation in Eq. (9).

$$V_{TC} = \frac{Lt}{b} f_t \sqrt{1 + \frac{\sigma_{0,mid}}{f_t}} \quad (9)$$

11 The vertical stress $\sigma_{0,mid}$ is the mean vertical stress at the mid-height of the panel, since it is assumed that diagonal cracking
12 initiates there. The factor b models the distribution of shear stresses along a horizontal section of the wall and corresponds to 1.5
13 if a parabolic shear stress distribution is assumed. For squat panels, however, this idealisation can be rather crude and a value of
14 $b=H/L$ ($1.0 \leq b \leq 1.5$) was found to be more appropriate (Benedetti and Tomažević 1984). The parameter f_t represents the tensile
15 strength of masonry along an inclined plane, and can be determined from diagonal compression tests. The Italian code, which
16 suggests this equation for irregular masonry or for walls built with weak units, provides also reference values for f_t .

17 If the failure criterion expressed in Eq. (9) is adopted for all tests with hybrid or shear failure modes, one experimental value of
18 tensile strength can be derived for each test using Eq. (10).

$$f_t = -\frac{\sigma_0}{2} + \sqrt{\left(\frac{\sigma_0}{2}\right)^2 + \left(\frac{b \cdot V_u}{Lt}\right)^2} \quad (10)$$

19 Fig. 14a shows the comparison of ranges proposed in the Italian code for the tensile strength of masonry for the different typologies,
20 with the values estimated from the collected tests. The obtained mean values are comparable—though typically slightly higher—
21 than the values included in the Italian code. It should be noted that typology B refers to unstrengthened conditions. The values
22 listed in Table 8 derive from a single test campaign and a limited number of tests, since the majority of collected tests of the same
23 typology was strengthened through grout injections. Similarly to what was found for the effective stiffness, the code ranges do not
24 appear currently suitable to represent 16th-84th fractiles of a probability distribution of the measure. The code ranges shown in Fig.
25 14a do not include the correction factors that are proposed by the Italian code to consider that the mortar of the test units tested in
26 laboratory conditions was most likely good quality mortar, often containing hydraulic lime. The quality of the mortar present in
27 existing buildings can be considerably lower, since its composition and conservation state might differ significantly to the ones of
28 mortars tested in laboratory. Therefore, depending on the state of the mortar, the adoption of conservative values for assessment
29 purposes can be advisable. An alternative method for estimating the tensile strength of an existing stone masonry could make use
30 of the Masonry Quality Index (MQI). In Fig. 14b the experimental values of tensile strength are related to the MQI estimated for
31 each panel, evaluated for in-plane actions. A regression of experimental values through a simple equation can be expressed as:

$$f_t = 0.015 + 0.006 \cdot MQI^{1.5} \quad (11)$$

32 Equivalent expressions that link upper and lower bounds of the tensile strength to the MQI were developed by (Borri et al. 2015).
33 These expressions, although their form is slightly different, show the same trend and lead to similar estimates of the tensile strength.

34

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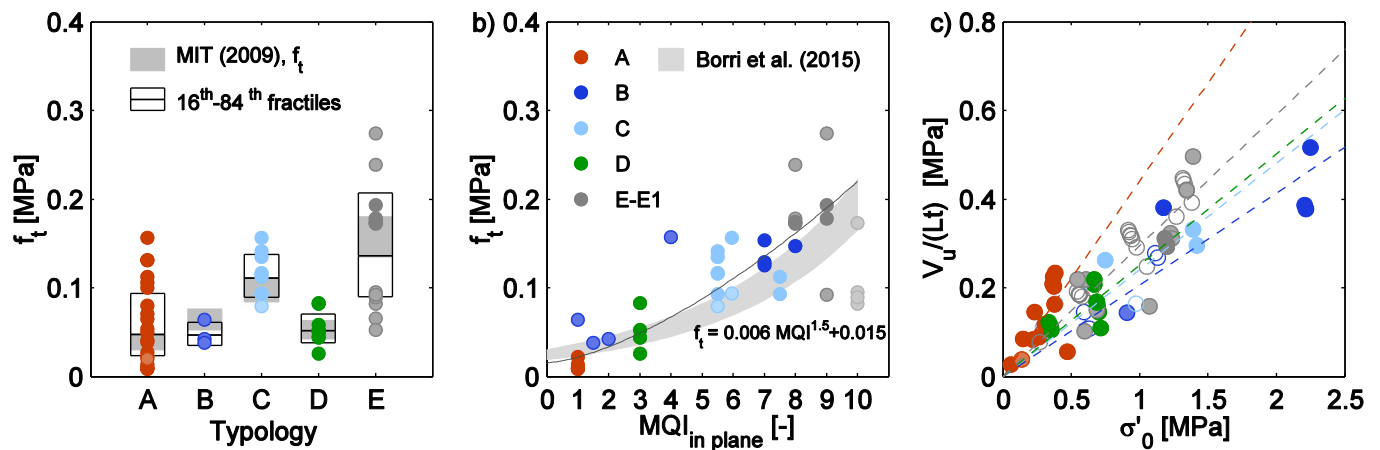
Table 8 Experimental and code ranges for the tensile strength of masonry f_t .

	Masonry typology				
	A	B	C	D	E-E1
Italian code MIT (2009a) ¹⁾ , f_c [MPa]	1.40	2.50	3.20	1.90	7.00
CoV	0.30	0.20	0.19	0.27	0.14
Italian code MIT (2009a) ¹⁾ , f_t [MPa]	0.039	0.065	0.098	0.053	0.158
CoV	0.24	0.19	0.14	0.20	0.14
Experimental f_t					
Median [MPa]	0.047	0.046	0.111	0.052	0.136
CoV	0.79	0.29	0.22	0.32	0.44
Friction coefficient, experimental					
Best fit	0.44	0.21	0.24	0.25	0.29
CoV	0.17	0.12	0.17	0.12	0.04

3

1 - Mean values and coefficients of variation calculated as in Table 6.

4



5

Fig. 14 a) Masonry tensile strength according to Turnšek-Čačovič criterion: comparison with ranges suggested in the Italian code (MIT 2009); **b)** Estimate of the experimental tensile strength from the Masonry Quality Index; **c)** Regression analysis for the estimation of the friction coefficient; the cohesive contribution is subtracted, assuming $c = 2\mu f_t$. The x-axis is derived from Eq. (8): $\sigma'_0 = \sigma_0 + 3f_t - 6 \frac{VH_0 f_t}{\sigma_0 L^2 t}$ where $V_u = \mu \cdot \sigma'_0 \cdot Lt$.

10

11

7.4 Comparison of different strength models

13

A comparison of the different capacity models for the prediction of the lateral strength of panels showing hybrid or shear failure modes are summarised in Table 9. In general, the application of a Turnšek-Čačovič failure criterion improves the prediction of the force capacity when compared to the standard approach prescribed in EC8-3. This applies to both approaches of estimating f_t , i.e., estimating f_t from MQI (Eq. (11)) and using reference values for f_t by the Italian code, which depend on the masonry typology.

16

1 For walls that fail in shear, the Turnšek-Čačovič criterion leads also to a more accurate prediction of the failure mode than the
 2 Mohr-Coulomb criterion with $\mu=0.4$. However, a similar accuracy can be achieved through the optimisation of the parameters of
 3 a Mohr-Coulomb criterion, such as the one in Eq. (8), among which the friction coefficient is the more relevant.

4 **Table 9 Estimation of force capacity through different models, for walls showing hybrid and shear failure.**

	EC8-3 $\mu=0.4, c$ from MIT (2009a) ¹	EC8-3 μ from Table 9, c from MIT (2009a) ¹	Eq. (9) f_i from MIT (2009a) ¹	Eq. (9) typology median f_i ,	Eq. (9) f_i , from Eq. Error! Reference source not found.
V^{pred}/V^{exp} , median	1.04	0.88	1.04	0.95	0.94
CoV	0.31	0.26	0.22	0.18	0.24
Predicted to fail in shear ²	72%	85%	77%	80%	76%

5 1 - Table C8A.2.1 in (MIT 2009). Correction coefficients in table C8A.2.2 in (MIT 2009) to account for the effect of grout injections and quality of mortar.

6 2 - Ratio of walls predicted to fail in shear to walls that experimentally showed shear failure.

7

8 Drift capacity of stone masonry walls

9 The deformation capacity of walls is a key input parameter when applying displacement-based assessment methods to masonry
 10 buildings. Current code provisions do not differentiate between brick and stone masonry when specifying the drift capacity of walls
 11 (Petry and Beyer 2014a). EC8-3 (CEN 2005a) limits its application to concrete and brick masonry, but in engineering practice the
 12 values given in EC8-3 are often also applied to stone masonry. The objective of this section is to derive drift capacities for stone
 13 masonry walls, to identify parameters that influence the drift capacities at different limit states and to provide the input data that is
 14 required for a probabilistic seismic assessment of stone masonry structures. In addition, two simple drift capacity models for stone
 15 masonry are put forward, which are suitable for implementation in engineering practice.

16 It was shown in Section 4 that monotonic tests lead to significantly larger drift capacities than cyclic tests. Since drift capacity
 17 values are typically used in conjunction with seismic assessments, only cyclic tests are considered in the following. Disregarded
 18 are also tests on walls that were injected or repaired as well as all tests that did not pass the quality check. In total, 67 test were
 19 considered of which 2 belonged to masonry typology A, 8 to B, 19 to C, 6 to D, 20 to E and 12 to E1 (Fig. 15a). The drift capacities
 20 are evaluated for the six element limit states introduced in Section 1: (i) the drift at the onset of cracking δ_{cr} , (ii), the drift at yield
 21 δ_y , (iii) the drift at maximum force δ_{max} , (iv) the drift at the limit state “Significant damage” $\delta_{SD} = \min(3\delta_{cr}, \delta_{max})$, (v) the drift
 22 at ultimate limit state (20% strength drop) δ_u , (vi) the drift at collapse (50% strength drop) δ_c . With the exception of the drift at the
 23 onset of cracking, the drift capacities are determined from the force-displacement envelope and its bilinear approximation. The
 24 drift at the onset of cracking is based on observations reported in the reference document but is not available for all tests. Note that
 25 the definition of onset of cracking differed between test campaigns. Some researchers distinguish between the appearance of
 26 flexural and shear cracks (e.g. Kržan and Bosiljkov 2012; Silva et al. 2014), others consider any type of crack (Vasconcelos 2005).
 27 Also, the minimum crack width that was detected probably differed between test series. The drift at the onset of cracking is therefore
 28 afflicted with an additional uncertainty. A detailed definition of the individual drift limits based on the envelopes in the positive
 29 and negative loading direction is included in the accompanying database.

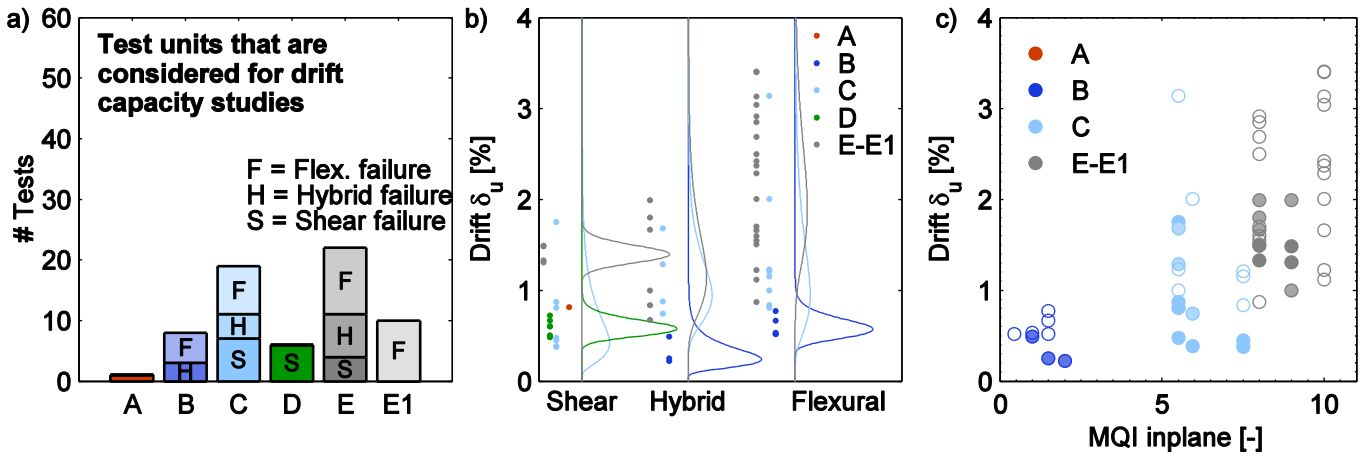
30 8.1 Sensitivity of drift capacities at different limit states

31 The minimum and the maximum ultimate drift values of the 67 tests differ by more than a factor of 15 ($\delta_{u,min} = 0.22\%$ and
 32 $\delta_{u,max} = 3.4\%$). This is a rather significant ratio and the objective of this section is to identify factors that influence the drift capacity
 33 of stone masonry walls at different limit states. EC8-3 (CEN 2005a) assumes that the ultimate drift capacity depends on the failure
 34 mode. Fig. 15b shows the distribution of the drift values for shear, hybrid and flexural failure. In general, shear and hybrid failures
 35 lead to a smaller drift capacity than flexural failures. Different trends are only observed when the sample size is very small (shear
 36 failure of Type E; hybrid failures Type C). To increase the size of the groups, the masonry typologies are regrouped as follows:
 37 the first group comprises types A-D and the second group types E and E1. Table 10 summarises for these two groups the median
 38 drift capacities and coefficients of variations for all considered limit states. Shear and hybrid failure modes lead to similar drift
 39 capacities and coefficients of variations. This finding suggests that it is not necessary to distinguish between shear and hybrid

1 failure modes and in the remainder of this section drift capacities obtained from hybrid failure modes are counted towards shear
2 failures.

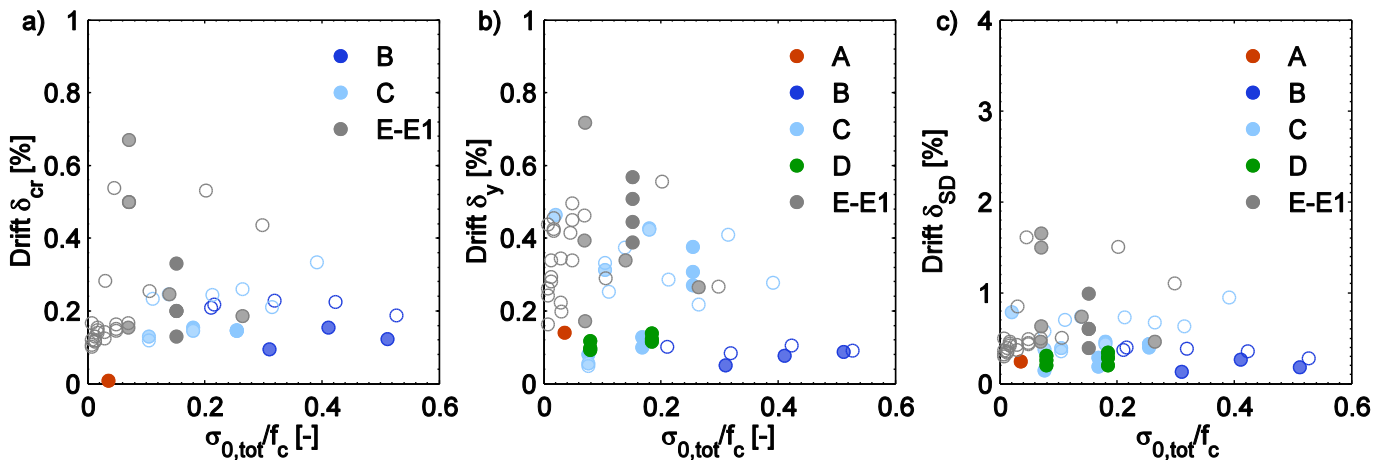
3 One might expect that the drift capacity is positively correlated with the Masonry Quality Index and this is indeed confirmed by
4 Fig. 15c. However, as shown by Fig. 4i, the axial load ratio also correlates strongly with the Masonry Quality Index (the larger the
5 Masonry Quality Index, the smaller the axial load ratio that was applied in the test). Based on the current database it is therefore
6 not possible to identify whether the drift capacity depends on the Masonry Quality Index or the axial load ratio or both. For other
7 masonry typologies, it was already shown that the drift capacity decreases with increasing axial load ratio (e.g. Petry and Beyer,
8 2014, Rosti et al., 2016). For this reason, we investigate in the following the influence of the axial load ratio on the drift capacity
9 of stone masonry walls at different limit states. Note that photos of the test units of typology D (Faella et al. 1992) were not
10 available and therefore the Masonry Quality Index could not be determined.

11 Fig. 16 shows the influence of the axial load ratio on the drift capacities for the different limit states. The drift δ_{cr} at the onset of
12 cracking is relatively independent of the axial load ratio and of the masonry typology; for most walls the drift at the onset of
13 cracking is between 0.1 and 0.3%. Only for some walls of typology E and E1, the drift at the onset of cracking is significantly
14 larger. Drift capacities of all limit states tend to reduce with the axial load ratio but this trend is particularly evident for δ_y , δ_{max}
15 and δ_u .



16
17 **Fig. 15** Distribution of test units considered for drift capacity studies (a). Ultimate drift capacity δ_u as a function of the
18 failure mode (b), and the Masonry Quality Index for in-plane loading (c). Solid markers represent walls failing in shear or
19 a hybrid mode; empty markers walls failing in flexure.

20



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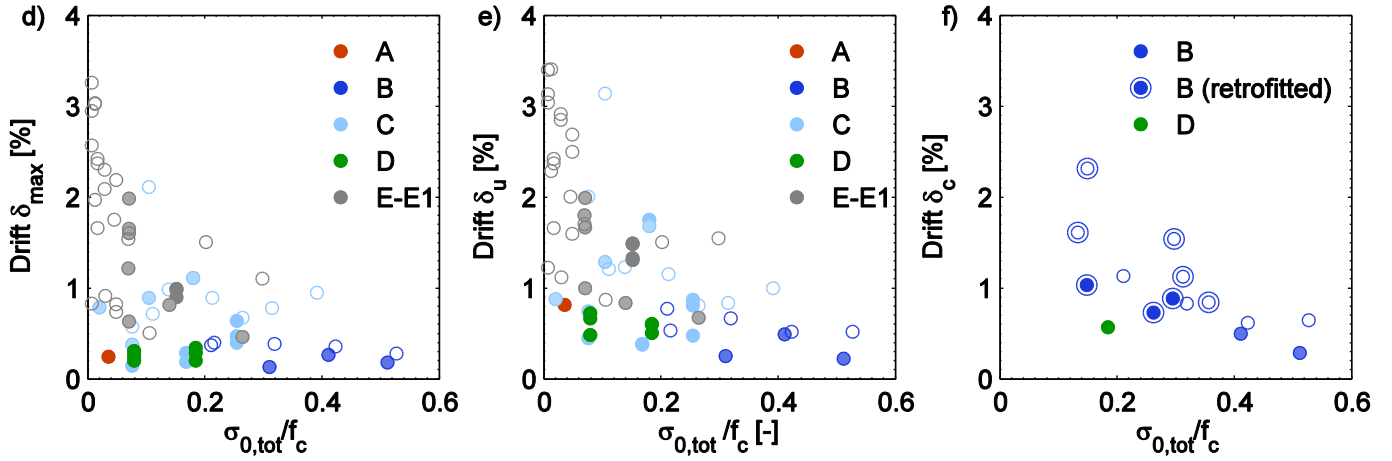


Fig. 16 Influence of the axial load ratio on the drift capacity at different limit states: a) Drift at the onset of cracking δ_{cr} ; b) Drift at yield δ_y ; c) Drift at maximum force δ_{max} ; d) Drift limit “Significant damage” $\delta_{SD}=\min(3\delta_{cr}, \delta_{max})$; e) Drift at ultimate LS δ_u ; f) Drift at collapse δ_c . Solid markers represent walls failing in shear or a hybrid mode; empty markers walls failing in flexure. Note: The scale of the y-axis of plot a and b is different from those in plots c-f.

Fig. 17a and b show the trends of the ultimate drift capacity with axial load ratio, if δ_u is normalised by H_0/L (CEN 2005a) and by H_0/H (Pfyl-Lang et al. 2011), respectively. The clearest trend with axial load ratio is obtained for $\delta_u L/H_0$. For brick masonry, it was further shown that the drift capacity decreases with the wall size (Petry and Beyer 2014a). For stone masonry walls, as for brick masonry, no test series investigated the effect of size on the drift capacity systematically. Fig. 17c show the drift capacity of the walls contained in this database as a function of the wall height. Although the drift values tend to decrease with wall height, the trend for a single masonry typology is not clear. One reason why the size effect might be less important for stone masonry walls than for brick masonry walls is the fact that the size of the stones can be relatively easily reduced while small-scale brick wall tests are typically conducted with full-size bricks.

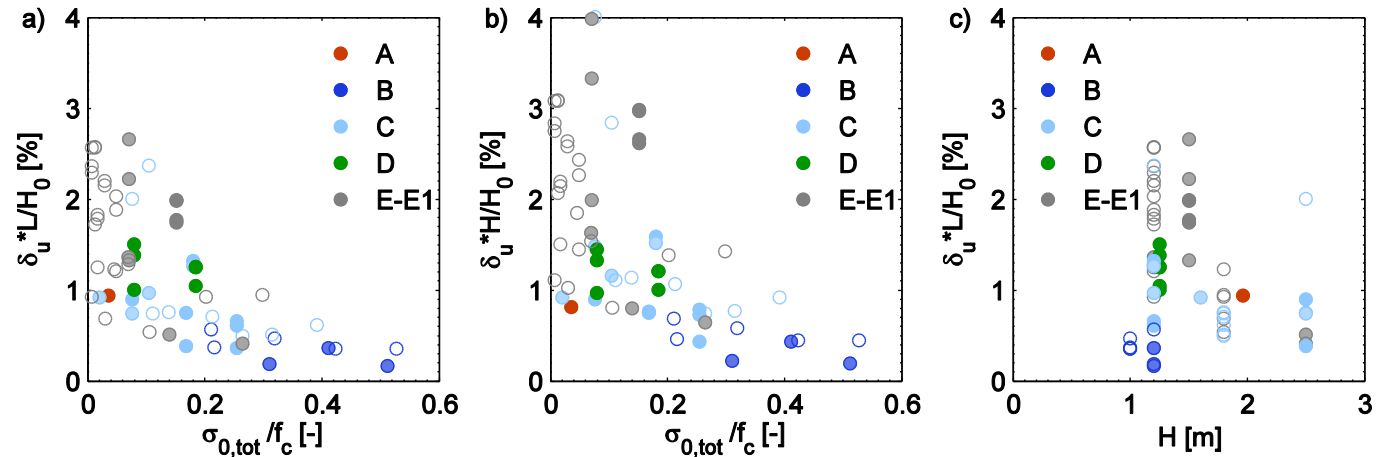
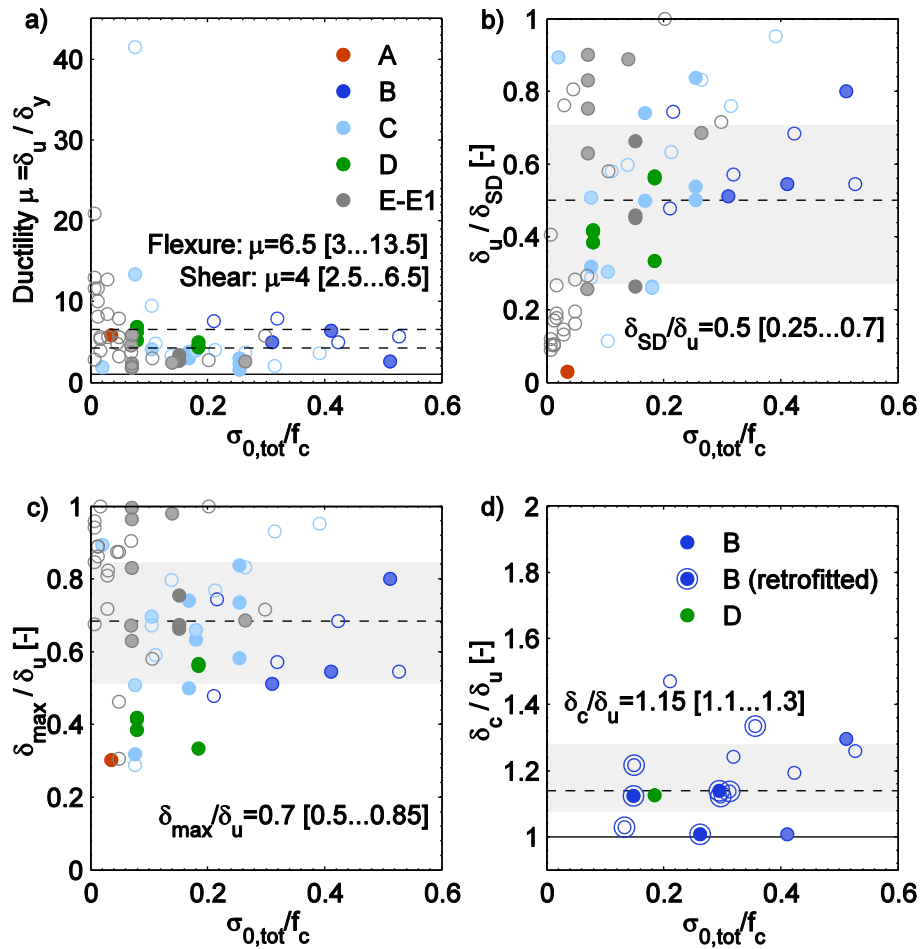


Fig. 17 Ultimate drift capacity δ_u : Normalising the drift capacity by L/H_0 (a) and H/H_0 (b). Influence of the wall size on the drift capacity (c).

Fig. 18a shows the displacement ductility $\mu = \delta_u/\delta_y$ as a function of the axial load ratio. The displacement ductilities vary between $\mu=1.5$ -13.4 for shear and hybrid failures and between $\mu=2.0$ -41.5 for flexural failures. The median displacement ductilities are $\mu=4$ for shear and hybrid failures and $\mu=6.5$ for flexural failures. The wide ranges highlight that displacement ductility is not a suitable parameter for characterising the deformation capacity of masonry walls. The ratio of the drift at the LS “Significant Damage” to the ultimate varies for shear/hybrid and flexural failure modes between $\delta_{SD}/\delta_u=0.5$ -1.0 (Fig. 18b). The median value is 0.5 and therefore smaller than what is assumed in EC8-3 ($\delta_{SD}/\delta_u=3/4$). The ratio of $3/4$ corresponds, however, rather well to the median ratios obtained for δ_{max}/δ_u (Fig. 18c), for which a median value of 0.70 was obtained.

1 The limit state for which the least amount of data is available is the collapse limit state (Fig. 16f, Fig. 18d). Only seven tests were
 2 continued up to collapse; six walls originate from a single test series conducted by Silva et al. (2014). Out of these six tests, two
 3 failed in shear and four in flexure. The average collapse drift of these six tests is considerably smaller than the average ultimate
 4 drift of all 67 tests (Table 10). In order to increase the data base, the walls that were strengthened were also considered for the
 5 collapse limit state. Of the strengthened walls, eight walls were tested up to collapse; these tests were conducted by Silva et al.
 6 (2014) and Mazzon (2010). The drift at collapse decreases significantly with increasing axial load ratio (Fig. 16f). For walls failing
 7 in flexure the drift capacities at collapse are slightly larger than for walls failing in shear but the difference for the tests reported
 8 here is not as large as one might have expected. Fig. 18d shows the collapse drift to ultimate drift ratio for the 15 strengthened and
 9 unstrengthened walls that were tested up to collapse. This ratio seems to be rather independent of the axial load ratio and failure
 10 mode and its median value is $\delta_c/\delta_u=1.15$.

11



12

13

14 **Fig. 18 Ratios of drifts at different limit states:** a) Displacement ductility $\mu=\delta_u/\delta_y$; b) Ratio of ultimate drift δ_u to drift at the
 15 limit state “Significant Damage”; c) Ratio of collapse drift δ_c to ultimate drift δ_u ; d) Ratio of collapse drift δ_c to ultimate drift δ_u . Solid markers represent walls failing in
 16 shear or a hybrid mode, empty markers walls failing in flexure. The dashed line represents the median value and the shaded
 17 area and the range corresponding to plus/minus one standard deviation.
 18

19

20 **Table 10 Median drift capacities and coefficients of variations for different limit states and masonry typologies.** Drift
 21 capacities and CoVs are rounded to the nearest 0.05; shear failure comprises shear and hybrid failures.

Number of test units per group		Drift capacity [%]		CoV	
Shear failure	Flexural failure	Shear failure	Flexural failure	Shear failure	Flexural failure

Drift at the onset of cracking δ_{cr}						
A-D	10	12	0.15 ²⁾	0.25	0.35	0.20
E, E1	11	21	0.25	0.15	0.55	0.65
All	21	33	0.15	0.15	0.75	0.55
Drift at yield δ_y						
A-D	21	12 ¹⁾	0.10	0.25	0.75	0.60
E, E1	11	21	0.45	0.35	0.55	0.30
All	32	33	0.25	0.30	0.85	0.45
Drift at “Significant Damage” LS δ_{SD}						
A-D	21	13	0.30	0.55	0.50	0.35
E, E1	11	21	0.65	0.45	0.55	0.65
All	32	34	0.40	0.45	0.80	0.55
Drift at maximum force δ_{max}						
A-D	21	13	0.30	0.65	0.75	0.65
E, E1	11	21	1.00	1.95	0.40	0.45
All	32	34	0.45	1.05	0.75	0.65
Drift at ultimate LS (20% drop in force) δ_u						
A-D	21	13	0.60	0.85	0.55	0.65
E, E1	11	21	1.50	2.35	0.30	0.35
All	32	34	0.80	1.65	0.55	0.55
Drift at collapse (50% drop in force) δ_c						
A-D	3	4	0.50 ³⁾	0.75 ³⁾	0.35	0.30
E, E1	0	0	-	-	-	-
All	3	4	0.50 ³⁾	0.75 ³⁾	0.35	0.30

- 1) For Test ID=33 only δ_{max} and δ_u but not the entire force-drift envelope were available. Therefore δ_y could not be determined.
- 2) The drift at the onset of cracking was only available for 10 out of the 21 tests that failed in shear. The 10 tests led in average to larger yield drifts than the 21 tests and this is why the median value of δ_{cr} is larger than the median value of δ_y for walls failing in shear. For the 10 tests, for which δ_{cr} is known, the median yield drift was 0.30%, i.e., twice the drift at the onset of a cracking. For a median yield drift of 0.10%, it is therefore recommended to assume $\delta_{cr}=0.05\%$.
- 3) The collapse drift was only available for 7 out of the 66 tests, for which δ_u could be determined. The 7 tests led in average to smaller drift capacities than the 66 tests and this is why the median value of δ_c is smaller than the median value of δ_u . It is recommended to assume that $\delta_c/\delta_u=1.1$ (Fig. 18d).

8.2 Simple drift capacity models for engineering practice

The median drift values and CoVs given in Table 10 can be directly used in probabilistic assessments of stone masonry buildings. However, simpler models that can be summarised in fewer equations might often be more practical. The objective of this section is to propose two of such models. The first relates drift capacities to failure modes and masonry typology and the second relates drift capacity to axial load ratio, slenderness ratio and masonry typology. These models are inevitably less exact than the values of Table 10 and their derivation required some judgment in order to find a good balance between accuracy and simplicity.

The drift capacities are determined for the ultimate limit state (δ_u). Based on the results presented in Fig. 18, drifts at all other limit states are expressed as a fraction of the drift at the ultimate limit state. Equations (12)-(17) summarise these relationships. The equations on the left represent median values and the equations on the right values that correspond to plus/minus one standard deviation assuming a lognormal distribution. One exception is the drift at the onset of cracking, for which a universal value of 0.20% is recommended, independent of the failure mode and masonry typology. The relationships between δ_u and the other drift limits apply independently of the chosen model for δ_u . For the yield drift, two approaches are investigated. In the first approach, the yield drift is computed assuming a constant displacement ductility values, which is assumed as dependent on the failure mode or independent of the failure mode. In the second approach, the yield drift is computed from the predicted shear resistance and the predicted effective stiffness (Sections 6 and 7).

$$\delta_{cr} = 0.20\% \qquad \delta_{cr} = [0.1\% \dots 0.35\%] \qquad (12)$$

Approach 1: Flexural failure: $\delta_y = 1/6.5 \cdot \delta_u$ Flexural failure: $\delta_y = 1/[3.0 \dots 13.5] \cdot \delta_u$
 Shear failure: $\delta_y = 1/4 \cdot \delta_u$ Shear failure: $\delta_y = 1/[2.5 \dots 6.5] \cdot \delta_u$ (13)
 All failure modes: $\delta_y = 1/5 \cdot \delta_u$ All failure modes: $\delta_y = 1/[2.5 \dots 10.5] \cdot \delta_u$

Approach 2: $\delta_y = V_R/K_{eff}$ (14)

$\delta_{SD} = 0.5 \cdot \delta_u$ $\delta_{SD} = [0.25 \dots 0.70] \cdot \delta_u$ (15)

$\delta_{max} = 0.7 \cdot \delta_u$ $\delta_{max} = [0.50 \dots 0.85] \cdot \delta_u$ (16)

$\delta_c = 1.15 \cdot \delta_u$ $\delta_c = [1.10 \dots 1.30] \cdot \delta_u$ (17)

1 8.2.1 Model 1: Drift capacity at ultimate limit state as a function of failure mode and masonry typology

2 In the absence of further test data, the masonry typologies are divided into two groups only (Group 1: A-D, Group 2: E-E1). The
 3 values of Table 11 are simplified so that the drift capacity of walls failing in flexure corresponds to 1.5 times the drift capacity of
 4 walls failing in shear:

$$\delta_{u,flexure} = 1.5 \cdot \delta_{u,shear} \quad (18)$$

5 The drift capacity of the more regular masonry typologies (E-E1) is set to 2.5 times the drift capacity of masonry typologies A-D.
 6 The drift capacities at ultimate limit state for this first model and the corresponding CoVs are summarised in Table 11. The
 7 recommended CoVs for probabilistic assessments are 0.6 for masonry typologies A-D and 0.4 for masonry typologies E-E1. These
 8 recommended CoVs are approximate values of the CoVs reported in Table 13.

9 The drift capacities at the other limit states are computed using Eqs. (12)-(17). For a deterministic assessment, one typically uses
 10 a capacity that corresponds to a lower fractile value. Strength evaluations are typically based on the 5%-fractile value, which is
 11 referred to as the characteristic value. Current code estimates for drift capacities do not specify to which fractile value the drift
 12 capacity corresponds. If one assumes a lognormal distribution and the CoVs in Table 11, one obtains the ratios between fractile
 13 values and the median drift capacities as given in Table 12. For failure modes and masonry typologies for which the drift capacity
 14 can be predicted with a CoV of 0.6, the median drift capacity needs to be multiplied by 0.40 in order to obtain a drift capacity that
 15 corresponds to the 5%-fractile value. For a CoV of 0.4, 0.55 times the median drift capacity corresponds to the 5%-fractile value.

16 **Table 11 Drift capacity model 1: Recommended median drift capacities and coefficients of variations for δ_u .**

Masonry typology	Drift capacity [%]		CoV	
	Shear failure	Flexural failure	Shear failure	Flexural failure
A-D	0.60	0.90	0.60	0.60
E, E1	1.50	2.25	0.40	0.40

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18 **Table 12 Ratios between fractile drift values and median drift values assuming that the drift capacities follow a lognormal**
 19 **distribution (ratios are rounded to the closest 0.05).**

Fractile value	CoV=0.10	CoV=0.20	CoV=0.30	CoV=0.40	CoV=0.50	CoV=0.60	CoV=0.70	CoV=0.80	CoV=0.90
	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$	$\delta_{x\%}/\delta_{median}$
5%	0.85	0.70	0.60	0.55	0.45	0.40	0.35	0.30	0.30
10%	0.90	0.80	0.70	0.60	0.55	0.50	0.45	0.40	0.35
16%	0.90	0.80	0.75	0.70	0.65	0.60	0.55	0.50	0.45
50%	1	1	1	1	1	1	1	1	1

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1 Fig. 19 shows the distribution of the error between predicted and experimentally determined drift values for all six limit states.
 2 Table 13 summarises for the same values the median ratios of the predicted to experimental drifts and the CoV for the two groups
 3 of masonry typology (Group 1: A-D, Group 2: E-E1) and failure modes (shear/hybrid and flexure). The comparison assumes that
 4 the failure mode can be predicted correctly. One point was excluded from these plots and tables; this concerns the drift at the onset
 5 of cracking for Test ID 73 (cyclic in-situ test by Costa et al. 2011), which was reported as 0.008% and which is about 25 times
 6 smaller than drifts at the onset of cracking that were reported for other walls (Fig. 19a). As outlined at the beginning of Section 8,
 7 the drift values at the onset of cracking are not determined from the envelope curve but are taken from the test reports and are
 8 therefore not evaluated according to uniform criteria.

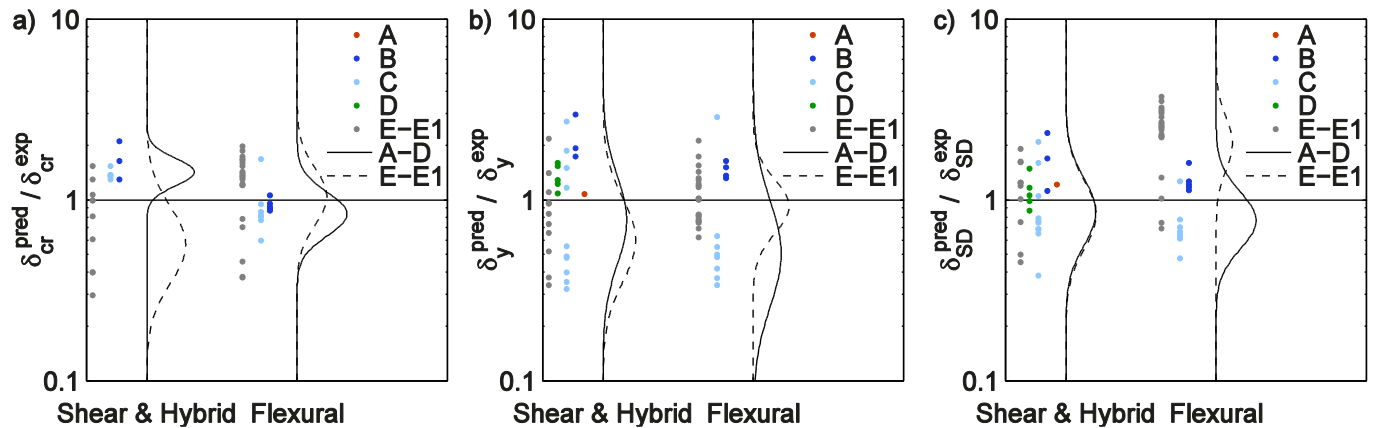
9 The displacement ductility values $\mu = \delta_u / \delta_y$ of the walls varied greatly (Section 8.1). This is reflected in the relatively large
 10 uncertainties (Table 13) when estimating the yield drift δ_y assuming constant ductility capacities for shear and flexural failures
 11 (Eq. (13)). However, due to the large uncertainty associated with the effective stiffness (Section 6), even larger CoVs are obtained
 12 when computing the yield drift from estimates of the shear strength and the effective stiffness (Eq. (14)). The distributions plotted
 13 in Fig. 19b show yield drift estimates that are computed assuming a fixed displacement ductility.

14 With the exception of the CoVs for δ_{cr} of masonry typology A-D, for which only a few data points are available, the CoVs of all
 15 limit states are rather similar and it is therefore recommended to use the CoVs that are given in Table 11 for the drift at the ultimate
 16 limit state as well for all other limit states. In some cases, the simple relationships of Eqs. (12)-(17) introduce a significant bias for
 17 a certain combination of failure mode and masonry typologies. Such a bias could of course be removed by assigning the coefficients
 18 of Eqs. (12)-(17) on a case-to-case basis. However, for the sake of simplicity and considering the imperfect data base, a drift
 19 capacity model of such complexity does not seem justified.

20 **Table 13 Drift capacity model 1: Median ratios and CoV for predicted to experimentally observed drift ratios ($\delta^{pred}/\delta^{exp}$).**
 21 **Mean ratios capacities and CoVs are rounded to the nearest 0.05; shear failure comprises shear and hybrid failures.**

Masonry typology	A-D				E-E1			
	Shear failure		Flexural failure		Shear failure		Flexural failure	
	Median ratio	CoV	Median ratio	CoV	Median ratio	CoV	Median ratio	CoV
δ_{cr}	1.40	0.20	0.90	0.30	0.80	0.50	1.35	0.35
$\delta_y - \text{const. duct.}$	1.25	0.60	0.60	0.75	0.85	0.55	1.00	0.35
$\delta_y = V_R/K_{eff}$	0.75	1.15	0.65	1.45	0.80	0.90	1.55	0.40
δ_{SD}	1.05	0.45	0.80	0.40	1.20	0.45	2.55	0.35
δ_{max}	1.50	0.55	0.95	0.50	1.05	0.45	0.80	0.65
δ_u	1.00	0.55	1.10	0.45	1.00	0.40	0.95	0.45
δ_c	1.40	0.40	1.40	0.25	-	-	-	-

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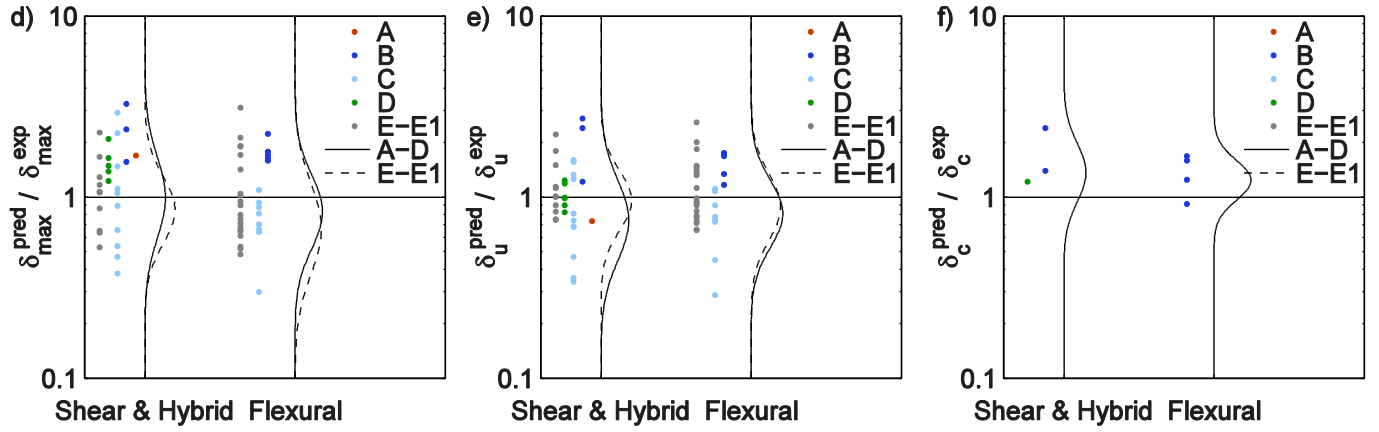


Fig. 19 Drift capacity model 1: Ratios of predicted to experimental drift capacities for the six different limit states.

8.2.2 Model 2: Drift capacity at ultimate limit state as a function of axial load ratio, shear span and masonry typology

The second drift capacity model links the ultimate drift capacity to the axial load ratio and the shear span, which is normalised by the height. It follows therefore the drift form introduced by Pfyl-Lang et al. (2011) and applied in Petry and Beyer (2014a). Fig. 20 plots the ultimate drift capacity that was normalised by $\min(H, L)/H_0$ against the axial load ratio. The trendlines included in the figures represent median values of drifts that were obtained for bins of axial load ratio (bin width: 0.1). Equations (19) and (20) aim at approximating these trend lines. This method was used in order to account for the fact that the number of tests per bin varies significantly and tends to decrease with increasing axial load ratio. Therefore, the higher axial load ratios would be underrepresented if a simple linear fit was performed. For masonry typologies A-D, the following equation for the ultimate drift is proposed:

$$\delta_u = \max(1.5\% - 4\% \cdot \frac{\sigma_{0,tot}}{f_c}, 0.3\%) \cdot \frac{H_0}{\min(H, L)} \quad (19)$$

The equations are applicable for $\sigma_{0,tot}/f_c \leq 0.6$ (Fig. 20b). For masonry typologies E and E1, the drift capacity is assumed to be 50% larger:

$$\delta_u = \max(2.25\% - 6\% \cdot \frac{\sigma_{0,tot}}{f_c}, 0.45\%) \cdot \frac{H_0}{\min(H, L)} \quad (20)$$

Note that for masonry typologies E and E1, only the first branch of the equation could be validated since walls of such typologies were not tested for large axial load ratios.

For both groups and failure modes, the CoVs for the ultimate drifts lie for this second model between 0.40 and 0.60 (Table 14). The CoV are with this model even somewhat smaller for masonry typologies A-D than for masonry typologies E-E1. For the sake of simplicity and because clear trends are not recognisable, it is recommended to use a CoV for all masonry typologies and failure modes, if this second drift capacity model is applied. It is suggested to use CoV=0.4 for δ_u and CoV=0.6 for all other limit states. The distribution of the error between the predicted and experimentally determined drift values for the second model is shown in Fig. 21.

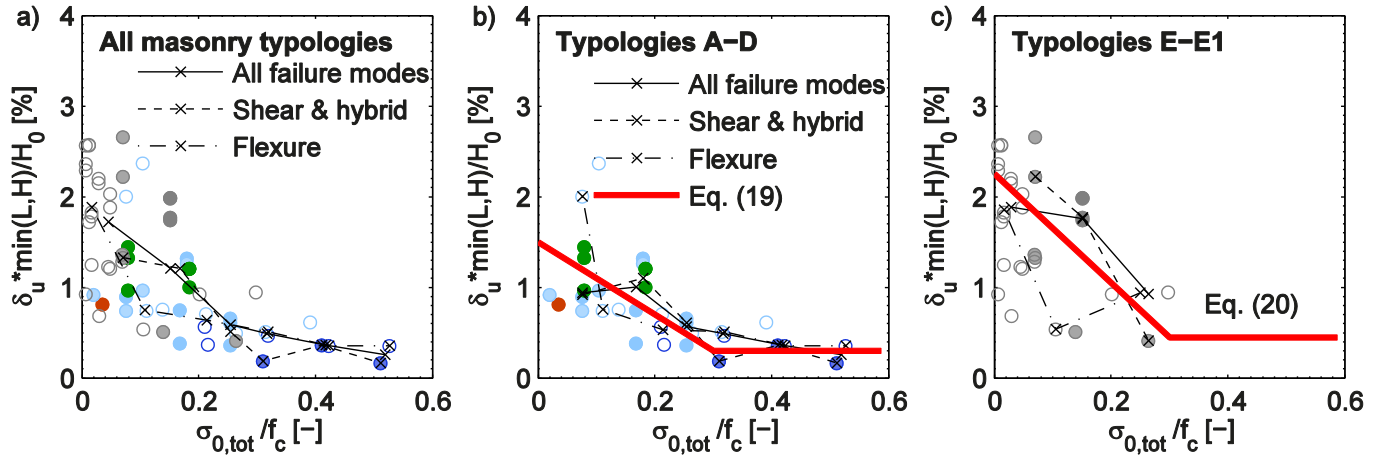


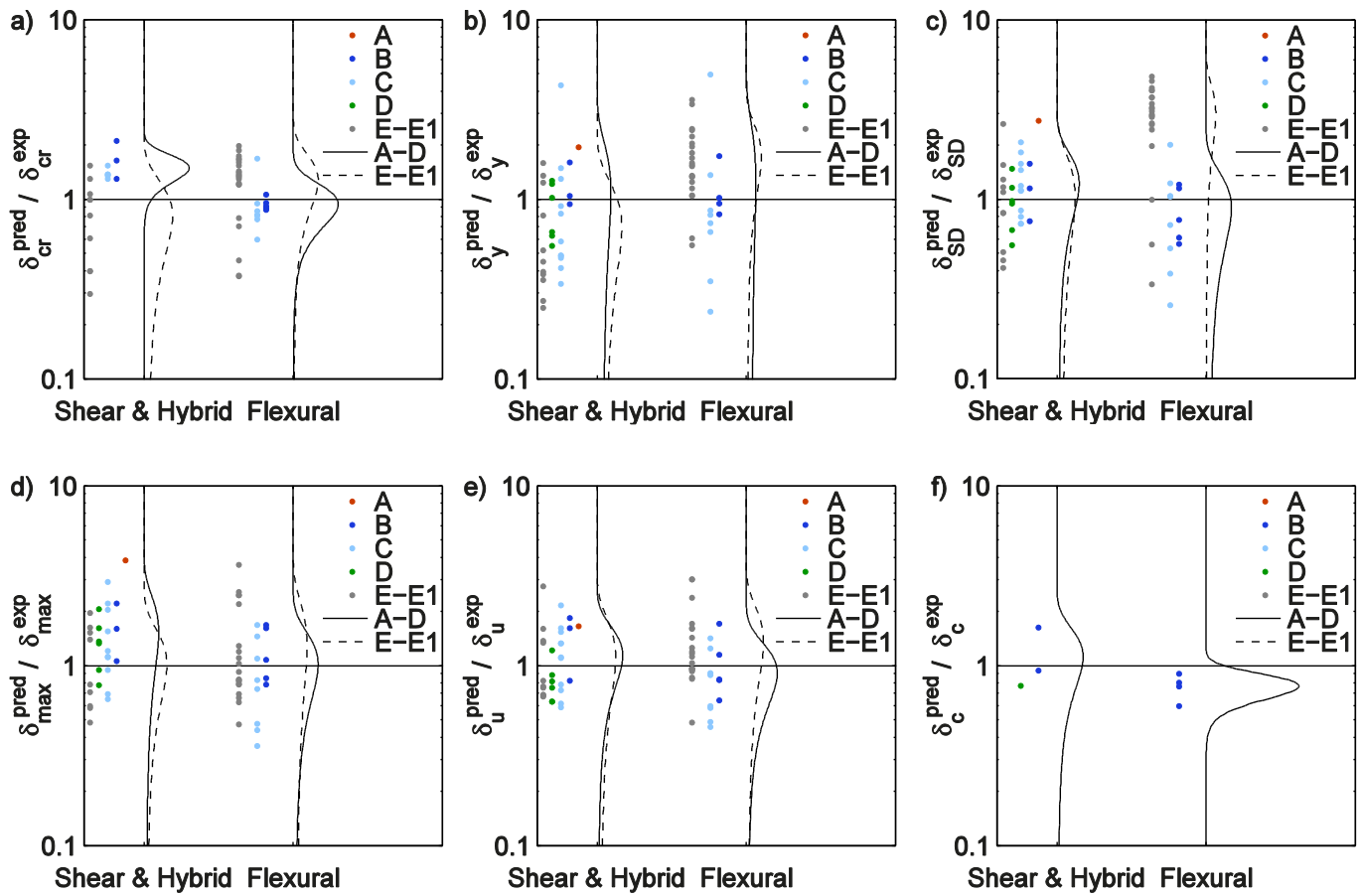
Fig. 20 Drift capacity model 2: Comparison of predicted and observed ultimate drift capacities for (a) all masonry typologies, (b) only masonry typology A-C, (c) only masonry typologies D-E1.

Table 14 Drift capacity model 2: Median ratio and CoV for predicted to experimentally observed drift ratios ($\delta^{pred}/\delta^{exp}$). Median ratios capacities and CoVs are rounded to the nearest 0.05; shear failure comprises shear and hybrid failures.

Masonry typology	A-D				E-E1			
	Shear failure		Flexural failure		Shear failure		Flexural failure	
	Median ratio	CoV	Median ratio	CoV	Median ratio	CoV	Median ratio	CoV
$\delta_{cr}^{1)}$	1.40	0.20	0.90	0.30	0.80	0.50	1.35	0.35
$\delta_y - \text{const. duct.}$	0.90	0.80	0.85	1.05	0.45	0.70	1.55	0.45
$\delta_y = V_R/K_{eff}^{1)}$	0.75	1.15	0.65	1.45	0.80	0.90	1.55	0.40
δ_{SD}	1.10	0.45	0.75	0.55	0.85	0.65	3.1	0.40
δ_{max}	1.35	0.55	0.85	0.45	0.70	0.50	0.85	0.65
δ_u	1.10	0.40	0.85	0.40	0.75	0.60	1.1	0.50
δ_c	0.95	0.40	0.80	0.15	-	-	-	-

1) Same values as for Model 1.

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Fig. 21 Drift capacity model 2: Ratios of predicted to experimental drift capacities for the six different limit states.

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8.2.3 Comparison of different drift capacity models

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The two models yield rather similar CoVs for the ultimate drift capacity (Model 1: 0.40-0.55; Model 2: 0.40-0.60). The error of Model 1 is expected to increase, if the predicted rather than the observed failure is used. The CoVs related to the ultimate deformation capacities of 0.40-0.60 might seem rather large. However, these CoVs are in fact similar to CoVs obtained for deformation capacities of reinforced concrete elements. Grammatikou et al. (2015) reported for reinforced concrete walls CoVs of 0.30 for the yield drift and between 0.30 and 0.50 for the ultimate drift, depending on the model used and the cross section of the wall. For reinforced concrete walls, the smallest CoVs were obtained with empirical models fitted to the data set and the largest CoVs with plastic hinge models (Grammatikou et al. 2015). More advanced analytical models for shear-critical reinforced concrete walls predict the ultimate drift capacity, however, with CoVs of less than 0.20 (e.g. Mihaylov et al. 2016). Similar CoVs for ultimate drift capacities are, however, also reached for clay brick masonry walls failing in shear or flexure if the drift capacity is predicted by an advanced analytical model (Petry and Beyer 2015; Wilding and Beyer 2017). Analytical models have therefore the potential to reduce the uncertainty related to the prediction of drift capacities and it is recommended to pursue in the future the development of such models for stone masonry walls. The reduction of the uncertainty is of course limited by the aleatoric variability, which—based on the limited data available—can be estimated to result in a CoV of 0.30 for the ultimate drift capacity (Table 3).

9 Summary and conclusions

The application of displacement-based assessment procedures requires robust estimates of the deformation capacity of every structural element. Eurocode 8, Part 3 (EC8-3, CEN (2005a)) as well as many other codes worldwide do not provide drift capacities specific to stone masonry walls. The objective of this project was to fill this gap and investigate specifically the drift capacity of stone masonry walls. In addition, the work aimed at providing input not only for the assessment of the ultimate limit state but for a large range of limit states ranging from the onset of cracking to the collapse of the wall. In view of probabilistic assessments, it was further the objective to provide next to median estimates also a measure of the confidence with which this quantity can be predicted. For this purpose, coefficients of variation (CoVs) were determined.

The work is based on a database of 123 shear-compression tests on stone masonry walls, which have been collected from 16 test campaigns documented in the literature; the database is made publically available. Based on these tests, stiffness, strength and deformation capacity were evaluated. The experimentally obtained values were compared to existing estimates and new or improved expressions proposed when this was indicated. More specifically, expressions for the following quantities as well as the corresponding CoVs were put forward (see summary in Table 15):

- Stiffness: New expression for the effective E-modulus for the use in conjunction with a Timoshenko beam element model. Two types of expressions are proposed: 1) Median values and CoVs for the effective E-modulus for each masonry typology. 2) A more refined expression that accounts for the masonry typology, the compressive strength and the axial load ratio.
- Strength: New values for the friction coefficient (Mohr-Coulomb criterion) and the tensile strength (Turnšek-Čačovič criterion). The values account for differences in stone masonry typologies.
- Drift capacity values for six limit states: Two simple drift capacity models for the ultimate limit state and relationships between other limit state and δ_u . The drift capacity models distinguish between two groups of stone masonry typologies (Group 1: A-D, Group 2: E-E1).
- Aleatoric variability: Aleatoric variabilities of stiffness, strength and drift limits for stone masonry.
- Effect of load history and light retrofit interventions: Factors accounting for the effect of load history (monotonic vs cyclic) and light retrofit interventions (mortar injections) on stiffness, strength and drift limits.

The following paragraphs discuss the main findings of this work and identify future research needs.

Typology:

- Following the classification in the Italian code, five typologies of stone masonry were distinguished, which account for the shape of the stones, the number of leaves and their connectivity as well as the stone properties. For regular dressed stone masonry (typology E), a sub-class E1 was introduced that comprises stone masonry walls of typology E with regular shape (ashlar) and dry joints. It was found that ashlar masonry with dry joints shows an increase in stiffness but have little influence on strength and deformation capacity.
- The current database is rather scarce with regard to tests on walls of masonry typology A and D. Due to its wide distribution in existing masonry buildings, further tests would be desirable, in particular, on walls of typology A.

Shear strength of stone masonry walls:

- From the three quantities needed to describe the bi-linear response curve of stone masonry walls (effective stiffness, strength and drift capacity), the strength of the masonry walls can be predicted with the largest confidence. However, the strength equations of the form given in EC8-3 do not predict the failure mode well. For about a quarter of the walls failing in shear, a flexural failure is predicted. To err with regard to the failure mode does not often result in a very large error with regard to the force estimate since shear and flexural capacity can be rather similar. However, it might lead to a considerable error in the drift capacity, if models are used that link the drift capacity to the failure mode (such as the one in EC8-3).
- EC8-3, which application is limited to concrete and brick masonry but in engineering practice often also applied to other masonry typologies, predicts the shear strength of masonry walls by a Mohr-Coulomb criterion assuming a friction coefficient of $\mu=0.4$. The latter appears to be too large when applied to stone masonry and the shear strength is therefore

1 often overestimated. Using regression analysis on the experimentally determined wall strengths, best estimates of friction
2 coefficients are calculated for each masonry typologies.

- 3 • Slightly smaller coefficients of variations are obtained if not a Mohr-Coulomb but a Turnšek-Čačovič criterion is used for
4 predicting the shear strength. This criterion needs as input a tensile strength of the masonry. The Italian code (NTC 2008;
5 MIT 2009) provides reference values, which predicted the shear strength of the walls in the database very well. However,
6 the CoV which could be desumed from the Italian code, assuming that the given range limits correspond to 16th and 84th
7 percentiles, seems to be too low by a factor of approximately 2. Borri et al. (2015) proposed an expression for the tensile
8 strength which includes the Masonry Quality Index. Regression analysis on the shear strength and Masonry Quality Index
9 of the walls included in the database confirm the expression proposed by Borri et al. (2015).

10 Effective stiffness of stone masonry walls:

- 11 • Estimating the effective stiffness of stone masonry walls is considerably more challenging than estimating their strength
12 and the CoVs of predicted to experimentally determined stiffness is for all masonry typologies approximately 2-3 times
13 larger than the CoVs for the strength. The effective stiffness can, however, be predicted with a slightly better confidence
14 than the elastic wall stiffness. The ratio of effective to elastic stiffness varies greatly but the median ratio is close to 0.5,
15 which corresponds to the value recommended in EC8-3.
- 16 • Available experimental results suggest that shear deformations contribute significantly to the flexibility of the walls but
17 direct evaluations of the effective shear stiffness from experimental results are scarce. If one assumes a ratio of the shear
18 to the elastic modulus and applies a Timoshenko beam element model, one can back-calculate the effective E-modulus
19 from the wall stiffness. It was found that this effective stiffness depends on the masonry typology, the compression
20 strength and the axial load ratio, i.e., the larger the axial load ratio, the larger the stiffness. The effect of the axial load
21 ratio on the stiffness is not accounted for by modelling recommendations in current codes such as EC8-3, which connect
22 the E-modulus solely to the compression strength, but it has already been identified by other research groups (Vasconcelos
23 2005; Bosiljkov et al. 2005). A new analytical expression for the effective E-modulus, which accounts for masonry
24 typology, compression strength and axial load ratio, is proposed.
- 25 • It was further investigated if results from material tests lead to an improved estimate of the wall stiffness. The considered
26 material tests were compression tests and dynamic identification tests. Surprisingly none of these results led to an
27 improved estimate of the horizontal wall stiffness. One reason could be that the material tests addressed the E-modulus
28 (i.e. flexural deformations) while shear deformations might contribute significantly to the wall flexibility. Another reason
29 could be that the applied Timoshenko beam model is not appropriate to describe the wall kinematics and therefore the E-
30 moduli that yields the best prediction is not related to a mechanical property of the material.

31 Drift capacity of stone masonry walls

- 32 • For the analysis of the drift capacities, only the cyclic tests were considered. Comparing the results of a monotonic and a
33 cyclic test that were carried out within one test series suggests that the deformation capacity of cyclic tests is approximately
34 only half of the deformation capacity under monotonic loading; this ratio was also observed for brick masonry walls
35 (Beyer et al. 2014). The available data set did not allow more advanced analyses of the effect of the load history on the
36 drift capacity as the parameters describing the cyclic loading protocol (number of cycles, drift intervals, mean value, ...) were not varied in any of the test campaigns.
- 37 • Six different drift limit states were considered; these are (i) the drift at the onset of cracking δ_{cr} , (ii) the drift at yield δ_y ,
38 (iii) the drift at maximum force δ_{max} , (iv) the drift at the limit state “Significant damage” $\delta_{SD} = \min(3\delta_{cr}, \delta_{max})$, (v) the
39 drift at ultimate limit state (20% strength drop) δ_u , (vi) the drift at collapse (50% strength drop) δ_c . With the exception of
40 the drift at the onset of cracking, all drift limits were determined from the envelope of the force-drift relationship or its
41 bilinear approximation. The drift at the onset of cracking was, if available, taken from test reports. The drift for which the
42 least information was available is the drift at collapse. Only a very few tests were continued up to collapse and any
43 estimates derived for this limit state need to be considered with great caution. To research this drift limit state further,
44 additional experimental data is needed.
- 45 • For analysing the drift capacities, the tests were divided into two groups; the first group comprised walls of typologies A-
46 D and the second walls of typologies E-E1. Given the rather large variability of the drift capacities and the limited number
47 of tests available, a finer analysis did not seem warranted. Next to median values and CoVs for each group and failure
48 mode, also two simple models for the ultimate drift capacity were proposed. The first connects the drift capacity to failure
49 mode and masonry typology and follows therefore the approach of EC8-3 and many other current codes. The second one
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1 links the drift capacity to masonry typology, axial load ratio and the factor $H_0/\min(H,L)$ where H_0 is the shear span and H
2 and L the wall height and length, respectively. The two models lead to very similar CoVs. With the exception of the limit
3 state at the onset of cracking, the drift capacities at the other limit states were expressed as a function of δ_u . The drift at
4 the onset of cracking was assigned a constant value ($\delta_{cr}=0.20\%$).

- 5 • The current drift capacity model as well as the models proposed in this paper are empirical drift capacity models. In future
6 tests, it would be desirable to also develop mechanical drift capacity models, which for brick masonry walls have already
7 led to a considerable improvement in the drift capacity prediction (Section 8.2.3). For this purpose, wall tests with detailed
8 measurements of the displacement fields are necessary. This would also allow to identify better the contributions of shear
9 and flexural deformations to the total deformations and therefore pave the way for improved stiffness estimates.
10 Furthermore, the effect of the stone pattern on the wall response should be investigated and first studies in this regard are
11 currently underway.

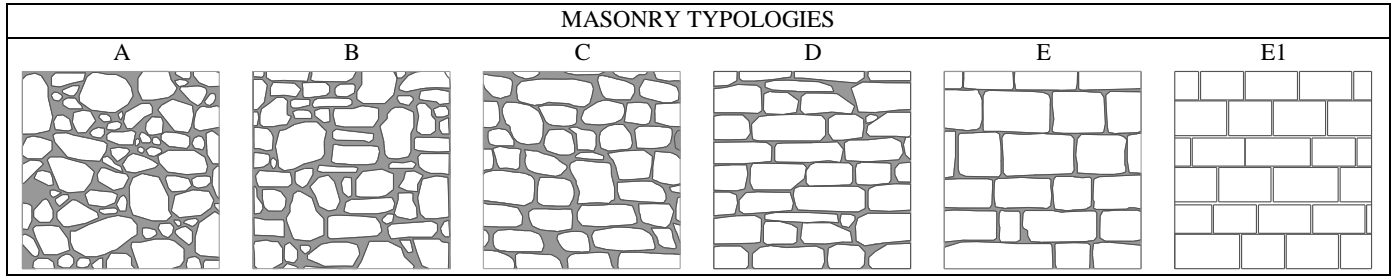
12 Aleatoric variability

- 13 • The database contains 18 groups of replicate tests, which were used to estimate the aleatoric variability of stiffness,
14 strength and drift capacities at different limit states. The strength varies in general the least (CoV=0.1). Stiffness and drift
15 capacities vary more (CoV=0.2-0.3). Only the drift at the onset of cracking seems to lead to a smaller CoV (CoV=0.1).
16 None of the replicate tests was continued up to collapse and therefore the aleatoric variability could not be determined for
17 δ_c . From the available data, it was not possible to identify the effect of the masonry typology on the aleatoric variability.
18 Also, all but one group of replicate tests were laboratory tests, which might not necessarily reproduce the aleatoric
19 variability in real buildings. From the available data no significant difference between laboratory and in-situ tests could
20 be identified. In future studies it would therefore be interesting to investigate the variation of aleatoric variability with
21 masonry typology and to conduct further replicate in-situ tests.

22 Effect of retrofit interventions on drift capacity

- 23 • Also included in the database are tests with minor retrofit intervention (mortar injections or reinforcement through the
24 wall thickness to improve the connection between the leaves). By comparing walls with mortar injections to their
25 unstrengthened counterparts, the effect of the retrofit interventions could be identified. For stiffness and strength, such
26 factors are already available in the Italian code (MIT 2009) and these were confirmed by the results obtained here. As a
27 novelty, factors for the drift capacity were derived. The results showed that the ultimate drift capacity can increase by a
28 factor of 3-6; the increase is particularly significant if the failure mode changes from shear to flexure. The experimental
29 data on the effect of retrofit interventions is, however, still rather scarce and more data necessary. Mechanical drift
30 capacity models, once they are available, might allow to predict the effect of retrofit interventions without testing all
31 possible configurations.

1 **Table 15 Summary of proposed median values and coefficients of variations for stone masonry assessment**



FORCE CAPACITY			A	B	C	D	E-E1
Flexure: $V_{fl} = \frac{L^2 t}{2H_0} \sigma_0 \left(1 - 1.15 \frac{\sigma_0}{f_c}\right)$, f_c from (1)		1. f_c [MPa] ¹	1.40	2.50	3.20	1.90	7.00
		CoV ¹	0.30	0.20	0.19	0.27	0.14
Shear: $V_{sh} = \frac{L t}{b} f_t \sqrt{1 + \frac{\sigma_0}{f_t}}$ $f_t \cong 0.015 + 0.006 \cdot MQI^{1.5}$, or from (3)		2. f_t code [MPa] ¹	0.039	0.065	0.098	0.053	0.158
		CoV	0.24	0.19	0.14	0.20	0.14
If a Mohr Coulomb criterion is preferred: values and CoVs for the friction angle in (4), $c = 2\mu f_t$		3. f_t exp. [MPa]	0.045	0.045	0.110	0.050	0.130
		CoV	0.80	0.30	0.20	0.50	0.40
		4. Friction coeff.	0.45	0.20	0.25	0.25	0.30
		CoV	0.20	0.15	0.15	0.10	0.10

¹ from MIT (2009); coefficient of variation derived from CNR (2013)

EFFECTIVE STIFFNESS			A	B	C	D	E-E1
$E_{eff} \cong \left(\frac{E}{f_c}\right)_{ref} f_c \cdot \frac{\sigma_0/f_c}{0.30}$ or from (1-2).		1. E_{eff} code [MPa] ¹	430	610	870	540	1400
		CoV ¹	0.20	0.20	0.15	0.20	0.15
$K_{eff} = \frac{1}{\frac{H^3}{2E_{eff}} \left(\frac{H_0}{3}\right) + \frac{6H}{5G_{eff} L t}}$ with $\frac{G_{eff}}{E_{eff}} = 0.33$		2. E_{eff} exp. [MPa]	320	(2240)	900	430	500-650
		CoV	0.50	(0.25)	0.40	0.40	0.50
		3. $(E/f_c)_{ref}$	400	(700)	300	250	200-250
		CoV	0.40	0.40	0.40	0.40	0.40

¹ from MIT (2009); coefficient of variation derived from CNR (2013)

DISPLACEMENT CAPACITY				A-B-C-D		E-E1	
Drift at cracking: $\delta_{cr} = 0.20\%$	Drift at SD limit state $\delta_{SD} = 0.50 \cdot \delta_u$			Shear failure	Flexural failure	Shear failure	Flexural failure
Yielding drift:	Drift at max. force: $\delta_{max} = 0.70 \cdot \delta_u$						
- shear $\delta_y = 1/4 \cdot \delta_u$	Drift at collapse $\delta_c = 1.15 \cdot \delta_u$			Model 1: δ_u			
- flexure $\delta_y = 1/6.5 \cdot \delta_u$				CoV	0.50	0.50	0.50
Ultimate drift:	- Model 1: reference values from table						
	- Model 2: $\delta_u = \max(1.5\% - 4\% \cdot \frac{\sigma_{0,tot}}{f_c}, 0.3\%) \cdot \frac{H_0}{\min(H,L)}$ (typologies A-B-C-D)						
	$\delta_u = \max(2.25\% - 6\% \cdot \frac{\sigma_{0,tot}}{f_c}, 0.3\%) \cdot \frac{H_0}{\min(H,L)}$ (typologies E-E1)						

ALEATORIC VARIABILITY	Suggested coefficients of variation							
	K_{eff}	V_u	δ_{cr}	δ_y	δ_{SD}	δ_{max}	δ_u	δ_c
A-E1	0.20	0.10	0.10	0.20	0.30	0.30	0.30	-

7 Acknowledgments

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9 Construction Department of the Canton Basel-Stadt.

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