Master thesis report

Quantum Technology: Single-Photon Source

CONFIDENTIAL

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Abstract

This report is a synthesis of my master thesis internship at the National Institute of Informatics in Tokyo that last during the summer of year 2012. I worked in the Quantum Information Science Theory (QIST) group under supervision of Prof. Kae Nemoto and Dr. Simon Devitt. The group works on theoretical and experimental implementations of quantum information science.

The aim of my project was to study and improve quantum optical systems. I first studied different fields and systems of quantum information science. Then I focused my research on single-photon sources, entangled photon sources and interferometric photonic switches. Finally, some strategies had to be found to design an efficient and optimized single-photon source that could be built with today’s technologies. This report describes in details the created and optimized design of a single-photon source based on Spontaneous Parametric Downconversion (SPDC).

Résumé (French)

Ce rapport est une synthèse de mon stage de fin de master à l’Institut National d’Informatique de Tokyo, qui s’est déroulé pendant l’été 2012. J’ai travaillé dans le groupe de recherche d’information quantique (QIST) sous la supervision du Prof. Kae Nemoto et du Dr. Simon Devitt. Ce groupe travaille à la réalisation théorique et pratique de systèmes et modules quantiques.

Le but de mon projet était d’étudier et de chercher à améliorer les systèmes optiques quantiques. J’ai tout d’abord étudié plusieurs domaines et systèmes relatifs à la théorie de l’information quantique. Par la suite, je me suis focalisé sur les sources monophotoniques, les sources photoniques intriquées et l’interférométrie quantique. Enfin, j’ai cherché une nouvelle stratégie pour améliorer et optimiser des sources monophotoniques implémentables avec la technologie actuelle. Ce rapport décrit en détail le fonctionnement et les composants de telles sources de type SPDC (Spontaneous Parametric Downconversion).

Riassunto (Italian)

Questo relacione è una sintesi del mio stage di master, presso l’Istituto Nazionale di Informatica nel Tokyo, che ha avuto durante l’estate 2012. Ho lavorato nel gruppo di ricerca di informazioni quantistiche (QIST) con la Prof. Kae Nemoto e il Dr. Simon Devitt. Questo gruppo lavora per realizzare moduli teorici e pratici di sistemi quantistici.

Lo scopo del mio progetto era di studiare e migliorare li sistemi ottici quantistici. Ho studiato vari campi e sistemi di scienza dell’informazione quantistica. Poi, ho focalizzato la ricerca sulle sorgenti di singoli fotoni, sulle sorgenti di fotoni intricati, e sulle sistemi con interferometria quantistica. Infine, ho trovato nuove strategie per realizzare sorgenti di singoli fotoni efficienti e ottimizzate, che potrebbe essere costruito con le tecnologie di oggi. Questo relacione è una descrizione de un sorgento di singoli fotoni di SPDC (Spontaneous Parametric Downconversion) ottimizzate.
 Acknowledgment

I would like to thank Prof. Kae Nemoto and D. Simon Devitt, my supervisors, for accepting me, for their support and for giving me the opportunity to discover, study and work in and the interesting domain of Quantum Information Theory.

I also acknowledge the QIST members for its welcome, for helping me, for giving me advice and for all the interesting discussions I had with them.
Contents

1 Working at NII 5
  1.1 The National Institute of Informatics ........................ 5
  1.2 The Quantum Information Science Theory group ............. 6
  1.3 Timetable .................................................. 7

2 Spontaneous Parametric Downconversion single-photon source 9
  2.1 Single-photon source ......................................... 9
  2.2 Single-photon detector ....................................... 9
  2.3 SPDC theory .................................................. 9
  2.4 SPDC source ................................................ 10
  2.5 Optical switch .............................................. 11
  2.6 Prior art SPDC based source ................................ 12

3 Design of SPDC based single-photon source with output rate up-conversion multiplexed architecture 13
  3.1 Generalities ................................................. 13
    3.1.1 Abstract .............................................. 13
    3.1.2 Aim .................................................. 13
  3.2 General scheme .............................................. 14
  3.3 Detailed description of elements .............................. 15
    3.3.1 Downconverters ....................................... 15
    3.3.2 Crossed by-passable binary delay register ............ 16
    3.3.3 Routing tree ......................................... 16
  3.4 Detailed functioning ......................................... 18
    3.4.1 Output rate up-conversion ............................. 18
    3.4.2 Stability enhancement .................................. 18
    3.4.3 Switching decisions ................................... 19
  3.5 Advantages to prior art ..................................... 19

4 Detailed analysis of the SPDC based single-photon source with output rate up-conversion multiplexed architecture 20
  4.1 Case analysis of emission probability ....................... 20
  4.2 Simulation .................................................. 20
    4.2.1 Working parameter variation .......................... 21
    4.2.2 Structure size ......................................... 23
    4.2.3 Feed-back ............................................. 23
  4.3 Conclusion of the analysis ................................ 24
Chapter 1

Working at NII

1.1 The National Institute of Informatics

The National Institute of Informatics is a Japanese research institute aiming at advancing the study of informatics in a very wide range (Fig. 2), from natural science to human and social sciences.

Figure 1: The NII main building.
The institute encourages international partnerships and is devoted to spreading of scientific information, graduate education, social development and managing of intellectual properties. The NII has established four research divisions (Tab. 1), six research centers and cooperations with 73 overseas institutes. The NII also maintains Webcat, a large and searchable information database on a variety of scientific and non-scientific topics, and publishes four public information magazines.

Table 1: The four research departments.

<table>
<thead>
<tr>
<th>Research Department</th>
<th>Principles of Informatics</th>
<th>Information Systems Archit.</th>
<th>Digital Content Media Sciences</th>
<th>Information and Society</th>
</tr>
</thead>
<tbody>
<tr>
<td>New principles and theories in informatics, as the development of technology or new domains that will support the society.</td>
<td>Research into the architecture and systemization of software and hardware for computers and networks.</td>
<td>Analysis and processing methods for diverse content and media, such as texts and video images, to their systemization.</td>
<td>Research in human and social sciences in a society in which information society and real world are integrated.</td>
<td></td>
</tr>
</tbody>
</table>

1.2 The Quantum Information Science Theory group

The QIST group is a small team of about ten researchers, led by Prof. Kae Nemoto. It focuses its research on the theoretical and experimental implementations of Quantum Information Science.

The group works mainly on photonic entanglement, optical quantum gates and semiconductor quantum gates, topological quantum computation and error analysis and quantification in quantum computation and communication.
1.3 Timetable

During my internship, I was part of the QIST group research fellow. I had to fit in the team and participate to the weekly presentations or discussions within the group and with the visiting researchers.

When I arrived at NII, I trained on quantum mechanics and technologies. I focused step by step on more specific research. I made presentations to explain my research and to make a comparison to the semi-classical world models I used during my studies. By this method, I spent a long time studying and discovering various fields and systems, which I reported the most interesting to my group.

The time table of my work at NII is the following:

- **Phase 1:** 20\(^{th}\) March (arrival) to 20\(^{th}\) April 2012
  - Training to quantum information theory
  - Training to quantum optics

- **Phase 2:** 20\(^{th}\) April to 20\(^{th}\) May 2012
  - Study of optical systems: quantum cavities, VSEL, photonic crystals
  - Introduction to quantum optics: Quantum Electrodynamics (QED), Nitrogen-Vacancy (NV) center, Linear Optic Quantum

- **Phase 3:** 20\(^{th}\) May to 10\(^{th}\) June 2012
  - Focusing on single-photon sources, entangled photon sources and Linear Optical Quantum Computation (LOQC)
  - Research of photon gun and entangled photon gun based on quantum cavities
  - Research of single-photon sources

- **Phase 4:** 10\(^{th}\) June to 1\(^{st}\) July 2012
  - Specific research on Spontaneous Parametric Downconversion (SPDC)
  - Specific research on interferometric switches with few photons
  - Specific research on multi-photon problems

- **Phase 5:** 1\(^{st}\) July to 20\(^{th}\) July 2012
  - Design of SPDC based systems
  - Calculation of interferometric structures for single-photon and multi-photon management

- **Phase 6:** 20\(^{th}\) July to 10\(^{th}\) August 2012
  - Optimization of the SPDC based single-photon source
  - Discussion on the interests and possibilities
  - Calculation (theoretical and by case analysis) of the device possibilities
  - Calculation of interferometric structures for single-photon and multi-photon management

- **Phase 7:** 10\(^{th}\) August to 30\(^{th}\) August 2012
  - Discussion on the device
– Simulation of the device
– Analysis of the device parametric variations with simulation

• Phase 8: From now...
  – Patenting with the NII
  – Writing of the paper with the QIST members
  – Preparing the first experimentation with overseas partners
  – Discussing again on MZI for single-photon and multi-photon management
Chapter 2

Spontaneous Parametric Downconversion single-photon source

2.1 Single-photon source

An ideal single-photon source is a source that can emit at any arbitrary and defined time (on-demand), in which the probability of single-photon emission is 100% and the probability of multiple-photon emission is 0%. Emitted photons are indistinguishable and repetition rate is arbitrarily fast.

We imagine building single-photon sources from various systems: quantum dots, single atom, ion or molecule. Another possibility is to use a probabilistic system based on photon Spontaneous Parametric Downconversion (SPDC).

2.2 Single-photon detector

Single-photon detectors based on single-photon avalanche photodiodes, photomultiplier tubes, superconducting nanowires are typically used as non photon-number resolving detectors. They can only distinguish zero photon and more than zero photons, and they are the most commonly used single-photon detectors.

Others are photon-number resolving detectors. While detecting a single photon is a very difficult task, discriminating the number of incident photons is even more difficult. One direct approach is simply to break the detector active area into distinct pixels and split the idler signal onto these pixel areas. Another approach is based on superconducting tunnel junction, but their complexity are high, their efficiencies are not very high, their resolution and speed are limited, and their working temperature very low (< 0.4 K).

2.3 SPDC theory

The response of an optical material to incoming fields is the combination of responses from a large number of atoms making up that material. The Maxwell equations for a simple linear material response with electric given by the following equation:

\[ P = \epsilon_0 \chi E \]  \hspace{1cm} (1)
where \( \mathbf{E} \) is the original electric field, \( \mathbf{P} \) is the material polarization and \( \chi \) the susceptibility tensor of the material (for isotropic media like a gas or a glass, it is a scalar).

In a nonlinear material, the response of the medium to an exciting field is non-linear, as:

\[
\mathbf{P} = \varepsilon_0 (\chi \mathbf{E} + \chi^{(2)} \mathbf{E}^2 + \chi^{(3)} \mathbf{E}^3 \ldots) \tag{2}
\]

where \( \chi^{(n)} \) are the susceptibility tensors of higher order in the material response. The nonlinear response is usually small. The second order term \( \chi^{(2)} \) is due to a lack of inversion symmetry in the material crystal. Thus amorphous materials like glass or polymers present the property \( \chi^{(2)} = 0 \).

For a monochromatic laser, the electric field is of the form:

\[
\mathbf{E}(x, t) = \mathbf{E}_0 e^{i(kx - \omega t)} \tag{3}
\]

The second order nonlinear susceptibility results in a polarization component which oscillates at twice the original frequency:

\[
\mathbf{P}^{(2)}(t) \propto \chi^{(2)} \mathbf{E}^2 \propto \chi^{(2)} \mathbf{E}_0^2 e^{-2i\omega t} \tag{4}
\]

This polarization component at a new frequency can be considered as a source in the Maxwell equations, and will propagate through the material according to the dispersion relation.

This process creates from a single photon a pair of photons of equal energy (half the energy of the original photon). It is a three wave mixing process. A laser pulsed onto a non-linear crystal results in the following quantum state:

\[
|\phi> = \frac{1}{cosh(r)} |00> + \frac{tanh(r)}{cosh(r)} |11> + \frac{tanh(r)^2}{cosh(r)} |22> + \frac{tanh(r)^3}{cosh(r)} |33> \ldots \tag{5}
\]

where \( r \propto \chi^{(2)} \varepsilon_0 t \) and \( t \) is the length of the non-linear crystal, so the interaction length of the non-linear process.

The state \( |00> \) is the non-creation of downconverted pair, so the conservation of the original photons. The state \( |nn> \) represents the creation of \( n \) pairs of photons \( |11> \) by downconversion of the original photon.

### 2.4 SPDC source

In a SPDC source, a pump laser illuminates a material with a \( \chi^{(2)} \) optical nonlinearity, creating two photons called Signal and Idler, under the constraints of momentum and energy conservation (Fig. 3). The detection of one trigger photon indicates, or heralds, the presence of its twin, that can thus be sent into an optical network and the photon-source output.

![Figure 3: Spontaneous Parametric Downconversion of one photon into two photons.](image-url)
It is a probabilistic process. Because of this nature, in addition to the probability of generating one pair of photons, there is also a finite probability of generating more than one pair via higher order emissions.

The Eq. 5 directly simplifies in probabilities of generating $n$ pairs of photons per pulse led by a Poisson distribution:

$$P_n = \frac{N^n e^{-N}}{n!}, \ n \in \mathbb{N}$$

(6)

where $N$ is the mean number of pairs, it depends on the pump power and parameters of the crystals.

Such behavior decreases the quality of the single-photon source. Since photon-number resolving detectors are too complicated to integrate and too expensive, non photon-number resolving detectors are used to herald the Idler photon. SPDC heralded sources must be held to average pair production levels much less than one to avoid producing multiple pairs which would result in the heralded channel containing more than one photon.

2.5 Optical switch

The best optical switch for single photons consists in a Mach-Zehnder Interferometer (MZI). A 3 dB splitter and a 3 dB combiner connected by two interferometer arms. By changing the effective refractive index of one of the arms, the phase difference at the beginning of the combiner can be changed, such that the light switches from one output port to the other. The structure is fabrication tolerant and polarisation insensitive. A schematic layout of the MZI-based switch is depicted on Fig. 4.

Figure 4: Schematic layout of the waveguiding structure of the MZI based switch.
after the different elements of the switch, as pictured on Fig. 4:

$$|\psi_{MM1} > = \frac{1}{\sqrt{2}}(|1_a0_b > + |0_a1_b >)$$  \hspace{1cm} (7)

$$|\psi_{Phase} > = \frac{1}{\sqrt{2}}(|1_a0_b > + e^{i\Delta\phi} |0_a1_b >)$$  \hspace{1cm} (8)

$$|\psi_{MM2} > = \frac{1}{2}[(1 + e^{i\Delta\phi}) |1_a0_b > + (1 - e^{i\Delta\phi}) |0_a1_b >]$$  \hspace{1cm} (9)

Interferences with $\Delta\phi$ led to a determined position of the photon into one of the output selected by setting $\Delta\phi$ to 0 or $\pi$.

\section*{2.6 Prior art SPDC based source}

Most of SPDC based sources work with a temporal or a spatial multiplexing of one or several pumped crystals using a switching network. Thus, they have the same frequency as pumping or a (low) divisor. In both cases, the multiplexing cannot control more than one photon and the Poissonian statistics of SPDC leads to a waste of photons or a stronger multi-photon rate\cite{11-13}\. Some SPDC based sources also try to use photon storage into different kinds of loops or cavity systems without meeting great success\cite{14,15}\. 
Chapter 3

Design of SPDC based single-photon source with output rate up-conversion multiplexed architecture

3.1 Generalities

3.1.1 Abstract

We describe a single-photon source based on an array of spontaneous parametric down-conversion (SPDC) modules multiplexed by an integrated structure composed of electro-optic switches and delay wave-guides.

The suggested optical device allows to increase the output photon source rate compared to the SPDC module laser pump rate and enhances both stability, controllability, and efficiency.

This device transforms the spatial multiplexing into a temporal multiplexing with temporary photon storage. The photons are stored into different delay lines and temporally sequentialized. This train of photon can then be used in high frequency emission and compensation of photon lack among the next pump cycles.

The implementation consists of a crossed multiplexed architecture using electro-optic switches. The architecture first drives the downconverters array outputs into several layers of delay lines organized in shared and by-passable binary delay register. The architecture then includes a routing tree driving all the photons into a single output.

3.1.2 Aim

I aimed at creating a high efficiency device, eliminating the waste of photons and the stability problems due to probabilistic behavior of spontaneous downconversion. I also wanted a different way of thinking. The tools are known, the direction is different, but the result is there, and better. It takes a logical and optimistic look toward advanced research on quantum computer.

The main advantages of the frequency up-conversion toward the pumping rate is the reduction of length of the integrated optics and the possibility to overtake heralding detector problems. While progress of integrated MZI interferometers, integrated wave-guides or pho-
tonic crystals is prompt, single-photon detector technology, number-resolving or non-number-resolving, is still far from the same level of development.

This suggested device offers the possibility to build an advanced integrated optical device, moreover functional element of a future quantum computer, whose design gives the most of its flexibility to its detectors and the most of its potential to its optical control.

3.2 General scheme

The following picture shows the general scheme of the generic device structure created, that can be modified in size or position of some components (see section 3.3.3).
3.3 Detailed description of elements

3.3.1 Downconverters

The pump laser illuminates a array of $\chi^{(2)}$ non-linear crystals, creating both idler and signal photons. The idler photons are sent to heralding detectors connected to a processor unit (as an FPGA). The signal photons are sent into the integrated architecture through delay fibers to let time for the processor unit to take path decisions.
The delay fibers have slightly different lengths to correct the entering time differences among emitted photons due to the growing distance between the pump and each crystal of the array.

The number of SPDC modules can be chosen and optimized for the symmetry of the linear then logarithmic routing into the single output. In the hypothesis of a photon driving demonstration, single-photon or multi-photon are driven in the same way through standard MZI switches. Thus, a small number of downconverters (below twenty) can be chosen with an exaggerated photon rate. For a demonstration of efficient single-photon source, number of downconverters must be higher (from a few tens to more than hundred).

3.3.2 Crossed by-passable binary delay register

![CBBDR Diagram]

Figure 6: 0-7T delay register paths. Delays: red: 2T, green: 3T, blue: 4T, yellow: 5T.

The crossed by-passable delay register (CBDR) structure is the heart of the invention. It distributes the photons in a train of period $T$. The CBDR can achieve photon delays between 0T to $(2^N - 1)T$ with $N$ number of delay steps. Thus, a 3-step register can delay photons from 0 to 7T (Fig. 6).

In a given architecture, due to the asymmetry of the structure, control of boundary photons is more or less limited as shown on Table 2. It is not an important problem if we choose good actuation rules (see fast-to-slow top-to-down driving in the next sections) or if we simply remove one or two boundary downconverters.

3.3.3 Routing tree

This structure simply drives the different delayed photons into a single output. The amount of switches increases in a logarithmic scale of the number of delayed single-photon inputs. It
Table 2: Limitation of control of boundary downconverters for a 0-7T register structure.

<table>
<thead>
<tr>
<th>SPDC N°</th>
<th>Inaccessible states</th>
<th>SPDC N°</th>
<th>Inaccessible states</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1T, 2T, 3T, 4T, 5T, 6T, 7T</td>
<td>N-2</td>
<td>0T</td>
</tr>
<tr>
<td>2</td>
<td>3T, 5T, 6T, 7T</td>
<td>N-1</td>
<td>0T, 1T, 2T, 4T</td>
</tr>
<tr>
<td>3</td>
<td>7T</td>
<td>N</td>
<td>0T, 1T, 2T, 3T, 4T, 5T, 6T</td>
</tr>
</tbody>
</table>

also allows to drive out of the structure the possible excess of photons.

For large structures and because of the low single-photon generation probability per down-converter (usually lower than 10%), we can imagine different trees. It may be distributed before, after or in between the steps of the crossed binary delay register (Fig. 8). In this case, a more complex driving of photons needs to be established to avoid photon bunching (but more opportunities come to drive out concurrent or excess) or to consider it (using MZI switches in different configurations).

Figure 7: Alternative structures. (left) Routing distributed in between delaying gives a more efficient integration on chip. (center) Routing before and after delaying is optimized for very low pumping power and high quality single-photon. (right) Reducing of one layer of switches by parity trade-off.

Figure 8: Alternative distributed network to optimize on chip integration.
3.4 Detailed functioning

3.4.1 Output rate up-conversion

The CBDR structure and routing tree build a T-periodic photon train at each pumping pulse on the downconverter array. The rate of downconverter and the number of downconverters is matched in order to obtain enough photons to emit a train of several photons at the frequency of the pumping. The photon source frequency is thus a multiple of the pump frequency. With a 0-\(7T\) by-passable binary delay register, the longest photon train is 8. In this example, the maximal frequency multiplication is 8.

The maximal photon source frequency is fixed by the CBDR implementation to the first delay step \(T\). The device frequency can be divided by skipping register steps and drive some photons out of the routing tree.

By trade-off on stability or multi-photon emission rate, the pumping period can be changed and lowered by several \(T\), the frequency multiplication is thus lower.

3.4.2 Stability enhancement

Multiplying frequency needs a constant number of photons per pump pulse. Probabilistically, it needs in average much more photons than the frequency multiple. It is achievable by increasing again the downconverter number or pump power, but will lead to multi-photon emissions and large waste of photons.

Keeping the source frequency below the maximum frequency multiple make possible a temporary photon storage of the excess photons into the longest delay lines. Photons can be delayed up to the next pump cycle and so will be emitted in the first place in this new pumping period. A little photon excess can be used during the next pulse, and a small lack can be corrected by the storage from the previous pulse (Fig. 9). This 1-cycle ahead memory allows to reduce the SPDC array average rate almost down to the frequency conversion multiple.

![Figure 9: Photon source frequency 6 times higher than pump rate. 1 or 2 photon excess (red) is stored and used at the beginning of the next cycle before the newly produced photons.](image)

With the 0-\(7T\) register example and by lowering the frequency multiplication to 6, two photons can be stored for the next pulse cycle. 1 or 2-photon excess can be used during the next pulse, and 1 or 2-photon lack can be corrected by the storage from the previous pulse (Fig. 9). In these conditions, probability of lack of photon at the output drops significantly, since it only occurs when several successive low photon numbers are issued from the downconverter array.
The size of the downconverter array will be a factor of stability in addition to increase the total photon rate. Stability can once more be improved easily by adding a feedback to increase the pumping power for the next cycle to refill the temporary photon storage.

### 3.4.3 Switching decisions

The best strategy to operate the suggested device and avoid CBDR limitation problems or photon bunching problems is to adopt a fast-to-slow top-to-down driving approach. It consists in allocating fastest photons (low delays) to slowest photons (high delays) from the top to the bottom of the CBDR structure.

In this operating mode, we reduce the need of inaccessible paths due to CBDR limitations and avoid any bunching of photons. Photons may share the same path, but at different times (Fig. 6).

With this approach, during a pumping cycle, each switch of the CBDR structure and the routing tree needs to be permuted at most once and all in the same direction (figure out the permutations in the CBDR and in the routing tree switches needed to drive the photon train out on Fig. 6). The use of photon storage for stability enhancement slightly changes this property by delaying some permutations to the next pump cycle.

Considering the photon loss into the delay lines on this approach, we could also consider different pump powers for the SPDC modules, knowing that down module photons will have a higher probability to be sent to long delay lines, thus higher loss.

### 3.5 Advantages to prior art

- Frequency up-conversion of the laser pumping rate to the photon source output.
- Tolerate low detector speed.
- High stability of the output photon rate.
- Possibility of feedback on the next cycle due to the efficient photon storage.
- High controllability at fixed source frequency (pump power, pump frequency, power or frequency feedback on next pump pulse).
- High control of the trade-off between frequency rise/multi-photon rate/output stability.
- Few waste of photon.
- Efficient use of multiplexing and customizable structure (SPDC number and CBDR level).
- Easy up-to-down switching programming.
Chapter 4

Detailed analysis of the SPDC based single-photon source with output rate up-conversion multiplexed architecture

4.1 Case analysis of emission probability

The following table shows various configurations of SPDC based single-photon source adapted with different error rates.

![Table showing emission probabilities and error rates for different configurations.](image)

Figure 10: Optimization of minimum photon emission probabilities and total error rate in function of number of sources, frequency multiple, mean photon number per module. First row of 19 sources tables with 18 sources considered for border limitation. Method: case analysis.

4.2 Simulation

A simulation tool has been realized with Maple. It assumes negligible photon loss inside the structure, considering a perfect waveguide and switching network. The following graphs show the absolute rate of lack error and multi-photon error of different configurations and parametrs of SPDC based single-photon source.
Each point has been simulated on 100,000 working cycles (on which multiplication factor for frequency must be applied to obtain the total photon number in ideal case) using the standard random tool of Maple. The simulator is also able to manage different power feed back responses (boost and turbo-boost modes).

4.2.1 Working parameter variation

The following Fig. 11 and 12 display the working characteristics of a large structure of 100 SPDC modules used without boosting with variation of frequency multiplication factor and pump power.

![Graph](image)

Figure 11: Error rates of a 100 SPDC structure with frequency multiple of 4 in function of the pump power (or N).

The results of the pump power variation for large structure as 100 SPDC modules show very low error rates and good possibilities of error trade-off. It gives an excellent device with high output gain.

The optimized point, with equivalence of lack and multi-photon error rates, is obtained at $N \approx 0.05$. The source quality is then around 95 % with 2.4 % multi-photons and 2.4 % lacks. No equivalent theoretical prior art SPDC source could achieve this quality at this rate.
We note that it is very easy to reduce the lack by changing the output multiple rate of the device. In the case of a variable pump frequency as feedback, lack could be drastically reduced while keeping an equivalent multi-photon error rate.

The multi-photon rate depends linearly on the pump power. We note that on the figures, particularly on Fig. 12, the pump power is fixed but the multi-photon error rate is not constant in the region of large lack. It is due to the absolute and homogeneous units used in this report, contrary to the relative multi-photon within emitted photon unit used in most of papers.

Figure 13: Error rates of 9 and 11 SPDC structures at multiple of 3 (right) and 4 (left) in function of the pump power.
The Fig. 13 shows several working configurations of very small structure (9 and 11 SPDC modules) with optimized points for output gain of 3 and 4. For these small structures, I preferred to keep working at high output gain that lowering the error rates as it is a strong advantage of this device on the alternative solutions.

4.2.2 Structure size

In Fig. 14, we analyze the variation error rates in function of the number of SPDC module of the structure.

![Figure 14: Lack error rate and relative multi-photon error rate of SPDC structure depending on size for three pump powers (green: N=0.025, red: N=0.05, blue: N=0.10), with frequency multiple of 4.](image)

4.2.3 Feed-back

The use of a pump frequency feed-back in case of photon lack will necessarily prevent almost all photon lack, but will also need a faster use of heralding detectors. This nearly on-demand laser pulsing configuration has not been simulated.

Simulations involving power-feed back have been realized with one and two boosting power associated to different low photon storage thresholds. These simulations have proved a overall error rate drop of 15 % of the source at the optimized point compared to the standard approach in some cases.

Other feed-back strategies have been proposed but not simulated, as a fully variable power pump for each storage level, or a continuous boosting easier to implement, or a totally controlled system controlling its quality trade-offs in function of the use.
4.3 Conclusion of the analysis

The results obtained by simulation confirm the excellent possibilities of the device. They motivate us to develop it and to keep working on more advanced simulators in order to consider photon losses in network, to consider alternative structures, to manage different routing strategies and to allow different pump power shared on the architecture (used in the fast-to-slow top-to-down with delay loss). We will also keep discussing the multi-photon problem.
Conclusion

This internship has given benefits to both the trainee and the trainer. I have designed a new device for Quantum Technology that can use all the potential of different technologies at their current level and in their future ameliorations. It is a success, and this device is currently under patenting, and will led to a longer partnership into publishing with my internship institution and experiments with overseas companies.

This internship was my first experience in Quantum Information Theory. It was a good experience and it allowed me to discover this unfamiliar field and to get a global point of view about it. Thanks to this internship, I improved my research and engineering skills such as methodology, organization, strategy and communication. It also enabled me to meet people coming from different places, having different backgrounds, and working on different projects.

I could then express my ideas and build my own research. With this internship, I can also confirm my objective to pursue my studies in a PhD.
Bibliography