

# Strategic Energy Planning under Uncertainty: a Mixed-Integer Linear Programming Modeling Framework for Large-Scale Energy Systems

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# Outline

- **Introduction**
  - The energy transition
  - Energy forecasting: learning from the past
  - Gaps & Objective
- **MILP model**
  - Main features
  - Model structure: sets and constraints
- **Results**
  - Application to the Swiss energy system
  - Robust Optimization
- **Conclusions**

# Introduction

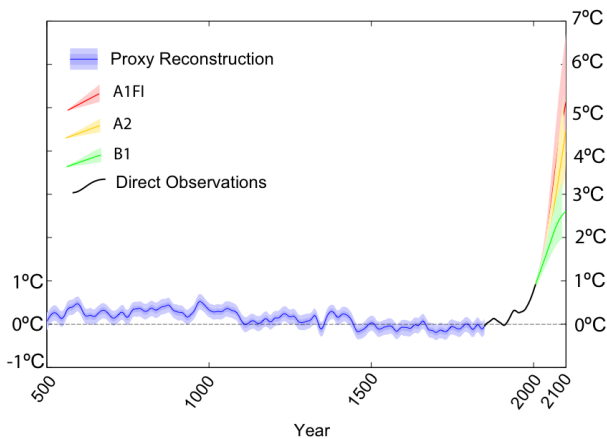
# Introduction

## The energy transition

Sources:

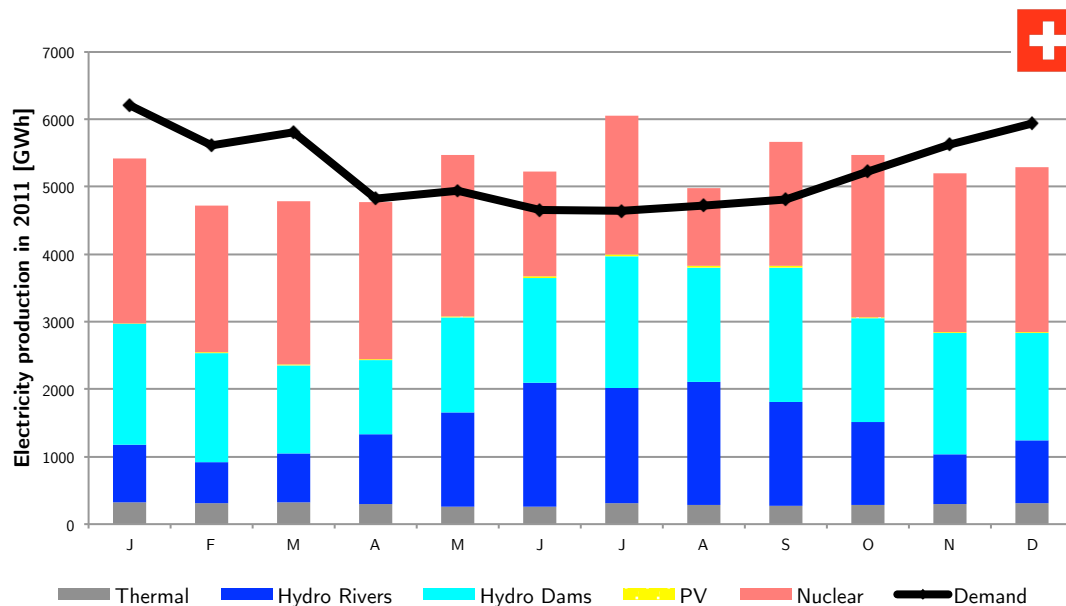
- [1] Allison et al., The Copenhagen Diagnosis, 2009 (p. 50)
- [2] IPCC 2013 report, Climate change 2013 - The physical science basis
- [3] IEA, Energy Technology Perspectives 2014
- [4] Swiss Federal Office of Energy, Swiss electricity statistics, 2011

Global Temperature Relative to 1800-1900 (°C)



IPCC 2013: climate has changed due to human activities [2]

To target the 2°C  $\Delta T$  limit CO<sub>2</sub> emissions need to be halved by 2050 [3]



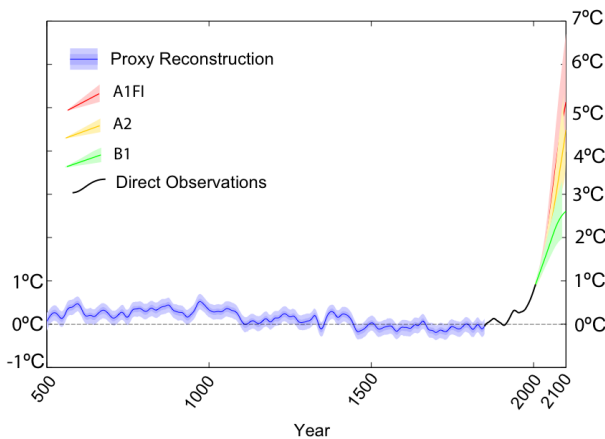
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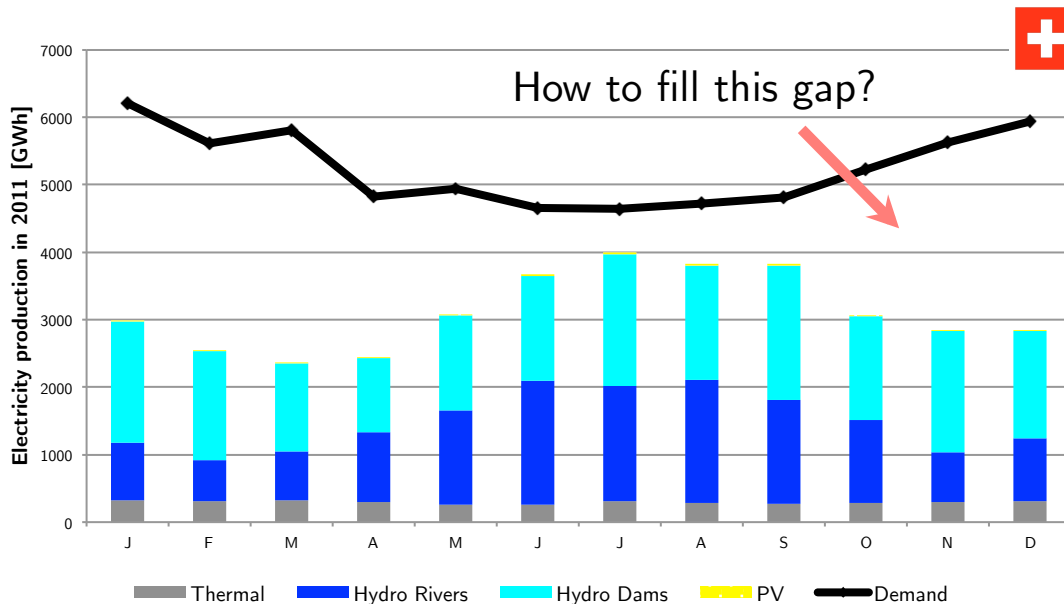
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### Strategic Energy Planning

Large scale: urban/national  
Time horizon: 20-50 years



### Common approach:

Long term deterministic evolution models based on forecasts

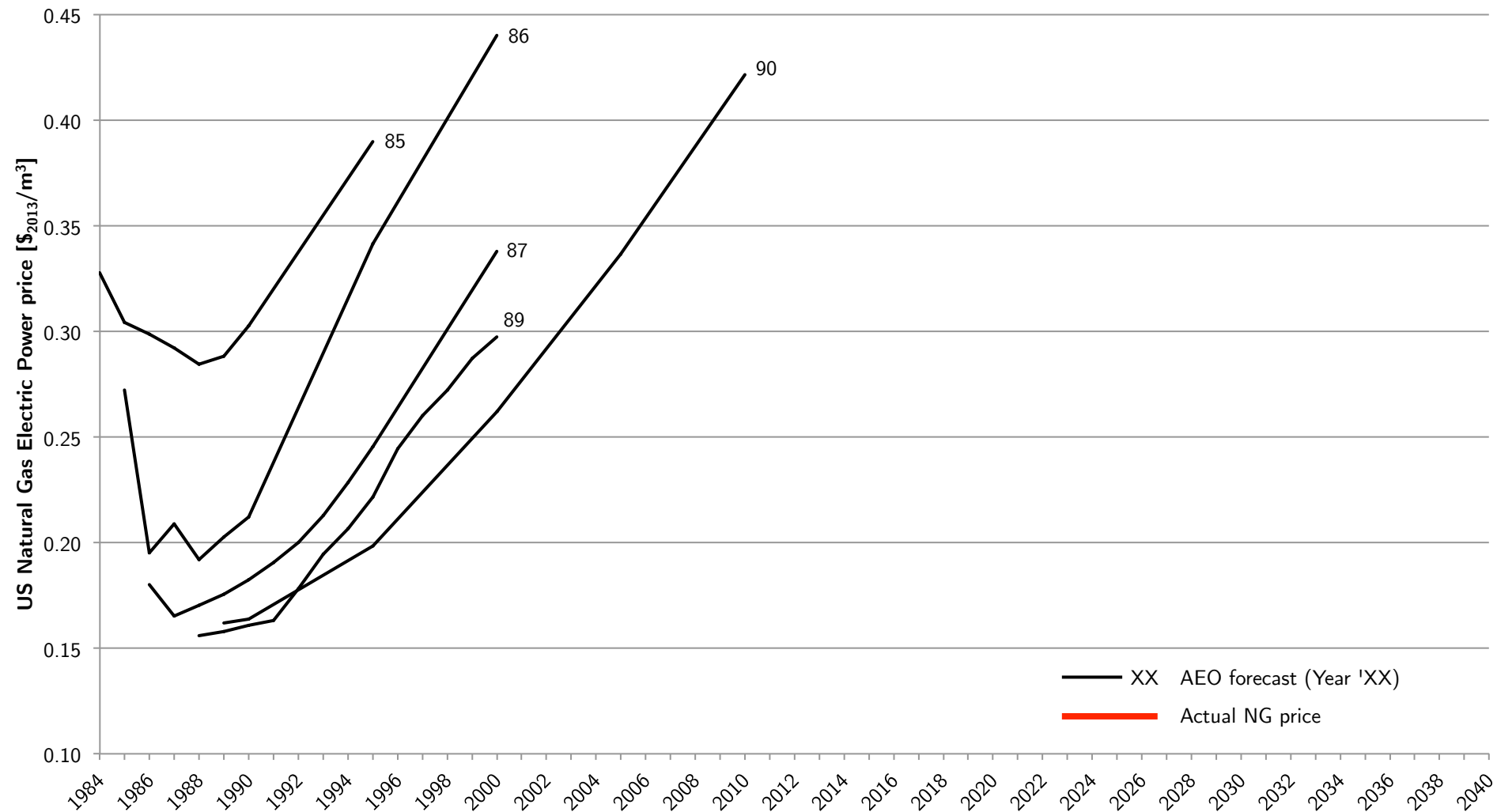
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## Energy forecasting: learning from the past

Sources:

- [1] U.S. EIA - Energy Information Administration.
- [2] R. Wiser and M. Bolinger. An Overview of Alternative Fossil Price and Carbon Regulation Scenarios. 2004

**Historical U.S. AEO Natural Gas for Electricity Production Price Forecast vs Actual Price**



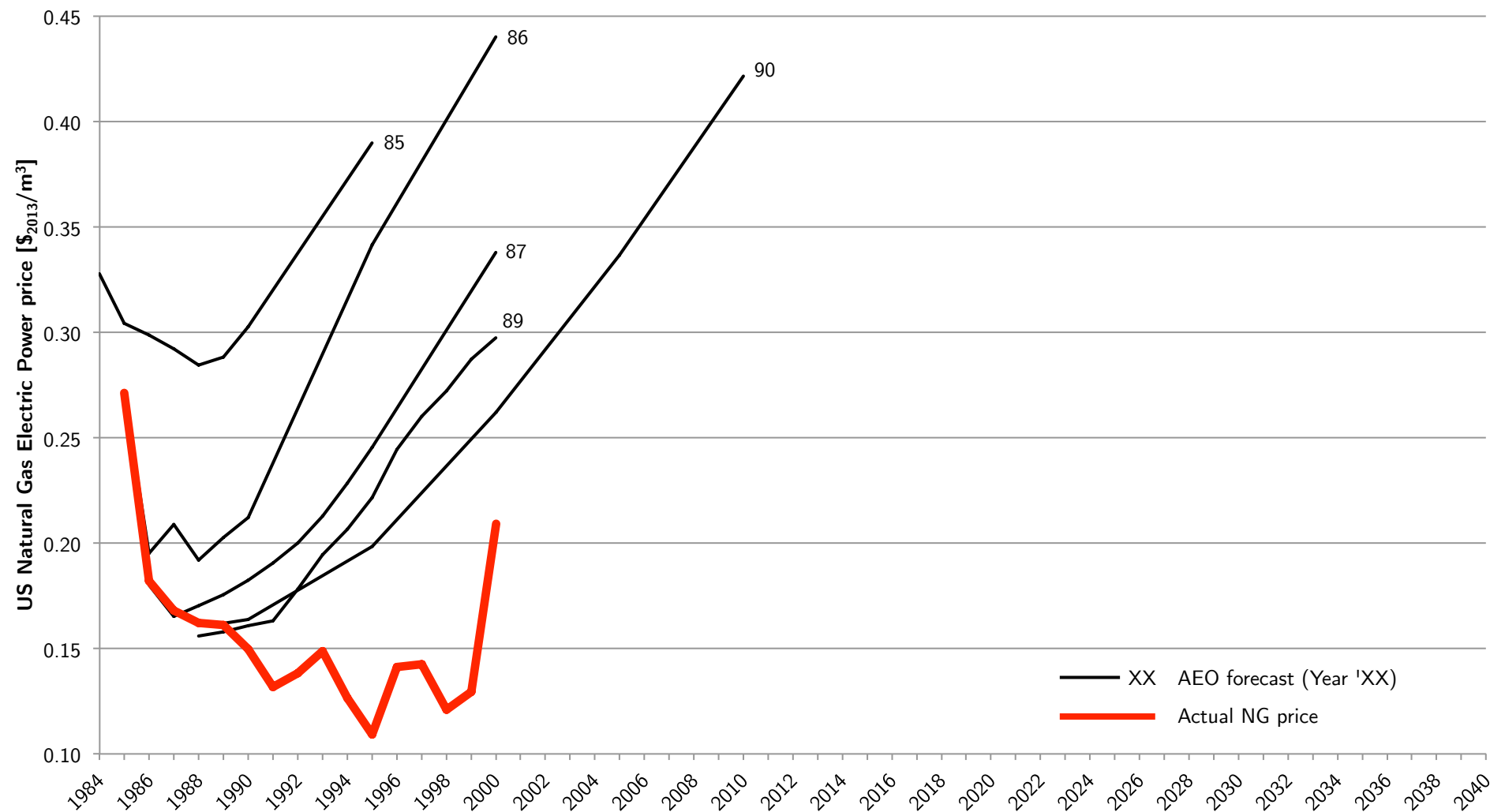
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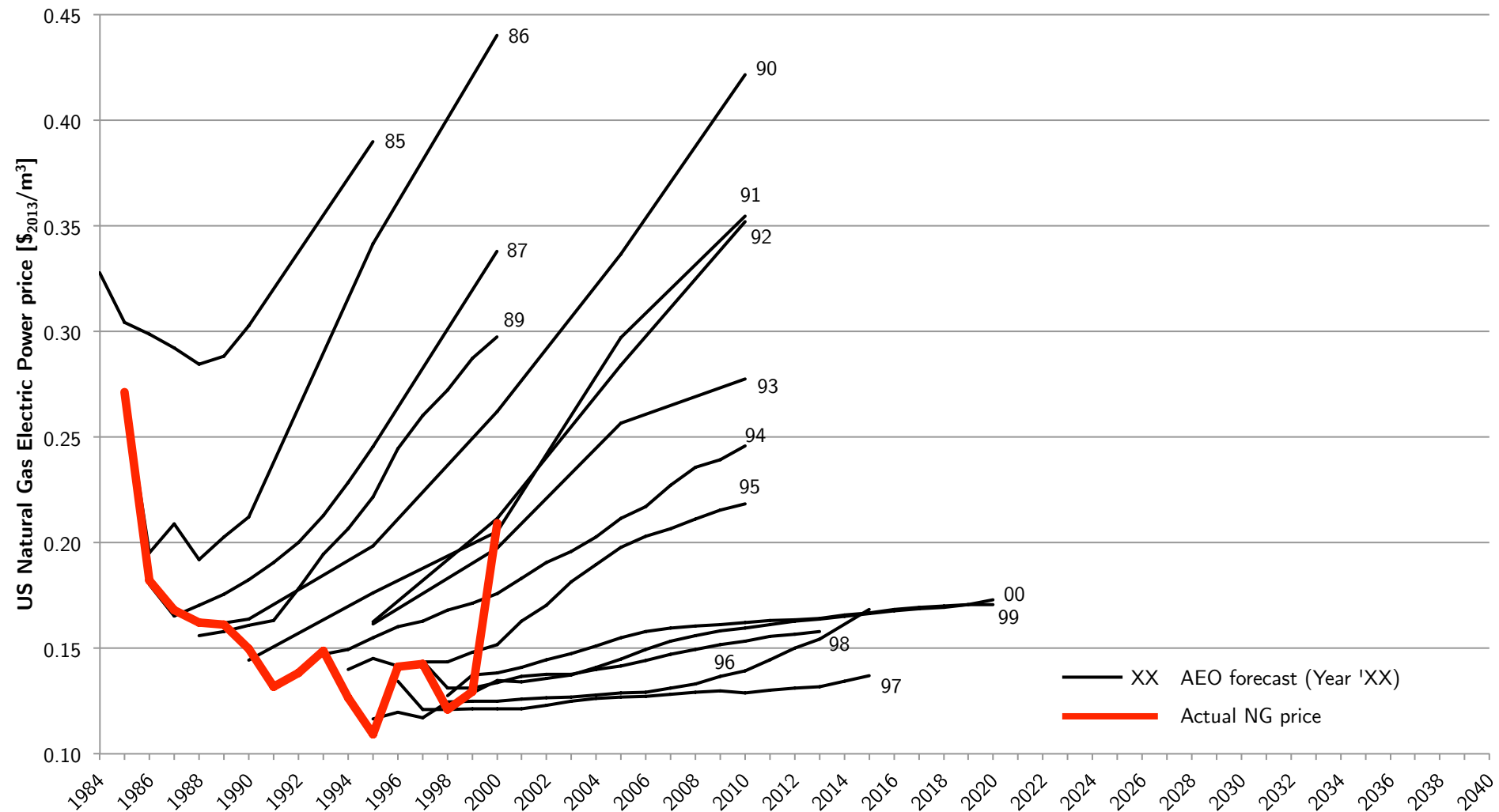
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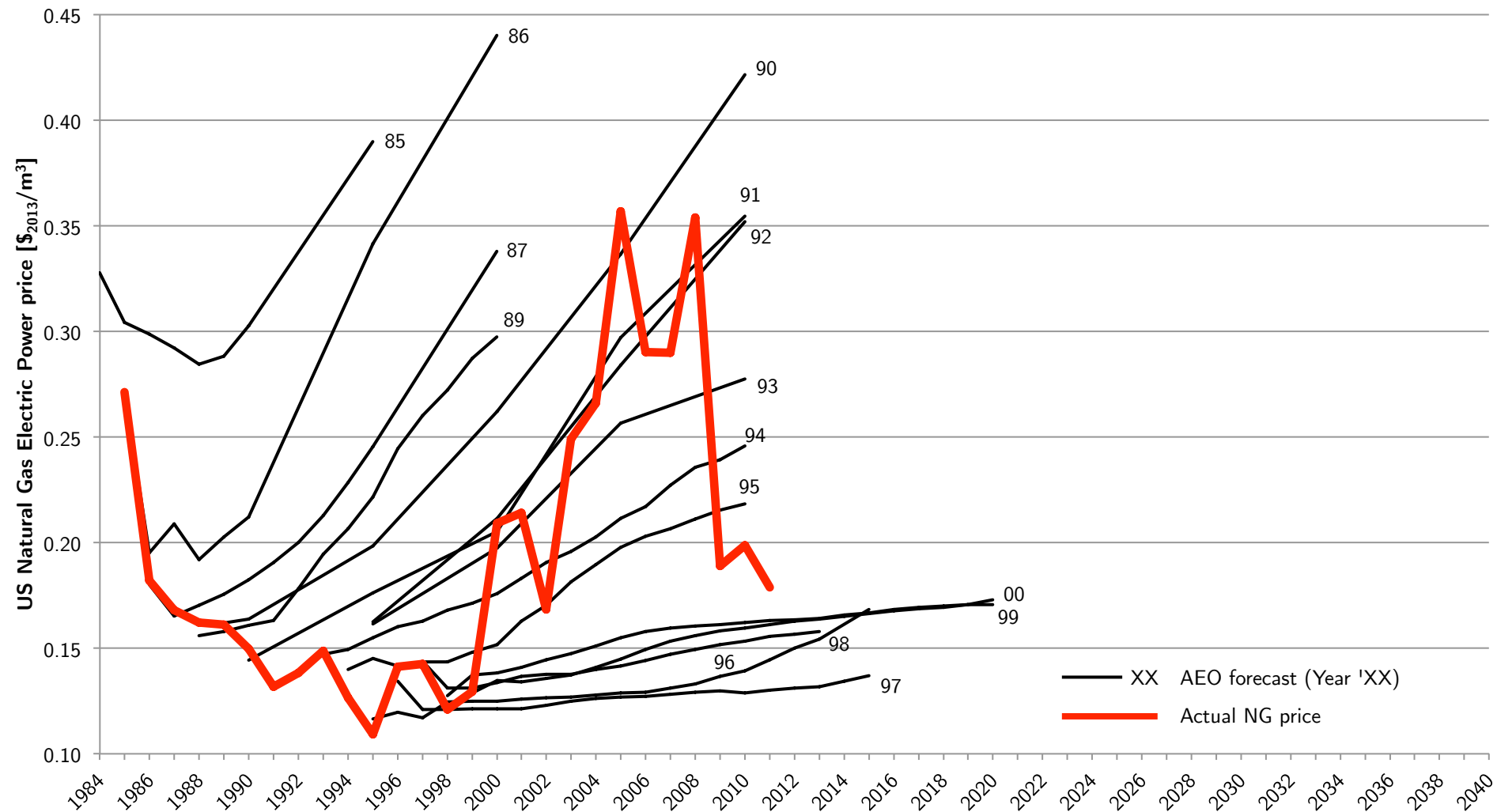
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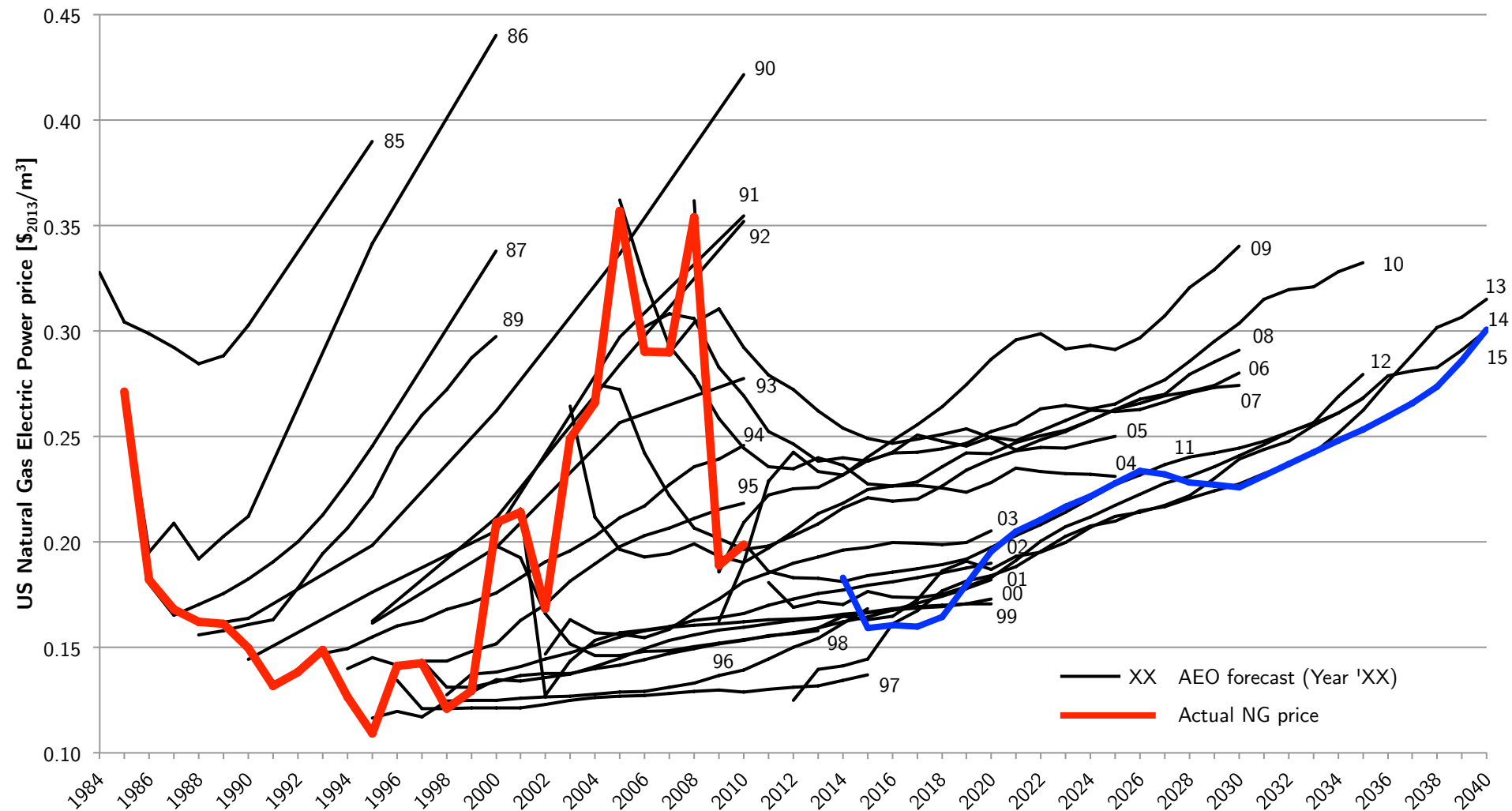
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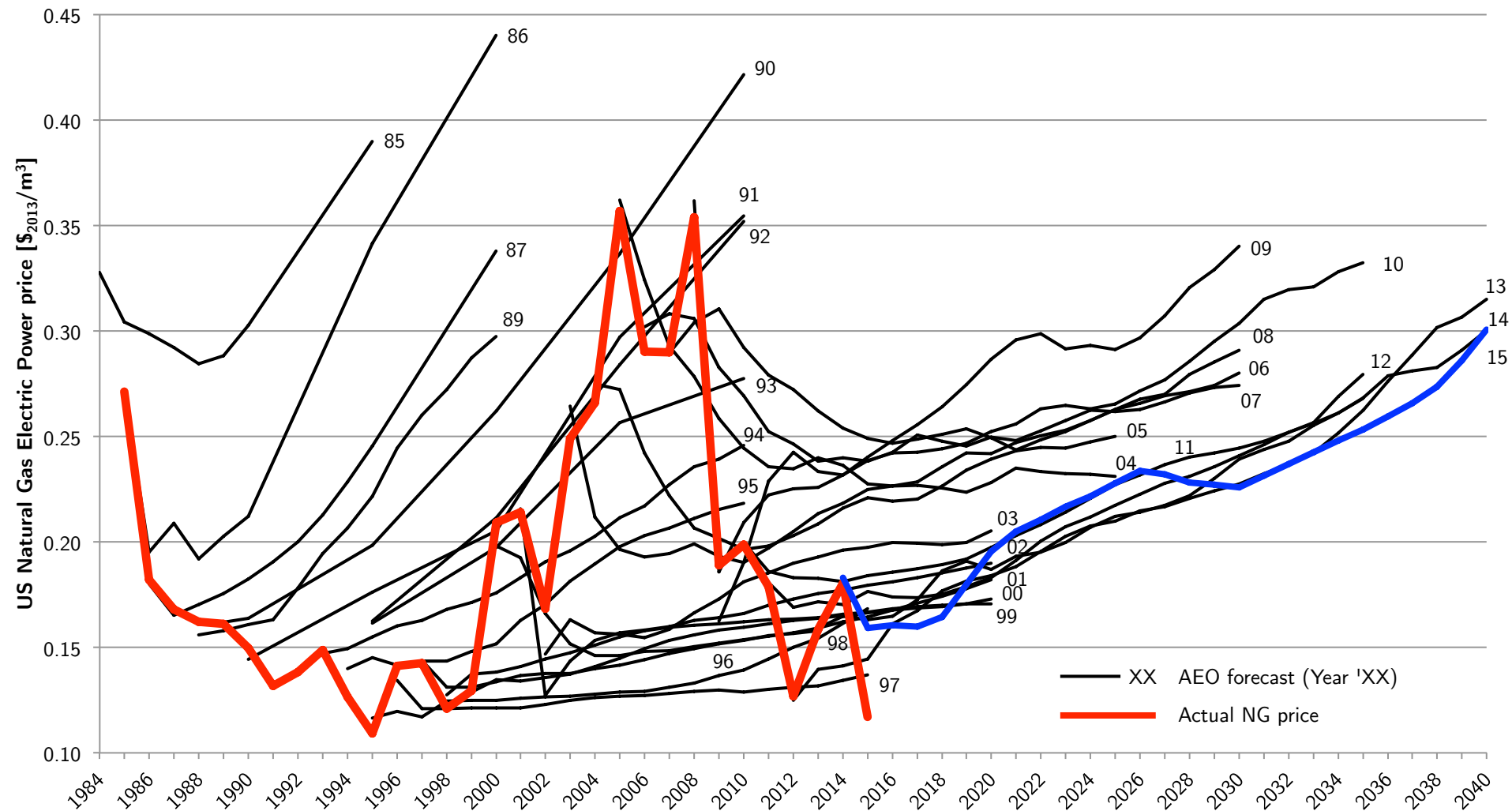
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- [2] R. Wiser and M. Bolinger. An Overview of Alternative Fossil Price and Carbon Regulation Scenarios. 2004

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# Introduction

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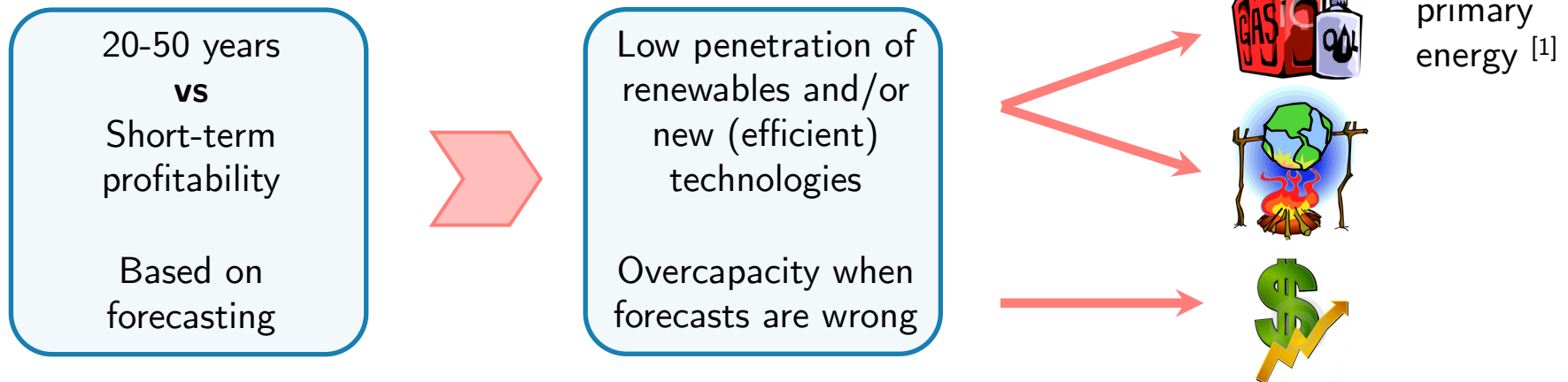
Sources:

[1] IEA, Key world energy statistics, 2014

[2] James S. Hodges and James A. Dewar. Is it you or your model talking? a framework for model validation. 1992

[3] J. Koomey et al. Improving long-range energy modeling: A plea for historical retrospectives. 2003.

Long-term, strategic planning for urban and national energy systems



Furthermore:

- energy models are “**non-validatable**”, i.e. doomed to inaccuracy [2]
- backcasting: models have missed pivotal events [3]

Need of accounting for **uncertainty** in long-term energy modeling

# Introduction

## Gaps & Objective

Sources:

- [1] Grossmann et al., Recent Advances in Mathematical Programming Techniques for the Optimization of Process Systems under Uncertainty. ESCAPE 25, 2015.
- [2] Marnay and Siddiqui, Addressing an Uncertain Future Using Scenario Analysis. 2006
- [3] Rager et al., Integrating Uncertainty into Urban Energy System Design. ESCAPE 26, 2016.

Still low penetration of uncertainty in the energy field:

- Grossmann et al.<sup>[1]</sup>: **model complexity** and **computational time** are key barriers
- Marnay & Siddiqui<sup>[2]</sup>: computational time of NEMS → scenario analysis
- Rager et al.<sup>[3]</sup>: **concise** models needed for robust optimization

Also, most energy models available today are **sector-specific** (usually electricity) and are based on **evolution** of the energy system with a **market-based** approach.



Concise MILP modeling framework for large-scale energy systems for strategic energy planning under uncertainty

# MILP model

# MILP model

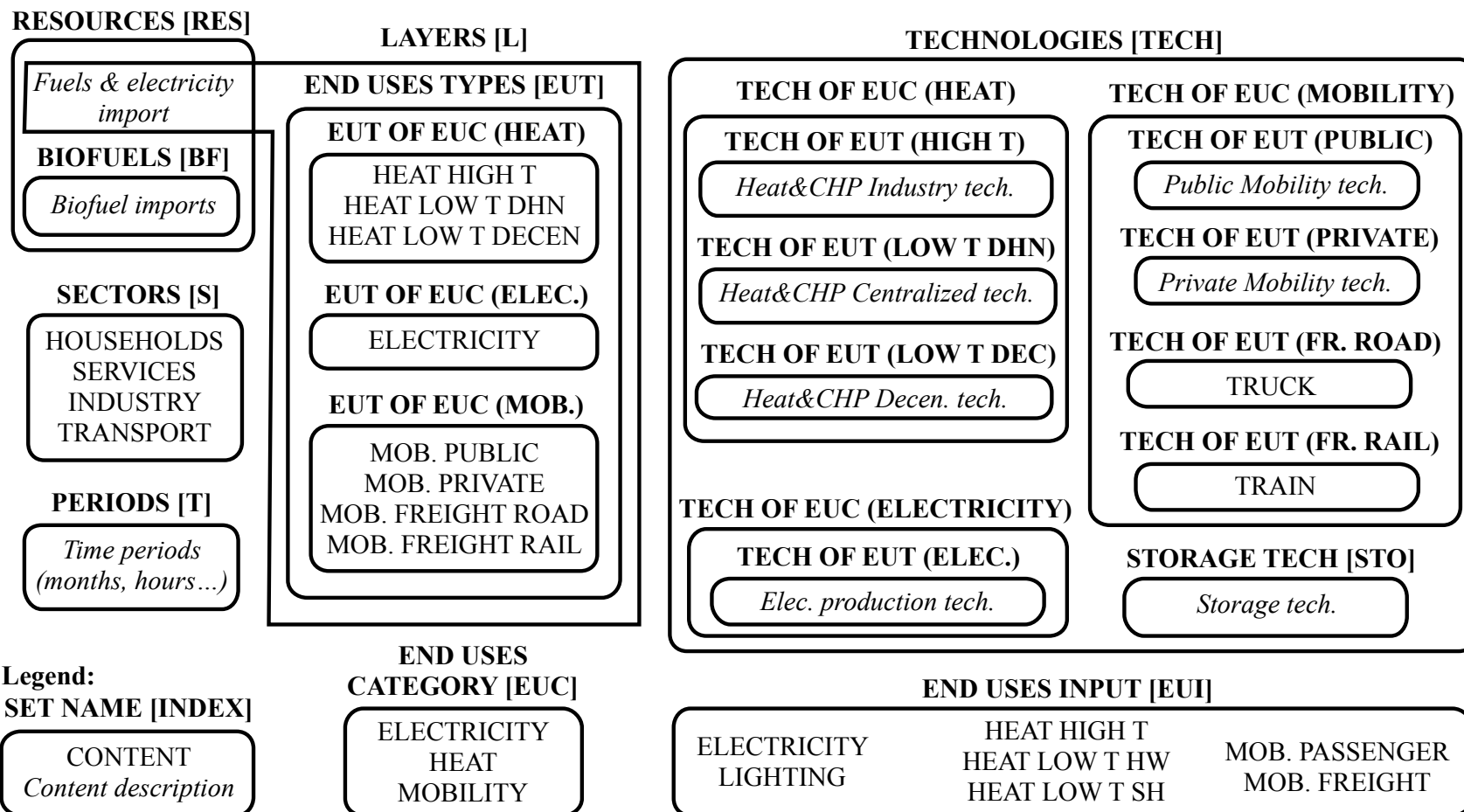
## Main features

Main features of the developed MILP framework:

- Energy based model
- “Snapshot” model: optimization of the energy system in a future target year
- Simplified yet complete energy system: inclusion of heating and mobility
- Multiperiod formulation: seasonality of demand and energy storage
- Concise structure
- Low number of integer variables
- Life Cycle Assessment: Global Warming Potential (CO<sub>2</sub>-eq. emissions)

# MILP model

## Model structure: sets



### Legend:

#### SET NAME [INDEX]

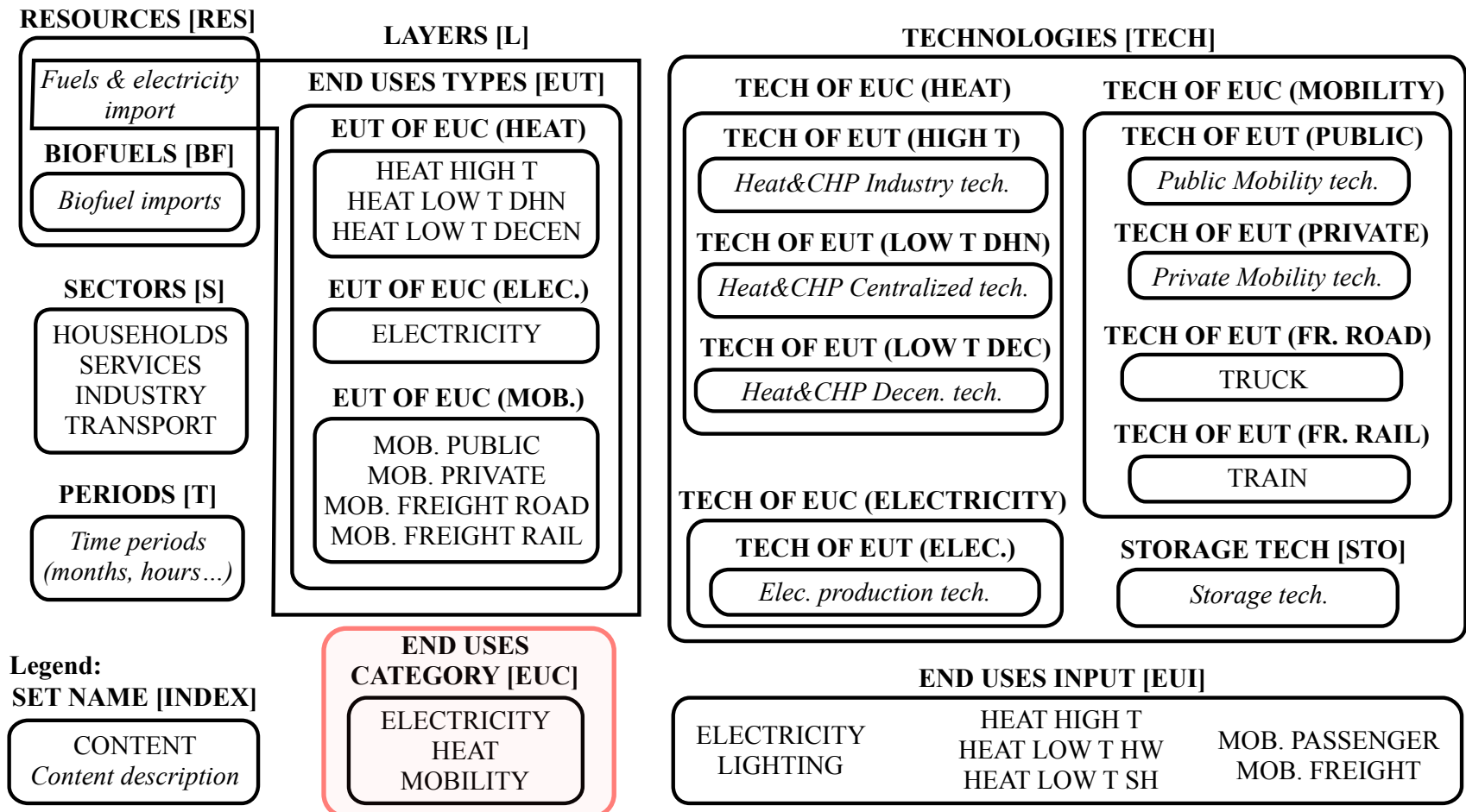
CONTENT  
Content description



# MILP model

## Model structure: sets

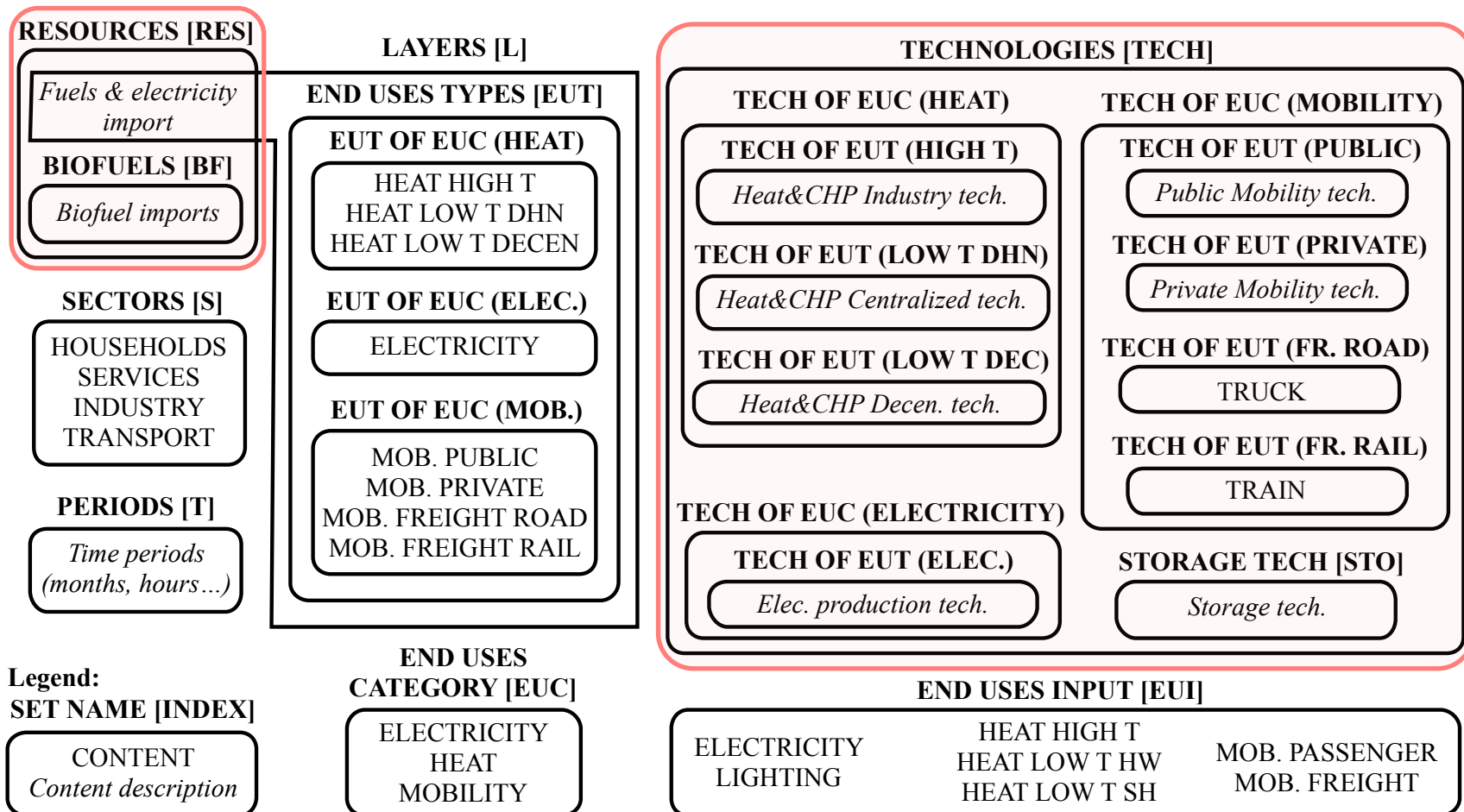
End-uses demand: sector-based → heating + electricity + mobility



# MILP model

## Model structure: sets

Distinction between **resources** (including biofuels) and **technologies**



# MILP model

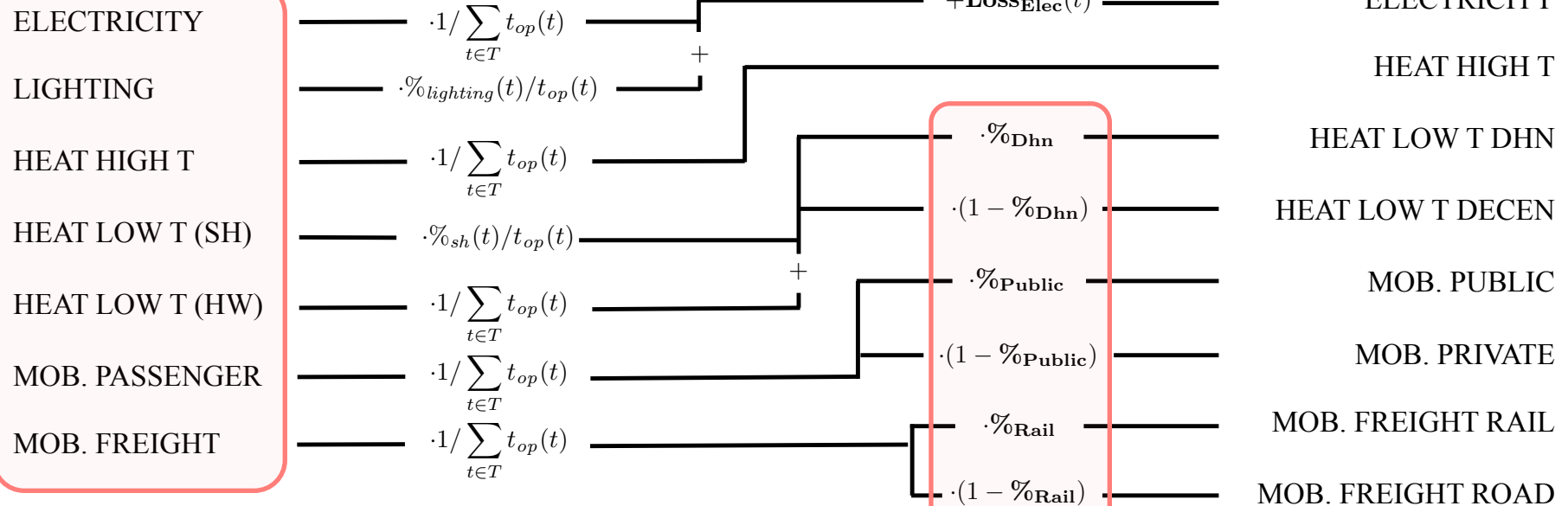
Sources:

[1] Codina Gironès et al., Strategic energy planning for large-scale energy systems: A modelling framework to aid decision-making. 2015

## Model structure: constraints

- Input to the model: **end-uses** for the target year from demand-side model<sup>[1]</sup>
- Decision variables: level of centralization for heating, penetration of public mobility and of rail transport in freight

$$\text{EndUsesInput}(eui) = \sum_{s \in S} \text{endUses}_{year}(eui, s) \quad \forall eui$$



# MILP model

## Model structure: constraints

Objective: supplying this end-use demand at the lowest total annual **cost**

$$\min \sum_{j \in TECH} (\tau(j) \mathbf{C}_{inv}(j) + \mathbf{C}_{maint}(j)) + \sum_{i \in RES} \mathbf{C}_{op}(i) \quad (1)$$

# MILP model

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Distinction between **technologies** and **resources**

$$\text{s.t. } \tau(j) = \frac{i_{\text{rate}}(i_{\text{rate}} + 1)^{n(j)}}{(i_{\text{rate}} + 1)^{n(j)} - 1} \quad \forall j \in \text{TECH} \quad (2)$$

$$\mathbf{C}_{\text{inv}}(j) = c_{\text{inv}}(j) * \mathbf{Mult}(j) \quad \forall j \in \text{TECH} \quad (3)$$

$$\mathbf{C}_{\text{maint}}(j) = c_{\text{maint}}(j) * \mathbf{Mult}(j) \quad \forall j \in \text{TECH} \quad (4)$$

$$f_{\text{min}}(j) \leq \mathbf{Mult}(j) \leq f_{\text{max}}(j) \quad \forall j \in \text{TECH} \quad (5)$$

$$\mathbf{N}(j) \text{mult}_{\text{ref}}(j) = \mathbf{Mult}(j) \quad \forall j \in \text{TECH} \quad (6)$$

$$\mathbf{C}_{\text{op}}(i) = \sum_{t \in T} c_{\text{op}}(i, t) \mathbf{Mult}_t(i, t) t_{\text{op}}(t) \quad \forall i \in \text{RES} \quad (9)$$

$$\sum_{t \in T} \mathbf{Mult}_t(i, t) t_{\text{op}}(t) \leq \text{avail}(i) \quad \forall i \in \text{RES} \quad (10)$$

# MILP model

## Model structure: constraints

This allows an easy integration of **Global Warming Potential** in the model: extraction, transportation and combustion emissions attributed to resources, construction, O&M and end-of-life emissions to technologies

Distinction between **technologies** and **resources**

$$\text{s.t. } \tau(j) = \frac{i_{rate}(i_{rate} + 1)^{n(j)}}{(i_{rate} + 1)^{n(j)} - 1} \quad \forall j \in TECH \quad (2)$$

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# MILP model

## Model structure: constraints

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Capacity factor:

- $c_{p,t}$  depending on resource availability (e.g. renewables)
- yearly capacity factor  $c_p$  accounting for technology downtime and maintenance

$$\mathbf{Mult}_t(j,t) \leq \mathbf{Mult}(j)c_{p,t}(j,t) \quad \forall j \in \mathit{TECH}, \forall t \in T \quad (7)$$

$$\sum_{t \in T} \mathbf{Mult}_t(j,t)t_{op}(t) \leq \mathbf{Mult}(j)c_p(j) \sum_{t \in T} t_{op}(t) \quad \forall j \in \mathit{TECH} \quad (8)$$

# MILP model

## Model structure: constraints

**Layers:** power balance in each time period

$$\sum_{i \in RES \cup TECH \setminus STO} f(i, l) \mathbf{Mult}_t(i, t) + \sum_{j \in STO} (\mathbf{Sto}_{out}(j, l, t) - \mathbf{Sto}_{in}(j, l, t)) - \mathbf{EndUses}(l, t) = 0 \quad \forall l \in L, \forall t \in T \quad (11)$$

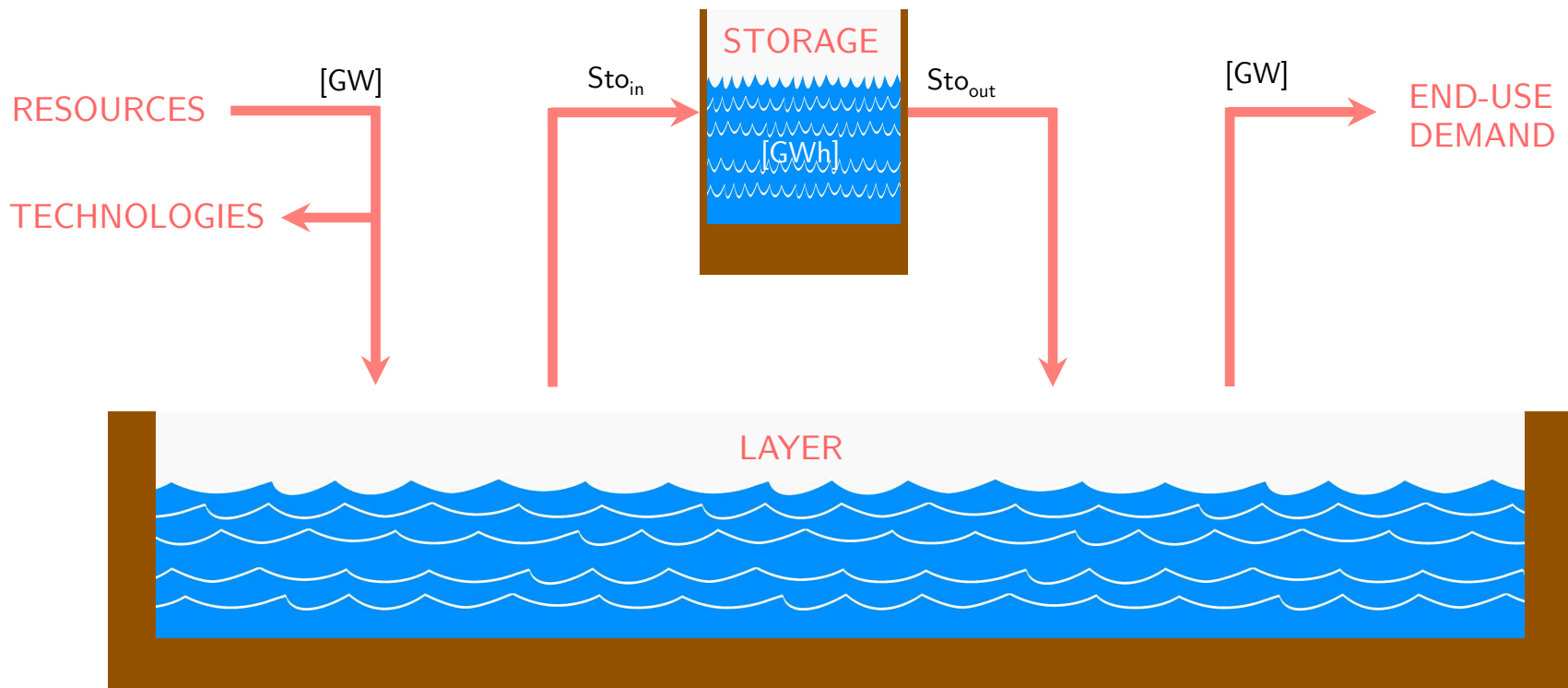


# MILP model

## Model structure: constraints

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$$\sum_{i \in \text{RES} \cup \text{TECH} \setminus \text{STO}} f(i, l) \mathbf{Mult}_t(i, t) + \sum_{j \in \text{STO}} (\mathbf{Sto}_{\text{out}}(j, l, t) - \mathbf{Sto}_{\text{in}}(j, l, t)) - \mathbf{EndUses}(l, t) = 0 \quad \forall l \in L, \forall t \in T \quad (11)$$



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LAYERS

		RESOURCES/BIOFUELS			END USES TYPES		
		ELEC	NG	...	HEAT	DHN	...
RESOURCES	ELEC	1	0				
	NG	0	1				
	SNG	0	1				
	...						
TECH/STO	HP	-0.25	0		1		
	CHP	1.25	-2.5		1		
	...						

Unitary output in main end-use type  $\rightarrow$  **Mult** corresponds to installed size of technology [GW]

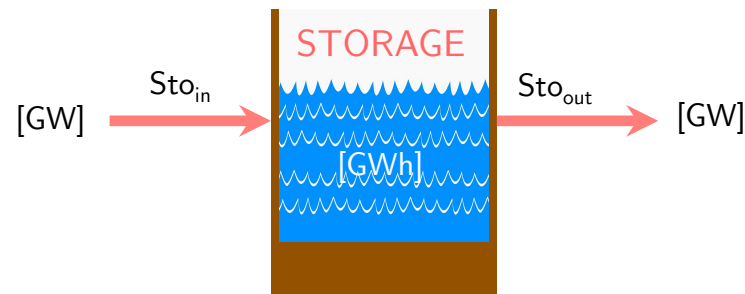
# MILP model

## Model structure: constraints

$$\mathbf{Mult}_t(j, t) = \mathbf{Mult}_t(j, t - 1) + t_{op}(t) \cdot$$

$$\left( \sum_{l \in L | \varepsilon_{sto, in}(j, l) > 0} \mathbf{Sto}_{in}(j, l, t) \varepsilon_{sto, in}(j, l) - \sum_{l \in L | \varepsilon_{sto, out}(j, l) > 0} \mathbf{Sto}_{out}(j, l, t) / \varepsilon_{sto, out}(j, l) \right) \quad \forall j \in STO, \forall t \in T \quad (12)$$

$\mathbf{Mult}_t$  storage level [GWh]  
 $\mathbf{Mult}$  max. level (inv. cost)



$$\mathbf{Sto}_{in}(j, l, t) (\lceil \varepsilon_{sto, in}(j, l) \rceil - 1) = 0 \quad \forall j \in STO, \forall l \in L, \forall t \in T \quad (13)$$

$$\mathbf{Sto}_{out}(j, l, t) (\lceil \varepsilon_{sto, out}(j, l) \rceil - 1) = 0 \quad \forall j \in STO, \forall l \in L, \forall t \in T \quad (14)$$

$$\left\lceil \sum_{l \in L | \varepsilon_{sto, in}(j, l) > 0} \mathbf{Sto}_{in}(j, l, t) \varepsilon_{sto, in}(j, l) \frac{t_{op}(t)}{f_{max}(j)} \right\rceil + \left\lceil \sum_{l \in L | \varepsilon_{sto, out}(j, l) > 0} \mathbf{Sto}_{out}(j, l, t) / \varepsilon_{sto, out}(j, l) \frac{t_{op}(t)}{f_{max}(j)} \right\rceil \leq 1 \quad \forall j \in STO, \forall t \in T \quad (15)$$

# Results

# Results

Sources:

- [1] Moret et al., Swiss-EnergyScope.ch: a Platform to Widely Spread Energy Literacy and Aid Decision-Making. 2014
- [2] Codina Gironès et al., Strategic energy planning for large-scale energy systems: A modelling framework to aid decision-making. 2015

## Application to the Swiss energy system



Excel<sup>[2]</sup> → MILP

COMPARE SITUATION

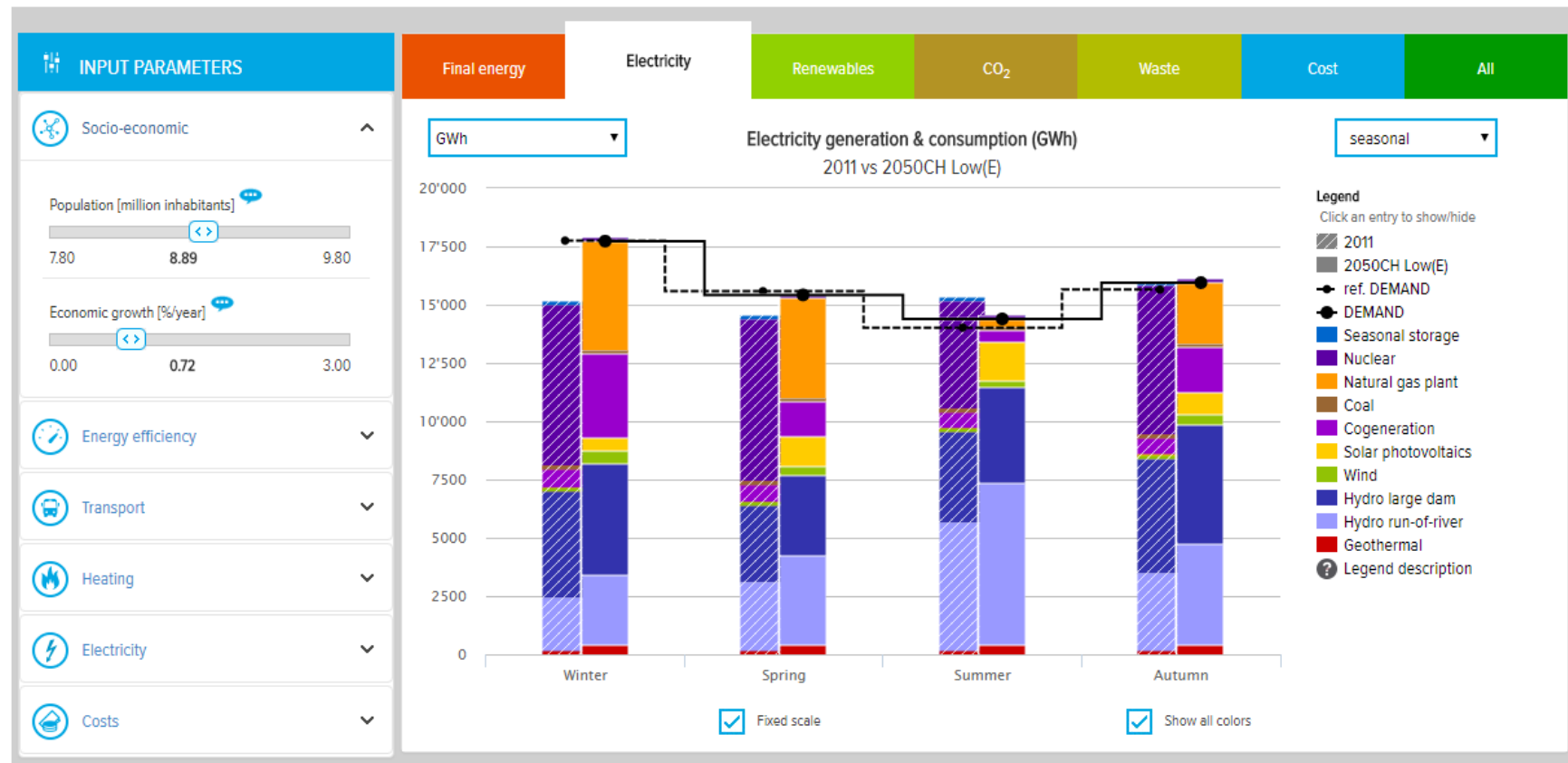
2011

TO

2050CH Low(E)

HIDE PARAMETERS

More



# Results

Sources:

[1] Soyster. Convex programming with set-inclusive constraints and applications to inexact linear programming. 1974

[2] Bertsimas &amp; Sim. The price of robustness. 2004.

## Robust optimization: methodology

Soyster<sup>[1]</sup>: Protection against all uncertain parameters at worst case. Very conservative  
 Bertsimas & Sim<sup>[2]</sup>: reduction of the “price of robustness” through probabilistic approach

$$\text{minimize } \mathbf{c}^T \mathbf{x}$$

The vector  $\mathbf{c}$  (cost coefficients) has some uncertain elements belonging to the set  $\mathbf{J}$ .  
 The  $j$ -th uncertain parameter can vary of a maximum value  $d_j$

$$c_j = [c_j, c_j + d_j] \quad j \in J$$

The “protection parameter” controls the number of uncertain parameters at worst case:

$$\Gamma_0 = [0, |J|] \begin{cases} \rightarrow \Gamma_0 = 0 & \text{Deterministic MILP, no parameter at worst case} \\ \rightarrow \Gamma_0 = |J| & \text{All parameter at worst case (Soyster)} \end{cases}$$

Application of the methodology to  $c_{op}$  (+40 %) and  $c_{inv}$  (+20 %)  $\rightarrow$  178 params

# Results

Sources:

[1] Moret et al., Robust optimization for strategic energy planning, 2014

[2] Bertsimas &amp; Sim. The price of robustness. 2004.

## Robust optimization: methodology

### New Parameters

$\Gamma_0$ : protection parameter

$d_{op}(i) \forall i \in RES$ : variation from the nominal value of the operating cost

$d_{inv}(j) \forall j \in TECH$ : variation from the nominal value of the investment cost

### New Variables

$\mathbf{z}_0, \mathbf{p}_{0,op}(i, t), \mathbf{y}_{op}(i, t), \mathbf{p}_{0,inv}(j), \mathbf{y}_{inv}(j) \forall i \in RES, \forall j \in TECH/STO, \forall t \in T$

### New Constraints

$\mathbf{z}_0 + \mathbf{p}_{0,op}(i, t) \geq d_{op}(i, t)\mathbf{y}_{op}(i, t) \quad \forall i \in RES, \forall t \in T$

$\mathbf{z}_0 + \mathbf{p}_{0,inv}(j) \geq d_{inv}(j)\mathbf{y}_{inv}(j) \quad \forall j \in TECH/STO$

$-\mathbf{y}_{op}(i, t) \leq \mathbf{Mult}_t(i, t)t_{op} \leq \mathbf{y}_{op}(i, t) \quad \forall i \in RES, \forall t \in T$

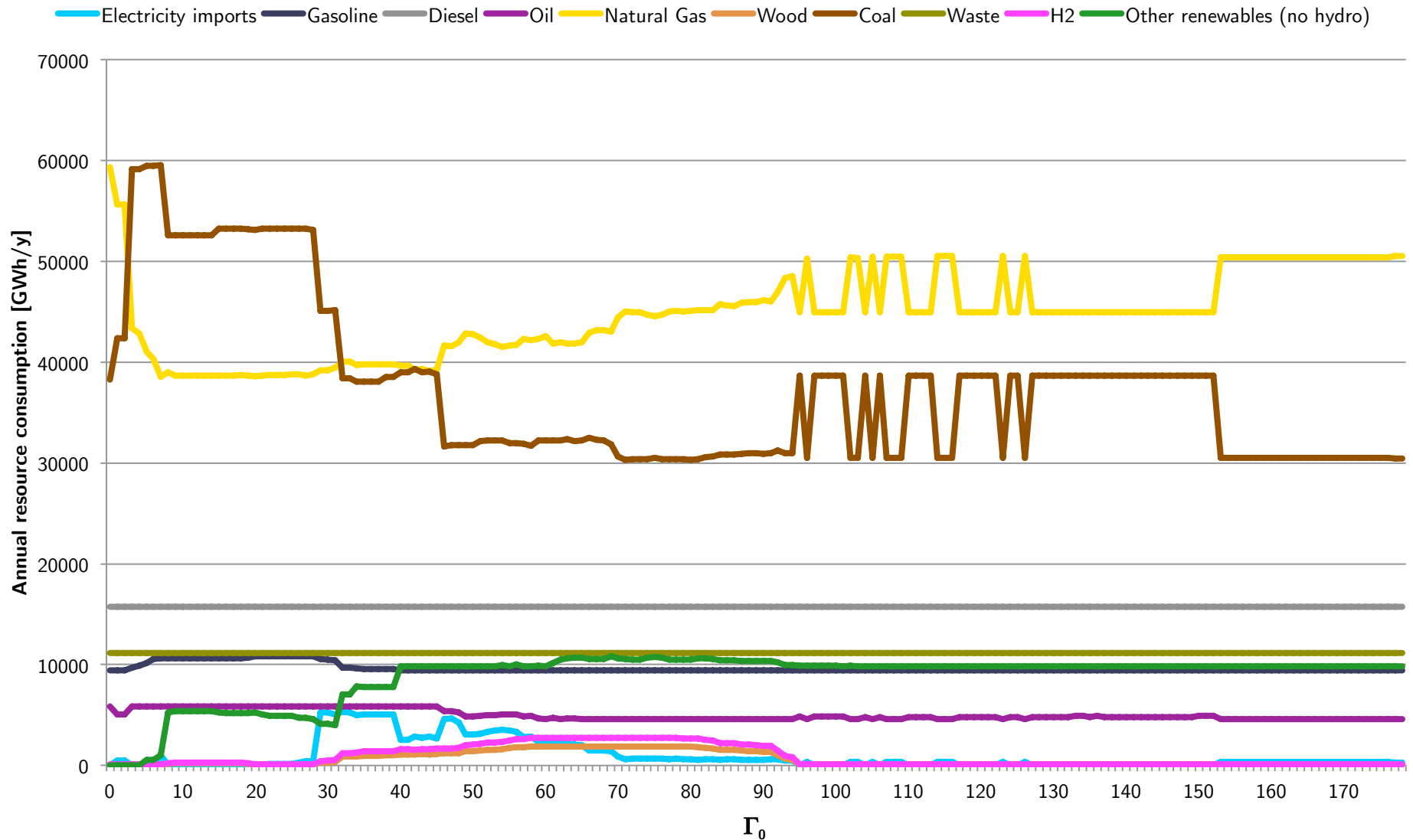
$-\mathbf{y}_{inv}(j) \leq \tau(j)\mathbf{Mult}(j) \leq \mathbf{y}_{inv}(j) \quad \forall j \in TECH/STO$

### New Objective

$$\begin{aligned} \min \quad & \sum_{j \in TECH} (\tau(j)\mathbf{C}_{inv}(j) + \mathbf{C}_{maint}(j)) + \sum_{i \in RES} \mathbf{C}_{op}(i) \\ & + \mathbf{z}_0\Gamma_0 + \sum_{i \in RES} \sum_{t \in T} \mathbf{p}_{0,op}(i, t) + \sum_{j \in TECH/STO} \mathbf{p}_{0,inv}(j) \end{aligned}$$

# Results

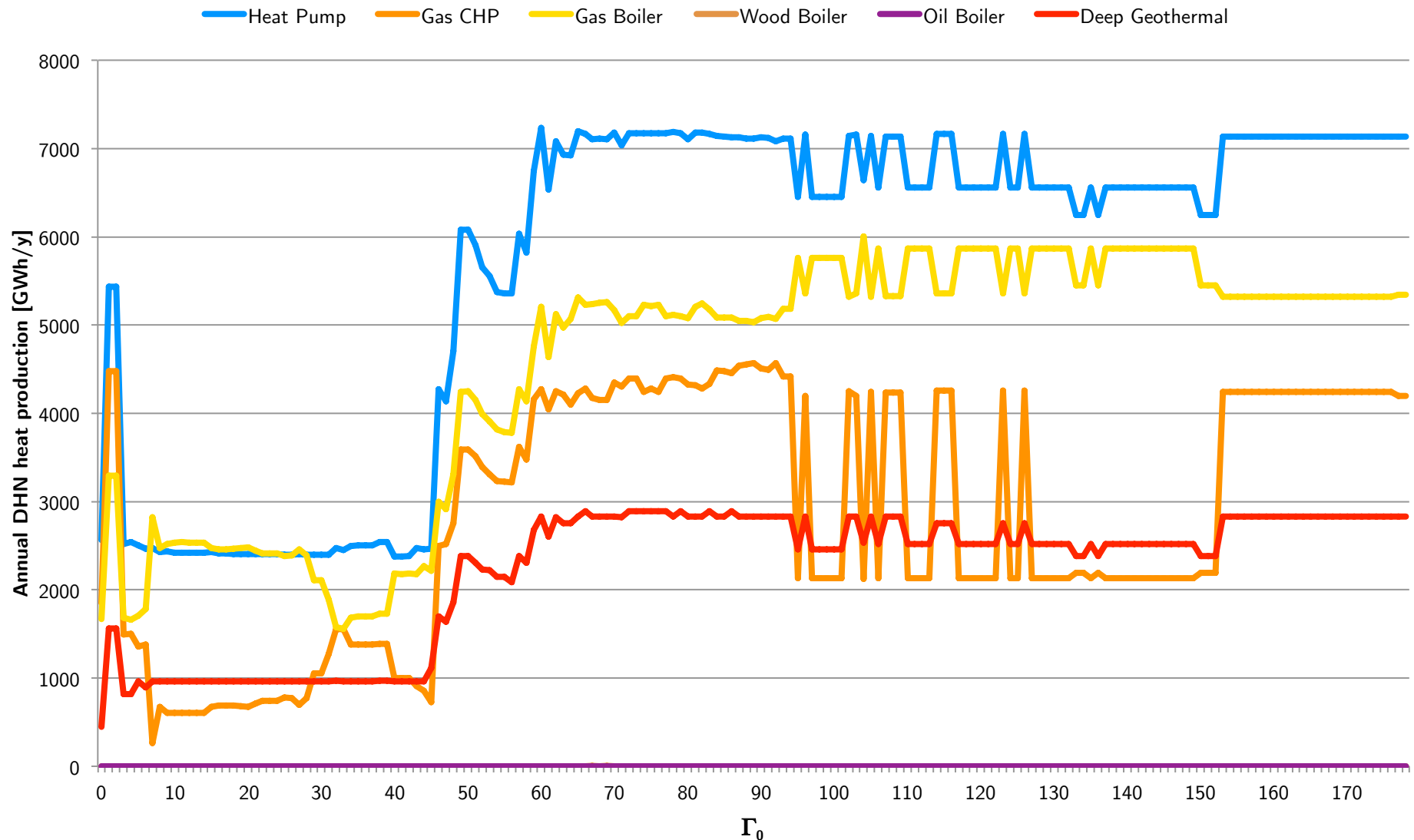
## Robust optimization: first results





# Results

## Robust optimization: first results



# Conclusions

# Conclusions

## Summary

MILP framework for strategic energy planning under uncertainty:

- Energy based model
- “**Snapshot**” model: optimization of the energy system in a future target year
- Simplified yet complete energy system: inclusion of **heating** and **mobility**
- Multiperiod formulation: seasonality of demand and energy **storage**
- Concise structure
- Low complexity: low number of **integer variables**
- Life Cycle Assessment: Global Warming Potential (CO<sub>2</sub>-eq. emissions)

Application to case study → preliminary results:

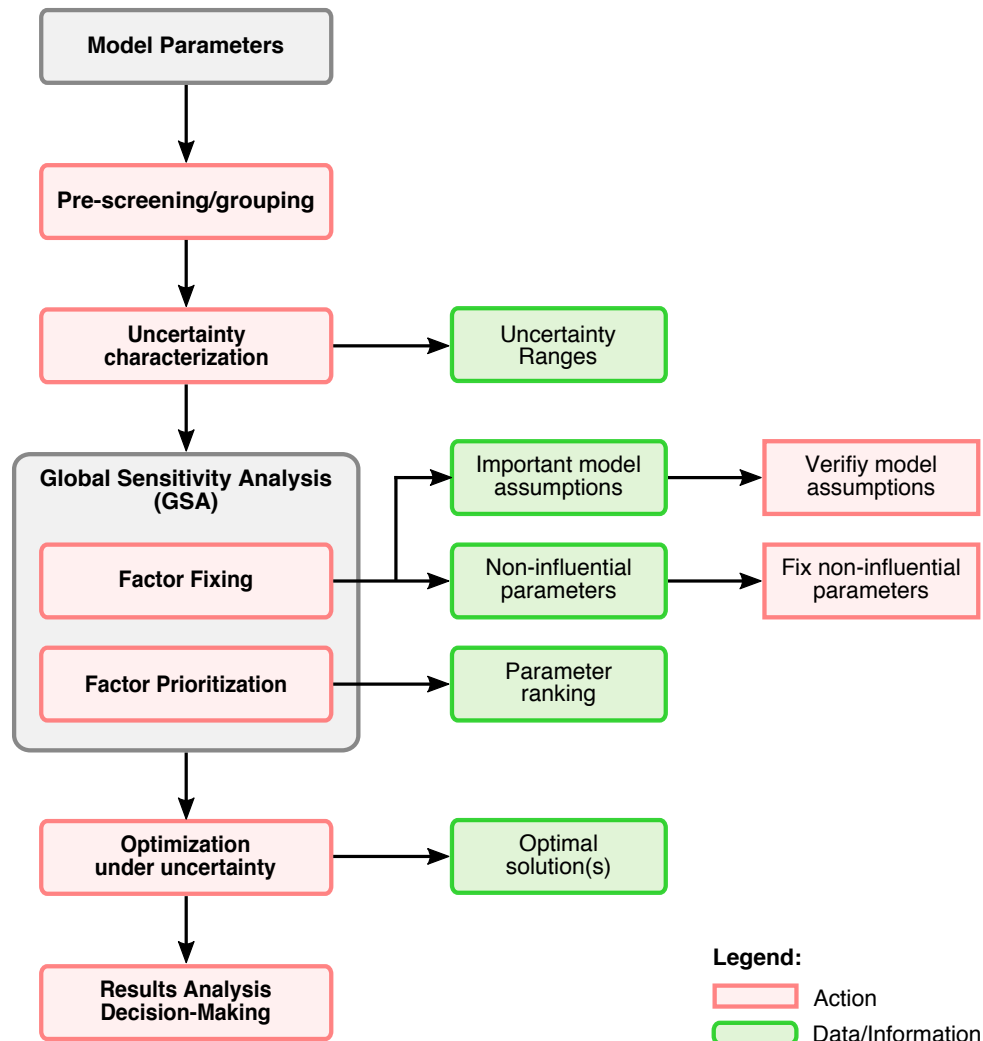
- Global Sensitivity Analysis
- Robust optimization



Impact of uncertainty on energy strategy

# Conclusions

## Future work



# Thank you! Questions?

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# Appendix

# MILP model

## Model structure: parameters

Table 1: Parameter list with description. Set indices as in Figure 1

Parameter	Units	Description
$endUses_{year}(eui, s)$	[GWh/y] <sup>a</sup>	Annual end-uses in energy services per sector
$i_{rate}$	[-]	Real discount rate
$\%_{public,min}, \%_{public,max}$	[-]	Upper and lower limit to $\%_{Public}$
$\%_{rail,min}, \%_{rail,max}$	[-]	Upper and lower limit to $\%_{Rail}$
$\%_{dhn,min}, \%_{dhn,max}$	[-]	Upper and lower limit to $\%_{Dhn}$
$t_{op}(t)$	[h]	Time periods duration
$\%_{lighting}(t)$	[-]	Yearly share (adding up to 1) of lighting end-uses
$\%_{sh}(t)$	[-]	Yearly share (adding up to 1) of SH end-uses
$f(res \cup tech \setminus sto, l)$	[GW] <sup>b</sup>	Input from (< 0) or output to (> 0) layers. $f(i, j) = 1$ if $j$ is main output layer for technology/resource $i$
$mult_{ref}(tech)$	[GW] <sup>bc</sup>	Reference size with respect to main output
$c_{inv}(tech)$	[M€/GW] <sup>bc</sup>	Technology specific investment cost
$c_{maint}(tech)$	[M€/GW/y] <sup>bc</sup>	Technology specific yearly maintenance cost
$n(tech)$	[y]	Technology lifetime
$f_{min}, f_{max}(tech)$	[GW] <sup>bc</sup>	Min./max. installed size of the technology
$avail(res)$	[GWh/y]	Resource yearly total availability
$c_{p,t}(tech, t)$	[-]	Period capacity factor (default 1)
$c_p(tech)$	[-]	Yearly capacity factor
$c_{op}(res, t)$	[M€/GWh]	Specific cost of resources
$\mathcal{E}_{sto,in}, \mathcal{E}_{sto,out}(sto, l)$	[-]	Efficiency [0; 1] of storage input from/output to layer. Set to 0 if storage not related to layer.
$\%_{lossElec}$	[-]	Losses [0; 1] in the electricity grid

# MILP model

## Model structure: variables

Table 2: Variable list with description. All variables are continuous and non-negative, unless otherwise indicated.

Variable	Units	Description
<b>EndUsesInput</b> ( $eui$ )	[GWh/y] <sup>a</sup>	Total annual end-uses in energy services
<b>EndUses</b> ( $l, t$ )	[GW] <sup>b</sup>	End-uses demand. Set to 0 if $l \notin EUT$
<b>%Public</b>	[-]	Ratio [0; 1] public mobility over total passenger mobility
<b>%Rail</b>	[-]	Ratio [0; 1] rail transport over total freight transport
<b>%Dhn</b>	[-]	Ratio [0; 1] centralized over total low-temperature heat
<b>N</b> ( $tech$ ) $\in \mathbb{N}$	[-]	Number of installed units of size $mult_{ref}$
<b>Mult</b> ( $tech$ )	[GW] <sup>bc</sup>	Installed capacity with respect to main output
<b>Mult</b> <sub><math>t</math></sub> ( $tech \cup res, t$ )	[GW] <sup>bc</sup>	Operation in each period
<b>C<sub>inv</sub></b> ( $tech$ )	[M€]	Technology total investment cost
<b>C<sub>maint</sub></b> ( $tech$ )	[M€/y]	Technology yearly maintenance cost
<b>C<sub>op</sub></b> ( $res$ )	[M€/y]	Total cost of resources
<b><math>\tau</math></b> ( $tech$ )	[-]	Investment cost annualization factor
<b>Sto<sub>in</sub>, Sto<sub>out</sub></b> ( $sto, l, t$ )	[GW]	Input to/output from storage units
<b>LOSS<sub>Elec</sub></b> ( $t$ )	[GW]	Electricity transmission losses

<sup>a</sup>[Mpkm] (millions of passenger-km) for passenger, [Mtkm] (millions of ton-km) for freight mobility end-uses

<sup>b</sup>[Mpkm/h] for passenger, [Mtkm/h] for freight mobility end-uses

<sup>c</sup>[GWh] if  $tech \in STO$



# MILP model

## Model structure: constraints

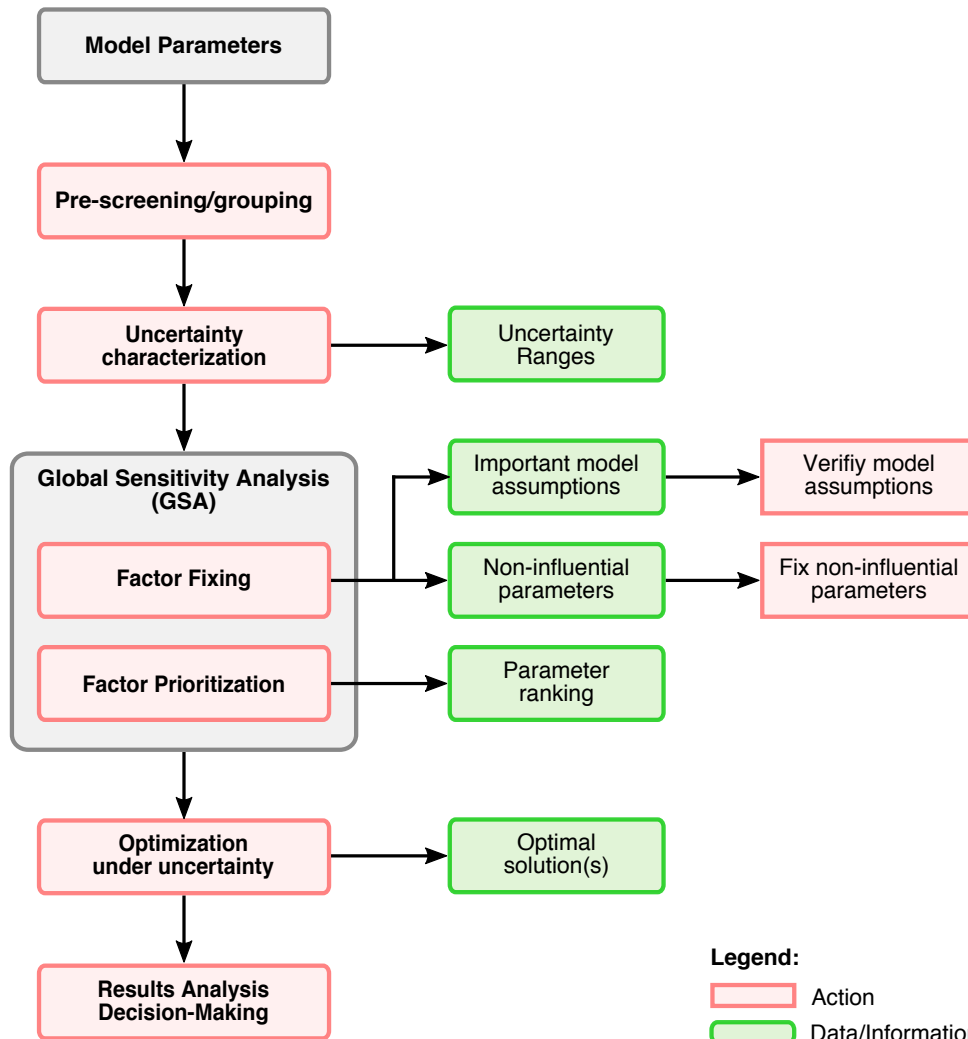
$$\mathbf{Loss}_{Elec}(t) = (\mathbf{EndUses}(k) - \sum_{j \in TECH \setminus STO | f(j,k) < 0} f(j,k) \mathbf{Mult}_t(j,t)) \%_{loss_{Elec}} \quad k = Elec, \forall t \in T \quad (16)$$

$$\mathbf{Mult}_t(j,t) + \mathbf{Mult}_t(k,t) \geq \frac{\mathbf{EndUses}(HeatLowTDHN,t) + \mathbf{EndUses}(HeatLowTDec,t)}{\mathbf{EndUsesInput}(HeatLowTSH) + \mathbf{EndUsesInput}(HeatLowTHW)} \sum_{t \in T} \mathbf{Mult}_t(j,t) t_{op}(t)$$

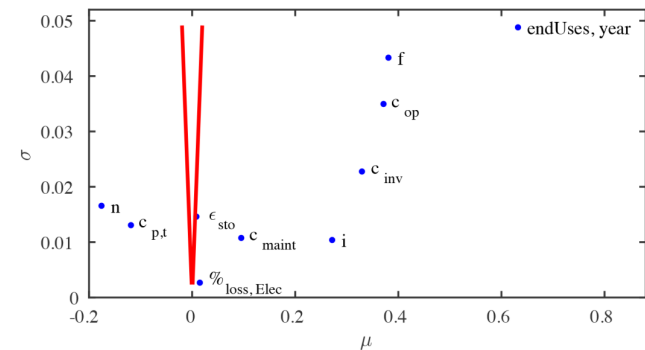
$$k = Dec_{Solar}, \forall j \in TECH \text{ OF } EUT(HeatLowTDec) \setminus \{k\}, \forall t \in T \quad (17)$$

# Results

## Global Sensitivity Analysis: First results



### Factor Fixing



- Morris method for factor fixing.
- $\pm 20\%$  variation for all the parameters.
- Parameters outside the  $\nabla$  are influential