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Holistic design guidelines for solar hydrogen production by photo-electrochemical routes†

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Device and system design choices for solar energy conversion and storage approaches require holistic design guidelines which simultaneously respect and optimize technical, economic, sustainability, and operating time constraints. We developed a simulation platform which allows for the calculation of solar-to-hydrogen efficiency, hydrogen price, device manufacture and operation energy demand, and the component degradation and replacement time of photo-electrochemical water splitting devices. Utilizing this platform, we assessed 16 different design types representing all possible combinations of a system: (i) operating with or without irradiation concentration, (ii) utilizing high-performing and highcost or low-performing but low-cost photoabsorbers, (iii) utilizing high-performing and high-cost or low-performing but low-cost electrocatalysts, and (iv) operating with or without current concentration between the photoabsorber and the electrocatalyst. Our results show that device types exist with a global optimum (a Pareto point), simultaneously maximizing efficiency, while minimizing cost and the energy demand of manufacture and operation. In our examples, these happen to be the device types utilizing high irradiation concentration, as well as expensive photoabsorbers and electrocatalysts. These device types and designs were the most robust to degradation, exhibiting the smallest price sensitivity for increasing degradation rates. Other device types did not show a global optimum, but rather a set of partially optimized designs, i.e. a Pareto front, requiring a compromise and prioritization of either performance, cost, or manufacture and operation energy demand. In our examples, these happen to be the device types using low-cost photoabsorbers. The targeted utilization of irradiation and current concentration predicted that even device types utilizing expensive components can provide competitive solutions to photo-electrochemical water splitting. The quantification of the influence of component degradation on performance allows the suggestion of best practice for device operational time and component replacement. The framework and findings presented here provide holistic design guidelines for photo-electrochemical devices, and support the decision-making process for an integral and practical approach to competitive solar hydrogen production in the future.

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Broader context

Solar energy is the most abundant renewable energy source on earth. It is dilute, unequally distributed, and intermittent but can be stored, for example, in an energy-dense and transportable fuel such as hydrogen. Photo-electrochemical water-splitting devices convert solar energy into chemical energy integrating photo absorption, charge generation and separation, and electrocatalysis in a single device. The viability of such a device is only possible if four requirements are simultaneously fulfilled: (i) high performance, (ii) low cost, (iii) sustainability, and (iv) robustness. All devices developed up to now provide combinations of these aspects but do not simultaneously fulfill all of them. Holistic design guidelines outlining a pathway for scalable systems are required to provide a fast route to practical implementation.

1. Introduction

Since the first demonstrations of photo-electrochemical (PEC) water splitting devices more than 40 years ago, much research has focused on the development of efficient, low-cost, sustainable, and stable PEC components. As component performance has increased and synthesis approaches have matured, research

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has considered questions related to the integration of complete working PEC devices and systems, as well as corresponding performance, cost, sustainability, and stability assessment.² Studies have assessed the economics of different PEC designs and systems ranging from particle-based to electrode-based systems,3 from closely integrated to decoupled systems,2 and from small to large scale facilities. 4,5 These studies indicate that solar hydrogen has the potential to be produced for \$2-\$10 per kilogram.3 The sustainability of the devices has been assessed by examining the energy demand and the energy payback time in order to ensure that such devices produce more energy during their operating time than required for their manufacture. 4,6,7 These studies indicated that PEC devices and systems can produce sustainable hydrogen when minimal efficiencies (in the range of 5%) and lifetimes (in the range of 10 years) can be guaranteed. Performance of PEC devices is usually assessed by solar-to-hydrogen (STH) efficiency, which has been used to compare novel device designs incorporating different components and materials as well as designs using concentration to reduce the mass of costly materials with energy intense processing steps.^{8,9} Measured STH efficiencies above 10% have been reported for lab-scale demonstration made of solely earth abundant materials, 10 high-cost rare materials, 11-13 and novel perovskite materials. 14 In addition to cost, sustainability, and efficiency, the long-term stability and robustness of a device are also of major concern for a practical PEC device design. 14,15 Measured device performance has shown stability up to several hours only. 12,14 These four indicators provide an assessment as to whether hydrogen production by PEC devices and systems has the potential to provide a scalable solution and, consequently, contribute significantly to a future renewable energy economy.

Recent detailed studies focusing on design improvement through a variety of material and component choices have shown that the lowest hydrogen cost of non-concentrating devices,⁵ and the largest energy yield ratios of concentrating devices,⁷ result from optimized material, component, and design choices. Therefore, life cycle assessments and economic studies which focus solely on one or few materials and components, or one or few device designs, provide limited guidance for integrated device design decisions. Moreover, these studies have only considered one indicator, e.g. price, energy input, or efficiency, ignoring whether at the maximized indicator the other indicators would still support a meaningful design, for example maximizing the device efficiency but providing a costly and energy-intense production design, or minimizing price but providing a low-efficiency and energy-intense production design. Maintaining this strategy will not provide holistic design guidelines, nor long-term meaningful guidance regarding which design strategies should be further investigated and optimized.

We proposed the use of multi-objective investigations to account for efficiency, price, manufacture and operation energy balance, and operating time in order to provide holistic guidelines for overall device design, material and component combinations and choices, operating conditions (e.g. using concentrated or non-concentrated irradiation), and component replacement time and degradation. We considered a device composed of photoabsorbers, membrane-separated electrocatalysts, and peripheral elements such as cables, wires, and pumps (balance of system, BOS). Multi-junction photovoltaics (PV) were considered as photoabsorbers, and polymer electrolyte membrane electrolyzers (PEMEC) as membrane-separated catalysts. A concentrator was used when concentrated irradiation was examined, together with a sun-tracking system to compensate for the low acceptance angle of concentrators. The photoabsorbers convert the incoming irradiation (concentrated or not) to electron and hole pairs, which are separated by internal electrical fields, and provide current at a sufficient potential to perform the anodic and cathodic electrochemical reactions, i.e. oxygen evolution and hydrogen evolution reactions, respectively. The modular nature of these devices was explored through the selection of two photoabsorber components (Si-based or III-V based cells) and two sets of electrocatalysts (Co₃O₄/Ni or RuO₂/ Pt). The component material choices were motivated by the desire to span a large range of possible material choices covering an exhaustive range of low-cost and low-performance, and high-cost but high-performance solutions. The material choices are examples and not preferential to, or selected to be optimal for our particular application. The components were combined in a range of device designs characterized by two concentration ratios: (i) irradiation concentration ratio, C, defined by the ratio of the irradiated concentrator area to the photoabsorber area $(C = A_{\text{conc}}/A_{\text{PV}})$, and (ii) the current concentration ratio, F, defined by the ratio of the catalyst-covered projected electrode area to the photoabsorber area ($F = A_{PEMEC}/A_{PV}$). The factor Fgenerally indicates whether a system is closely coupled (F = 1), for example, in the case of traditional photoelectrochemical devices where the photoabsorber is closely integrated with the electrocatalyst, or indicates whether a system is loosely coupled or completely decoupled $(F \neq 1)$, for example, in the case of externally wired PV and electrolyzers. An obvious exception to this are nano-structured photoelectrodes such as catalyst covered micro-wires, which provide a similar effect as F. The device and the component choices are indicated in Fig. 1. The system boundary was set to only account for the device and immediate peripheral components (BOS) allowing for comparison of different device designs with different combinations of materials. Requirements associated with the installation, operation, maintenance, decommissioning, and overall management of a large scale H2 production plant were not considered.

The characteristic device types and designs studied in this work and the corresponding codes used are depicted in Table 1. Design types 1–4 and 9–12 are types using concentrated irradiation ($C \neq 1$), and design types 5-8 and 13-16 are types using no concentration (C = 1). Design types 1–8 are loosely coupled PV-electrolyzer designs $(F \neq 1)$, and design types 9–16 are more closely coupled designs (F = 1). If not indicated otherwise, the replacement time of a device and its components is assumed to be 30 years, except for the PEMEC, whose replacement time is assumed to be 10 years. The four device indicators - performance, cost, sustainability, and degradation - were assessed using STH efficiency, hydrogen price (\$ kg_{H2}⁻¹), energy input (MJ kg_{H2}⁻¹), and operational time (years).

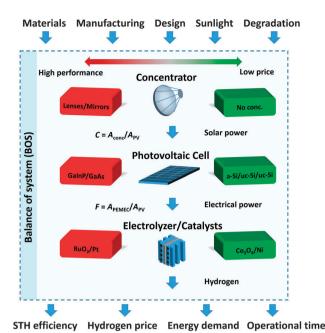


Fig. 1 Schematic representation of device component choices with inputs and outputs of this study. The choice between advantageous performance or cost for the concentrator, the PV cell, and the PEMEC results in 8 possible device solutions, which are extended by considering current concentration for each case ($F \neq 1$), resulting in 16 device types investigated. For the concentrator, low price technology implies no concentration.

2. Methods and assumptions

The device types considered are integrated photo-electrochemical devices, composed of multiple protected photoabsorbers in the form of traditional multi-junction photovoltaics (PV), coupled to membrane-separated electrocatalysts in the form of a polymer electrolyte membrane electrolyzer (PEMEC). Current concentration was possible between the photoabsorber and the electrocatalyst, characterized by the factor $F = A_{PEMEC}/A_{PV}$. The device was irradiated by sunlight. Irradiation concentration was possible by using a concentrator with a characteristic irradiation concentration ratio $C = A_{\text{conc}}/A_{\text{PV}}$. The concentrator was composed of a concentrating module - Fresnel lenses, parabolic trough, or solar tower - and a sun-tracking system acting as a support. The efficiency of a concentrator was assumed 85% at the beginning of its lifetime.⁷

Devices were modeled using equivalent circuit models for the photoabsorber and membrane-separated electrocatalysts. The influence of 1D and 2D on the performance has been

investigated elsewhere. 16,17 The PV cell was either a Si-based triple junction cell (a-Si/µc-Si/µc-Si) or a III-V dual-junction cell (GaInP/GaAs). The PV cells were modeled using either the Shockley-Queisser limits¹⁸ and an ideal diode equation, see eqn (Si) and (Sii) in ESI,† for the III-V based cells (band gaps 1.9 and 1.43 eV), or experimental data 19,20 and equation fitting, see eqn (Siii) to (Sv) in ESI,† for the Si-based cells. Potentially, the radiation will be partially absorbed in the electrolyte before incident on the PV.21 This effect as well as phenomena related to two-phase flow were neglected as they heavily depend on the design. The electrolyzer model accounted for ohmic losses in the membrane and solid electrolyte (see eqn (Svi) and (Sviii) in ESI†), activation overpotentials of the anodic and cathodic reactions (see eqn (Svii) in ESI†), mass transport limitations due to concentration overpotentials (see egn (Six) in ESI†), and potential losses due to degradation (see eqn (Sxiii) in ESI†). 22-24 The proton conducting membrane had the properties of commercial Nafion (thickness 50 µm and conductivity of 10 S m⁻¹). Two PEMEC types were considered with two selected sets of catalysts: expensive but efficient catalysts (Pt for the cathode and RuO2 for the anode with exchange current densities of $7.2 \times 10^{-4} \text{ A cm}^{-2}$ and $3.0 \times 10^{-8} \text{ A cm}^{-2}$, respectively) and catalysts made of earth abundant materials (Ni and Co₃O₄ with exchange current densities of $2.5 \times 10^{-6} \text{ A cm}^{-2}$ and 1.1×10^{-9} A cm⁻², respectively). Typical current-voltage curves for devices with different irradiation and current concentrations are shown in Fig. S1 (ESI†).

The BOS specifications included a pump for the water cooling system, therefore device operation was assumed isothermal at T = 298 K for all types and concentrations. Potential temperature increase at high concentrations which could reduce the PV performance and increase the PEMEC performance were neglected.²⁶ This assumption was justified as preliminary numerical analysis on thermal management in concentrated PEC suggested that the performance decrease due to increased temperature can be minimized. 26,27

The materials were chosen as reasonable lower and upper limits in terms of price and efficiency. GaInP/GaAs cells were selected as an example of an efficient and costly technology, predominantly used in space applications. The double junction cells provided enough electrical potential for water splitting. Triple junction a-Si/μc-Si/μc-Si cells were chosen as a low price silicon cell technology able to provide enough potential for water splitting. The choice of electrocatalysts was based on the previous selection of Rodriguez et al.5 who reported the price

Table 1 Number coding of device types investigated according to PV cell and the PEMEC component choice, with $(C \neq 1)$ or without (C = 1)concentrated irradiation, and with $(F \neq 1)$ or without (F = 1) current concentration

		With current concentration (variable F) No current concentration ($F = 1$)							
		High quality catalyst (RuO ₂ /Pt)	Low price catalyst (Co ₃ O ₄ /Ni)	High quality catalys (RuO ₂ /Pt)	t Low price catalyst (Co ₃ O ₄ /Ni)				
With concentrator (variable <i>C</i>)	High quality photoabsorber (III–V)	1	2	9	10				
	Low price photoabsorber (Si)	3	4	11	12				
No concentrator $(C = 1)$	High quality photoabsorber (III–V)	5	6	13	14				
	Low price photoabsorber (Si)	7	8	15	16				

and performance of 6 electrocatalysts. We selected the most efficient ones (RuO_2 and Pt) and the cheapest ones (Co_3O_4 and Ni) for our study. All the selected materials needed available data to conduct the study, namely: price and energy demand, efficiency, electrochemical performance and photoabsorber behavior under concentrated irradiation, which was not available for other candidate device designs and materials such as highly efficient devices made of earth abundant materials or perovskite-based PECs, and hence were not chosen in our analysis. The material choices are examples and not preferential to, or selected to be optimal for our particular application.

The model was implemented in its transient form in order to account for the non-linear effects of degradation on operating performance. This transient investigation didn't account for the variation in solar irradiation during the day but assumed constant yearly-averaged irradiation values. Details on the effect of the irradiation variation on performance and sustainability of a device have been given elsewhere.^{7,26} Degradation of components and materials was included in the model to account for the decrease of the short circuit current of the PV cell and additional overpotentials in the PEMEC with time. Degradation rates were selected from literature and assumed the same for III-V and Si-based cells, i.e. 0.17% year⁻¹ to 2.5% year⁻¹ reduction in the short circuit current.^{28,29} The increase of the PEMEC overpotential with aging was 1 μ V h⁻¹ to 14 μ V h⁻¹. Mean degradation rates were chosen for the reference case, if not indicated otherwise, but the minimum (optimistic case) and maximum (conservative case) values were used in order to assess the effect of additional degradation sources such as high temperature, corrosion, and light intermittency. The degradation of the 85% efficient concentrator was assumed to be linear at 19.5% loss in optical efficiency after 30 years, i.e. a 0.65% loss per year.

Energy input and the price of devices were evaluated according to life cycle inventories and cost analysis of the four components: the concentrator device with tracking and support, the PV cells, the PEMEC, and the balance of system (BOS). BOS includes the peripheral components (cables, wires, control systems, pumps). The device cost accounted for materials and manufacturing. The energy assessment included the energy input required for materials mining, the manufacture of device components, and operation. We will call this energy input for the sustainability assessment the energy demand of the device. Details on device performance modeling, prices and energy inventory, and degradation and replacement time considerations are given in Table 2 and in the ESI.†

The hydrogen production of a given device type and design was determined by Faraday's law of electrolysis utilizing the operating current resulting from the simultaneous fulfillment of the current-voltage requirements in the PV cell and the PEMEC.

The hydrogen price was calculated as the ratio of the cumulated cost of the device to the cumulated hydrogen production at a given operational time L,

$$p_{\rm H_2}(L) = \frac{\sum_{i} p_i A_i E(L/L_i) + P_{\rm op} L}{\int_0^L \dot{m}_{\rm H_2}(L^*) dL^*}$$
(1)

Table 2 Energy demand and price for the components of the device

	$e (\mathrm{MJ} \mathrm{m}^{-2})$	p (\$ m ⁻²)
Concentrators		
Parabolic troughs	$1639^{34,35}$	$295^{36,37}$
Solar tower heliostats	2356^{35}	$164^{36,37}$
Flatcon	1882^{38}	170^{39}
Dishes	_	$176^{40,41}$
2-Axis Fresnel	_	$202^{40,41}$
Amonix 7700	3129^{42}	198^{43}
Average value	2251	201
Photoabsorbers	_	
PV (Si)	1230^{7}	145^{5}
PV (III-V)	8540^{44}	75000^{45}
Electrochemistry		
PEMEC (RuO ₂ /Pt)	$2948^{46,47}$	1000
PEMEC (Co ₃ O ₄ /Ni)	2064	245
Peripherals		
BOS (with concentration)	550^{42}	137 ^{39,45}
BOS (no concentration)	$550^{48,49}$	76 ^{48,49}

using the produced mass flow rate of hydrogen in kg year⁻¹, $\dot{m}_{\rm H_2}$, the year-averaged operational electrical cost in \$ year⁻¹, $\dot{p}_{\rm op}$, the cost per unit area in \$ m⁻², p_i , the area in m², A_i , and the replacement time in years, L_i , all for the $i^{\rm th}$ component. The operational time L, ranged from 1 year to a maximum of 30 years. E is a ceiling function accounting for the replacement of components. This calculation method accounted for the effect of replacement time, size, and performance of the components. A component replacement time of 10 years was assumed for the PEMEC, and 30 years for all the other components (concentrator, PV cell, and BOS). ^{7,28,32,33}

The hydrogen energy requirement in MJ ${\rm kg_{H_2}}^{-1}$ was calculated using the same approach, utilizing the energy requirements of materials instead of cost.

The yearly and operational time-averaged STH efficiencies at a given operational time were calculated as:

$$STH_y(L) = \frac{\dot{m}_{H_2}(L) \frac{2F}{M_{H_2}} \Delta E_0}{\Phi_{\text{sun}}},$$
 (2)

$$STH(L) = \frac{1}{L} \int_0^L STH_y(L^*) dL^*, \qquad (3)$$

using the equilibrium potential for water electrolysis at standard conditions, $\Delta E_0 = 1.23$ V, and the solar power in W, $\Phi_{\rm sun}$, incident on the concentrator for concentrated devices or directly on the PV cell for non-concentrated devices. The AM1.5 spectral distribution was considered as the incoming non-concentrated irradiation spectrum. It was weighed with the 2093 kW h m⁻² year⁻¹ yearly-averaged direct normal irradiation (DNI) of Tabernas in southern Spain for tracked concentrating devices, while the 1872 kW h m⁻² year⁻¹ global horizontal irradiation (GHI) was used for untracked, non-concentrating devices. The tracked direct irradiation and the untracked combined direct and diffuse irradiation represented 77% and 69%, respectively, of the 2716 kW h m⁻² year⁻¹ maximum collectable irradiation at

that location. Since the calculation of the STH was based on the total irradiation and not on the DNI, the values reached by the devices in this study were lower than similar setups where DNI has been taken as the reference irradiation. 11,51

3. Results and discussion

The generally expected effects of the two design parameters – C and F – on each of the four indicators have been partially explored. ^{5,7} Our observations followed these expected effects. An increase in C affected the PV cell by an increase in the photocurrent density, increased open circuit voltage, $V_{\rm oc}$, and reduced efficiency, unless the PV cell was specifically designed for large C. An increase in C affected the PEMEC through the PV provided current, which increased, consequently increasing the overpotentials in the PEMEC. An increased C reduced the importance of the PV cell and PEMEC to the device price and energy requirements, as their area and weight fractions in the device were decreased. An increase in F reduced the current density in the PEMEC and therefore the overpotentials. An increased F however also increased the price of the device because of the larger electrode area.

Indicators' dependence on operational time

The performance of the PV cell, the PEMEC, and the concentrator (if used) decreased with time and an additional price and energy investment was required when components needed to be replaced. The hydrogen price decreased with operational time as a given set of components produced an increased cumulative quantity of hydrogen before replacement. Typical transient behaviors of the yearly STH efficiency, hydrogen price, component prices, and energy demand are depicted in Fig. 2 (for device type 2 - concentrating/III-V based PV cells/low-cost catalysts – with $C = C_{opt} = 1000$ and $F = F_{opt} = 3.2$, and device type 7 - non-concentrating/Si-based PV cells/high-quality catalysts – with C = 1 and F = 0.013). Superscript "opt" indicates the irradiation and current concentration factors which lead to the lowest device price for a device type. The minimum hydrogen price, p_{\min} (\$ kg_{H₂}⁻¹), was typically observed when the operational time was equal to the component replacement time (30 years or 60 years). The minimum energy demand for the device, e_{\min} (MJ kg_{H2}⁻¹), was also achieved when the operational time was equal to the component replacement time. Device types with concentrator and Si-based PV cells showed the lowest prices and energy demand already 1-3 years before

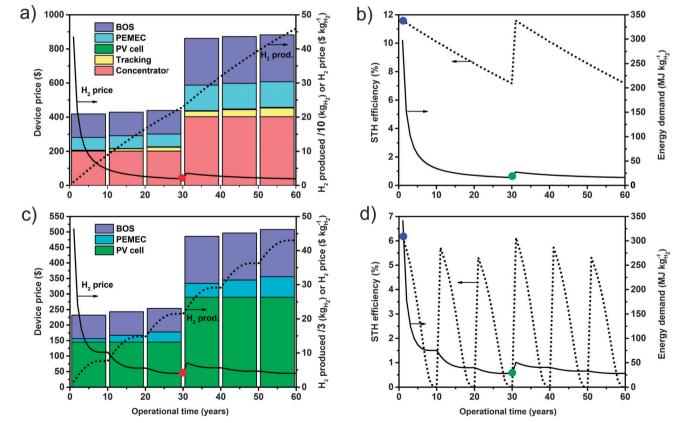


Fig. 2 Transient device price (\$), total hydrogen production (kg_{H_2}), hydrogen price (\$ kg^{-1}), yearly-averaged STH efficiency, and energy input (MJ $kg_{H_2}^{-1}$) for (a and b) device type 2 (concentrating/III–V based PV cells/low-cost catalysts) with $C = C_{\rm opt} = 1000$ and $F = F_{\rm opt} = 3.2$, and (c and d) device type 7 (non-concentrating/Si-based PV cells/high-quality catalysts) with C = 1 and F = 0.013. All components are replaced after 30 years, except for the PEMEC, which was replaced after 10 years. The most profitable configuration ($p_{\rm min}$) is indicated by a red dot, the most sustainable ($e_{\rm min}$) by a green dot, and the most efficient by a blue dot.

the component replacement time (at years 27 to 29) as the continuous tracking expenses can't be compensated because of the low hydrogen production resulting from degradation in the components and relatively low V_{oc} . The difference in price or energy requirement were however very low (less than 1%) compared to the values obtained for an operating time of 30 years. Therefore all the following results are shown for a 30 years operational time. The performance was lowest when the operational time was equal to the component replacement time, and maximal at the beginning of operation. The exact behavior differed between device types and between device designs. For example the influence of the degradation was more detrimental to device type 7 than device type 2. For device type 7 the hydrogen production dropped to almost zero already before the PEMEC was to be replaced (after 10 years in this case).

The observation that device performance was maximal at operational debut, and cost and energy were minimal when the operational time was equal to the component replacement time, was generally true for all device types. Since a device operational time of one year, for which the yearly-averaged STH efficiency (eqn (2)) was maximized, was unrealistic, an operational time-averaged efficiency (eqn (3)), STH, was additionally used for characterization. Consequently, for each device type and design there were three possible strategic choices: (i) design for minimum hydrogen price (p_{\min}) , (ii) design for minimum energy demand (e_{\min}) , and (iii) design for maximized performance

over the operational time (STH_{max}). Fig. S7 (ESI†) quantifies the irradiation concentration, C, and current concentration, F, for each of 16 different device types for the three strategies.

Influence of irradiation and current concentration on cost

The detailed influence of C and F on the hydrogen price is shown in Fig. 3 for design types 1–4 $(F \neq 1)$ and 9–12 (F = 1), the latter representing subsets of the plot and the corresponding C-F-space. Note that for device types 5-8 and 13-16, no concentrator and tracker are used and consequently the prices were different than indicated in Fig. 3 along the y-axis for C = 1. Device types 1 and 2, i.e. concentrating devices using III-V PV based cells, showed lowest hydrogen prices at highest irradiation concentration and slight current dilution (F > 1). The extremely high cost of the III-V based PV cells favors these irradiation concentrations. Slight current dilution is beneficial for the performance while acceptable for device cost as the PEMEC cost is negligible at these C, as shown in Fig. 4: Costs are dominated by the cost of the concentrator, BOS, and PV cells. Therefore also F can be freely adjusted to obtain maximum performance with a small variation in the hydrogen price (less than $\pm 15\%$ variation in hydrogen price when $F_{\rm opt}$ < F < 10), also shown in Fig. S2 (ESI†). The III-V based cells investigated exhibit a high V_{oc} , providing enough potential to drive at these C and high operating currents. The slight current dilution ensures that mass transport limitations are not limiting

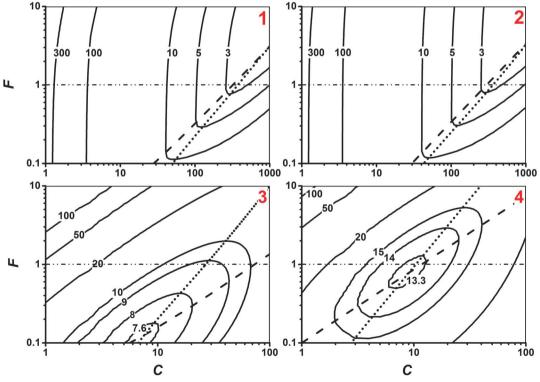


Fig. 3 p_{min} (in precent sequential sesubtypes 9-12. Optimum F for a given C is shown by the dashed line, optimum C for a given F is shown by the dotted line. Minimum hydrogen prices $(\$2.03 \text{ kg}_{\text{H}_2}^{-1}, \$2 \text{ kg}_{\text{H}_2}^{-1}, \$7.54 \text{ kg}_{\text{H}_2}^{-1}, \$13.2 \text{ kg}_{\text{H}_2}^{-1} \text{ for devices 1, 2, 3, and 4, respectively)}$ are reached at the cross point between these two curves ($C = 1.00 \text{ kg}_{\text{H}_2}^{-1}$) $C_{\rm opt} = 1000$ and $F = F_{\rm opt} = 3.2$ for devices 1 and 2, $C = C_{\rm opt} = 7$ and $F = F_{\rm opt} = 0.12$ for device 3, and $C = C_{\rm opt} = 9$ and $F = F_{\rm opt} = 0.74$ for device 4). Minimum hydrogen prices for designs 9-12 ($C = C_{opt} = 400$, 380, 28 and 11) are given by the intersection of the dotted and the dot-dashed lines at F = 1.

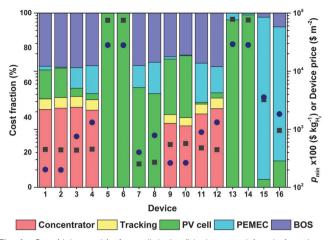


Fig. 4 Cost (right *y*-axis) of overall device (black rectangle) and of produced hydrogen (blue circle), and cost fraction of the various components (left *y*-axis): concentrator, solar tracking, photoabsorber (PV), electrocatalysts and separator (PEMEC), and peripherals (BOS). The data is shown for cost-optimized device designs of type 1–16 (see Table 1).

in the PEMEC, as visible in Fig. S1 (ESI†). The maximum performance was not affected by the degradation of the PEMEC as the operating voltage was much smaller than the $V_{\rm oc}$ provided by the PV cell. This allowed the device to cope with additional potential losses in the PEMEC while still operating in the maximum current plateau region of III–V PV cells during the complete operational time. This also explains why hydrogen prices showed little dependence on the choice of PEMEC in this case, with $p_{\rm min}$ = \$2.03 kg $_{\rm H_2}^{-1}$ and \$2 kg $_{\rm H_2}^{-1}$ for devices 1 and 2, respectively, with an optimum irradiation concentration of $C_{\rm opt}$ = 1000 and an optimum current concentration of $F_{\rm opt}$ = 3.2. $p_{\rm min}$ was reached after 30 years before the concentrator and the BOS were replaced (see Fig. 2).

Device types 3 and 4, i.e. concentrating devices using Si-based PV cells, benefited from their low PV cell price and showed lowest hydrogen prices at only low irradiation concentration ($C_{\text{opt}} = 7$ for device 3, and $C_{\text{opt}} = 9$ for device 4) and low current concentration $(F_{\rm opt} = 0.12 \text{ and } 0.74 \text{ for device types } 3 \text{ and } 4)$. Current concentration was beneficial for the cost while not yet limiting performance. The decreased performance of our chosen Si-based cell with increasing C and their low V_{oc} limits the acceptable irradiation concentration, therefore the relative price of the PEMEC was larger compared to device types 1 and 2 (see Fig. 4) where F was still relatively large. If a maximization of the efficiency is targeted instead, the current concentration should be weak, i.e. F values should be maximized (F = 10, which was the maximum Finvestigated). The quality of the PEMEC was critical for device types 3 and 4 since hydrogen production was very sensitive to the small differences in the operating voltage as well as to degradation. Overall, the lower performance of these particular Si-based PV cells which we investigated did not compensate for their cost advantage, since p_{\min} (\$7.54 kg_{H₂}⁻¹ and \$13.2 kg_{H₂}⁻¹ for device types 3 and 4, respectively) was 3.7 to 6.6 times higher than p_{\min} of design types 1 and 2. The STH efficiency at the minimum price design was 3.8 to 6.4 times lower for device types 3 and 4

(STH = 2.4 and 1.4%, respectively) than for device types 1 and 2 (STH = 9% for both). This means that devices with an area of about 3.8 to 6.4 times larger are required for device types 3 and 4 to reach the same hydrogen production as device types 1 and 2.

 $p_{\rm min}$ was increased by 30% when comparing design type 1 to design type 9, and design type 2 to design type 10, *i.e.* when current concentration was suppressed (F=1). The optimal concentration for minimized cost, $C_{\rm opt}$, decreased from 1000 (for device types 1 and 2) to 400 (for device type 9) and 380 (for device types 10) due to increased overpotentials in the PEMEC at smaller F. Consequently, the cost contribution of the PV cells to the overall device increased for device types 9 and 10 compared to device types 1 and 2.

Both p_{\min} and C_{opt} showed a moderate increase in device 11 (for which F=1) compared with device 3 (18.5% increase in p_{\min} , and an increase from 7 to 28 for C_{opt}) and remained almost unchanged for device 12 (for which F=1) compared with device 4 (0.3% increase in p_{\min} , and an increase from 9 to 11 for C_{opt}) since F_{opt} was already close to 1 for device types 4, as visible in Fig. 3.

For device types using no solar irradiation concentration and high-performing III–V PV cells (device types 5, 6, 13, and 14), the impact of the very high PV price was not compensated for by concentration, resulting in very high hydrogen prices (above \$200 ${\rm kg_{H_2}}^{-1}$), making these devices not practical for scalable hydrogen production. Non-concentrating device types using Si-based PV cells with F=1, device types 15 and 16, also resulted in unpractically high hydrogen prices (\$35.7 ${\rm kg_{H_2}}^{-1}$ and \$18.3 ${\rm kg_{H_2}}^{-1}$), stemming from low hydrogen production and the unmitigated high price of the PEMEC.

For device types using no solar irradiation concentration and Si-based PV cells (device types 7, 8, 15, and 16), not only the PV performance but also the PEMEC choice became important for performance and cost. This explains why F_{opt} (0.013 for device 7, and 0.066 for devices 8) was very sensitive to the choice of the PEMEC. Device types 7 and 8 had the potential to produce hydrogen at a price that was lower than their corresponding concentrating devices (p_{\min} = \$4 kg_{H₂}⁻¹ for device 7, and p_{\min} = \$7.9 kg_{H₂}⁻¹ for device 8), with a moderate sensitivity to $F(\pm 5\% \text{ of }$ variation in hydrogen price when changing F by a factor of two, see Fig. S2, ESI†). However, F values had to be kept low (F < 1) to avoid high PEMEC prices at the expense of reduced performance as the high current densities in the PEMEC led to larger overpotentials and consequently lower device operating currents. Consequently, minimum hydrogen prices were reached for low STH efficiencies (2.6% for device 7, and 1.4% for device 8) meaning that device areas of 3.5 to 6.4 times larger would be required to obtain equally affordable hydrogen production at a comparable magnitude as for device 1 and 2. This technical limitation resulted from the low V_{oc} of the Si-based PV cell and a corresponding low flexibility in dealing with overpotentials in the PEMEC or losses in the PV fill factor resulting from high current densities, long operational times, or degradation.

Simultaneous consideration of performance, cost, and sustainability

The ranges of operating time-averaged STH efficiency (assumed 30 years operation), hydrogen price (*p* for 30 years operation,

usually p_{\min}), and energy demand (e for 30 years operation, usually e_{\min}) spanned by the different device types for varying Cand F are shown in Fig. 5 for a set of device types.

Device type 1 predicted the existence of a single design choice (the Pareto point) which simultaneously maximized performance and minimized cost and energy demand. This design used irradiation and current concentration ($C \neq 1$ and $F \neq 1$). Generally, irradiation concentration increases the cost competitiveness of designs, while low C designs show higher efficiency and lower energy demand. Moderate current dilution ($F \approx 1$ –1.4) results in lowest cost design, but has no clear advantage for efficiency or energy demand, i.e. depending highly on the irradiation concentration (see Fig. S4, ESI†).

The operating time-averaged efficiencies, STH, for device types 1 were 9% for a wide range of C values and for F > 3(for larger C).

Device type 9, using irradiation concentration but no current concentration (F = 1), didn't predict a global optimum (a Pareto point) but rather a range of designs (Pareto front) with high efficiency, low cost and energy demand indicating a requirement for a strategic choice between highest performance, lowest cost, and lowest manufacturing energy demand. The Pareto front was below the Pareto point of device 1 indicating inferior indicator characteristics. Design types 5 and 13, not using a concentrator, showed significantly higher cost and higher as well as lower STH efficiency than device type 1. Note that the

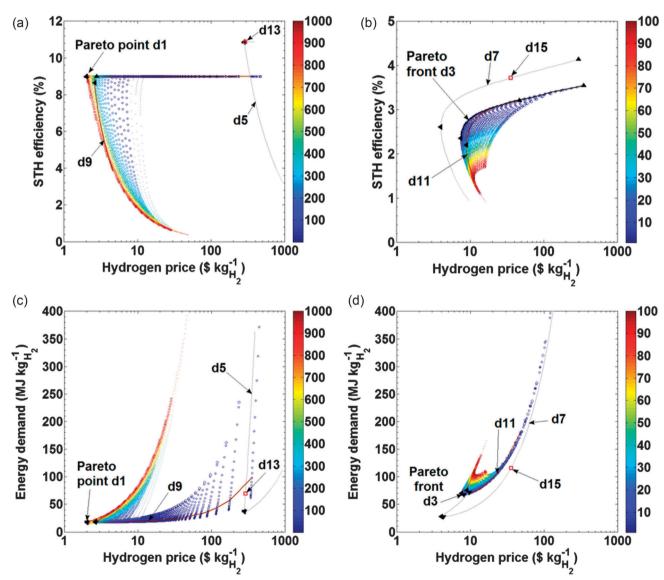


Fig. 5 Operating time-averaged efficiency (a and b), and energy demand (c and d) as a function of hydrogen price, for (a and c) device types 1, 5 (gray line, C = 1), 9 (brown line, F = 1), and 13 (red rectangle, C = F = 1), and (b and d) device types 3, 7 (gray line, C = 1), 11 (brown line, F = 1), and 15 (red rectangle, C = F = 1). Device types j are indicated as dj in the plots. Point colors indicate the irradiation concentration (indicated by the color bar), C, for device types 1 and 3; point sizes indicate the log_{10} of the current concentration, F, for device types 1 and 3 (colored in Fig. S4, ESI†). Pareto front or point of device types 1 and 3 are indicated by the black line. Black triangles indicate the design for highest operational time-averaged STH efficiency (A), lowest price (\blacktriangleleft), and lowest energy demand (\blacktriangledown).

STH efficiencies of device type 5 shown in Fig. 5 were obtained for $0.01 \le F \le 10$, while the efficiency data for device type 1 is shown only for $0.1 \le F \le 10$. The cost inferiority of device types 5 and 13 compared to device types 1 and 9, stems from the use of the extremely expensive PV cells, for which the absence of concentrator and tracking cost couldn't compensate.

Device types 2, 6, 10, and 14, showed the same efficiency-cost-sustainability behavior as designs 1, 5, 9, and 13, even though they utilized low cost catalysts. Performance and cost were insignificantly influenced by this change as the PEMEC cost was negligible (see Fig. 4) while the performance stayed about the same. A recent demonstration of a non-concentrated III-V based cell using Ni-based catalysts operating with an efficiency of 8.6%¹³ could be seen as a demonstration of device design type 14, a type which proves unpractical unless the device is further developed to operate at high irradiation concentrations.

Device type 3 predicted the existence of a range of designs (Pareto front) with high efficiency, low cost and low energy demand with no single best design. Rather, compromises between efficiency, cost, and sustainability were required. Generally, low to no irradiation concentration is required for best performance. No clear trends of C on the price and energy demand are observed. Current concentration (F < 1) clearly benefits all design choices in terms of cost and energy demand, but has no clear trend on efficiency. Device type 11, using irradiation concentration but no current concentration (F = 1), predicted also a Pareto front. This front lay below the front of device type 3 indicating inferior indicator characteristics. Design types 7 and 15, not using a concentrator, showed a potential cost and STH efficiency advantage, and generally lower energy demand compared to device types 3 and 11. Current concentration (F < 1) clearly benefits the cost of non-concentrating device types, device type 15 is far away from the optimum. The cost and energy input advantage for some designs results from the absence of concentrator and tracker related cost and energy expenses, and generally from the low Si-based PV cell price.

Fig. 6 and 7 show the limiting points of the Pareto fronts and points of all device designs investigated, *i.e.* sensitivity of each design with optimized operational time-averaged efficiency towards cost-minimized designs and sensitivity of each design with optimized energy demand towards cost-minimized designs. The linear connection between the limiting points is introduced for better readability but doesn't represent the actual behavior of the Pareto front, as evident from Fig. 5.

Before we discuss the range of optimized devices for the various device types, we will introduce several additional device types. This was motivated by the observation that the choice of the Si-based cells was not well suited for this application, *i.e.* the low fill factor and low open circuit potential of the chosen Si-based cell were limiting for the overall performance and competitiveness of this device types (types 3, 4, 7, 8, 11, 12, 15, and 16). We examined the potential improvement of these device types by introducing new Si-based device types (indicated by superscript *) with an assumed higher $V_{\rm oc}$ of 2.5 V,

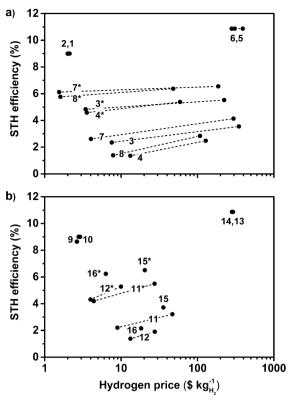


Fig. 6 Minimum hydrogen price (p_{min} at maximum operating time) and operating time-averaged STH efficiency of various device types for the most efficient and most profitable design for (a) a non-constrained F, and (b) F = 1. Device types with superscript * indicate PV cells with an artificially increased V_{oc} of 2.5 V. Devices using III–V PV cells (concentrating: 1, 2, 9, 10, and non-concentrating: 5, 6, 13, 14) show the highest STH efficiency. Upgraded non-concentrating devices using Si-based cells (types 7* and 8*) show the lowest hydrogen price.

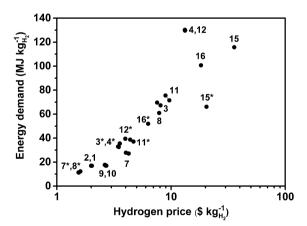


Fig. 7 Minimum hydrogen price and minimum energy demand for the most profitable and most sustainable designs (for 1 to 16 and devices 7*, 8*, 15*, and 16* with increased $V_{\rm oc}$). Non concentrating devices using III–V PV cells (device types 5, 6, 13, and 14) are not represented due to their high $p_{\rm min}$ (between 280 \$ kgH₂ $^{-1}$ and 292 \$ kgH₂ $^{-1}$) despite their relatively low $e_{\rm min}$ (between 36 MJ kgH₂ $^{-1}$ and 69 MJ kgH₂ $^{-1}$). Upgraded nonconcentrating devices using Si-based cells (device types 7* and 8*) show the lowest hydrogen price and the lowest energy demand, followed by concentrating devices using III–V PV cells (device types 1, 2, 9, and 10).

instead of 1.9 V. Parameter sweeps in the V_{oc} of the Si-based PV cells were done (see Fig. S3, ESI \dagger), which predicted that a $V_{\rm oc}$ of at least 2.3 to 2.5 V was required to provide improved performance, cost, and sustainability characteristics. The assumed increase in V_{oc} suggested the use of quadruple junction PV cells, 52,53 or designed triple junction cells for high concentrations, both with a $V_{\rm oc}$ of at least 2.5 V assuming no additional cost.

Fig. 6 shows that minimum prices of \$1.55 $kg_{H_0}^{-1}$ and \$1.6 $kg_{H_2}^{-1}$ can be reached for non-concentrating Si-based devices 7* and 8* with operational time-averaged STH efficiencies reaching 6.1% and 5.8% at this minimum price design for about an order of magnitude smaller area of PEMEC than for devices 7 and 8 ($F_{\text{opt}} = 0.0043$ for device 7*, and 0.011 for device 8*). An increase in V_{oc} was also advantageous for Si-based device types using concentrated irradiation: minimal prices of \$3.34 kg $_{\rm H_2}^{-1}$ for device 3* (with $C_{\rm opt}$ = 6 and $F_{\rm opt}$ = 0.032), and \$3.56 kg $_{\rm H_2}^{-1}$ for device 4* (with $C_{\rm opt}$ = 5 and $F_{\rm opt}$ = 0.08) were observed, and maximal operational time-averaged STH efficiencies of 5.5% for device 3*, and 5.4% for devices 4* were achieved. This corresponded to a decrease of 2.3 (for 3*) and 3.7 (for 4*) fold in price, and an increase of 1.6 (for 3*) and 2.2 (for 4*) fold in efficiency when compared with device 3 and 4. The additional costs arising from a raise in the V_{oc} of these PV cells were, however, not included in the calculations.

The comparison shown in Fig. 6 predicts that device types 1 and 2, and device types 7* and 8* are among the cheapest device types investigated. Irradiation concentration greatly benefits high-cost and high-performance PV cells, while its cost (including tracking) isn't compensated for in low-cost PV cells which additionally show reduced performance at large C. Current management $(F \neq 1)$ is essential for low-cost design types through either dilution (F > 1) to ensure that mass transport limitations are not present (critical for devices with large C) or through concentration (F < 1) to reduce the cost contribution of the usually expensive PEMEC (critical for devices with low *C*).

For concentrating devices using III-V PV cells (except devices 5, 6, 9, and 10) the most profitable design was also the most efficient one, i.e. the Pareto front collapsed into a point. Several combinations of C and F for these device types exhibited the same efficiency because the maximum current provided by the PV cell could be reached for these various combinations. This was not the case for device types using Si-based cells where the two design strategies (minimum price or maximum operational time-averaged efficiency) led to very different hydrogen prices. This was especially pronounced for design types with varying F (the price difference between the two design strategies ranged from \$46.5 kg_{H2}⁻¹ for device 8* and \$340.6 kg $_{\rm H_2}^{-1}$ for device 3). However, the difference in STH efficiency remained relatively low for these devices (maximum 1.5 point difference for all devices considered). This predicts that profitable designs might provide a better compromise than efficient designs.

Non-concentrating device types using Si-based PV cells with F = 1, device types 15 and 16, also resulted in unpractically high hydrogen prices (\$35.7 kg $_{\rm H_2}^{-1}$ and \$18.3 kg $_{\rm H_2}^{-1}$), even with an increased $V_{\rm oc}$, devices 15* and 16* (\$20.4 kg $_{\rm H_2}^{-1}$ and \$6.3 kg $_{\rm H_2}^{-1}$).

The sustainability, i.e. energy demand, and corresponding minimum hydrogen price calculated (see Fig. 7 with the corresponding Pareto points or limiting points of the Pareto front), suggest that hypothetical device types 7* and 8* are the most sustainable (11.4 MJ $kg_{H_2}^{-1}$ for F = 0.0062, and 12.3 MJ $kg_{H_2}^{-1}$ for $F = F_{\text{opt}} = 0.011$, respectively) followed by device types 1 and 2 (16.9 MJ kg_{H₂}⁻¹ for $F = F_{\text{opt}} = 3.2$, $C = C_{\text{opt}} = 1000$ and C = 980, respectively). Most of the devices showed a price per energy requirement of the same order of magnitude (\$0.12 MJ⁻¹ or \$0.43 kW h⁻¹ \pm 17%), about 4.3 times a typical electricity price in the USA for a common energy mix.‡ Device type 15 showed a higher price per energy requirement (\$0.3 MJ⁻¹ or \$1.1 kW h⁻¹), 11 times the electricity price in the USA for a common energy mix. 49 Devices 5, 6, 13 and 14 showed higher values (above \$4 MJ⁻¹), suffering from the very high price of III-V based PV cells, even though they show relatively good sustainability (e_{\min} between 36 MJ kg_{H,}⁻¹ and 69 MJ kg_{H,}⁻¹).

The estimated range of obtained price per unit energy requirement provides a better conversion factor when switching from sustainability to economic studies of such devices, which up to now have used typical electricity prices for a common energy mix, therefore underestimating the price by about one order of magnitude. Most devices reach e_{\min} and p_{\min} for very similar choices of C and F, i.e. variations within $\pm 22\%$, exceptions made for devices 3 and 7 with $\pm 108\%$ in F, and for devices 11 and 11* with $\pm 50\%$ variation in C.

After comparing the devices, it appears that concentrating devices using III-V PV cells are the best trade-off between profitability, sustainability and size. These device types also provide one single Pareto point, providing a design choice simultaneously optimizing efficiency, cost and sustainability. Their high STH efficiency implies lower space or aerial requirements than other devices for a given hydrogen production. Their optimum design lies at a high C value (C = 1000), meaning that price and energy requirement depend on the concentrator and the BOS without being impacted significantly by the price and design of the PV cell and the PEMEC. Consequently, PV and PEMEC can be chosen for maximized performance neglecting cost or energy requirement.

Non-concentrated and concentrated devices using Si-based cells can achieve low hydrogen prices and good sustainability, however for a STH efficiency 4.5 to 8.9 times lower than devices 1 and 2, implying a required solar collection area 4.5 to 8.9 times greater to obtain the same hydrogen production. These devices could compete with concentrating devices using III-V based PV cells when using Si-based PV cells with a higher $V_{\rm oc}$, of at least 2.5 V (see Fig. S3, ESI†), implying the use of additional junctions or targeted cell designs.

Degradation and replacement time

The replacement time of components is approached when the device has reached a certain threshold of degradation. For Si-based PV cells, a 20% efficiency decline has been considered a failure,²⁹ but running a device with a PV cell with a 70%

[‡] http://www.eia.gov/electricity/monthly/epm_table_grapher.cfm?t = epmt_5_6_a

degraded efficiency may have less impact on hydrogen price than replacing it. We examined the relationships between degradation rate and hydrogen price to determine the optimum replacement time of components for the best-performing concentrating device type (device type 2 using III-V based PV cells and low cost electrocatalyst) and non-concentrating device types (device types 7 and 7* using Si-based PV cells and high quality electrocatalysts) in their most cost-effective C and F design configuration (i.e. at C_{opt} and F_{opt}). We used the previously defined optimistic, reference, and conservative degradation cases since the degradation effects for solar water splitting devices caused by concentrated irradiation, temperature, or light intermittency is sparsely reported: Concentrator degradation was a linear decrease in efficiency of 0.65% loss per year for all degradation cases (optimistic, reference, conservative); PV short circuit current degradation ranged between 0.17% year⁻¹ (optimistic) to 2.5% year⁻¹ (conservative), with 0.7% year⁻¹ as reference case; and PEMEC voltage degradation ranged between 1 μ V h⁻¹ (optimistic) to 14 μ V h⁻¹ (conservative), with 6 μ V h⁻¹ as reference case.

We found that at low degradation rates, p_{\min} was mostly dependent on the PV cell replacement time (see Fig. 8 and Fig. S5, ESI†) for device types 2 and 7*, while it slightly increased for longer PEMEC replacement times for device type 7.

The impact of the PEMEC replacement time on the hydrogen price was negligible for device types 2 and 7* since the PV cell dominated the cost of the device. In this optimistic degradation configuration, the price of the components prevailed over their performance and the device worked at a sufficient performance for a long time, allowing the PV cell and the PEMEC to be replaced over their recommended operational times of 30 and 10 years, respectively. This explains why operational timeaveraged STH efficiencies for cost-optimized designs did not change with replacement time (0.102 \pm 1.2%, 0.0625 \pm 3.3% and $0.0728 \pm 2.8\%$ for device types 2, 7 and 7*, respectively, see Fig. S6, ESI†). This conclusion didn't hold in the instance of high degradation rates, where the price and performance of the components defined the optimum replacement times. For device type 2, the PV cell and PEMEC needed to be replaced every 15 and 5 years, respectively. For device type 7, the PEMEC needed to be replaced almost every year to prevent device operation at a very low hydrogen production (see Fig. S6, ESI†). For device type 7^* an interesting case arose: p_{\min} presented a local minimum (\$2.88 kg_{H2}⁻¹) for a PV cell replacement time of 15 years and PEMEC replacement time of 1 year, and showed an even lower value (\$2.43 kg_{H2} ⁻¹) for a PV cell replacement time of 30 years and PEMEC replacement time of 4 years. In the first case, the replacement of components increases the performance

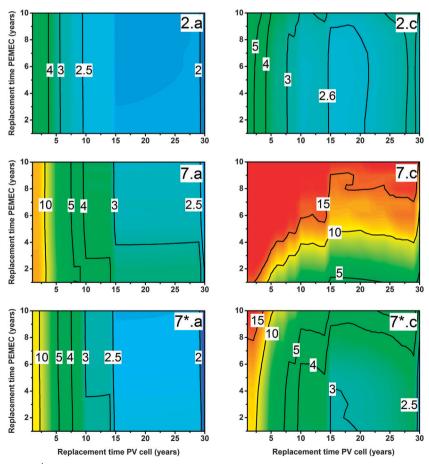


Fig. 8 Hydrogen price p_{min} (\$ kg $_{H_2}^{-1}$) as a function of PV cell and PEMEC replacement time for cost-optimized devices 2 (concentrating/III–V based PV cells/low-cost catalysts), 7, and 7* (non-concentrating/Si-based PV cells/high-quality catalysts) for optimistic (a) and conservative (c) degradation rates.

			Hydroge	n price	;	Energy demand						
Device	2		7		7*		2		7		7*	
Min. Ref. Value	2 \$ kg _{H2} ⁻¹		4 \$ kg _{H2} ⁻¹		1.5 \$ kg _{H2} ⁻¹		16.8 MJ kg _{H2} ⁻¹		27.1 MJ kg _{H2} ⁻¹		11.3 MJ kg _{H2} ⁻¹	
Conc. or BOS	9.2%		5.9%		6.5%		12.9%		6.1%		6.4%	
PV Cell	3.4%		11.2%		12.4%				12.6%		13.2%	
PEMEC			3%		1.1%				1.3%			
Irradiance	1	13.1%		14.4%		15.4%		13.1%		14.4%		15.4%

Fig. 9 Sensitivity analysis of +20% variation of parameter values on p_{min} (\$ kg $_{H_2}^{-1}$) and e_{min} (MJ kg $_{H_2}^{-1}$) for cost-optimized device types 2 (concentrating/ III-V based PV cells/low-cost catalysts), 7, and 7* (non-concentrating/Si-based PV cells/high-quality catalysts). Empty entries correspond to a variation of less than 0.5%

of the device, while in the second case, the longer replacement time alleviates the resulting additional cost.

In general, we observe that for low degradation rates p_{\min} was lower at the optimal choice of component replacement times, with less sensitivity for device type 2 ($\$1.77 \text{ kg}_{H_2}^{-1}$ for low degradation rates, and $\$2.53~{\rm kg_{H_2}}^{-1}$ for high degradation rates) compared with device types 7 ($\$1.74 \text{ kg}_{\text{H}_2}^{-1}$ for low, and $\$4.37 \text{ kg}_{\text{H}_2}^{-1}$ for high rates) and 7* ($\$1.31 \text{ kg}_{\text{H}_2}^{-1}$ for low, and $\$2.43 \text{ kg}_{\text{H}_2}^{-1}$ for high rates). For a given degradation case, the ratio between maximum and minimum p_{min} obtained at different component replacement time combinations was also less sensitive to replacement time in device type 2 (2.8 and 2.4 for low and high degradation rates, respectively) than for device types 7 (7.1 and 17.1) and 7* (7.8 and 8.1).

The degradation analysis shows that there is a need for a beforehand accurate knowledge of the degradation rates before deciding on the replacement time of components. Additionally, an informed decision can then be made to select component replacement times e.g. with maximized hydrogen prices. This is especially pronounced for non-concentrating devices using the low-cost Si-based PV cells of this study (device type 7).

Sensitivity analysis for price, energy requirements and effective irradiation

The sensitivity of p_{\min} and e_{\min} for selected component prices and energy demand as well as incoming irradiation is presented in Fig. 9 for device types 2, 7, and 7* at their cost and energy demand optimized designs. p_{\min} and e_{\min} displayed a four times higher PV cell requirement sensitivity for device types 7 and 7* compared to device type 2, despite the much higher energy requirements and cost of III-V based PV cells. The p_{\min} and e_{\min} of device type 2 showed more sensitivity with respect to the concentrator and the BOS because of a high operating C (about 1/3 more sensitivity for device type 2 compared to device types 7 and 7*). Device types 2, 7, and 7* were not sensitive to the PEMEC requirements, mainly because of a high C and F ratios. The $V_{\rm oc}$ improvement of the Si-based PV cells utilized in this study (device types 7* compared to 7) is generally more favorable to performance, cost, energy, and operational time behavior. Nevertheless, the V_{oc} improvement was profitable only if it implied less than a 160% cost and energy requirement increase compared to the initial PV cell. A comfortable 750% increase in

energy requirement in the PV cell was required for device type 7* to remain more sustainable than device type 2, but less than a 30% PV price increase was required to produce cheaper hydrogen than device 2. Device types using concentrated solar irradiation illustrate that a focus on reduction in cost and energy requirement of the concentrator and the BOS is most important. Price and energy demand showed a similar sensitivity to irradiation (and by extension to optical efficiency of the concentrator or of the PV cell) with a decrease of 0.65% to 0.77% per 1% increase in irradiation. This implies that the location of the device will strongly determine its outputs and that optical efficiency is a major parameter to be improved.

The sensitivity analysis allowed for a quantification of the influence of the error margin in the collected data on the efficiency, cost, and energy demand results for a given device design type. Assuming a $\pm 33\%$ uncertainty on the cost and energy requirement of concentrators and PV cells (see Table 2) and a $\pm 15\%$ uncertainty on the collected data,³⁸ the calculated variations in p_{min} and e_{\min} were 33% and 34% for device type 2, and 53% and 52% for device types 7 and 7*.

4. Conclusions

This study provides holistic and quantified design guidelines for hydrogen production through integrated photo-electrochemical water-splitting approaches, with the option to use irradiation concentration and current concentration. The results compared several design types (types 1-16, 3*, 4*, 7*, 8*, 11*, 12*, 15*, and 16*) and design choices (varying irradiation concentration, C, and varying current concentration, F) using four indicators: operation timeaveraged STH efficiency, hydrogen cost, device manufacture and operation energy demand per mass unit of hydrogen produced, and operational time. The device types were built based on different material choices, which are examples and not preferential to, or selected to be optimal for our particular application.

The operational dependence of performance, cost, and energy demand showed two trends. Due to the increase of the cumulative quantity of produced hydrogen, the cost and energy demand decreased with increasing operational time and was usually lowest right before the majority of the components were replaced. On the other hand, due to the degradation of the various components, the device performance decreased with

operating time, with partial performance restoration when a few components were intermediately replaced. These trends were generally observed for all device types investigated. Nevertheless, if the performance of the device intermediately dropped to almost zero due to the failure of one component (high degradation rate or low performance components), a local minima for cost was observed a few years before the device operational lifetime was reached. This resulted from almost no increase in the cumulative generated hydrogen, while cost for tracking continued to increase. Generally, one can conclude that the operating time before complete device replacement should be as short as possible if maximum efficiency is the targeted indicator, while the replacement should be pushed towards the end of the device operational time if cost and energy demand minimization is targeted. For each device type there are, therefore, three possible strategic choices: (i) design for minimum hydrogen price, (ii) design for minimum energy demand, and (iii) design for maximized performance over the operational time. The latter strategy is unpractical and instead an optimization of the operational time-averaged performance should be approached.

Applying irradiation and current concentration to the design of the various concentrating device types provided significant advantages to all three indicators (performance, cost, and energy input). Thanks to this, hydrogen prices were significantly decreased and cost-competitive design solutions for device types utilizing very expensive components (e.g. the III-V based PV cells) were observed. As the performance didn't significantly decrease with increasing irradiation concentration for the III-V based PV cells modeled, the optimal irradiation concentration was reached for the largest investigated concentration C = 1000. For the Si-based device types modeled, on the other hand, an optimal irradiation (in the range of C = 10) and current concentration existed for which the cost was minimized. This concentration combination reduced the mass of expensive materials while still ensuring non-limiting losses in the PV cell and electrolyzer. Nevertheless, non-concentrating device types using Si-based PV cell showed a cost, efficiency, and energy demand advantage compared to the low concentrated case. This resulted from the requirement on direct irradiation of concentrating devices reducing the actual use of the total solar irradiation (composed of direct and diffuse fractions), the reduced performance of Si-based cells at higher concentrations, and the additional cost for a concentrator, all of which was not compensated by the lower device area and cost with increasing concentration. Generally, it was observed that in order to be commercially competitive and sustainable with minimum land use, concentrating devices must use PV cells which can produce high currents at large potentials and withstand high concentrations (up to C = 1000) without losing efficiency.

A holistic approach to photo-electrochemical water splitting devices requires a simultaneous optimization of cost, energy input, and performance over a long operational time. We observed two distinct behaviors for the various device types investigated: (i) device types which exhibited a design allowing for a global optimum (a Pareto point) simultaneously maximizing performance,

while minimizing cost and energy input, and (ii) device types which exhibited a range of partially optimal designs (a Pareto front) with high efficiency, low cost, and low energy demand, indicating a tradeoff and the requirement for a strategic choice between highest performance, lowest cost, and lowest energy demand. Device types using high-performing and high-cost PV cells and allowing for an adaptation of C and F (device types 1 and 2) were device types which exhibited a Pareto point, i.e. provided a design which allowed for the simultaneous optimization of performance, cost, and energy demand. These designs perform best at high irradiation concentrations, and also showed the lowest variation in characteristics with respect to component replacement time and degradation rate. Hydrogen price and energy requirements were not affected by the current concentration, F, as long as F > 2. A decrease of F below 1 was detrimental for the hydrogen cost due to the occurrence of mass transport limitations at these high current densities (since C was already large). Further improvement in the performance characteristics of these device types can be achieved through the enhancements of the concentrator's optical efficiency without additional cost or energy requirement, and by lowering the cost of the balance of system (BOS). Generally, the cost-optimized devices were obtained for large C, therefore the PEMEC didn't play a significant role in the price or energy requirements. Consequently, best-performing catalysts could be used no matter their cost.

Device types using low-performing and low cost PV cells (types 3 and 4) were device types which exhibited a Pareto front. In other words, a set of device designs existed which optimized performance, cost, and energy input, but not simultaneously, therefore requiring a tradeoff between the indicators. Nonconcentrating devices using our modeled Si-based cells showed the potential for higher profitability and sustainability than concentrating devices. The latter mainly resulted from the inability of concentrating devices to collect and absorb diffuse solar irradiation as well as the inability of compensating the performance losses at high concentrations by the reduction in device cost. These device types were highly sensitive to the degradation rate, replacement time choices, and variation in component price and energy requirement. In order to compete with device types 1 and 2, the $V_{\rm oc}$ of the PV cell needed to be increased to higher values of around 2.5 V, with either no, or a tightly controlled increase in cost, potentially achievable with a Si-based PV technology with better performance such as crystalline Si.

The quantification of the influence of component degradation on the performance allows the suggestion of best practice for device operational time and component replacement. The results indicated that a detailed knowledge of the component degradation rates beforehand was required in order to determine the best replacement time for the various components. Generally, two competing effects were observed: (i) reduced performance with increasing replacement time, and (ii) reduced cost and energy demand due to the increase in cumulative hydrogen produced. For the low degradation scenarios investigated, PV replacement time was critical for the cost, while PEMEC replacement was insignificant. This was especially true

for PV cell choices with significantly higher V_{oc} than the operating potential. For high degradation scenarios, the PEMEC replacement time became more critical, especially for device types using PV cells with low $V_{\rm oc}$. For the device types with high performing PV cells (types 2 and 7*), local cost minima were observed, usually around a PEMEC replacement time of 5-6 years and a PV cell replacement of 15-16 years.

The methodology presented provides a pathway for a holistic assessment of photo-electrochemical water splitting device types and design. Obviously the concrete outcomes depend strongly on the material performance properties, and the cost and energy input assumed. We aim at providing a web-based version of the modeling framework presented here§ allowing for the assessment of, and guidance for specific device types, designs, and ideas, of which there are currently many existing in the community. A sensitivity study was conducted to get a general idea of the importance of various assumptions on the results. Optimized cost and energy demand displayed a four times higher PV cell requirement sensitivity for device types 7 and 7* compared to device type 2. The cost and energy demand sensitivity of the latter device type was highest with respect to the concentrator and BOS cost and energy input, as this device type operated at high irradiation concentration.

Since hydrogen compression, hydrogen storage, the end-oflife of a device, and all operational costs were not included in this study, and because of the uncertainties associated with the cost estimation of emerging technologies, the actual hydrogen prices and energy demands will likely vary. Accurate values for these devices will only be obtained once they are built and installed at a specific location with a specific irradiation, energy mix, and within a specific economic and policy environment. Furthermore, requirements associated with the installation, operation, maintenance, and overall management of a large scale H₂ production plant were considered out of scope. Consequently, this study cannot comment on economy of scale. This study allows for comparison of systems on a device level (including their immediate peripherals) in order to compare different types of material selections under different designs. Price and energy requirement used in this study were reported per unit area of the device, implying that the results are valid for a variable device size.

Our study provides trends and guidelines for the meaningful focus of research concerning scalable hydrogen production technologies. The proposed framework allows for a quantifiable comparison between different device types, device designs, material choices, operating choices, and stability, and provides sensitivities of the obtained values to variations in the input data (performance, cost, energy demand, and degradation values) caused by fluctuations in the market and with technological improvement.

The findings presented here show that only the combined consideration of efficiency, price, sustainability, and operational time can provide a holistic approach for the design of integrated photo-electrochemical devices, and provide guidelines for a scalable, sustainable, and competitive solar hydrogen production for the future.

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[§] Web-based version is currently under development and will be available on http://lrese.epfl.ch/research.

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Holistic design guidelines for solar hydrogen production by photo-electrochemical routes

(Electronic Supplementary Information)

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Model development

The performance of the PEC device was assessed by modeling the performance of the photoabsorbers (i.e. PV) and the membrane-separated electrocatalysts (i.e. PEMEC) by equivalent circuits. The operating current was determined by ensuring simultaneous fulfillment of the current-voltage characteristics of the photoabsorbers and the membrane-separated electrocatalysts.¹

II.1 Performance model of the photovoltaics

Two different PV cells were considered: i) III-V cells (GaInP/GaAs) representing high-performing and high-cost cells, and ii) Si-based cells representing low-cost, low performance cells. Isothermal operation at T = 298 K was assumed for both PV cells at all irradiation concentrations. The AM1.5 spectrum distribution was considered as the incoming non-concentrated irradiation spectrum and was weighed with the 2093 kWh m⁻² yr⁻¹ yearly-averaged direct normal irradiation (DNI) of Sevilla in southern Spain for tracked concentrating devices while the 1872 kWh m⁻² yr⁻¹ global horizontal irradiation (GHI) was used for untracked non-concentrating devices. This represents a 77% and 69%, respectively, of the 2716 kWh m⁻² yr⁻¹ total yearly-averaged irradiation at this location.² The performance of the multi-junction GaInP/GaAs PV was assumed constant for concentrations ranging from 1 to 1000 suns, with a fill factor of 85%, close to an ideal behavior.³ The open-circuit characteristics of GaInP/GaAs tandem cells (band gaps 1.9 eV and 1.43 eV)⁴ were the Shockley-Queisser limits.⁵ Current-voltage behavior of GaInP/GaAs PV cells was modeled by the ideal diode equation:

$$i = i_{sc} - i_{rec} \left(e^{F_F V/RT} - 1 \right). \tag{i}$$

The dark current i_{rec} was calculated as:

$$i_{\rm rec} = i_{\rm sc} e^{-F_{\rm F} V_{\rm oc}/RT}. \tag{ii}$$

The maximum STH efficiency (based on the i_{sc} and the total irradiation of 2716 kWh m⁻² yr⁻¹) was 12 % considering the efficiency of the concentrator (which is initially 85 %). The maximum STH efficiency for the non-concentrated case was 12.6 %.

The short current behavior of a-Si/µc-Si/µc-Si PV cells was obtained by a phenomenological correlation combining two sets of reported experimental values.^{6,7} The resulting current-voltage characteristics were given as (with $\phi_{ref} = 223 \text{ W m}^{-2}$):

$$\frac{i}{i_{\text{sc}}} = 1 + f - f \left(1 + \frac{1}{f} \right)^{\frac{V}{V_{\text{oc}}}},$$

$$f = 10^{-5} \frac{c\phi}{\phi_{\text{ref}}} \left(\frac{c\phi}{\phi_{\text{ref}}} + 1 \right).$$
(iii.b)

$$f = 10^{-5} \frac{\ell \phi}{\phi_{\text{ref}}} \left(\frac{\ell \phi}{\phi_{\text{ref}}} + 1\right). \tag{iii.b}$$

The maximum STH efficiency of this cell was 7.3% considering the efficiency of the concentrator. The maximum STH efficiency for the non-concentrated case was 7.6% considering that there is no sun tracking.

This correlation was experimentally validated for C between 1 and 20 and was assumed valid for the Crange considered in this study. Concentration, C, and irradiation, Φ , dependence of short circuit currents
and open circuit voltages for all cells were estimated neglecting the effect of series and shunt
resistances,⁸

$$i_{\rm sc}(\mathcal{C},\phi) = \mathcal{C}\,\eta_{\rm c}(L)\,\eta_{\rm PV}(L)\,i_{\rm sc}(1,\phi_0)\frac{\phi}{\phi_0},\tag{iv}$$

$$V_{\rm oc}(C,\phi) = V_{\rm oc}(1,\phi_0) + \frac{RT}{F_{\rm F}} ln\left(\frac{C\phi}{\phi_0}\right),\tag{v}$$

where η_c and η_{PV} are the operating time-dependent efficiencies of the concentrator and of the PV cell. Φ_0 is the irradiation value at which the reference short circuit currents and open circuit voltage are calculated or measured (9 mA cm⁻² and 1.83 V for Si-based cells, 14.6 mA cm⁻² and 2.7 V for III-V cells, both at $\Phi_0 = 1000 \text{ W m}^{-2}$).

II.2 Performance model of the PEM electrolyzer

The operating voltage is the sum of the thermodynamic equilibrium potential required for the electrolysis of water at standard conditions ($V_0 = 1.23 \text{ V}$) and current-dependent overpotentials generated by chemical reactions, mass and charge transport, and degradation:

$$V = V_{o} + \eta_{ohm} + \eta_{act} + \eta_{conc} + \eta_{degrad}.$$
 (vi)

The activation overpotential, η_{act} , is the sum of anodic and cathodic activation overpotentials and were modeled using Tafel correlations:

$$\eta_{\rm act} = \frac{RT}{2F_{\rm F}\alpha_{\rm a}} ln\left(1 + \frac{j}{j_{\rm 0,a}}\right) + \frac{RT}{2F_{\rm F}\alpha_{\rm c}} ln\left(1 + \frac{j}{j_{\rm 0,c}}\right),\tag{vii}$$

with $j_{0,a}$ and $j_{0,c}$ being the anodic and cathodic exchange current densities, and $\alpha_a = 0.85$ and $\alpha_c = 1$ being the anodic and cathodic charge transfer coefficients. A reaction overpotential of 227 mV for the Pt/RuO₂-based PEMEC and of 348 mV for the Ni/Co₃O₄-based PEMEC is required at 10 mA cm⁻². Ohmic losses, η_{ohm} , in the Nafion membrane with the thickness of $e_m = 50 \mu m$ and conductivity of $\sigma = 10$ S m⁻¹ was modeled using:

$$\eta_{\text{ohm}} = \frac{j e_{\text{m}}}{\sigma}.$$
(viii)

Mass transport losses, η_{conc} , were modeled using the phenomenological equation from Kim et al.:¹⁰

$$\eta_{\rm conc} = ae^{bj}.$$

The phenomenological coefficients a = 0.01 V and $b = 5 \cdot 10^{-4}$ m² A⁻¹ were fitted to experimental results given by Dedigama et al..¹¹ Isothermal operation at T = 298 K was assumed for the PEMEC. η_{degrad} is the operating time-dependent degradation overpotential, effectively reducing the potential available for the PEMEC operation (see below for details).

II.3 Device operation

The resulting operating PV cell current density, i_{op} , and potential was obtained by iteratively estimating the current and potential simultaneously satisfying eqs. (i) to (ix). The hydrogen mass production was calculated as:

$$\dot{m}_{\rm H_2} = \frac{\eta_{\rm F} \, i_{\rm op} \, A_{\rm PV} M_{\rm H_2}}{2 F_{\rm F}},$$
 (x)

with the photoabsorber area A_{PV} , hydrogen molar mass $M_{H2} = 0.002$ kg mol⁻¹, and Faradaic efficiency $\eta_F = 1$. Typical current-potential performance characteristics for the two sets of PVs (Si-based and Gabased) and PEMECs are depicted in Figure S1.

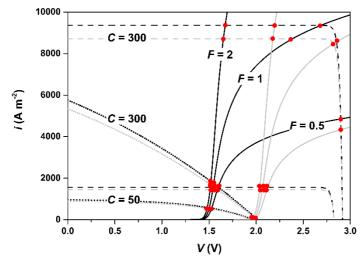


Figure S1. Typical current-voltage behavior of the device for varying C and F. The current is normalized by the area of the PV cell. The current density-voltage characteristic of the Ga-based cells (dashed lines) and the Si-based cells (dotted lines) are shown for C = 50 and 300. Pt is used as electrocatalysts in the PEMEC, for which current-voltage behavior for F = 0.5, 1, and 2 (solid lines) at initial operating time (black lines) or after 10 years operation (gray lines) is shown. At large C and small F, mass transport limitations in the PEMEC decrease the operating current. Operating voltages and currents are given at the intersection of the PEMEC and PV cell curves and are indicated by red dots.

Life cycle energy and cost inventory

The energy demand per unit area has been assessed in previous work using reported data on single components, BOS not considered, and is summarized in Table 2 in the main paper text. The price per unit area of components was assessed using the same method, focusing on the requirements for the manufacturing process only and excluding transportation, assembly, maintenance, and recycling of the system.

The prices of parabolic troughs and solar heliostats for tower plants have been reported to be \$295 m⁻² and \$164 m⁻². 12,13 The price of parabolic dishes and 2-axis Fresnel concentrators have been reported to be \$125 m⁻² and \$172 m⁻² for the concentrator and \$51 m⁻² and \$30 m⁻² for the tracker. 14,15 The price of Fresnel-lens-based concentrators has been reported per unit of power: The price of the concentrating module and of the tracker of the 22.7% efficient Flatcon device adds up to \$0.75 W_p⁻¹ resulting in a cost of \$170 m⁻². 16 The price of a 18.3 kW and 267 m² AMONIX 7700 module was reported to be \$2.9 W⁻¹, resulting in \$198.4 m⁻². 17 Excluding the price of the III-V cell (adjusted with the area ratio C = 550) and the BOS, the price of a module and tracker for this device accounted for \$138 m⁻². The energy demand per unit area for the manufacturing of the concentrating module was assessed in previous studies from

reported LCAs on concentrated solar devices.^{1,18–21} In this study, we averaged all the reported energy demand values to 2251 MJ m⁻² and the cost values to \$201 m⁻² for the concentrator.

For concentrating devices, yearly energy demand for tracking was estimated to be $30.9 \text{ MJ} (\text{yr}^{-1}\text{m}^{-2})^1$ and the price $$0.9 \text{ yr}^{-1}\text{m}^{-2}$ was obtained using the electricity cost in the U.S. and a typical energy intensity of the electricity production. <math>^{22}$

The price of silicon based cells has been reported to be within \$90 m^{-2} to \$200 m^{-2} .^{23,24} The mean between these values was used. The price of III-V PV cells was reported to be between \$30 000 m^{-2} and \$100 000 m^{-2} .^{14,25} We considered the latter value from the detailed report of King et al.²³ as the most reliable and conservative case and we excluded the packaging price of \$2.5 cm⁻² which was not suited for our design, resulting in a \$75 000 m^{-2} price for III-V cells.

The price of PEMFC stacks has been reported to be within \$42 m⁻² to \$1000 m⁻² and resulted mostly from cost analyses on fuel cells for automotive applications. The two major causes for price variability were the platinum load on the electrodes and the production type. Price and energy demand for these PEMEC were adapted accordingly with data for electrode materials obtained from the ecoinvent database, knowing that the precious metals accounted for 30% and 40% of these cost and energy demand, respectively. The maximum price - \$1000 m⁻² - was chosen for the most expensive PEMEC (RuO₂ and Pt-based) and represented a conservative value. The price of the cheap PEMEC (Co₃O₄ and Ni-based) resulted in \$245 m⁻².

The price of the BOS for a generic irradiation concentration installation, its operation, maintenance, and financing was reported to be \$260 m⁻².²⁵ The price of the BOS for the Flatcon device was estimated to be 0.33 €Wp¹ resulting in a total price of \$74 m⁻².¹6 The sum of the energy demands of transformers, hydraulic drives, motor cables, controllers, anemometers, and sensors of the AMONIX 7700 was reported to be 550 MJ m⁻².²¹ The price of the BOS was also estimated between \$40 m⁻² and \$112 m⁻² for non-concentrating devices, and the energy demand of the BOS for non-concentrating devices was estimated as 550 MJ m⁻².²²²,³⁶ The reference area for the BOS was the concentrator area. The reported price for the BOS were averaged and resulted in \$137 m⁻² for concentrating devices, \$76 m⁻² for non-concentrating ones. These averages also accounted for slightly different BOS definitions in the various studies. The averaged BOS energy demand was 550 MJ m⁻² for non-concentrating and concentrating systems.

The water needed to for the electrochemical reaction and ensuring no electrode and membrane dry out was calculated to be 86 kg yr⁻¹m⁻² (per unit area of receiver, either PV cell or concentrator). The energy to produce distilled water was estimated experimentally to be 3.6 kJ kg⁻¹ by Moore et al., ³⁷ resulting in a power cost of 0.15 MJ yr⁻¹m⁻² (per unit area of concentrator) for the distilled water supply of the device. The price of the required water was assessed to be \$1.5·10⁻³ yr⁻¹ m⁻² using the price of electricity and the energy mix in the U.S.²²

Operating time, replacement, and degradation

The reference operating time, L_{ref} , of the device was assumed 30 years, with all components having a replacement time of 30 years, except for the PEMEC which had a replacement time of 10 years. The degradation of the optical efficiency of the concentrator was given as:

$$\eta_{\rm c} = \eta_{\rm c,0} - G(\dot{\eta}_{\rm c} L, L_{\rm conc}), \tag{xi}$$

$$\eta_{\text{PV}} = 1 - G(\dot{\eta}_{\text{PV}} L, L_{\text{conc}}), \tag{xii}$$

where $\eta_{c,0}$ is the initial efficiency (85%)¹ and $\dot{\eta}_c$ the degradation rate (0.65% yr⁻¹). The degradation of the PV cell short circuit current was given with a similar formula with degradation rates $\dot{\eta}_{PV}$ ranging from 0.17% yr⁻¹ to 2.5% yr⁻¹.^{3,8} The degradation overpotential was given as:

where $\dot{\eta}_{\rm C}$ is the voltage degradation rate (1 $\mu {\rm V}~{\rm h}^{\text{-1}}$ to 14 $\mu {\rm V}~{\rm h}^{\text{-1}}$). ^{39,40} G is a periodic function for every positive integer n defined as $G(\dot{\eta}_{\rm ref},L,L_{\rm ref})=\dot{\eta}_{\rm ref}(L-nL_{ref})$ for $nL_{\rm ref}< L<(n+1)L_{\rm ref}$. The performance of every device is therefore renewed after the component replacement took place.

Additional figures

The following figures provide additional information of optimum designs for different device types (Figures S2 and S4), the benefits of increasing the V_{oc} of Si-based PV cells (Figure S3), the minimum hydrogen price and STH efficiency sensitivity of device types 2, 7, and 7* to degradation and replacement time of components (Figures S5 and S6). Figure S7 provides hydrogen energy demand, hydrogen price, and STH efficiency for the most sustainable, the most profitable and the most efficient designs at their optimum operating times.

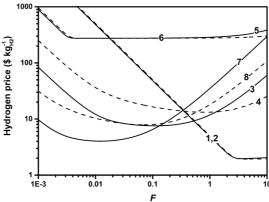


Figure S2. Hydrogen price as a function of current concentration, F, for devices 1 to 4 at C_{opt} , and for devices 5 to 8, at C = 1 using high quality (solid lines) or low cost electrocatalysts (dashed lines).

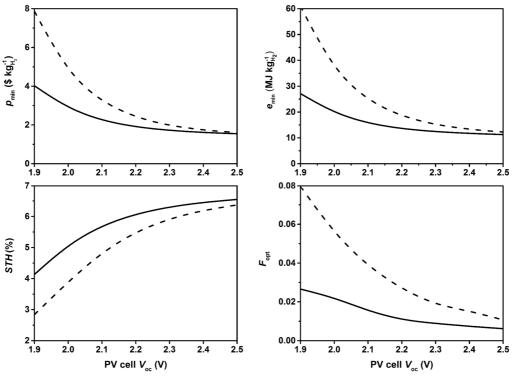


Figure S3. Evolution of p_{\min} , e_{\min} , STH_{\max} , and F_{opt} with the PV cell's V_{oc} of device 7 (solid line) and 8 (dashed line). Device types 7 and 8 with $V_{\text{oc}} = 2.5$ represent device types 7* and 8*.

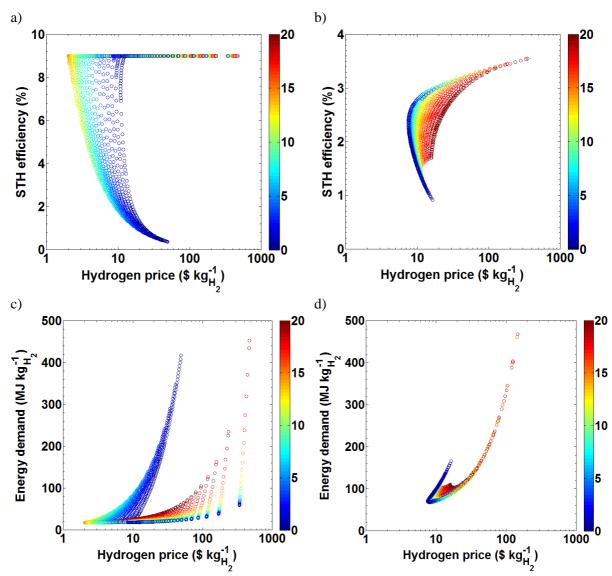


Figure S4. Operating time-averaged efficiency as a function of hydrogen price (a,b) and energy demand as a function of hydrogen price (c,d) for device types (a,c) 1 and (b,d) 3. The color of the points indicates a normalized current concentration ($[\log_{10}(F)+1]\cdot 10$).

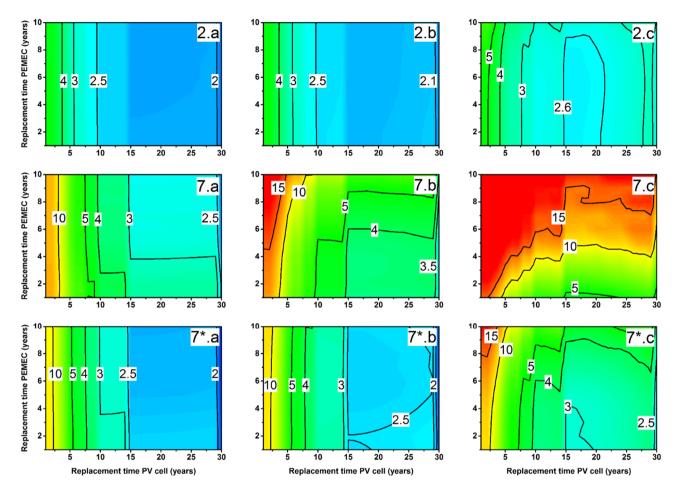


Figure S5. Hydrogen price p_{min} (in kg_{H2}^{-1}) as a function of replacement time of PV cells and PEMEC for cost-optimized devices 2, 7*, and 7, for (a) optimistic, (b) reference, and (c) conservative degradation rates.

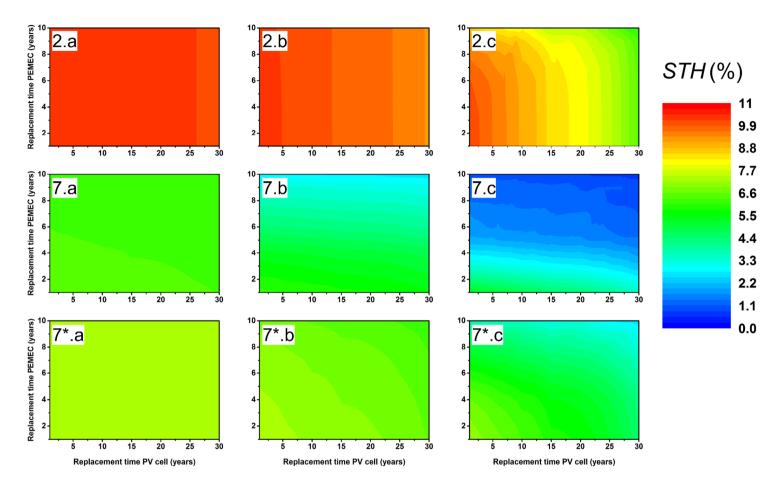


Figure S6. Operating time-averaged STH efficiency as a function of the replacement time of PV cells and PEMEC for cost-optimized devices 2, 7*, and 7, for (a) optimistic, (b) reference, and (c) conservative degradation rates.

	Strategy		Strategy				Strategy				Strategy				
DEVICE 1	Min e	Min p	Max STH	DEVICE 2	Min e	Min p	Max STH	DEVICE 3	Min e Min p Max STH		DEVICE 4	Min e	Min p	Max STH	
С	1000	1000	1000	С	980	1000	1000	С	6	7	1	С	7	9	1
F	3.2	3.2	10	F	3.2	3.2	10	F	0.25	0.12	10	F	0.74	0.74	10
e (MJ kg _{H2} ⁻¹)	16.9	16.9	17.2	e (MJ kg _{H2} ⁻¹)	16.9	16.9	17.1	e (MJ kg _{H2} ⁻¹)	67.3	69.6	1064.4	e (MJ kg _{H2} ⁻¹)	129.6	130.1	1089.8
$p \ (\$ kg_{H2}^{-1})$	2.0	2.0	2.1	$p \ (\$ \ kg_{H2}^{-1})$	2.0	2.0	2.0	$p \ (\$ \ kg_{H2}^{-1})$	8.1	7.5	348.1	$p \ (\$ \ kg_{H2}^{-1})$	13.2	13.2	128.3
STH (%)	9.0	9.0	9.0	STH (%)	9.0	9.0	9.0	STH (%)	2.6	2.4	3.5	STH (%)	1.4	1.4	2.5
DEVICE 5	Min e	Min p	Max STH	DEVICE 6	Min e	Min p	Max STH	DEVICE 7	Min e	Min p	Max STH	DEVICE 8	Min e	Min p	Max STH
F	0.1	0.1	10	F	0.1	0.1	10	F	0.027	0.013	10	F	0.066	0.066	10
e (MJ kg _{H2} ⁻¹)	37.2	37.2	363.3	e (MJ kg _{H2} ⁻¹)	36.2	36.2	264.5	e (MJ kg _{H2} ⁻¹)	27.1	27.8	882.5	e (MJ kg _{H2} -1)	61.0	61.0	905.8
$p \ (\$ kg_{H2}^{-1})$	280.8	280.8	391.4	$p \ (\$ \ kg_{H2}^{-1})$	280.0	280.0	307.1	$p \ (\$ \ kg_{H2}^{-1})$	4.3	4.0	295.9	$p \ (\$ \ kg_{H2}^{-1})$	7.9	7.9	107.8
STH (%)	10.9	10.9	10.9	STH (%)	10.9	10.9	10.9	STH (%)	2.9	2.6	4.1	STH (%)	1.4	1.4	2.8
DEVICE 9	Min e	Min p	Max STH	DEVICE 10	Min e	Min p	Max STH	DEVICE 11	Min e	Min p	Max STH	DEVICE 12	Min e	Min p	Max STH
С	340	400	310	С	320	380	270	С	14	28	1	С	9	11	1
$e (MJ kg_{H2}^{-1})$	17.0	17.7	17.0	e (MJ kg _{H2} ⁻¹)	17.0	17.7	17.0	$e (MJ kg_{H2}^{-1})$	71.5	75.6	180.6	e (MJ kg _{H2} -1)	129.7	130.2	244.2
$p \ (\$ kg_{H2}^{-1})$	2.7	2.6	2.8	$p \ (\$ kg_{H2}^{-1})$	2.7	2.6	2.9	$p \ (\$ \ kg_{H2}^{-1})$	9.7	8.9	46.9	$p \ (\$ \ kg_{H2}^{-1})$	13.3	13.2	27.6
STH (%)	9.0	8.6	9.0	STH (%)	9.0	8.6	9.0	STH (%)	2.5	2.2	3.2	STH (%)	1.4	1.4	1.9
DEVICE 13	Min e	Min p	Max STH	DEVICE 14	Min e	Min p	Max STH	DEVICE 15	Min e	Min p	Max STH	DEVICE 16	Min e	Min p	Max STH
e (MJ kg _{H2} ⁻¹)	69.1	69.1	69.1	e (MJ kg _{H2} ⁻¹)	58.5	58.5	58.5	e (MJ kg _{H2} ⁻¹)	115.8	115.8	115.8	e (MJ kg _{H2} -1)	100.7	100.7	100.7
$p \ (\$ kg_{H2}^{-1})$	291.6	291.6	291.6	$p \ (\$ \ kg_{H2}^{-1})$	282.6	282.6	282.6	$p \ (\$ \ kg_{H2}^{-1})$	35.7	35.7	35.7	$p \ (\$ \ kg_{H2}^{-1})$	18.3	18.3	18.3
STH (%)	10.9	10.9	10.9	STH (%)	10.9	10.9	10.9	STH (%)	3.7	3.7	3.7	STH (%)	2.2	2.2	2.2
DEVICE 3*	Min e	Min p	Max STH	DEVICE 4*	Min e	Min p	Max STH	DEVICE 7*	Min e	Min p	Max STH	DEVICE 8*	Min e	Min p	Max STH
С	5	6	1	С	5	5	1	С	1	1	1	С	1	1	1
F	0.046	0.032	10	F	0.08	0.08	10	F	0.0062	0.0043	10	F	0.011	0.011	10
$e (MJ kg_{H2}^{-1})$	32.4	32.6	683.7	$e (MJ kg_{H2}^{-1})$	35.4	35.4	502.3	$e (MJ kg_{H2}^{-1})$	11.3	11.4	557.1	e (MJ kg _{H2} ⁻¹)	12.3	12.3	404.1
$p \ (\$ \ kg_{H2}^{-1})$	3.4	3.3	223.6	$p \ (\$ \ kg_{H2}^{-1})$	3.6	3.6	59.1	$p \ (\$ \ kg_{H2}^{-1})$	1.6	1.5	186.8	$p \ (\$ \ kg_{H2}^{-1})$	1.6	1.6	48.1
STH (%)	5.0	4.9	5.5	STH (%)	4.6	4.6	5.4	STH (%)	6.2	6.1	6.6	STH (%)	5.8	5.8	6.4
DEVICE 11*	Min e	Min p	Max STH	DEVICE 12*	Min e	Min p	Max STH	DEVICE 15*	Min e	Min p	Max STH	DEVICE 16*	Min e	Min p	Max STH
С	19	38	1	С	14	16	1	С	1	1	1	С	1	1	1
e (MJ kg _{H2} ⁻¹)	37.1	38.7	105.6	e (MJ kg _{H2} ⁻¹)	39.4	39.5	88.1	e (MJ kg _{H2} ⁻¹)	66.2	66.2		e (MJ kg _{H2} ⁻¹)	51.9	51.9	51.9
$p \ (\$ \ kg_{H2}^{-1})$	4.7	4.4	27.4	$p \ (\$ \ kg_{H2}^{-1})$	4.0	4.0	10.0	$p \ (\$ \ kg_{H2}^{-1})$	20.4	20.4	20.4	$p \ (\$ \ kg_{H2}^{-1})$	6.3	6.3	6.3
STH (%)	4.7	4.2	5.5	STH (%)	4.4	4.3	5.3	STH (%)	6.5	6.5	6.5	STH (%)	6.2	6.2	6.2

Figure S7. Irradiation concentration, C, current concentration, F, hydrogen energy requirements, e, hydrogen price, p, and operating time-averaged STH, for the most sustainable (Min e), the most profitable (Min p), and the most efficient (Max STH, averaged over 30 years operational time) designs of device types 1 to 16 and devices 3^* , 4^* , 7^* , 8^* , 11^* , 12^* 15^* and 16^* . Minimum p and e are reached for operating time between 27 and 30 years operational time. Grey color indicates a constrained C or F.

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