

INT 144/88

PROGRAMME ISTART3  
C o u r a n t d ' a c c r o c h a g e d ' u n g y r o t r o n  
t r a v a i l l a n t e n m o d e T E m p 1

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Juillet 88

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MIT 140 GHz gyrotron ( $TE_{03}$ )	
42 GHz gyrotron ( $TE_{02}$ )	
CRPP 8 GHz gyrotron ( $TE_{01}$ )	
CRPP 8 GHz gyrotron ( $TE_{02}$ , 2 <sup>ème</sup> harmonique)	

### Appendices

- A) Fichier de sortie du programme
- B) Listage du programme (sur demande)

### 1. BUT DU PROGRAMME ISTART3

Dessiner le courant d'accrochage en fonction du champ magnétique statique  $B_0$ , pour différents modes TE.

### 2. MODELE ET EQUATIONS UTILISEES

Le calcul analytique est basé sur les hypothèses suivantes:

Champ électrique dans la cavité cylindrique [1]:

$$\underline{E} = (E_r \hat{r} + E_\phi \hat{\phi}) e^{i(\omega t + \psi)} \quad \text{avec:}$$

$$\begin{cases} E_r = i \frac{m}{k_\perp r} E_0 f(z) J_m(k_\perp r) e^{-im\phi} \\ E_\phi = E_0 f(z) J'_m(k_\perp r) e^{-im\phi} \end{cases}$$

A un instant donné, le champ électrique physiquement mesurable est la partie réelle de  $\underline{E}$ .

$$k_\perp = \frac{\gamma_{mp}}{a} \quad \gamma_{mp}: p^{\text{ième}} \text{ zéro non nul de } J'_m(x)$$

$a$  = rayon de la cavité

Le champ  $E$  a un profil supposé gaussien selon  $z$ , l'axe du faisceau d'électrons:

$$f(z) = \exp\left[-\left(\frac{2z}{L}\right)^2\right] \quad \begin{array}{l} L = \text{longueur d'interaction} \\ 1.201 \cdot \text{FWHM de } f(z) \end{array}$$

Le faisceau électronique est caractérisé par sa tension  $V_0$ , son anisotropie  $\alpha = \beta_\perp / \beta_\parallel$ , son rayon  $R_e$ .

La longueur d'interaction normalisée est définie par:  $\mu = \pi \frac{\beta_\perp^2}{\beta_\parallel} \frac{L}{\lambda}$

Pour une bonne efficacité dans le régime non-linéaire (soft excitation region), il faut prendre  $\mu \simeq 9$  (cf Fig.3 de ref [1]).

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[1] Generalized Nonlinear Harmonic Gyrotron Theory,  
B.G. Danly and R.J. Temkin, PFC, MIT, April 85.

Le "detuning" normalisé est défini par

$$\Delta = \frac{2}{\beta_{\perp}^2} \left( 1 - \frac{n \Omega_0}{\gamma_0 \omega} \right) \quad \text{avec} \quad \Omega_0 = \frac{e B_0}{m_e} \quad ; \quad \gamma_0 = 1 + \frac{e V_0}{m_e c^2}$$

$$\text{d'où} \quad B_0 = \frac{m_e}{n \cdot e} \gamma_0 \omega \left( 1 - \frac{\beta_{\perp}^2}{2} \Delta \right) \quad \beta_{\parallel} = \sqrt{\frac{1 - \gamma_0^{-2}}{1 + \alpha^2}} \quad ; \quad \beta_{\perp} = \alpha \beta_{\parallel}$$

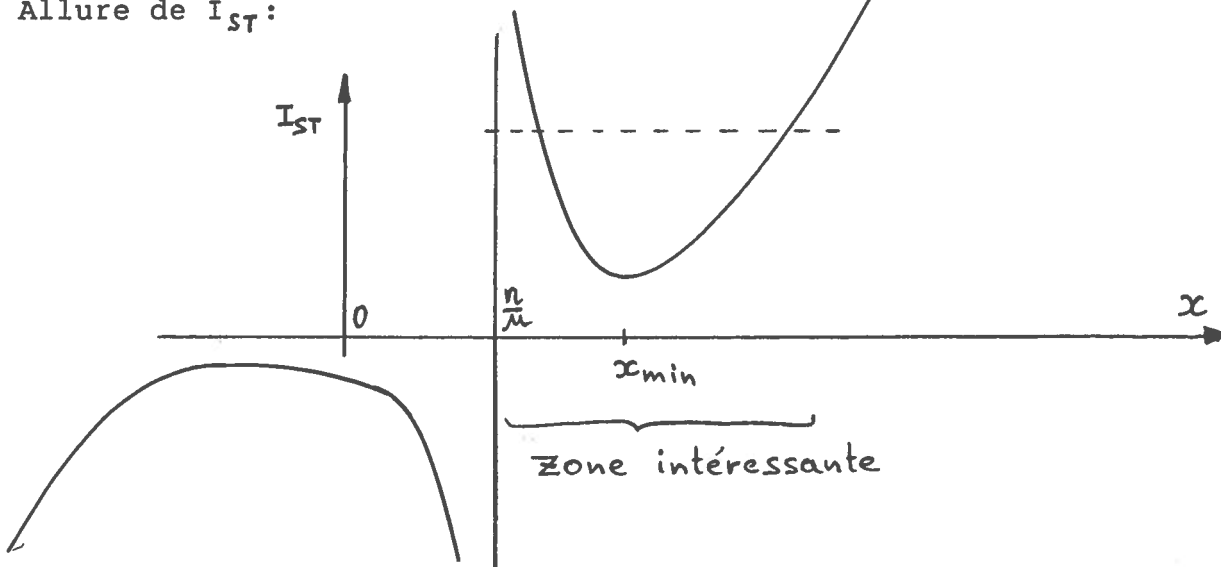
$n = n^{\circ}$  de l'harmonique: 1, 2...

Le courant d'accrochage normalisé est alors donné par

$$I_{ST}(\Delta, \mu) = \frac{4}{\pi \mu^2} \cdot \frac{e^{2x^2}}{\mu x - n} \quad \text{avec} \quad x = \frac{\mu \Delta}{4}$$

$$\text{Minimum:} \quad x_{\min} = \frac{1}{2} \left[ \frac{n}{\mu} + \sqrt{\frac{n^2}{\mu^2} + 1} \right]$$

Allure de  $I_{ST}$ :



Le courant normalisé est relié au courant en Ampères via:

$$I = \left( \frac{2}{\pi} \right)^{\frac{5}{2}} \frac{e}{\epsilon_0 m_e c^3} \frac{Q_{mp} I_A}{\gamma_0} \beta_{\perp}^{2n-6} \left( \frac{\lambda}{L} \right) \left( \frac{n^n}{2^n n!} \right)^2 \frac{J_{m \pm n}^2(k_{\perp} R_e)}{(\gamma_{mp}^2 - m^2) J_m^2(\gamma_{mp})}$$

$Q_{mp}$  = facteur de qualité du mode  $TE_{mp1}$

$J_{m \pm n}$  : le signe dépend de la polarisation du mode ( $\pm i m \phi$ ).  
Donc pour  $m \neq 0$ , il y aura 2 courbes  $I_{ST}(B_0)$ .

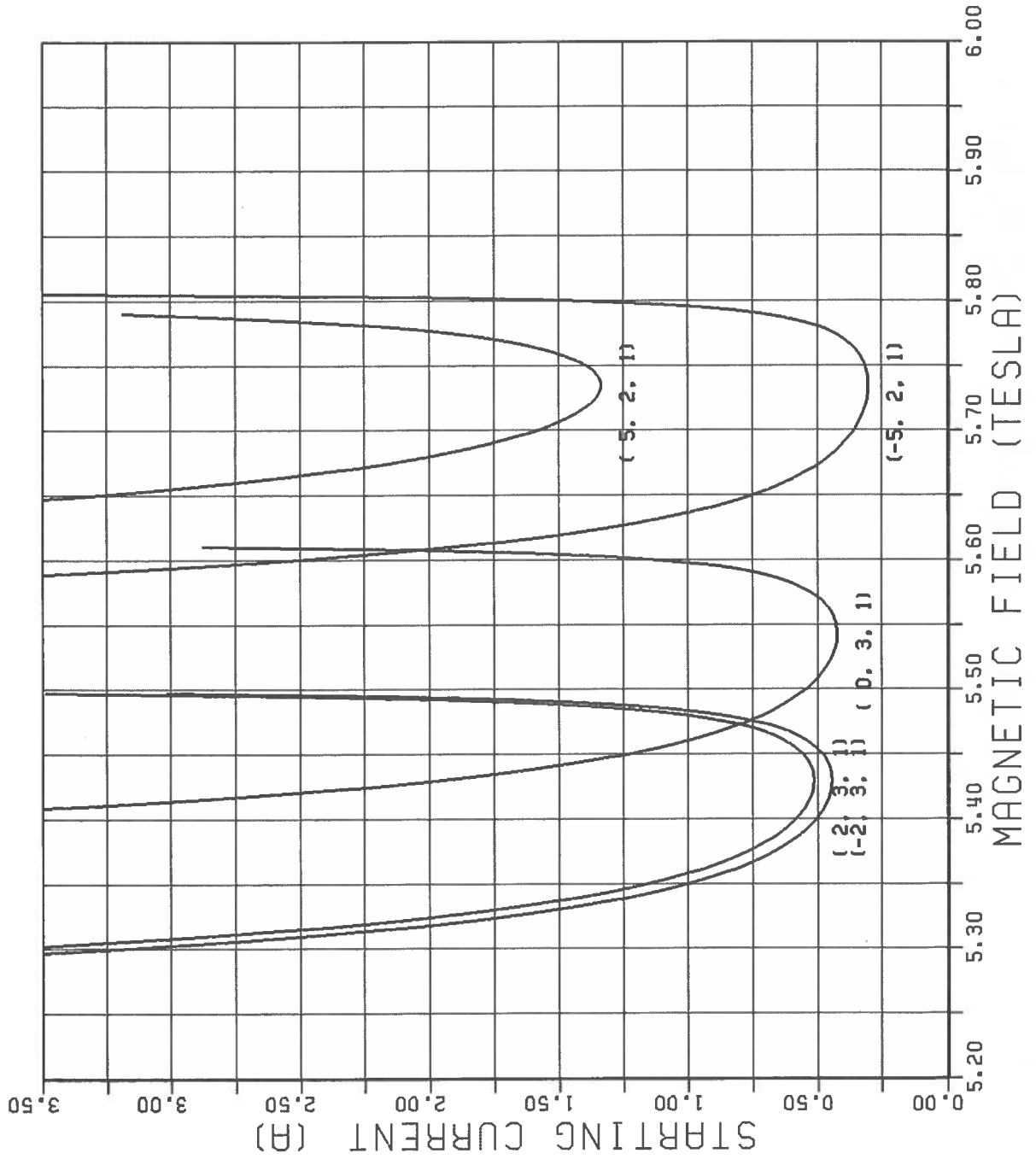
$\lambda$  = longueur d'onde de l'onde e.m. dans le vide



MIT 140 GHz Gyrotron

CRPP - 88/07/09. 10.59.90.  
GYROTRON PROJECT

STARTING CURRENT VERSUS STATIC MAGNETIC FIELD PROGRAM ISTART3

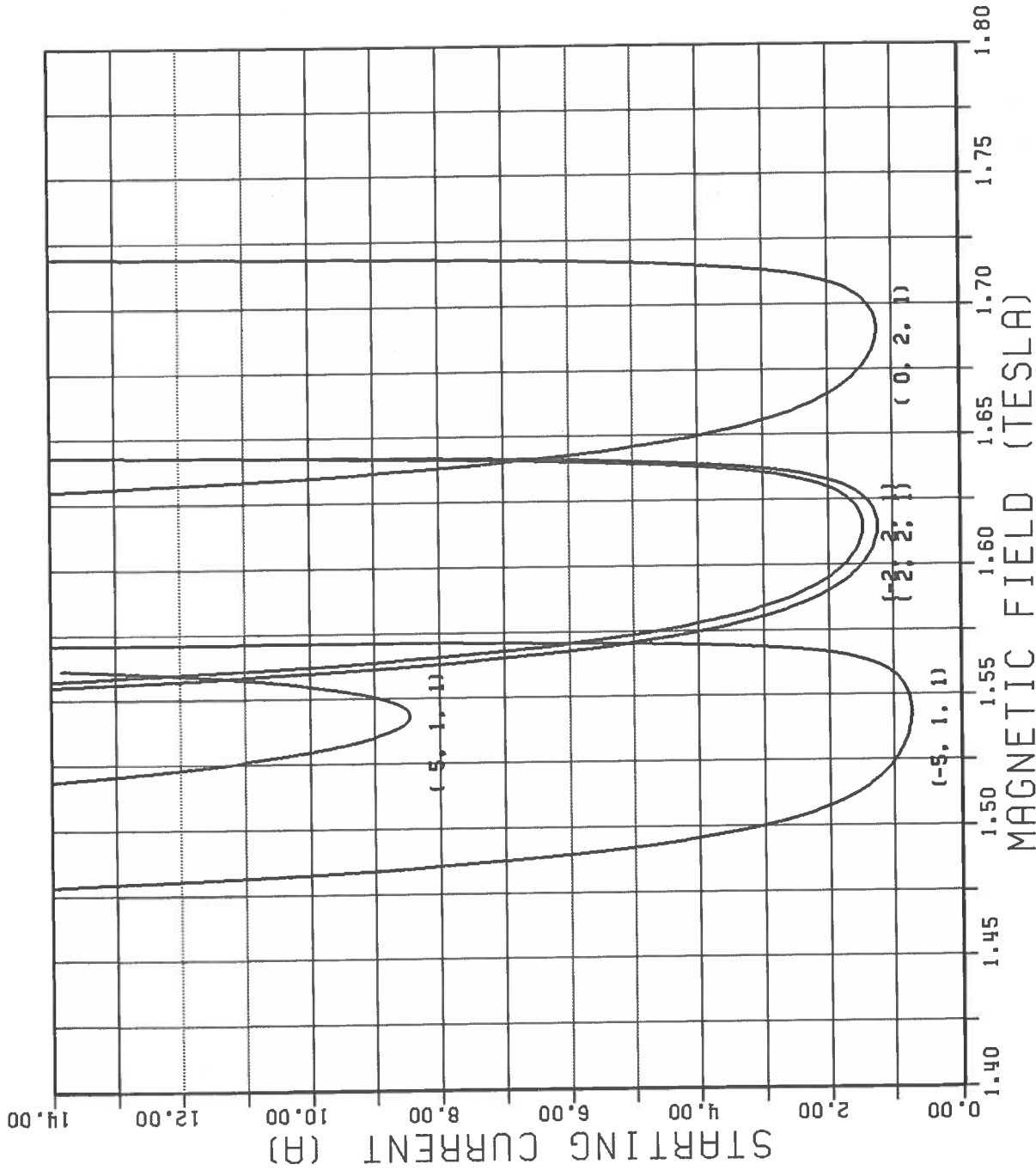


RESONATOR RADIUS: 3.47 MM  
 GAMMA: 1.1272  
 ALPHA: 1.5000  
 BEAM VOLTAGE: 65.00 KV  
 ANNULAR BEAM RADIUS: 1.82 MM  
 HARMONIC #: 1

MODE	L [MM]	Q	FREQUENCY [GHZ]
TE (0, 3, 1)	12.0	1450.	139.888
(2, 3, 1)	12.0	1400.	137.083
(5, 2, 1)	12.0	1300.	144.651

42 GHz Gyrotron  
=====

STARTING CURRENT VERSUS STATIC MAGNETIC FIELD PROGRAM ISTART3



CAPP - 88/07/04. 14.30.25.  
GYROTRON PROJECT

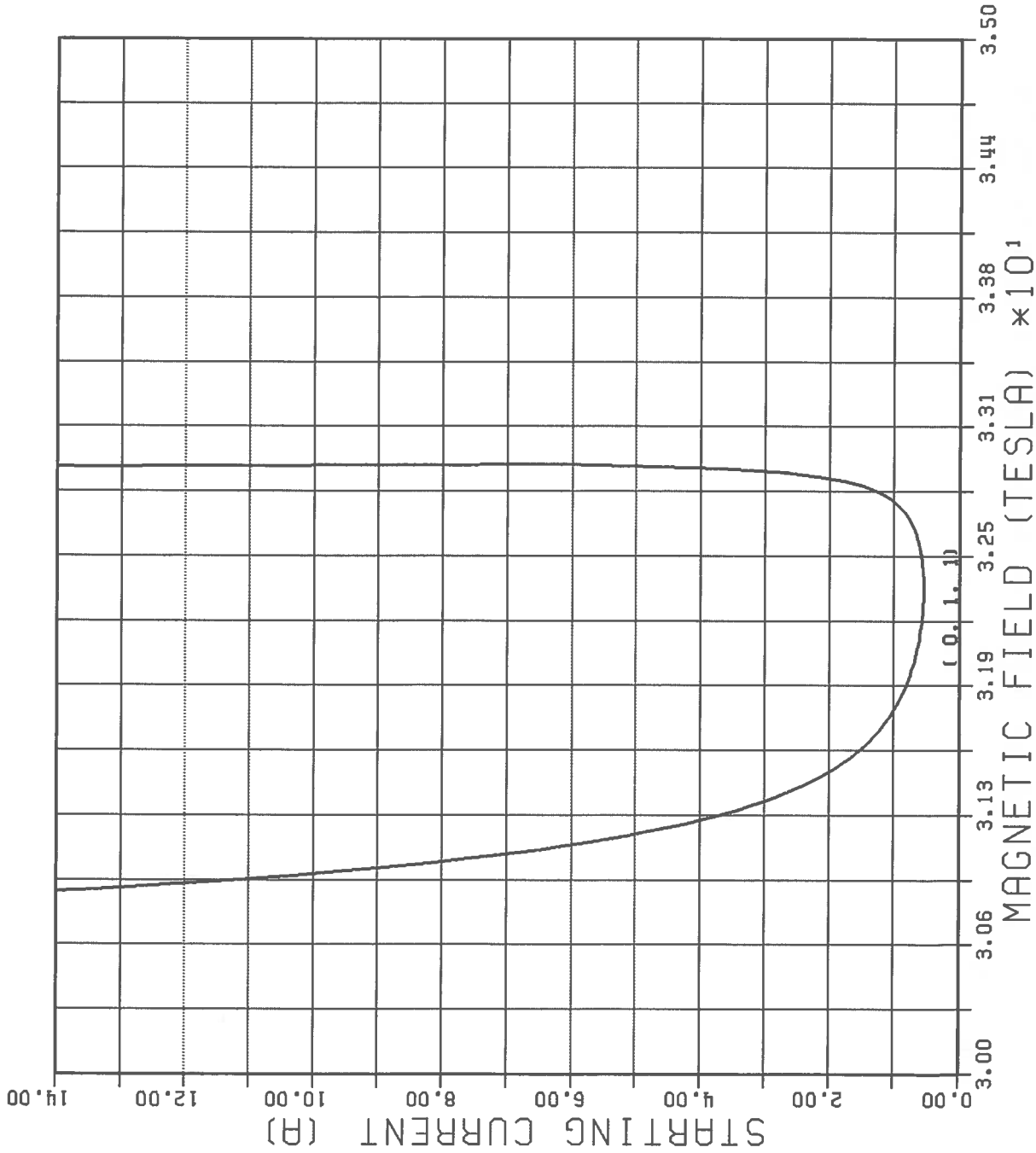
RESONATOR RADIUS: 8.00 MM  
 GAMMA: 1.1566  
 ALPHA: 1.5000  
 BEAM VOLTAGE: 80.00 KV  
 ANNULAR BEAM RADIUS: 6.00 MM  
 HARMONIC #: 1

MODE	Q	FREQUENCY [GHZ]
TE (0, 2, 1)	618.	41.842
TE (2, 2, 1)	556.	39.997
TE (5, 1, 1)	503.	38.264

8 GHz Gyrotron

=====

STARTING CURRENT VERSUS STATIC MAGNETIC FIELD PROGRAM ISTART3



CRPP - 88/07/05. 08.46.34.  
GYROTRON PROJECT

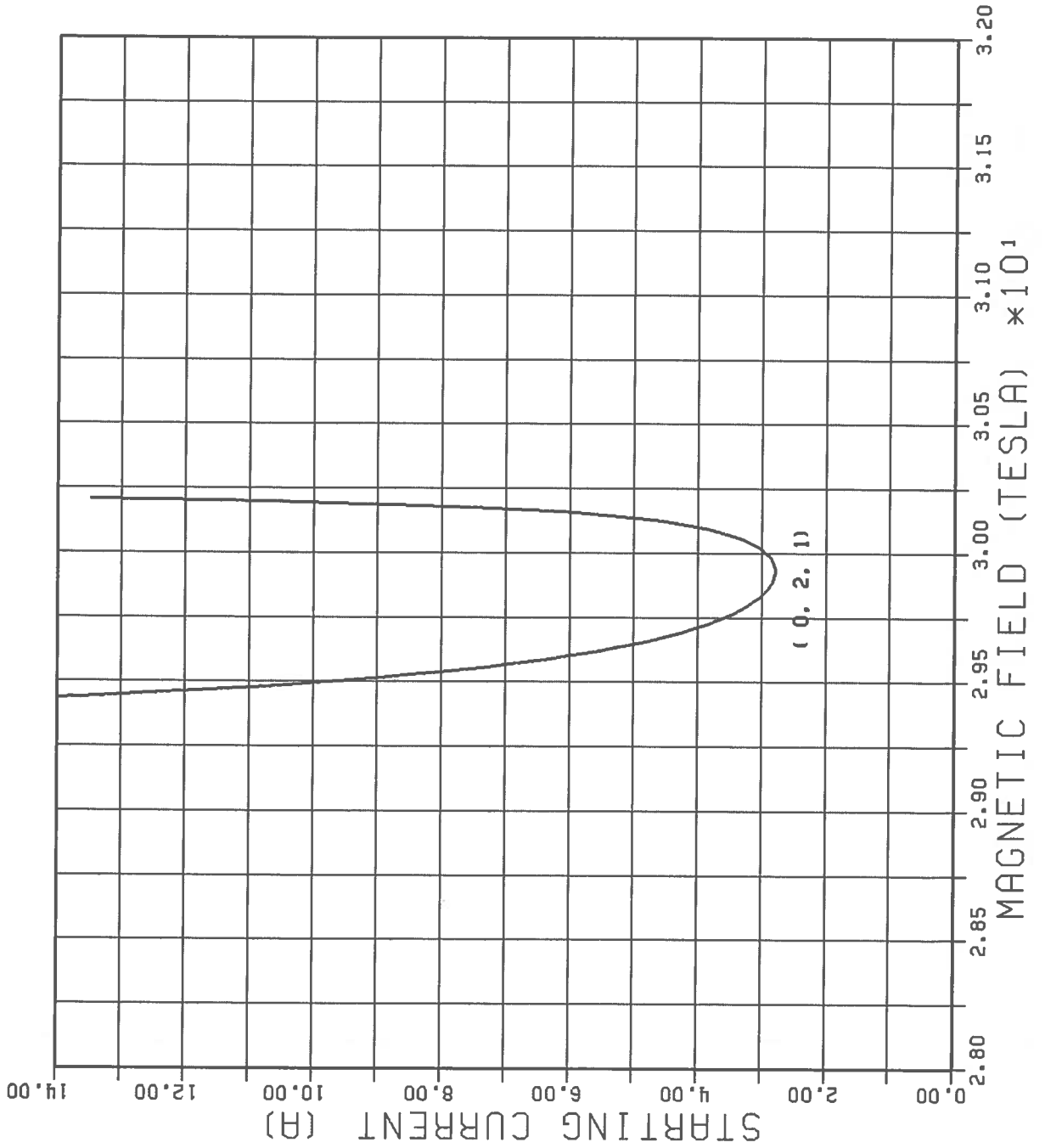
RESONATOR RADIUS: 22.80 MM  
 GAMMA: 1.1566  
 ALPHA: 1.8900  
 BEAM VOLTAGE: 80.00 KV  
 ANNULAR BEAM RADIUS: 11.18 MM  
 HARMONIC #: 1  
 MODE Q FREQUENCY  
 TE 227. 8.019  
 ( 0, 1, 1)



8 GHz Gyrotron

CRPP - 88/07/05. 09.00.47.  
GYROTRON PROJECT

STARTING CURRENT VERSUS STATIC MAGNETIC FIELD PROGRAM ISTART3



RESONATOR RADIUS: 22.80 MM  
 GAMMA: 1.1566  
 ALPHA: 1.8900  
 BEAM VOLTAGE: 80.00 KV  
 ANNULAR BEAM RADIUS: 11.18 MM  
 HARMONIC #: 2

MODE	Q	FREQUENCY [GHz]
TE (0, 2, 1)	200.	14.681

## APPENDICE A

Sortie des résultats (Fichier de sortie)

Pour tourner le programme SUR CYBER (NOS)

```
GET, ISTART3/UN=AP1.  
FTN5, I=ISTART3, L=0, ANSI=0.  
LIBRARY, MAPP5.  
LGO, IST140, OUTPUT.  
RASTER.  
ROUTE, GLDX.
```

PROGRAM ISTART3      88/07/11. 10.17.21.  
=====

A1

ZERDES OF DERIVATIVES OF BESSEL FUNCTIONS

J'( 0, 5)	=	16.47063005	ITER =	4
J'( 0, 4)	=	13.32369194	ITER =	4
J'( 0, 3)	=	10.17346814	ITER =	3
J'( 0, 2)	=	7.01558667	ITER =	4
J'( 0, 1)	=	3.83170597	ITER =	4
J'( 1, 5)	=	14.86358863	ITER =	4
J'( 1, 4)	=	11.70600490	ITER =	4
J'( 1, 3)	=	8.53631637	ITER =	4
J'( 1, 2)	=	5.33144277	ITER =	4
J'( 1, 1)	=	1.84118378	ITER =	4
J'( 2, 5)	=	16.34752232	ITER =	4
J'( 2, 4)	=	13.17037086	ITER =	4
J'( 2, 3)	=	9.96946782	ITER =	4
J'( 2, 2)	=	6.70613319	ITER =	4
J'( 2, 1)	=	3.05423693	ITER =	4
J'( 3, 5)	=	17.78874787	ITER =	4
J'( 3, 4)	=	14.58584829	ITER =	5
J'( 3, 3)	=	11.34592431	ITER =	4
J'( 3, 2)	=	8.01523660	ITER =	4
J'( 3, 1)	=	4.20118894	ITER =	4
J'( 4, 5)	=	19.19602880	ITER =	5
J'( 4, 4)	=	15.96410704	ITER =	5
J'( 4, 3)	=	12.68190844	ITER =	4
J'( 4, 2)	=	9.28239629	ITER =	4
J'( 4, 1)	=	5.31755313	ITER =	4
J'( 5, 5)	=	20.57551452	ITER =	5
J'( 5, 4)	=	17.31284249	ITER =	5
J'( 5, 3)	=	13.98718863	ITER =	4
J'( 5, 2)	=	10.51986087	ITER =	4
J'( 5, 1)	=	6.41561638	ITER =	5

MIT 140 GHz Gyrotron  
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\$MODES

NCAS = 3,  
MM = 0, 2, 5, 0, 0, 0, 0, 0, 0, 0,  
PP = 3, 3, 2, 0, 0, 0, 0, 0, 0, 0,  
QQ = .145E+04, .14E+04, .13E+04, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,  
LL = .12E-01, .12E-01, .12E-01, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,  
N = 1,  
BMIN = .52E+01,  
BMAX = .6E+01,  
IAMAX = .35E+01,



V0 = .65E+05,  
 ALPHA = .15E+01,  
 RE = .182E-02,  
 A = .347E-02,

A2

\$END  
 GAMMA0 = 1.12720  
 BETA PERP = .383971  
 BETA PARA = .255981  
 CONST = .238402E-03

MODE TE( 0, 3,1)

QUALITY FACTOR = 1450.00  
 INTERACTION LENGTH = .120000E-01  
 NUMP = 10.1735  
 JM (NUMP) = -.249705  
 KPERP\*RE = 5.33594  
 LAMBDA = .214309E-02  
 JPN = -.346123  
 FREQUENCY = .139888E+12  
 MU = 10.1317  
 XMIN = .551780

	BO [TESLA]	IA START [A]
1	.5616E+01	.1418E+02
2	.5613E+01	.4760E+01
3	.5611E+01	.2878E+01
4	.5608E+01	.2074E+01
5	.5606E+01	.1628E+01
6	.5603E+01	.1346E+01
7	.5601E+01	.1152E+01
8	.5598E+01	.1011E+01
9	.5596E+01	.9041E+00
10	.5593E+01	.8205E+00
11	.5591E+01	.7536E+00
12	.5588E+01	.6992E+00
13	.5586E+01	.6542E+00
14	.5583E+01	.6167E+00
15	.5581E+01	.5850E+00
16	.5578E+01	.5581E+00
17	.5576E+01	.5352E+00
18	.5574E+01	.5156E+00
19	.5571E+01	.4987E+00
20	.5569E+01	.4843E+00
21	.5566E+01	.4720E+00
22	.5564E+01	.4615E+00
23	.5561E+01	.4526E+00
24	.5559E+01	.4452E+00
25	.5556E+01	.4391E+00
26	.5554E+01	.4342E+00
27	.5551E+01	.4304E+00
28	.5549E+01	.4276E+00
29	.5546E+01	.4258E+00
30	.5544E+01	.4249E+00
31	.5541E+01	.4249E+00
32	.5539E+01	.4258E+00
33	.5536E+01	.4274E+00
34	.5534E+01	.4299E+00
35	.5531E+01	.4332E+00



A3

36	.5529E+01	.4372E+00
37	.5526E+01	.4421E+00
38	.5524E+01	.4477E+00
39	.5522E+01	.4542E+00
40	.5519E+01	.4615E+00
41	.5517E+01	.4696E+00
42	.5514E+01	.4786E+00
43	.5512E+01	.4885E+00
44	.5509E+01	.4993E+00
45	.5507E+01	.5111E+00
46	.5504E+01	.5239E+00
47	.5502E+01	.5379E+00
48	.5499E+01	.5529E+00
49	.5497E+01	.5691E+00
50	.5494E+01	.5866E+00
51	.5492E+01	.6054E+00
52	.5489E+01	.6257E+00
53	.5487E+01	.6474E+00
54	.5484E+01	.6708E+00
55	.5482E+01	.6958E+00
56	.5479E+01	.7228E+00
57	.5477E+01	.7517E+00
58	.5474E+01	.7827E+00
59	.5472E+01	.8159E+00
60	.5470E+01	.8517E+00
61	.5467E+01	.8900E+00
62	.5465E+01	.9312E+00
63	.5462E+01	.9754E+00
64	.5460E+01	.1023E+01
65	.5457E+01	.1074E+01
66	.5455E+01	.1129E+01
67	.5452E+01	.1188E+01
68	.5450E+01	.1252E+01
69	.5447E+01	.1320E+01
70	.5445E+01	.1394E+01
71	.5442E+01	.1474E+01
72	.5440E+01	.1560E+01
73	.5437E+01	.1652E+01
74	.5435E+01	.1752E+01
75	.5432E+01	.1861E+01
76	.5430E+01	.1978E+01
77	.5427E+01	.2105E+01
78	.5425E+01	.2242E+01
79	.5422E+01	.2391E+01
80	.5420E+01	.2553E+01
81	.5418E+01	.2728E+01
82	.5415E+01	.2918E+01
83	.5413E+01	.3126E+01
84	.5410E+01	.3351E+01
85	.5408E+01	.3597E+01

MAPPED - VECTOR

\*\*\*\*\*PLOT OPTIONS IN EFFECT\*\*\*\*\*

MODEL	=	8224	,XMIN	=	.00	,XMAX	=	100.00
YMIN	=	.00	,YMAX	=	58.51	,MSGVL	=	1
XSTART	=	.00	,YSTART	=	.00	,SCALE	=	1.00
XFACT	=	1.00	,YFACT	=	1.00	,UNITS	=	2.54
STRIP	=	58.52	,STRIP0	=	.00	,SPACE	=	10.16
PAPIER	=	0	,FC	=	1			

MODE TE( 2, 3,1)

QUALITY FACTOR = 1400.00



INTERACTION LENGTH= .120000E-01  
 NUMP = 9.96947  
 JM (NUMP) = .254744

ROTATING MODE: 1  
 KPERP\*RE 5.22894  
 LAMBDA = .218694E-02  
 JMPN = .320362  
 FREQUENCY = .137083E+12  
 MU = 9.92851  
 XMIN = .552890

A4

	BO [TESLA]	IA START [A]
1	.5502E+01	.1717E+02
2	.5500E+01	.5765E+01
3	.5497E+01	.3486E+01
4	.5495E+01	.2512E+01
5	.5492E+01	.1973E+01
6	.5490E+01	.1632E+01
7	.5487E+01	.1397E+01
8	.5485E+01	.1225E+01
9	.5483E+01	.1096E+01
10	.5480E+01	.9945E+00
11	.5478E+01	.9136E+00
12	.5475E+01	.8476E+00
13	.5473E+01	.7932E+00
14	.5470E+01	.7477E+00
15	.5468E+01	.7093E+00
16	.5465E+01	.6768E+00
17	.5463E+01	.6490E+00
18	.5460E+01	.6252E+00
19	.5458E+01	.6048E+00
20	.5455E+01	.5874E+00
21	.5453E+01	.5724E+00
22	.5450E+01	.5597E+00
23	.5448E+01	.5489E+00
24	.5445E+01	.5400E+00
25	.5443E+01	.5326E+00
26	.5441E+01	.5266E+00
27	.5438E+01	.5220E+00
28	.5436E+01	.5187E+00
29	.5433E+01	.5165E+00
30	.5431E+01	.5154E+00
31	.5428E+01	.5154E+00
32	.5426E+01	.5165E+00
33	.5423E+01	.5185E+00
34	.5421E+01	.5215E+00
35	.5418E+01	.5254E+00
36	.5416E+01	.5303E+00
37	.5413E+01	.5362E+00
38	.5411E+01	.5430E+00
39	.5408E+01	.5508E+00
40	.5406E+01	.5597E+00
41	.5403E+01	.5695E+00
42	.5401E+01	.5804E+00
43	.5399E+01	.5924E+00
44	.5396E+01	.6055E+00
45	.5394E+01	.6198E+00
46	.5391E+01	.6353E+00
47	.5389E+01	.6521E+00
48	.5386E+01	.6703E+00
49	.5384E+01	.6899E+00
50	.5381E+01	.7111E+00
51	.5379E+01	.7338E+00
52	.5376E+01	.7583E+00
53	.5374E+01	.7846E+00



AS

54	.5371E+01	.8128E+00
55	.5369E+01	.8432E+00
56	.5366E+01	.8757E+00
57	.5364E+01	.9106E+00
58	.5361E+01	.9491E+00
59	.5359E+01	.9883E+00
60	.5357E+01	1.031E+01
61	.5354E+01	1.078E+01
62	.5352E+01	1.127E+01
63	.5349E+01	1.181E+01
64	.5347E+01	1.238E+01
65	.5344E+01	1.300E+01
66	.5342E+01	1.366E+01
67	.5339E+01	1.438E+01
68	.5337E+01	1.514E+01
69	.5334E+01	1.597E+01
70	.5332E+01	1.686E+01
71	.5329E+01	1.782E+01
72	.5327E+01	1.886E+01
73	.5324E+01	1.998E+01
74	.5322E+01	2.118E+01
75	.5319E+01	2.249E+01
76	.5317E+01	2.390E+01
77	.5315E+01	2.543E+01
78	.5312E+01	2.708E+01
79	.5310E+01	2.888E+01
80	.5307E+01	3.082E+01
81	.5305E+01	3.294E+01
82	.5302E+01	3.523E+01

ROTATING MODE:-1  
KPERP\*RE = 5.22894  
LAMBDA = .218694E-02  
JMPN = -.344363  
FREQUENCY = .137083E+12  
MU = 9.92851  
XMIN = .552890

	B0 [TESLA]	IA START [A]
1	.5502E+01	.1486E+02
2	.5500E+01	.4989E+01
3	.5497E+01	.3017E+01
4	.5495E+01	.2174E+01
5	.5492E+01	.1708E+01
6	.5490E+01	.1412E+01
7	.5487E+01	.1209E+01
8	.5485E+01	.1061E+01
9	.5483E+01	.9484E+00
10	.5480E+01	.8607E+00
11	.5478E+01	.7907E+00
12	.5475E+01	.7336E+00
13	.5473E+01	.6865E+00
14	.5470E+01	.6471E+00
15	.5468E+01	.6139E+00
16	.5465E+01	.5857E+00
17	.5463E+01	.5617E+00
18	.5460E+01	.5411E+00
19	.5458E+01	.5235E+00
20	.5455E+01	.5083E+00
21	.5453E+01	.4954E+00
22	.5450E+01	.4844E+00
23	.5448E+01	.4751E+00
24	.5445E+01	.4673E+00
25	.5443E+01	.4609E+00
26	.5441E+01	.4558E+00
27	.5438E+01	.4518E+00



A6

28	.5436E+01	.4489E+00
29	.5433E+01	.4470E+00
30	.5431E+01	.4461E+00
31	.5428E+01	.4461E+00
32	.5426E+01	.4470E+00
33	.5423E+01	.4487E+00
34	.5421E+01	.4513E+00
35	.5418E+01	.4547E+00
36	.5416E+01	.4590E+00
37	.5413E+01	.4641E+00
38	.5411E+01	.4700E+00
39	.5408E+01	.4767E+00
40	.5406E+01	.4844E+00
41	.5403E+01	.4929E+00
42	.5401E+01	.5023E+00
43	.5399E+01	.5127E+00
44	.5396E+01	.5240E+00
45	.5394E+01	.5364E+00
46	.5391E+01	.5498E+00
47	.5389E+01	.5644E+00
48	.5386E+01	.5801E+00
49	.5384E+01	.5971E+00
50	.5381E+01	.6154E+00
51	.5379E+01	.6351E+00
52	.5376E+01	.6563E+00
53	.5374E+01	.6790E+00
54	.5371E+01	.7035E+00
55	.5369E+01	.7297E+00
56	.5366E+01	.7579E+00
57	.5364E+01	.7881E+00
58	.5361E+01	.8205E+00
59	.5359E+01	.8553E+00
60	.5357E+01	.8927E+00
61	.5354E+01	.9328E+00
62	.5352E+01	.9758E+00
63	.5349E+01	.1022E+01
64	.5347E+01	.1072E+01
65	.5344E+01	.1125E+01
66	.5342E+01	.1182E+01
67	.5339E+01	.1244E+01
68	.5337E+01	.1311E+01
69	.5334E+01	.1382E+01
70	.5332E+01	.1459E+01
71	.5329E+01	.1542E+01
72	.5327E+01	.1632E+01
73	.5324E+01	.1729E+01
74	.5322E+01	.1833E+01
75	.5319E+01	.1946E+01
76	.5317E+01	.2069E+01
77	.5315E+01	.2201E+01
78	.5312E+01	.2344E+01
79	.5310E+01	.2499E+01
80	.5307E+01	.2668E+01
81	.5305E+01	.2851E+01
82	.5302E+01	.3049E+01
83	.5300E+01	.3265E+01
84	.5297E+01	.3500E+01
85	.5295E+01	.3755E+01

MODE TE( 5, 2,1)

QUALITY FACTOR = 1300.00  
INTERACTION LENGTH = .120000E-01  
NUMP = 10.5199



JM (NUMP) = -.261092

ROTATING MODE: 1

KPERP\*RE = 5.51762

LAMBDA = .207252E-02

JMPN = .188849

FREQUENCY = .144651E+12

MU = 10.4766

XMIN = .549998

A7

	BO [TESLA]	IA START [A]
1	.5808E+01	.4476E+02
2	.5805E+01	.1502E+02
3	.5803E+01	.9081E+01
4	.5800E+01	.6542E+01
5	.5798E+01	.5137E+01
6	.5795E+01	.4247E+01
7	.5793E+01	.3634E+01
8	.5791E+01	.3188E+01
9	.5788E+01	.2850E+01
10	.5786E+01	.2586E+01
11	.5783E+01	.2375E+01
12	.5781E+01	.2204E+01
13	.5778E+01	.2062E+01
14	.5776E+01	.1943E+01
15	.5773E+01	.1843E+01
16	.5771E+01	.1758E+01
17	.5768E+01	.1686E+01
18	.5766E+01	.1624E+01
19	.5763E+01	.1571E+01
20	.5761E+01	.1525E+01
21	.5758E+01	.1486E+01
22	.5756E+01	.1453E+01
23	.5753E+01	.1425E+01
24	.5751E+01	.1402E+01
25	.5748E+01	.1382E+01
26	.5746E+01	.1367E+01
27	.5743E+01	.1355E+01
28	.5741E+01	.1346E+01
29	.5738E+01	.1341E+01
30	.5736E+01	.1338E+01
31	.5733E+01	.1338E+01
32	.5731E+01	.1340E+01
33	.5728E+01	.1346E+01
34	.5726E+01	.1353E+01
35	.5723E+01	.1364E+01
36	.5721E+01	.1377E+01
37	.5718E+01	.1392E+01
38	.5716E+01	.1410E+01
39	.5714E+01	.1430E+01
40	.5711E+01	.1453E+01
41	.5709E+01	.1479E+01
42	.5706E+01	.1507E+01
43	.5704E+01	.1539E+01
44	.5701E+01	.1573E+01
45	.5699E+01	.1610E+01
46	.5696E+01	.1651E+01
47	.5694E+01	.1695E+01
48	.5691E+01	.1742E+01
49	.5689E+01	.1794E+01
50	.5686E+01	.1849E+01
51	.5684E+01	.1908E+01
52	.5681E+01	.1972E+01
53	.5679E+01	.2041E+01
54	.5676E+01	.2115E+01
55	.5674E+01	.2195E+01



56	.5671E+01	.2280E+01
57	.5669E+01	.2371E+01
58	.5666E+01	.2470E+01
59	.5664E+01	.2575E+01
60	.5661E+01	.2688E+01
61	.5659E+01	.2810E+01
62	.5656E+01	.2940E+01
63	.5654E+01	.3080E+01
64	.5651E+01	.3231E+01
65	.5649E+01	.3393E+01
66	.5646E+01	.3567E+01

A8

ROTATING MODE:-1  
 KPERP\*RE = 5.51762  
 LAMBDA = .207252E-02  
 JMPN = .396118  
 FREQUENCY = .144651E+12  
 MU = 10.4766  
 XMIN = .549998

	BO [TESLA]	IA START [A]
1	.5808E+01	.1017E+02
2	.5805E+01	.3414E+01
3	.5803E+01	.2064E+01
4	.5800E+01	.1487E+01
5	.5798E+01	.1168E+01
6	.5795E+01	.9652E+00
7	.5793E+01	.8260E+00
8	.5791E+01	.7247E+00
9	.5788E+01	.6479E+00
10	.5786E+01	.5879E+00
11	.5783E+01	.5399E+00
12	.5781E+01	.5008E+00
13	.5778E+01	.4686E+00
14	.5776E+01	.4416E+00
15	.5773E+01	.4189E+00
16	.5771E+01	.3996E+00
17	.5768E+01	.3832E+00
18	.5766E+01	.3691E+00
19	.5763E+01	.3570E+00
20	.5761E+01	.3467E+00
21	.5758E+01	.3378E+00
22	.5756E+01	.3303E+00
23	.5753E+01	.3239E+00
24	.5751E+01	.3186E+00
25	.5748E+01	.3142E+00
26	.5746E+01	.3107E+00
27	.5743E+01	.3080E+00
28	.5741E+01	.3060E+00
29	.5738E+01	.3047E+00
30	.5736E+01	.3041E+00
31	.5733E+01	.3041E+00
32	.5731E+01	.3047E+00
33	.5728E+01	.3059E+00
34	.5726E+01	.3076E+00
35	.5723E+01	.3100E+00
36	.5721E+01	.3129E+00
37	.5718E+01	.3164E+00
38	.5716E+01	.3204E+00
39	.5714E+01	.3251E+00
40	.5711E+01	.3303E+00
41	.5709E+01	.3361E+00
42	.5706E+01	.3426E+00
43	.5704E+01	.3497E+00
44	.5701E+01	.3575E+00
45	.5699E+01	.3660E+00



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46	.5696E+01	.3752E+00
47	.5694E+01	.3852E+00
48	.5691E+01	.3960E+00
49	.5689E+01	.4077E+00
50	.5686E+01	.4202E+00
51	.5684E+01	.4338E+00
52	.5681E+01	.4483E+00
53	.5679E+01	.4640E+00
54	.5676E+01	.4808E+00
55	.5674E+01	.4988E+00
56	.5671E+01	.5182E+00
57	.5669E+01	.5390E+00
58	.5666E+01	.5613E+00
59	.5664E+01	.5853E+00
60	.5661E+01	.6110E+00
61	.5659E+01	.6386E+00
62	.5656E+01	.6683E+00
63	.5654E+01	.7002E+00
64	.5651E+01	.7344E+00
65	.5649E+01	.7712E+00
66	.5646E+01	.8109E+00
67	.5644E+01	.8535E+00
68	.5641E+01	.8994E+00
69	.5639E+01	.9488E+00
70	.5637E+01	.1002E+01
71	.5634E+01	.1060E+01
72	.5632E+01	.1122E+01
73	.5629E+01	.1189E+01
74	.5627E+01	.1261E+01
75	.5624E+01	.1339E+01
76	.5622E+01	.1424E+01
77	.5619E+01	.1516E+01
78	.5617E+01	.1615E+01
79	.5614E+01	.1723E+01
80	.5612E+01	.1840E+01
81	.5609E+01	.1967E+01
82	.5607E+01	.2105E+01
83	.5604E+01	.2255E+01
84	.5602E+01	.2418E+01
85	.5599E+01	.2596E+01
86	.5597E+01	.2790E+01
87	.5594E+01	.3002E+01
88	.5592E+01	.3233E+01
89	.5589E+01	.3486E+01
90	.5587E+01	.3762E+01

DIMENSIONS X MINIMUM = .00 X MAXIMUM = 29.00  
DU DESSIN: Y MINIMUM = .00 Y MAXIMUM = 21.00

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PROGRAM ISTART3      74/855 OPT=1,ROUND=A/S/M/-D,-DS      FTM 5.1+670
DO=-LONG/-OT,ARG=-COMMON/-FIXED,CS=USER/-FIXED,DB=-TB/-SB/-SL/-ER/-ID/-PMD/-ST,-AL,PL=5000
FTN5,I=ISTART3,L=LIS,ANSI=0,LO=S/-A,PN.

PROGRAM ISTART3(INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT)
C
C COMPUTATION OF THE STARTING CURRENT OF A CONVENTIONAL GYROTRON
C PLOT ON VERSATEC (CYBER)
C
C - MODE TE(M,P,1) (SIMPLE CAVITY)
C - ANALYTICAL APPROXIMATION (LINEAR REGIME)
C - MKSA UNITS
C - DOCUMENTATION: INT 144/88
C
C ANDRE PERRENOUD      CRPP/EPFL      VERSION 1      04 JULY 1988
C-----
C PARAMETERS
C-----
C NMAX      MAX NUMBER OF MODES
C NPOINT    MAX NUMBER OF B FIELD POINTS
C MMAX      MAX AZYMUTHAL INDEX      ( MMAX < 51 )
C IPMAX     MAX RADIAL INDEX
C
C INPUT DATA
C-----
C NCAS      NUMBER OF MODES TO BE COMPUTED
C MM(1...NCAS) AZYMUTHAL INDEX
C PP(1...NCAS) RADIAL INDEX
C QQ(1...NCAS) QUALITY FACTOR OF MODE TE(M,P,1)
C LL(1...NCAS) INTERACTION LENGTH OF MODE TE(M,P,1)
C N         HARMONIC #      (MAX 3)
C A         RADIUS OF RESONATOR (CYLINDRICAL CAVITY)
C BMIN     LOWEST VALUE OF B FIELD (FOR THE PLOT)
C BMAX     HIGHEST VALUE OF B FIELD ( " " " )
C IAMAX    HIGHEST VALUE OF CURRENT ( " " " )
C V0       BEAM VOLTAGE
C ALPHA    BEAM ANISOTROPY (VPERP/VPARA)
C RE       BEAM RADIUS
C-----
C
C PARAMETER (NMAX=10, NPOINT=200, MMAX=5, IPMAX=5)
C INTEGER P, PP
C REAL IAMAX, IA, MU0, L, LL, NFAC(10), LAMBDA, MU, KRE,
C * KPERP, NUMP, JMNUMP, JMPN, IST
C DIMENSION B0(NPOINT), IA(NPOINT), BJZP(MMAX+1,IPMAX+2), BJ(50)
C CHARACTER DATE*10,TIME*10,DATE1*10,TIME1*10, LABEL*80
C
C COMMON /TITRE1/ LABEL(2)
C COMMON /TITRE2/ DATE1,TIME1
C COMMON /BEAM/ V0, ALPHA, RE, GAMMA0
C COMMON /CAVITY/ A, M, P, N, ISIG
C COMMON /MODE/ NCAS, MM(NMAX), PP(NMAX), QQ(NMAX), LL(NMAX),
C * FREQ(NMAX)
C COMMON /PAGE/ XA4,YA4,DXL,DXR,DYU,DYD, CH, X0,Y0,AXEX,AXEY
C
C NAMELIST /MODES/ NCAS, MM, PP, QQ, LL, N, BMIN,BMAX, IAMAX,
C * V0, ALPHA, RE, A
C-----
C
C 1. CAS STANDARD (BENCHMARK)
C
C DATA LABEL(1) //' M I T 1 4 0 G H Z G Y R O T R O N ' //
C DATA LABEL(2) // '=====' //

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C
IF (N.GT. 3) STOP ' N TOO LARGE '
IFIRST = 1
DO 490 NC=1,NCAS
M = MM(NC)
P = PP(NC)
Q = QQ(NC)
L = LL(NC)
IF (M.GT. MMAX) STOP ' M TOO LARGE '
IF (P.GT. IPMAX) STOP ' P TOO LARGE '
NUMP = BJZP(M+1,P)
CALL BESSEL (M, NUMP, BJ)
JMNUMP = BJ(M+1)

C
WRITE (6,120) M,P
FORMAT (//, ' MODE TE(' ,I2,' ,',I2,' ,',I2,' ,',1) ' //, '
WRITE (6,110) ' QUALITY FACTOR = ' , Q
WRITE (6,110) ' INTERACTION LENGTH = ' , L
WRITE (6,110) ' NUMP = ' , NUMP
WRITE (6,110) ' JM (NUMP) = ' , JMNUMP

C
CF1 = CF*Q/((NUMP**2 - M**2)*JMNUMP**2)
NSIG = 2
IF (M.EQ.0) NSIG=1
DO 480 NS=1,NSIG
ISIG = 3 - 2*NS
MN = M + ISIG*N
KPERP = NUMP/A
KRE = KPERP*RE
LAMBDA = 2.*PI/KPERP
IF (M.NE.0) WRITE (6,435) ISIG
FORMAT (//, ' ROTATING MODE:' ,I2)
WRITE (6,110) ' KPERP*RE ' , KRE
WRITE (6,110) ' LAMBDA = ' , LAMBDA
CALL BESSEL(MN,KRE, BJ)
JMPN = BJ(MN+1)
WRITE (6,110) ' JMPN = ' , JMPN
CF2 = CF1*JMPN**2*(LAMBDA/L)
OMEGA = KPERP*CLIGHT
FREQ(NC) = OMEGA/(2.*PI)
WRITE (6,110) ' FREQUENCY = ' , FREQ(NC)
MU = PI * BPERP**2/BPARA * (L/LAMBDA)
WRITE (6,110) ' MU = ' , MU
XM = N/MU
XMIN = 0.5*(XM + SQRT(XM**2 + 1.))
WRITE (6,110) ' XMIN = ' , XMIN

C-----
C
C 5. COMPUTES POINTS (B0, IA) FOR X > XM
DX = (XMIN-XM)/30.
DX2 = DX
J = 1
DX2 = DX2/2.
X = XM + DX2
DELTA = 4.*X/MU
B0(J) = EMASS/ECHARG*GAMMA0*OMEGA*(1. - 0.5*BPERP**2 *DELTA)/N
IST = 4./(PI*MU**2) * EXP(2.*X**2) / (MU*X - N)
IA(J) = IST/CF2
IF (J.EQ.1 .AND. IA(J).LT.IAMAX) GOTO 425
IF (IA(J).GT.IAMAX .AND. X.GT.XMIN) GOTO 440

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182 IF (J.GE.NPOINT) GOTO 440
183 J=J+1
184 K=X+DX
185 GOTO 430
186 WRITE (6,445)
187 FORMAT (/10X,'B0 [TESLA] IA START [A]'/)
188 WRITE (6,450) (J1, B0(J1), IA(J1), J1=1,J)
189 FORMAT (15,2E15.4)
190 -----
191 C
192 C 6. PLOT ON VERSATEC
193 C
194 IF (IA(1).GT.IAMAX .AND. IA(2).LT.IAMAX) THEN
195   B0(1) = B0(2) + (IAMAX-IA(2))*(B0(1)-B0(2))/(IA(2)-IA(1))
196   IA(1) = IAMAX
197   ENDIF
198 IF (IA(J).GT.IAMAX .AND. IA(J-1).LT.IAMAX) THEN
199   B0(J) = B0(J-1) - (IAMAX-IA(J-1))*(B0(J-1)-B0(J))/
200   * (IA(J)-IA(J-1))
201   IA(J) = IAMAX
202   ENDIF
203 CALL PLOTST(B0,IA,J, BMIN,BMAX,IAMAX,IFIRST)
204 C
205 CONTINUE
206 CONTINUE
207 CALL TITLE
208 CALL PLOT(0.,0.,999)
209 STOP
210 END

```

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```

SUBROUTINE BESSEL
DO=-LONG/-OT,ARG=-COMMON/-FIXED,CS=USER/-FIXED,DB=-TB/-SB/-SL/-ER/-ID/-PMD/-ST,-AL,PL=5000
FTN5,I=ISTART3,L=LIS,ANSI=0,LO=S/-A,PN.

```

```

1 SUBROUTINE BESSEL(LMAX,X,BJ)
2
3 C CALCULATE BESSEL FUNCTIONS BY BACKWARD RECURSION
4
5 C ON RETURN: BJ(1)=J0(X), BJ(2)=J1(X), ... BJ(LMAX+1)=BJLMAX(X)
6
7 C
8 C PARAMETER (XMIN=.00001,XMAX=100.,MSTART=200,DEL=1.E-60)
9 C DIMENSION TEMP(MSTART),BJ(*)
10
11 C IF (ABS(X).GT.XMIN) GOTO 20
12 C IF (ABS(X).GT.XMAX) STOP 'BESSEL: ARGUMENT TOO BIG'
13 C IF ( LMAX .GT.50 ) STOP 'BESSEL: ORDER TOO BIG'
14 C BJ(1)=1
15 C IF (LMAX.EQ.0) RETURN
16 C DO 10 L=1,LMAX
17 C BJ(L+1)=X/FLOAT(2*L)*BJ(L)
18 C RETURN
19
20 C LSTART=2*(5*INT(ABS(X))+(LMAX+1)/2+10)+1
21 C .....ORDER OF HIGHEST BESSEL FUNCTION IS EVEN TO GUARANTEE CORRECT
22 C .....PARITY (JN(X)) = (-1)**N *JN(-X)
23 C ..... IF (LSTART.GT.MSTART) LSTART=MSTART
24 C TEMP(LSTART)=DEL
25 C TEMP(LSTART-1)=DEL*FLOAT(2*(LSTART-2))/X
26 C TS=TEMP(LSTART)**2
27 C DO 30 L=LSTART-1,2,-1
28 C TEMP(L-1)=FLOAT(2*(L-1))/X*TEMP(L)-TEMP(L+1)
29 C TS=TS+TEMP(L)**2
30 C TS=1./SQRT(TEMP(1)**2+2.*TS)
31 C DO 40 L=1,LMAX+1
32 C BJ(L)=TS*TEMP(L)
33 C RETURN
34 C END

```

```

1 SUBROUTINE PLOTST
2 DO=-LONG/-OT, ARG=-COMMON/-FIXED, CS= USER/-FIXED, DB=-TB/-SB/-SL/-ER/-ID/-PMD/-ST, -AL, PL=5000
3 FTN5, I=ISTART3, L=LIS, ANSI=0, LO=S/-A, PN.
4
5 SUBROUTINE PLOTST(B0, IA, J, BMIN, BMAX, IAMAX, IFIRST)
6 COMMON /PAGE/ XA4, YA4, DXL, DXR, DYU, DYD, CH, X0, Y0, AXEX, AXEY
7 REAL B0(*), IA(*), IAMAX
8 INTEGER P
9 CHARACTER T*20
10 COMMON /CAVITY/ A, M, P, N, ISIG
11 DATA XA4, YA4/29., 21./, DXL, DXR, DYU, DYD/3., 2., 2.5, 3./, CH/0.2/
12 DATA X0, Y0, AXEX, AXEY/3., 2.5, 16., 14./
13 IF (IFIRST.EQ.0) GOTO 25
14 CALL PLOTS ('VERSATEC', 100., 8224, 0, 1)
15 CALL FRAME(BMIN, BMAX, 0., IAMAX, X0, Y0, AXEX, AXEY)
16 CALL CHPEN(3)
17 IFIRST=0
18
19 C
20
21 CONTINUE
22 IPEN=3
23 DO 30 K=1, J
24 CURR=IA(K)
25 IF (CURR.LT.0. .OR. CURR.GT.IAMAX) GOTO 30
26 XX = X0 + (B0(K)-BMIN)/(BMAX-BMIN) * AXEX
27 YY = Y0 + CURR/IAMAX * AXEY
28 CALL PLOT(XX, YY, IPEN)
29 IPEN=2
30 CONTINUE
31
32 SMIN=1.E+20
33 DO 40 K=1, J
34 IF (IA(K).LT.SMIN) THEN
35 NN=K
36 SMIN=IA(K)
37 ENDIF
38 CONTINUE
39 XX = X0 + (B0(NN)-BMIN)/(BMAX-BMIN) * AXEX -1.2
40 YY = Y0 + IA(NN)/IAMAX * AXEY -0.5
41 WRITE (T, 50) ISIG*M, P
42 FORMAT ('I2', 'I2', 'I2', 'I2', '1')
43 CALL SYMBOL(XX, YY, 0.2, T, 0., 10)
44 RETURN
45 END

```

SUBROUTINE FRAME 74/855 OPT=1, ROUND= A/ S/ M/-D, -DS FTN 5.1+670 88/07/04.15.13.18  
 DO=-LONG/-OT, ARG=-COMMON/-FIXED, CS= USER/-FIXED, DB=-TB/-SB/-SL/-ER/-ID/-PMD/-ST, -AL, PL=5000  
 FTN5, I=ISTART3, L=LIS, ANSI=0, LO=S/-A, PN.

```

1 SUBROUTINE FRAME(BMIN,BMAX,ISMIN,ISMAX)
2 COMMON /PAGE/ XA4,YA4,DXL,DXR,DYU,DYD, CH, X0,Y0,AXEX,AXEY
3
4 REAL ISMIN,ISMAX
5
6 DATA MASK/'O"525252525252525252525252"/
7
8 CH = CHARACTER HEIGHT
9
10 A4 FRAME
11
12 CALL CHPEN(2)
13 CALL PLOT(0, 1, 3)
14 CALL PLOT(0, 0, 2)
15 CALL PLOT(1, 0, 2)
16 CALL PLOT(XA4-1, 0, 3)
17 CALL PLOT(XA4, 0, 2)
18 CALL PLOT(XA4, 1, 2)
19 CALL PLOT(XA4-1, YA4, 3)
20 CALL PLOT(XA4, YA4, 2)
21 CALL PLOT(XA4, YA4-1, 2)
22 CALL PLOT(0, YA4-1, 3)
23 CALL PLOT(0, YA4, 2)
24 CALL PLOT(1, YA4, 2)
25
26 AXES AND GRID
27
28 DB=(BMAX-BMIN)/AXEX
29 CALL AXIS(X0,Y0,AXEX,0.,BMIN,DB,'MAGNETIC FIELD (TESLA)',22)
30
31 DIS=(ISMAX-ISMIN)/AXEY
32 CALL AXIS(X0,Y0,AXEY,90.,ISMIN,DIS,'STARTING CURRENT (A)',-20)
33 CALL CHPEN(3)
34 CALL PLOT(X0,Y0,3)
35 CALL PLOT(X0,Y0+AXEY,2)
36 CALL PLOT(X0+AXEX,Y0+AXEY,2)
37 CALL PLOT(X0+AXEX,Y0,2)
38 CALL PLOT(X0,Y0,2)
39 CALL CHPEN(2)
40 IAXEX=AXEX
41 IAXEY=AXEY
42 CALL GRID(X0,Y0,IAXEX,1.,IAXEY,1.,MASK)
43 RETURN
44 END
  
```



```

60
61 YT=YT-2.*CH
62 T, TE
63 CALL SYMBOL(XT,YT,CH,T,0.,33) [GHZ]
64 DO 20 NC=1,NCAS
65 YT=YT-2.*CH
66 WRITE (T,21) MM(NC), PP(NC), QQ(NC), FREQ(NC)/1.E+09
67 FORMAT(' ',I2,' ',I2,' ',I2,' ',I2,' ',F10.0,2X,F9.3)
68 CALL SYMBOL(XT,YT,CH,T,0.,31)
69 RETURN
70 END

```

21  
20  
C