The role of silver on the stabilization of the incommensurately modulated structure in calaverite, \( \text{AuTe}_2 \)

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**ABSTRACT**

Structural investigations of several minerals belonging to the calaverite group with composition \( \text{Au}_x\text{Ag}_y\text{Te}_z \) \((x = 0.00, 0.02, 0.05, 0.09, 0.19, \text{and} 0.33) \) indicate that Ag is randomly distributed on the Au sites. This suppresses the valence fluctuation of Au and, therefore, the structure modulations. The results are compared with the previously published incommensurately modulated structure of calaverite, \( \text{Au}_{0.0}\text{Ag}_{0.1}\text{Te}_2 \), which is characterized by valence fluctuations of Au reinforced by an ordered distribution of Ag. The \((3+1)\)-dimensional calaverite structure type is able to reproduce both \((3+1)\)D and 3D related structures with the general formula \( \text{AB}_2 \) \((A = \text{Au}, \text{Ag}, \text{Cu}, \text{Nb}, \text{Ta}; B = \text{Te}) \).

**Keywords:** Calaverite, modulated structure, valence fluctuations, krennerite

**INTRODUCTION**

Calaverite was first identified by Ghent (1861) and, since its discovery, it has been the subject of numerous studies, in large part because of the difficulties mineralogists encountered in indexing crystalline specimens from different locations. It was later found that the diffraction pattern of calaverite exhibited satellite reflections, which pointed to the presence of an incommensurately modulated structure (Chapuis 2003 and references therein). Calaverite belongs to the group of gold-silver tellurides with the chemical formula \( \text{Au}_x\text{Ag}_y\text{Te}_z \), the most important group of minerals from an economic standpoint in the Au-Ag-Te system. This group comprises calaverite, \( \text{AuTe}_2 \) \((\text{the monoclinc polymorph})\); krennerite, \( \text{AuTe}_2 \) \((\text{the orthorhombic polymorph})\); and sylvanite, \( \text{AuAgTe}_2 \). Based on the experimental data of Cabri (1965), calaverite, krennerite, and sylvanite contain 0.00 to 2.8 wt\%, 3.4 to 6.2 wt\%, and 6.7 to 13.2 wt\% Ag, respectively. These minerals occur in several epizonal and mesozonal gold and gold-silver telluride deposits including the Golden Mile, Kalgoorlie, Australia \((\text{e.g., Clout et al. 1990; Shackleton et al. 2003)}\), Emperor, Fiji \((\text{e.g., Ahmad et al. 1987; Pals and Spry 2003)}\), Cripple Creek, Colorado \((\text{e.g., Thompson et al. 1985)}\), and Săcărimb, Romania \((\text{Alderton and Fallick 2000)}\) deposits, which are among the largest gold deposits in the world.

From the crystallographic standpoint, calaverite has received much attention in the past century because its morphology was considered to violate Haidy’s law of rational indices (Goldschmidt et al. 1931 and references therein). It is surprising that the introduction of diffraction techniques did not solve the puzzle initially. Indeed, it was first Tunell and Ksanda (1936) and then Tunell and Pauling (1952) who were able to solve the average \( C2/m \) structure of calaverite. However, they did not propose any interpretation of the so-called “adventive diffraction spots” \((\text{now called satellites})\) observed in the diffraction pattern of calaverite.

Sueno et al. (1979) were the first to identify the additional spots as “wavy displacements” in the structure. These authors found that the satellite positions were at 27.3° from the +c* axis and 62.7° from the +a* axis, with a wave vector normal to the \((3\overline{0}3)\) lattice plane. Nonetheless, Sueno et al. (1979) could not solve the structure with a sinusoidal wave-distribution function for the displacement of the Te atoms in a commensurate enlarged supercell. Later, based on a transmission electron microscopy \((\text{TEM})\) study, Van Tendeloo et al. (1983a) pointed out that the satellite reflections in calaverite were due to an incommensurately displaceable modulation superimposed on the average \( C2/m \) structure. Using the information gained from the TEM study, Dam et al. (1985) were able to clarify the morphology of calaverite by indexing the crystal faces with four instead of three indices, the extra index applying to \( q = -0.4095a^* + 0.4492c^* \).

Finally, Schutte and de Boer (1988), using the superspace approach, solved the incommensurately modulated structure of calaverite in the superspace group \( C2/m(0\overline{0}7)\overline{0}b\). These authors showed that the modulation consists mainly of displacements of Te atoms and the observed modulations are interpreted in terms of valence fluctuations between \( \text{Au}^+ \) and \( \text{Au}^{3+} \). More recently, Balzuweit et al. (1993) studied the variation of the modulation wave vector in synthetic calaverite as a function of temperature and silver content \((\text{up to 3.0 at\% of Ag})\) using X-ray diffraction and morphological techniques.

In the course of research projects dealing with the characterization of tellurium-bearing minerals from museum collections \((\text{Bindi and Cipriani 2003a, 2003b, 2004a, 2004b, 2004c, 2004d; Bindi et al. 2004, 2005; Bindi 2008, 2009)}\), we analyzed calaverite samples with variable silver contents. The aim of the present work is to characterize calaverite by single-crystal X-ray diffraction, scanning electron microscopy \((\text{SEM})\), and electron probe microanalysis \((\text{EPMA})\) and to discuss the role of silver in the stabilization of the incommensurately modulated structure in the framework of the superspace concept.
OCCURRENCE, PHYSICAL AND OPTICAL PROPERTIES

A list of the samples investigated in this study, together with their locations and chemical formulae, is given in Table 1. All the samples came from the mineralogical collection of the Museo di Storia Naturale, Università di Firenze. The calaverite samples have colors ranging from yellow to silver white, show a greenish to yellowish gray streak and exhibit a metallic luster. The crystals are brittle and their fractures are uneven to subconchoidal. Micro-indentation measurements carried out with a VHN load of 100 g give the mean values reported in Table 2.

In plane-polarized incident light, calaverite is white in color, with moderate bireflectance (from white to brownish gray). Under crossed polars, calaverite shows weak anisotropism without internal reflections. Reflectance measurements were performed for all the samples in air by means of a MPM-200 Zeiss microphotometer equipped with a MSP-20 system processor on a Zeiss Axiosplan ore microscope. The filament temperature was approximately 3350 K. An interference filter was adjusted to select, in turn, four wavelengths for measurement (471.1, 548.3, 586.6, and 652.3 nm). Readings were taken for the specimen and standard (SiC) under the same focus conditions. The diameter of the circular measuring area was 0.1 mm. Reflectance percentages for \( R_{\min} \) and \( R_{\max} \) are given in Table 2. It appears that the reflectivity values decrease with the increase of silver replacing gold.

Chemical composition

Qualitative chemical analysis using energy dispersive spectrometry, performed on the crystal fragments used for the structural study, did not indicate the presence of elements (\( Z > 9 \)) other than Ag, Au, and Te. Quantitative chemical compositions were then determined using wavelength dispersive analysis (WDS) by means of a JEOL JXA-8600 electron microprobe. Concentrations of major and minor elements were determined at an accelerating voltage of 20 kV and a beam current of 40 nA, with 10 s as the counting time. For the WDS analyses, the following lines were selected in turn, four wavelengths for measurement (471.1, 548.3, 586.6, and 652.3 nm). An interference filter was adjusted to fit the wavelength of interest, and an electronic multiplier was adjusted to give the mean counts. The standards employed were native elements for Ag, Au, and Te. The crystal fragments were found to be homogeneous within the analytical errors. The average chemical compositions (six to eight analyses on each grain) are reported in Table 4. The chemical formulae were calculated on the basis of three atoms.

Single-crystal X-ray diffraction

The diffraction quality of the single crystals was initially checked by means of an Enraf-Nonius CAD4 single crystal diffractometer equipped with a conventional point detector. The crystals were then carefully investigated using an Oxford Diffraction “Xcalibur 3” single-crystal diffractometer (enhanced X-ray source, X-ray radiation MoK\( \alpha \), \( \lambda = 0.71073 \) Å) fitted with a Sapphire 2 CCD detector. A total of 500 frames of data were collected\(^1\) for each crystal at room temperature consisting of 5 sets of omega runs with an exposure time of 30 s per frame and a frame width of 0.75°. Data frames were processed using the Crysalis software package (Oxford Diffraction 2006) running on the Xcalibur 3 control PC. A relatively high \( \sin(\theta)/\lambda \) cut off and a high redundancy were chosen in the recording settings. Unit-cell parameters for the selected crystals are given in Table 3. The modulation wave vectors (Table 6) were obtained by the least-squares refinement of the setting angles of the first-order satellites along with the main reflections. Only first-order satellites could be observed after integration for \( \text{Ag}_{0.09}, \text{Ag}_{0.05}, \text{Ag}_{0.02}, \) and \( \text{Ag}_{0.01} \). No satellites have been detected for the Ag-rich members. Other crystals tested from the different samples (3–4 for each sample) gave similar results both in terms of observed

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satellites and modulation wave vectors. In an attempt to detect observable satellites for the Ag-rich members, a second measurement was performed with longer exposure times (400 s). No appreciable time-dependent change in intensities and/or positions of both main and satellite reflections was observed. A similar result was obtained when the same crystals were collected at a temperature ca. 110 K, the low temperature being achieved by means of an Oxford cryostream cooler. Before measurement, the samples were held at the specified temperature for about 180 min. After the cooling experiment, the crystals were re-heated to ca. 300 K, and new data were collected. The obtained unit-cell parameter and modulation wave vectors did not reveal significant variation from the previous ones. Intensity integration and standard Lorentz-polarization correction were performed with the CrysAlis RED (Oxford Diffraction 2006) software package. The program ABSPACK in CrysAlis RED was applied for the absorption correction. The least-squares program JANA2006 (Petříček et al. 2006) was used for the refinements of all the structures. Neutral scattering curves for Au, Ag, and Te were taken from the International Tables for X-ray Crystallography (Ibers and Hamilton 1974). Refinements of the incommensurately modulated structures were performed in the superspace group \( C2/m(0\alpha 0\gamma)0s \) for \( Ag_{0.00}, Ag_{0.02}, Ag_{0.05}, \) and \( Ag_{0.09} \) and in the space group \( C2/m \) for \( Ag_{0.09} \) and \( Ag_{0.23} \) (no satellites detected). Experimental details of the data collections and refinements are given in Table 7. Fractional atomic coordinates, anisotropic displacement parameters, and selected bond distances are reported in Tables 8–11.

The incommensurately modulated structures of \( Ag_{0.00}, Ag_{0.02}, Ag_{0.05}, \) and \( Ag_{0.09} \) have been refined according to the following scheme: first, the average structure was refined. Then the first harmonic of positional modulation wave was introduced for both Te and (Au,Ag). The only possible amplitude of the (Au,Ag) positional modulation (Table 8) was equal to 0 within 1 standard deviation for \( Ag_{0.00} \) and \( Ag_{0.02} \) and within 2 standard deviations for \( Ag_{0.05} \). The refinement of the Te positional modulation improved all R factors; however, the essential decrease of \( R_{s\text{atellite}} \) from about 15% to about 7%, was reached by applying an additional crenel function \((0.5 \text{ length along } t_4 \text{ with the center at } t_4 = 0.25)\) for \( Ag_{0.00}, Ag_{0.02}, \) and \( Ag_{0.05} \). This crenel function results in a small shift of Te from the mirror plane \([v_{Te} ≈ -0.04 \text{ to } -0.02] \) (Table 8). The refined contributions of Ag in

### Table 5. Unit-cell parameters for the selected calaverite crystals

<table>
<thead>
<tr>
<th>Sample</th>
<th>( a (\text{Å}) )</th>
<th>( b (\text{Å}) )</th>
<th>( c (\text{Å}) )</th>
<th>( \beta (^\circ) )</th>
<th>( V (\text{Å}^3) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ag_{0.0}</td>
<td>7.190(15)</td>
<td>4.407(3)</td>
<td>5.070(14)</td>
<td>90.037(2)</td>
<td>160.68(2)</td>
</tr>
<tr>
<td>Ag_{0.02}</td>
<td>7.194(5)</td>
<td>4.410(3)</td>
<td>5.079(5)</td>
<td>90.035(2)</td>
<td>161.751</td>
</tr>
<tr>
<td>Ag_{0.05}</td>
<td>7.211(5)</td>
<td>4.412(3)</td>
<td>5.091(2)</td>
<td>90.028(2)</td>
<td>162.00(2)</td>
</tr>
<tr>
<td>Ag_{0.09}</td>
<td>7.235(6)</td>
<td>4.416(3)</td>
<td>5.111(2)</td>
<td>90.030(3)</td>
<td>163.32(2)</td>
</tr>
<tr>
<td>Ag_{0.23}</td>
<td>7.299(8)</td>
<td>4.425(3)</td>
<td>5.156(3)</td>
<td>90.032(3)</td>
<td>166.56(2)</td>
</tr>
<tr>
<td>Ag_{0.00}</td>
<td>7.400(2)</td>
<td>4.436(2)</td>
<td>5.241(5)</td>
<td>90.034(2)</td>
<td>172.09(2)</td>
</tr>
</tbody>
</table>

### Table 6. Modulation wave vectors for the selected calaverite crystals

<table>
<thead>
<tr>
<th>Sample</th>
<th>Modulation wave vector</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ag_{0.0}</td>
<td>(-0.4026(2)a^* + 0.4470(2)c^* )</td>
</tr>
<tr>
<td>Ag_{0.02}</td>
<td>(-0.4051(2)a^* + 0.4479(2)c^* )</td>
</tr>
<tr>
<td>Ag_{0.05}</td>
<td>(-0.4071(3)a^* + 0.4491(3)c^* )</td>
</tr>
<tr>
<td>Ag_{0.09}</td>
<td>(-0.4112(2)a^* + 0.4511(2)c^* )</td>
</tr>
<tr>
<td>Ag_{0.23}</td>
<td>– – – – – – – –</td>
</tr>
</tbody>
</table>

### Table 7. Data and experimental details for the selected calaverite crystals

| Sample   | Temperature (K) | Cell setting | Superspace group/Space group | Crystal color | Crystal shape | Crystal size (mm) | Diffracontor | Radiation | Monochromator | Scan mode | Detector to sample distance (cm) | Measuring time (s) | Theta range (°) | Range of h,k,l/m | No. of measured refl. | No. of observed refl. | Criterion for obs. | \( R_{s\text{max}} \) | Refinement coefficient | No. of refined parameters | Weighting scheme |
|----------|----------------|--------------|-----------------------------|---------------|---------------|------------------|--------------|------------|--------------|-----------|-------------------------------|-------------------|----------------|----------------|---------------------|----------------------|------------------|-----------------|----------------|----------------------|---------------------|----------------|
| Ag_{0.0} | 298            | monoclinic   | \( C2/m(0\alpha 0\gamma)0s \) | yellow        | irregular     | 0.11 × 0.12 × 0.13 | Oxford        | MoL23       | graphite     | ϕ/ω       | 5                             | 30                | 1–45             | \( -14 \leq s \leq 14 \) | 5289                | 698                  | \( > 3\sigma(l) \)  | 0.057               | F                    | 34                   | \( w = 1 / (|F|^2)+ \) |
| Ag_{0.02} | 298            | monoclinic   | \( C2/m(0\alpha 0\gamma)0s \) | yellow        | irregular     | 0.09 × 0.10 × 0.13 | Oxford        | MoL23       | graphite     | ϕ/ω       | 5                             | 30                | 1–45             | \( -14 \leq s \leq 14 \) | 5312                | 678                  | \( > 3\sigma(l) \)  | 0.105               | F                    | 34                   | \( w = 1 / (|F|^2)+ \) |
| Ag_{0.05} | 298            | monoclinic   | \( C2/m(0\alpha 0\gamma)0s \) | yellow        | irregular     | 0.08 × 0.09 × 0.11 | Oxford        | MoL23       | graphite     | ϕ/ω       | 5                             | 30                | 1–45             | \( -14 \leq s \leq 14 \) | 5302                | 756                  | \( > 3\sigma(l) \)  | 0.037               | F                    | 34                   | \( w = 1 / (|F|^2)+ \) |
| Ag_{0.09} | 298            | monoclinic   | \( C2/m(0\alpha 0\gamma)0s \) | yellow        | irregular     | 0.10 × 0.10 × 0.12 | Oxford        | MoL23       | graphite     | ϕ/ω       | 5                             | 30                | 1–45             | \( -14 \leq s \leq 14 \) | 5344                | 751                  | \( > 3\sigma(l) \)  | 0.064               | F                    | 35                   | \( w = 1 / (|F|^2)+ \) |
| Ag_{0.23} | 298            | monoclinic   | \( C2/m \)                 | yellow        | irregular     | 0.07 × 0.09 × 0.10 | Oxford        | MoL23       | graphite     | ϕ/ω       | 5                             | 30                | 1–45             | \( -14 \leq s \leq 14 \) | 5401                | 746                  | \( > 3\sigma(l) \)  | 0.039               | F                    | 36                   | \( w = 1 / (|F|^2)+ \) |
the (Au,Ag) position confirm the chemical analysis for Ag$_{0.05}$ and Ag$_{0.09}$. For Ag$_{0.02}$, the Ag value was fixed at 0.02 because of its uncertainty, which was equal to the value of the Ag contribution, i.e., 0.02(2). Refinement of the ordered distribution of Ag on the Au/Ag position is not justified following the absence of second-order satellites, which should appear as a result of the occupation modulations (Schutte and de Boer 1988). Refinement of the AdP modulations (Table 9) improved all the $R$ factors.

The refinement of Ag$_{0.19}$ and Ag$_{0.33}$ did not present any problem. Nevertheless, in both cases the refined occupancies for silver in the (Au,Ag) positions yielded lower Ag contents in comparison to those obtained by electron microprobe analyses [refined values: 0.112(3)Ag and 0.218(3)Ag for Ag$_{0.19}$ and Ag$_{0.33}$, respectively].

### Discussion

#### Crystal Chemistry and Structure Modulations

The crystal structure of calaverite (Pertlik 1984a; Schutte and de Boer 1988; Reithmayer et al. 1993) is represented in Figure 1. It is based on a distorted hexagonal closed-packed array of Te$^{2-}$ anions with Au (and Ag) cations occupying the octahedral sites. AuTe$_6$ octahedra form sheets parallel to (001) that are linked by Te-Te bonds.

The refinement of the site-occupancy factor of the (Au,Ag) position in all the investigated calaverite crystals indicates that Ag randomly substitutes for Au in the octahedral site. A strong differentiation of the (Au,Ag)-Te distances is observed for all CN of (Au,Ag): two long distances are essentially shorter and two others are essentially longer than their mean value (Fig. 2, left). Moreover, only two long distances and CN = 2 + 2 can be considered in two symmetrically related ranges along the t-axis, $−0.05 < t < 0.05$ and $0.45 < t < 0.55$ (gray areas in Fig. 2, left); two additional distances are >3.1 Å. In the remaining ranges, $0.05 < t < 0.45$ and $0.55 < t < 0.95$, the coordination number (CN) of (Au,Ag) can be considered as CN = 2 + 4 for Ag$_{0.05}$, Ag$_{0.02}$, and Ag$_{0.09}$. With increasing Ag content (i.e., Ag$_{0.05}$, Ag$_{0.02}$, and Ag$_{0.09}$), the coordination number of (Au,Ag) tends to converge to CN = 2 + 4 (Fig. 2, left). According to Schutte and de Boer (1988), the displaceable modulation of the atoms resulting in the differentiation of CN is associated with a valence fluctuation of Au$^{3+}$ and Au$^{3+}$; in addition, the occupation modulation of the (Au,Ag) position (ordered distribution of Ag) strengthens this valence fluctuation and the CN differentiation (dashed line graphs in Fig. 2). Our results confirm and complete their conclusion. Indeed, the differentiation of the CN is associated with a significant differentiation of the bond valence sum calculated for Au in Ag$_{0.09}$ (Fig. 2, top right). This differentiation of the bond valence sum disappears consistently with increased randomness of the Ag distribution, so that starting from Ag$_{0.19}$ the structure loses its modulation character. Hence, one can conclude that randomly distributed Ag suppresses the valence fluctuation of Au$^{3+}$ and Au$^{3+}$, whereas an ordered distribution reinforces it.

A portion of the incommensurately modulated structures of Ag$_{0.00}$ and Ag$_{0.09}$ (present work) is shown in Figure 3, in comparison with the corresponding portion of the incommensurately

<table>
<thead>
<tr>
<th>Occupancy Wave</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>U$_{iso}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Au 1.000Au</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02352(9)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.6917(12)</td>
<td>−0.024(4)</td>
<td>0.295(3)</td>
<td>0.035(2)</td>
</tr>
<tr>
<td>Au 0.98Au + 0.02Ag</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02390(6)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.6889(12)</td>
<td>−0.035(4)</td>
<td>0.290(2)</td>
<td>0.029(3)</td>
</tr>
<tr>
<td>Au 0.948(3)Au + 0.052Ag</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02342(5)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.6886(9)</td>
<td>−0.0448(3)</td>
<td>0.2894(13)</td>
<td>0.0303(11)</td>
</tr>
<tr>
<td>Au 0.908(8)Au + 0.092Ag</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02235(16)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.6788(3)</td>
<td>0</td>
<td>0.28710(11)</td>
<td>0.03501(15)</td>
</tr>
<tr>
<td>Au 0.888(3)Au + 0.112Ag</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02288(6)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.68692(5)</td>
<td>0</td>
<td>0.28722(7)</td>
<td>0.0324(1)</td>
</tr>
<tr>
<td>Au 0.782(3)Au + 0.218Ag</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.02274(5)</td>
</tr>
<tr>
<td>Te 1.000Te</td>
<td>0.68552(3)</td>
<td>0</td>
<td>0.28681(5)</td>
<td>0.02951(17)</td>
</tr>
</tbody>
</table>

Note: The waves are sorted by the terms (s for sinu, c for cosinu) and m.
TABLE 9. Final values of the anisotropic displacement parameters (Å²) and Fourier amplitudes of the displacive modulation functions

<table>
<thead>
<tr>
<th>Wave</th>
<th>U₁₁</th>
<th>U₁₂</th>
<th>U₁₃</th>
<th>U₂₂</th>
<th>U₂₃</th>
<th>U₃₃</th>
</tr>
</thead>
<tbody>
<tr>
<td>Au</td>
<td>0.02294(15)</td>
<td>0.02287(15)</td>
<td>0.02476(15)</td>
<td>0</td>
<td>0.0001(8)</td>
<td>0</td>
</tr>
<tr>
<td>Te</td>
<td>0.02032(10)</td>
<td>0.02290(11)</td>
<td>0.02576(10)</td>
<td>0</td>
<td>0.0001(6)</td>
<td>0</td>
</tr>
</tbody>
</table>

TABLE 10. The interatomic distances (Å) and angles (°) in the modulated structures of Ag₁₈₀, Ag₁₈₂, Ag₁₈₄, and Ag₁₈₆

<table>
<thead>
<tr>
<th>Wave</th>
<th>Ag₁₈₀</th>
<th>Ag₁₈₂</th>
<th>Ag₁₈₄</th>
<th>Ag₁₈₆</th>
</tr>
</thead>
<tbody>
<tr>
<td>Au-Te⁺</td>
<td>2.675(15)</td>
<td>2.671(18)</td>
<td>2.684(12)</td>
<td>2.684(12)</td>
</tr>
<tr>
<td>Au-Te⁻</td>
<td>2.99(2)</td>
<td>2.87(2)</td>
<td>3.219(16)</td>
<td>3.50(2)</td>
</tr>
<tr>
<td>Au-Te⁺</td>
<td>2.70(2)</td>
<td>2.80(15)</td>
<td>3.00(2)</td>
<td>3.00(2)</td>
</tr>
</tbody>
</table>

Note: Symmetry codes: (a) x, y, z; (b) x + 1/2, y + 1/2, z; (c) x + 1/2, y + 1/2, z; (d) x + 1/2, y + 1/2, z.

TABLE 11. Selected bond distances and angles for the average structures of Ag₁₈₀ and Ag₁₈₂

<table>
<thead>
<tr>
<th>Wave</th>
<th>Ag₁₈₀</th>
<th>Ag₁₈₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>Au-Te₁⁺</td>
<td>2.7240(4)</td>
<td>2.7713(3)</td>
</tr>
<tr>
<td>Au-Te₁⁻</td>
<td>2.9913(3)</td>
<td>3.0105(2)</td>
</tr>
</tbody>
</table>

modulated structure of Ag₁₈₀ reconstructed using the data of Schütt and de Boer (1988). Distances only shorter than 3.1 Å are shown in this figure. In Ag₁₈₀, the square coordination of Au (Fig. 3, top) with CN = 2 + 2 and distances 2.67 Å × 2 and ~2.88 Å × 2 (gray region in Fig. 2, left-top) is associated with the lower valence fluctuation of Au (gray region in Fig. 2, right-top). In Ag₁₈₀, the random distribution of Ag on the (Au,Ag) position leads to a stabilization of the octahedral coordination (CN = 2 + 4) for all the (Au,Ag) atoms (Fig. 3, middle) and the absence of the valence fluctuation of Au (Fig. 2, middle-right).
Our investigation of the natural minerals in the series Au$_{1-x}$Ag$_x$Te$_2$ completes other studies on calaverite (Pertlik 1984a; Schutte and Boer 1988; van tendeloo et al. 1983a; Reithmayer et al. 1993), sylvanite (Van Tendeloo et al. 1983b; Pertlik 1984c), and krennerite (Van Tendeloo et al. 1984; Pertlik 1984b). All these examples taken together show that different degrees of valence fluctuations on the Au-position are possible and, further, that these fluctuations can induce the structure modulation.

Variation of the unit-cell parameters and the modulation wave vector

As shown in Figure 4, the incorporation of Ag on the octahedral site causes an anisotropic expansion of the unit cell. Both the $a$ and $c$ parameters (Figs. 4a and 4c) increase linearly,
whereas the $b$ parameter remains essentially unchanged (Fig. 4b). No clear trend can be observed for the $\beta$ angle, which does not appear to be related to the Ag content (Table 5). The marked increase of the $a$ and $c$ parameters as a function of Ag content is mainly related to the pronounced lengthening of the two shortest octahedral distances.

Figure 5 illustrates the variation of the coefficients $\alpha$ and $\gamma$ of the modulation vector as a function of the Ag content. We observe a constant linear decrease of $\alpha$ and a linear increase of $\gamma$ with increasing the Ag content. The observed variation of the modulation wave vector indicates that for the samples of calaverite studied here no characteristic phase with a specific $q$ is observed. Furthermore, the variations in the modulation wave vector (Table 5) are larger than those observed by Balzuweit et al. (1993) for synthetic Ag-bearing calaverites.

The calaverite (3+1)D structure-type family

It is remarkable that calaverite, krennerite, sylvanite, and related compounds can be described within a unique (3+1)D structure-type, similar to another large group of related compounds jointly described within the scheelite (3+1)D structure-type (Arakcheeva and Chapuis 2008). This “calaverite (3+1)D structure type” is characterized by: (1) the (3+1)-dimensional superspace group $C2/m(00\gamma)$ with the vector $q = 0a^* + 0c^*$; (2) unit-cell parameters $a = 7.3\text{ Å}$, $b = 4.3\text{ Å}$, $c = 5.1\text{ Å}$, and $\beta = 90^\circ$; and (3) two Wyckoff positions, $A$ (Au, Ag) – 2$a$: (000) and $B$ (Te) 4$i$: (x0z). The coefficients of the $q$ vector and modulation functions of both $A$ and $B$ (both positional and occupational) as well as the variable coordinates of the $B$ position are independent variables. Moreover, the incommensurately modulated structure of calaverite (Schutte and de Boer 1988) can be considered as the parent structure for the starting model of the structure refinements (as has been done in the present work), or for the generation of some related structures. For example, the structure of sylvanite can be derived from calaverite with the rational coefficients of $q = \frac{1}{2}a^* + 0c^*$ and an occupation function of $A$ position defined by Ag in the symmetrically related intervals $-0.125 < t < 0.125$ and $0.375 < t < 0.625$ and by Au in the symmetrically related intervals $0.125 < t < 0.375$ and $0.625 < t < 0.875$. The mineral kostovite (CuAuTe$_4$; Van Tendeloo and Amelinckx 1986) is isostructural with sylvanite and can also be included in the calaverite (3+1)D family. The structure of krennerite, Ag$_{0.2}$Au$_{0.8}$Te$_2$, can be described as calaverite with ordered twin $m$-mirror planes leading to orthorhombic symmetry (Van Tendeloo et al. 1984). Some synthetic compounds can also be described in the calaverite (3+1)D structure type. For example, the crystal structures of NbTe$_2$, TaTe$_2$, (Brown 1966), and VTe$_2$ (Bronsema et al. 1984) correspond to this structure type as commensurately modulated structures with $q = \frac{1}{2}a^* + \frac{1}{2}c^*$.

CONCLUDING REMARKS

The present study of various calaverite samples with the chemical compositions Au$_{1-x}$Ag$_x$Te$_2$, $0 \leq x \leq 0.33$, extends the study of Schutte and de Boer (1988) and sheds new light on

**FIGURE 4.** Variation of the unit-cell parameters as a function of the Ag content (apfu).
the origin of the structural modulations observed in this family of compounds. Silver atoms present two types of distribution on the Au sites, either randomly distributed or ordered. The original study of Schutte and de Boer (1988) was concerned with an ordered distribution of Ag, which induces very strong valence fluctuations of Au in the structure. The present study demonstrates another aspect of the Au₆Ag₃Te₂ compounds, specifically those with random distributions of Ag on the Au position. By combining the results of both studies, we contend that the valence fluctuation of Au produces the structure modulation in AuTe₂. Moreover, the ordered distribution of silver reinforces the valence fluctuation of Au. A random distribution of Ag suppresses the valence fluctuation of Au and, therefore, their structural modulations. Apparently, natural samples can be found with the same composition but with both types of Ag ordering, which is not surprising considering the various growth conditions of the minerals.

Another interesting aspect of the Au₆₋ₓAgₓTe₂ series is related to the (3+1)D superspace embedding of the calaverite structure type. We have shown that the same model, independently of their 3D structures and periodicities, can describe all the samples with the same general formula. This formalism opens new perspectives, not only for a uniform description of this family of minerals, but also for other synthetic compounds related to the calaverite structure.

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