Estimating the Real-Time Respiratory Rate from the ECG with a Bank of Notch Filters

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Introduction

- **Goal:** Estimate the respiratory rate from a single-lead ECG with low delay
- **Waveforms:**
  - Respiratory sinus arrhythmia (RSA)
  - Respiratory modulation of R-peak amplitudes (RPA)
- **State-of-the-art:** Fast Fourier transform or adaptive filters
- **Shortcomings:** Large delays
- **Proposed algorithm:** based on the outputs of a bank of notch filters
- **Dataset:** PhysioNet Fantasia

Conclusions

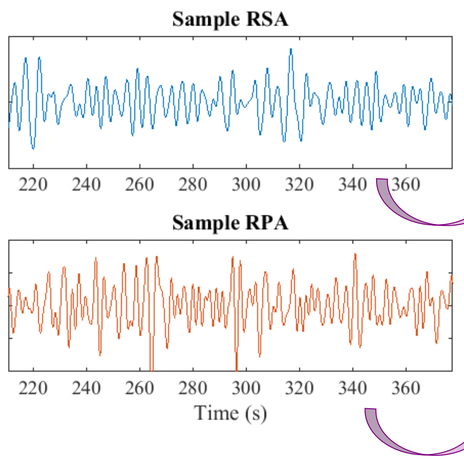
- Respiratory rate estimates are **accurate** (lower error than the state-of-the-art)
- The estimates have **low delays**
- Algorithm is **moderately sensitive** to its parameters

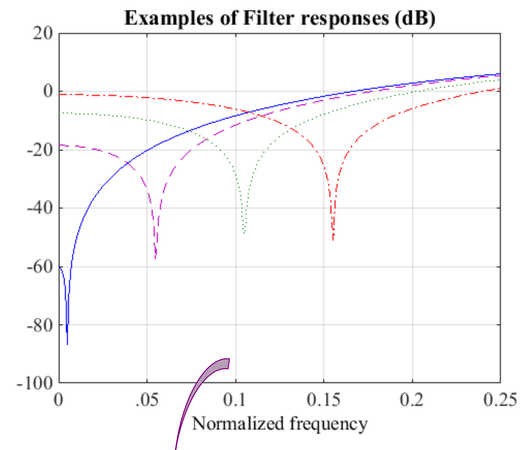
✓ **Good candidate to estimate the real-time instantaneous respiratory rate from the ECG**

Methods

Algorithm input

- RSA: R peak-to-peak distances
- RPA: R peak amplitudes
  - re-sampled @ 4 Hz
  - filtered 0.1-0.5 Hz



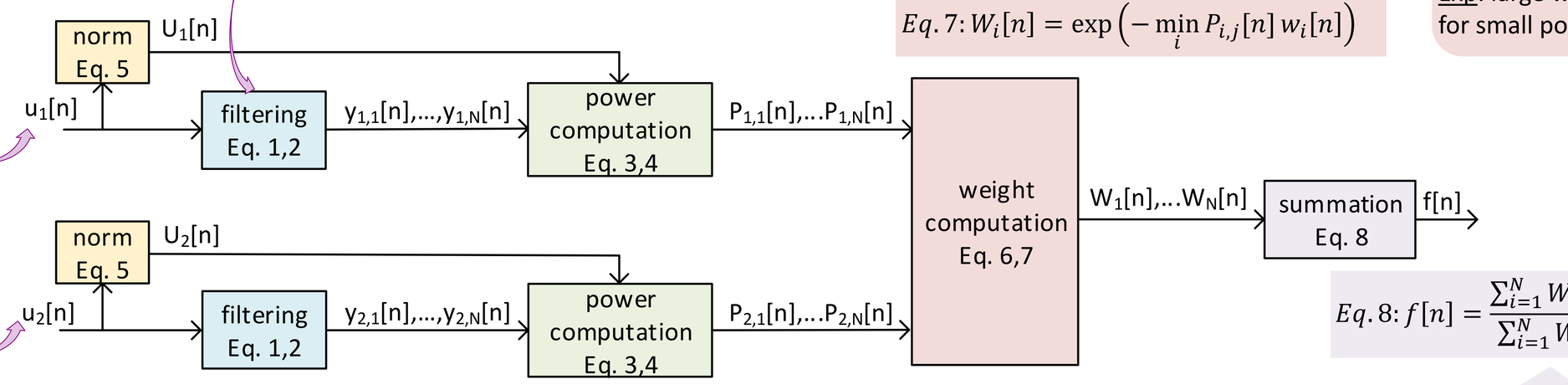


Algorithm flow

Order-3 FIR filters

$Eq.1:\ H(z) = 1 - 2z^{-1}\cos(2\pi f_i) + z^{-2}$

$Eq.2:\ y_i[n] = u[n] - 2u[n-1]\cos(2\pi f_i) + u[n-2]$



$Eq.5:\ U[n] = \delta U[n-1] + (1-\delta)u^2[n]$

Recursive mean square value

$Eq.3: P_i[n] = \delta P_i[n-1] + (1-\delta)c_i^2[n]$

$Eq.4: c_i[n] = y_i[n]/\sqrt{U[n]}$

Recursive output normalized with respect to input

$Eq.6: w_i[n] = \frac{1}{Nsig}\sum_{j=1}^{Nsig} P_{i,j}[n]$

$Eq.7: W_i[n] = \exp\left(-\min_i P_{i,j}[n]\, w_i[n]\right)$

Averaging: single weight over all inputs
Exp: large weights for small powers

$Eq.8: f[n] = \frac{\sum_{i=1}^{N} W_i[n] f_i}{\sum_{i=1}^{N} W_i[n]}$

Algorithm output:
f: frequency estimate. Weighted sum of notch frequencies

Test data

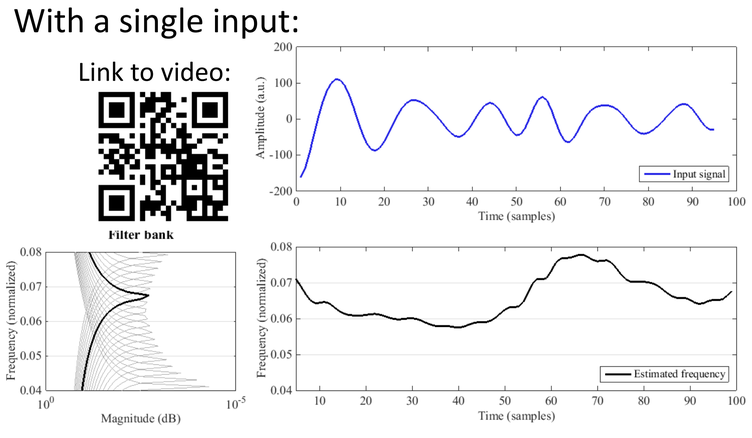
- PhysioNet Fantasia data set
- Single-lead ECG and respiration
- 40 subjects: young and elderly
- 2 hour recordings/subject

Results

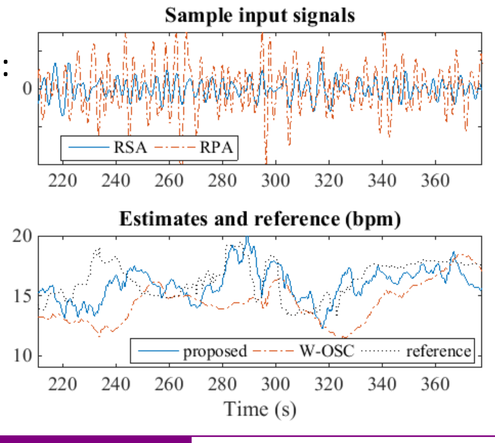
Illustration of the algorithm

- With a single input:

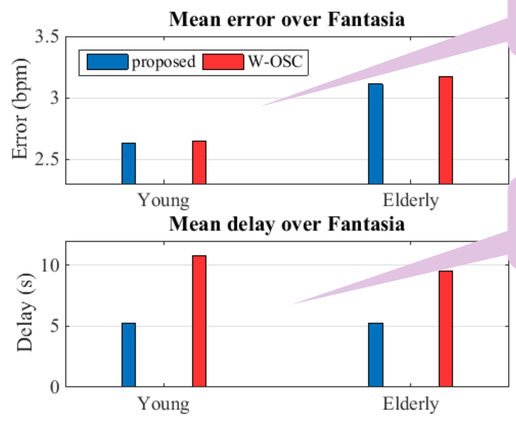
Link to video:



- With two inputs:



Performance



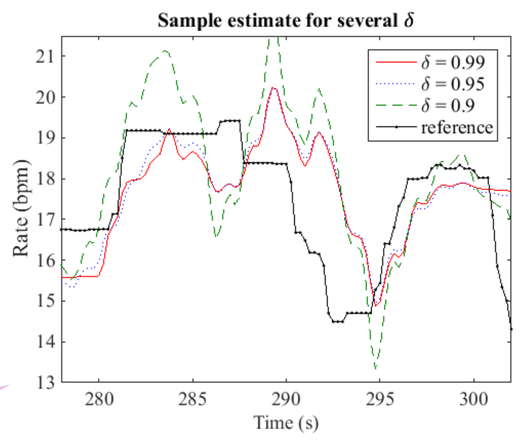
✓ **Lower error than the W-OSC**

✓ **Half the delay of the W-OSC**

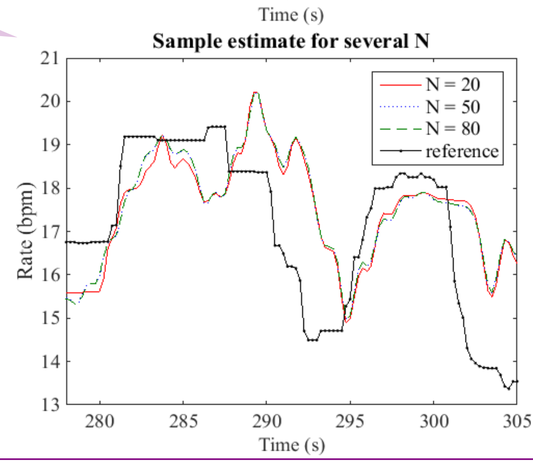
- Mean absolute error (bpm)
- Delay (seconds, measured by correlation analysis)
- Comparison to the state-of-the-art adaptive filter (W_OSC method [1])

[1] Mirmohamadsadeghi and Vesin, Biomed Signal Process Control, 2014

Sensitivity analysis



✓ **Moderate sensitivity**



- High N: less quantization ↔ more computations
- High δ: less variability ↔ slower adaptation

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