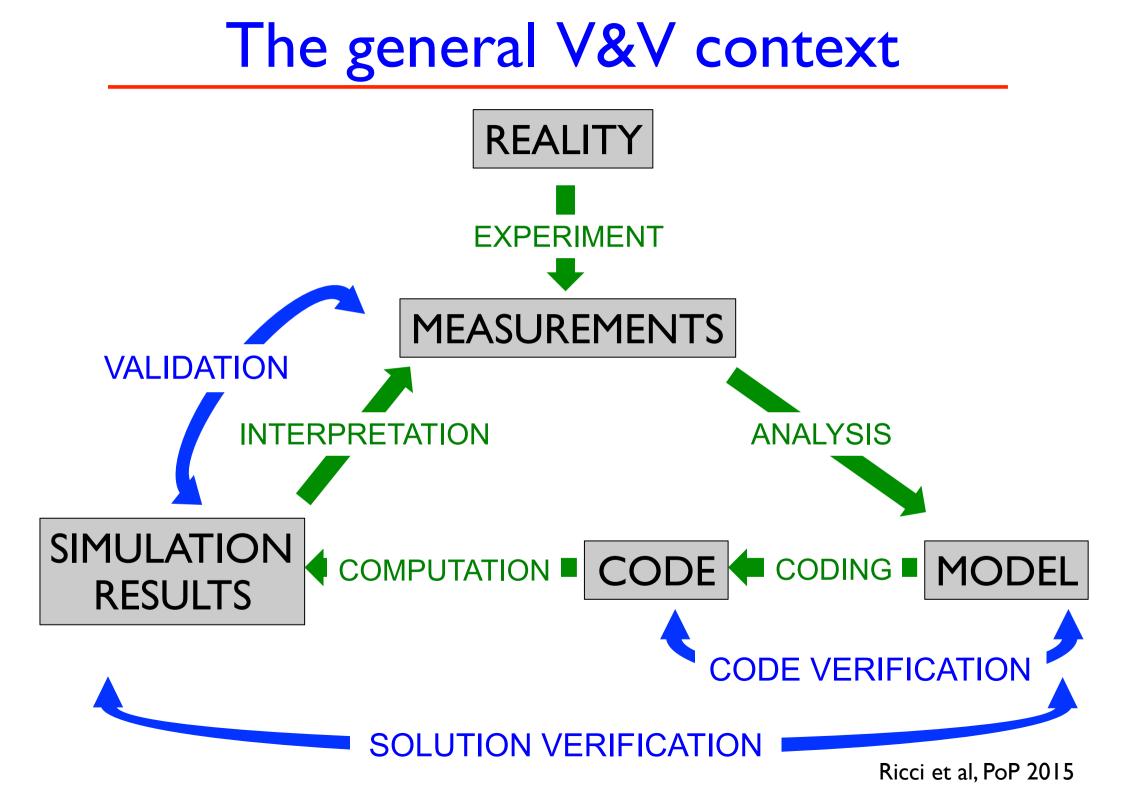
Verification & Validation of plasma turbulence codes in scrape-off layer conditions

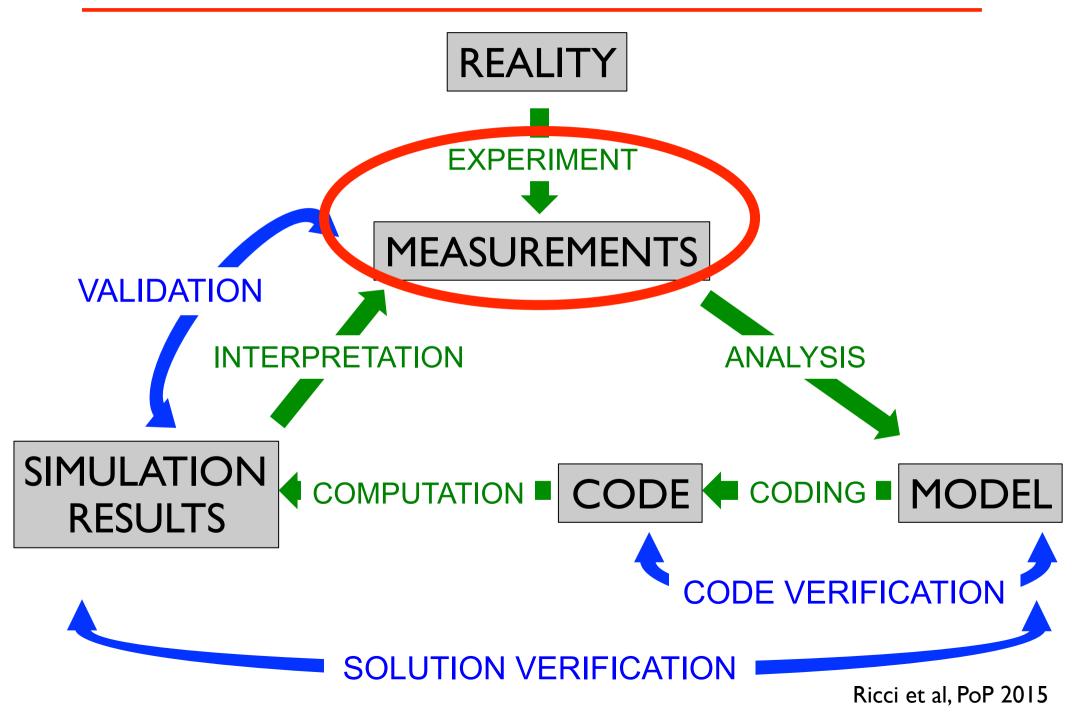
Paolo Ricci

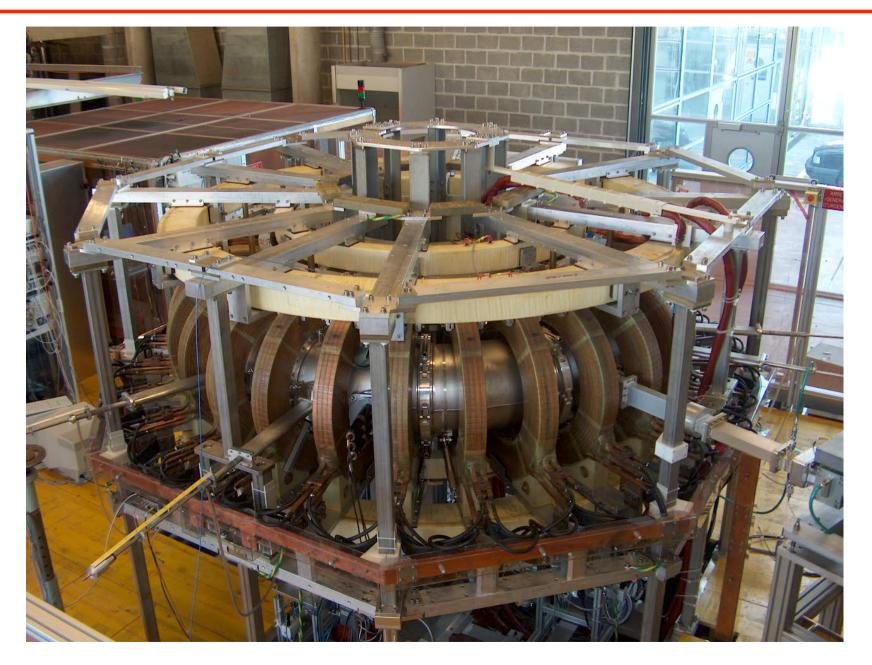
F. Riva, C. Theiler, A. Fasoli, I. Furno, F. Halpern, J. Loizu

Centre de Recherches en Physique des Plasmas École Polytechnique Fédérale de Lausanne, Switzerland

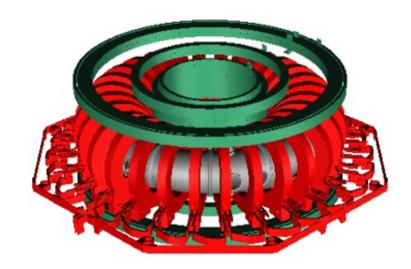
Validation in the general "Verification & Validation" (V&V) context A rigorous V&V procedure through a practical example GBS code and TORPEX experiment, stepping stone to tokamak SOL Initial results of tokamak SOL validation

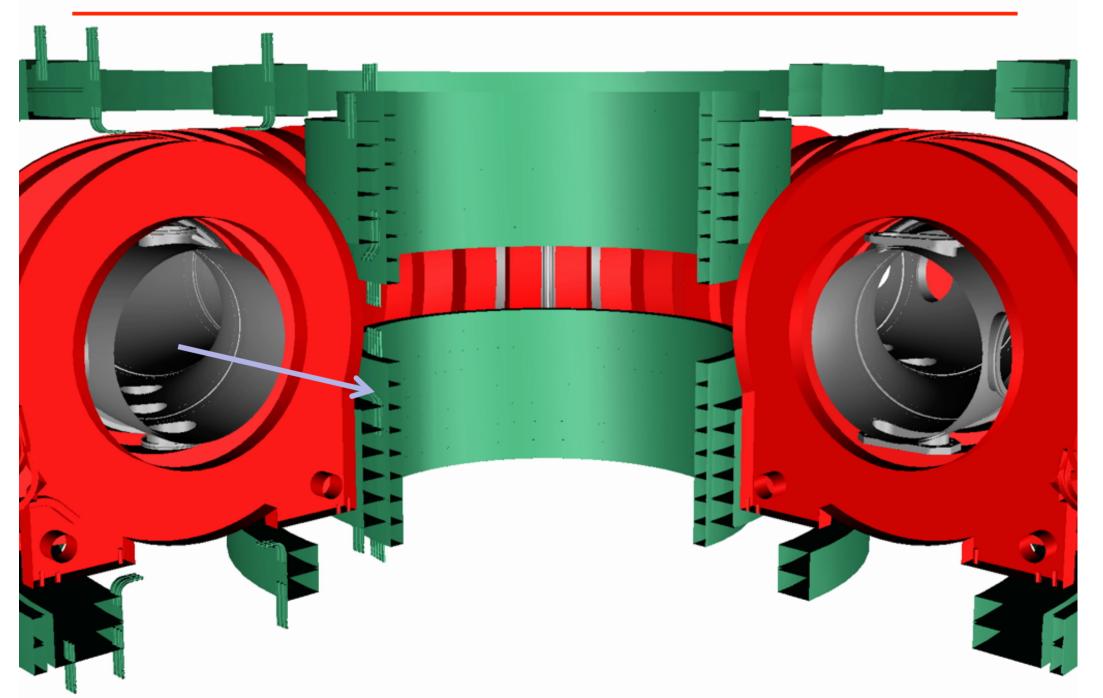


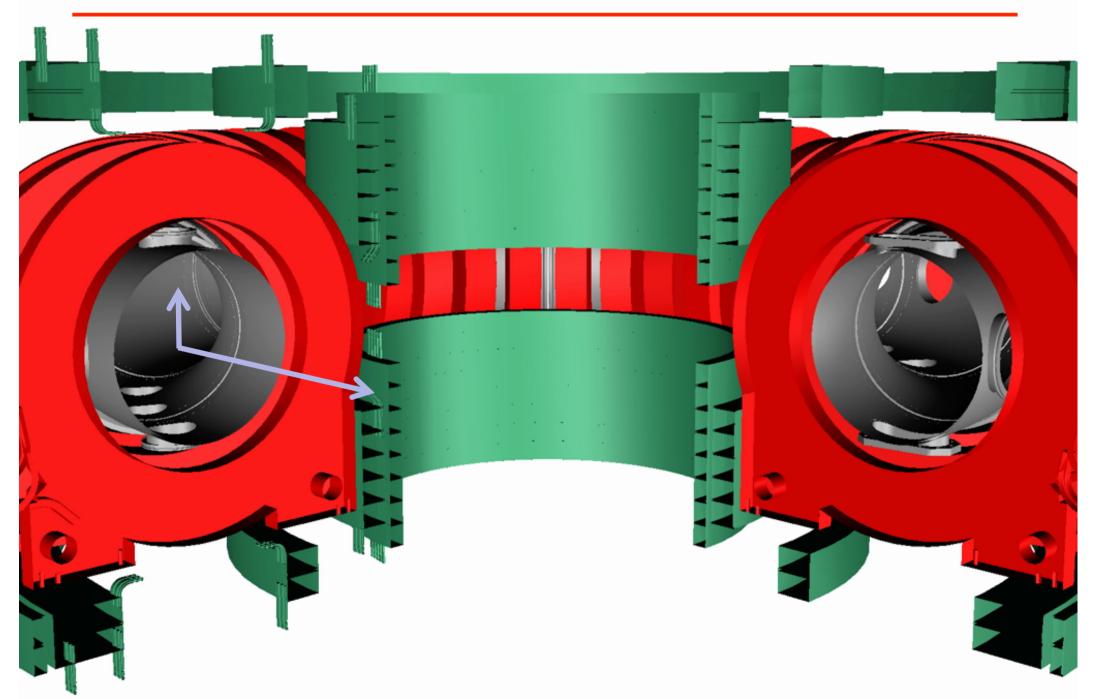


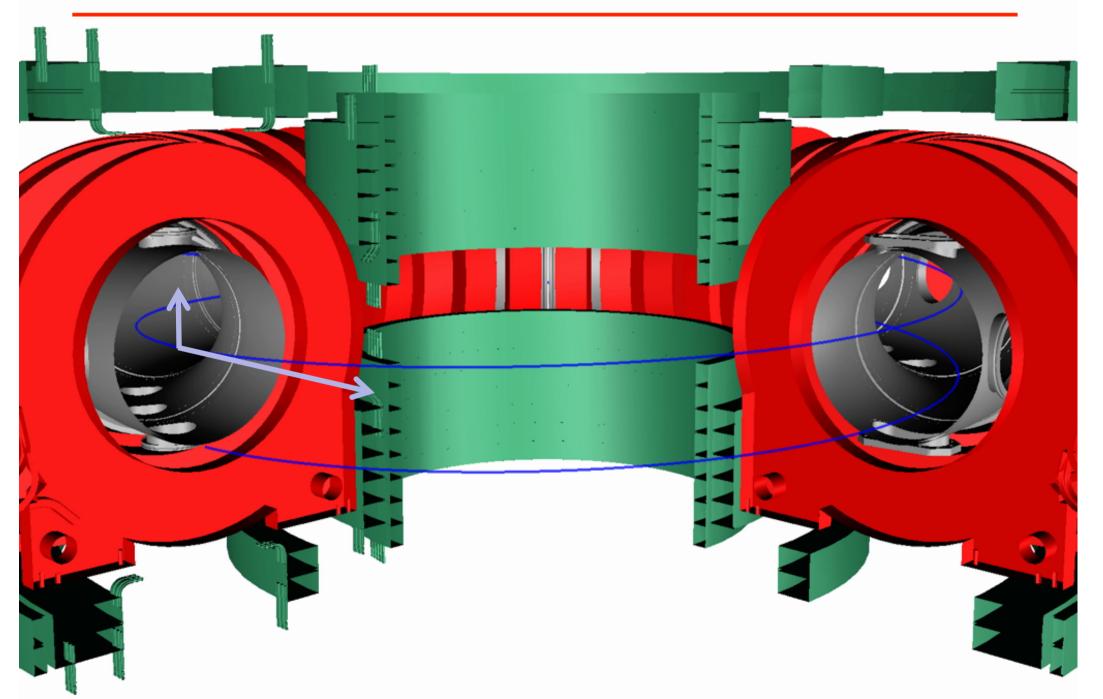


Fasoli et al., PoP 2006; PPCF 2010

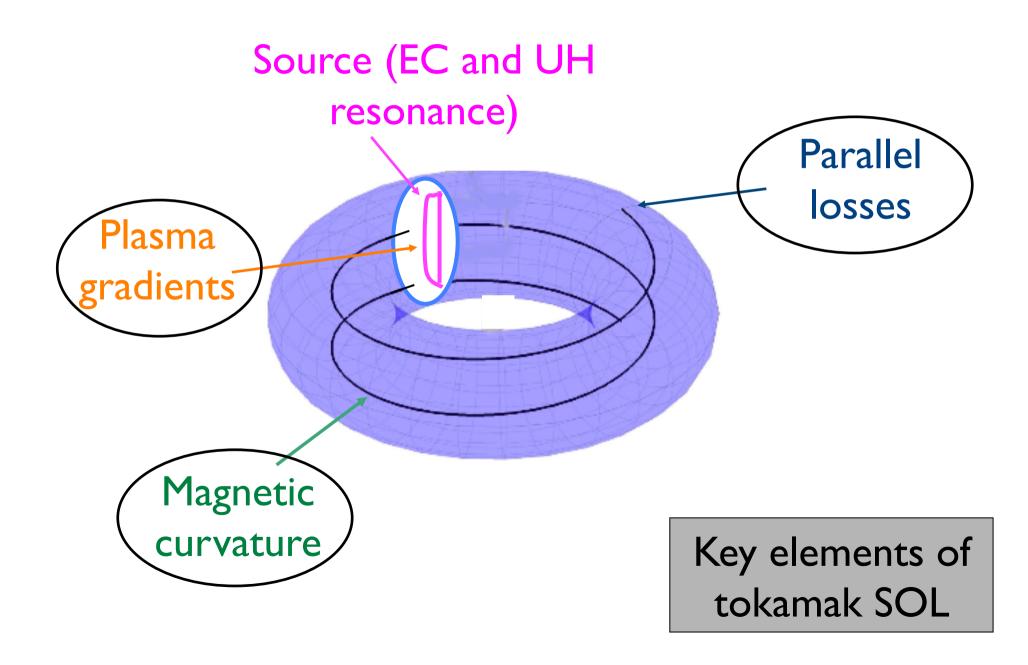




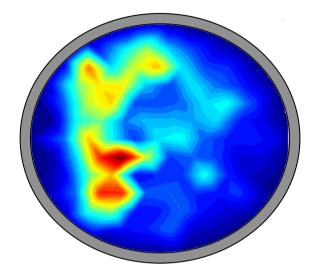




Key elements of the TORPEX device

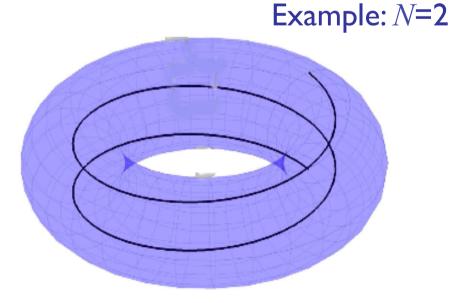


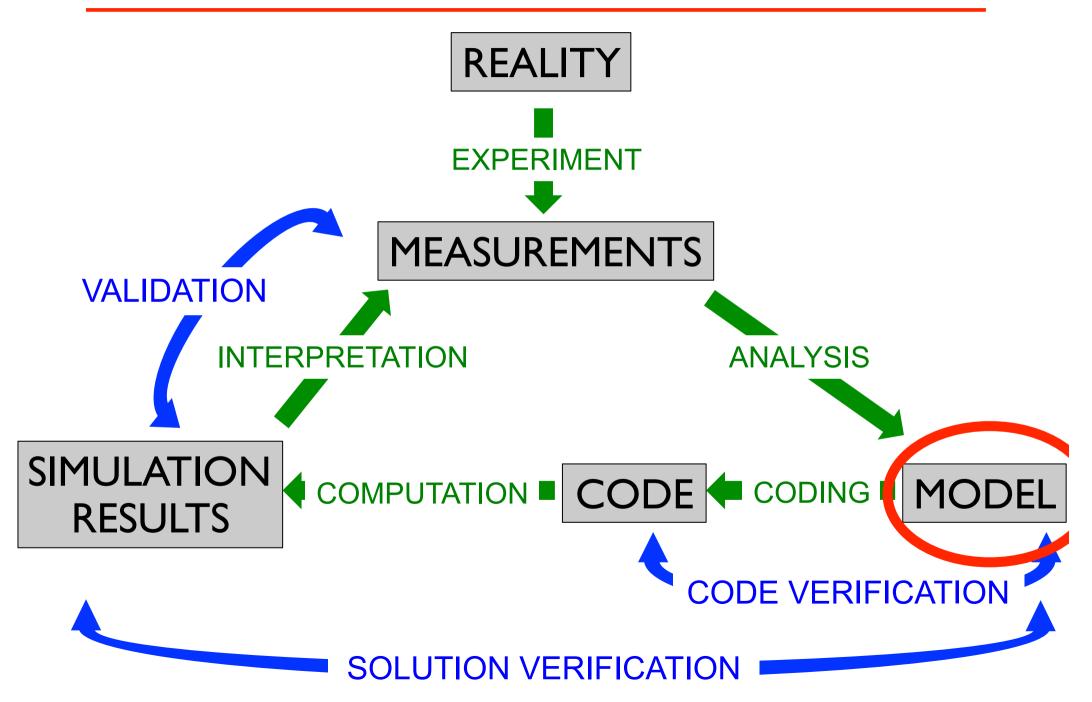
TORPEX: an ideal verification & validation testbed



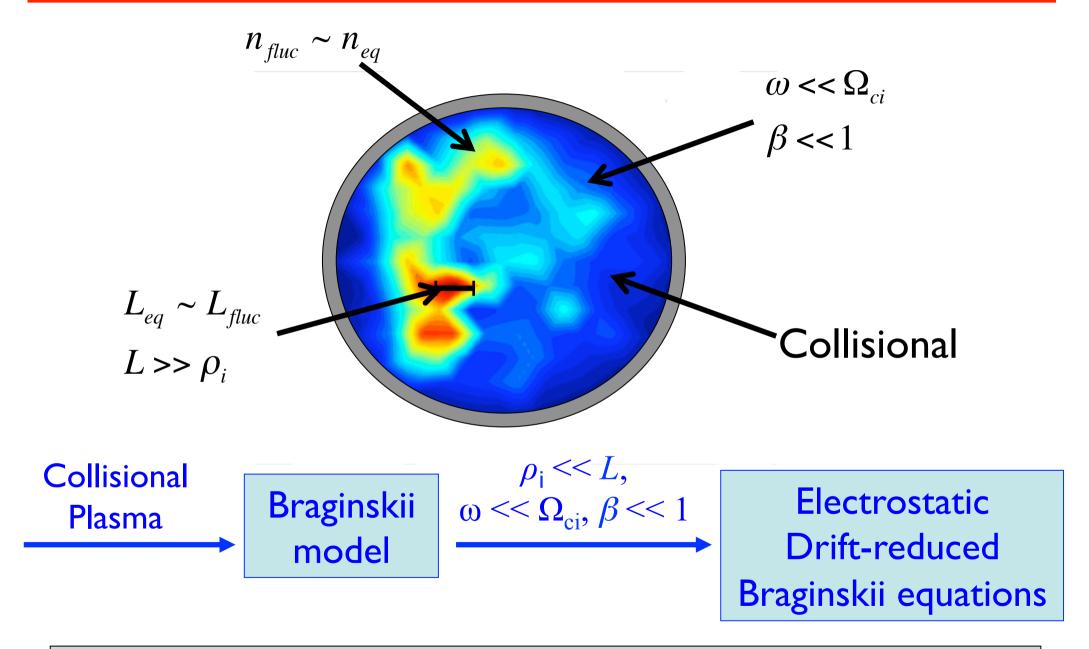
- Complete set of diagnostics, full plasma imaging possible

- Parameter scan, N- number of field line turns

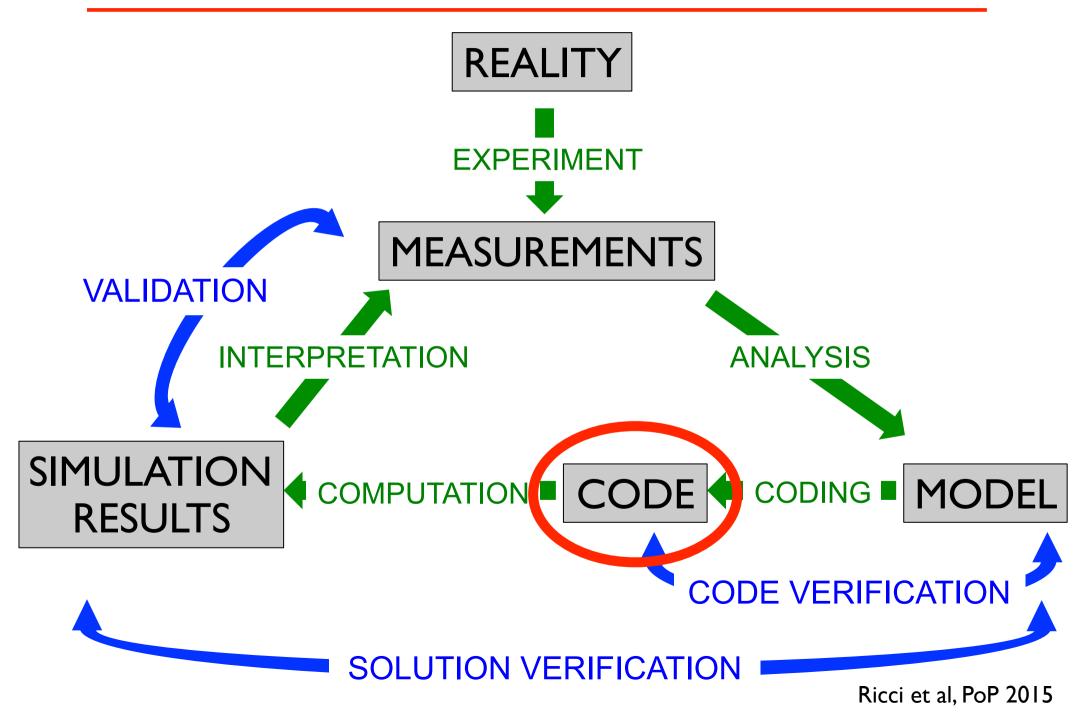


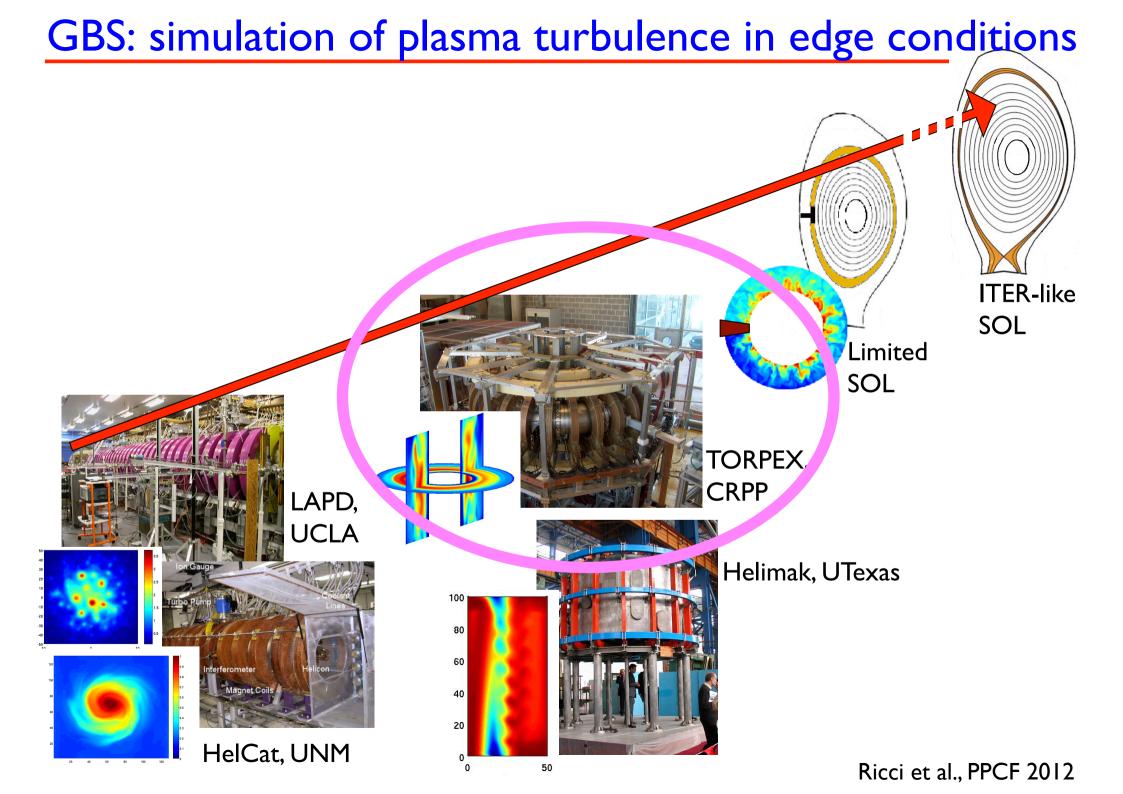


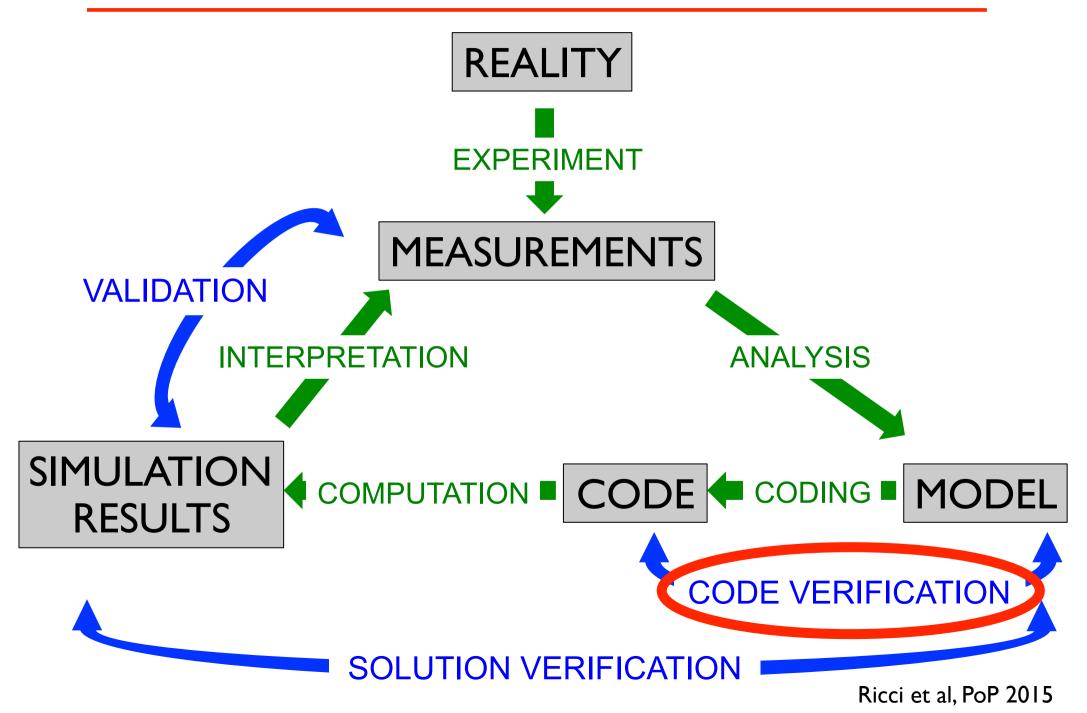
The model

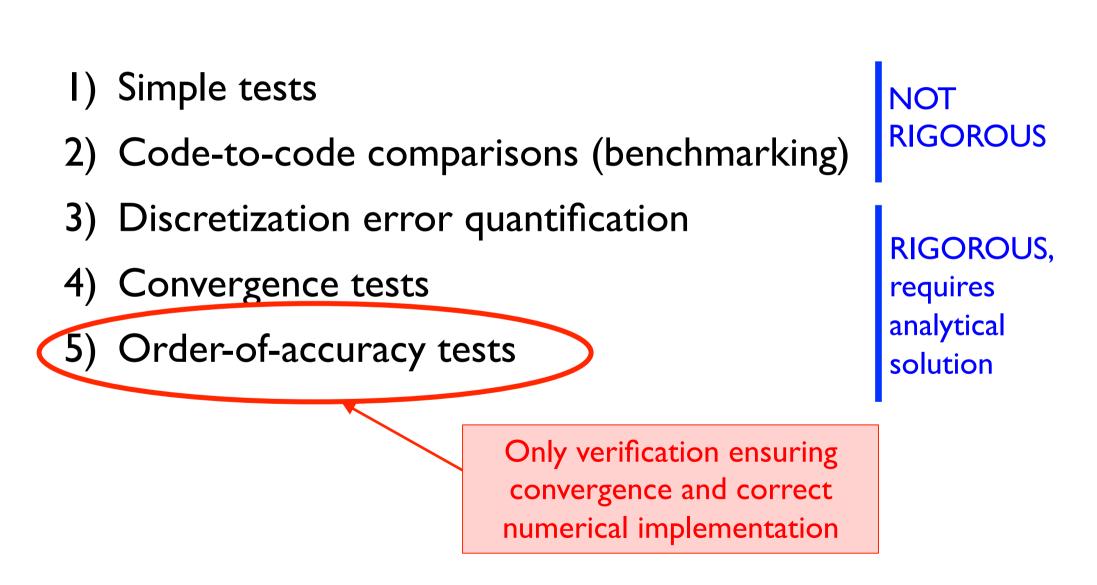


No separation between equilibrium and fluctuations







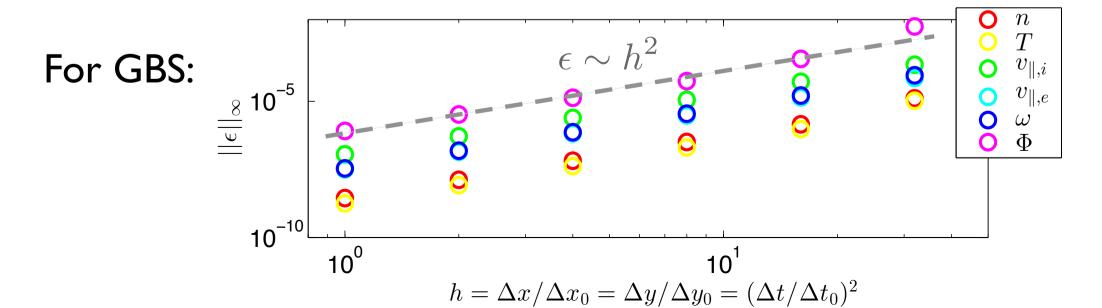


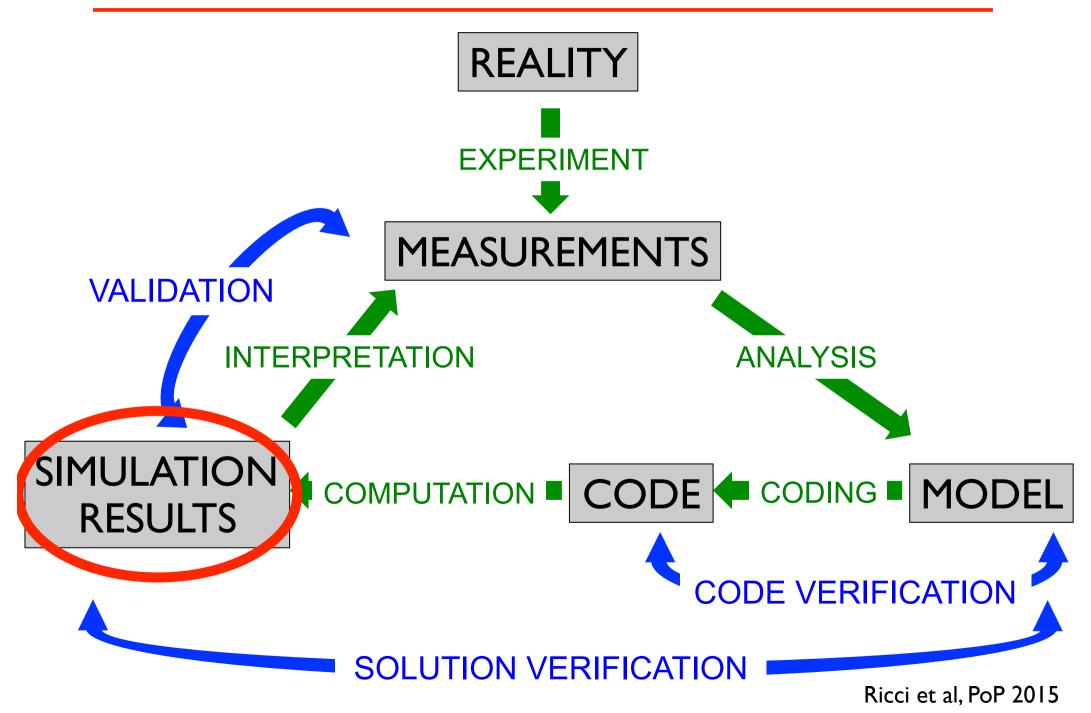
Order-of-accuracy tests, method of manufactured solution

Our model:
$$A(f) = 0$$
, f unknown
Ne solve $A_n(f_n) = 0$, but $\epsilon_n = f_n - f = ?$

Method of manufactured solution:

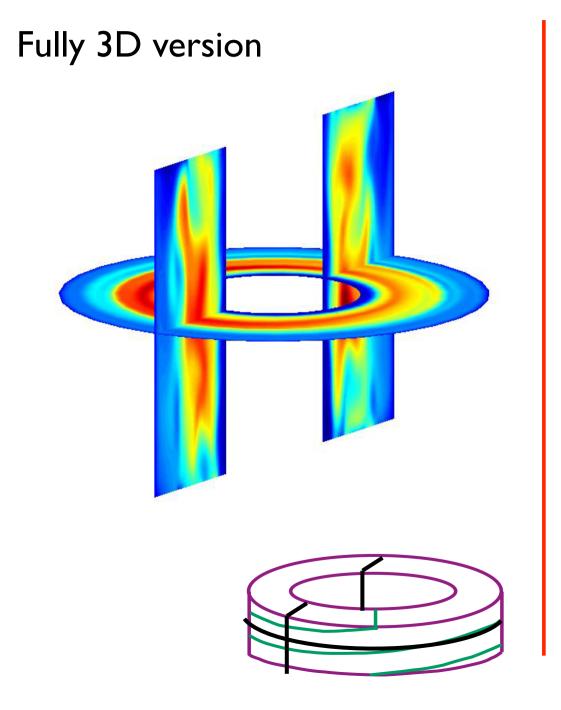
I) we choose
$$g$$
, then $S = A(g)$
2) we solve: $A_n(g_n) - S = 0$



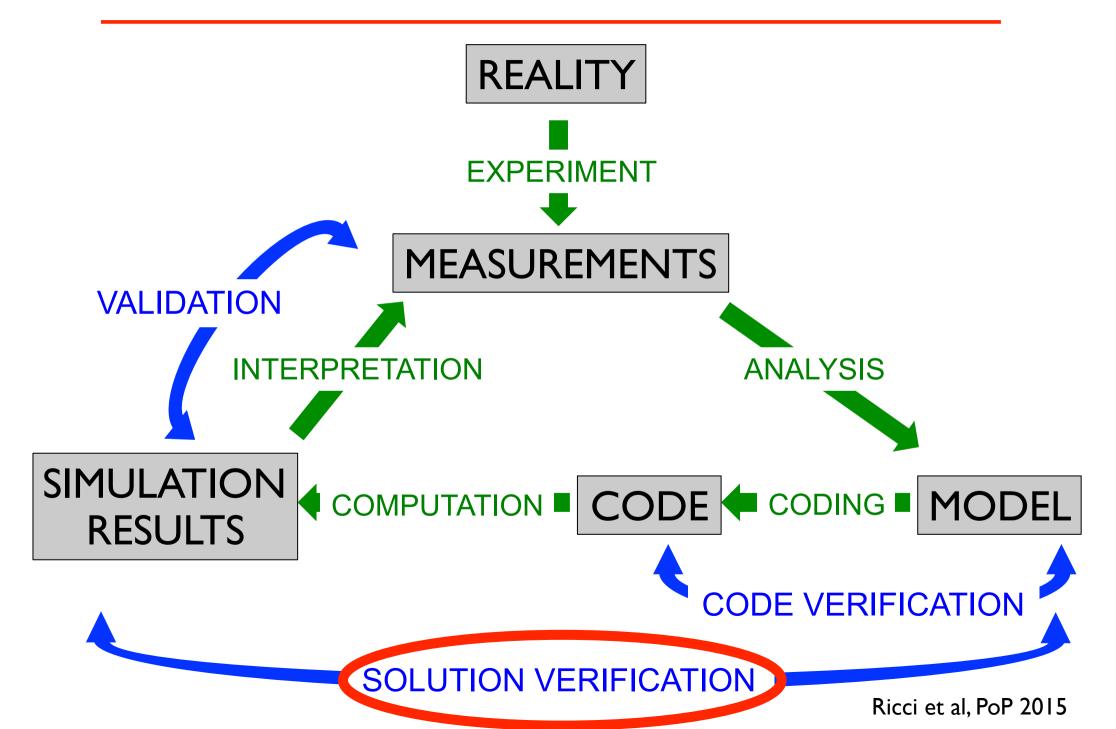


3D and 2D GBS simulations

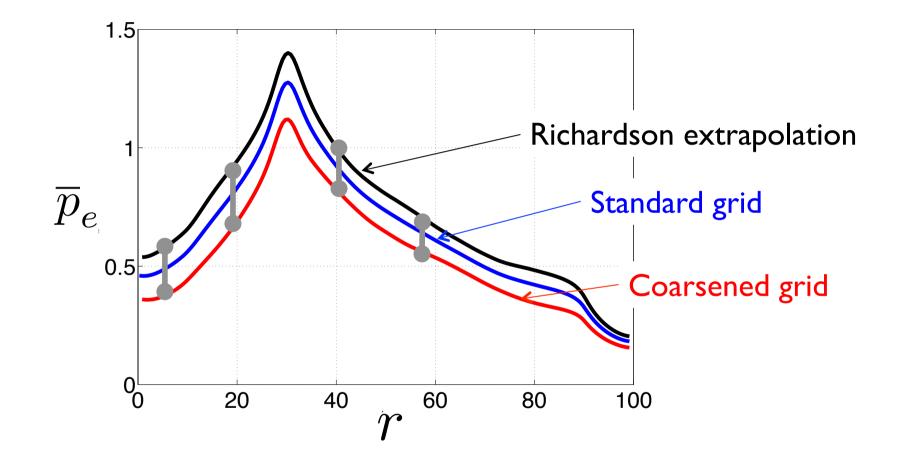
Ζ



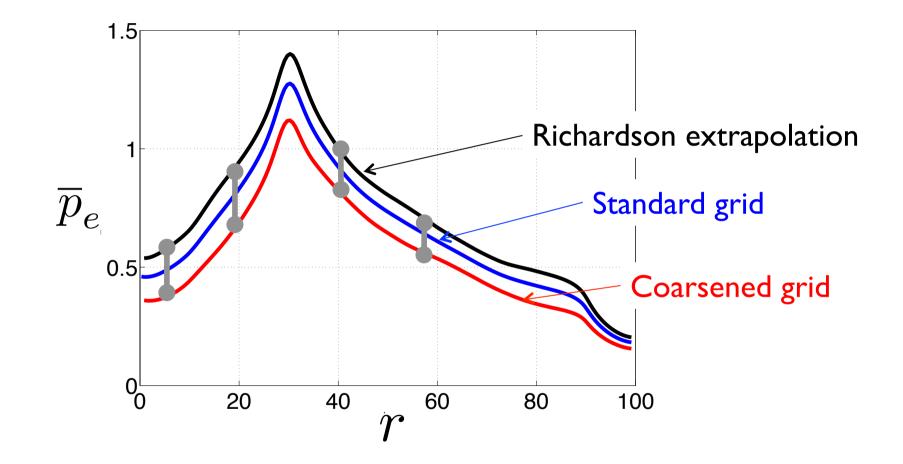
2D version (k_{\parallel} =0 hypothesis)



Solution verification, Richardson extrapolation

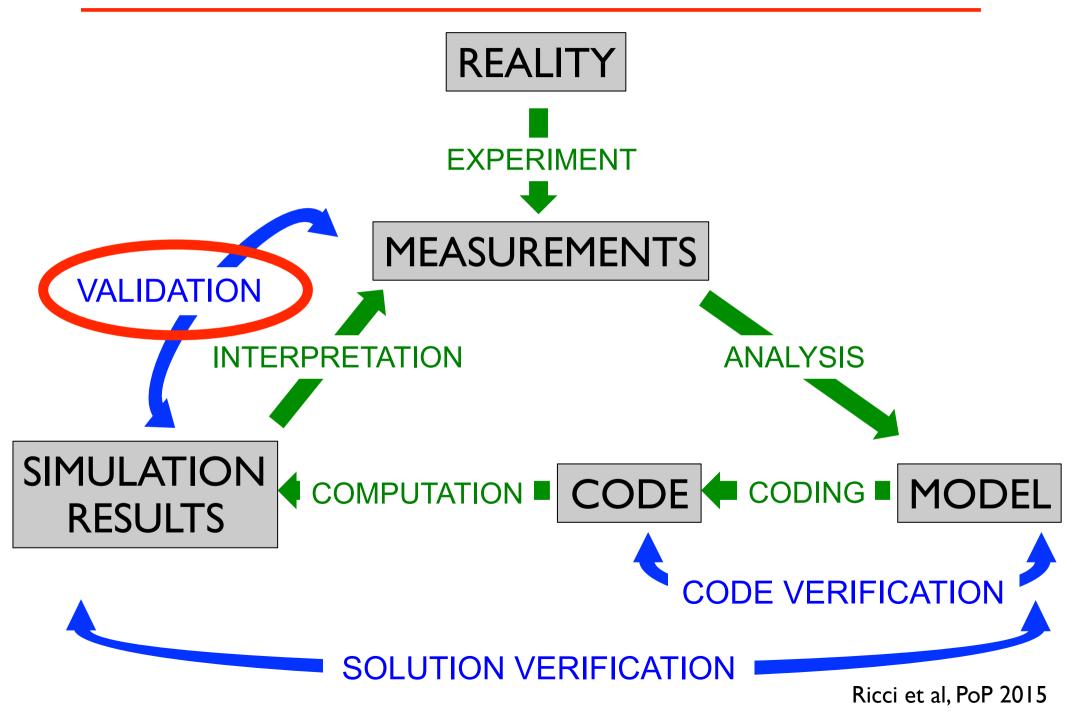


Solution verification, Richardson extrapolation



Use Roache's GCI error estimate if far from convergence

Riva et al., PoP 2014

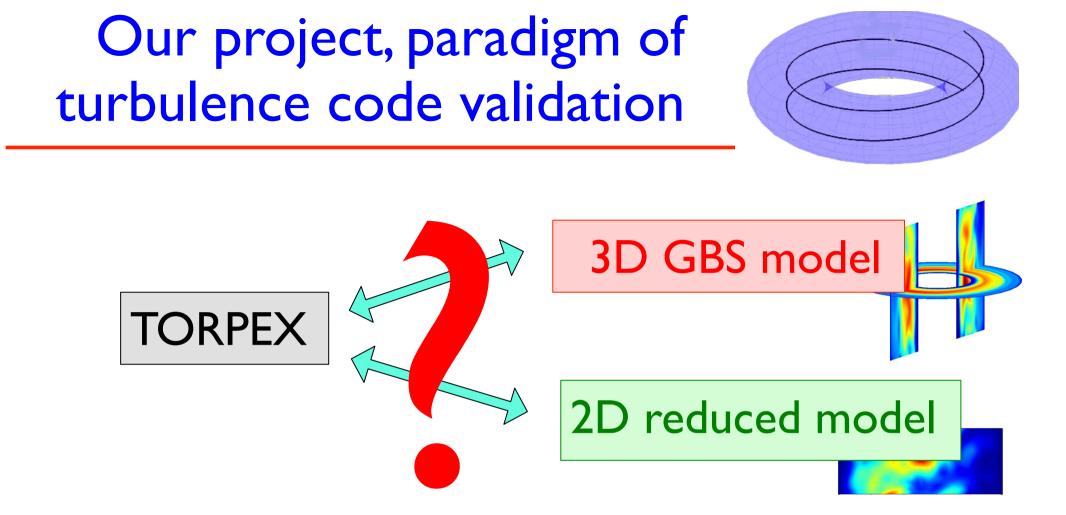


Validation goals

- Make progress in physics understanding
- Compare experiments and simulations to assess physics of the model
- Consider different models and parameter scans to guide us to key physics



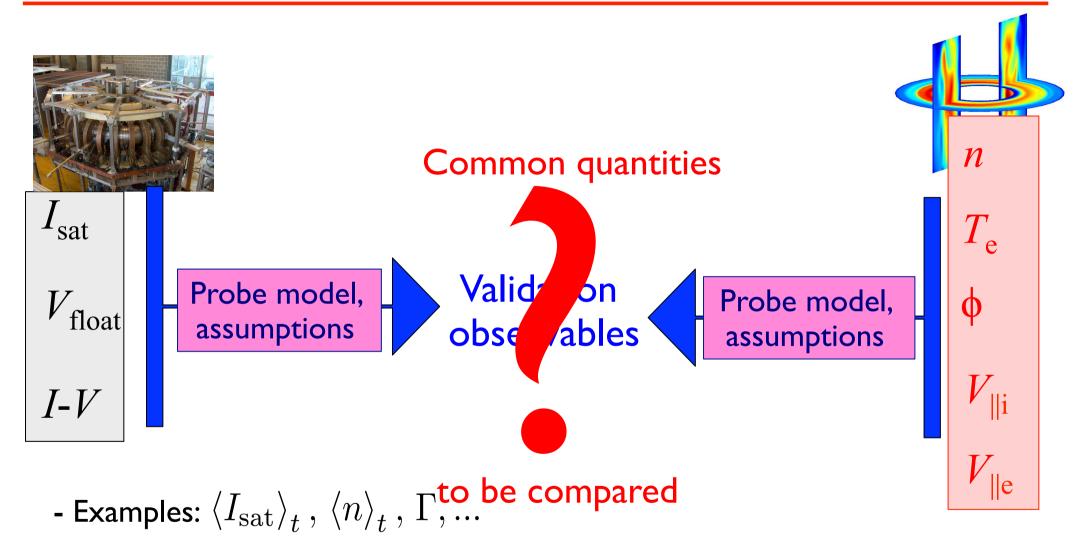
- Avoid fortuitous agreement
- Rigorous tool, but easy to use



- For the 2 codes, what is the agreement of experiment and simulations as a function of N?
- Are 3D effects important? Role of 3D in TORPEX physics?

Methodology based on ideas of Terry et al., PoP 2008; Greenwald, PoP 2010

Definition of the validation observables

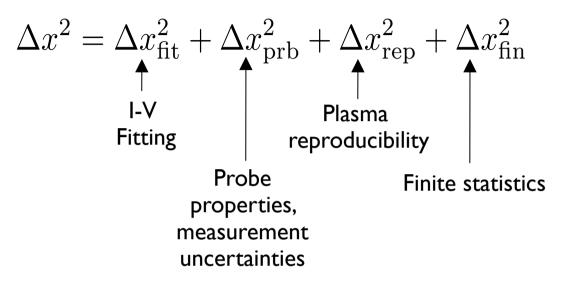


- A validation observable should not be a function of the others
- -11 observables for our validation:

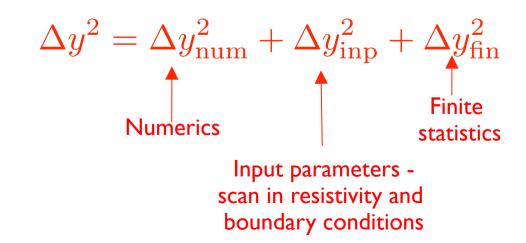
 $\langle n(r) \rangle_t$, $\langle T_e(r) \rangle_t$, $\langle I_{\text{sat}}(r) \rangle_t$, $\delta I_{\text{sat}}/I_{\text{sat}}$, k_v , $\text{PDF}(I_{\text{sat}})$, ...

Uncertainty analysis

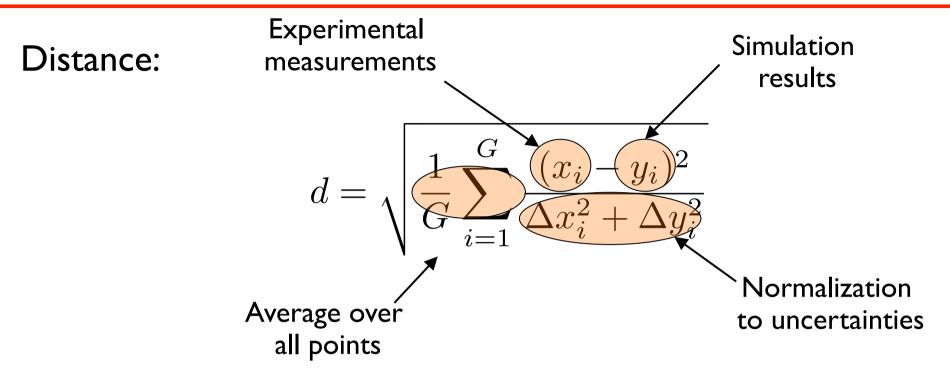
Experiment



Simulation



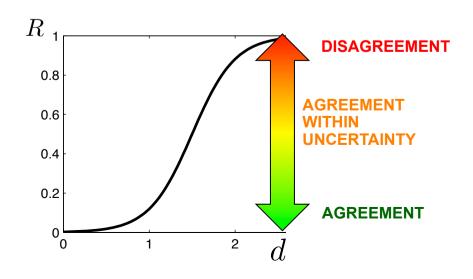
Agreement with respect to an individual observable



Level of agreement:

$$R = \frac{\tanh[(d-d_0)/\lambda] + 1}{2}$$

$$d_0 = 1.5$$
$$\lambda = 0.5$$



Observable hierarchy

Not all the observables are equally worthy...

The hierarchy assesses the assumptions used for their deduction

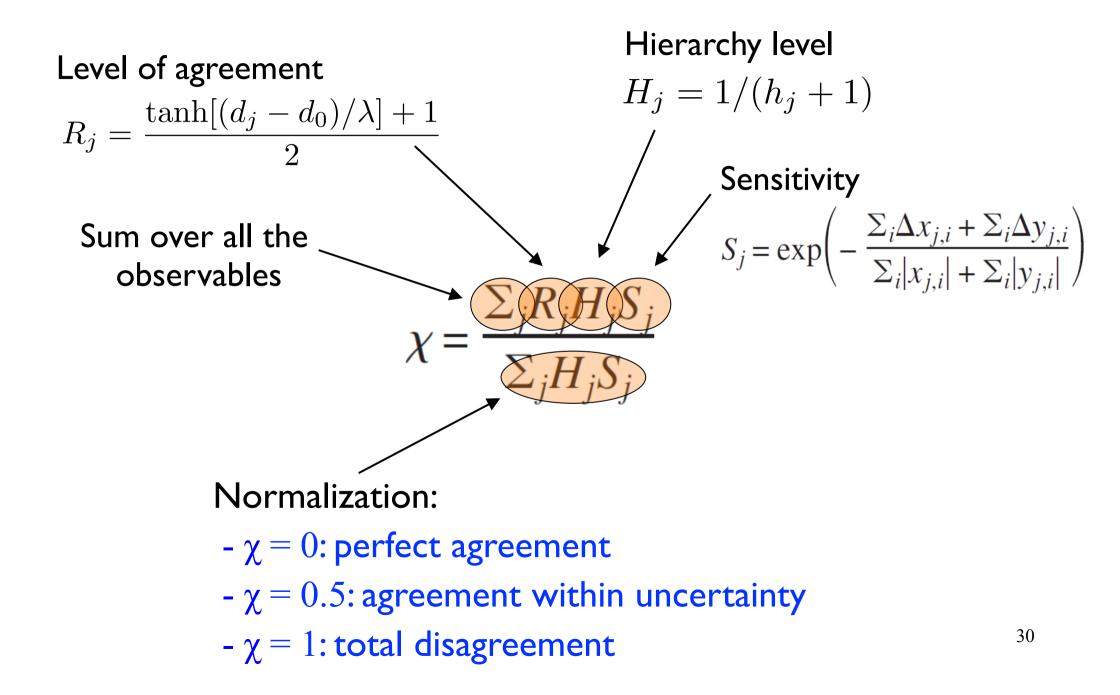
 h^{\exp} : # of assumptions to get the observable from experimental data

$$h^{sim}$$

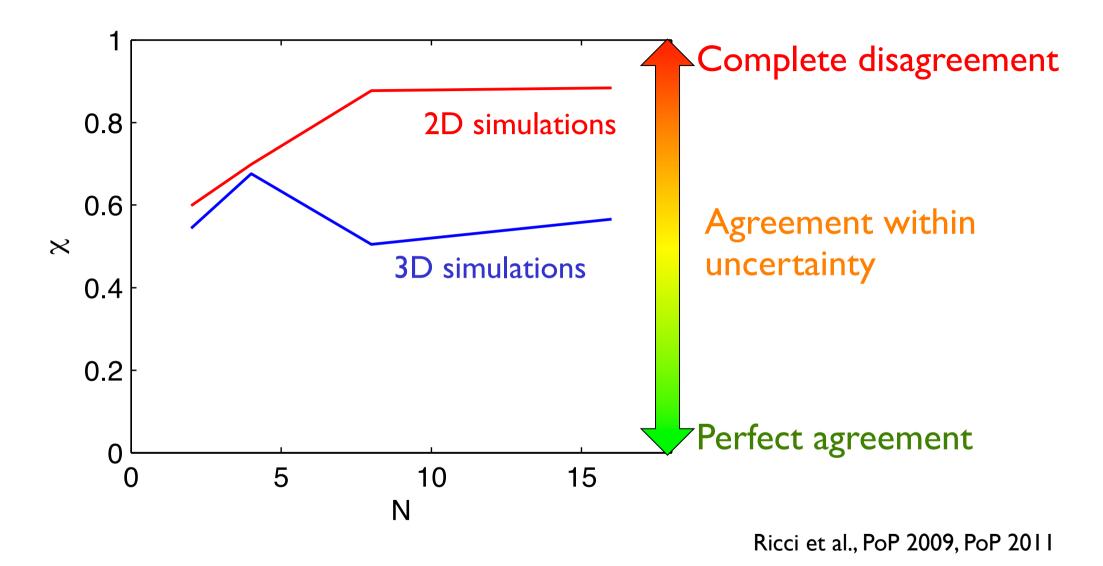
results

Examples:
$$-\langle n \rangle_t$$
 : $h^{\exp} = 1$, $h^{\sin} = 0$, $h = 1$
- $\Gamma_{I_{\text{sat}}}$: $h^{\exp} = 2$, $h^{\sin} = 1$, $h = 3$

Composite metric



The validation results



Why 2D and 3D work equally well at low N and 2D fails at high N? What can we learn on the TORPEX physics?

Flute instabilities - ideal interchange mode

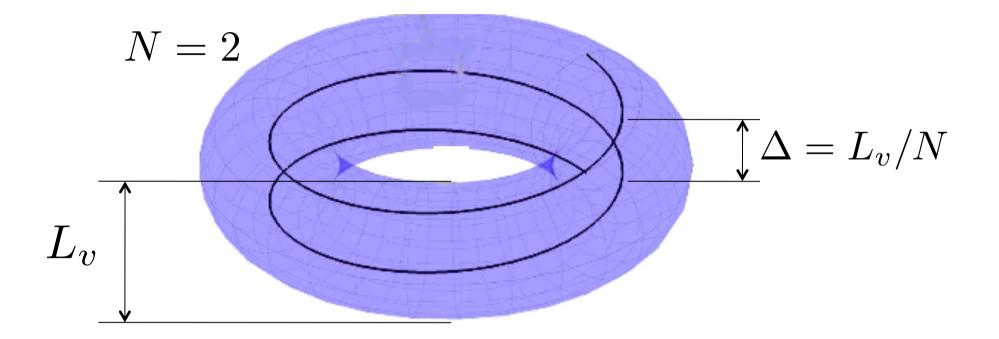
 $k_{\parallel} = 0 \implies$

$$n + T_{e} \text{ eqs.} \longrightarrow \frac{\partial p_{e}}{\partial t} = \frac{c}{B} [\phi, p_{e}]$$
Vorticity eq. $\longrightarrow \frac{\partial \nabla_{\perp}^{2} \phi}{\partial t} = \frac{2B}{cm_{i}Rn} \frac{\partial p_{e}}{\partial y}$

$$\implies \gamma = \gamma_I \qquad \gamma_I = c_s \sqrt{\frac{2}{L_p R}}$$

Compressibility stabilizes the mode at $k_v \rho_s > 0.3 \gamma_I R/c_s$

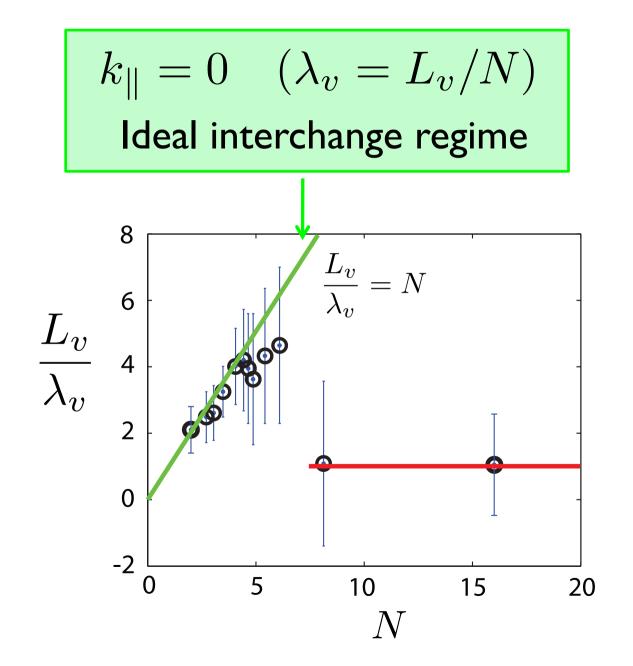
Anatomy of a $k_{\parallel} = 0$ perturbation



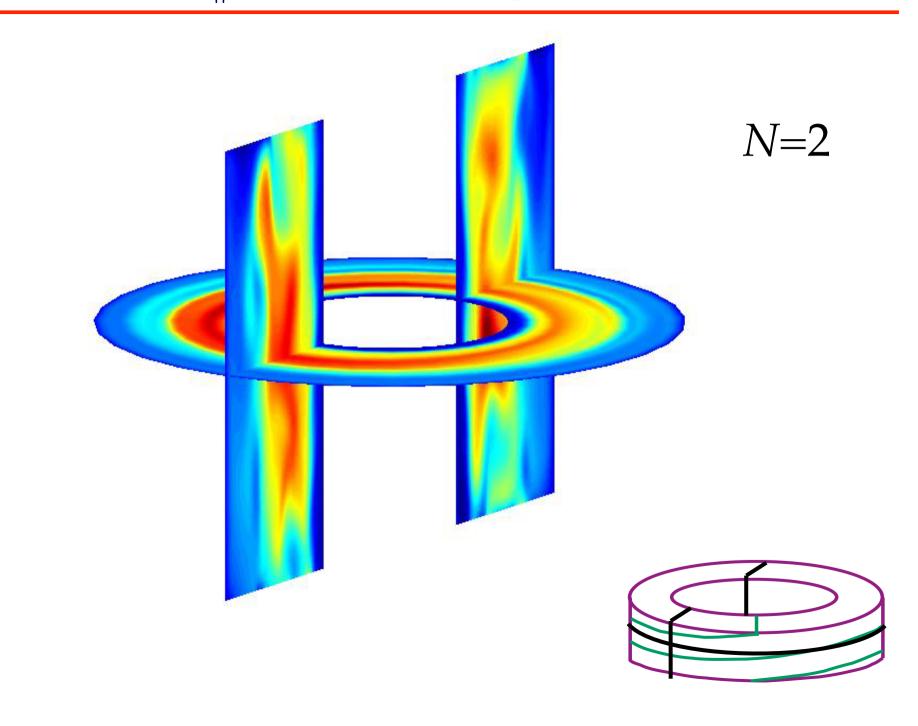
 λ_v : longest possible vertical wavelength of a perturbation

If
$$k_{\parallel} = 0$$
 then $\lambda_v = \Delta = \frac{L_v}{N}$

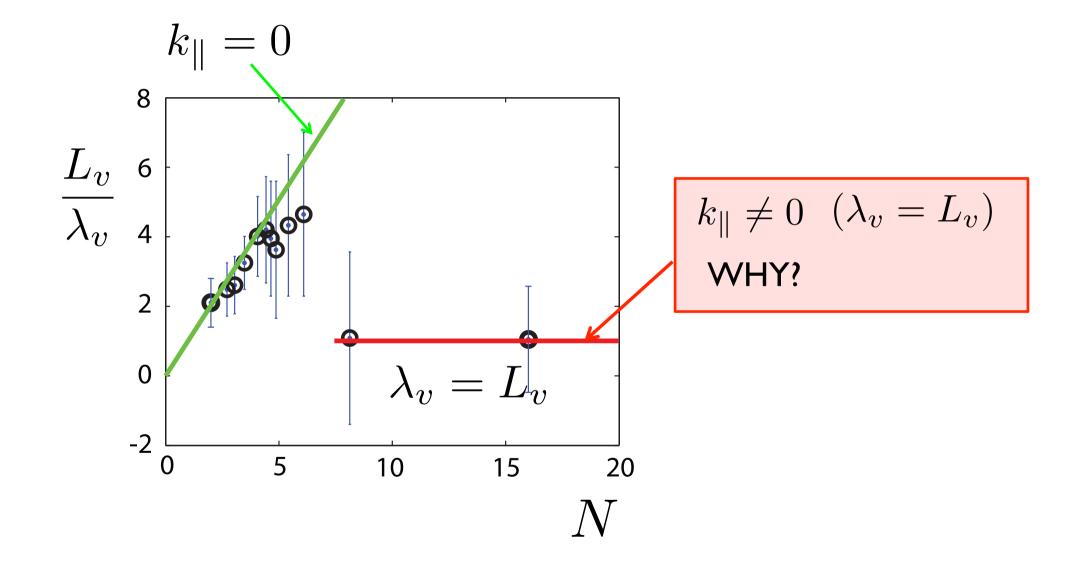
TORPEX shows $k_{\parallel} = 0$ turbulence at low N



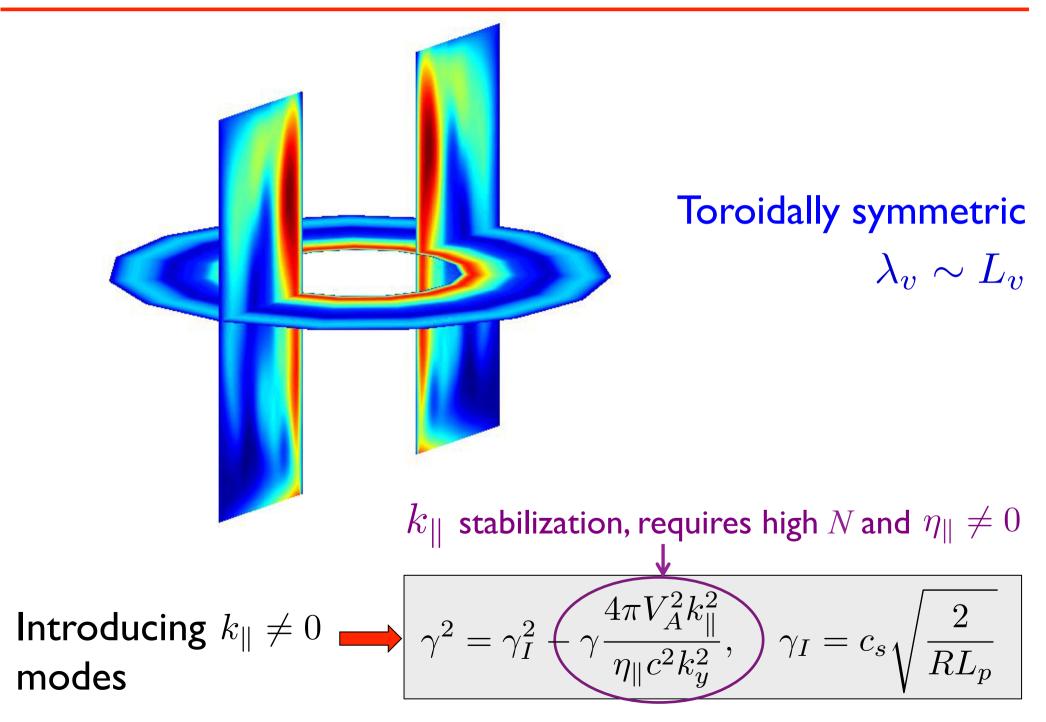
For $N \sim 1-6$, ideal $k_{\parallel} = 0$ interchange modes dominant



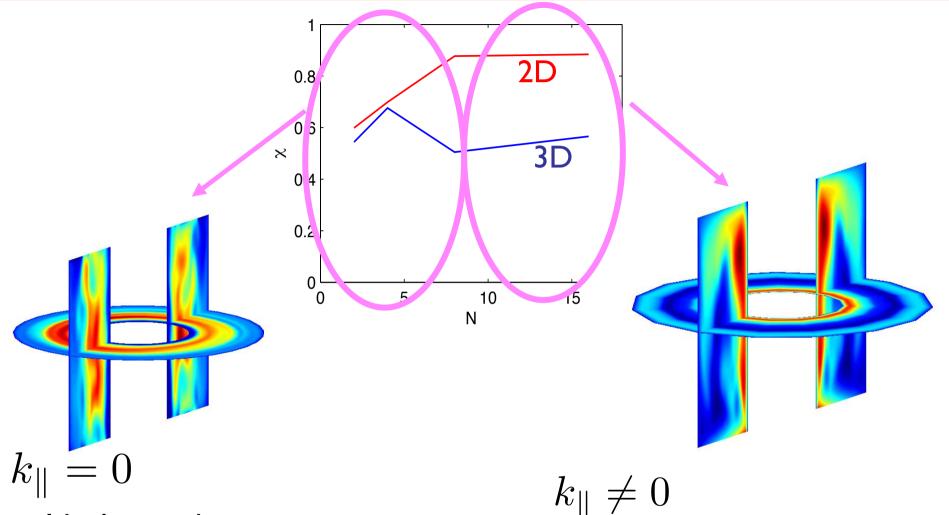
Turbulence changes character at N>7



At high N>7, Resistive Interchange Mode turbulence



Interpretation of the validation results

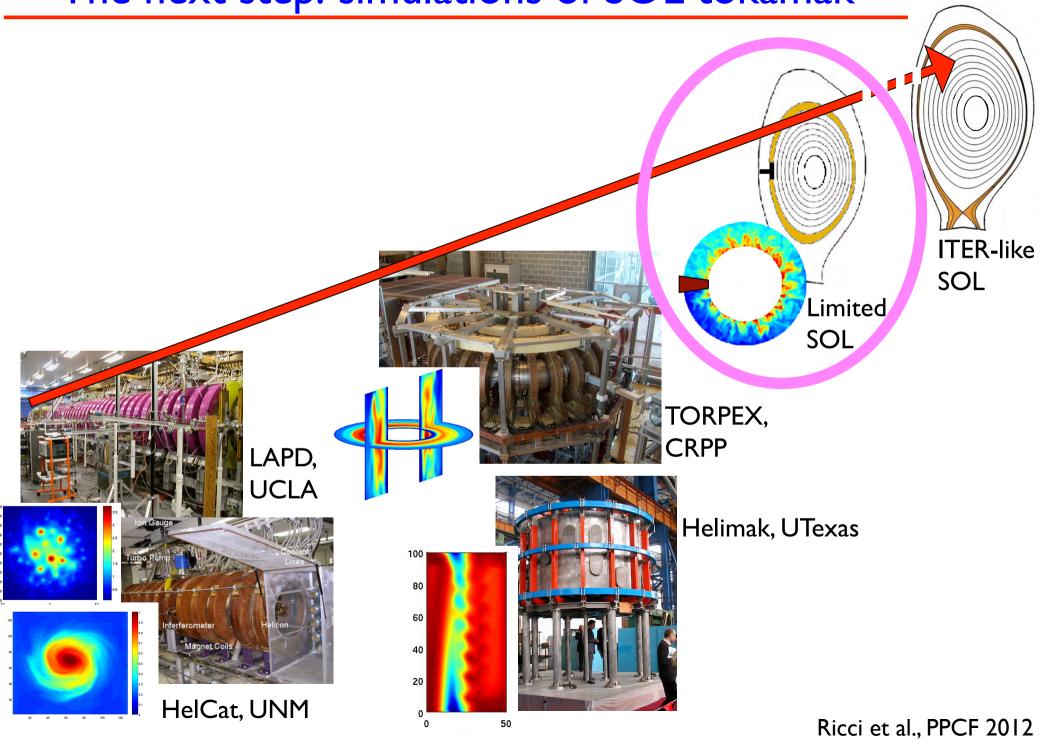


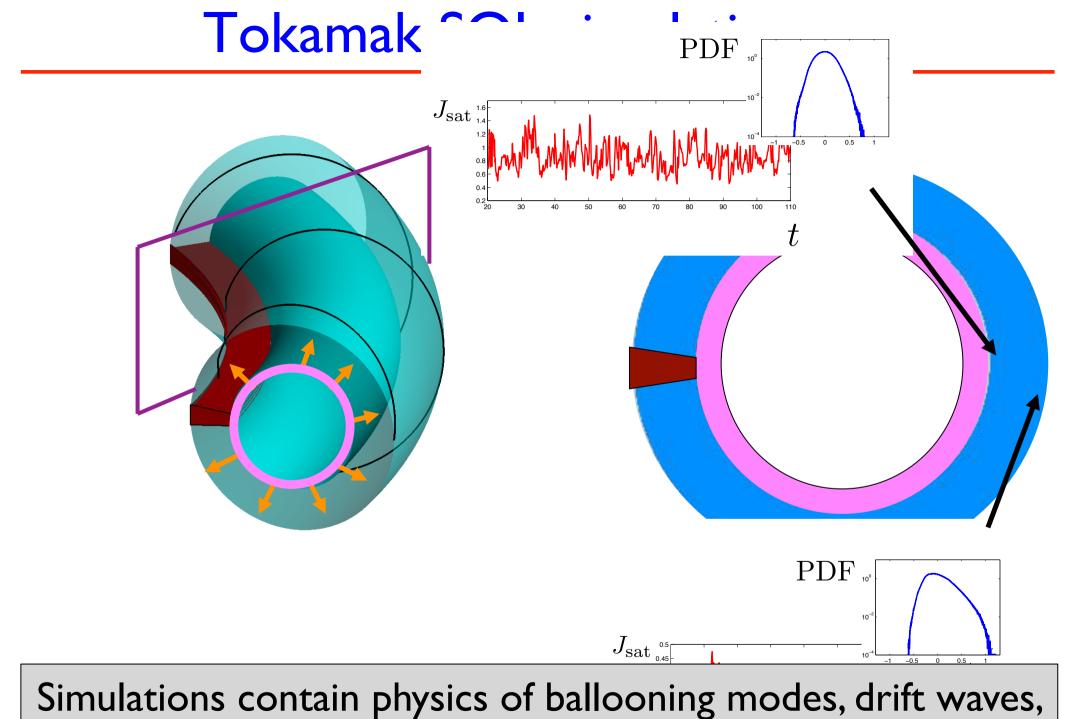
- Ideal interchange turbulence
- 2D model appropriate

Ricci & Rogers, PRL 2010

- Compressibility stabilizes ideal interchange
- Resistive interchange turbulence
- 2D model not appropriate

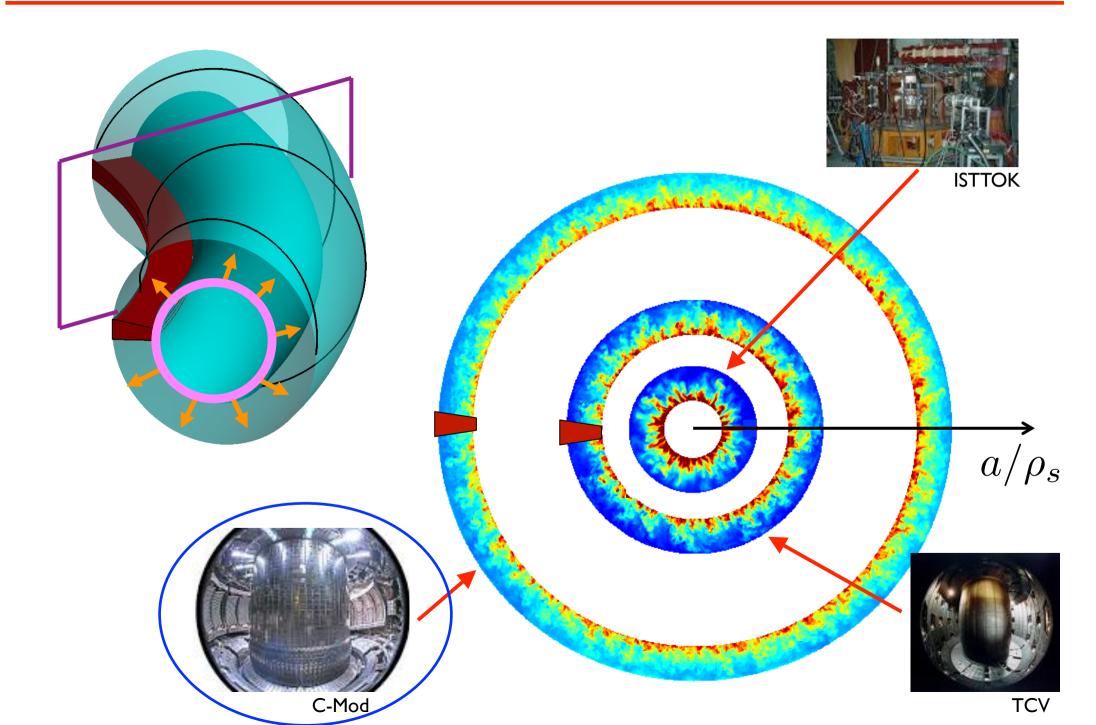
The next step: simulations of SOL tokamak

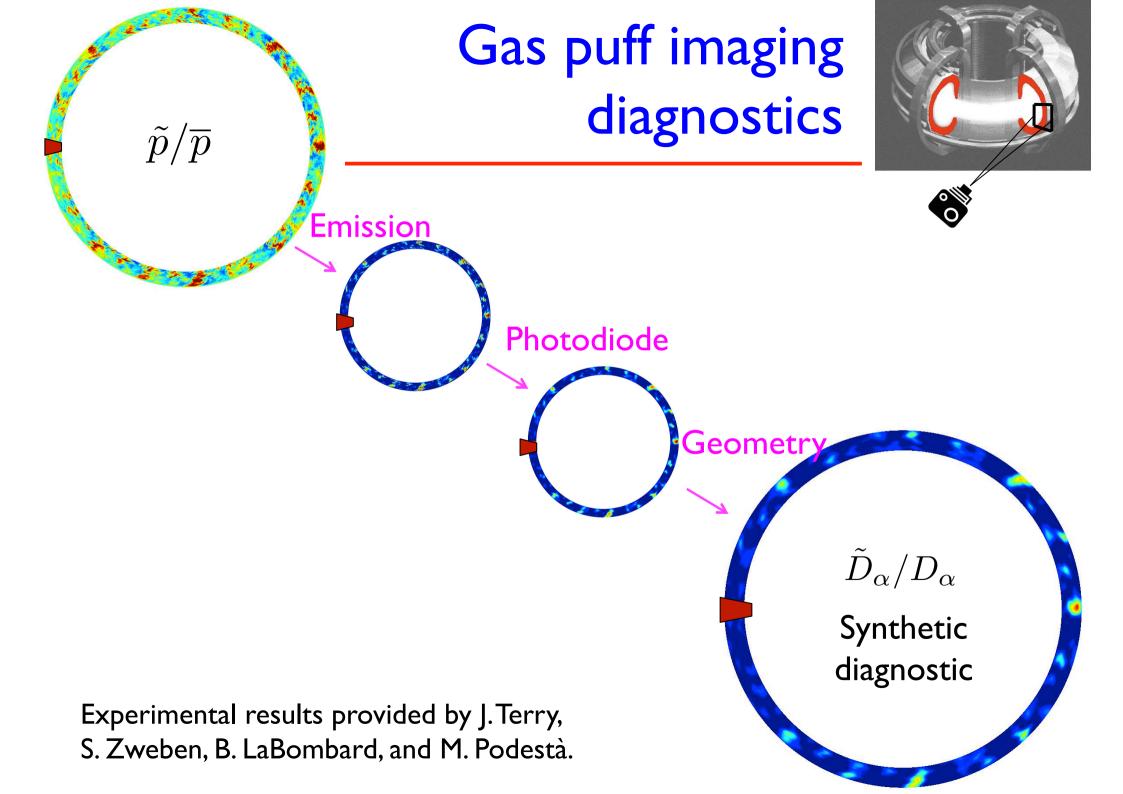




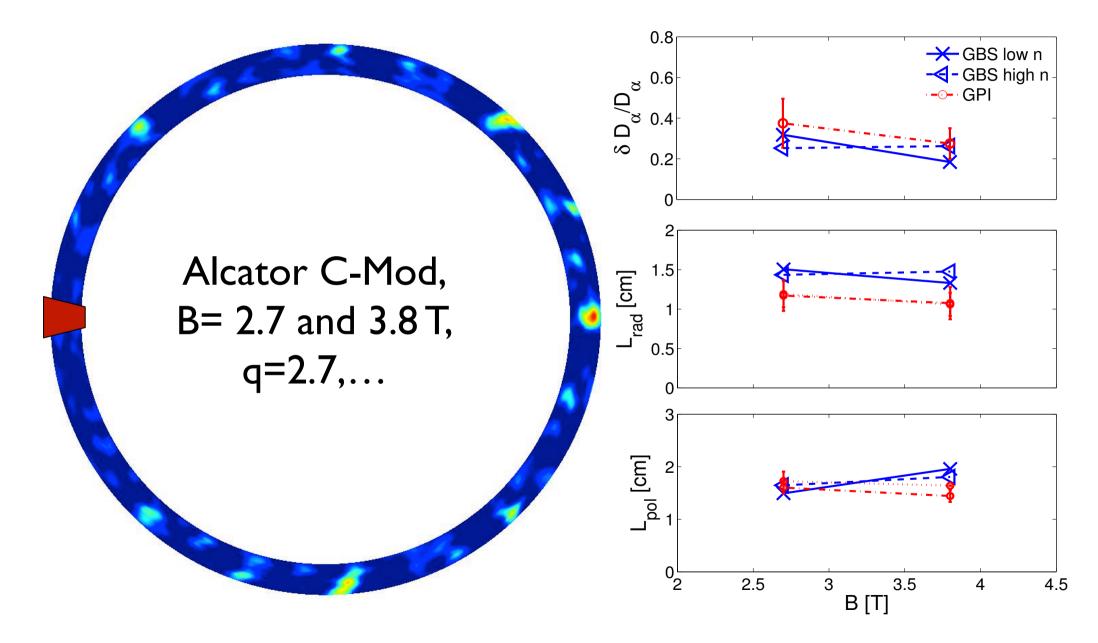
Kelvin-Helmholtz, blobs, parallel flows, sheath losses...

GBS simulations of tokamaks in limited configurations





C-Mod fluctuation properties well captured



Halpern et al, PPCF 2015

Where can a Verification & Validation exercise help?

I. Make sure that the code works correctly, and asses the numerical error

The correct implementation of GBS rigorously shown, the discretization error estimate for the quantity of interest estimated

2. Compare codes

2D and 3D simulations agree with experimental measurements similarly at low N.

Global 3D simulations are needed to describe the plasma dynamics at high N.

3. Let the physics emerge

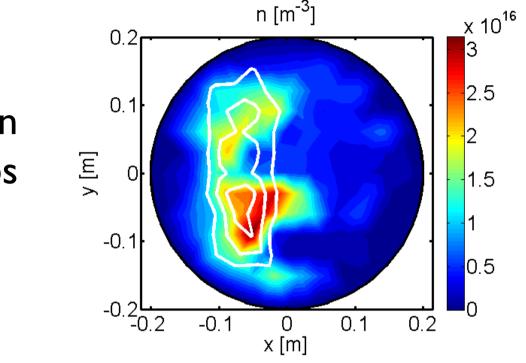
Two turbulent regimes: ideal interchange mode at low N and non-flute modes at high N.

Parameter scans have a crucial role



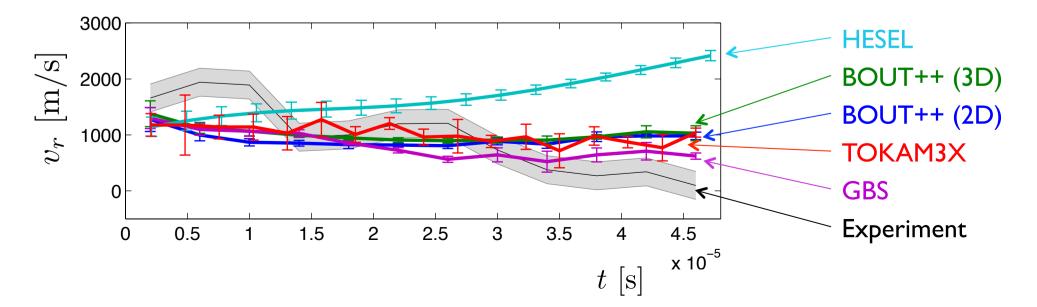


EU project for the validation of SOL turbulence codes



Multi-code validation against TORPEX blobs

EURO*fusion*



Where can a Verification & Validation exercise help?

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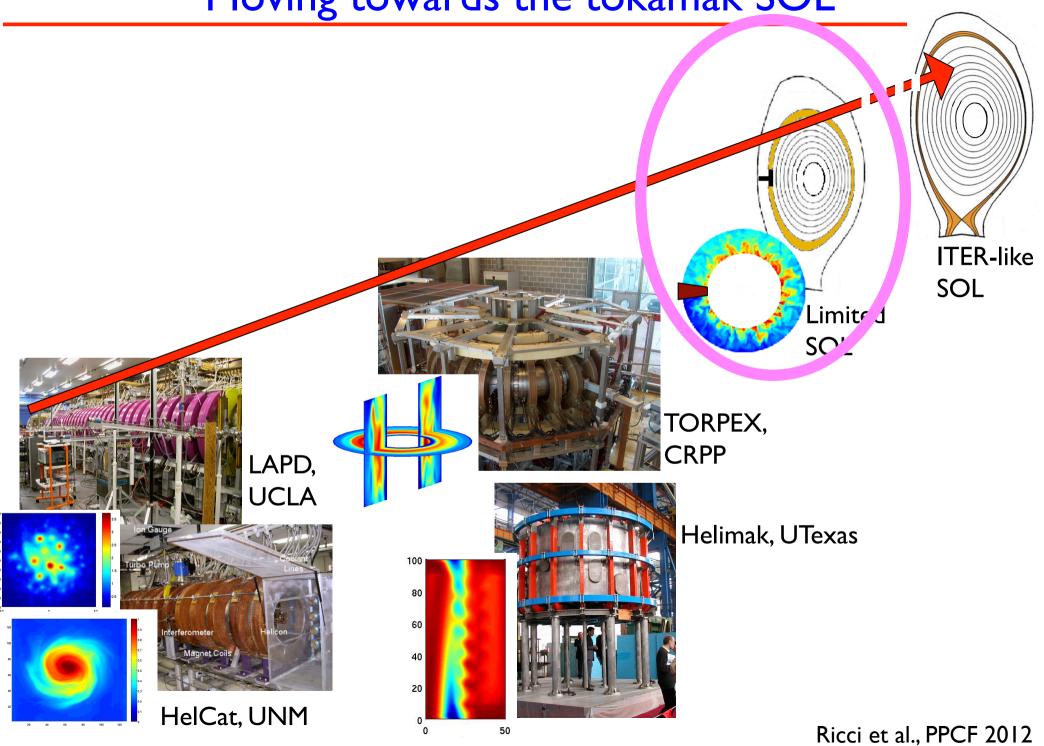
Two turbulent regimes: ideal interchange mode at low N and non-flute modes at high N.

Parameter scans have a crucial role





Moving towards the tokamak SOL



The validation methodology

[Based on ideas of Terry et al., PoP 2008; Greenwald, PoP 2010]

What quantities can we use for validation? The more, the better...

- Definition & evaluation of the validation observables

What are the uncertainties affecting measured and simulation data?

- Uncertainty analysis

For one observable, within its uncertainties, what is the level of agreement?

- Level of agreement for an individual observable

How directly can an observable be extracted from simulation and experimental data? How worthy is it, i.e. what should be its weight in a composite metric?

- The observable hierarchy

How to evaluate the global agreement and how to interpret it

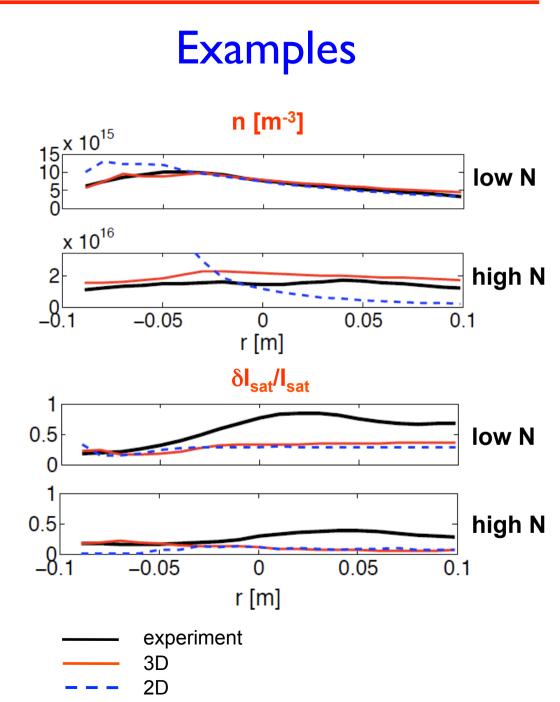
- Composite metric

Evaluation of the validation observables

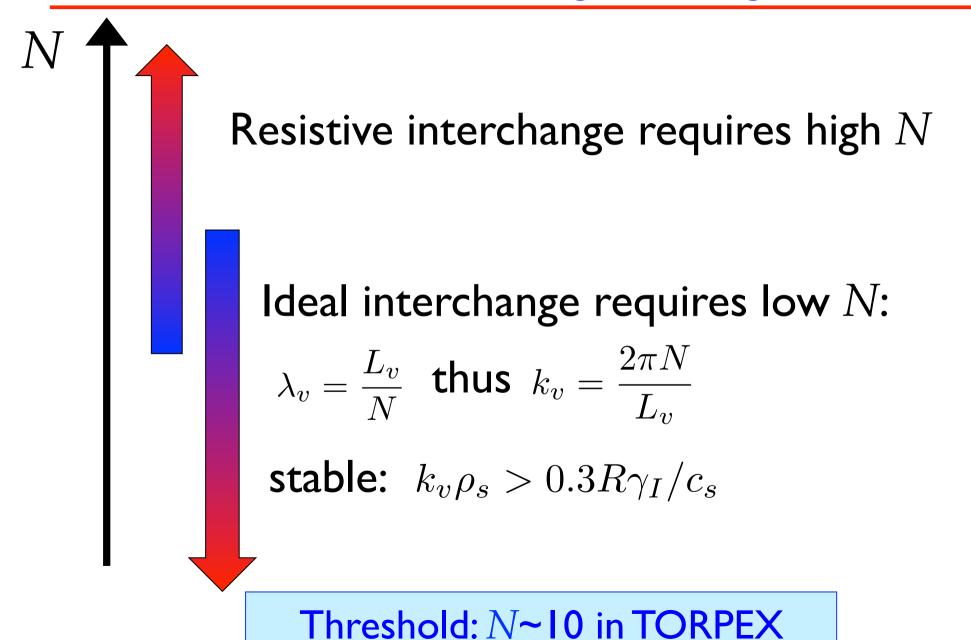
We evaluate 11 observables:

$$- \langle n(r) \rangle_t - \langle T_e(r) \rangle_t - \langle I_{sat}(r) \rangle_t - \delta I_{sat}/I_{sat} - k_v - PDF(I_{sat})$$

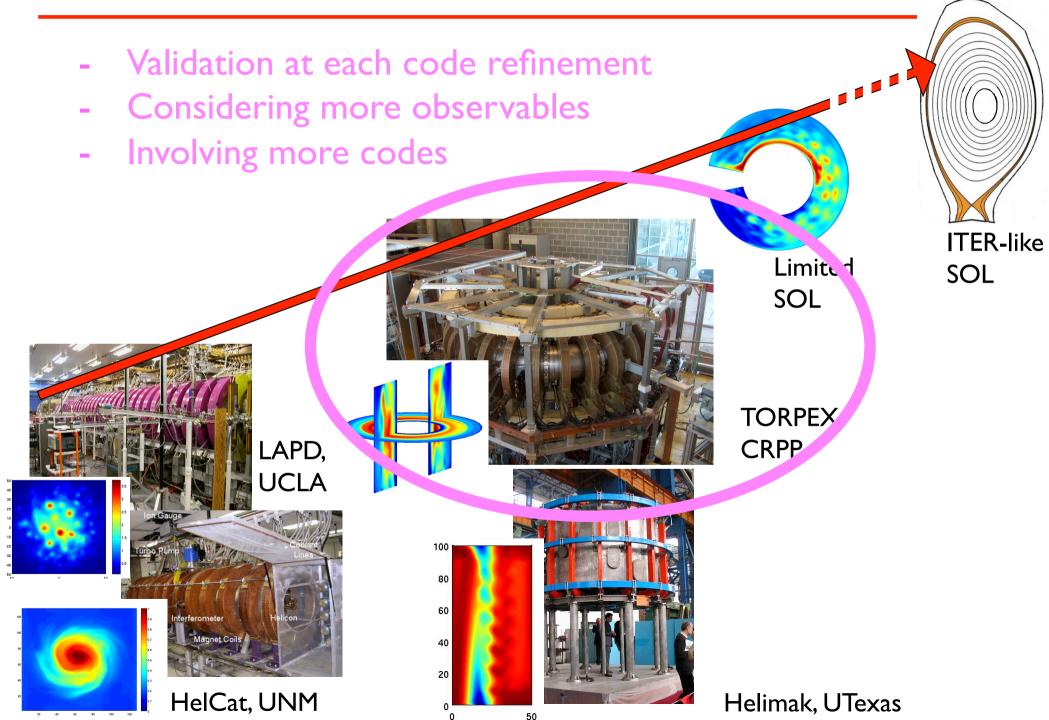
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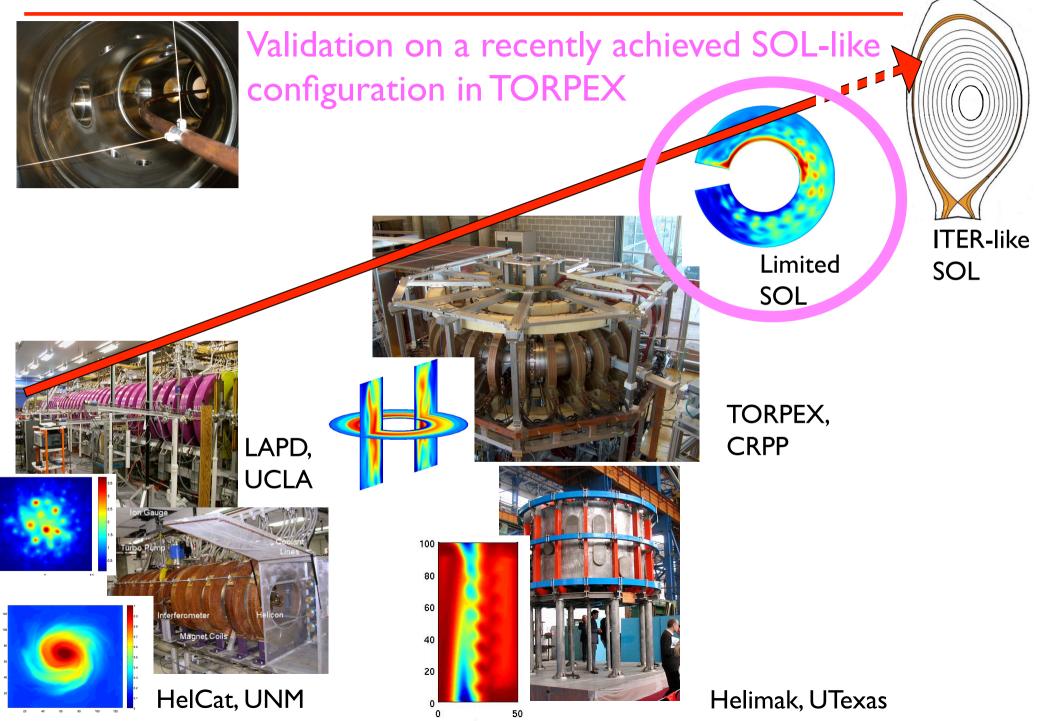
Why does TORPEX transition from ideal to resistive interchange for large N?



What comes next?



What comes next?



Where can a verification & validation exercise help?

I. Make sure that the code works correctly

Rigorously, with discretization error estimate

2. Compare codes

2D and 3D simulations agree with experimental measurements similarly at low N.

Global 3D simulations are needed to describe the plasma dynamics at high N.

3. Let the physics emerge

Two turbulent regimes: ideal interchange mode at low N and non-flute modes at high N.

Parameter scans have a crucial role

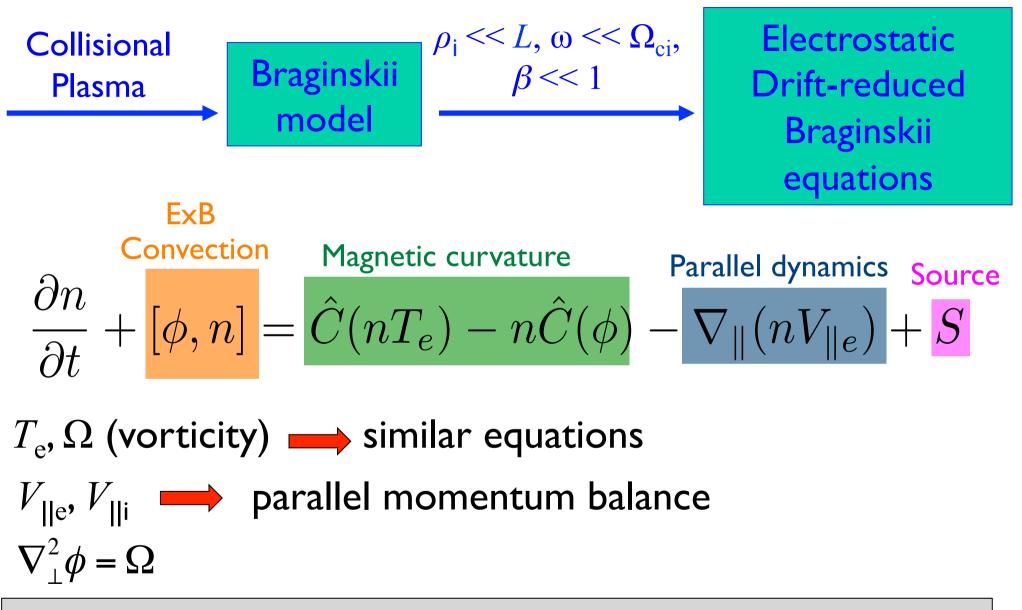
4. Assess the predictive capabilities of a code

3D simulations predict (within uncertainty) profiles of n but not of I_{sat}

CRPP



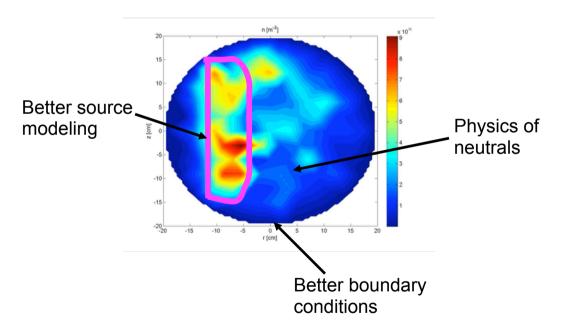
The model



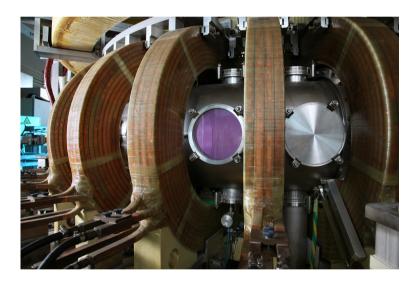
Quasi steady state – balance between: plasma source, perpendicular transport, and parallel losses

Future work

Missing ingredients for a complete description Use of more diagnostics: Mach probes, Triple of plasma dynamics in TORPEX:



probes or Bdot probes to compare other interesting observables.



V&V

A validation project requires a four step procedure:

- (i) Model qualification
- (ii) Code verification
- (iii) Definition and classification of observables
- (iv) Quantification of agreement

$$\frac{\partial n}{\partial t} = R[\phi, n] + 2\left(n\frac{\partial T_e}{\partial y} + T_e\frac{\partial n}{\partial y} - n\frac{\partial \phi}{\partial y}\right) + D_n \nabla_{\perp}^2 n$$
$$-n\frac{\partial V_{\parallel e}}{\partial z} - V_{\parallel e}\frac{\partial n}{\partial z} + S_n, \tag{1}$$

$$\frac{\partial \nabla_{\perp}^{2} \phi}{\partial t} = R[\phi, \nabla_{\perp}^{2} \phi] - V_{\parallel i} \frac{\partial \nabla_{\perp}^{2} \phi}{\partial z} + 2\left(\frac{T_{e}}{n} \frac{\partial n}{\partial y} + \frac{\partial T_{e}}{\partial y}\right) + \frac{1}{n} \frac{\partial j_{\parallel}}{\partial z} - \frac{\eta_{0i}}{n} \left(2\frac{\partial^{2} V_{\parallel i}}{\partial y \partial z} + \frac{\partial^{2} \phi}{\partial y^{2}}\right) + D_{\phi} \nabla_{\perp}^{4} \phi, \quad (2)$$

$$\frac{\partial T_e}{\partial t} = R[\phi, T_e] - V_{\parallel e} \frac{\partial T_e}{\partial z} + \frac{4}{3} \left(\frac{7}{2} T_e \frac{\partial T_e}{\partial y} + \frac{T_e^2}{n} \frac{\partial n}{\partial y} - T_e \frac{\partial \phi}{\partial y} \right) + D_T \nabla_{\perp}^2 T_e + \frac{2}{3} \frac{T_e}{n} 0.71 \frac{\partial j_{\parallel}}{\partial z} - \frac{2}{3} T_e \frac{\partial V_{\parallel e}}{\partial z} + S_T, \qquad (3)$$

$$\frac{m_e}{m_i} n \frac{\partial V_{\parallel e}}{\partial t} = \frac{m_e}{m_i} n R[\phi, V_{\parallel e}] - \frac{m_e}{m_i} n V_{\parallel e} \frac{\partial V_{\parallel e}}{\partial z} - T_e \frac{\partial n}{\partial z} + n \frac{\partial \phi}{\partial z}$$
$$- 1.71 n \frac{\partial T_e}{\partial z} + n \nu j_{\parallel} + \frac{4}{3} \eta_{0e} \frac{\partial^2 V_{\parallel e}}{\partial z^2} + \frac{2}{3} \eta_{0e} \frac{\partial^2 \phi}{\partial y \partial z}$$
$$- \frac{2}{3} \frac{\eta_{0e}}{n} \frac{\partial^2 p_e}{\partial z \partial y} + D_{V_e} \nabla_{\perp}^2 V_{\parallel e}, \qquad (4)$$

$$n\frac{\partial V_{\parallel i}}{\partial t} = nR[\phi, V_{\parallel i}] - nV_{\parallel i}\frac{\partial V_{\parallel i}}{\partial z} - T_e\frac{\partial n}{\partial z} - n\frac{\partial T_e}{\partial z} + \frac{4}{3}\eta_{0,i}\frac{\partial^2 V_{\parallel i}}{\partial z^2} + \frac{2}{3}\eta_{0,i}\frac{\partial^2 \phi}{\partial y \partial z} + D_{V_i}\nabla_{\perp}^2 V_{\parallel i},$$
(5)