

1 **REAL-TIME FULL BODY MOTION IMITATION ON**
2 **THE COMAN HUMANOID ROBOT**

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4 **ABSTRACT-** On-line full body imitation with a humanoid robot standing on
5 its own two feet requires simultaneously maintaining the balance and imitating
6 the motion of the demonstrator. In this paper we present a method that allows
7 real-time motion imitation while maintaining stability, based on prioritized
8 task control. We also describe a method of modified prioritized kinematic
9 control that constrains the imitated motion to preserve stability only when
10 the robot would tip over, but does not alter the motions otherwise. To cope
11 with the passive compliance of the robot, we show how to model the estimation
12 of the center-of-mass of the robot using support vector machines. In the paper
13 we give detailed description of all steps of the algorithm, essentially providing
14 a tutorial on the implementation of kinematic stability control. We present the
15 results on a child sized humanoid robot called Compliant Humanoid Platform
16 or COMAN. Our implementation shows reactive and stable on-line motion
17 imitation of the humanoid robot.

19 **1 Introduction**

20 The transfer of human motion to humanoid robots can be accomplished in
21 many manners, one of them being motion capture (^{1,2}). Different kinematic
22 and dynamic properties of humans and robotic mechanisms do not allow direct
23 transfer or mapping of movement from one to the other.³ This becomes even
24 more evident when the robot should be, just as the demonstrator, standing on
25 its own feet. For example, recorded joint movement of humans when squatting
26 will, if directly copied to a humanoid robot, most likely result in the robot
27 tipping over.

28 Thus the observed human motion needs to be adapted to the properties of the
29 humanoid robot, but this requires the availability of models specifying robot
30 kinematics and dynamics in order to control the robot's stability criterion.

31 Probably the most commonly used criterion to maintain robotic stability is
32 the zero moment point (ZMP) (^{4,5}), defined as the point on the ground where
33 the tipping moment acting on the humanoid robot, due to gravity and inertia
34 forces, equals zero (⁶). A biped humanoid robot is dynamically stable at
35 any given time if its ZMP lies within the area defined by the convex hull of
36 the supporting feet – in the double support phase, or one foot in the single
37 support phase. ZMP is commonly used to evaluate the center of mass (CoM)
38 acceleration boundaries, i.e. to determine the highest possible accelerations of
39 the CoM, which keep the ZMP inside of the support polygon.

40 This method was for example used by Harada et al.,⁷ who developed the ZMP
41 dynamic-evaluation criterion, which enables generalized multicontact loco-
42 motion behaviors. Kajita et al.⁸ designed a control system which minimizes the
43 error between the desired ZMP and the output ZMP by applying a preview
44 controller. Later Hyon et al.⁹ proposed the compliant multicontact behavior

45 using optimal distribution of contact forces. Even before that Sugihara et al.¹⁰
46 applied an inverted pendulum control to generate dynamically stable walking
47 patterns in real-time. The advantage of inverted pendulum approaches is that
48 they require only a rough model of the robot dynamics to be successful.

49 One of the above mentioned approaches is commonly used to constrain the
50 movement of the robot, so that the ZMP moves along the desired trajectory
51 or even remains stationary.¹¹

52 Humanoid robots are kinematically redundant.¹² The redundant DOFs can
53 be used to effectively control the stability while performing some other task.
54 The prioritized task control can be used to implement such behaviors. For the
55 case of stability control, the motion of ZMP is considered as a primary task
56 while other tasks or movements are considered as secondary tasks projected
57 onto the null space of the primary task.

58 The goal of this paper is to show how to integrate stability control with motion
59 capture systems to generate stable reproductions of human movements in real-
60 time. We propose to exploit the kinematical redundancy of a humanoid robot
61 and apply whole-body prioritized control. In the context of humanoid robots,
62 prioritized control was used for example to enable the unified control of center
63 of mass, operation-space tasks, and internal forces.¹³ Prioritized control for
64 locomotion and balance control was also addressed by Mistry et al.¹⁴

65 Since keeping the stability of a robot is normally the most important motor
66 task, it thus constrains all other tasks to its null space and effectively alters
67 the motions executed on the robot. In this paper we propose and evaluate
68 a method which in certain situations allows unconstrained execution of the
69 secondary task while the robot is securely stable. The primary task of stability
70 control takes over only when approaching a predefined threshold, when the
71 robot is in danger of becoming unstable. On top of that, it also allows smooth,
72 continuous and reversible transition between the two modes. Such behavior,

73 when applied to stability control, allows arbitrary movement of the robot while
74 it is in a stable configuration. Furthermore, it does not interfere with the
75 desired movement, for example the demonstrated movement the robot should
76 track. Once a predefined threshold of a selected criterion, e.g. the location
77 of ZMP is reached, the primary task takes over, and constrains the desired,
78 demonstrated movement.

79 To demonstrate the applicability of the algorithm we show how it can be ap-
80 plied to real-time motion imitation of a humanoid robot, which at the same
81 time preserves stability by standing on its own two feet. We performed the
82 experiments on the Compliant Humanoid Platform or COMAN, which boasts
83 14 series-elastic joints, of which 6 in the legs are in the sagittal plane. The
84 discrepancies between the CAD data of the robot and the real robot, and the
85 passive elements in the kinematic chains lead to an error of the estimation of
86 the center-of-mass. We show in the paper how we can model the discrepan-
87 cies with the use of support vector machines, a supervised machine learning
88 approach.^{15,16} Other approaches were demonstrated to account for the behav-
89 ior of the springs on the same platform. Lee et al.¹⁷ have used a time-delay
90 estimation in their control scheme, focusing on the behavior when carrying
91 load. On the other hand, Mosadeghzad et al.¹⁸ have proposed optimal com-
92 pliance regulation. The emphasis of the paper was on the control with respect
93 to external impacts. A model free approach, completely excluding the kine-
94 matics, was used for postural control of the same compliant robotic platform
95 by Gay et. al.¹⁹ In their approach, the authors used visual flow and gyro-
96 scopes as the input into optimized neural networks. In our paper, we show
97 how we can perform postural control and motion imitation online, without
98 of-line optimization.

99 To implement the real-time motion imitation we used a low cost RGB-D sensor,
100 namely Kinect for the tracking of a human body. A similar approach applied

101 to a dynamic simulation was proposed by.²⁰ Real-time motion transfer using
102 precise motion capture on a Nao robot was described by.²¹ Dynamic motion
103 capture and imitation using motion capture was described by Ramos et al.²²
104 The paper describes of-line optimizations of motion and uses precise motion
105 capture, while we describe real-time on-line motion imitation, where the pos-
106 sibility of optimizing motions is limited by the time-step of the control loop.
107 Even so, we achieve reactive and stable motion imitation, which we demon-
108 strated on a real robotic platform. In a recent paper, Zheng and Yamane²³ have
109 extended motion tracking with strict contact force constraints, implemented
110 by solving a nonlinear optimization problem with complex constraints in every
111 control-loop step. They demonstrated the results in a dynamics simulator.
112 In order to apply the prioritized task control on the robot one needs the com-
113 plete kinematic description of the robot and the means to control the CoM or
114 ZMP using inverse kinematics. In Section 2 we briefly outline the calculation
115 of kinematic descriptions of humanoid robots. In Section 3 we present motion
116 imitation based on prioritized task control. The paper continues with the al-
117 gorithm to manipulate the ZMP through the COM and the final prioritized
118 control. Section 4 explains the modified task control, while Section 5 gives the
119 results on the real robot. In Section 6 we describe how we can model the be-
120 havior of passive elements of the robot using SVM. Discussion and conclusions
121 are given in Section 7.

122 **2 Kinematics of a Humanoid Robot**

123 When calculating the kinematics of a humanoid robot, one has to take into
124 consideration that the robot is not attached to the ground, as it is the case
125 with conventional industrial manipulators. A humanoid robot is bound to
126 the ground by a one-way constraint, given by the current support plane, for
127 instance with the feet. Defining an inertial frame is necessary in order to

128 describe the position and orientation of the multi-legged kinematic chain with
129 the use of systematical approaches for serial mechanisms.

130 The humanoid robot can be modeled as a combination of four kinematic chains,
131 one for each limb, which all originate in the same starting point, called the base
132 or root.²⁴ This point is often in the “abdomen” of the robot. The base frame
133 attached to the robot is then connected to the inertial frame via 6 unactuated
134 DOFs. In a kinematical aspect, using these DOF to calculate the kinematics
135 becomes equivalent to imposing a null velocity reference to the feet.²⁴ Since
136 these DOFs cannot be directly actuated, the term floating-base systems is
137 often used to describe them.

138 Systematical approaches for serial mechanisms can be used to describe the
139 kinematics of each of the four chains of a humanoid robot. The four chains
140 consist of the two legs and the two arms (see Fig.1 showing the robot). Any
141 systematical approach, such as the DenavitHartenberg (DH) parameters or the
142 vector parameters²⁵ can be used for the description of the kinematic description
143 of the chains.

144 **3 Motion Imitation with Stability Control**

145 The task of our algorithm is to allow on-line motion imitation on top of stabil-
146 ity control. Therefore we have chosen the primary task to be stability control
147 and the secondary task to be imitation of a demonstrator’s movements, ex-
148 tracted with the Kinect sensor. In order to keep the robot stable, we wish to
149 manipulate ZMP through the CoM. The relationship between the velocity of
150 the center of mass in base coordinates (denoted by ${}^b \mathbf{x}_{\text{CoM}}$) and joint angle
151 velocity $\dot{\mathbf{q}}$ is given by the Jacobian of the center of mass $\mathbf{J}_{\text{CoM}} \in \mathbb{R}^3$.

152 3.1 Center of Mass Jacobian

153 The center-of-mass Jacobian in base coordinates ${}^b\mathbf{J}_{\text{CoM}}$ is obtained from

$${}^b\mathbf{x}_{\text{CoM}} = \frac{\sum_{i=1}^n m_i {}^b\mathbf{x}_i}{\sum_{i=1}^n m_i} \quad (1)$$

154 from the relation

$${}^b\mathbf{x}_{\text{CoM}} = \frac{\sum_{i=1}^n m_i {}^b\mathbf{J}_i \dot{\mathbf{q}}}{\sum_{i=1}^n m_i} = \frac{\sum_{i=1}^n m_i {}^b\mathbf{J}_i}{\sum_{i=1}^n m_i} \dot{\mathbf{q}} = {}^b\mathbf{J}_{\text{CoM}} \dot{\mathbf{q}}. \quad (2)$$

155 where ${}^b\mathbf{J}_i$ is the geometric Jacobian of the center of mass of body part i in
 156 base coordinates. Algorithm 1 gives a pseudo code on how to calculate the
 157 CoM Jacobian.

Algorithm 1 Center of Mass Jacobian

```

1: function  $\mathbf{J}_{\text{CoM}}$ 
2:    $M = \sum_{j=1}^n m_j$ 
3:   for all kinematic chains do
4:      $m_\lambda = 0$ ;
5:     for  $j = n : -1 : 1$  do
6:        $m_\lambda = m_\lambda + m_j$ 
7:        $\mathbf{p}_{\text{CoM},j} = m_j \mathbf{x}_{\text{CoM},j} / m_\lambda - \mathbf{O}_j$ 
8:        $\mathbf{J}_{\text{CoM},j} = m_\lambda / M (\mathbf{r}_j \times \mathbf{p}_{\text{CoM},j})$  ▷ × cross product

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158 Basically, to calculate the center-of-mass Jacobian, one calculates how much a
 159 differential motion of a separate joint differentially displaces the center of mass.
 160 The pseudocode provided in algorithm 1 starts at the end of a kinematic chain
 161 and calculates the effect of moving the last joint, all the way to the first joint
 162 in the chain, which moves the mass of the complete chain. In this pseudocode,
 163 the variable $\mathbf{p}_{\text{CoM},j}$ is an auxiliary variable, \mathbf{O}_j refers to the origin of frame j ,
 164 \mathbf{r}_j is the j -th joint axis direction in the base frame, and m_λ is the recursively
 165 calculated mass from the current frame to the end of the kinematic chain.
 166 The complete \mathbf{J}_{CoM} is calculated by combining the $\mathbf{J}_{\text{CoM},j}$ columns of all the

167 kinematic chains.

168 Eq. 2 provides the geometric Jacobian of the center of mass of body part i in
 169 base coordinates. However, since we are dealing with a free floating base, one
 170 has to take into account that one or two support feet are fixed in the world
 171 coordinate system, as they provide the support for the robot. We therefore
 172 have to calculate the Jacobian matrix in the corresponding coordinate system
 173 of the support foot and take into consideration that the feet do not move. The
 174 velocities of the feet are 0, i.e. $\dot{\mathbf{x}}_R = \omega_R = 0$ and $\dot{\mathbf{x}}_L = \omega_L = 0$. The variables
 175 $\dot{\mathbf{x}}_{R,L}$ and $\omega_{R,L}$ stand for respectively the linear and the angular velocities of
 176 both feet in the world coordinate system. It was shown by¹⁰ that the ${}^b J_{\text{CoM}}$
 177 can be transformed to assume the main support foot

$$\mathbf{J}_{\text{CoM},F} = \mathbf{R}({}^b \mathbf{J}_{\text{CoM}} - {}^b \mathbf{J}_F + \Omega({}^b \mathbf{x}_{\text{CoM}} - {}^b \mathbf{x}_F) {}^b \mathbf{J}_{\omega F}), \quad (3)$$

178 F being either L or R (i.e. left or right foot). Here $\Omega(\mathbf{v})$ is defined as

$$\Omega(\mathbf{v}) = \begin{bmatrix} 0 & -v(3) & v(2) \\ v(3) & 0 & -v(1) \\ -v(2) & v(1) & 0 \end{bmatrix}. \quad (4)$$

179 and \mathbf{R} is the orientation of the base of the robot in world coordinates. ${}^b \mathbf{J}_F$
 180 and ${}^b \mathbf{J}_{\omega F}$ are the translational and rotational part of the Jacobian of the foot,
 181 while ${}^b \mathbf{x}_F$ is the position of the foot, all in robot base coordinates.

182 To maintain the other foot on the ground in double support phase, we have to
 183 add the constraint which prevents the other foot from moving. For example,
 184 if $F = R$ in eq. (3), we have to add the constraint

$$\mathbf{J}_L \dot{\mathbf{q}}_{LW} = 0, \quad (5)$$

185 where $\mathbf{J}_L \in \mathbb{R}^{6 \times n}$ is the Jacobian of the left foot in the world coordinates and
 186 \mathbf{q}_{LW} the joints that span the chain from the right to the left foot. Figure 2
 187 illustrates the situation. Since we have all the Jacobian matrices calculated
 188 in the base coordinate systems, i.e. the kinematic chains originating in the
 189 abdomen of the robot, we have to generate the Jacobian (in our case when F
 190 $= R$) matrix that defines the relation between the joints of both legs and the
 191 tip of the left foot with respect to the tip of the right foot. The transformation
 192 can be derived from

$$\mathbf{T}_L^R = \mathbf{J}_L = \begin{bmatrix} \mathbf{R}_R^T \mathbf{R}_L & \mathbf{R}_L^T (\mathbf{x}_R - \mathbf{x}_L) \\ \mathbf{0} & 1 \end{bmatrix}, \quad (6)$$

193 and deriving separately for the position and the orientation parts. By replacing
 194 \mathbf{x} with $\mathbf{J}\dot{\mathbf{q}}$ and expressing separately for the joints of the left and right foot,
 195 we get

$$\mathbf{J}_L = \begin{bmatrix} -\mathbf{R}_R \Omega (\mathbf{x}_L - \mathbf{x}_R)^T \mathbf{J}_{\omega R} - \mathbf{R}_R^T \mathbf{J}_{pR} & \mathbf{R}_R^T \mathbf{J}_{pL} \\ -\mathbf{R}_R^T \mathbf{J}_{\omega R} & \mathbf{R}_R^T \mathbf{J}_{\omega R} \end{bmatrix}, \quad (7)$$

196

$$\mathbf{q}_{LW} = \begin{bmatrix} \mathbf{q}_R \\ \mathbf{q}_L \end{bmatrix}. \quad (8)$$

197 Considering the constraints of the support feet, the velocity of the center of
 198 mass and the kinematic constraints with respect to the joint motion, can now
 199 be expressed as

$$\dot{\mathbf{x}}_e = \mathbf{J}_e \dot{\mathbf{q}}, \quad (9)$$

200 where index e stands for augmented. The augmented Jacobian accounts for
 201 both the stability task and the kinematic constraint with

$$\dot{\mathbf{x}}_e = \begin{bmatrix} \dot{\mathbf{x}}_{\text{CoM}} \\ \mathbf{0} \end{bmatrix}, \quad (10)$$

$$\mathbf{J}_e = \begin{bmatrix} \mathbf{J}_{\text{CoM}} \\ \mathbf{J}_F \end{bmatrix}, \quad (11)$$

202 for the double support phase. For the single support phase eqs. (10,11) simplify
 203 into $\dot{\mathbf{x}}_e = \dot{\mathbf{x}}_{\text{CoM}}$ and $\mathbf{J}_e = \mathbf{J}_{\text{CoM}}$.
 204 An alternative approach to constraining the motion of the non-leading foot
 205 would be to simply set the primary task of the robot to maintain the position
 206 of the other foot and then map the stability control to the null space of the
 207 task. The drawback is mainly in not having the stability as the primary task
 208 and therefore the velocities for maintaining the stability are always projected
 209 through the null space of the task of keeping the feet stationary.

210 3.2 ZMP Manipulation Through CoM Jacobian

211 Controlling the center-of-mass allows for the control of static stability. In
 212 order to control the dynamic stability of a humanoid robot we need to control
 213 its motion so that ZMP stays within the support polygon. It was shown by
 214 Sugihara et al.¹⁰ that, neglecting the inertia matrices, the relationship between
 215 the CoM, defined in eq. (1) and given by $\mathbf{x}_{\text{CoM}} = [x_{\text{CoM}}, y_{\text{CoM}}, z_{\text{CoM}}]$, and the
 216 ZMP can be expressed by

$$\ddot{x}_{\text{CoM}} = \omega^2(x_{\text{CoM}} - x_{\text{ZMP}}), \quad (12)$$

$$\ddot{y}_{\text{CoM}} = \omega^2(y_{\text{CoM}} - y_{\text{ZMP}}), \quad (13)$$

$$\omega = \sqrt{\frac{\ddot{z}_{\text{CoM}} + g}{z_{\text{CoM}} - z_{\text{ZMP}}}} \quad (14)$$

217 Here g is the gravitation constant. Eq. (14) requires desired ZMP planning to
 218 calculate the desired z_{CoM} , which can be obtained from an inverted pendulum
 219 control. For details on inverted pendulum control see Kajita et al.²⁶
 220 Figure 3 shows real robot results of manipulating the measured center of pres-
 221 sure (CoP), which can be assumed to represent the ZMP when within the

222 support polygon,²⁷ with the use of the CoM Jacobian. The main advantage is
 223 that the robot can react to external forces. In the results of Fig. 3 we can see
 224 the measured forces, the desired ZMP location, the actual CoP location and
 225 the actual (estimated) CoM location if both forward-backward (x) and left-
 226 right (y) directions of the robot. We can see that if an external force appears,
 227 the CoM is shifted. Due to the passive elements of the robot, the location
 228 of the CoP overshoots when external forces disappear and the robot wobbles
 229 slightly. The offset of the forces in the y direction show a discrepancy between
 230 the model and the real robot.

231 3.3 Prioritized task control

232 Stable reproduction of human movements can be formulated using prioritized
 233 control. Classically, one defines the stability as the primary task and movement
 234 imitation as the secondary task. This leads to the control policy

$$\dot{\mathbf{q}} = \mathbf{J}_e^+ \dot{\mathbf{x}}_e + \mathbf{N} \dot{\mathbf{q}}_{KIN} \quad (15)$$

235 where $N = (\mathbf{I} - \mathbf{J}_e^+ \mathbf{J}_e)$ defines the null space of \mathbf{J}_e and $\dot{\mathbf{q}}_{KIN}$ are the desired
 236 joint angles velocities to account for the Kinect tracking of the human motion,
 237 with $\dot{\mathbf{q}}_{KIN} = k_p(\mathbf{q}_{actual} - \mathbf{q}_{KIN})$ and k_p a positive gain.

238 When controlling the non-supporting leg of the robot in the single stance phase,
 239 one should exclude some of the degrees of freedom from the above matrices.
 240 The other degrees of freedom should preserve the stability.

241 4 Modified Prioritized Task Control

242 In the double support phase the robot allows considerable motion of the upper
 243 part of the body that does not move the ZMP out of the support polygon. The
 244 lower part, namely the feet, are completely constrained and remain motionless
 245 on the ground.

246 In order to allow upper body to freely move until the ZMP starts approaching
 247 the support polygon, we divide the problem per degrees of freedom. While the
 248 degrees of freedom of the legs follow the control policy from Section 3.3, we
 249 propose using a modified task control for the arms and the body of the robot.
 250 The control method is based on the reflexive stability control framework for
 251 humanoid robots,³ which allows unconstrained motion while the ZMP is well
 252 within the stability polygon. In this paper we evaluate for the first time the
 253 approach on a real robot in 3 dimensions. The modified prioritized control
 254 policy suggests

$$\dot{\mathbf{q}} = \eta(\mathbf{x}_{ZMP})^n \mathbf{J}_e^+ \dot{\mathbf{x}}_e + \mathbf{N}_\eta \dot{\mathbf{q}}_{KIN}, \quad (16)$$

255 with

$$\mathbf{N}_\eta = (1 - \eta(\mathbf{x}_{ZMP})^n) \text{diag}(\mathbf{N}) + \eta(\mathbf{x}_{ZMP})^n \mathbf{N} \quad (17)$$

256 and $\mathbf{N} = (\mathbf{I} - \mathbf{J}_e^+ \mathbf{J}_e)$. The weighting function $\eta(\mathbf{x}_{ZMP})$ defines the transition be-
 257 tween the constrained, i.e. in the null space of the stability, and unconstrained
 258 motion imitation. The weighting function takes into account the normalized
 259 distance of the ZMP to the edge of the support polygon

$$\eta(\mathbf{x}) = \begin{cases} \frac{d(\mathbf{x}_p) - d(\mathbf{x})}{d(\mathbf{x}_p) - d_{min}}, & d(\mathbf{x}) > d_{min} \\ 1, & \text{else} \end{cases} \quad (18)$$

260 with \mathbf{x}_p defining the center of the support polygon and d_{min} being the minimal
 261 allowed distance to the edge of the support polygon.

262 Alternatively to eq.(17), one can also use

$$\mathbf{N}'_\eta = \mathbf{I} - \eta(\mathbf{x}_{ZMP})^n \mathbf{J}^+ \mathbf{J}' \quad (19)$$

263 For the details on such use see Petrič et al.³

264 5 Experimental Evaluation

265 In this section we present both simulation and real-world application of the
266 proposed modified task priority algorithm for stability control.

267 5.1 Compliant Humanoid Platform COMAN

268 The Compliant Humanoid Platform COMAN^{28,29} approximates the dimen-
269 sions of a 4 year old child, with the height from the foot to the center of the
270 neck 945mm. The distance between the centers of the shoulders is 312mm.
271 The total weight of the robot is 31.2kg, out of which the legs and the waist
272 module weigh 18.5kg. The complete robot has 25 DOF, but the 2 neck de-
273 grees of freedom are not being used at the time. Each leg has 6 DOF: 3 at
274 the hip, 1 at the knee level and 2 at the ankle. For the trunk there is a 3
275 DOF waist while each arm has currently 4 DOF, i.e. 3 in the shoulder and
276 1 in the elbow. Passive compliance based on series elastic actuation (SEA)
277 was added to the 14 of the 25 DOF including all flexion/extension DOF of
278 the legs, the flexion/extension of the shoulders and elbows and the shoulder
279 abduction/adduction. The robot is presented in Fig. 1.

280 In the motion imitation algorithm we used the Kinect sensor to track and
281 imitate the motion of the complete arms (4 DOF) and of the hips and knees
282 of the legs. Additionally, we implemented the rotation of the torso around the
283 vertical axis. This was calculated from the positions of the shoulder joints of
284 the demonstrator.

285 5.2 Experimental results

286 The difference when using modified prioritized task control compared to using
287 standard prioritized task space control is that the task with the higher priority
288 is only observed when necessary, so stability is only controlled when neces-
289 sary. This can be clearly seen in the results of an experiment, where we set
290 the desired hip angles of the robot to sinusoidally oscillate from the original

291 configuration at -0.3 rad to $-\pi/2$ rad, resulting in the robot bending forward
292 and backward periodically. The motion of the hips is presented in the top
293 plot of Fig. 4. In the bottom plot we can see the location of the CoM. It
294 remains stationary when using the classical approach, as reflected in eq. (15),
295 which through the primary task reduces the error of the CoM. On the other
296 hand, when using the modified task space approach, the CoM moves because,
297 as defined in (16), the primary task is pre-multiplied with $\eta(\mathbf{x}_{ZMP})^n$, which is
298 virtually zero when close to the center of the support polygon.

299 The stability control was set to fully take over 6 cm from the edge of the
300 stability polygon. Fig. 5 shows in the top plot how this affects the behavior
301 of other joints, in the given case the ankles. We can see that when using
302 the modified approach, the joint values remain constant (one instance marked
303 with dashed lines) when the distance from the edge of the support polygon is
304 sufficient, given by $\eta(\mathbf{x}_{ZMP})^5$ as defined in eq. (18). The value of $\eta(\mathbf{x}_{ZMP})^5$ is
305 shown in the bottom plot. In other words, the stability control is not active
306 and does not change the (desired) joint positions when $\eta(\mathbf{x}_{ZMP})^5 \cong 0$.

307 Figure 6 shows a sequence of photos showing a simulated robot in a dynamic
308 simulator Webots³⁰ imitating the motion of a human in real time. The sequence
309 shows the robot lifting one foot. When using the modified task priority control,
310 the demonstrator can move the CoM within the support polygon, but has to
311 observe the current location of CoM to perform the required motion. In our
312 case we defined the desired CoM to move under one foot when the tracking
313 detected that the other foot was considerably higher.

314 Figure 7 shows the real-time motion imitation of COMAN robot. The demon-
315 strator was tracked with the Kinect sensor. We can see imitation with the
316 arms, the body and with the legs when performing a squat and bending over.
317 The robot safely and reliably maintained the stability with very little delay,
318 which can only be observed in very fast demonstrator motions. The algorithm

319 has proven very robust and would only fail in the case of tracking errors. A
320 video showing the real-time motion imitation on the real robot is available at
321 <http://biorob.epfl.ch/files/content/sites/biorob/files/public/Coman/KinectDemoVideo.mov>.

322 **6 Estimating Robot-Model Discrepancies Using Sup-** 323 **port Vector Machines**

324 Since we used only the CAD data to describe the mass properties of the robot
325 and since we do not account for the passive elements, there is a discrepancy
326 between the position of the center of mass $\mathbf{x}_{\text{CoM}}^{\text{model}}$ as calculated from the avail-
327 able model data and the actual CoM \mathbf{x}_{CoM} . While the discrepancy between the
328 model and the real CoM is present in both forward-backward (anteroposterior)
329 and left-right (mediolateral) direction of the robot, all of the springs act in the
330 sagittal plane and therefore the discrepancy is larger in the anteroposterior
331 direction. In this section we show how we can account for the discrepancy
332 in the forward-backward direction using support vector machines (SVM).¹⁵ A
333 similar approach using Gaussian Process Regression (GPR) was used to correct
334 the estimation of kinematics of a mechanism for manipulation.³¹

335 In our approach we first record a very slow and stable motion of the robot,
336 which covers the expected human demonstrated motion and maintains postural
337 stability. Due to very slow motion we can assume that the measured center
338 of pressure \mathbf{x}_{CoP} obtained from pressure sensors on the feet is approximately
339 the same as the center of mass \mathbf{x}_{CoM} . They both move within the support
340 polygon. We can model the error between $\mathbf{x}_{\text{CoM}}^{\text{model}}$ and the measured $\mathbf{x}_{\text{CoP}} \approx$
341 \mathbf{x}_{CoM} using SVM regression. We perform the estimation and correction only in
342 the anteroposterior (x) direction of the robot. SVM training was implemented
343 using the LIBSVM¹⁵ library in Matlab. After training we can estimate the

344 discrepancy as follows

$$x_{\text{CoM}}^{\text{corrected}} = x_{\text{CoM}}^{\text{model}} + \Delta x \quad (20)$$

$$\Delta x = f_{\text{SVM}}(x_{\text{CoM}}^{\text{model}}, \mathbf{q}), \quad (21)$$

345 where f_{SVM} is the function estimated by SVM regression and \mathbf{q} are the robot's
346 joint angles. The data for learning consists of $x_{\text{CoP},i}$, $x_{\text{CoM},i}^{\text{model}}$, \mathbf{q}_i . $i = 1, \dots, N$
347 are the sample indices. The training outputs are calculated as

$$\Delta x_i = x_{\text{CoP},i} - x_{\text{CoM},i}^{\text{model}}. \quad (22)$$

348 Theoretically, all joint angles affect the stability of the robot. However, it
349 would require a large amount of training data to estimate f_{SVM} if all of the
350 joint angles were considered in the optimization process. To reduce the di-
351 mensionality of the input space, we rather use the center of pressure x_{CoM}
352 calculated from the available model and a small number of joints that affect
353 the stability most. These are the leg joints, i. e. ankle, knee, and hip joints.
354 Thus the input joint angles \mathbf{q}_i consist of some subset of the measured joint
355 angles of the legs. The different joint angle combinations we tested are: ankle
356 joints, additionally added knee joints, and finally also with added hip joints.
357 Figure 8 shows the results of using different input data for estimating the dis-
358 crepancy between the real CoM and the CoM calculated from the model. For
359 testing we used data that was not used for estimating the SVM regression
360 function f_{SVM} . Table 1 shows the standard deviations of the difference be-
361 tween the corrected center of pressure $x_{\text{CoM}}^{\text{corrected}}$ and the center of pressure x_{CoP}
362 estimated from the foot pressure sensors, i. e. $x_{\text{CoP}} - x_{\text{CoM}}^{\text{corrected}}$. We can see that
363 the standard deviation of the error increases in case D, which is a result of a
364 finite set of training data. The best result was achieved when using ankle and
365 knee joints in addition to the center of mass coordinates as input.

366 7 Discussion and Conclusion

367 We have shown that we can effectively apply the modified prioritized task
368 control for simultaneous stability control and motion imitation in real-time.
369 In this aspect, we have shown how to apply the described algorithm for both
370 center-of-mass and center-of-pressure control approach. While the former is
371 somewhat easier to implement, the latter takes into consideration the external
372 forces and can adapt the posture of the robot accordingly.

373 If ZMP of the robot moves away from the center of the support polygon and
374 approaches the edge of the support polygon, our stability control takes over,
375 if necessary completely overriding the imitation. The primary task at that
376 point only allows motion that would move the ZMP towards the center of the
377 support polygon. The prioritized task control, through the Jacobian and if
378 enough degrees of freedom are available, may also move the other joints so
379 that the secondary task the imitation is observed.

380 The presented approaches are effective in controlling the stability, yet several
381 issues remain with the applicability to the passively compliant platform used
382 in the experiments. As COMAN boasts series elastic elements, i. e. springs
383 after the motors, the behavior of the springs cannot be directly influenced and
384 specialized controllers need to be developed to account for the spring behav-
385 ior. While the springs come in handy for interaction with the environment
386 and walking, i. e. to reduce the impact forces, for the task of stability they
387 simply introduce an error in the posture. Nevertheless, we successfully demon-
388 strated that our method can be applied, despite the inaccuracies brought by
389 the springs. They can be partially accounted for by the proposed SVM re-
390 gression method. For this method, we first acquire a data set of CoM values
391 obtained from the available kinematic model, the center of pressure values
392 estimated from the foot pressure sensors, and the associated joint angles of
393 the robot. In the future we would like to improve these results with a more

394 in-depth analysis of this approach.

395 The modified stability approach has allowed us to transfer the motion of the
396 demonstrator to the robot in real time, including the lifting of separate legs.
397 This proves that the proposed method enables the transfer of human motion
398 to the robot without the explicit need for the demonstrator to take into con-
399 sideration the behavior of the robot. Since we do not explicitly control the
400 stability all the time, but only when necessary, and by keeping a well defined
401 prioritized control policy with smooth transitions between the tasks, we can
402 perform a variety of tasks, which are not feasible with the strictly prioritized
403 approach.

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Figure 1: COmpliant HuMANoid Platform – COMAN, developed by IIT, and used in the experiments to demonstrate the possibility of using modified task space control for motion imitation.

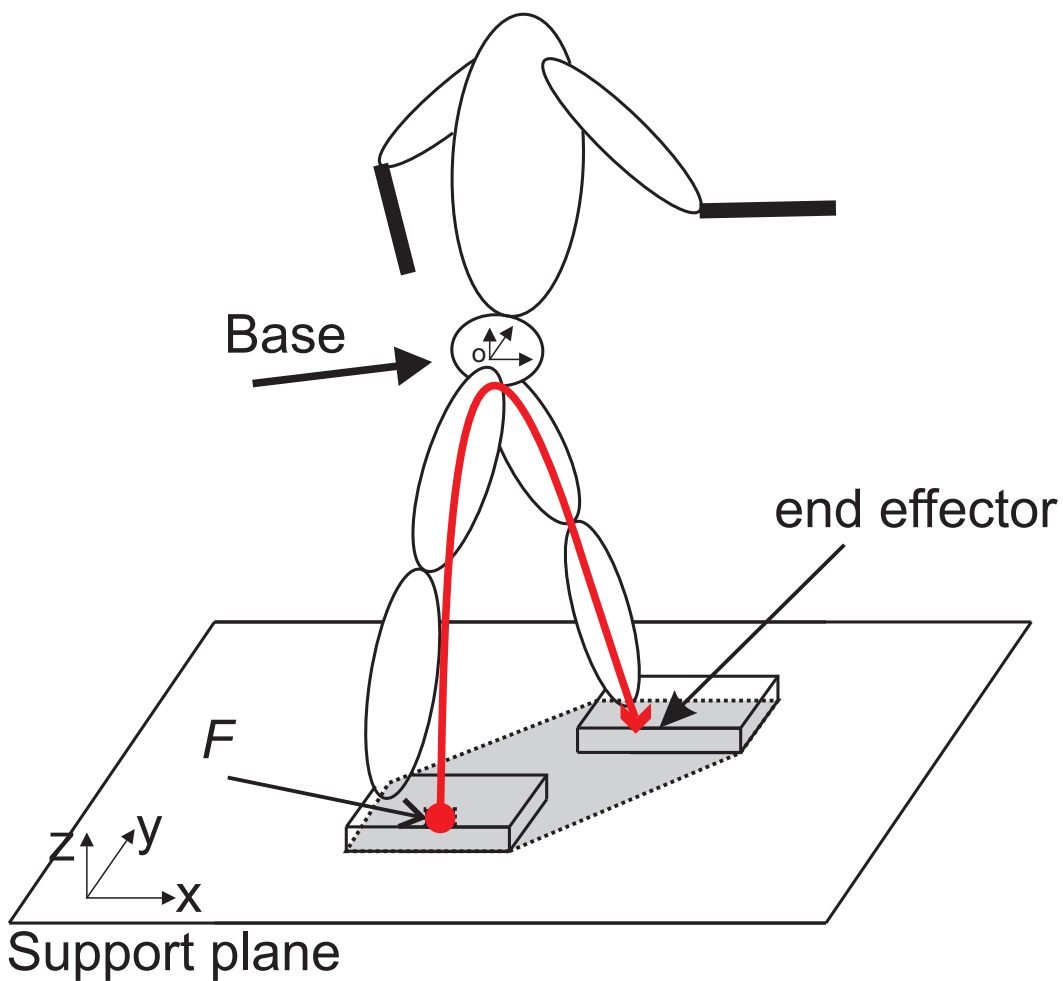


Figure 2: Based on the assumption that the feet do not move when the robot is standing, one foot F is considered as the new, fictional base of the robot. The Jacobian of the CoM has to be transformed so that it assumes the new base. The same goes for the other foot. When maintaining the other, non-leading foot stationary, one can consider the chain from one foot to the other as a serial mechanism, given by the red arrow.

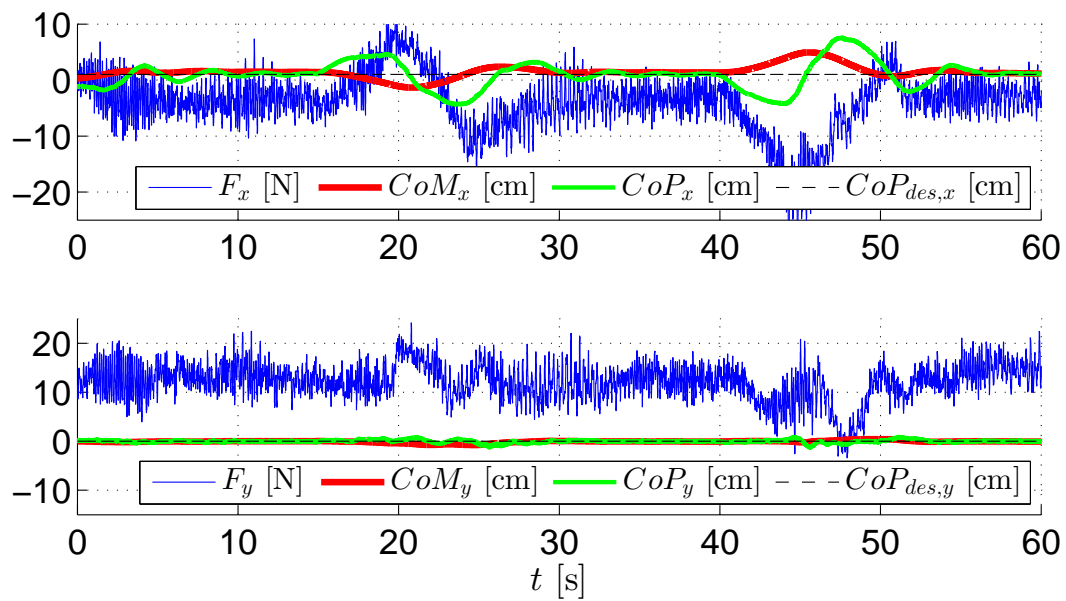


Figure 3: The locations of the CoM (red), CoP (green), desired CoP (dotted) and the measured forces (blue) in the x direction of the robot (forward-backward) in the top plot. The same for the y direction in the bottom plot. The forces are in N while the locations are in cm (for scale) relative to the most stable point of the support polygon.

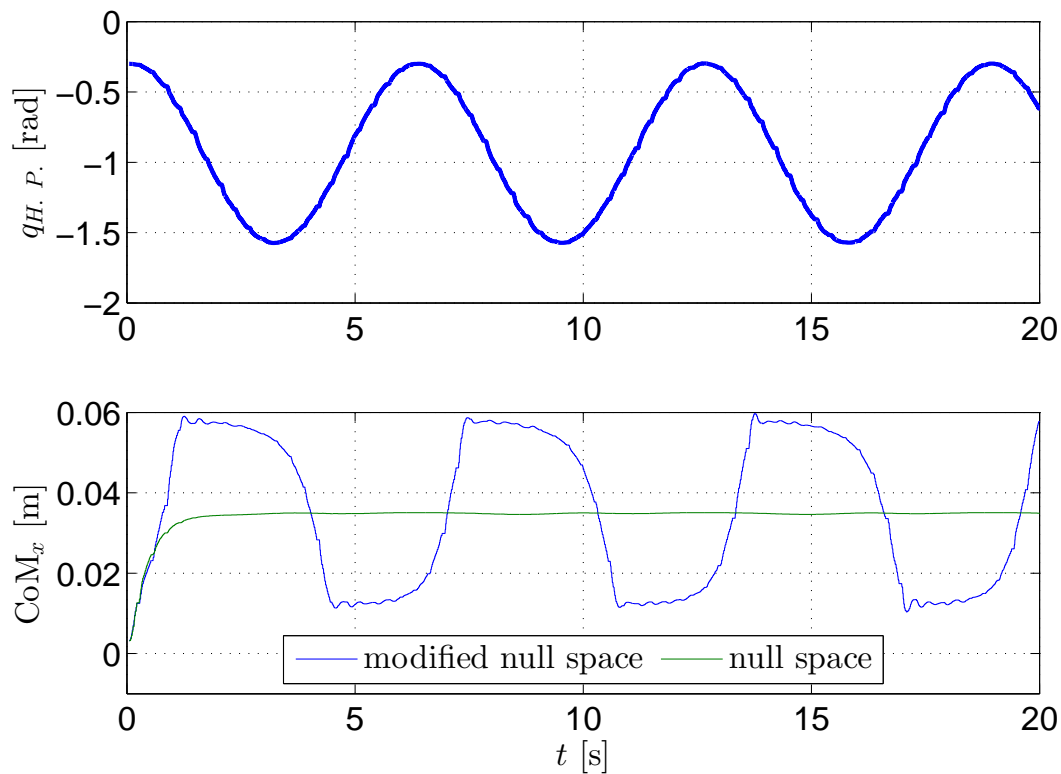


Figure 4: Top: the hip pitch angles for both both hips ($q_{H.P.}$). Bottom: the resulting forward-backward location (x -direction) of the CoM projected along the z -axis when using the modified (in blue) or classical (in green) prioritized task control. While the classical prioritized task control does not allow any movement of the CoM, the modified null space controller only prevents the CoM from leaving the support polygon, at the same time allowing stable displacement of the CoM due to the movement of the hips.

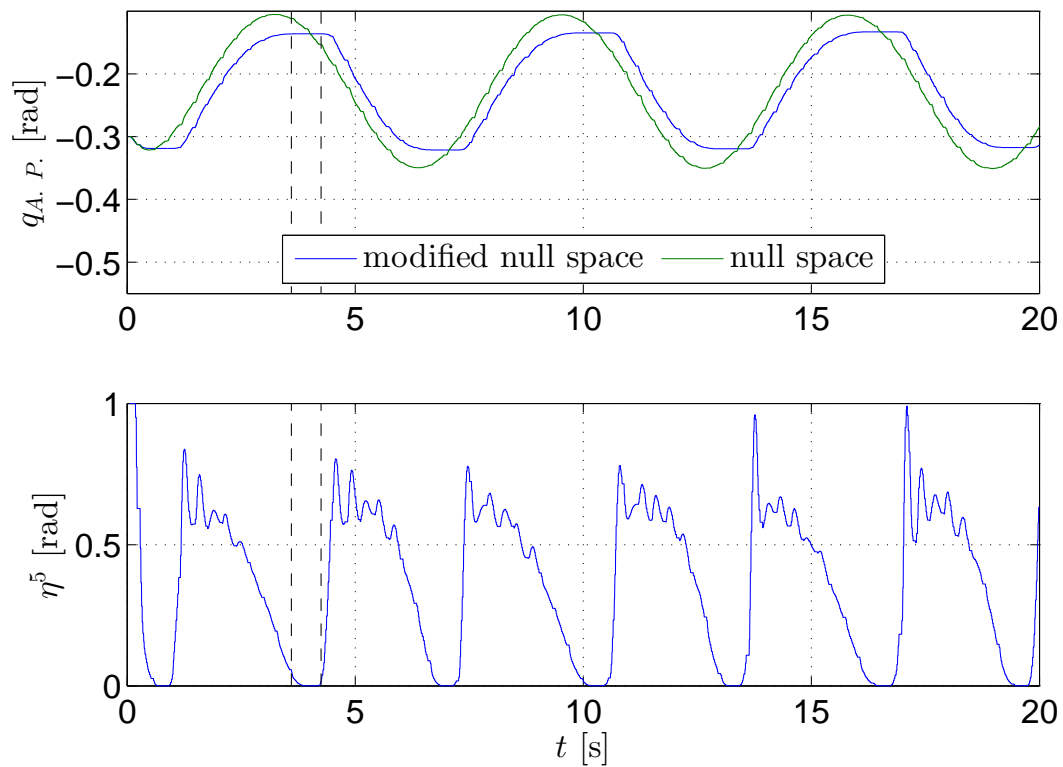


Figure 5: The motion of the ankles ($q_{A.P.}$) when maintaining the stability during the experiment presented also in Fig. 4 in the top plot. The value of η^5 is shown in the bottom plot. Vertical dashed lines mark a time span when the primary task, i.e. stability, is not controlled.

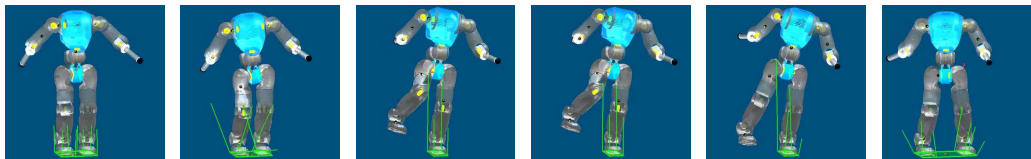


Figure 6: Images showing a simulated COMAN robot while imitating human behavior in real time. The sequence shows the example where the demonstrator performs a side-step.

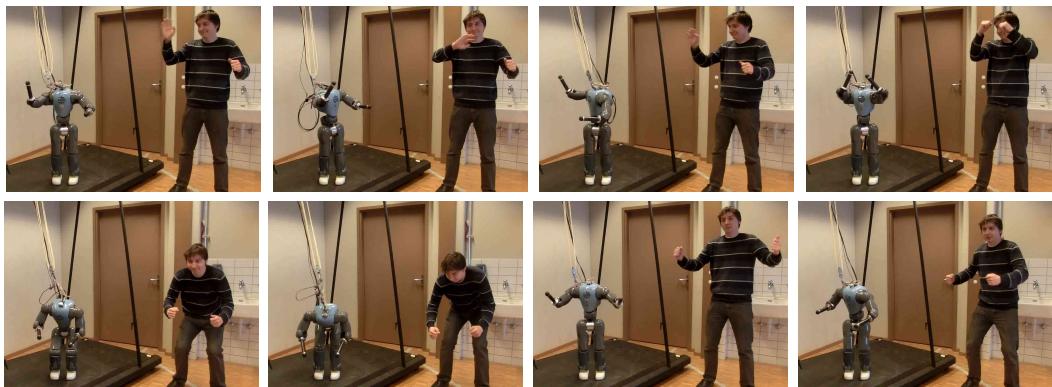


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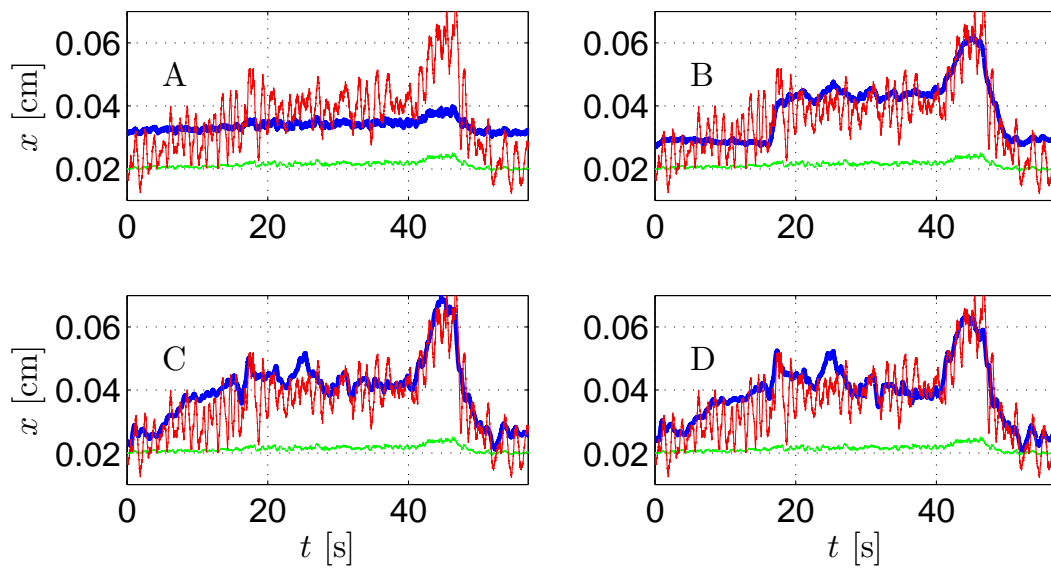


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Table 1: Standard deviation of the error (in meters) of x_{COM} estimation using different input and training data

Input data	Standard Deviation
A	0.0102
B	0.0067
C	0.0062
D	0.0065