Understanding Trends in CO₂ Adsorption in Metal–Organic Frameworks with Open-Metal Sites

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Supporting Information

ABSTRACT: Using van der Waals-corrected density functional theory and a local chemical bond analysis, we study and explain trends in the binding between CO₂ and open-metal coordination sites within a series of two metal–organic frameworks (MOFs), BTT, and MOF-74 for Ca, Mg, and nine divalent transition-metal cations. We find that Ti and V result in the largest CO₂ binding energies and show that for these cations the CO₂ binding energies for both structure types are twice the value expected based on pure electrostatics. We associate this behavior with the specific electronic configuration of the divalent cations and symmetry of the metal coordination site upon CO₂ binding, which result in empty antibonding orbitals between CO₂ and the metal cation. We demonstrate that a chemical bond analysis and electrostatic considerations can be used to predict trends of CO₂ binding affinities to MOFs with transition-metal cations.

SECTION: Molecular Structure, Quantum Chemistry, and General Theory

Climate change due to anthropogenic emissions of CO₂ is now well accepted, and several initiatives have been proposed to reduce such emissions.¹ These include, among others, the increase in the use of renewable energy and the improvement of the efficiency and conservation of fossil fuel resources, including a significant contribution from CO₂ capture and storage (CCS).² Among the different candidate approaches that enable more efficient separations of CO₂ from other gases, physisorption by metal–organic frameworks (MOFs) is one of the most promising.³–⁶ MOFs are 3-D nanoporous extended solids composed of metal centers connected by organic molecules, called bridging ligands. Their high surface area, high CO₂ selectivity, and chemical tunability⁷,⁸ can allow for the design of optimum materials for carbon capture. In particular, MOFs exhibiting coordinatively unsaturated metal centers have been observed to provide promising selectivity of CO₂ over N₂ and a high CO₂ capacity at very low pressures,⁸ which is relevant for efficient gas separations from a postcombustion process. Improving CO₂ capacity of these materials would be desirable, and a way to achieve this is by increasing the interaction energy with the metal center. For this reason, several studies have quantified changes in the CO₂ heat of adsorption when replacing the metal atom for a given MOF topology.⁸–¹⁴ Interestingly, a large binding strength has been computed for early transition metals, for example, Ti and V, which are found to bind differently than expected from their size and nominal charge state.¹³,¹⁴ However, chemical intuition is still missing for why these metal cations lead to strong CO₂ binding or selectivity, and such intuition is needed for guiding further experimental efforts.

Here, we calculate MOF-CO₂ binding energies using density functional theory (DFT) with van der Waals dispersion corrections,¹⁵ explaining computed trends in open-metal sites using electrostatic arguments and a local chemical bond analysis. We focus on a class of recently synthesized sodalite-type frameworks called M-BTT (H₄[(M₄Cl)₃(BTT)₈], M = M²⁺ metal, BTT = 1,3,5-benzenetristetrazolate)¹⁶–¹⁹ possessing coordinatively unsaturated metal centers, which, in prior work,²⁰ have been shown to exhibit promising CO₂ binding energies that are sensitive to the choice of the metal (Mg, Ca, Sr, and Cu) and ligand (tetrazole, triazole and oxazole).²⁰ Examining CO₂ binding across a range of first-row transition-metal cations within BTT-type frameworks, we predict binding energies ranging from 32.2 kJ/mol for Cu to 80.2 kJ/mol for V. We show that for Ti and V, the trend in CO₂ binding energy deviates significantly from expectations based on the formal charge of the cation and the metal–oxygen distance (or ionic...
radius). The electronic configurations of these metals (d^2 and d^3) result in empty antibonding σ* states between the CO2 and the metal cation, which are populated for cations with a greater number of d electrons (Cr and later); the empty σ* antibonding states can thus be connected to the predicted enhanced binding energy. More generally, our study demonstrates that a chemical bond analysis and electrostatic considerations can be used to predict trends of CO2 binding affinities to MOFs with transition-metal cations and suggests that MOFs synthesized with early transition-metal open sites will lead to significantly enhanced molecular adsorption.

Our DFT calculations are performed within the generalized gradient approximation.21 van der Waals dispersion corrections are treated with the Grimme method (DFT+D2).15 We use the SIESTA package, a localized atomic orbital basis, and norm-conserving pseudopotentials for all calculations. (See the SI for details.) Adsorption energies neglect zero-point energy and thermal contributions (binding energies). In recent calculations, thermal contributions at room temperature, together with zero-point energies, reduce the CO2 binding energy by ~5 kJ/mol. The binding energies reported here have been obtained without a Hubbard U correction; results obtained using DFT + U are reported in the SI. Although we find that they can vary in magnitude by ~8 kJ/mol with choice of U (see SI), such corrections do not change the trends described here.

The CO2 binding geometry in M-BTT MOFs is similar for all metal cations and has already been described in detail in previous work.20 A three-site interaction between the CO2 and the MOF, where the CO2 oxygen atoms interact with both the hydrogen and metal atoms of the framework, respectively, leads to the CO2 carbon atom being concomitantly attracted to the negatively charged nitrogen of the tetrazole ligand, as illustrated in our recent work.20 In Table 1, we report computed binding energies, optimized binding geometries, the lattice parameter of the bare MOF, the metal Mulliken charge, Q, and the magnetic moment, μ, of the metal cation in the bare framework. The lattice parameter correlates well with the ionic radii of the metal ions, in agreement with recent diffraction studies for Mn-BTT,16 Fe-BTT,19 and Cu-BTT,24 where cell parameters of 19.116,16 18.824,19 and 18.595 Å24, respectively, are reported for the solvated MOFs. Our calculations led to a binding energy of 21.7 kJ/mol20 for a similar MOF, Cu-BTTr (BTTr = 1,3,5-tri(1H-1,2,3-triazol-4-yl)benzene), in good agreement with the value of 21 kJ/mol computed from the temperature dependent

Table 1. CO2 Adsorption (Binding) Energies and Geometries Computed with DFT+D2

<table>
<thead>
<tr>
<th>metal</th>
<th>E_ads (kJ/mol)</th>
<th>O–C–O (deg)</th>
<th>O–M (Å)</th>
<th>C–N (Å)</th>
<th>μ (μB)</th>
<th>Q</th>
<th>a (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>67.2</td>
<td>172.1</td>
<td>2.207</td>
<td>2.605</td>
<td>1.10</td>
<td>19.010</td>
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<tr>
<td>Ca</td>
<td>60.6</td>
<td>173.6</td>
<td>2.475</td>
<td>2.758</td>
<td>1.20</td>
<td>19.646</td>
<td></td>
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<tr>
<td>Ti</td>
<td>73.2</td>
<td>171.3</td>
<td>2.327</td>
<td>2.660</td>
<td>1.48</td>
<td>0.77</td>
<td>18.973</td>
</tr>
<tr>
<td>V</td>
<td>80.2</td>
<td>170.0</td>
<td>2.188</td>
<td>2.648</td>
<td>2.82</td>
<td>0.69</td>
<td>18.832</td>
</tr>
<tr>
<td>Cr</td>
<td>36.6</td>
<td>175.5</td>
<td>2.747</td>
<td>2.781</td>
<td>3.90</td>
<td>0.59</td>
<td>18.769</td>
</tr>
<tr>
<td>Mn</td>
<td>50.8</td>
<td>174.2</td>
<td>2.401</td>
<td>2.732</td>
<td>4.82</td>
<td>0.90</td>
<td>19.073</td>
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<tr>
<td>Fe</td>
<td>47.3</td>
<td>173.8</td>
<td>2.405</td>
<td>2.720</td>
<td>3.66</td>
<td>0.78</td>
<td>18.909</td>
</tr>
<tr>
<td>Co</td>
<td>39.0</td>
<td>174.8</td>
<td>2.521</td>
<td>2.732</td>
<td>0.98</td>
<td>0.54</td>
<td>18.350</td>
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<tr>
<td>Ni</td>
<td>38.9</td>
<td>174.7</td>
<td>2.567</td>
<td>2.756</td>
<td>1.40</td>
<td>0.60</td>
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<td>Cu</td>
<td>32.2</td>
<td>176.0</td>
<td>2.752</td>
<td>2.809</td>
<td>0.52</td>
<td>0.55</td>
<td>18.743</td>
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<tr>
<td>Zn</td>
<td>43.2</td>
<td>174.5</td>
<td>2.441</td>
<td>2.726</td>
<td>0.71</td>
<td>0.71</td>
<td>18.909</td>
</tr>
</tbody>
</table>

aCO2 adsorption energies computed using a van der Waals-corrected functional (DFT+D2) for BTT MOFs and corresponding bond distances and the bond angle of CO2. The metal magnetic moment, metal Mulliken charges, Q, in units of electron, and the lattice parameter for the bare frameworks, also computed using DFT+D2, are reported here. An antiferromagnetic ordering and high spin configuration is predicted for all systems considered, except Co-BTT. Zero point and thermal contributions are neglected.

Figure 1. CO2 adsorption energy plotted over Q/r, a measure of the strength of the electrostatic contribution to CO2 binding, as a function of MOF-CO2 binding energy for the different metal cations. Here Q is either the Mulliken charge of metal atom or ligand nitrogen closest to CO2 (see Figure 1), computed from a bare MOF. The distance, r, is either the CO2 oxygen—metal or CO2 carbon—ligand nitrogen separation, respectively. From Figure 1, the ligand contribution can be seen to be roughly independent of metal cation; the CO2—metal Q/r plot, however, shows a strong, positive correlation between binding energy and Q/r, with the exception of Ti and V, which exhibit a much stronger binding energy than that expected from electrostatics. Indeed, if the interaction was dominated by
electrostatics, the CO$_2$ binding energy for V-BTT would be the same as Fe-BTT. The large binding energy for V and Ti is directly related to electronic occupation of their d orbitals, as we now discuss. For the bare framework, the metal atom is five-fold-coordinated and has nearly square pyramidal symmetry. In the absence of CO$_2$ adsorption, the σ bonds involving the lone pairs of the five coordinating ligands split the d orbitals, as shown in Figure 2. In the present case, the five ligands are the four axial tetrazole nitrogens and the apical chlorine, as described in ref 16.

When CO$_2$ binds, a coordination-type bond is formed between the metal d$_{z^2}$ orbital and one of the oxygen lone pairs of CO$_2$, leading to approximately octahedral symmetry about the metal cation. This forces the oxygen lone pair down in energy and the d$_{z^2}$ orbital up in energy and results in the formation of a σ* antibonding state with the CO$_2$ lone pair. When the electronic occupation of the metal is d$^2$ and d$^3$ (for Ti and V), there is a net stabilization upon binding associated with the lowering of the oxygen lone pair energy; because the d$_{z^2}$ antibonding molecular orbital is empty, there is no energy penalty when the d$_{z^2}$ orbital increases in energy upon adsorption. However, when the metal has an occupation of four or more electrons and is high spin, the scenario changes: an additional d electron is pushed up by roughly the interaction energy between the metal d$_{z^2}$ and the oxygen lone pair, reducing the binding energy. For V and Fe, for example, this has a significant consequence: while trends in electrostatic interactions suggest that the CO$_2$ binding energy would be nearly the same for V and Fe (see Figure 1), the occupied d$_{z^2}$ orbital in the Fe case leads to a computed binding energy in Fe-BTT of 47.2 kJ/mol, roughly half the amount calculated for V-BTT (80.2 kJ/mol). The antibonding orbital associated with CO$_2$ and the metal cation d$_{z^2}$ state is shown in Figure 2. This state is occupied for Cr and transition-metal atoms to its right and unoccupied for Ti and V.

When the d electron count is 9 or 10, as for Cu or Zn cations, the d$_{z^2}$ orbital becomes doubly occupied and another decrease in binding energy is expected. This is observed, but because of the already weak bond between CO$_2$ and the metal for d $\geq$ 4, the double occupation of the antibonding σ* state has just a modest effect on the binding energy, comparable to the electrostatic contribution. This leads to a predicted CO$_2$ binding energy for Cu-BTT of 32.2 kJ/mol, the smallest of all cations considered here, consistent with a doubly occupied d$_{z^2}$ orbital and smallest Q/r. We note that the CO$_2$ binding energy for Zn-BTT (43.2 kJ/mol) is larger than that for Cr-BTT (36.6 kJ/mol), Co-BTT (39.0 kJ/mol), and Ni-BTT (38.9 kJ/mol) due to the larger electrostatic interaction between CO$_2$ and Zn. (See Figure 1.)

The lower CO$_2$ binding strength of Mg and Ca (relative to Ti and V) can be understood by the fact that their 3s and 4s electrons screen the nucleus more effectively than the partially filled 3d electrons of Ti and V (d$_{x^2}$, d$_{y^2}$, and d$_{xy}$), reducing the effective positive charge of alkaline earth cations. (This effect has been recently pointed out by Yu et al. in the context of their calculations of CO$_2$ binding to MOF-74 MOFs with different metal cations.)

According to the energy diagram shown in Figure 2, we expect that upon CO$_2$ binding the d$_{z^2}$ orbital will shift upward in energy. This is indeed what we observe, as the U-corrected density of states of V-BTT shows in Figure S2 in the SI. We note that the inclusion of a Hubbard U does not significantly affect the binding mechanism because the occupation of antibonding σ* orbitals does not depend on U.

The bonding mechanism discussed here can be generally applicable to other MOFs with unsaturated open-metal sites possessing similar symmetry. For example, a similar analysis of the CO$_2$ binding energy in MOF-74 results in essentially the same trend across the first-row transition metals (see SI for detailed results), in agreement with recent works. Early first-row transition metals (Ti and V) with empty d$_{z^2}$ orbitals show strong binding to CO$_2$ (53.1 and 62.8 kJ/mol for Ti-MOF-74 and V-MOF-74, respectively). Cr- and Cu-MOF-74 lead to the lowest computed CO$_2$ binding energies (30.1 and 29.4 kJ/mol, respectively), consistent with occupied d$_{z^2}$ orbitals and weak electrostatic contributions. Binding energies at frozen geometries (see SI) show a maximum deviation of 8.5 kJ/mol for V-MOF-74 when a Hubbard U is included. However, the same trend as a function of the occupation of the d orbitals is found for the U-corrected binding energies. The robustness of the chemical bonding mechanism proposed here is confirmed by a recent study where a related analysis is used to rationalize large binding energies computed for N$_2$ and CH$_4$ to V-MOF74.

In conclusion, we have shown that although the trends in CO$_2$ binding with open-metal coordination sites are primarily dominated by electrostatic interactions in BTT-type MOFs, binding energies are also highly sensitive to the electronic configuration of the divalent cations. Depending on the metal cation choice, we find that the CO$_2$ binding energy in BTT can be tuned from a minimum of 32.2 kJ/mol for Cu-BTT to a maximum of 67.2 kJ/mol for Mg-BTT. For Ti and V, however, the CO$_2$ binding energies are significantly larger than expected from electrostatics arguments (73.2 kJ/mol for Ti-BTT and 80.2 kJ/mol for V-BTT) due to unpopulated antibonding σ* orbitals formed between the metal d$_{z^2}$ orbital and the CO$_2$ lone pair. For example, replacing Cu with V can increase the CO$_2$ binding affinity by almost a factor of three. The observation of enhanced CO$_2$ binding to frameworks with open V and Ti sites also applies to M-MOF-74 and in general any MOF in which the crystal field created upon CO$_2$ adsorption gives rise to antibonding molecular orbitals that are not populated for a d electron count of 2 or 3, provided that no structural distortions...
take place as a function of electron count. More generally, a strong CO$_2$ affinity with an open-metal site is expected when the $\sigma^*$ antibonding orbitals between the CO$_2$ lone pair and metal d orbitals are empty. For example, a crystal field change from square planar to square pyramidal, upon binding, where CO$_2$ binds apically, can potentially give a larger binding energy for $d \leq 3$. Similarly, if a metal geometry changes from tetrahedral to trigonal bipyramidal, upon CO$_2$ adsorption, a larger binding energy for $d \leq 4$ could be obtained. If the metal has a low spin configuration, a larger binding is instead expected for $d \leq 6$ and $d \leq 8$, respectively. This work shows that upon CO$_2$ binding, that is, upon formation of a $\sigma$ bond between the CO$_2$ oxygen and the metal, a chemical bond picture that uses the crystal-field theory and electrostatic considerations of the metal atom, together with the geometry around the metal site, can be used to predict and understand meaningful trends in the CO$_2$-MOF binding energy with different open-metal coordination sites. This intuition offers a unique approach to design open-metal site MOFs where, for example, a spin crossover transition could lead to significantly reduced CO$_2$ desorption energy.

**REFERENCES**


