Recent developments in Configurational-Bias Monte Carlo (CBMC) techniques allow the accurate calculation of the sorption isotherms for alkanes, and their mixtures, in various zeolites. The CBMC simulations give new insights into subtle entropy effects affecting mixture adsorption. Three types of entropy effects can be distinguished. (1) **Size entropy effects** favour the component with the smaller number of C atoms because the smaller molecule finds it easier to fill in the 'gaps' within the zeolite matrix at high molecular loadings. (2) **Configurational entropy effects** come into play for mixtures of alkanes that differ in the degree of branching. For a mixture of linear and branched alkanes with the same number of C atoms, configurational entropy effects favour the linear isomer because such molecules ‘pack’ more efficiently within, say, the intersecting channel topology of MFI zeolite. (3) **Length entropy effects** come into force for sorption of linear and branched alkanes within the cylindrical channels of say AFI and MOR zeolites; here the double branched alkane has the shortest length and can be packed more efficiently within the channels. We demonstrate that CBMC simulations allow the efficient screening of zeolite structures for a given separation duty and aid the development of novel separation processes exploiting entropy effects.

1 Introduction

The separation of mixtures of alkanes is an important activity in the petroleum and petrochemical industries. For example, the
products from a catalytic isomerization reactor consist of a mixture of linear, mono-methyl and di-methyl alkanes. Of these, the di-branched molecules are the most desired ingredients in petrol because they have the highest octane number. It is therefore required to separate the di-methyl alkanes and recycle the linear and mono-methyl alkanes back to the isomerization reactor. In the detergent industry, the linear alkanes are the desired components and need to be separated from the alkane mixture.

Selective sorption on zeolites is often used for separation of alkane mixtures. Zeolites are crystalline nanoporous materials that are used widely in the chemical industry as catalysts and adsorbents. A wide variety of zeolitic crystal structures are available, e.g. LTA, MFI, MEL, MOR, FAU, BEA, and these are used along with binders in the form of a pellet or coated on to a stainless steel support to form a zeolite membrane. The choice of the zeolite depends on the specific separation task in hand. For example, small-pore LTA zeolite is used for separation of linear alkanes using the molecular sieving principle; the branched molecules cannot enter the zeolite structure. Both linear and branched molecules are allowed inside the medium-pore MFI matrix and the sorption hierarchy in MFI will be dictated both by the alkane chain length and degree of branching. For the development of separation technologies we need to be able to calculate the mixture sorption characteristics for a wide range of operating conditions (pressures, temperatures, compositions). While there are several experimental studies on pure component isotherms, there is considerably less information on mixture isotherms. The lack of mixture sorption data is most probably due to the difficulty of experimentation. Mixture isotherms can be estimated from pure component isotherm data using the Ideal Adsorbed Solution Theory in some cases, but in general we need to account for thermodynamic non-ideality effects.

Recent developments in Monte Carlo (MC) simulations have allowed the calculation of pure component and mixture sorption isotherms with only modest computational power. In MC simulations the zeolite crystals are allowed to exchange molecules with a reservoir of molecules at a fixed chemical potential in the Grand-Canonical (or $\mu, V, T$) ensemble; see Fig. 1. In this ensemble the temperature, volume and chemical potential are fixed. The equilibrium conditions dictate that the temperature and chemical potential of fluid phase inside the zeolite and in the external reservoir must be equal. We therefore need to know only the $\mu$ and $T$ of the gas in the reservoir in order to determine the equilibrium concentration of molecules within the zeolite; this equilibrium is not affected by say the resistance of the gas–zeolite interface to transport of molecules. In a MC simulation one does not have to follow the ‘natural’ path of the molecule, as in a Molecular Dynamics (MD) simulation, and one can perform ‘moves’ to locate a molecule within an arbitrary position within the zeolite. This technique works very well for small molecules such as methane. In an MC simulation for methane sorption, we observe that out of 1000 attempts to place a methane molecule to a random position within a zeolite, 999 attempts will be rejected because the methane molecule overlaps with an atom within the zeolite matrix. For ethane, only 1 move in $10^6$ attempts will be successful. Clearly, the strategy of randomly inserting molecules within a zeolite matrix will not work for long chain alkanes. To make MC simulations of long chain molecules feasible, the Configurational-Bias Monte Carlo (CBMC) technique has been developed.

We first review the principles of the CBMC technique. Later, we show that CBMC simulations can provide new insights into the sorption behaviours of alkanes in zeolites and provide clues to the development of novel separations relying on these insights.

### 2 CBMC simulation technique

The principle of the CBMC technique is to grow an alkane chain, atom by atom, instead of attempting to insert the entire molecule at random. Fig. 2 shows one of the steps in this algorithm; four atoms have been inserted successfully, and an attempt is made to insert the fifth.

![Fig. 1 Simulation of sorption of molecules in a zeolite using grand-canonical Monte Carlo techniques.](image1)

![Fig. 2 Schematic drawing of the growing of an alkane in a zeolite in a CBMC move. The octagons represent the atoms of the zeolite and the circles represent the atoms of the alkane. Four atoms have been inserted successfully, and an attempt is made to insert the fifth.](image2)
a chain is selected at random and part of the molecule is regrown using the CBMC scheme; (4) exchange with a reservoir that fixes the chemical potential of the components—it is decided at random whether to add or to remove a molecule from the zeolite following the acceptance rules derived in Vlugt et al.;16,17 (5) change of identity (only in the case of mixtures)—one of the components is selected at random and an attempt is made to change its identity.16,17 This type of move has as important practical advantage that in step (4) one only has to exchange the smallest molecules with the reservoir.

Typically the number of MC cycles performed is $10^7$. Of these, 15% are displacements, 15% rotations, 15% partial regrowths, 50% exchanges with the reservoir and the remaining 5% of the moves are attempts to change the identity of a molecule. These probabilities can be further optimized depending on the details of the simulations.

Fig. 3 Schematic of structure of MFI (silicalite-1). The cross-sections of the straight and zig-zag channels are shown in the inset.

Fig. 4 Comparison of the experimental data23,26 for pure component isotherms for (a) methane, (b) ethane, (c) propane, and (d) n-butane in MFI at 300 K with CBMC simulations.22–24
A simple approach to describe the alkane molecules is to use the \textit{united-atom model}, in which CH\textsubscript{3}, CH\textsubscript{2}, and CH groups are considered as single interaction centers. When these pseudo-atoms belong to different molecules or to the same molecule but separated by more than three bonds, the interaction is given by a Lennard-Jones potential. The Lennard-Jones parameters are chosen to reproduce the vapor–liquid curve of the phase diagram as shown in Siepmann \textit{et al.}\cite{18}. The bonded interactions include bond-bending and torsion potentials; details for the alkane model can be found in Vlugt \textit{et al.}\cite{16,17}.

For the calculation of the sorption isotherms of alkanes in silicalite, Macedonia and Maginn\cite{19} have adopted a more detailed \textit{all-atom model} to represent the alkanes. Both the \textit{united-atom model} and the \textit{all-atom model} gave comparable results for the prediction of sorption of C\textsubscript{1}–C\textsubscript{3} alkanes in silicalite.\cite{19}

Most simulation studies follow the approach of Kiselev and co-workers\cite{20} and assume the zeolite lattice to be \textit{rigid} and that interactions of an alkane with the zeolite are dominated by the dispersive forces between pseudo-atoms of the alkane (within the framework of the \textit{united-atom description}) and the oxygen atoms of the zeolite. In the Kiselev model the total interaction energy is represented by two terms, an attractive term and a repulsive term, and is described by a Lennard Jones potential;\cite{16,17} the potential parameters are usually obtained by fitting to experimental heats of adsorption and Henry coefficients. In the more recent PN intermolecular potential model of Nicholson and co-workers,\cite{21} effects of polarizability and fixed charges in the zeolite matrix can be accounted for, but at significantly higher computational cost.

3 Entropy effects during sorption

3.1 Sorption of pure alkanes

Consider CBMC simulations for sorption of alkanes in the 1–4 C atom range in MFI zeolite, specifically silicalite-1.\cite{22,23,24} Fig. 3 shows a schematic of the structure of MFI that consists of a system of intersecting channels composed of zig-zag channels along \(x\), cross-linked by straight channels along \(y\). Both channels are defined by 10-rings. The straight channels are approximately elliptical in shape having a 0.53 nm \(\times\) 0.56 nm cross section while the zig-zag channels have a 0.51 nm \(\times\) 0.55 nm cross section. The pure component isotherms at 300 K for methane, ethane, propane and n-butane are shown in Fig. 4. The CBMC simulations are seen to be in very good agreement with the experimental data of Sun \textit{et al.}\cite{25} and Zhu \textit{et al.}\cite{26} Such good agreement of CBMC simulations with measured isotherm data for pure alkanes is typical.\cite{17,27}

CBMC simulations provide much more insight into sorption behaviour than is available from experiments alone. In order to illustrate this let us consider the experimental data for sorption of isobutane in MFI at 300–303 K,\cite{25,26} the sorption isotherm shows a pronounced inflection at a loading of 4 molecules per unit cell [see Fig. 5(a)]. This inflection behaviour is nicely reproduced by CBMC simulations. Up to a system pressure of 1 kPa, the isobutene molecules are exclusively located at the intersections, that have a maximum capacity of 4 molecules per unit cell [see the schematic in Fig. 5(b)]. This means that zeolite loadings in excess of 4 molecules per unit cell can only be achieved by pushing isobutene into the straight and zig-zag channels. Only when the pressure is significantly increased beyond 10 kPa do the zig-zag channels and straight channels tend to get occupied. Due to its branched configuration, isobutane demands an extra ‘push’ to locate within these channels. This extra push is the root cause of the inflection behaviour.

Interestingly, n-hexane also shows a slight inflection at a loading of 4 molecules per unit (see e.g. Fig. 6); this inflection is due to ‘commensurate’ freezing\cite{31} caused by the fact that the length of the n-hexane molecule is commensurate with the length of the zig-zag channel [see Fig. 7(a)]. All mono-branched alkanes in the 5–8 C atom range are found to exhibit inflection behaviour,\cite{17,27,30} witness for example the inflection behaviour.
exhibited by 3-methylpentane (3MP) in MFI zeolite [see Fig. 6]. Just as in the case of isobutane, 3MP prefers to locate at the intersections [see Fig. 7(b)] due to the availability of extra ‘leg room’. Di-branched alkanes, typified by 2,2-dimethyl butane (22DMB), also prefer to locate at the intersections of MFI. However, these molecules are much bulkier than mono-branched alkanes and, consequently, they cannot be pushed into the channel interiors. The maximum loading of di-branched alkanes such as 22DMB, in MFI is restricted to 4 molecules per unit cell [see Fig. 6].

The inflection behaviour of mono-branched alkanes in MFI at a loading of 4 molecules per unit cell, as well as the restriction of the maximum loading of di-branched alkanes to this loading, is a consequence of configurational differences. This configurational entropy effect causes the saturation loadings of hexane isomers in MFI to follow the hierarchy linear > mono-branched > di-branched.

With other zeolite structures the configurational entropy effects may act in a completely different manner. Consider the sorption of hexane isomers nC6, 3MP and 22DMB in AFI. The CBMC simulations of the sorption isotherms at 403 K are shown in Fig. 8. The sorption hierarchy, at saturation loading, is found to be di-branched > mono-branched > linear which is opposite to the hierarchy for MFI. AFI consists of cylindrical channels of 0.73 nm diameter. The channel dimension is large enough to accommodate the bulky 22DMB and there is therefore no configurational penalty for these molecules.

However, the length of the molecules decreases with increased degree of branching (see Fig. 9); this implies that the number of molecules that can be accommodated into the channels increases with the degree of branching. The increased sorption strength with increased branching can be termed a length entropy effect, arising as it does with decreasing linear dimension of the molecule. The length entropy effect has also been highlighted by Talbot\textsuperscript{32} in a more general, but idealized, manner.

3.2 Size entropy effects during mixture sorption

Almost all applications of adsorption involve mixtures, yet the number of experimental studies on adsorption of mixtures is very limited due to the difficulty of experimentation. Often in practice, the sorption selectivity of mixtures is estimated on the basis of the values of the Henry coefficients, i.e. the sorption strengths at near-zero loadings.\textsuperscript{33,34} We shall demonstrate below that using Henry coefficients to estimate the sorption selectivity of mixtures can lead to completely wrong conclusions regarding separation possibilities.

Let us first consider sorption of a 95:5 mixture of methane (C1) and n-butane (nC4) in MFI at 300 K. The component
Based on the sorption selectivity in MFI dictated by the experimentally determined Henry coefficients reported by Denayer,33 we would conclude that it is not possible to separate the linear and the mono-branched alkanes with high selectivities. In order to test this conclusion let us consider CBMC simulations4,27 for sorption of a 50:50 mixture of n-C6 and 3MP in MFI at a temperature of 362 K. The component loadings in the mixture are shown in Fig. 12(a) for a range of pressures. It is interesting to note the maximum in the loading of 3MP at about 100 Pa. When the pressure is raised above 100 Pa the loading of 3MP reduces virtually to zero. The n-C6 molecules fit nicely into both straight and zig-zag channels [see Fig. 7(a)] whereas the 3MP molecules are preferentially located at the intersections between the straight channels and the zig-zag channels [Fig. 7(b)]. Below a total loading of 4 molecules per unit cell, there is no real competition between n-C6 and 3MP. The n-C6 locates within the channels and 3MP at the intersections. When all the intersection sites are occupied, to further adsorb 3MP we need to provide an extra ‘push’. Energetically, it is more efficient to obtain higher mixture loadings by ‘replacing’ the 3MP with n-C6; this configurational entropy effect is the reason behind the curious maxima in the 3MP loading in the mixture. The n-C6/3MP sorption selectivity is plotted in Fig. 12(b). We see that the sorption selectivity increases from near-unity values for pressures below 100 Pa to values of around 50 near saturation loadings. Clearly, the Henry selectivity values [denoted by the dashed lines in Fig. 12(b)] are too pessimistic and ignore a potentially attractive separation possibility at high mixture loadings.

For an equimolar ternary mixture of n-C6, 3MP and 22DMB configurational entropy effects act in such a way as to exclude both branched isomers from the MFI zeolite as the pressure is increased; see the CBMC simulations at 362 K shown in Fig. 13(a). The loadings of the three components follow ‘normal’ behaviour for pressures below 50 Pa, i.e., follow the hierarchy dictated by the Henry coefficients. At a pressure of 500 Pa, the total mixture loading is 4 molecules per unit cell; at this loading all the intersection sites are fully occupied. At pressures exceeding 500 Pa, the MFI matrix prefers to accept n-C6 into its matrix rather than either of the branched isomers. The loadings of both 3MP and 22DMB decrease as the pressure is increased beyond 500 Pa. There are three types of entropic ‘battles’ in play at pressures exceeding 500 Pa. The battle between linear isomer and its branched isomers is won by the linear isomer. The battle between the mono-methyl and di-methyl isomer is won by the mono-methyl isomer. The n-C6/3MP and 3MP/22DMB sorption selectivities both increase significantly, beyond the Henry selectivity values (indicated by the dashed lines), when the total mixture loading exceeds 4; see Fig. 13(b).

Direct experimental verification of the validity of these simulations is provided by the experimental data of Santilli.38,39

3.3 Configurational entropy effects in mixture sorption

Let us now consider the separation of hexane isomers, an important separation problem in the petroleum industry.4-6 Based on the sorption selectivity in MFI dictated by the
The sorption hierarchy in MFI for a 5-component equimolar mixture of hexane isomers consisting of nC6, 2-methylpentane (2MP), 3MP, 2,2-dimethylbutane (22DMB) and 2,3-dimethylbutane (23DMB) at high mixture loading is nC6 ≈ 2MP ≈ 3MP > > 22DMB ≈ 23DMB; see CBMC calculation results in Fig. 14(a). Hexane isomers can therefore be separated into three fractions linear, mono-branched and di-branched alkanes. This is exactly the hierarchy in which these components are eluted in a pulsed chromatographic test; see Fig. 14(b). But the important objective from a practical point of view to achieve such a separation hierarchy starting with a mixture say in the 5–7 C atoms range. CBMC simulations for mixture of linear, mono-branched and di-branched alkanes in the 5–7 C atom range in MFI at 300 K are shown in Fig. 15. At low loadings (i.e. low pressures) we see that the sorption hierarchy is dictated by the number of C atoms, i.e. C7 isomers > > C6 isomers > > C5 isomers. Operating at low loadings does not yield the desired separation depending on the degree of branching. However, for mixture loadings approaching 8 molecules per unit cell, the situation changes dramatically; see the right end of Fig. 15. We see that the separation hierarchy is now linear > > mono-branched > > di-branched, exactly as desired. This separation potential is of immense importance in the petroleum industry.4–6

Molecular simulations can also help us to screen promising zeolite structures for a given separation task, relying on differences in component loadings at equilibrium. For the separation of a 50:50 mixture of nC6 and 2MP, the nC6/2MP sorption selectivity in six different zeolite topologies, MFI, MEL, FAU, BEA, MOR and AFI are shown in Fig. 16. In FAU, which has large cages, entropy effects do not come into play and the separation selectivity is about unity over the whole pressure range. Large pore BEA also cannot be used to separate the hexane isomers. For the intersecting channel structures of medium pore size structures MFI and MEL, configurational entropy effects favour the linear isomer at mixture loadings exceeding 4 molecules per unit cell. In AFI and MOR, consisting of straight cylindrical channels, length entropy effects favour 2MP at high mixture loadings. To emphasise this further, in Fig. 17 we present CBMC simulations of a 5-component mixture of nC6, 2MP, 3MP, 22DMB and 23DMB in AFI and MOR at 300 K. In AFI the sorption hierarchy at high mixture loadings is 23DMB > 22DMB ≈ 3MP > 2MP > > nC6; this hierarchy is opposite of that observed in Fig. 14 for MFI. In MOR, the sorption hierarchy at high mixture loadings is 23DMB > 22DMB ≈ 3MP ≈ 2MP > > nC6. The sorption hierarchy in AFI and MOR are dictated by length entropy effects.

4 Concluding remarks

In this review we have demonstrated the power of CBMC simulations in determining the adsorption isotherms for pure alkanes and their mixtures in various zeolites. Besides providing useful data for zeolite process design, molecular simulations provide insights not possible by experiments alone. The inflection in the isotherm of branched alkanes in MFI, is due to preferential location at the intersections between straight and zig-zag channels. CBMC simulations also help to highlight subtle entropy effects. For binary mixtures of linear alkanes, size entropy effects come into play at high mixture loadings and these counter chain length effects to reduce separation selectiv-
Fig. 14 (a) CBMC simulations of component loadings for equimolar mixture of nC₆, 2MP, 3MP, 22DMB and 23DMB in MFI at 300 K. (b) Elution profiles in a pulsed chromatographic experiment. 

Fig. 15 Component loadings in an equimolar 8-component mixture nC₅–2MB–nC₆–2MP–22DMB–nC₇–2MH–22DMP at 300 K in MFI as a function of total mixture loading Qₘᵢₓ.

Fig. 16 CBMC simulations of sorption selectivity in a 50:50 mixture of nC₆–2MP at 300 K in various zeolite structures.

ities; see Figs. 10 and 11. The molecule of the smaller size is preferentially adsorbed at high loadings because the few empty voids can be more easily filled up. For sorption of linear and mono-branched isomers in MFI the selectivity increases in favour of the linear isomer for mixture loadings > 4; see Figs. 12–15. This is due to configurational entropy effects. This effect is so strong that the branched alkanes are virtually excluded from the MFI matrix at saturation loadings. The configurational entropy concept can be exploited in practice to separate a mixture of linear and branched isomers in the 5–7 C atom range. 28

In AFI and MOR zeolites, consisting of cylindrical channels, the length entropy effect comes into play and this favours the sorption of the isomer with the lower molecular length; see Figs 16 and 17.

For any separation task, CBMC simulations can be used to screen promising zeolite structures on the basis of their sorption selectivities at equilibrium; see e.g. Fig. 16. The more conventionally used method of using Henry coefficients to screen zeolites can lead to pessimistic conclusions because it does not reflect the subtle entropy effects that manifest at higher loadings.

There are many separations using zeolites that rely on differences in the rates of diffusion, rather than on differences in sorption loadings at equilibrium. Even in such cases, sorption isotherms are required because sorption and diffusion phenomena are intertwined, as has been shown by Krishna and Paschek. 3

Finally, we would like to add a note of caution with regard to the predictions of the sorption isotherms from CBMC simulations. These simulations pertain to ideal, rigid, crystalline zeolite structures, free from defects. In practice, zeolites are almost never defect free and there is some flexibility in the lattice; these may cause significant deviations between simulations and experiment. 41 For zeolite process design, therefore, experiments are indispensable; the role of molecular simulations in this case would be to steer the experimental effort in fruitful directions.

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6 References
