Stability Study of a Mixed Islanded Power Network

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Abstract—This paper presents the modeling, simulation and analysis of the dynamic behavior of a mixed power network of 2.78 GW including hydro, thermal and wind power plants. The modeling of each power plant is described. The set of parameters of the turbine speed governor of the hydroelectric power plant is determined with a specific identification procedure to achieve stable operation for different cases such as interconnected, isolated or islanded operation. The analysis of the stability of the entire mixed islanded power plant is investigated through time domain simulations for different sets of controllers parameters and for different disturbances (load rejection and turbulent wind speed profile).

Index Terms—Wind park, hydroelectric power station, power network, stability, identification

I. INTRODUCTION

RENEWABLE energy sources like wind farms and hydroelectric power plants will play in the next coming years a more important role in the production of electricity. The stability study and analysis of the transient behavior of mixed power networks involving different types of energies such as hydro, thermal and wind power, become an important challenge for planners of such complex power networks.

The aim of the present study is to investigate the dynamic behavior of an islanded power network of 2.78 GW presented in Fig. 1, featuring about 17% of wind power, 35% of hydropower and 47% of thermal power. It is well-known that the governor control characteristics of the hydroelectric units have a great importance to stabilize the network, and accurate turbines models are also very important for the controllers’ parameters tuning [1] [2]. Therefore, the power system behavior is analyzed from the hydroelectric power plant point of view in order to determine the best control parameters set of the hydraulic turbine speed governor to guarantee the stability of the frequency of the mixed islanded power network.

In order to determine the control parameters of the hydroelectric power plant, an identification procedure is used in the present study. It consists of the determination of a discrete transfer function of the turbine. The input and output signals are respectively the guide vanes opening and the turbines speed. Two different input signals are employed: a pseudo random binary sequence (PRBS) is used to estimate high-frequency Bode diagram (0.5 to 20 Hz), and a square-wave signal is used to estimate low frequency Bode diagram (0 to 0.5Hz). A similar process of identification was successfully implemented for a pump-storage unit [3]. This identification procedure has been applied for different cases of operation of the network: interconnected, isolated and islanded operation. For each case of operation, the corresponding turbine transfer functions are deduced and governor parameters determined.

The paper is organized as follows. First, the models of different power plants are presented in section II. The identification procedure is described in section III, and the results of identification of the governor parameters are presented in section IV. Finally, the performances of different sets of controllers’ parameters are compared in section V through time domain simulations in the case of a load rejection and turbulent wind speed profile.

II. MODELING

A. Power network presentation

Figure 1 presents the power network comprising a 1.3GW thermal power plant, a 1.0GW hydroelectric power plant and a 480MW wind farm. Table I presents three circuit breaker configurations. Each configuration represents one mode of operation, as described below:

1) Interconnected operation: only the hydroelectric power plant is connected to an infinite network;
2) Isolated operation: the hydroelectric power plant is connected to a passive consumer load;
3) Islanded operation: the three power plants are connected to a passive consumer load.

The transmission lines of 500KV have the same parameters: \( R = 0.1\Omega \) and \( L = 1mH \). The power network represented in Fig. 1 is simulated using the software package SIMSEN, developed for the simulation and the analysis of power systems [4], [5], [6]. The modeling of the 3 power plants are presented below.

![Fig. 1. Layout of the mixed power network.](image-url)
TABLE I
CIRCUIT BREAKERS CONFIGURATION.

<table>
<thead>
<tr>
<th>Operation</th>
<th>CB A</th>
<th>CB B</th>
<th>CB C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Interconnected</td>
<td>ON</td>
<td>OFF</td>
<td>OFF</td>
</tr>
<tr>
<td>Isolated</td>
<td>OFF</td>
<td>ON</td>
<td>OFF</td>
</tr>
<tr>
<td>Islanded</td>
<td>OFF</td>
<td>ON</td>
<td>ON</td>
</tr>
</tbody>
</table>

Fig. 2. Hydroelectric power plant layout.

B. Hydroelectric power plant model

1) Hydraulic circuit modeling: The hydraulic components are modeled in SIMSEN with an equivalent electric circuit, where pressure is analogue to voltage and discharge is analogue to current, leading to a T-shaped equivalent circuit diagram modeling an elementary hydraulic pipe. Based on this approach, other hydraulic components models such as pipes, valves, surge tanks and turbines are presented in [7] or [8]. The modeling of the hydraulic system takes into account water hammer, mass oscillation, and turbine characteristics effects.

2) Hydroelectric power plant model: The 1GW hydroelectric power plant model of Fig. 2 is composed of four Francis turbines and four synchronous machines of 250 MVA rated power each. The turbines are connected to the upstream dam through a 5km gallery, a surge tank and a 1.1km penstock. The maximum head is 315m. The turbines are modeled using the turbine characteristics $Q_{ll} = Q_{ll}(N_{ll})$ and $T_{ll} = T_{ll}(N_{ll})$ where $N_{ll}$, $Q_{ll}$ and $T_{ll}$ are respectively the speed, discharge and torque factors, see [7]. The excitation system has a standard PID voltage regulator. Its model is based on the block diagram of the regulator UNITROL developed by ABB.

C. Wind farm model

1) Wind turbine model: A great variety of wind turbines architectures had been developed [9] [10] [11]. The architecture modeled in this work is a doubly fed induction generator, hereafter DFIG, with variable speed of ±7% [12] [13]. The general diagram is presented in Fig. 3. The power converter control is shown in Fig. 4. The chosen control strategy optimizes the conversion of power by using a look-up table defining the optimal turbine speed $n_{set}$ and the optimal pitch angle $\theta_{p, set}$, set according to the wind velocity. Moreover, the rotational speed is selected in order to maximize the turbine power coefficient.

Indeed, the mechanical power $P_m$ transmitted by the wind to the turbine is calculated as follows [11]:

$$P_m = \frac{1}{2} \rho C_p C_{\infty} \frac{\pi D_{ref}^2}{4}$$

where $C_p$ is the power coefficient, $C_{\infty}$ is the wind velocity, $D_{ref}$ is the turbine diameter and $\rho$ is the density of the fluid. $C_p$ can be approximated using [11]:

$$C_p = \frac{1}{2} \left( 116 \lambda_i - 0.4 \beta_{p} - 5 \right) e^{-\frac{\lambda}{\lambda_i}}$$

$$\lambda = \frac{\omega_{turbine} R_{ref}}{C_{\infty}}$$

$$\lambda = \frac{\omega_{turbine} R_{ref}}{C_{\infty}}$$

The power coefficient $C_p$ is a function of the pitch angle $\theta_p$ and tip speed ratio $\lambda$, which is function of the turbine speed $\omega_{turbine}$ in [rad/s]. So, an optimal speed exists for a given wind velocity and pitch angle. The $C_p$ curves as a function of $\lambda$ and $\theta_p$ are presented in Fig. 5.

2) Wind farm aggregate model: The wind farm considered for this study is a collection of 96 wind turbines represented in Fig. 6.

In order to reduce the dimension of the global system equation set and thus, reducing computational effort, an aggregated model of the wind farm can be employed [15] [16]. It consists of one wind turbine equivalent model of the whole wind

Fig. 3. Doubly fed induction generator diagram.

Fig. 4. Power converter control.

The main parameters of the wind turbine model are presented in Table II. More details about the DFIG architecture can be found in [14].
TABLE II
WIND TURBINE PARAMETERS

<table>
<thead>
<tr>
<th>Turbine</th>
<th>Rated rotational speed</th>
<th>$N_n = 17 \text{rpm}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rated power</td>
<td>$P_n = 5 \text{MW}$</td>
</tr>
<tr>
<td></td>
<td>Rated wind speed</td>
<td>$C_n = 14 \text{m/s}$</td>
</tr>
<tr>
<td></td>
<td>Referential diameter</td>
<td>$D_{ref} = 118.6 \text{m}$</td>
</tr>
<tr>
<td></td>
<td>Turbine inertia</td>
<td>$J = 7.89 \cdot 10^6 \text{kgm}^2$</td>
</tr>
<tr>
<td></td>
<td>Torsional stiffness of shaft</td>
<td>$K = 2.4 \cdot 10^9 \text{Nm/rad}$</td>
</tr>
<tr>
<td></td>
<td>Viscous damping</td>
<td>$C = 162050 \text{Nms/rad}$</td>
</tr>
<tr>
<td></td>
<td>Gear box ratio</td>
<td>$N_{gb} = 19.6$</td>
</tr>
</tbody>
</table>

DFIG machine

<table>
<thead>
<tr>
<th>Rated power</th>
<th>$S_n = 5 \text{MVA}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated voltage</td>
<td>$U_{ns} = 15.75 \text{kV}$</td>
</tr>
<tr>
<td>Frequency</td>
<td>$F_n = 50 \text{Hz}$</td>
</tr>
<tr>
<td>Winding ratio stator/rotor</td>
<td>$u = 0.7917$</td>
</tr>
<tr>
<td>Pairs of poles</td>
<td>$P_p = 9$</td>
</tr>
<tr>
<td>Rotor inertia</td>
<td>$J = 162110 \text{kgm}^2$</td>
</tr>
</tbody>
</table>

The total power of the equivalent turbine in this case is $P_{total} = 96 \times 5 \text{MW} = 480 \text{MW}$.

The electrical parameters are defined in per unit, and thus are also valid for aggregate model.

3) Wind farm modeled with an array of aggregate models: The aggregate model imposes the same wind conditions to every turbine. As the area of a wind farm is large enough to expect an irregular distribution of the wind, it is necessary to modify the aggregate model to take into account the wind irregularity inside the wind farm. Two effects reinforce this assumption: (i) the park effect: the wind turbines placed close to each other are simultaneously shadowing each other; (ii) the wake effect: the turbulence produced by the blades of the wind turbine inducing a stronger turbulence on the last rows of turbines. One of the consequences is a difference in the total mechanical power transmitted to the wind farm. Another difference to be considered is the difference of potential energy accumulated in the shafts of each turbine [15].

In order to consider an irregular distribution of the wind, an array of aggregate models is used, as proposed by [15] and presented in Fig. 6. Thus, six aggregate models representing each row of the wind farm are simulated with different wind velocities. The wind velocity decreases 0.5m/s each time it passes through a row.

D. Thermal power plant model

The model of the 1.3GW thermal power plant is based on steam flux and takes into account a constant pressure steam vessel, a regulating valve, a high pressure steam turbine, a re-heater and two low pressure steam turbines as presented in Fig. 7 [17].

III. IDENTIFICATION PROCEDURE

In order to select the appropriate hydraulic turbine speed governor parameters, it is necessary to deduce the turbine transfer function. The hydraulic turbine transfer function is calculated as the ratio of the discrete Fourier transform of the turbine’s speed $N_k$ and discrete Fourier transform of the guide vane opening $Y_k$.

Samples with period $\tau$ of the continuous time signals $y$ and $n$ obtained by a time domain simulation are considered for the discrete Fourier transforms. Two different sets of inputs are used. First, a pseudo random binary sequence is used to estimate the system’s high frequency response for frequency range of 0.5 to 20 Hz. For low frequencies, below 0.5 Hz, a square wave input with a 2000s period is used. The reason for using a square wave input is to avoid prohibitive simulation time required to properly estimate the transfer function for low frequencies using a PRBS input. Figure 8 presents the general process.

IV. FREQUENCY DOMAIN ANALYSIS

One of the targets of this study is to characterize the power network as seen from the hydro turbine. The identification of the transfer function for different operation modes aims
to evidence that in islaned operation, the system behaves differently from the other modes of operation.

One of the classical approaches is to use a set of parameters of the turbine governor dimensioned for isolated operation\(^1\). The other approach realized in this study consists of the design of optimized set of parameters of the turbine governor for islaned operation. Thus, when the network starts operating in islaned mode (being disconnected from a larger grid), the turbine governor parameters is adapted to improve the system stability.

To demonstrate the differences in each mode of operation, the Bode diagrams of the turbine transfer function are calculated for interconnected operation, isolated operation and islaned operation. Table III summarizes the initial conditions and references used for the identification of these transfer functions. During the procedure the wind velocity is kept constant and equal to 14\text{m/s}.

### TABLE III
INITIAL CONDITIONS AND SET POINTS.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydroelectric power plant</td>
<td>initial active power</td>
</tr>
<tr>
<td>Thermal power plant</td>
<td>active power reference</td>
</tr>
<tr>
<td>Wind speed</td>
<td>(C_{\text{sc}} = 14\text{m/s})</td>
</tr>
<tr>
<td>Wind farm reactive power</td>
<td>set point</td>
</tr>
</tbody>
</table>

\(^1\)Most governors of hydroelectric generators are tuned to be able to govern isolated loads [18].

C. Hydroelectric power plant in islaned operation

Figure 11 presents the Bode diagram of the hydraulic turbine transfer function for low frequencies in islaned operation. The main difference with the isolated and interconnected operation is a resonant peak that appears for the same frequency as the closed-loop thermal power plant mode\(^2\). The thermal power plant has a clear influence on the hydraulic turbine dynamics which can eventually bring the system to instability if an inappropriate set of parameters of the turbine governor is chosen. The high frequency Bode diagram of the turbine transfer function estimated using the PRBS signal is presented in Fig. 12, where the torsional shaft modes appear [8]. The other network configurations have similar results in this frequency range.

D. Turbine Governor

The hydraulic turbine governor architecture including servomotor model is presented in Fig. 13. The governor is a PID in series with power and speed control loops. The results of the previous section and the governor’s transfer function are used

\(^2\)This mode can be visualized after a load rejection, when the thermal power plant is connected in islaned operation.
to design three turbine governors. The governor' parameters can be adjusted in order to achieve an open-loop frequency response with a desired stability criteria and performance. The set of parameters of the three turbine governors are presented in Table IV. Each set of parameters is described as follows:

1) The first set of parameters related to a classical design defines a governor that imposes 60° of phase margin to the system in isolated operation. The Bode diagram of the governor transfer function in series with the islanded operation system is presented in Fig. 14. It represents the controlled open-loop system. This governor is employed in islanded operation in order to guarantee full-stability.

2) The second set of parameters is selected in order to show an instable behavior due to the interaction between the thermal and hydroelectric power plants as presented in Fig. 15. This example demonstrates the risk for using a not properly designed set of parameters. In this case, the gain in the range near 0.05 Hz would appear lower and the instability could be unpredictable.

3) The third set defines a governor optimized for isolated operation, imposing also a 60° of phase margin, as presented in Fig. 16. This governor is tuned also to minimize the influence of the thermal power plant mode.

Note that there are no general rules for tuning a turbine governor in islanded operation since each power system has its own peculiarities.

V. TIME DOMAIN ANALYSIS

The case of hydroelectric power plant in islanded operation is used to perform two time domain simulations. First, the
three turbine governor parameter sets are compared in the case of a load rejection considering the wind velocity constant and equal to 14 m/s.

The second investigation compares the first and the third governors when a turbulent wind is introduced.

### A. Load rejection

Using the same initial conditions presented in Table III, a 20% load rejection is simulated in the case of islanded operation.

The hydraulic turbine response is presented in Fig. 17, where \( n \) is the turbine speed, \( h \) is the head in the turbine, \( y \) is the guide vane opening \((y \in [0, 1])\) and \( q \) is the discharge. All values are in per unit. One can notice that, as expected, the first and the third governors are stable, while the second governor is unstable.

Figure 18 presents the time evolution of the load voltage frequency, see Fig. 18(a) and of the voltage RMS value, see Fig. 18(b). One can notice that the third governor exhibits better performance for both, frequency and voltage. Even if the turbine governor does not have a direct influence on the voltage control, it introduces a beneficial effect. One important point is that the thermal mode is attenuated with the third governor. The settling times of frequency and voltage are improved as well.

### B. Turbulent Wind

A turbulent wind velocity profile is created, using the wind model described in [19]. Figure 19 presents the wind velocity time evolution. Figure 20 compares the turbine’s performance using the first and third turbine governors. The third governor provides smallest frequency deviation than the first governor, see Fig. 21. However, the third governor solicits the hydraulic turbine more intensively. Indeed, the guide vane opening \( y \), the head \( h \) and the charge \( q \) feature larger variations than using the first governor. In the case of governor \( n^3 \), the hydraulic turbine power control devices, i.e. servomotors, guide vanes and bearings, have higher solicitations. Since the islanded operation mode can be considered as a temporary situation, these strong solicitations are not applied in normal operation.

The third governor performances are presented in Fig. 22, where the total power being consumed and the power delivered by each power plant are represented as function of time. The hydroelectric power plant is the principal supplier of energy compensating the wind power fluctuations. This supplementary power is coming from the inertial masses of the hydro generators and from the turbine governor action. It is interesting to note that the 3 Hz shaft mode of the wind turbine appears in the power curves. This behaviour is explained by the strong coupling between the speed and the electric parameters in the induction generator [15].

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### TABLE IV

**Turbine Governor Parameters**

<table>
<thead>
<tr>
<th>Set</th>
<th>( K_1 )</th>
<th>( K_2 )</th>
<th>( T_1 )</th>
<th>( T_2 )</th>
<th>( T_3 )</th>
<th>( K_{sp} )</th>
<th>( T_{sp} )</th>
<th>( T_{sw} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.7</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>9</td>
<td>0</td>
<td>0.1</td>
<td>0.33</td>
</tr>
<tr>
<td>2</td>
<td>1.0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0.2</td>
<td>0</td>
<td>0.1</td>
<td>0.33</td>
</tr>
<tr>
<td>3</td>
<td>1.2</td>
<td>1</td>
<td>3.18</td>
<td>0.318</td>
<td>1.6</td>
<td>0</td>
<td>0.1</td>
<td>0.33</td>
</tr>
</tbody>
</table>
Fig. 18. Time evolution of (a) the frequency and (b) the load voltage resulting from load rejection.

Fig. 19. Turbulent wind profile.

VI. CONCLUSION

This paper presents the modeling, simulation and analysis of the dynamic behavior of a mixed islanded power network including hydro, thermal and wind power plants of total capacity of 2.78 GW. The analysis is performed in order to select the best control parameters set of the hydroelectric power plant in order to achieve the highest stability of the network frequency. The analysis of the hydraulic turbine transfer function for interconnected, islanded and isolated production modes points out:

- in interconnected operation, the hydraulic turbine operation benefits from high stabilization effects for low frequencies from the connection to the grid;
- in isolated operation, the stability of the hydraulic turbine depends mainly on the hydraulic system dynamics, i.e. mass oscillation, water hammer, turbine characteristics, see also [7];
- in islanded operation, the stability of the hydraulic turbine

Fig. 20. Simulations results with turbulent wind obtained with (a) the first turbine governor and, (b) for the third turbine governor.

Fig. 21. Simulations results with turbulent wind obtained with the governor \( n=1 \) and \( n=3 \) for the load frequency.

Fig. 22. Time evolution of the power produced by each power plant, with the third turbine governor.
is largely influenced by the other production sites; in our test case, the thermal power plant dynamics restricts the performances of the turbine speed governor.

The determination of the hydraulic turbine transfer function considering interconnected, isolated and islanded operation appears to be a very efficient tool to set properly the parameters of the turbine speed governor according to the power network dynamics.

REFERENCES


Christophe Nicolet (M’08) received the M.S. degree in mechanical engineering and the Ph.D. degree from the Ecole polytechnique federale de Lausanne (EPFL), Lausanne, Switzerland, in 2001 and 2007, respectively. Since then, he has been the Managing Director and the Principal Consultant of Power Vision Engineering, Lausanne. He is also a Lecturer at EPFL in the Field of Flow Transients in systems.

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François Avellan received the M.S. degree in hydraulic engineering from INPG, Ecole Nationale Superieure d’Hydraulique, Grenoble, France, in 1977 and, in 1980, he received the Ph.D. degree in engineering from the University of Aix-Marseille II, France. He was a Research associate at the Ecole Polytechnique Federale de Lausanne, Lausanne, Switzerland, in 1980, has been the Director of the Laboratory for Hydraulic Machines since 1994, and was appointed Ordinary Professor in 2003. Prof. F. Avellan is the Chairman of the IAHR Section on Hydraulic Machinery and Systems.