# Photo-ionic cells: Two solutions to store solar 

 energy and generate electricity on demandManuel Mendez $\ddagger$, Pekka Peljo $\ddagger$, Micheal Scalon, Heron Vrubel and Hubert H.
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## 1 Validation of the finite element method

The finite element method was validated by reproducing the calculations by W . John Albery for a thin layer photogalvanic concentration cell. ${ }^{1}$ In the system the photoexited dye A will react with the electron donor R , as described in Eq. S 1 .

$$
\begin{equation*}
\mathrm{A}+\mathrm{R} \xrightarrow{h v} \mathrm{~B}+\mathrm{O} \tag{S1}
\end{equation*}
$$

Now the reduced dye can be oxidized by O in the recombination reaction:

$$
\begin{equation*}
\mathrm{B}+\mathrm{O} \rightarrow \mathrm{~A}+\mathrm{R} \tag{S2}
\end{equation*}
$$

The absorption of light is described by

$$
\begin{equation*}
\partial I / \partial x=-\varepsilon c_{\mathrm{A}} I \tag{S3}
\end{equation*}
$$

where $I$ is the light intensity, $\varepsilon$ the extinction coefficient of A and $c_{\mathrm{A}}$ is the concentration of $A$. The light at the intensity of $I_{0}$ is shining through the light electrode at $x=0$. In the steady state the transport and kinetics of A is:

$$
\begin{equation*}
D_{\mathrm{A}} \frac{\partial^{2} c_{\mathrm{A}}}{\partial x^{2}}-\phi \varepsilon c_{\mathrm{A}} I+k_{r e c} c_{B} c_{O}=0 \tag{S4}
\end{equation*}
$$

where $\phi$ is the quantum efficiency for the generation of B and $k_{\mathrm{rec}}$ is the recombination rate constant. Correspondingly for other species

$$
\begin{align*}
& D_{\mathrm{R}} \frac{\partial^{2} c_{\mathrm{R}}}{\partial x^{2}}-\phi \varepsilon c_{\mathrm{A}} I+k_{r e c} c_{B} c_{O}=0  \tag{S5}\\
& D_{B} \frac{\partial^{2} c_{\mathrm{B}}}{\partial x^{2}}+\phi \varepsilon c_{\mathrm{A}} I-k_{r e c} c_{B} c_{O}=0  \tag{S6}\\
& D_{\mathrm{O}} \frac{\partial^{2} c_{\mathrm{O}}}{\partial x^{2}}+\phi \varepsilon c_{\mathrm{A}} I-k_{r e c} c_{B} c_{O}=0 \tag{S7}
\end{align*}
$$

In the simulated case the $\mathrm{O} / \mathrm{R}$-couple does not react at the electrode, so insulating boundary condition is used. The electrode processes are the reduction of A to B at the dark electrode at $x=l$ and oxidation of B to A at the illuminated electrode at $x=0$. The boundary conditions are therefore

$$
\begin{align*}
& D_{\mathrm{A}}\left(\frac{\partial c_{\mathrm{A}}}{\partial x}\right)_{x=l}=-D_{\mathrm{B}}\left(\frac{\partial c_{\mathrm{B}}}{\partial x}\right)_{x=l}=-i / F A  \tag{S8}\\
& D_{\mathrm{A}}\left(\frac{\partial c_{\mathrm{A}}}{\partial x}\right)_{x=0}=-D_{\mathrm{B}}\left(\frac{\partial c_{\mathrm{B}}}{\partial x}\right)_{x=0}=i / F A \tag{S9}
\end{align*}
$$

The initial values were $c_{\mathrm{A}}=c_{\mathrm{A}, 0}, c_{\mathrm{B}}=0, c_{\mathrm{O}}=0$ and $c_{\mathrm{R}}=c_{\mathrm{R}, 0}$. The diffusion coefficients for the all the species were set as $D$.

The analytical model for the dimensionless form was presented, ${ }^{1}$ where

$$
\begin{align*}
\chi & =x / l  \tag{S10}\\
u & =c_{\mathrm{B}} / c_{\mathrm{A}}^{0}  \tag{S11}\\
p & =I / I_{0}  \tag{S12}\\
\beta & =l \varepsilon c_{\mathrm{A}}  \tag{S13}\\
\gamma & =l \sqrt{\phi \varepsilon I_{0} / D_{\mathrm{A}}}  \tag{S14}\\
\kappa & =l \sqrt{k_{\mathrm{rec}} c_{0} / D_{\mathrm{B}}} \tag{S15}
\end{align*}
$$

The three parameters $\beta$, $\gamma$ and $\kappa$ compare a characteristic length with the cell length $l$. The parameter $\beta$, compares the cell length to the optical length, that is the length over which the dye absorbs the light. When $\beta>1$, all the light is absorbed very efficiently. The parameter $\gamma$ compares the cell length to the generation length. In the light intensity of $I_{0}$ the dye A can diffuse on average a distance of $\sqrt{D_{\mathrm{A}} / \phi \varepsilon I_{0}}$ before being converted to B . The last parameter $\kappa$ compares the cell length to the reaction length, so the distance over which B can diffuse before being converted to A in the recombination reaction.

To validate the model we used, calculations presented in ref. 1 were repeated using the finite element model. The concentration profile of the reduced dye obtained form the analytical solutions in the closed circuit conditions, as well as the light intensity profile for three different parameter values for $\beta$, $\gamma$ and $\kappa$ are shown in Figure S 1 , and the corresponding results obtained with the finite element method are shown in Figure S2.


Figure S1. The light intensity profiles and the concentration profiles of the photoproduct B across the cell for three different values of three different parameter values for $\beta, \gamma$ and $\kappa .{ }^{1}$ Reprinted with permission from Elsevier.


Figure S2. The light intensity profiles of the cases E, D and F calculated with the finite element method.

Comparison of Figures S1 and S2 clearly show that both analytical expressions and finite element method give very similar results. The derivation of the analytical expressions required some assumptions. For finite element method, no assumptions was necessary, and hence the results from the finite element simulations are more accurate, as long as the meshing is refined enough.

## 2 Model for the light absorption, photoreaction and extraction

The mechanism described in the previous chapter was modified to include the formation of the photoexited state A*, where the average life-time of the photoexited state is $\tau$. Now the reactions are photoexitation of A, followed by reaction with electron donor $R$ producing $B$ and $O$, or relaxation of the exited state $A^{*}$ back to $A$.

$$
\begin{align*}
& \mathrm{A} \xrightarrow{h \nu} \mathrm{~A}^{*}  \tag{S16}\\
& \mathrm{~A}^{*}+\mathrm{R} \xrightarrow{k_{\text {pholo }}} \mathrm{B}+\mathrm{O} \tag{S17}
\end{align*}
$$

As previously, the reduced dye can be oxidized by O in the recombination reaction:

$$
\begin{equation*}
\mathrm{B}+\mathrm{O} \xrightarrow{k_{\text {rec }}} \mathrm{A}+\mathrm{R} \tag{S18}
\end{equation*}
$$

or B can be extracted into the oil phase.

The absorption of light is described as previously (Eq. S3) In the steady state the transport and kinetics of A is:

$$
\begin{equation*}
D_{\mathrm{A}} \nabla c_{\mathrm{A}}-\mathbf{u} \cdot \nabla c_{\mathrm{A}}-\varphi \delta c_{\mathrm{A}} I+k_{r e c} c_{B} c_{O}+\frac{c_{\mathrm{A}^{*}}}{\tau}=0 \tag{S19}
\end{equation*}
$$

where $\phi$ is the quantum efficiency for the generation of $\mathrm{B}, k_{\text {rec }}$ is the recombination rate constant and $\tau$ is the lifetime of the exited state. $\mathbf{u}$ is the velocity field. Correspondingly for other species

$$
\begin{align*}
& D_{\mathrm{A}^{*}} \nabla c_{\mathrm{A}^{*}}-\mathbf{u} \cdot \nabla c_{\mathrm{A}^{*}}+\varphi \mathscr{c _ { \mathrm { A } } I - k _ { \text { photo } } c _ { \mathrm { A } ^ { * } } c _ { R } - \frac { c _ { \mathrm { A } ^ { * } } } { \tau } = 0}  \tag{S20}\\
& D_{\mathrm{R}} \nabla c_{\mathrm{R}}-\mathbf{u} \cdot \nabla c_{\mathrm{R}}-k_{\text {photo }} c_{\mathrm{A}^{*}} c_{R}+k_{\text {rec }} c_{B} c_{O}=0  \tag{S21}\\
& D_{B} \nabla c_{\mathrm{B}}-\mathbf{u} \cdot \nabla c_{\mathrm{B}}+k_{\text {photo }} c_{\mathrm{A}^{*}} c_{R}-k_{\text {rec }} c_{B} c_{O}=0  \tag{S22}\\
& D_{\mathrm{O}} \nabla c_{\mathrm{O}}-\mathbf{u} \cdot \nabla c_{\mathrm{O}}+k_{\text {photo }} c_{\mathrm{A}^{*}} c_{R}-k_{\text {rec }} c_{B} c_{O}=0 \tag{S23}
\end{align*}
$$

The reduced dye B can partition into the oil phase, with the partition coefficient defined as:

$$
\begin{equation*}
K=\frac{c_{\mathrm{B}}^{\text {oil }}}{c_{\mathrm{B}}{ }^{\text {aq }}}=\frac{k_{f}}{k_{b}} \tag{S24}
\end{equation*}
$$

Where $k_{f}$ and $k_{b}$ are rate constants for the transfer of B from aqueous phase to DCE phase. This was implemented into the flux boundary condition as described below:

$$
\begin{equation*}
D_{\mathrm{B}, \mathrm{DCE}}\left(\frac{\partial c_{\mathrm{B}, \mathrm{DCE}}}{\partial x}\right)_{x=0}=-D_{\mathrm{B}, \mathrm{aq}}\left(\frac{\partial c_{\mathrm{B}, \mathrm{aq}}}{\partial x}\right)_{x=0}=k_{f} c_{\mathrm{B}, \mathrm{aq}}-k_{b} c_{\mathrm{B}, \mathrm{DCE}} \tag{S25}
\end{equation*}
$$

This set of equations was used to estimate the phase separation in the steady state conditions in 1D. Also, to estimate the photoconversion efficiency of the system
where the two-phase flow in a thin layer is illuminated through the organic phase, 2D simulations with the flow described by the Navier-Stokes equation for the incompressible Newtonian fluids:

$$
\begin{equation*}
\rho(\mathbf{u} \cdot \nabla \mathbf{u})=-\nabla p+\mu \nabla^{2} \mathbf{u} \tag{S26}
\end{equation*}
$$

Where $\rho$ is the density of the material, $p$ is pressure, and $\mu$ is dynamic viscosity of the fluid. The inlet boundary condition for the flow was set as laminar inflow velocity, meaning that for simulation purposes the flow at constant velocity through the inlet 1 m before the cell to allow the fully developed parabolic flow profile at the inlet of the cell. The outlet pressure was set to 0 Pa . The values of water at room temperature were used for both density and viscosity.

For all the species, the boundary conditions at the inflows was constant concentration, and outflow at the outlets $(\mathrm{c}=0)$. The cell walls were set as insulating (no flux through the boundary).

## 3 Calculation of the Galvani potential difference across the liquid-liquid interface

In a system where ionic species of the two immiscible liquid phases are in equilibrium, the potential difference across the interface can be calculated with the Nernst-Donnan equation ${ }^{2}$.

$$
\begin{equation*}
\Delta_{\mathrm{o}}^{\mathrm{w}} \phi=\Delta_{\mathrm{o}}^{\mathrm{w}} \phi_{\mathrm{i}}^{0}+\frac{R T}{z F} \ln \frac{c_{i}^{\mathrm{o}}}{c_{i}^{\mathrm{w}}} \tag{S27}
\end{equation*}
$$

The mass balance for the species $i$ is

$$
\begin{align*}
& n_{i, \text { total }}=n_{i}^{\mathrm{o}}+n_{i}^{\mathrm{w}}  \tag{S28}\\
& V_{\mathrm{o}} c_{i, \text { initial }}^{\mathrm{o}}+V_{\mathrm{w}} c_{i, \text { initial }}^{\mathrm{w}}=V_{\mathrm{o}} c_{i}^{\mathrm{o}}+V_{\mathrm{w}} c_{i}^{\mathrm{w}} \tag{S29}
\end{align*}
$$

Additionally, electroneutrality condition of the both phases must be fulfilled:

$$
\begin{equation*}
\sum_{i} z_{i} c_{i}^{\mathrm{w}}=\sum_{i} z_{i} c_{i}^{\mathrm{o}}=0 \tag{S30}
\end{equation*}
$$

In a case where $V_{\mathrm{o}}=V_{\mathrm{w}}$ combination of the equations (S27-30) gives

$$
\begin{equation*}
\sum_{i} z_{i} \frac{c_{i, \text { total }}}{1+\exp \left[\frac{z F}{R T}\left(\Delta_{\mathrm{o}}^{\mathrm{w}} \phi-\Delta_{\mathrm{o}}^{\mathrm{w}} \phi_{\mathrm{i}}^{0}\right)\right]}=0 \tag{S31}
\end{equation*}
$$

Solution of the equation (S31) by iteration gives the Galvani potential difference of the system in equilibrium, and Nernst equation and mass balance equations can be used to calculate the compositions of both phases, as shown in Table 4 of the main text. The values for the standard potentials of ion transfer for different ions were taken from the Gibbs energy database of our group. ${ }^{3}$ The value for $\mathrm{PF}_{6}{ }^{-}$was estimated from the measured value for dichlorobetzene as -0.070 V , as described in the Supporting Information of ref. 4.

## 4 Preliminary determination of quantum yield

Preliminary experiments carried out in a 1 cm path length quartz cuvette are presented in Figure S3. The spectra before and after 15 minutes of irradiation are presented in Figure. Estimation of the efficiency with which photons are converted into extracted dye in the organic phase ( 2 x moles of photons absorbed/moles of HTh extracted into DCE) gives only 0.34 \% efficiency. This value is obtained assuming that there is $100 \%$ absorption, which is actually not the case as significant amount of light was scattered from the cell. Additionally, since the solution bleaches gradually, more light passes through the cell without being absorbed. In summary, the actual quantum yield is being largely underestimated under these specific experimental conditions. More accurate measurements of the quantum yield are being currently pursued in our lab using a single aqueous droplet and shorter time scales.


Figure S3. Determining the efficiency of the reaction with respect to the number of photons converted to extracted neutral dye (HTh). The separation efficiency of the photo-product (HTh) was determined after irradiating the biphasic cell initially containing aqueous solubilized $\mathrm{Th}^{+}$and $[\mathrm{Co}(\mathrm{II}) \text { EDTA }]^{2-}$ at 543.5 nm for 15 minutes. The electrochemical cell configuration for the biphasic system before illumination is illustrated in Scheme 1B, main text, ( $x=0, y=0, z=0.051$ ). UV-visible spectra of five-fold diluted aqueous phase were obtained before (green) and after (violet) irradiation. .

## References

(1) Albery, W. J.; Archer, M. D. J. Electroanal. Chem. 1978, 86, 1.
(2) Peljo, P.; Girault, H. H. Liquid/Liquid Interfaces, Electrochemistry at. In Encyclopedia of Analytical Chemistry; John Wiley \& Sons, Ltd, 2012.
(3) ElectroChemical database. Gibbs energies of transfer. Available from. Lausanne: Laboratoire d'Electrochimie Physique et Analytique, École Polytechnique Fédérale de Lausanne,; http://sbsrv7.epfl.ch/instituts/isic/lepa/cgi/DB/InterrDB.pl, 2014.
(4) Peljo, P.; Rauhala, T.; Murtomäki, L.; Kallio, T.; Kontturi, K. Int. J. Hydrogen Energy 2011, 36, 10033.

## Simple Thionine CoEDTA Model

### 1.1 Definitions

### 1.1.1 Variables

## Variables 1

## Selection

| Geometric entity level | Entire model |
| :--- | :--- |


| Name | Expression | Description |
| :--- | :--- | :--- |
| eps1 | $6.5 \mathrm{e} 4[\mathrm{~L} / \mathrm{mol} / \mathrm{cm}]$ | extinction coefficient |
| I0 | $1.57 \mathrm{e}-$ <br> $3\left[\mathrm{~mol} / \mathrm{m}^{\wedge} 2 / \mathrm{s}\right]$ | Light intensity |
| S0 | $3.5 \mathrm{e}-5[\mathrm{~mol} / \mathrm{L}]$ | Dye concentration |
| N0 | $1 \mathrm{e}-9[\mathrm{mmol} / \mathrm{L}]$ | Reduced dye concentration |
| R0 | $75[\mathrm{mmol} / \mathrm{L}]$ | Concentration of reduced species |
| O0 | $1 \mathrm{e}-9[\mathrm{mmol} / \mathrm{L}]$ | Concentration of oxidized species |
| tau | $16 \mathrm{e}-6[\mathrm{~s}]$ | Lifetime of the exited state of the dye |
| Abs | $-\log (\mathrm{I} / \mathrm{IO})$ | Absorbance |
| K | 14.6 | Partition of the dye |
| kf | kb*K | Rate of transfer to oil |
| kb | $1[\mathrm{~m} / \mathrm{s}]$ | Rate of transfer to water |
| krec | $3 \mathrm{e} 4[\mathrm{~L} / \mathrm{mol} / \mathrm{s}]$ | Recombination rate 3e5 [L/mol/s] should be 9e4 |
| k | $1 \mathrm{e} 7[\mathrm{~L} / \mathrm{mol} / \mathrm{s}]$ | Quenching rate original $6.7 \mathrm{e} 9[\mathrm{~L} / \mathrm{mol} / \mathrm{s}]$ should be <br> 6.1 e 7 |
| Kphoto | $\mathrm{k} / \mathrm{krec}$ | Photoreaction equilibrium |
| D_Co | $5.35 \mathrm{e}-6\left[\mathrm{~cm}{ }^{\wedge} 2 / \mathrm{s}\right]$ | Diffusion coefficient of Co(II)EDTA in pH 7 |
| D_Th | $5.73 \mathrm{e}-7[\mathrm{~cm} 2 / \mathrm{s}]$ | Diffusion coefficient of thionine |

### 1.2 Transport of Diluted Species 2 (Aq)

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Equations

$$
\nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i}
$$

$$
\mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}
$$

Settings

| Description | Value |
| :--- | :--- |
| Concentration | Linear |
| Compute boundary fluxes | 1 |
| Apply smoothing to boundary fluxes | 1 |
| Value type when using splitting of complex variables | Real |
| Equation form | Study controlled |
| Migration in electric field | 0 |
| Convection | 1 |
| Convective term | Non - conservative form |
| Equation residual | 1 |
| Streamline diffusion | 1 |
| Crosswind diffusion | Do Carmo and Galeão |
| Crosswind diffusion type | 0 |
|  | 0 |
| Isotropic diffusion | 0 |
| Enable space-dependent physics interfaces | $\{0,0,0,0,0\}$ |
| Synchronize with COMSOL Multiphysics | std1/stat |
|  | $1,1,1,1\}$ |
| Show equation assuming |  |

## Used products

COMSOL Multiphysics
Chemical Reaction Engineering Module

### 1.2.1 Convection and Diffusion 1

## Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Equations

$$
\begin{aligned}
& \nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i} \\
& \hdashline \mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}
\end{aligned}
$$

## Settings

## Settings

| Description | Value |
| :---: | :---: |
| Velocity field | User defined |
| Velocity field | $\{0,0,0\}$ |
| Electric potential | User defined |
| Electric potential | 0 |
| Diffusion coefficient | User defined |
| Diffusion coefficient | \{\{D_Th, 0, 0\}, \{0, D_Th, 0\}, \{0, 0, D_Th\}\} |
| Diffusion coefficient | User defined |
| Diffusion coefficient | \{\{D_Th, 0, 0\}, \{0, D_Th, 0\}, \{0, 0, D_Th \} |
| Diffusion coefficient | User defined |
| Diffusion coefficient | \{\{D_Th, 0, 0\}, \{0, D_Th, 0\}, \{0, 0, D_Th \} |
| Diffusion coefficient | User defined |
| Diffusion coefficient | \{\{D_Co, 0, 0\}, \{0, D_Co, 0\}, \{0, 0, D_Co\}\} |
| Diffusion coefficient | User defined |
| Diffusion coefficient | \{\{D_Co, 0, 0\}, \{0, D_Co, 0\}, \{0, 0, D_Co $\}$ \} |
| Bulk material | None |

## Used products

COMSOL Multiphysics

### 1.2.2 No Flux 1

## Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 3 |

## Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{i}=0
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Apply for all species | Apply for all species |

## Used products

COMSOL Multiphysics

### 1.2.3 Initial Values 1

Selection

| Geometric entity level | Domain |
| :--- | :--- |


| Selection | Domain 2 |
| :--- | :--- |

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Concentration | S0 |
| Concentration | 0 |
| Concentration | N0 |
| Concentration | R0 |
| Concentration | O 0 |

Used products
COMSOL Multiphysics

### 1.2.4 Reactions 1

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Equations

$$
\nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i}
$$

Settings

## Settings

| Description | Value |
| :---: | :---: |
| Total rate expression | ```{krec*Naq*O - I*eps1*S + Sst/tau, I*eps1*S - Sst/tau - k*Sst*R, k*Sst*R - krec*Naq*O, -k*Sst*R + krec*Naq*O, k*Sst*R - krec*Naq*O}``` |

Used products
COMSOL Multiphysics

### 1.2.5 Flux 1

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 2 |

## Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{i}=N_{0 j}
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Species S | 0 |
| Species Sst | 0 |
| Species Naq | 1 |
| Species R | 0 |
| Species O | 0 |
| Inward flux | $\{0,0$, kb*No - kf*Naq, 0, 0\} |
| Flux type | General inward flux |
| Bulk concentration | 0 |
| Mass transfer coefficient | 0 |

## Used products

COMSOL Multiphysics

### 1.3 Transport of Diluted Species (Oil)

## Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 1 |

## Equations

$$
\nabla \cdot\left(-D_{i} \nabla c_{i}\right)=R_{i}
$$

$$
\mathbf{N}_{i}=-D_{i} \nabla c_{i}
$$

Settings

| Description | Value |
| :--- | :--- |
| Concentration | Linear |
| Compute boundary fluxes | 1 |
| Apply smoothing to boundary fluxes | 1 |
| Value type when using splitting of complex variables | Real |
| Equation form | Stationary |
| Migration in electric field | 0 |
| Convection | 0 |
| Convective term | Non - conservative form |
| Equation residual | Approximate residual |
| Streamline diffusion | 1 |
| Crosswind diffusion | 1 |
| Crosswind diffusion type | 0 |
|  | Do Carmo and Galeão |


| Description | Value |
| :--- | :--- |
| Enable space-dependent physics interfaces | 0 |
| Synchronize with COMSOL Multiphysics |  |
|  | 0 |
|  | 1 |
| Show equation assuming | std1/stat |

Used products
COMSOL Multiphysics

### 1.3.1 Diffusion

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 1 |

## Equations

$$
\begin{aligned}
& \nabla \cdot\left(-D_{i} \nabla c_{i}\right)=R_{i} \\
& \cdots \cdots \cdots \cdots \cdots \\
& \mathbf{N}_{i}=-D_{i} \nabla c_{i}
\end{aligned}
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Velocity field | User defined |
| Velocity field | $\{0,0,0\}$ |
| Electric potential | User defined |
| Electric potential | 0 |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{D_{-} T h / .8346,0,0\right\},\left\{0, D_{-}\right.\right.$Th/.8346, 0\}, \{0, 0, D_Th/.8346\}\} |
| Bulk material | None |

### 1.3.2 No Flux 1

## Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 1 |

## Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{i}=0
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Apply for all species | Apply for all species |

### 1.3.3 Initial Values 1

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 1 |

## Settings

## Settings

| Description | Value |
| :--- | :--- |
| Concentration | 0 |

### 1.3.4 Flux 1

## Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 2 |

## Equations

$$
\mathbf{- n} \cdot \mathbf{N}_{i}=N_{0 j}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Species No | 1 |
| Inward flux | $-\mathrm{kb}^{*}$ No + kf*Naq |
| Flux type | General inward flux |

### 1.4 General Form PDE (g)

General Form PDE

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

Settings

| Description | Value |
| :--- | :--- |
| Shape function type | Lagrange |
| Element order | Quadratic |
| Compute boundary fluxes | 1 |
| Apply smoothing to boundary fluxes | 1 |


| Description | Value |
| :--- | :--- |
| Value type when using splitting of complex variables | Complex |
| Equation form | Study controlled |
| Dependent variable quantity | Molar flux (mol/(m^2*s)) |
| Source term quantity | None |
| Unit | $\mathrm{mol} / \mathrm{m}^{\wedge} 3 / \mathrm{s}$ |
| Show equation assuming | 0 |

Used products
COMSOL Multiphysics

### 1.4.1 General Form PDE 1

General Form PDE 1

## Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Equations

$$
\begin{aligned}
& e_{a} \frac{\partial^{2} l}{\partial t^{2}}+d_{a} \frac{\partial l}{\partial t}+\nabla \cdot \Gamma=f \\
& \nabla=\frac{\partial}{\partial x}
\end{aligned}
$$

## Settings

## Settings

| Description | Value |
| :--- | :--- |
| Source term | -eps1*S*I |
| Conservative flux | I |
| Damping or mass coefficient | 0 |
| Mass coefficient | 0 |

### 1.4.2 Zero Flux 1

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | No boundaries |

## Equations

$$
-\mathbf{n} \cdot \Gamma=0
$$

### 1.4.3 Initial Values 1

Initial Values 1

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Initial value for I | 0 |
| Initial time derivative of I | 0 |

### 1.4.4 Dirichlet Boundary Condition 1

Dirichlet Boundary Condition 1
Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 2 |

## Equations

$$
I=r
$$

$g_{\text {reaction }}=-\mu$
Settings
Settings

| Description | Value |
| :--- | :--- |
| Value on boundary | I0 |
| Prescribed value of I | 1 |
| Apply reaction terms on | Individual dependent variables |
| Use weak constraints | 0 |

### 1.4.5 Dirichlet Boundary Condition 2

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | No boundaries |

## Equations

$I=r$
$g_{\text {reaction }}=-\mu$

## Settings

Settings

| Description | Value |
| :--- | :--- |


| Description | Value |
| :--- | :--- |
| Value on boundary | 0 |
| Prescribed value of I | 1 |
| Apply reaction terms on | Individual dependent variables |
| Use weak constraints | 0 |

### 1.4.6 Flux/Source 1

Flux/Source 1

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 3 |

## Equations

$$
-\mathbf{n} \cdot \Gamma=g-q l
$$

Settings

## Settings

| Description | Value |
| :--- | :--- |
| Boundary flux/source | 0 |
| Boundary absorption/impedance term | 1 |

### 1.5 Mesh 1

Mesh statistics

| Property | Value |
| :--- | :--- |
| Minimum element quality | 1.0 |
| Average element quality | 1.0 |
| Edge elements | 10000 |
| Vertex elements | 3 |

Mesh 1

### 1.5.1 Size (size)

Settings

| Name | Value |
| :--- | :--- |
| Maximum element size | $2.0 \mathrm{E}-7$ |
| Minimum element size | $4.0 \mathrm{E}-8$ |
| Resolution of curvature | 0.2 |
| Resolution of narrow regions | 1000 |
| Maximum element growth rate | 1.5 |


| Name | Value |
| :--- | :--- |
| Predefined size | Extremely fine |
| Custom element size | Custom |

### 1.5.2 Distribution 1 (dis1)

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 1 |

Distribution 1

Settings

| Name | Value |
| :--- | :--- |
| Distribution properties | Predefined distribution type |
| Number of elements | 5000 |
| Element ratio | 10000 |
| Distribution method | Geometric sequence |
| Reverse direction | On |

### 1.5.3 Distribution 2 (dis2)

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domain 2 |

## Distribution 2

Settings

| Name | Value |
| :--- | :--- |
| Distribution properties | Predefined distribution type |
| Number of elements | 5000 |
| Element ratio | 10000 |
| Distribution method | Geometric sequence |

1.5.4 Edge 2 (edg2)

Selection

$$
\text { Geometric entity level } \quad \text { Remaining }
$$

## 2 Study 2

### 2.1 Time Dependent

Study settings

| Property | Value |
| :--- | :--- |
| Include geometric nonlinearity | Off |

Times: .01, .1, 1, 100, 1000, 10000, 100000
Mesh selection

| Geometry | Mesh |
| :--- | :--- |
| Geometry 1 (geom1) | mesh1 |

Physics selection

| Physics | Discretization |
| :--- | :--- |
| Transport of Diluted Species 2 (chds2) | physics |
| Transport of Diluted Species (chds) | physics |
| General Form PDE (g) | physics |

### 2.2 Solver Configurations

### 2.2.1 Solver 3

Compile Equations: Time Dependent (st1)
Study and step

| Name | Value |
| :--- | :--- |
| Use study | Study 2 |
| Use study step | Time Dependent |

Time-Dependent Solver 1 (t1)
General

| Name | Value |
| :--- | :--- |
| Defined by study step | Time Dependent |
| Time | $\{0.01,0.1,1,100,1000,10000,100000\}$ |
| Relative tolerance | 0.00001 |

## Thionine CoEDTA Model with Extraction 2D

## 1 2D model with convection (mod2)

### 1.1 Definitions

### 1.1.1 Variables

## Variables 2a

## Selection

| Geometric entity level | Entire model |
| :--- | :--- |


| Name | Expression | Description |
| :--- | :--- | :--- |
| eps1 | $7.15 \mathrm{e} 4[\mathrm{~L} / \mathrm{mol} / \mathrm{cm}]$ | extinction coefficient |
| I0 | $1 \mathrm{e}-3\left[\mathrm{~mol} / \mathrm{m}^{\wedge} 2 / \mathrm{s}\right]$ | Light intensity |
| Th0 | $30[\mathrm{mmol} / \mathrm{L}]$ | Thionine concentration |
| STh0 | $1 \mathrm{e}-9[\mathrm{mmol} / \mathrm{L}]$ | Semithionine dye conc |
| LTh0 | $1 \mathrm{e}-9[\mathrm{mmol} / \mathrm{L}]$ | Leucothionine conc |
| R0 | $100[\mathrm{mmol} / \mathrm{L}]$ | Concentration of reduced species |
| O0 | $1 \mathrm{e}-9[\mathrm{mmol} / \mathrm{L}]$ | Concentration of oxidized species |
| tau | $16 \mathrm{e}-6[\mathrm{~s}]$ | Lifetime of the exited state of the dye |
| Abs | $-\log (\mathrm{I} / \mathrm{l0})$ | Absorbance |
| K | 10 | Partition of the leucothionine |
| kf | kb *K | Rate of transfer to oil |
| kb | $10[\mathrm{~m} / \mathrm{s}]$ | Rate of transfer to water |
| krec | $1 \mathrm{e} 3[\mathrm{~L} / \mathrm{mol} / \mathrm{s}]$ | Recombination rate |
| k | $1 \mathrm{e} 6[\mathrm{~L} / \mathrm{mol} / \mathrm{s}]$ | Quenching rate |
| Kphoto | $\mathrm{k} / \mathrm{krec}$ | Photoreaction equilibrium |

1.1.2 Coordinate Systems

Boundary System 1

| Coordinate system type | Boundary system |
| :--- | :--- |
| Identifier | sys1 |

Settings

| Name | Value |
| :--- | :--- |


| Name | Value |
| :--- | :--- |
| Coordinate names | $\{\mathrm{t} 1, \mathrm{n}$, to $\}$ |
| Create first tangent direction from | Global Cartesian |

### 1.2 Geometry 2



Geometry 2

Units

| Length unit | m |
| :--- | :--- |
| Angular unit | deg |

## Geometry statistics

| Property | Value |
| :--- | :--- |
| Space dimension | 2 |
| Number of domains | 2 |
| Number of boundaries | 7 |

1.2.1 Rectangle 1 (r1)

Position

| Name | Value |
| :--- | :--- |
| Position | $\{0,0\}$ |
| Width | 0.0005 |
| Height | 0.01 |
| Size | $\{0.0005,0.01\}$ |

1.2.2 Rectangle 2 ( r 2 )

Position

| Name | Value |
| :--- | :--- |


| Name | Value |
| :--- | :--- |
| Position | $\{-.5 \mathrm{e}-3,0\}$ |
| Width | 0.0005 |
| Height | 0.01 |
| Size | $\{0.0005,0.01\}$ |

### 1.3 Transport of Diluted Species Water (water)

Equations

$$
\begin{aligned}
& \nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i} \\
& \mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}
\end{aligned}
$$

Settings

| Description | Value |
| :--- | :--- |
| Concentration | Linear |
| Compute boundary fluxes | 1 |
| Apply smoothing to boundary fluxes | 1 |
| Value type when using splitting of complex variables | Real |
| Equation form | Study controlled |
| Migration in electric field | 0 |
| Convection | 1 |
| Convective term | Non - conservative form |
| Equation residual | Approximate residual |
| Streamline diffusion | 1 |
| Crosswind diffusion | 1 |
| Crosswind diffusion type | 0 |
|  | 0 |
| Isotropic diffusion | 0 |
| Enable space-dependent physics interfaces | $\{0,0,0,0,0,0\}$ |
| Synchronize with COMSOL Multiphysics | $\{1,1,1,1,1,1\}$ |
|  | std2/time |
| Show equation assuming |  |

Used products

| COMSOL Multiphysics |
| :--- |
| Chemical Reaction Engineering Module |

### 1.3.1 Convection and Diffusion

## Equations

$$
\begin{aligned}
& \nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i} \\
& \cdots \cdots \cdots \cdots \cdots \cdots \cdots \cdots \\
& \mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}
\end{aligned}
$$

## Settings

## Settings

| Description | Value |
| :--- | :--- |
| Velocity field | Velocity field (spf/fp1) |
| Electric potential | User defined |
| Electric potential | 0 |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Bulk material | None |

## Used products

COMSOL Multiphysics

### 1.3.2 No Flux 1

Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{j}=0
$$

## Settings

## Settings

| Description | Value |
| :--- | :--- |
| Apply for all species | Apply for all species |

## Used products

COMSOL Multiphysics

### 1.3.3 Initial Values 1

Settings
Settings

| Description | Value |
| :--- | :--- |
| Concentration | Th0 |
| Concentration | 0 |
| Concentration | STh0 |
| Concentration | LTh0 |
| Concentration | O0 |
| Concentration | R0 |

Used products
COMSOL Multiphysics

### 1.3.4 Reactions 1

Equations

$$
\nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i}
$$

## Settings

Settings

| Description | Value |
| :---: | :---: |
| Total rate expression | ```{krec*STh*Ox - I*eps1*Th + Thst/tau, I*eps1*Th - Thst/tau - k*Thst*Red, k*Thst*Red - krec*STh*Ox, 0, k*Thst*Red - krec*STh*Ox, -k*Thst*Red + krec*STh*Ox}``` |

Used products
COMSOL Multiphysics

### 1.3.5 Flux 1

Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{i}=N_{0 j}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Species Th | 0 |
| Species Thst | 0 |
| Species STh | 1 |
| Species LTh | 0 |


| Description | Value |
| :--- | :--- |
| Species 0x | 0 |
| Species Red | 0 |
| Inward flux | $\left\{0,0,{\left.\text { kb*STh_o }-k f^{*} S T h, ~ 0,0,0\right\}} \begin{array}{ll}\text { Flux type } & \text { General inward flux } \\ \hline\end{array}{ }^{2}\right.$ |

Used products
COMSOL Multiphysics

### 1.3.6 Inflow 1

Equations

$$
c_{i}=c_{0 j}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Concentration | $\{$ Th0, 0, STh0, LTh0, 00, R0\} |
| Apply reaction terms on | All physics (symmetric) |
| Use weak constraints | 0 |

## Used products

## COMSOL Multiphysics

### 1.3.7 Outflow 1

Equations

$$
-\mathbf{n} \cdot D_{i} \nabla c_{i}=0
$$

Used products
COMSOL Multiphysics

### 1.4 Transport of Diluted Species Oil (oil)

Equations

$$
\begin{aligned}
& \nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i} \\
& \mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}
\end{aligned}
$$

Used products

| COMSOL Multiphysics |
| :--- |
| Chemical Reaction Engineering Module |

### 1.4.1 Convection and Diffusion 1

Equations
$\nabla \cdot\left(-D_{i} \nabla c_{i}\right)+\mathbf{u} \cdot \nabla c_{i}=R_{i}$
$\mathbf{N}_{i}=-D_{i} \nabla c_{i}+\mathbf{u} c_{i}$
Settings
Settings

| Description | Value |
| :--- | :--- |
| Velocity field | Velocity field (spf/fp1) |
| Electric potential | User defined |
| Electric potential | 0 |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Diffusion coefficient | User defined |
| Diffusion coefficient | $\left\{\left\{1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0,0\right\},\left\{0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right], 0\right\},\left\{0,0,1 \mathrm{e}-9\left[\mathrm{~m}^{\wedge} 2 / \mathrm{s}\right]\right\}\right\}$ |
| Bulk material | None |

## Used products

COMSOL Multiphysics

### 1.4.2 No Flux 1

Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{j}=0
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Apply for all species | Apply for all species |

Used products
COMSOL Multiphysics

### 1.4.3 Initial Values 1

Settings
Settings

| Description | Value |
| :--- | :--- |
| Concentration | 0 |
| Concentration | 0 |

Used products
COMSOL Multiphysics

### 1.4.4 Flux 1

Equations

$$
-\mathbf{n} \cdot \mathbf{N}_{i}=N_{0 j}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Species STh_o | 1 |
| Species LTh_o | 0 |
| Inward flux | $\{$-kb*STh_o + kf*STh, 0\} |
| Flux type | General inward flux |

## Used products

COMSOL Multiphysics

### 1.4.5 Inflow 1

Equations
$c_{i}=c_{0 j}$.
Settings
Settings

| Description | Value |
| :--- | :--- |
| Concentration | $\{0,0\}$ |
| Apply reaction terms on | All physics (symmetric) |
| Use weak constraints | 0 |

Used products
COMSOL Multiphysics

### 1.4.6 Outflow 1

## Equations

$$
-\mathbf{n} \cdot D_{i} \nabla c_{i}=0
$$

Used products
COMSOL Multiphysics

### 1.5 General Form PDE 2 (Light)

Settings

| Description | Value |
| :--- | :--- |
| Shape function type | Lagrange |


| Description | Value |
| :--- | :--- |
| Element order | Quadratic |
| Compute boundary fluxes | 1 |
| Apply smoothing to boundary fluxes | 1 |
| Value type when using splitting of complex variables | Complex |
| Equation form | Study controlled |
| Dependent variable quantity | Molar flux (mol/(m^2*s)) |
| Source term quantity | None |
| Unit | $\mathrm{mol} / \mathrm{m}^{\wedge} 3 / \mathrm{s}$ |
| Show equation assuming | 0 |

Used products

## COMSOL Multiphysics

### 1.5.1 General Form PDE 1

Equations

$$
e_{a} \frac{\partial^{2} l}{\partial t^{2}}+d_{a} \frac{\partial l}{\partial t}+\nabla \cdot \Gamma=f
$$

$$
\nabla=\left[\frac{\partial}{\partial x}, \frac{\partial}{\partial y}\right]
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Source term | -eps1*Th*I |
| Conservative flux | $\{\mathrm{I}, 0\}$ |
| Damping or mass coefficient | 0 |
| Mass coefficient | 0 |

### 1.5.2 Zero Flux 1

## Equations

$-\mathbf{n} \cdot \Gamma=\mathbf{0}$

### 1.5.3 Initial Values 1

Settings
Settings

| Description | Value |
| :--- | :--- |
| Initial value for I | 0 |
| Initial time derivative of I | 0 |

### 1.5.4 Dirichlet Boundary Condition 1

Equations

$$
I=r
$$

$$
g_{\text {reaction }}=-\mu
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Value on boundary | I0 |
| Prescribed value of I | 1 |
| Apply reaction terms on | Individual dependent variables |
| Use weak constraints | 0 |

### 1.5.5 Flux/Source 1

Equations

$$
-\mathbf{n} \cdot \Gamma=g-q l
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Boundary flux/source | 0 |
| Boundary absorption/impedance term | 1 |

### 1.6 Laminar Flow (spf)

Equations

$$
\begin{aligned}
& \rho(\mathbf{u} \cdot \nabla) \mathbf{u}= \\
& \nabla \cdot\left[-p \mathbf{I}+\mu\left(\nabla \mathbf{u}+(\nabla \mathbf{u})^{\top}\right)\right]+\mathbf{F} \\
& \rho \nabla \cdot \mathbf{u}=0
\end{aligned}
$$

Used products

| COMSOL Multiphysics |
| :--- |
| Chemical Reaction Engineering Module |

### 1.6.1 Fluid Properties 1

Equations

$$
\begin{aligned}
& \rho(\mathbf{u} \cdot \nabla) \mathbf{u}= \\
& \nabla \cdot\left[-p \mathbf{l}+\mu\left(\nabla \mathbf{u}+(\nabla \mathbf{u})^{\top}\right)\right]+\mathbf{F} \\
& \cdots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \\
& \rho \nabla \cdot \mathbf{u}=0
\end{aligned}
$$

### 1.6.2 Wall 1

Equations

$$
\mathbf{u}=\mathbf{0}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Temperature | User defined |
| Temperature | $293.15[\mathrm{~K}]$ |
| Electric field | User defined |
| Electric field | $\{0,0,0\}$ |
| Boundary condition | No slip |
| Apply reaction terms on | Individual dependent variables |
| Use weak constraints | 0 |

### 1.6.3 Initial Values 1

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Velocity field | $\{0,0,0\}$ |
| Pressure | 0 |

### 1.6.4 Inlet 1

Equations

$$
\begin{gathered}
L_{\text {entr }} \nabla_{\mathrm{t}} \cdot\left[-\mathrm{p} \mathbf{l}+\mu\left(\nabla_{\mathrm{t}} \mathbf{u}+\left(\nabla_{\mathrm{t}} \mathbf{u}\right)^{\top}\right)\right]=-p_{\mathrm{entr}} \mathbf{n}, \quad \nabla_{\mathrm{t}} \cdot \mathbf{u}=0 \\
\ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots
\end{gathered}
$$

## Settings

Settings

| Description | Value |
| :--- | :--- |
| Use weak constraints | 0 |
| Boundary condition | Laminar inflow |
| Pressure | 0.02 |
| Laminar inflow option | Average velocity |
| Average velocity | .01 |
| Flow rate | $0.001[\mathrm{~L} / \mathrm{s}]$ |
| Entrance length | 1 |
| Constrain endpoints to zero | 0 |


| Description | Value |
| :--- | :--- |
| Entrance thickness | .002 |
| Standard pressure | $1[\mathrm{~atm}]$ |
| Standard molar volume | $0.0224136\left[\mathrm{~m}^{\wedge} 3 / \mathrm{mol}\right]$ |
| Normal mass flow rate | $1 \mathrm{e}-5[\mathrm{~kg} / \mathrm{s}]$ |
| Mass flow type | Mass flow rate |
| Standard flow rate defined by | Standard density |
| Channel thickness | $1.0[\mathrm{~m}]$ |

### 1.6.5 Outlet 1

Equations

$$
p=p_{0},\left[\mu\left(\nabla \mathbf{u}+(\nabla \mathbf{u})^{T}\right)\right] \mathbf{n}=\mathbf{0}
$$

Settings
Settings

| Description | Value |
| :--- | :--- |
| Apply reaction terms on | All physics (symmetric) |
| Use weak constraints | 0 |
| Boundary condition | Pressure, no viscous stress |
| Pressure | 0 |

## Used products

COMSOL Multiphysics

### 1.7 Mesh 2

Mesh statistics

| Property | Value |
| :--- | :--- |
| Minimum element quality | 0.3344 |
| Average element quality | 0.9593 |
| Triangular elements | 531358 |
| Quadrilateral elements | 1708 |
| Edge elements | 11882 |
| Vertex elements | 6 |

### 1.7.1 Size (size)

Settings

| Name | Value |
| :--- | :--- |
| Calibrate for | Fluid dynamics |


| Name | Value |
| :--- | :--- |
| Maximum element size | $4.5 \mathrm{E}-5$ |
| Minimum element size | $2.0 \mathrm{E}-6$ |
| Resolution of curvature | 0.3 |
| Maximum element growth rate | 1.15 |

### 1.7.2 Size 1 (size1)

## Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundaries 1,7 |

Settings

| Name | Value |
| :--- | :--- |
| Calibrate for | Fluid dynamics |
| Maximum element size | $2.8 \mathrm{E}-5$ |
| Minimum element size | $4.0 \mathrm{E}-7$ |
| Resolution of curvature | 0.25 |
| Predefined size | Finer |

### 1.7.3 Size 2 (size2)

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundaries 2-3, 5-6 |

Settings

| Name | Value |
| :--- | :--- |
| Calibrate for | Fluid dynamics |
| Maximum element size | $2 \mathrm{E}-6$ |
| Minimum element size | $.5 \mathrm{E}-8$ |
| Resolution of curvature | 0.2 |
| Resolution of narrow regions | 1.1 |
| Predefined size | Extremely fine |
| Custom element size | Custom |

### 1.7.4 Size 3 (size3)

Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundary 4 |


| Settings |
| :--- |
| Name Value <br> Calibrate for Fluid dynamics <br> Maximum element size $1 \mathrm{E}-6$ <br> Minimum element size $.50 \mathrm{E}-8$ <br> Resolution of curvature 0.2 <br> Resolution of narrow regions 1.05 <br> Predefined size Extremely fine <br> Custom element size Custom |

1.7.5 Corner Refinement 1 (cr1)

## Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domains 1-2 |

### 1.7.6 Free Triangular 1 (ftri1)

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domains 1-2 |

1.7.7 Boundary Layers 1 (bl1)

Selection

| Geometric entity level | Domain |
| :--- | :--- |
| Selection | Domains 1-2 |

Settings

| Name | Value |
| :--- | :--- |
| Handling of sharp corners | Trimming |

Boundary Layer Properties 1 (blp1)

## Selection

| Geometric entity level | Boundary |
| :--- | :--- |
| Selection | Boundaries 1, 7 |

Settings

| Name | Value |
| :--- | :--- |
| Number of boundary layers | 2 |

1.7.8 Free Triangular 2 (ftri2)

Selection

| Geometric entity level | Remaining |
| :--- | :--- |

2 Navier Stokes ss

### 2.1 Stationary

Study settings

| Property | Value |
| :--- | :--- |
| Include geometric nonlinearity | Off |

Mesh selection

| Geometry | Mesh |
| :--- | :--- |
| Geometry 1 (geom1) | mesh1 |
| Geometry 2 (geom2) | mesh2 |

Physics selection

| Physics | Discretization |
| :--- | :--- |
| Laminar Flow (spf) | physics |

### 2.2 Solver Configurations

### 2.2.1 Solver 5

Compile Equations: Stationary (st1)
Study and step

| Name | Value |
| :--- | :--- |
| Use study | Navier Stokes ss |
| Use study step | Stationary |

Dependent Variables 1 (v1)
General

| Name | Value |
| :--- | :--- |
| Defined by study step | Stationary |

Initial values of variables solved for

| Name | Value |
| :--- | :--- |
| Solution | Zero |

Values of variables not solved for

| Name | Value |
| :--- | :--- |
| Solution | Zero |

## 3 Dye Partitioning 2D ss

### 3.1 Stationary

Study settings

| Property | Value |
| :--- | :--- |
| Include geometric nonlinearity | Off |

Mesh selection

| Geometry | Mesh |
| :--- | :--- |
| Geometry 1 (geom1) | mesh1 |
| Geometry 2 (geom2) | mesh2 |

Physics selection

| Physics | Discretization |
| :--- | :--- |
| Transport of Diluted Species Water (phys1) | physics |
| Transport of Diluted Species Oil (phys2) | physics |
| General Form PDE 2 (g2) | physics |

### 3.2 Solver Configurations

### 3.2.1 Solver 7

Compile Equations: Stationary (st1)
Study and step

| Name | Value |
| :--- | :--- |
| Use study | Dye Partitioning 2D ss |
| Use study step | Stationary |

Stationary Solver 1 (s1)
General

| Name | Value |
| :--- | :--- |
| Defined by study step | Stationary |
| Relative tolerance | 0.000010 |

