

# John Adams Institute for Accelerator Science Lecture Series

Oxford, 21<sup>st</sup> March 2013

## **Crab-waist collisions. From lepton to hadron colliders**

José L. Abelleira, PhD candidate.

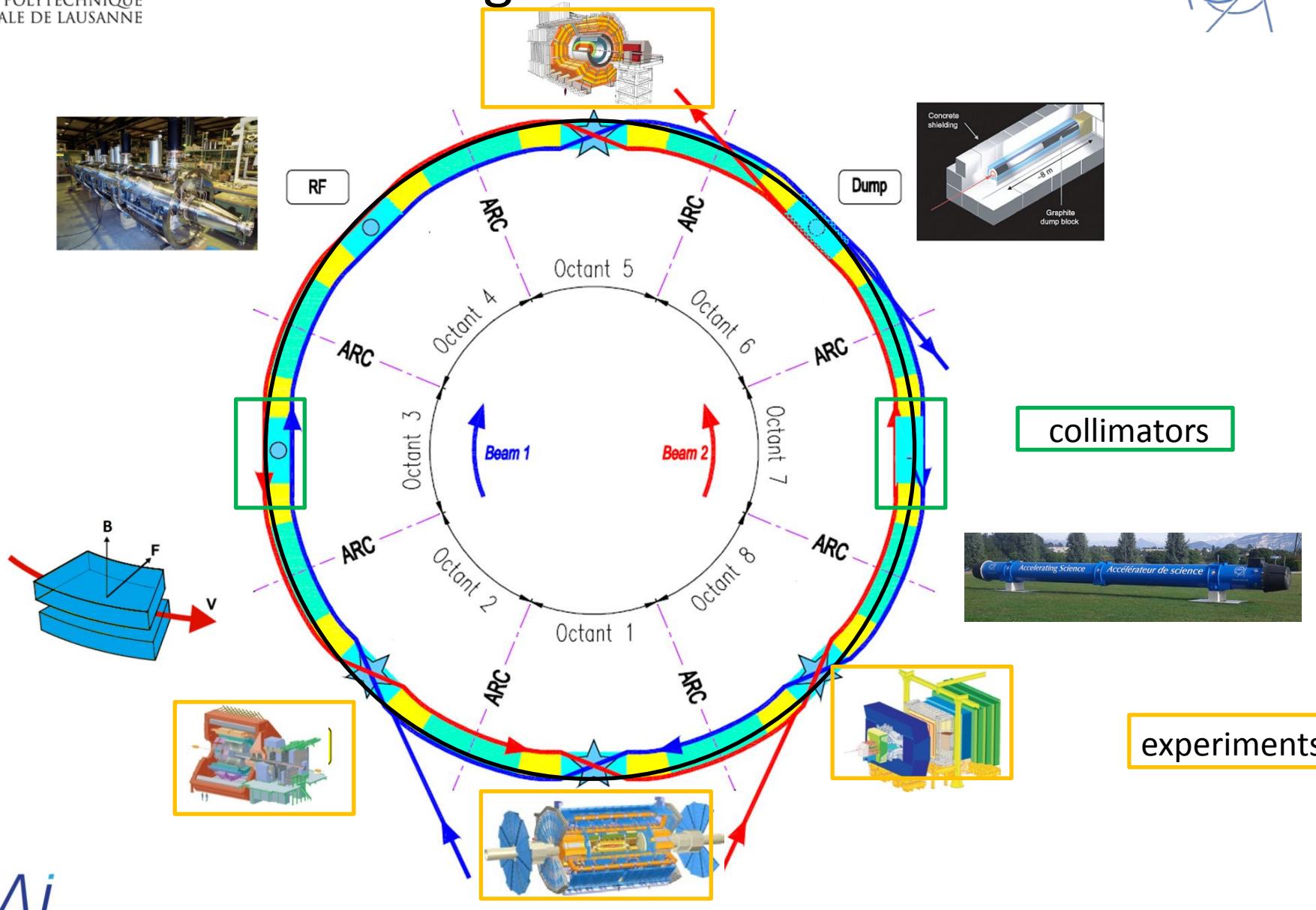
École Polytechnique Fédérale de Lausanne (EPFL)

Thanks to: R. de Maria, S.Russenschuck, F. Zimmermann (CERN), D.Shatilov (BINP SB RAS, Novosibirsk),  
C. Milardi, M. Zobov (INFN/LNF, Frascati (Roma))

# Contents

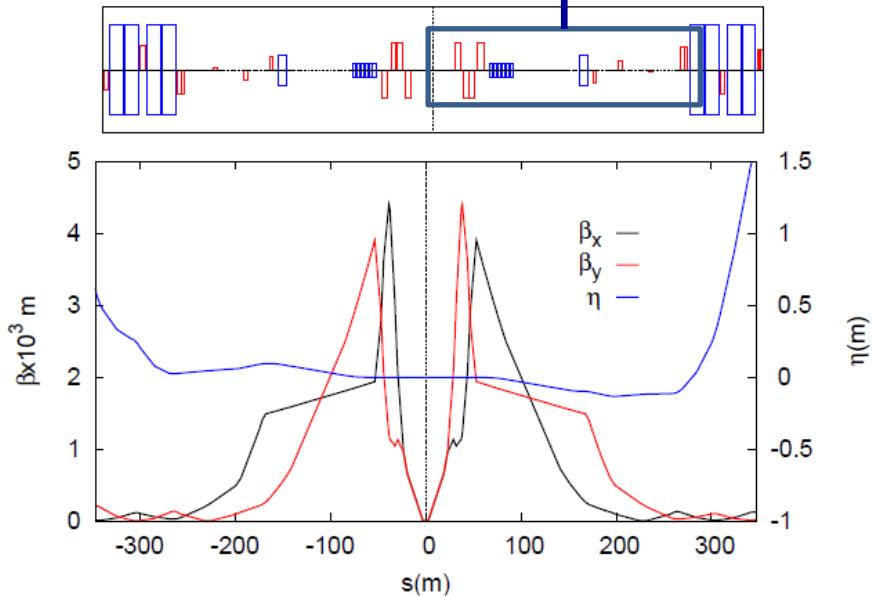
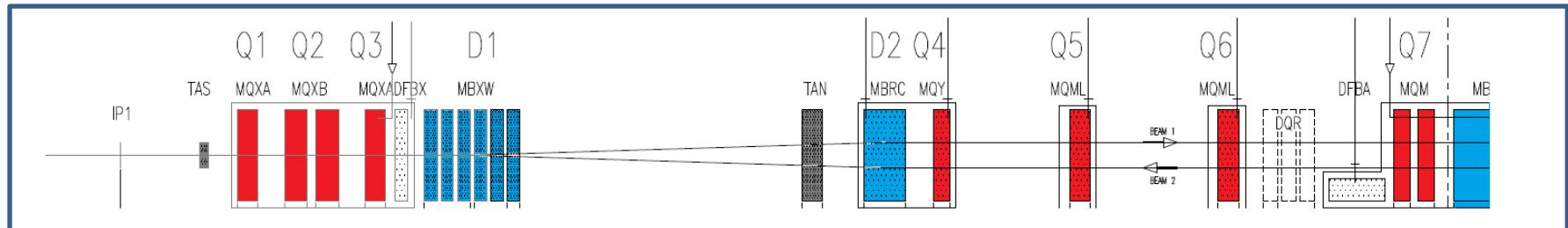
- The LHC
- Flat beams
- Crab-waists collisions concept
- Crab-waist in DAΦNE
- A new IR for LHC

# The Large Hadron Collider

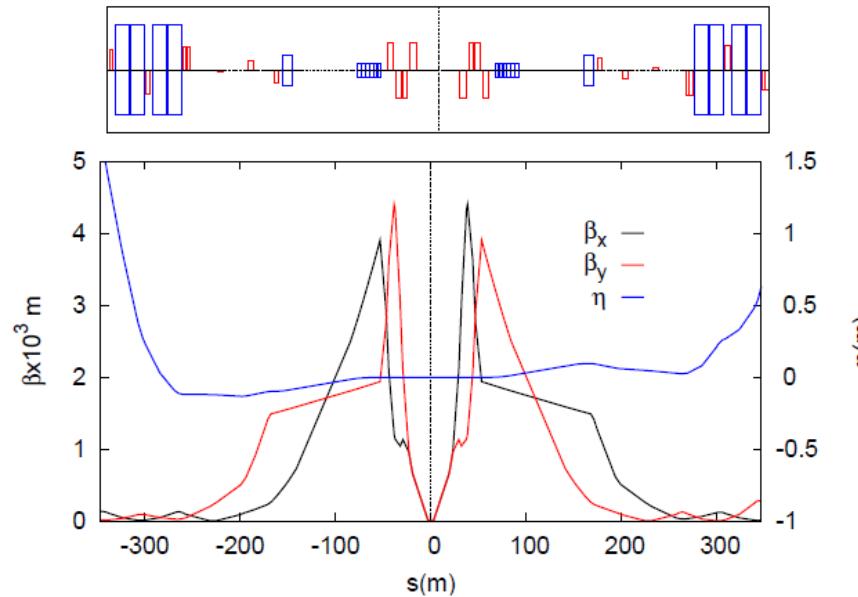


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# LHC final focus system



Beam 1



Beam 2

Antisymmetric optics due to the opposite direction of the beams

# Luminosity

The event rate for a process (number of collisions) is given by the cross section of the process times the luminosity.

$$\frac{dR}{dt} = L\sigma_p$$

Luminosity depends on by the beam parameters as follows.

$$L = \frac{N^2 n_b f}{4\pi \sigma_x^* \sigma_y^*} \frac{1}{\sqrt{1 + \Phi^2}} \quad \Phi = \frac{\theta \sigma_z}{2\sigma_x^*} \quad \text{Piwinski angle}$$

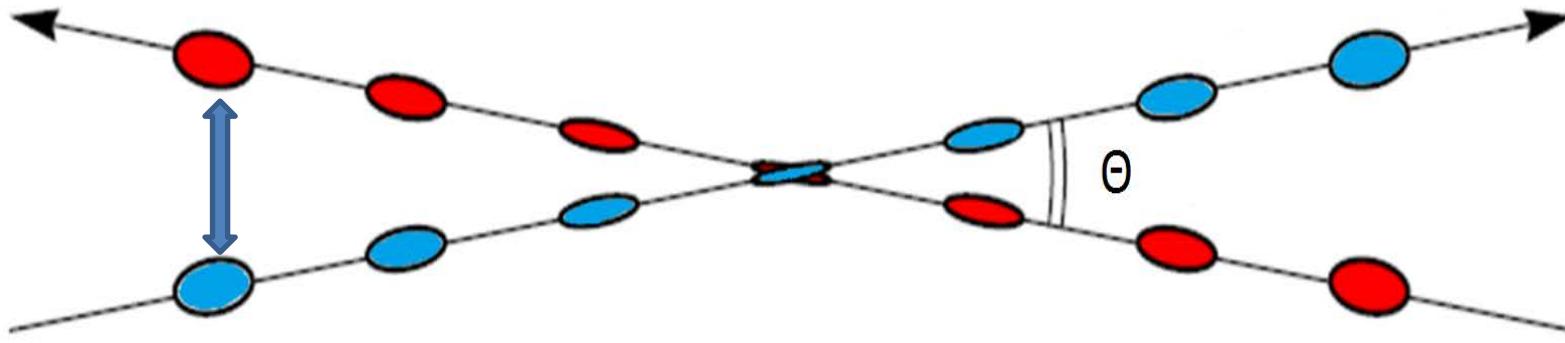
The values for nominal LHC are given

$N$	Particles per bunch.	$1.15 \times 10^{11}$
$n_b$	Number of bunches.	2808
$f$	Revolution frequency	11.245 kHz
$\sigma_{x,y}^*$	Hor/vert beam size at IP*	16.7 μm
$\sigma_z^*$	bunch length	7.55 cm
$\theta$	Crossing angle*	285 μm
$\Phi$	Piwinski angle*	0.64
$L$	Luminosity*	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

\*For the experiments at IP1 and IP5.

# Normalized separation

A crossing angle is introduced to avoid parasitic collisions



Even though there are collisions only in the IP, there are long range interactions between the two beams.

A measure of the interaction between the beams is the normalized separation.

$$\Delta_{sep} = \frac{d_{sep}}{\sigma_x} \approx \frac{\theta}{\sigma_x},$$

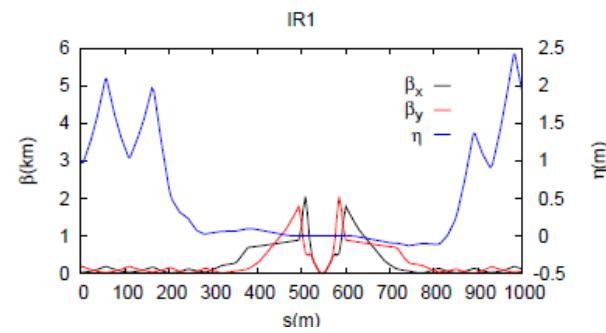
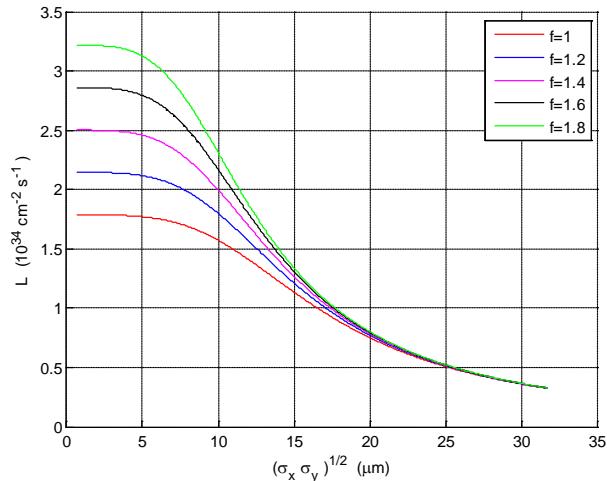
# Flat beams

$$\Delta_{sep} \approx \frac{\theta}{\sigma_x} = \frac{\theta}{\sqrt{\varepsilon/\beta^*_x}}$$

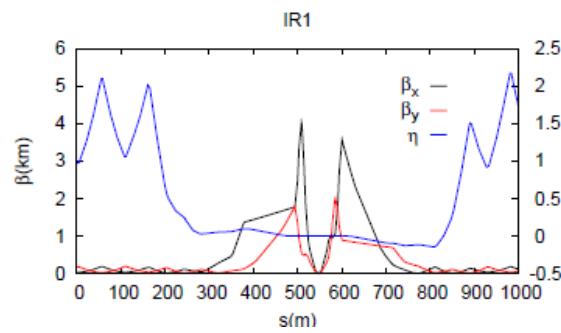
For the same section area  $\sigma_x \sigma_y$

Flat beams increase  $\Delta_{sep}$ , for a given  $\theta$

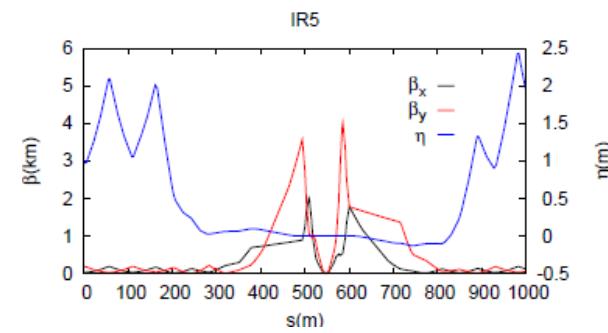
Less  $\theta$  for the same  $\Delta_{sep}$



$$\begin{aligned}\beta_x &= 1.20 \text{ m} \\ \beta_y &= 1.20 \text{ m}\end{aligned}$$



$$\begin{aligned}\beta_x &= 0.60 \text{ m} \\ \beta_y &= 1.20 \text{ m}\end{aligned}$$



$$\begin{aligned}\beta_x &= 1.20 \text{ m} \\ \beta_y &= 0.60 \text{ m}\end{aligned}$$

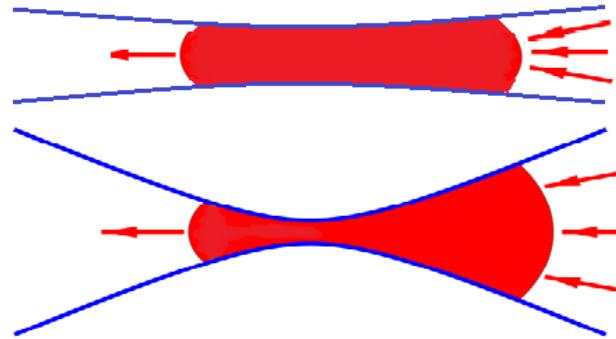
R. De Maria

José L. Abelleira

# Hourglass effect

Beam size is given as  $\sigma = \sqrt{\varepsilon\beta}$ .

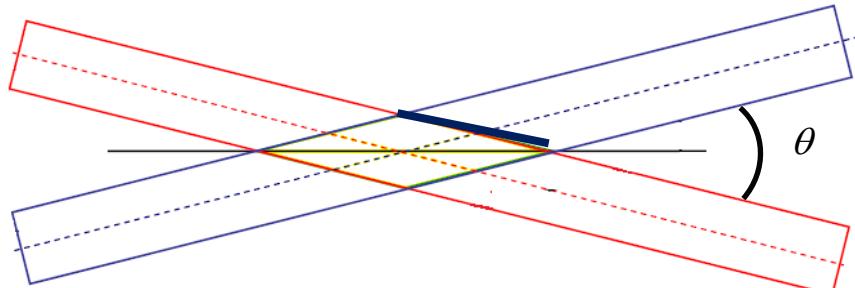
$$\beta(s) = \beta^* + \frac{s^2}{\beta^*}$$



Especially important when the  $\beta$  function at the IP approaches the bunch length.

What is important is the length of the collision section.

## *Length of the Collision section*



With Head-on collisions or small  $\phi$

$$l_{OA} \approx \sigma_z$$

But in Large Piwikins Angle (LPA) regime

$$l_{OA} \approx \frac{2\sigma_x}{\theta}$$

# Crab-waist collisions

An important limitation in hadron machines is beam-beam tune shift

$$L \propto \frac{N\xi_y}{\beta_y}; \quad \xi_y \propto \frac{N\beta_y}{\sigma_x \sigma_y \sqrt{1+\phi^2}}; \quad \xi_x \propto \frac{N}{\varepsilon_x(1+\phi^2)}; \quad \phi = \frac{\theta \sigma_z}{2\sigma_x}$$

## A Large Piwinski Angle $\Phi$ (LPA)

reduces tune shift, allowing  $N \uparrow$

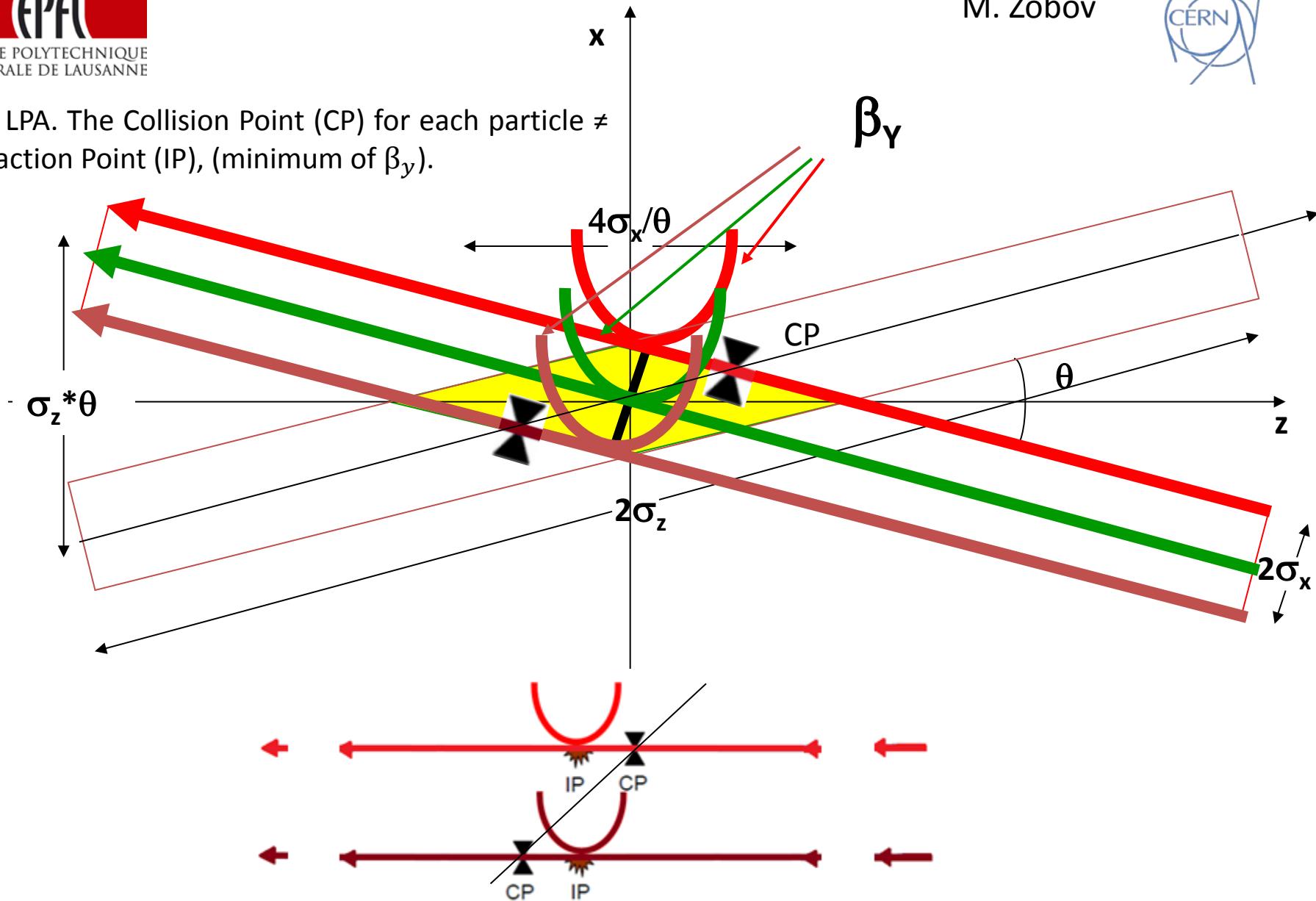
reduces the length of the collision section, allowing  $\beta_y \downarrow$

} More luminosity

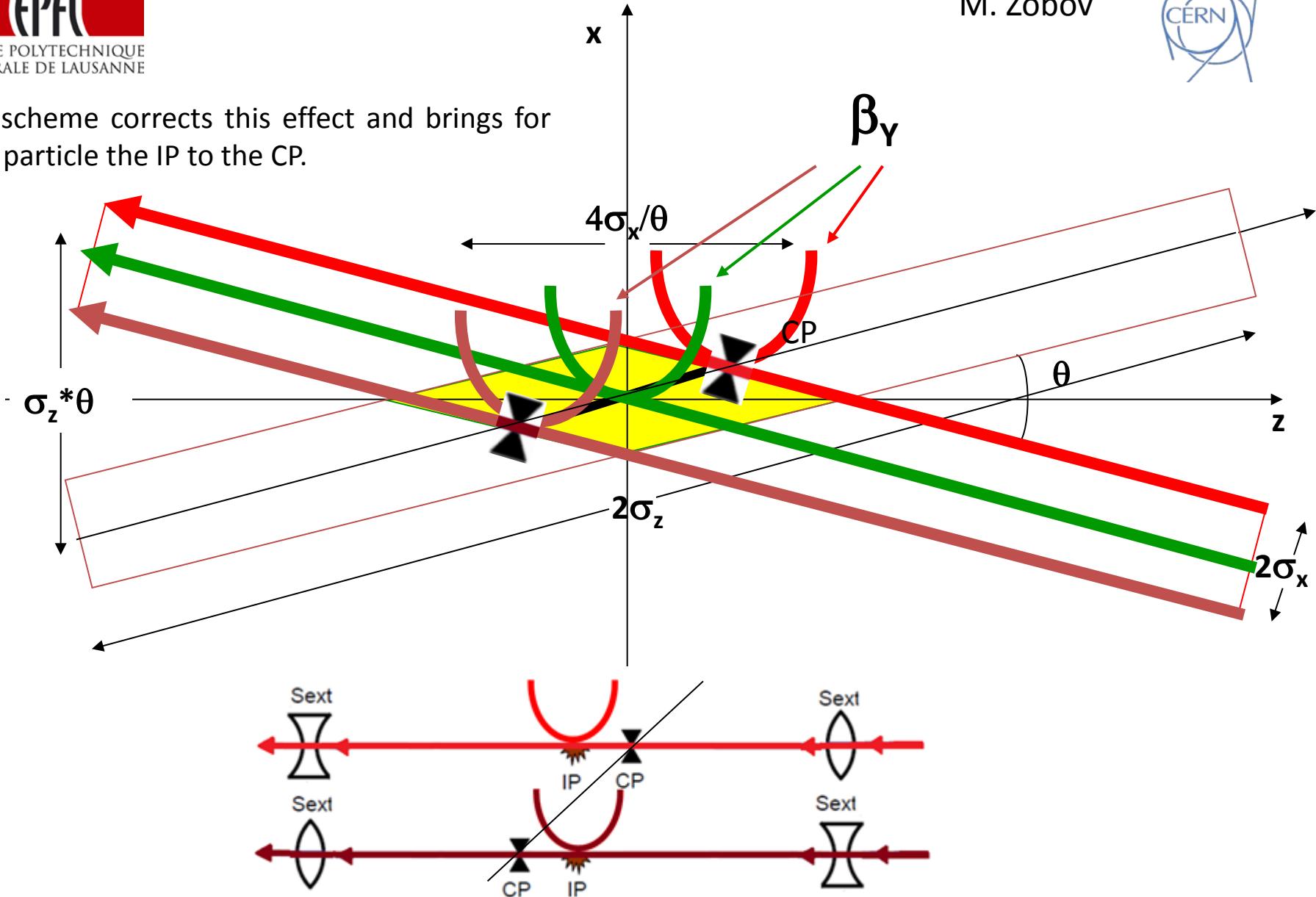
On the other hand, a LPA induces strong X-Y resonances

Suppressed by crab-waist scheme

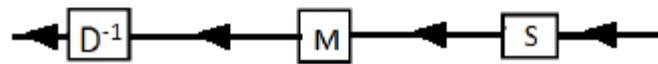
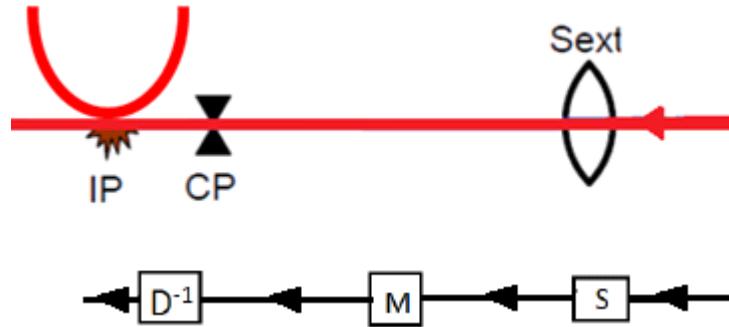
With LPA. The Collision Point (CP) for each particle  $\neq$  Interaction Point (IP), (minimum of  $\beta_y$ ).



C-W scheme corrects this effect and brings for each particle the IP to the CP.



# Crab-waist collisions



$$\hat{M}_y = D^{-1} M_y S = \begin{pmatrix} 1 & \Delta l \\ 0 & 1 \end{pmatrix}^{-1} \begin{pmatrix} \pm \alpha_{CP} \sqrt{\frac{\beta_y^*}{\beta_{y,cs}}} & \pm \sqrt{\beta_{y,cs} \beta_y^*} \\ \mp \frac{1}{\sqrt{\beta_{y,cs} \beta_y^*}} & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -1/f & 1 \end{pmatrix}$$

$$\Delta l = \frac{x_{IP}}{\theta} \quad f = \frac{1}{k_{sl} x_{cs}}$$

# Crab-waist collisions

Conditions for the crab-waist sextupole

$$\begin{aligned}\Delta\mu_x &= \pi m \\ \Delta\mu_y &= \frac{\pi}{2}(2n + 1)\end{aligned}$$

Sextupole strength

$$kl_s = \frac{\sqrt{\beta_x^*/\beta_x}}{\theta\beta_y^*\beta_y}$$

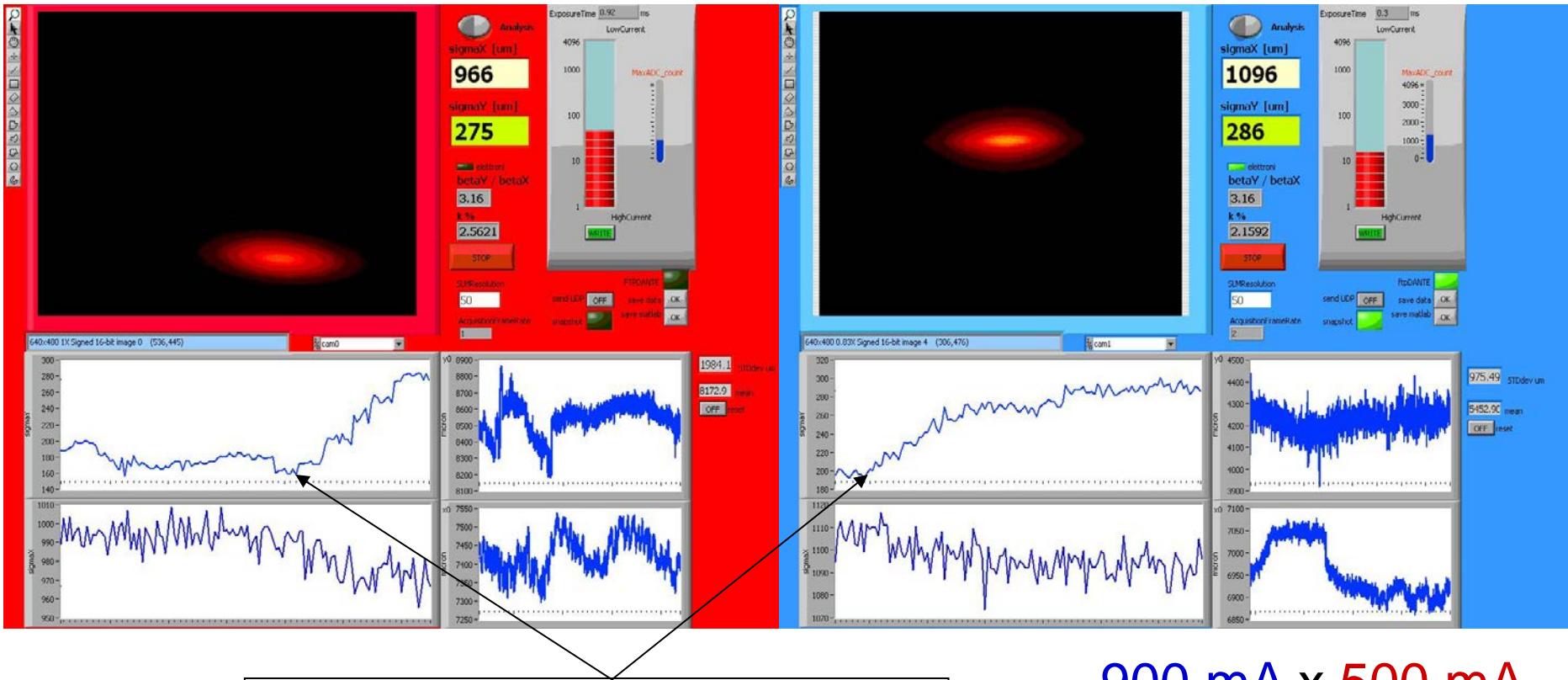
$$\sigma_x^*/\sigma_y^* \geq 10$$

$$\varepsilon_x = \varepsilon_y$$

$$\beta_x^*/\beta_y^* \geq 100$$

Suitable for lepton machines ( $\varepsilon_x \neq \varepsilon_y$ )  
More challenging for hadron colliders

# Crab waist collisions in DAΦNE



Start of switching off the CW sextupoles  
in both rings: 200 A → 0 A

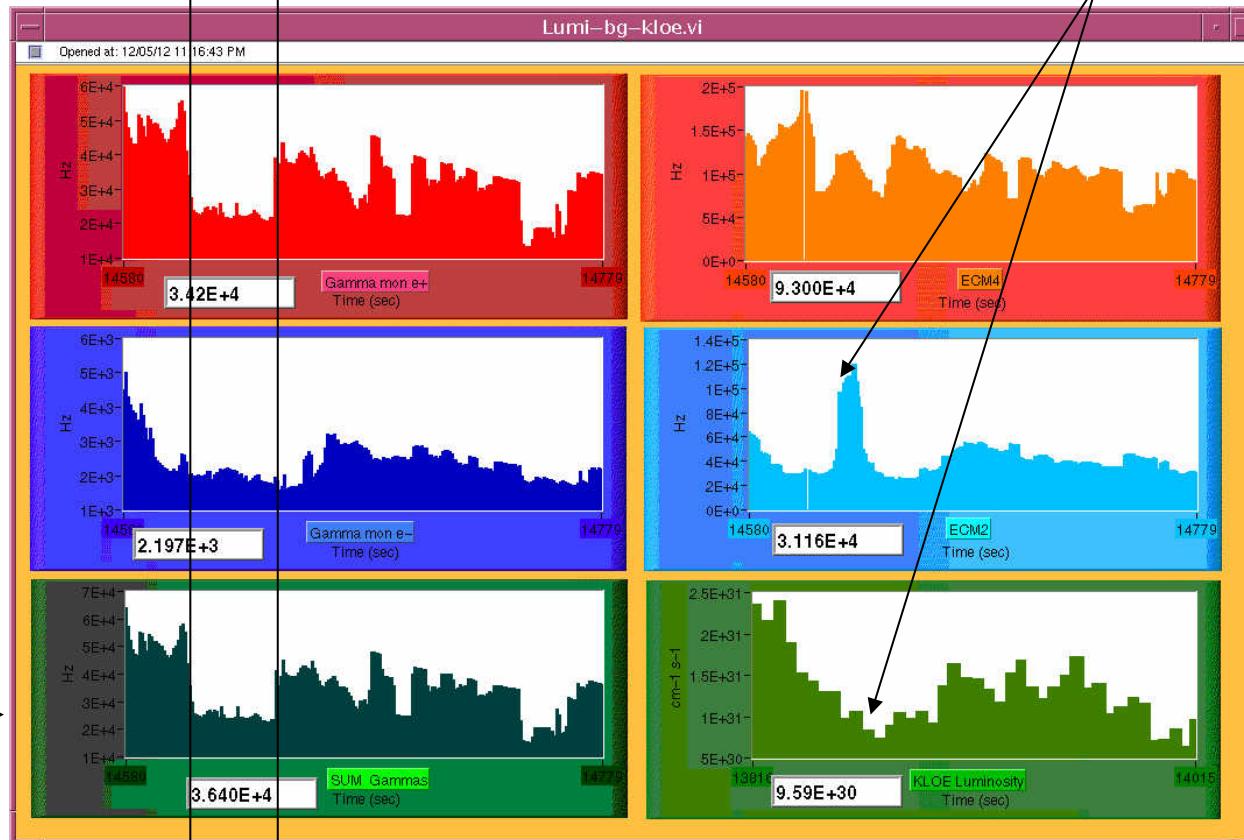
900 mA × 500 mA

C. Milardi  
M. Zobov

# Crab waist collisions in DAΦNE

OFF ON

Minimum luminosity, highest background  
when the sextupoles are OFF



DAΦNE luminosity monitor

C. Milardi  
M. Zobov

José L. Abelleira

# C-W collisions for hadron colliders

There are several facts that make difficult the implementation of crab-waist collisions in LHC:

- Same charge of particles
- Large  $L^*$
- Large energy
- Same emittance in the two planes

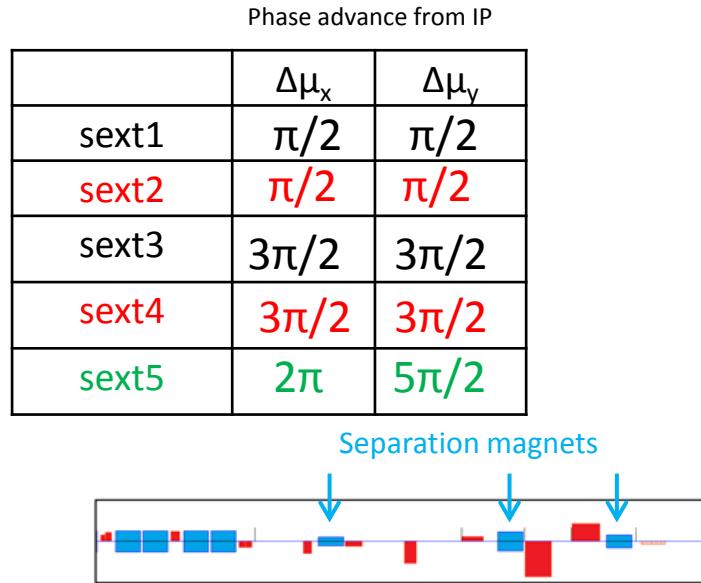
A new IR for HL-LHC is presented with the following ingredients:

- Large Piwinski Angle
- Flat beams
- Local chromatic correction ?
- Crab-waists

# A new IR for LHC

$$\beta_x^* = 1.5 \text{ m}$$

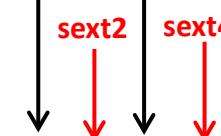
$$\beta_y^* = 1.5 \text{ cm}$$



Local chromatic correction in both planes + crab-waist collisions

Chromatic correction

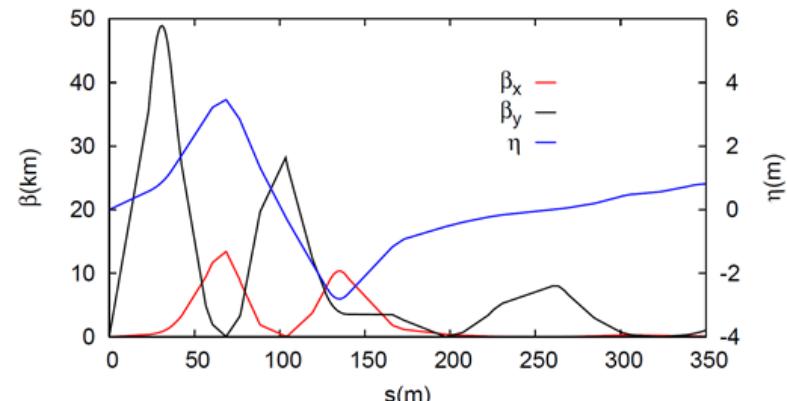
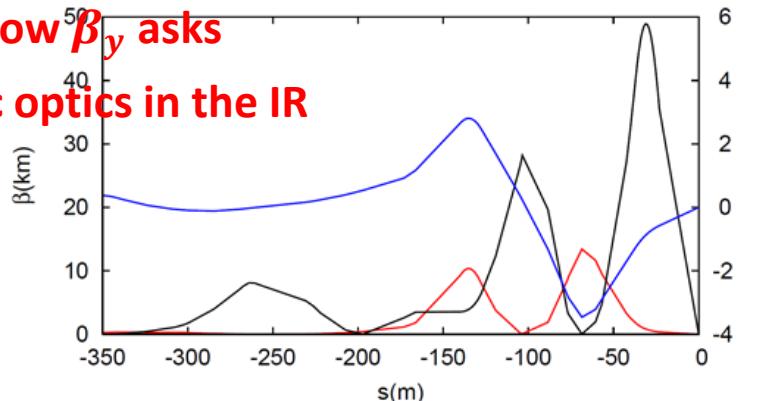
sext1    sext3



CRAB-WAIST SEXTUPOLE

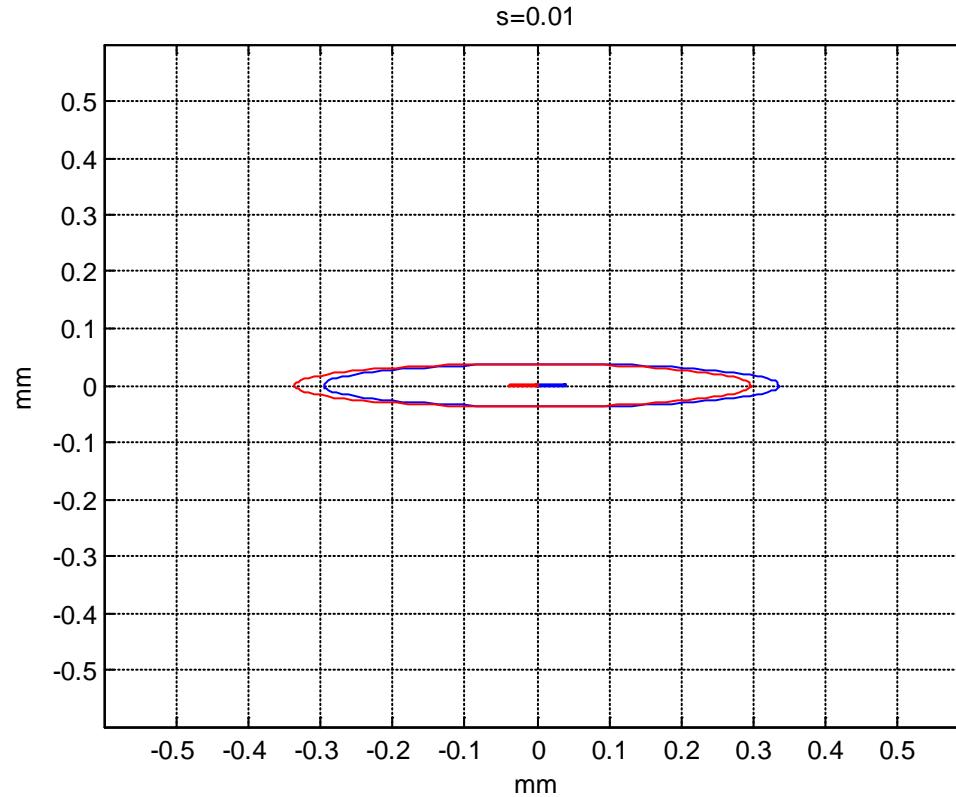


The extremely low  $\beta_y$  asks  
for a symmetric optics in the IR

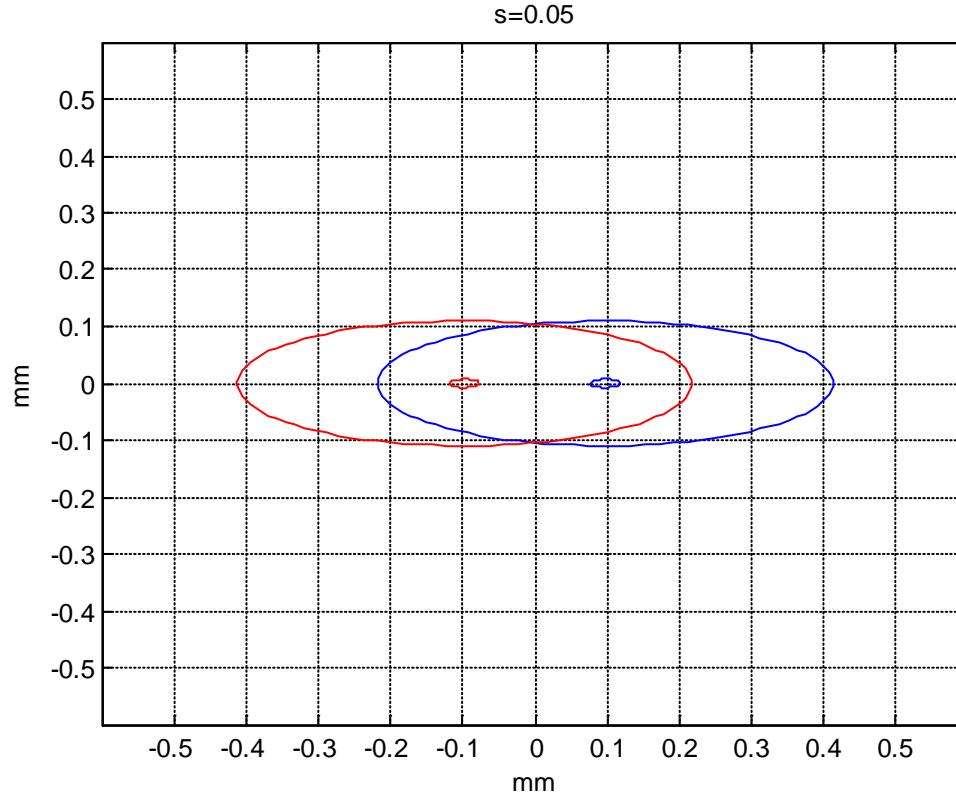


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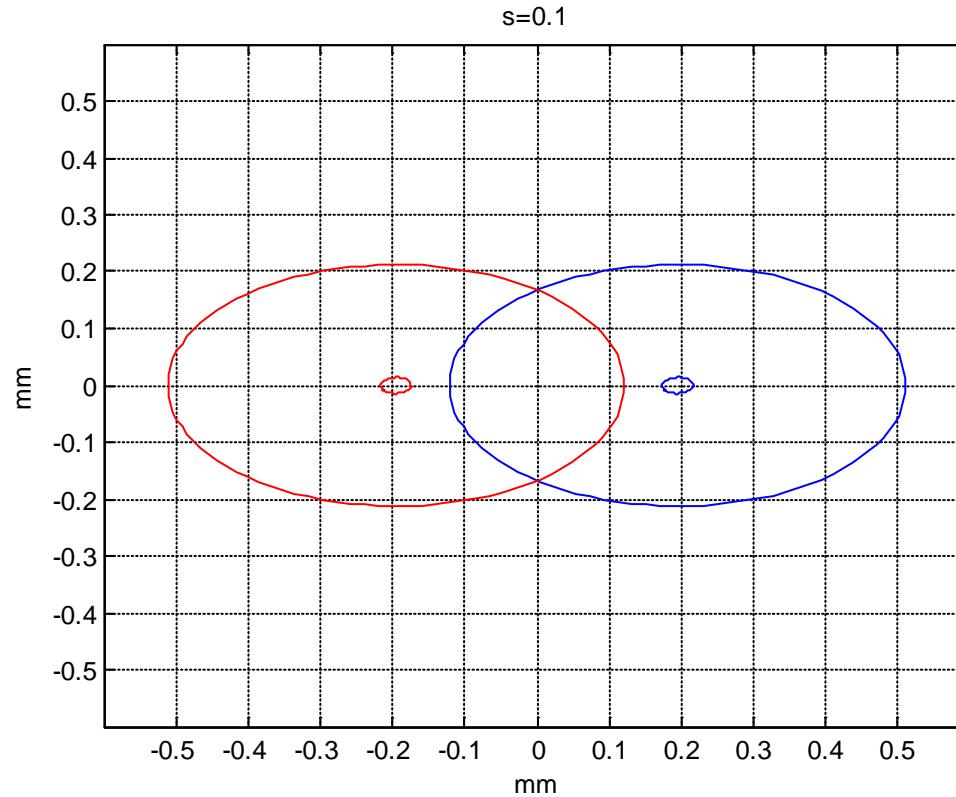
# A new IR for LHC



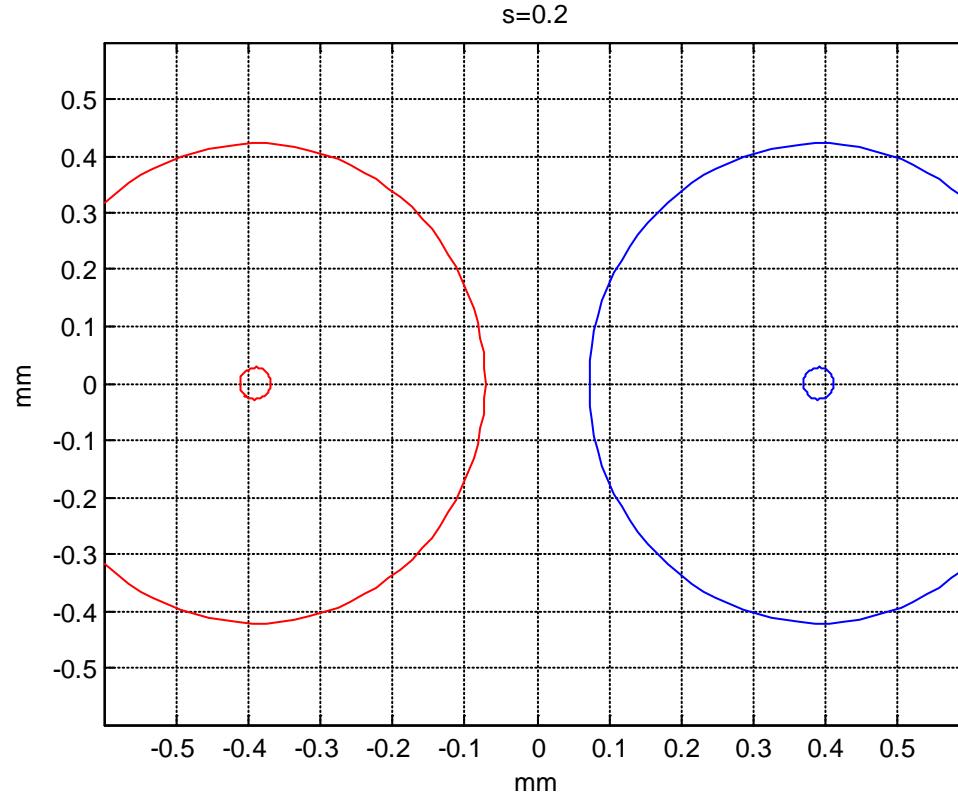
# A new IR for LHC



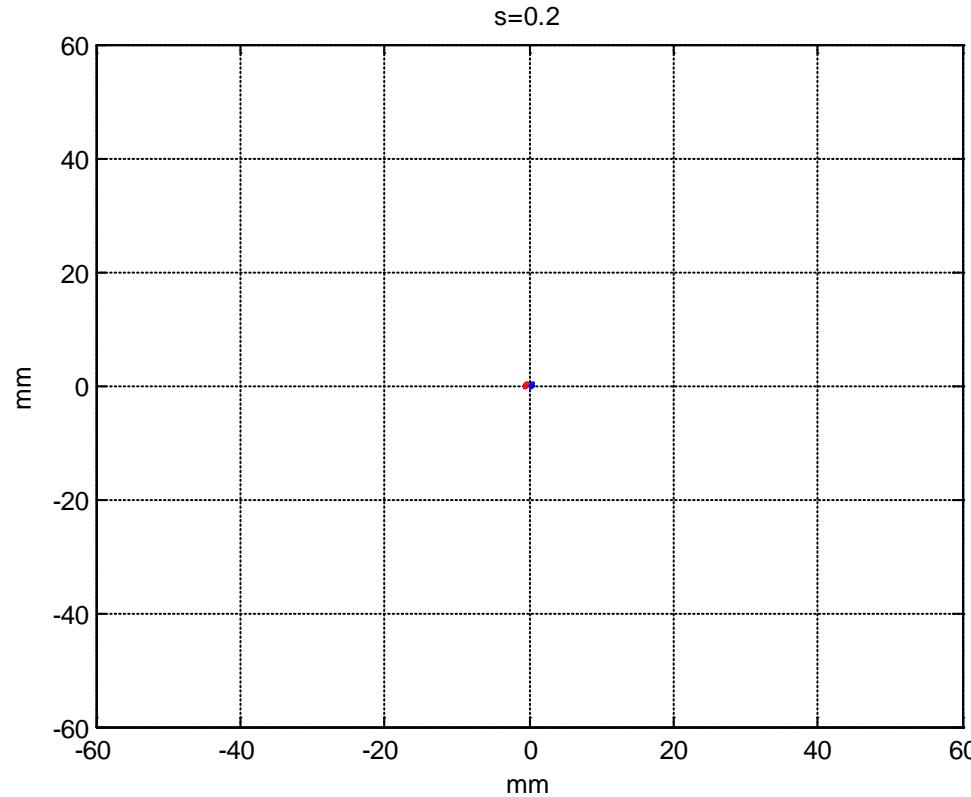
# A new IR for LHC



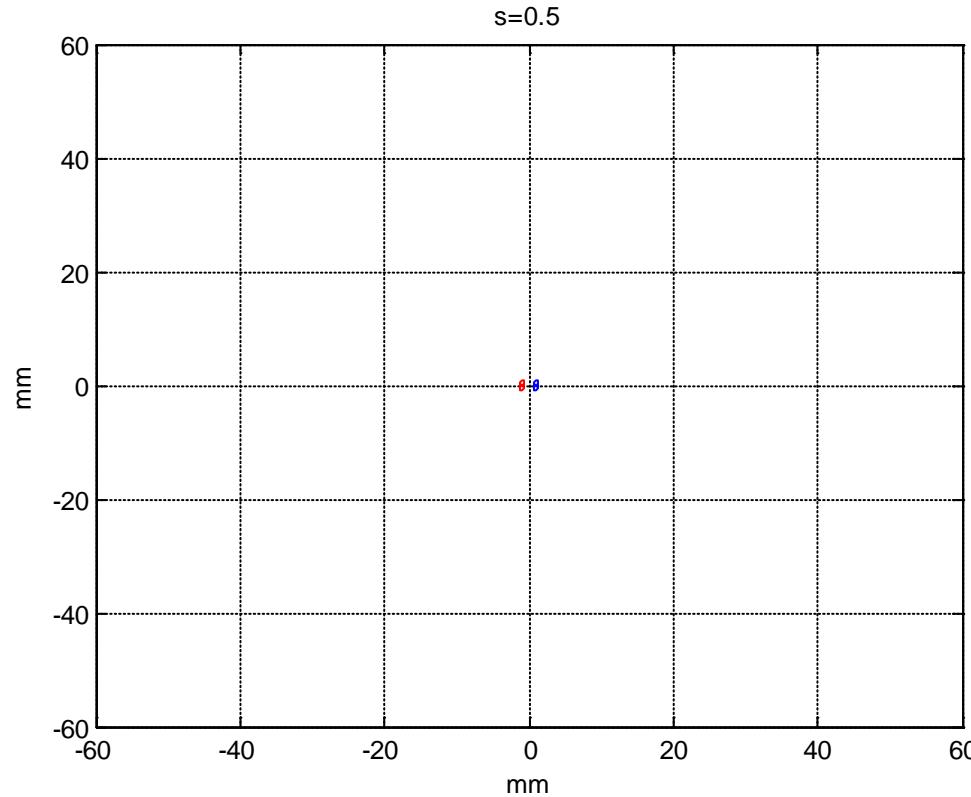
# A new IR for LHC



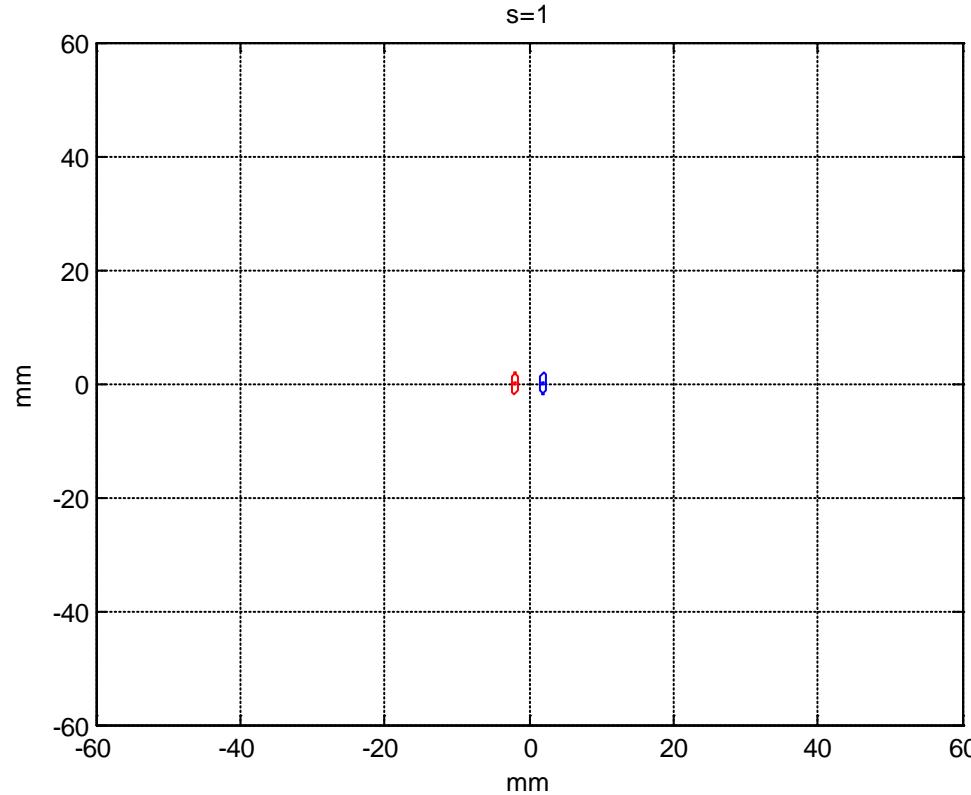
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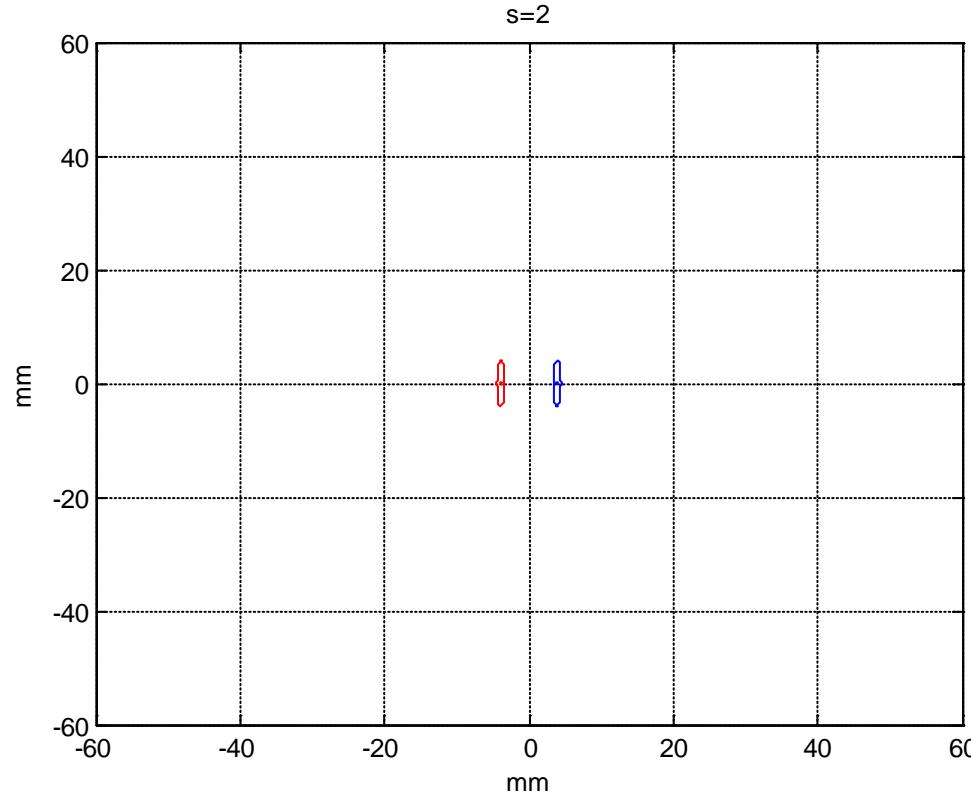
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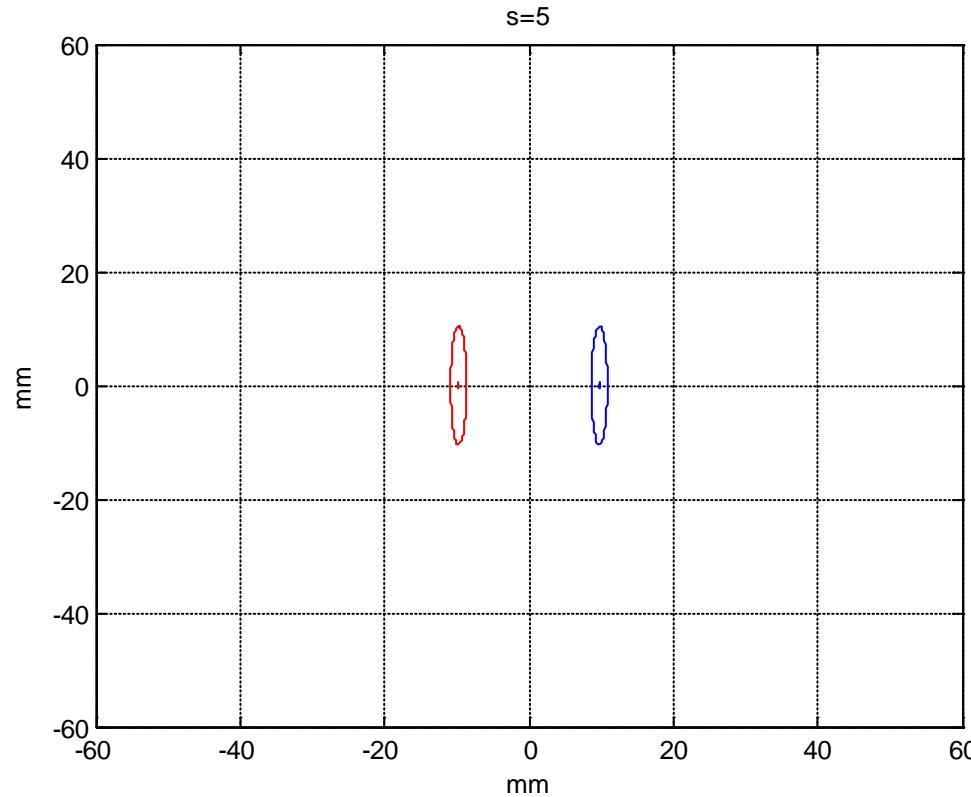
# A new IR for LHC



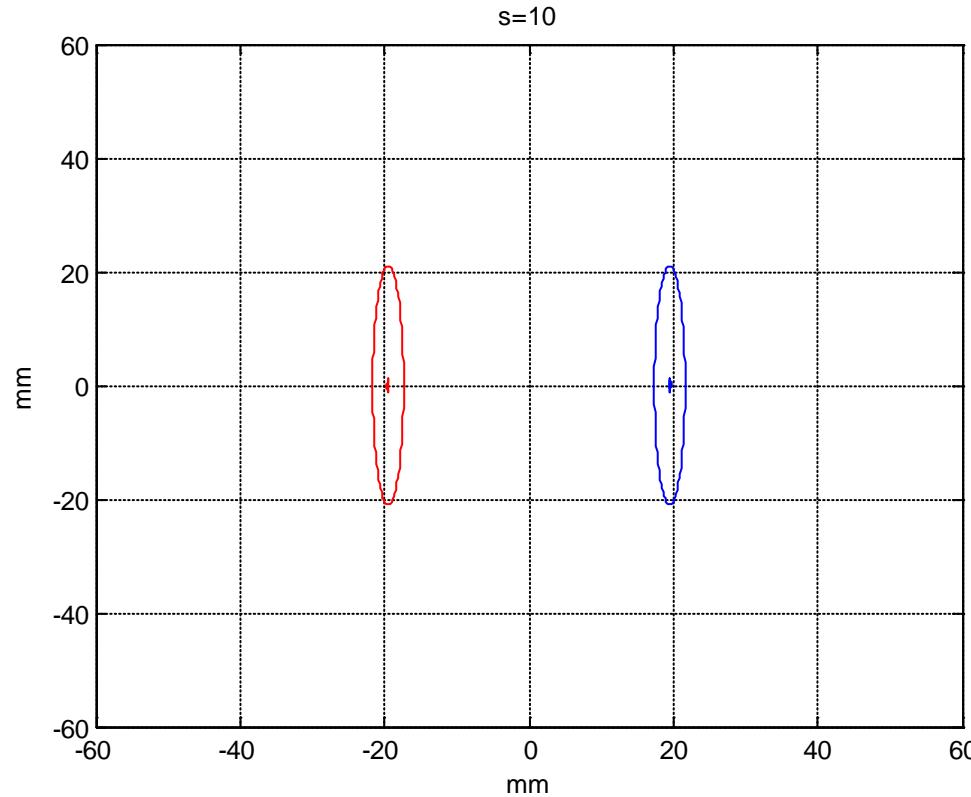
# A new IR for LHC



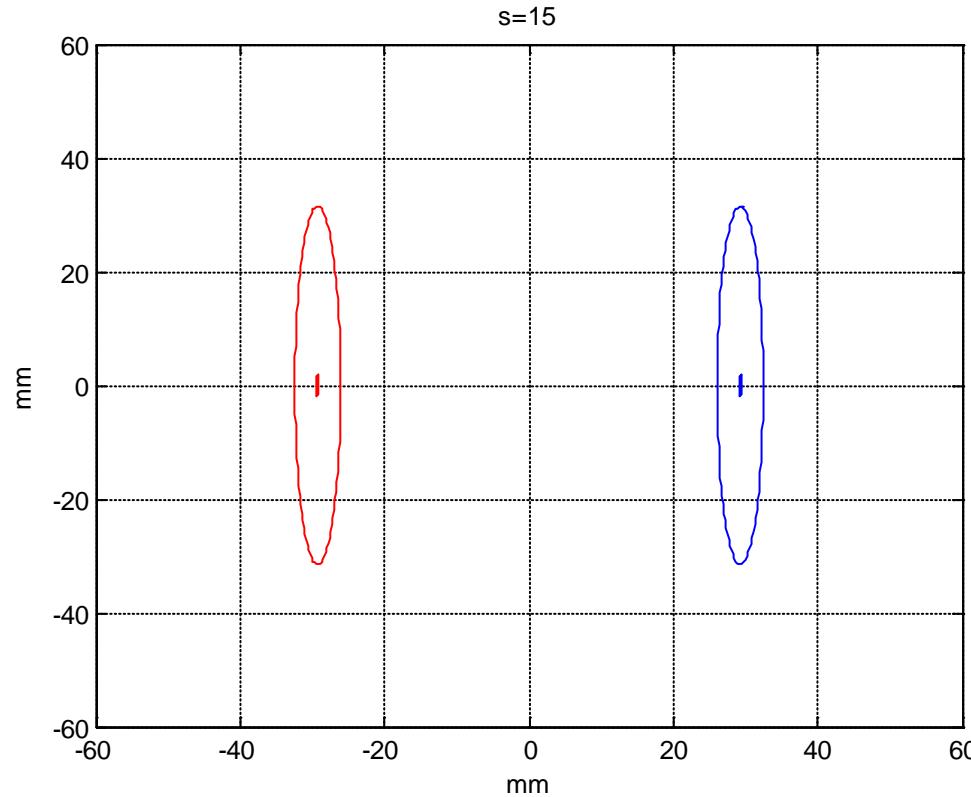
# A new IR for LHC



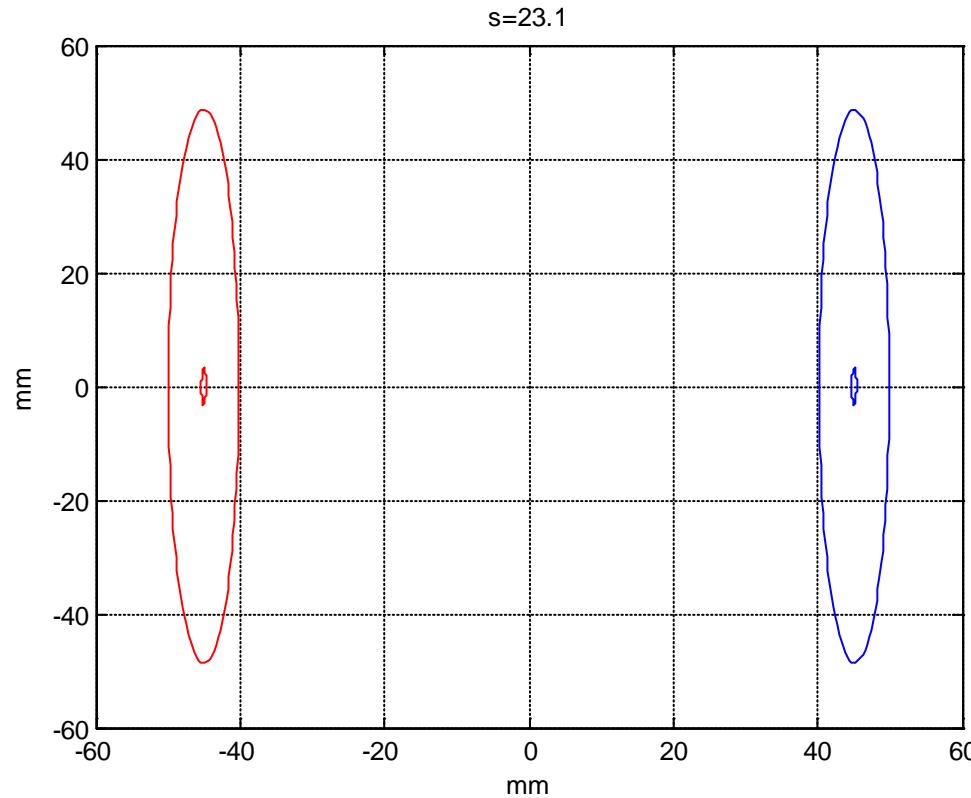
# A new IR for LHC



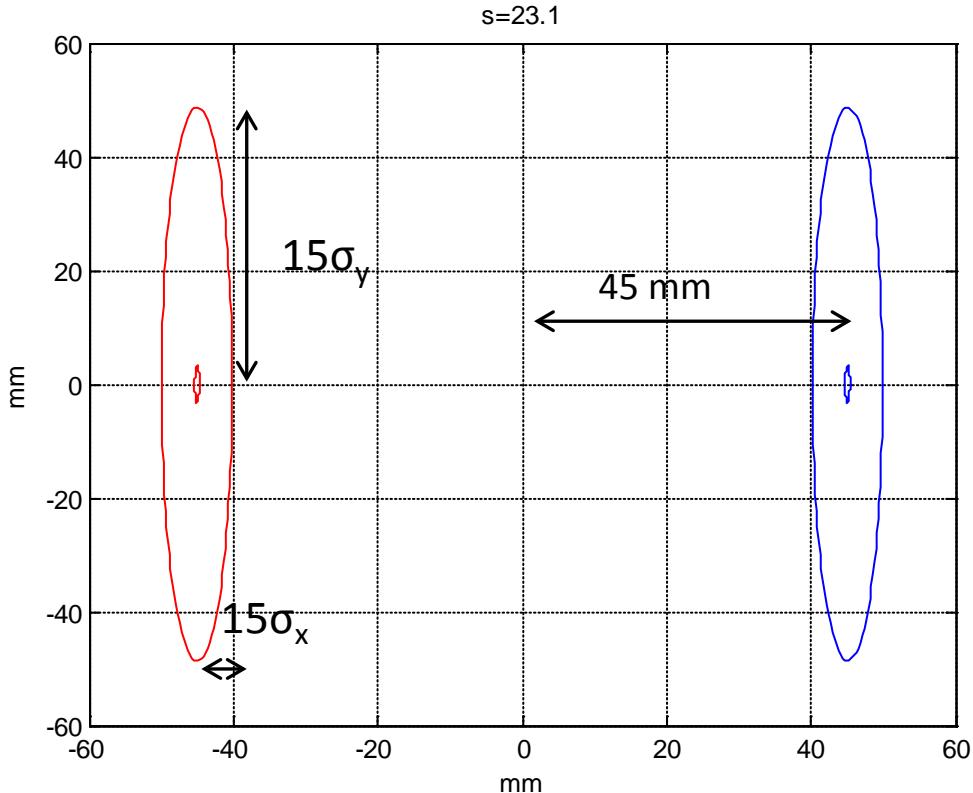
# A new IR for LHC



# A new IR for LHC

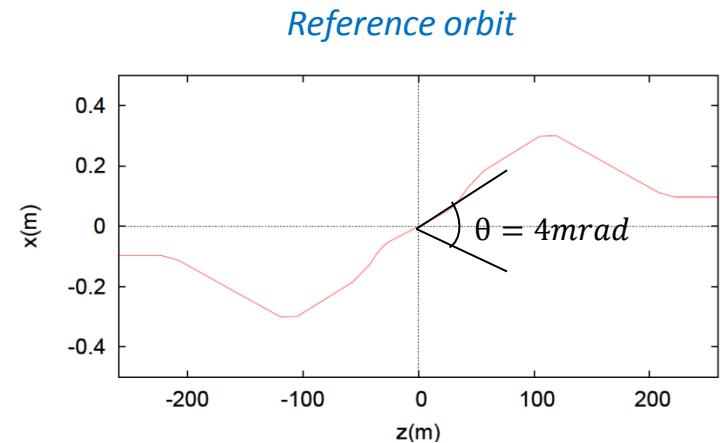


# A new IR for LHC



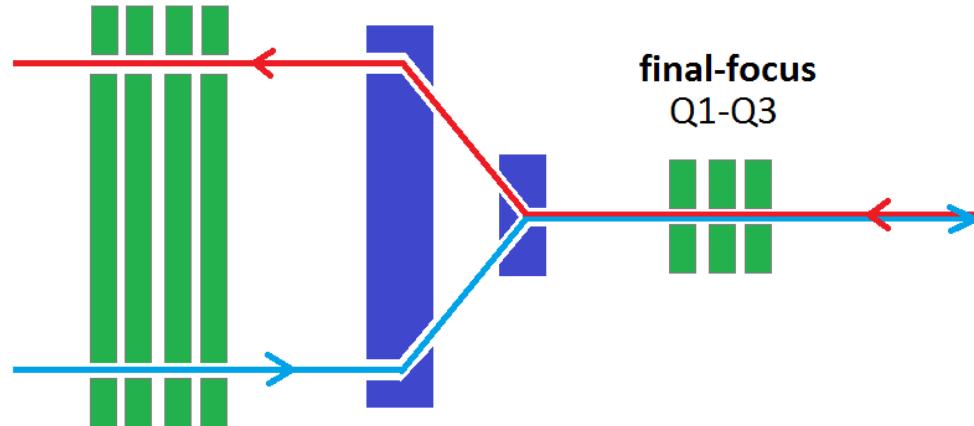
$$\sigma^*_x / \sigma^*_y = 10$$

Minimum required according to  
beam-beam simulations.

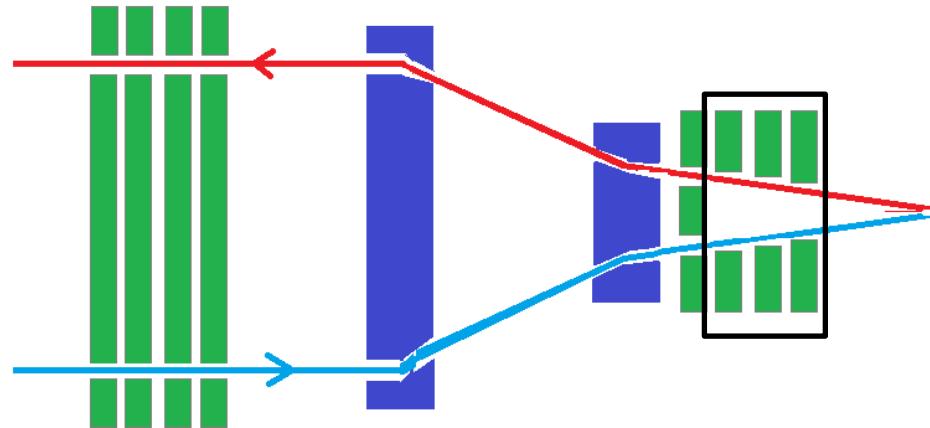


# A new IR for LHC

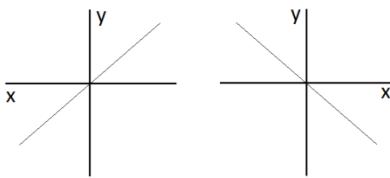
Present IR LHC



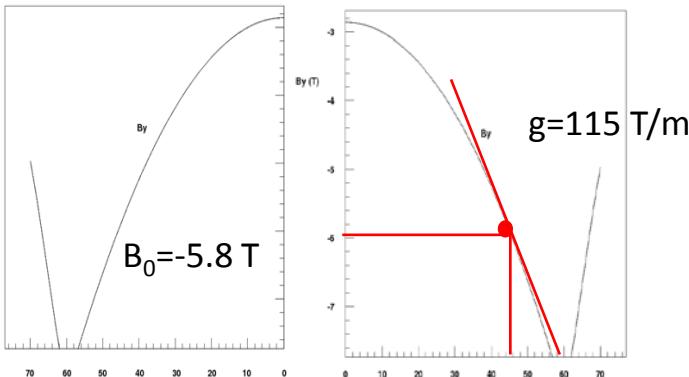
Proposed IR



# Last quadrupole

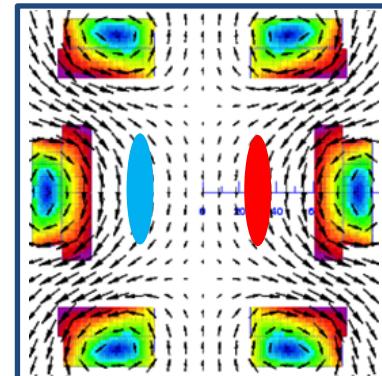


$B_y(x)$

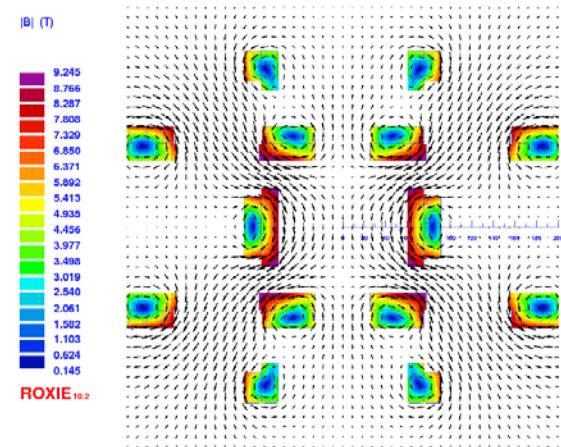


Dipolar component and sextupolar component

*Double half quadrupole*



solution to have diff quadrupole sign for the 2 beams in the same aperture

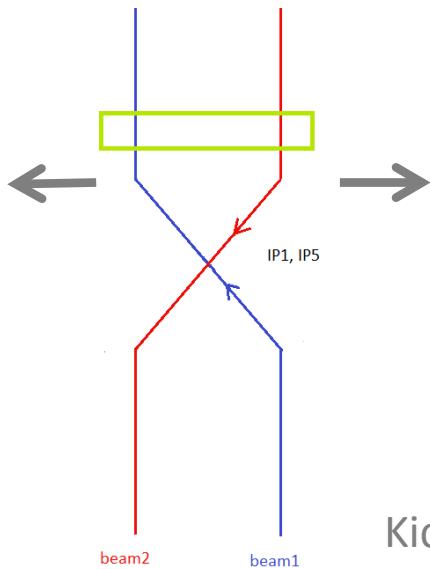
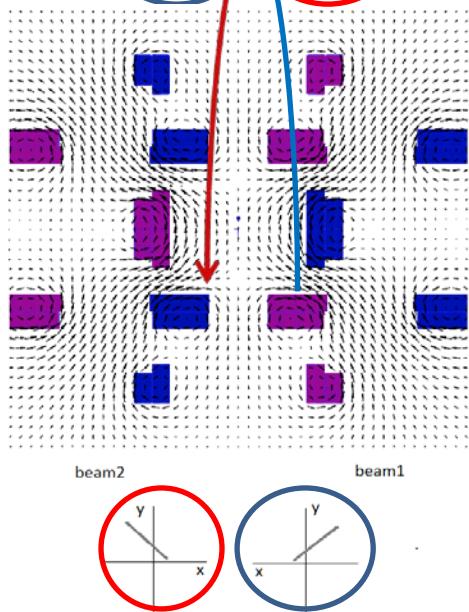
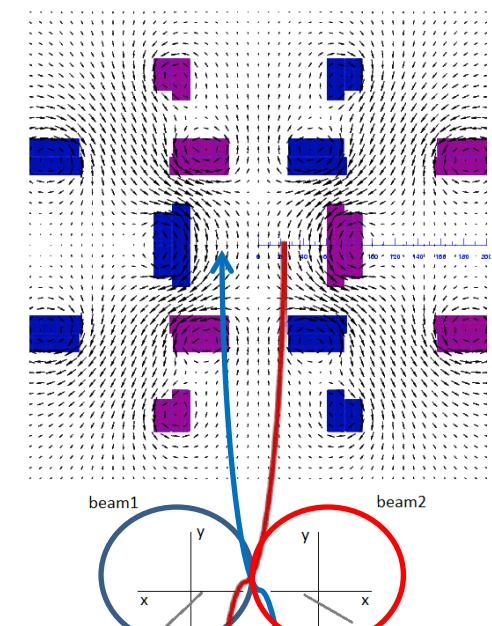


JAI

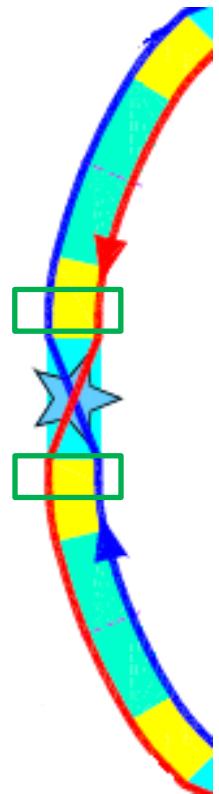
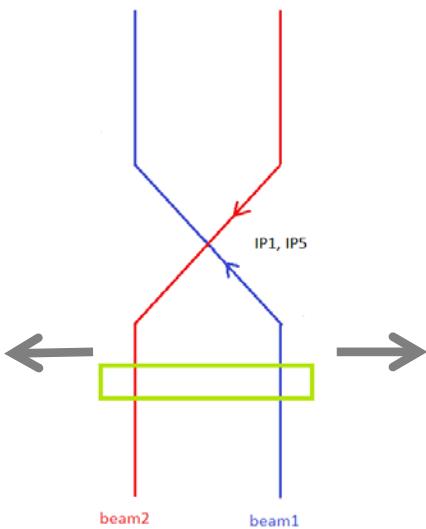
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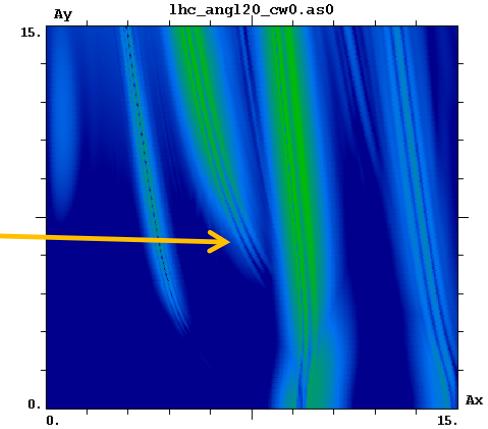
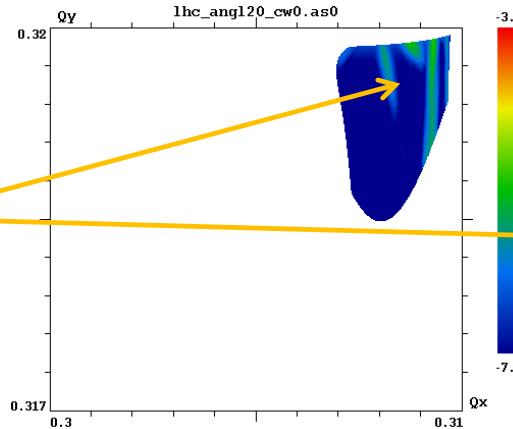
Kick due to the dipolar term



# Crab-waist simulations

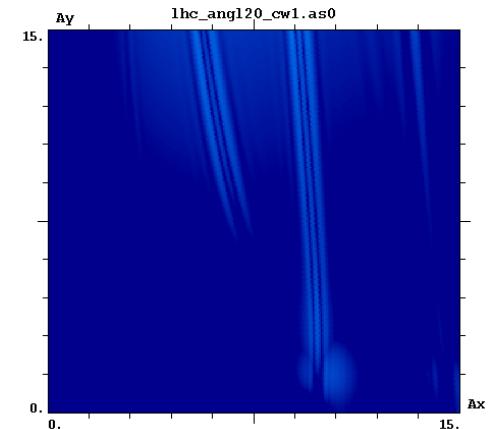
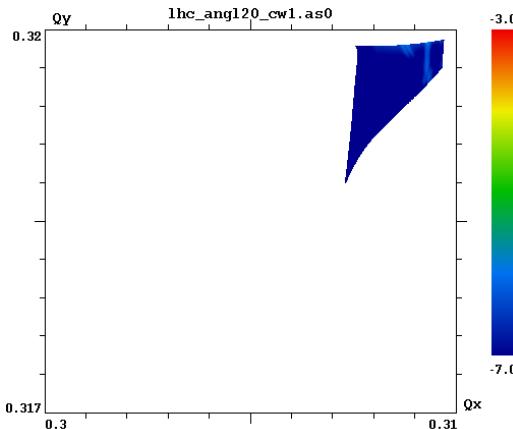
**CW = 0**

Resonances



**CW = 0.5**

Resonances suppressed



Frequency Map Analysis (FMA)

Effective for the beam-beam resonance suppression.

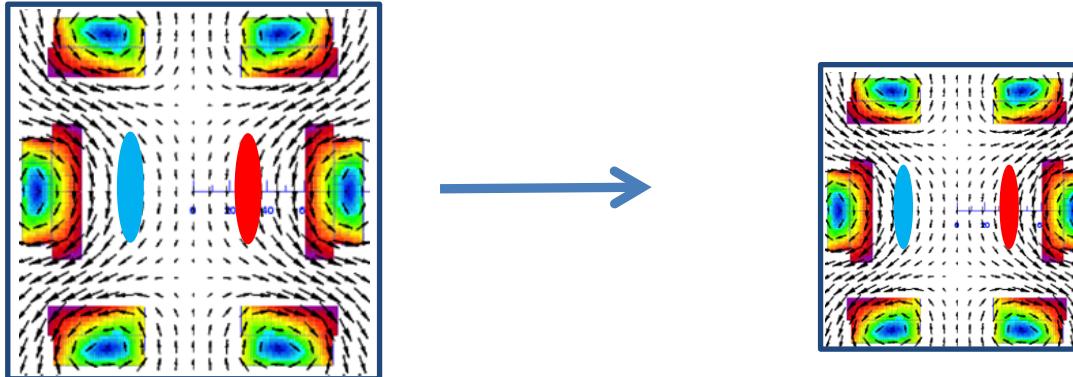
Plot shown for  $\theta_c = 1.5$  mrad

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Mikhail Zobov

José L. Abelleira

# Work on progress

- Chromatic correction and sextupole compensation
- Plan B



$$\beta_x^* = 1.5 \text{ m}$$

$$\beta_y^* = 1.5 \text{ cm}$$

$$\theta = 4 \text{ mrad}$$

$$\beta_x^* = 3.5 \text{ m}$$

$$\beta_y^* = 3.5 \text{ cm}$$

$$\theta = 2.6 \text{ mrad}$$

# Conclusions

- An extremely-flat beam optics ( $\beta_y^*/\beta_{y'}^*=100$ ) is conceptual possible for LHC and HELHC
  - Large Piwinski angle, to reduce the collision area and allow for a lower  $\beta_y^*$
  - Local chromatic correction
  - Possibility to have crab waist collisions that can increase luminosity and suppress resonances
  - Can accept higher brightness.

# Bibliography



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- P. Raimondi<sup>1</sup>, D. Shatilov, M. Zobov, *Beam-beam issues for colliding schemes with large Piwinski angle and crabbed waist* .
- J.L. Abelleira, *et. al.* "Local Chromatic Correction Scheme and Crab-Waist Collisions for an Ultra-low beta\* at the LHC", *Proc. of the 2012 International Particle Accelerator Conference, New Orleans, USA*, p. 118 (2012).
- J.L. Abelleira,"Flat beam IR optics", *Joint Snowmass-EUCARD/AccNet-HiLumi LHC meeting Frontier capabilities for Hadron colliders. February 22-23; 2013, CERN, Switzerland*
- J.L. Abelleira, "Towards an extremely-flat beam optics with large crossing angle for the LHC", *EUCARD Annual Meeting, April 25-27, 2012, Warsaw, Poland*.

Thank you...

*...For your attention*