Stretching and Breaking of Ultrathin MoS$_2$

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Two-dimensional crystals, consisting of single or few atomic layers extracted from layered materials such as graphite or MoS$_2$,¹⁻³ are attracting a great deal of interest due to their promising potential for applications in nanotechnology. Graphene is the best known 2D material because of its high mobility, presence of massless Dirac fermions,⁴,⁵ and a wealth of interesting physical phenomena such as the fractional quantum Hall effect.⁶ Other 2D materials such as transition metal dichalcogenides or BN could have practical applications and fundamental properties complementary to those of graphene, although they are at this point much less explored.

Single-layer MoS$_2$ is a typical two-dimensional semiconductor from the class of layered transition metal dichalcogenides (TMD). Individual layers, 6.5 Å thick, can be extracted from bulk crystals using the micromechanical cleavage technique commonly associated with the production of graphene,²,³ lithium-based intercalation,⁷,⁸ or liquid phase exfoliation⁹ and used as ready-made blocks for electronic device fabrication.¹⁰ Bulk MoS$_2$ is an indirect gap semiconductor with a band gap of 1.2 eV (ref 11). Reducing the number of layers modifies the band structure and, as a consequence, monolayer MoS$_2$ becomes a direct gap semiconductor¹²⁻¹⁵ with a band gap of 1.8 eV (ref 14) due to quantum confinement.¹⁵ The presence of a band gap in monolayer MoS$_2$ makes it interesting for applications in nanoelectronics where it allows the fabrication of transistors with low power dissipation and current on/off ratios exceeding $10^8$ at room temperature. Together with the possibility of large-scale liquid-based processing of MoS$_2$ and related 2D materials,⁵ MoS$_2$ could also be very interesting for applications in flexible electronics where it would combine high performance with low cost. It is however not clear at this point if monolayer MoS$_2$ would be characterized by mechanical properties necessary for integration with stretchable polymer substrates in order to produce high-end bendable electronics.

Previous measurements on MoS$_2$ and WS$_2$ nanotubes,¹⁶,¹⁷ which can be thought of as monolayers of MoS$_2$ and WS$_2$ wrapped up in the form of a cylinder, show superior mechanical properties with Young's modulus reaching 255 GPa and strength reaching 11% of its Young's modulus.¹⁸,¹⁹ Subnanometer MoS$_2$ nanowires on the other hand have lower Young's modulus, 120 GPa.²⁰ Here, we report on the measurement of the in-plane elastic modulus and breaking strength of single and bilayer MoS$_2$. MoS$_2$ consists of a stack of covalently bonded S–Mo–S layers weakly interacting with each other via van der Waals forces. The in-plane elastic modulus is 180 (60 Nm$^{-1}$, corresponding to an effective Young's modulus of 270 (100 GPa, which is comparable to that of steel. Breaking occurs at an effective strain between 6 and 11% with the average breaking strength of 15 (3 Nm$^{-1}$ (23 GPa). The strength of strongest monolayer membranes is 11% of its Young's modulus, corresponding to the upper theoretical limit which indicates that the material can be highly crystalline and almost defect-free. Our results show that monolayer MoS$_2$ could be suitable for a variety of applications such as reinforcing elements in composites and for fabrication of flexible electronic devices.

**KEYWORDS:** two-dimensional materials · dichalcogenides · MoS$_2$ · AFM · mechanical properties

We report on measurements of the stiffness and breaking strength of monolayer MoS$_2$, a new semiconducting analogue of graphene. Single and bilayer MoS$_2$ is exfoliated from bulk and transferred to a substrate containing an array of microfabricated circular holes. The resulting suspended, free-standing membranes are deformed and eventually broken using an atomic force microscope. We find that the in-plane stiffness of monolayer MoS$_2$ is 180 ± 60 Nm$^{-1}$, corresponding to an effective Young's modulus of 270 ± 100 GPa, which is comparable to that of steel. Breaking occurs at an effective strain between 6 and 11% with the average breaking strength of 15 ± 3 Nm$^{-1}$ (23 GPa). The strength of strongest monolayer membranes is 11% of its Young's modulus, corresponding to the upper theoretical limit which indicates that the material can be highly crystalline and almost defect-free. Our results show that monolayer MoS$_2$ could be suitable for a variety of applications such as reinforcing elements in composites and for fabrication of flexible electronic devices.
crystal structure is determined by polar covalent bonds resulting from the overlap between the 4d and 3p electron orbitals of molybdenum and sulfur. The in-plane stiffness ($E^{2D}$) of an ideal defect-free single-layer MoS$_2$ is related to the effective spring constant of these molecular bonds. A defect-free material would have the upper theoretical limit of the breaking strength ($\sigma_{\text{max}}^{2D} \approx 10\%$ of the Young’s modulus). We use nanoindentation in an atomic force microscope in order to perform nanomechanical measurements on ultrathin MoS$_2$ suspended over circular holes in patterned substrates, using a technique previously used for measurements on multilayer and single-layer graphene. Mechanical properties of graphene have also been probed by performing uniaxial measurements.

**RESULTS AND DISCUSSION**

Single- and few-layer MoS$_2$ was extracted from bulk crystals of naturally occurring MoS$_2$ using the micromechanical cleavage technique commonly employed for the production of graphene. We found that direct exfoliation on patterned substrates yielded a relatively small number of samples, presumably because of reduced adhesion between the substrate and MoS$_2$. We therefore employed a transfer technique to first exfoliate MoS$_2$ on polymer films and then transfer the resulting material onto prepatterned surfaces. MoS$_2$ is first deposited on Si substrates covered with 270 nm SiO$_2$ on top of which polyvinyl alcohol (PVA) and polymethyl methacrylate (PMMA) films have previously been spin-coated. We have reported elsewhere that this SiO$_2$ thickness results in optimal visibility of monolayer MoS$_2$. Once an interesting flake with an optical contrast corresponding to a monolayer is located using an optical microscope, AFM is used to verify the thickness. The sample is then immersed in water to dissolve the PVA film and release the PMMA layer which ends up floating on the water surface. The film is moved onto a pierced glass slide and aligned to the new substrate with the help of a micromanipulator. The new substrate consisted of a 270 nm thick SiO$_2$ (ref 28) patterned with 550 nm diameter holes defined by e-beam lithography followed by dry etching. Finally, the sample is kept in vacuum at 400 °C for 4 h in order to release the polymer film without the use of solvents that could break MoS$_2$ during drying. In this way, we obtain a relatively high yield of intact MoS$_2$ membranes suspended over circular holes. Figure 1a shows a monolayer flake after the transfer on the new substrate, while Figure 1b shows a corresponding AFM image of the sample topography. Resulting suspended ultrathin layers of MoS$_2$ are tightly clamped to the edges of the holes, without visible wrinkles or discontinuities.

Mechanical properties of the membranes were probed with indentation experiments using an AFM (Asylum Research Cypher) with a standard silicon cantilever (Olympus AC240). Figure 1c shows the schematic depiction of the experiment. For each hole, an AFM topographical image of the suspended membrane was acquired in amplitude modulation mode and used to position the tip in the middle of the membrane; see Figure 2a. Cantilever deflection is measured while the probe is moved in the vertical direction with a speed of 2nm s$^{-1}$, resulting in controlled loading and unloading of the suspended MoS$_2$ membrane. Typical force versus piezo extension curves are shown on Figure 2d. Mechanical drift is minimized by means of a temperature controller integrated with the AFM system. Multiple curves with increasing indentation depths were acquired for each hole until mechanical failure was observed, as illustrated in Figure 2b. Mechanical failure typically occurs for vertical deflections <50 nm, well below the hole depth. No evidence of MoS$_2$ sheets sliding over the substrate was observed. The height profile in Figure 2c shows that the membrane adheres to the sidewalls of the hole over a distance on the order of 5 nm. This adhesion is due to van der Waals interaction and is presumably at the origin of the membrane pretensioning. Similar sidewall adhesion and pretension was reported in suspended graphene membranes. SEM imaging was used to check tip quality, confirming that no damage occurred to the Si AFM tips during measurements. This observation is also supported by the fact that AFM image quality and measured results did not show any observable change during the experiment.
We performed experiments on a total of 9 mono-layer (1 L) and 6 double-layer (2 L) MoS₂ membranes. A representative force $F$ versus $z$-piezo extension ($\Delta Z_{\text{ext}}$) curve for a monolayer membrane and the substrate is shown on Figure 2d. Loading and unloading curves in general overlap, indicating that no plastic deformation or membrane detachment occurs during the measurements and that the material can be considered as elastic.

The schematic diagram of the measurement geometry is given in Figure 3a. Because the measurement geometry (both tip and the sample) has circular symmetry and MoS₂ has six equivalent crystalline directions in terms of the stress-strain response, we model MoS₂ as an isotropic film characterized by Young's modulus $E_Y$, Poisson ratio $\nu$, and thickness $h$. Simulations on MoS₂ and measurements on WS₂ nanotubes¹⁸,¹⁹ show that these materials related to monolayer MoS₂ are brittle and deform as materials with linear stress/strain relationship up to their failure.

This is in stark contrast to carbon nanotubes or graphene where carbon atom chain formation and Stone-Wales transformations can lead to ductile behavior.²¹ Such mechanisms are absent in MoS₂.¹⁹ Because MoS₂ monolayers and nanotubes share the same type of chemical bonds, we also model MoS₂ as a linear elastic material.

The membrane is suspended over a circular hole with diameter $a = 2r = 550 \pm 10$ nm and deformed in the middle by an AFM tip with a radius $r_{\text{tip}} = 12 \pm 2$ nm. We suppose that the film is prestretched due to van der Waals adhesion between the film and the substrate leading to internal strain $\varepsilon_0$. Mechanical response of such free-standing films can then fall into three distinct regimes, depending on the geometric factor $h/a$, applied load, and internal prestrain $\varepsilon_0$.²² Linear plate bending and prestrained membrane deflection are characterized by linear force versus deflection behavior and are valid for small loads. Which one of these two governs the mechanical behavior depends on whether stiffness generated by prestrain is greater than the bending stiffness. The nonlinear membrane behavior...
characterized by a cubic $F \sim \delta^3$ relationship dominates at large loads. In order to elucidate between these different deformation regimes, we plot a typical force–deflection curve in a logarithmic scale on Figure 3b. We can see that for small deflection and loading forces, limited by the resolution of our setup to $\sim 1$ nN, the curve follows a linear behavior (dashed line). For forces $> 10$ nN, the curve starts to follow cubic behavior, typical of deformed membranes. We therefore fit the force–deflection data using a formula that captures both the linear behavior for small deformations and the cubic term for larger deformations:\[^{32}\]

$$F = \sigma_0^{2D} \pi \delta + E^{2D} \frac{q \delta^3}{r^2}$$  \hspace{1cm} (1)

where the cubic term containing the elastic modulus $E^{2D}$ represents the modified form of the classical Schwerin solution for point loading of a circular membrane\[^{33}\] valid for all values of the Poisson’s ratio.\[^{32}\] The term linear with deformation $\delta$, where $\sigma_0^{2D}$ is the pretension in the membrane, corresponds to the linear, prestretched membrane regime with an internal strain of $\varepsilon_0$.

Finite element simulations by Lee et al.\[^{24}\] showed that this model can be applied to small and finite sized indenters as long as $r_{tip} \ll r$. We extract the tip radius $r_{tip}$ as $12$ nm from SEM images, resulting in $r_{tip}/r = 0.05$ in our case. The dimensionless constant $q$ is related to the Poisson ratio $\nu$ as $q = 1/(1.05 - 0.15\nu - 0.16\nu^2) = 0.95$, where $\nu = 0.27$ is the Poisson ratio of bulk MoS$_2$.\[^{34}\] The map of possible regimes of film response according to Komaragiri et al.\[^{32}\] is presented on Figure 3c, together with the range of range of tests covered in this paper, confirming that most of the mechanical response that we record is expected to be in the region described by the cubic $F \sim \delta^3$ behavior.

Figure 4 shows representative experimental force–deflection curves acquired for mono- and bilayer MoS$_2$. From a least-squares fit of the experimental curves with the eq 1, we can extract the pretension $\sigma_0^{2D}$ and the membrane elastic modulus $E^{2D}$. The fit agrees well with experimental data, validating our assumptions that led to the choice of eq 1 as the model. For a total of 9 monolayers (1 L), we obtain the average value for the elastic modulus $E^{2D}$ of $180 \pm 60$ N m$^{-1}$ (Figure 5, left) and prestress $\sigma_0^{2D}$ in the $0.02$ to $0.1$ N m$^{-1}$ range. Throughout the paper, the experimental uncertainty for the measured values of the elastic modulus and the breaking strength corresponds to the standard deviation of experimental values. Assuming an effective monolayer thickness of $0.65$ nm, we obtain for the Young’s modulus $E_{\text{Young}} = 270 \pm 100$ GPa, close to the Young’s modulus of MoS$_2$ nanotubes (230 GPa, ref 18), bulk MoS$_2$ (238 GPa, ref 34), or steel (210 GPa, ref 35). The elastic modulus of bilayer MoS$_2$ is $260 \pm 70$ N m$^{-1}$, which corresponds to a lower Young’s modulus of $200 \pm 60$ GPa, possibly due to defects or interlayer sliding.

During nanomechanical measurements, suspended membranes are deformed up to their mechanical failure, denoted by the symbol $\times$ in Figure 4, typically occurring for fracture forces of $F_{\text{max}} \approx 200$ nN and
Weak deflections $\approx 50$ nm. For such extreme deformation, in addition to large-scale deformation, the membrane is locally indented within a typical area extending $\sim 2r_{tip}$ distance from the center.\textsuperscript{33} Here, the local curvature of the membrane is constrained by the tip diameter of the AFM probe, as long as the membrane is allowed to deform smoothly onto the indenter. Our experiment falls in the limit of small indenters characterized by $r_{tip}/r < 1$ ($r_{tip}/r = 0.05$ in our case) and large loads with respect to pretension, characterized by a factor $\kappa < 1$ defined as\textsuperscript{36}

$$\kappa = \left( \frac{\varepsilon_0}{r_{tip}} \right)^{1/3} \left( \frac{2r_{tip}}{r} \right)^{2/3}$$ \tag{2}

In our case, $\kappa < 0.02$. Here, we can extract the maximum stress at the central, protruding part of the film $\sigma_{max}^{2D}$ using the expression for the indentation of a linearly elastic membrane by a spherical indenter in the limit of large load:\textsuperscript{36}

$$\sigma_{max}^{2D} = \sqrt{\frac{F_{max}E^{2D}}{4\pi r_{tip}}}$$ \tag{3}

The averages of maximum stress values for 1 L and 2 L-MoS$_2$ membranes are 15 ± 3 and 28 ± 8 N m$^{-1}$, respectively (corresponding to 22 ± 4 GPa for a monolayer and 21 ± 6 GPa for a bilayer), as reported in Figure 4. On the average, these correspond to 8 and 10% of the Young’s modulus for monolayer and bilayer MoS$_2$. The strength of individual MoS$_2$ monolayers is between 6 and 11% of their Young’s modulus. These values are at the theoretical upper limit of a material’s breaking strength and thus represent the intrinsic strength of interatomic bonds in MoS$_2$. This exceptionally high strength indicates that MoS$_2$ membranes are mostly defect-free. To put these high values of breaking strength and Young’s modulus in perspective, we can compare them to several common engineering materials in Table 1. The strength of monolayer MoS$_2$ is exceeded only by carbon nanotubes and graphene. Even though MoS$_2$ has a smaller Young’s modulus and strength than graphene, the absolute 2D elastic modulus $E^{2D}$ and strength $\sigma_{max}^{2D}$ of monolayer MoS$_2$ are smaller than those of graphene only by a factor of $\sim 2$.

In order to investigate if MoS$_2$ could be suitable for integration with flexible materials, for example, in flexible electronic circuits, it is necessary to quantify the membrane strain at the breaking point, $\varepsilon_{int}$, and compare it to the breaking strain of standard flexible substrates. Assuming a linear relationship between stress and strain $\sigma = E\varepsilon$ leads to an internal stress at failure $\varepsilon_{int} \sim 0.06–0.11$.

In comparison, thin polymer films such as polyimide (PI) or polydimethylsiloxane (PDMS), commonly used as substrates for flexible electronics, break at a strain of $\sim 7\%$ (ref 37), which is smaller than the aforementioned value extracted for single-layer MoS$_2$. This suggests that 2D MoS$_2$ can be readily integrated with PI or PDMS substrates for use in flexible electronics.

**CONCLUSIONS**

Our results show that monolayer MoS$_2$ is a flexible and strong material with a high Young’s modulus, comparable to stainless steel. The measured strength of monolayer MoS$_2$ is close to the theoretical intrinsic strength of the Mo–S chemical bond, indicating that the monolayer is mostly free of defects and dislocations capable of reducing mechanical strength. As MoS$_2$ can be readily dispersed in a wide variety of solvents,\textsuperscript{9} our finding indicates that MoS$_2$ could be interesting as a reinforcing element in composites. The presence of sulfur in MoS$_2$ could furthermore allow easy functionalization and efficient load transfer between MoS$_2$ and the composite matrix.

We also find that the exceptional mechanical properties of monolayer MoS$_2$ make it suitable for incorporation into flexible electronic devices where commonly used substrates such as PI would undergo mechanical failure at a smaller deformation than MoS$_2$.

**MATERIALS AND METHODS**

Single layers of MoS$_2$ are exfoliated from commercially available crystals of molybdenite (SPI Supplies Brand Moly Disulfide) using the scotch-tape micromechanical cleavage technique pioneered for the production of graphene.\textsuperscript{1} Monolayer and few-layer MoS$_2$ was first deposited on a silicon substrate with 270 nm thick SiO$_2$ that has previously been coated with polyvinyl alcohol (Sigma-Aldrich) and polymethyl methacrylate (PMMA, Microchem Corp). The PMMA film is released by dissolving PVA in water and transferred on top of a prepatterned SiO$_2$ substrate. After transfer, PMMA is removed by heating the
sample in a vacuum furnace at 400 °C for 4h. AFM imaging and indentation experiment was performed using the Asylum Research Cypher AFM equipped with the air temperature controller for minimizing drift and using Olympus AC240 silicon cantilevers. AFM probe spring constants were calibrated using the thermal method.  

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Supporting Information Available: SEM images of atomic force microscope probes. This material is available free of charge via the Internet at http://pubs.acs.org.

REFERENCES AND NOTES

42. Kevlar Technical Guide.