

## Measurement of Magnetic Excitations in the Two-Dimensional Antiferromagnetic $\text{Sr}_2\text{CuO}_2\text{Cl}_2$ Insulator Using Resonant X-Ray Scattering: Evidence for Extended Interactions

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We measured the momentum dependence of magnetic excitations in the model spin-1/2 2D antiferromagnetic insulator  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$  (SCOC). We identify a single-spin-wave feature and a multimagnon continuum, with different polarization dependences. The spin waves display a large (70 meV) dispersion between the zone-boundary points  $(\pi, 0)$  and  $(\pi/2, \pi/2)$ . Employing an extended  $t$ - $t'$ - $t''$ - $U$  one-band Hubbard model, we find significant electronic hopping beyond nearest-neighbor Cu ions, indicative of extended magnetic interactions. The spectral line shape at  $(\pi, 0)$  indicates sizable quantum effects in SCOC and probably more generally in the cuprates.

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Magnetism in low-dimensional cuprates remains of considerable interest, in relation both to the fundamental quest to understand strong electron correlation and quantum spin effects in Mott insulators, and to the search for the mechanism of high- $T_c$  superconductivity. To lowest order, the undoped cuprate superconductors can be described by the spin 1/2 two-dimensional (2D) square-lattice nearest-neighbor (NN) Heisenberg antiferromagnet, which is among the simplest and most studied models in magnetism [1]. The ground state displays classical order, reduced by quantum fluctuations at zero temperature and destroyed by thermal fluctuations at finite temperature. A possible crossover between renormalized classical [2] and quantum critical [3] scaling was tested experimentally in the undoped cuprates  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$  (SCOC) [4] and  $\text{La}_2\text{CuO}_4$  (LCO) [5], and in the organometallic salt  $\text{Cu}(\text{DCOO})_2 \cdot 4\text{D}_2\text{O}$  (CFTD) [6]. However, while the latter shows only nearest-neighbor coupling, high-energy inelastic neutron scattering (INS) data on LCO [7] suggest that further-neighbor magnetic interactions influence the scaling measurements. Frustrated further-neighbor interactions could also bring the undoped cuprates closer to the valence bond liquid proposed as mechanism for superconductivity [8].

It is therefore timely to investigate the excitation spectrum of SCOC, as an important model system. Inelastic neutron scattering (INS) measurements of SCOC have been limited to low energies and small momenta around the ordering wave vector [4]. In this Letter we report the full magnetic excitation spectrum measured by resonant inelastic x-ray scattering (RIXS). We discover a surprisingly large dispersion along the magnetic Brillouin zone boundary (ZB). An analysis of the data in terms of an extended Hubbard model yields a quantitative estimation

of sizable further-neighbor electronic hopping. The resulting series of longer-ranged magnetic interactions enhance quantum fluctuations, in agreement with the reduced ordered moment. The importance of quantum fluctuations is further revealed by differences in the spectral line shapes at the  $(-\pi, 0)$  and  $(-\pi/2, \pi/2)$  ZB points.

SCOC is an insulating single-layer parent compound of the high- $T_c$  superconducting (SC) materials. It is isostructural to the high-temperature tetragonal phase of LCO, with La replaced by Sr, and apical oxygens replaced by Cl. The distance between adjacent  $\text{CuO}_2$  planes is 18% larger than in LCO. Antiferromagnetic (AFM) order develops below  $T_N = 256$  K with reduced ( $0.34 \mu_B$ ) moments aligned along the (110) direction in the  $\text{CuO}_2$  plane. Both the in-plane ( $XY$ ) anisotropy and the interlayer coupling are very small, and SCOC is an almost ideal realization of an  $S = 1/2$  2D square-lattice Heisenberg AFM [5]. Magnetic excitations in SCOC have been identified by optical spectroscopies. A structure at 0.35 eV in absorption [9] is interpreted as a quasibound state of two magnons assisted by a phonon with momentum  $Q_{\text{ph}} \sim (\pi, 0)$  [10]. Two-magnon excitations at  $E_{2M} = 0.35$  eV in the Raman spectra suggest a superexchange energy  $J \sim 0.13$  eV [11,12]. Neither Raman nor optics are sensitive to single magnons, which are optically forbidden spin-flip ( $\Delta S = 1$ ) excitations.

RIXS in transition metal (TM) oxides probes excitations with mixed charge and spin character across or inside the Mott gap [13–15]. At the TM  $L_{2,3}$  ( $2p \rightarrow 3d$ ) edges the large  $2p$  spin-orbit interaction couples the angular momentum of the photon to the electron spin, and pure spin-flip excitations are possible [16,17]. Dispersive  $\Delta S = 0$  excitations have been observed in LCO both at the Cu  $K$  ( $1s$ ) [18] and  $L_3$  [19] edges, and in the ladder compound

$\text{Sr}_{14}\text{Cu}_{24}\text{O}_{41}$  [20]. More recent work has shown that  $L_{2,3}$  edge RIXS can be used to map the dispersion of single magnons in 2D cuprates [21]. Therefore RIXS is an interesting alternative to INS, requiring only sub-mm<sup>3</sup> samples.

Measurements were performed at the SAXES end station of the ADDRESS beam line of the Swiss Light Source (SLS) [22]. Single crystals ( $4 \times 4 \times 0.5$  mm<sup>3</sup>) grown from the flux with the  $c$  axis perpendicular to the large surface, and characterized by x-ray and neutron diffraction, were mounted on a flow cryostat, with the  $c$  axis and either the (100) or the (110) directions in the horizontal scattering plane. By adjusting the undulator, data were taken with incoming polarization either perpendicular ( $\sigma$ ) or within ( $\pi$ ) this plane. At the fixed scattering angle of  $130^\circ$  the transferred momentum was  $\|Q\| = 0.85 \text{ \AA}^{-1}$ . By a rotation around a vertical axis, the projection  $Q_{\parallel}$  of  $Q$  on the  $ab$  plane was varied in the range  $\pm 0.73 \text{ \AA}^{-1}$  ( $\pm 0.92\pi/a$ ). Positive (negative)  $Q$  values correspond to a grazing emission (incidence) geometry. The combined energy resolution was  $\Delta E = 130$  meV, and the accuracy on the energy zero was  $\pm 7$  meV, as determined from the elastic peak measured on a coplanar polycrystalline carbon sample. The momentum resolution, determined by the detector size, was better than  $\pm 2.5 \times 10^{-3}(\pi/a)$ . Postcleaving *in situ* or in air produced very similar results.

Figure 1(b) is an overview of the spectra for the (100) direction for  $\pi$  polarization. They were normalized to the same integrated intensity in the 1–2.5 eV energy range, to remove intensity variations due to the angular dependence of absorption, and any other angular or time dependence. The main feature at  $\sim 1.5$  eV is the manifold of

optically forbidden  $dd$  electron-hole excitations [15,23]. In the 0–1.5 eV energy range, where no electronic excitations are expected, the spectra exhibit a loss feature dispersing symmetrically from  $Q_{\parallel} = 0$  [Fig. 1(c)]. Near the zone boundary, spectral weight extends beyond 300 meV, well above the highest phonon mode (70 meV) in SCOC [24]. Its maximum follows the calculated spin-wave dispersion for  $J = 130$  meV (red line, see below), strongly suggesting a magnetic origin of this feature.

A model independent analysis was performed by fitting the main peak to a resolution-limited Gaussian line shape representing the single-magnon ( $M$ ) contribution [Fig. 2(a), top]. Subtracting this line shape from the raw spectrum yields asymmetric features (dashed line) on both sides of the magnon peak. The low-energy one at  $\sim 50$  meV, contains the elastic line, phonon losses and possibly a residue due to the approximate magnon line shape. The higher-energy feature reflects two-magnon ( $2M$ ) and higher-order excitations, which give rise to the continuum above the single-magnon dispersion curve in Fig. 1(c). The uncertainty on the magnon energy is  $\pm 10$  meV. For LCO, a similar approach yields a magnon dispersion in excellent agreement with INS [21].

An unexplored aspect of RIXS is the possibility to separate single- and multimagnon contributions by exploiting their different edge- and polarization-dependent cross sections, as illustrated in Fig. 2(a). The top panel shows spectra ( $Q_{\parallel} = 0.58 \text{ \AA}^{-1}$ ) for two polarizations, normalized in the  $2M$  region for ease of comparison. The single-magnon peak is reduced for  $\sigma$  polarization. The bottom panel compares Cu  $L_3$  and O  $K$  edge ( $1s$ , 530 eV;  $\Delta E = 60$  meV) data, for the same  $Q_{\parallel}$  ( $0.19 \text{ \AA}^{-1}$ ). Similar to the Cu  $K$ -edge case, the O  $K$

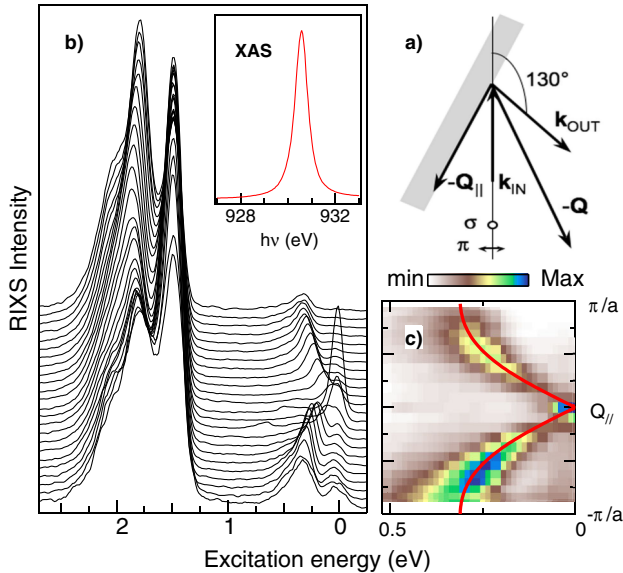


FIG. 1 (color online). (a) Schematics of the scattering geometry. (b) Cu  $L_3$  RIXS spectra ( $T = 15$  K) along the (100) direction. The incident energy is set at the maximum of the absorption (XAS) (inset). (c) Intensity map extracted from (b). The red line is the spin-wave dispersion for the NN Heisenberg model and  $J = 130$  meV.

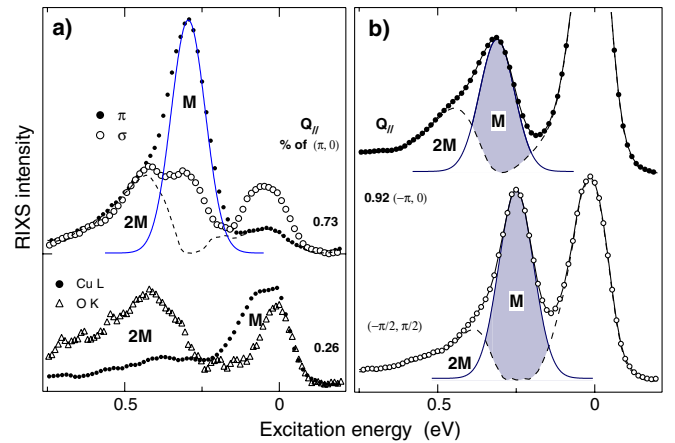


FIG. 2 (color online). (a) (top) RIXS spectra for  $\sigma$  and  $\pi$  polarization and  $Q_{\parallel} = 0.58 \text{ \AA}^{-1}$  along (100). The dashed line is the difference between the  $\pi$  spectrum and the Gaussian line shape ( $M$ , solid blue line) representing the single-magnon contribution. (bottom) Comparison of Cu  $L$ -edge and O  $K$ -edge RIXS for  $Q_{\parallel} = 0.19 \text{ \AA}^{-1}$ . (b) RIXS spectra at  $0.92(-\pi, 0)$  and  $(-\pi/2, \pi/2)$  measured with  $\sigma$  polarization. The two magnons ( $2M$ ) to single-magnon ( $M$ ) intensity ratio is 0.26 at  $(-\pi/2, \pi/2)$ , and increases to 0.49 at  $0.92(-\pi, 0)$ .

edge spectrum contains only the  $2M$  continuum, which was suggested by previous experiments [25,26], and is now clearly resolved around 0.4 eV for this  $Q_{\parallel}$ . By contrast, the  $L_3$  line shape exhibits a prominent single-magnon loss at  $\sim 0.1$  eV. Figure 2(b) illustrates the spectral line shapes near the ZB points  $(-\pi/2, \pi/2)$  and  $(-\pi, 0)$ . Near  $(-\pi, 0)$  the magnon peak is weaker, and spectral weight is transferred to the higher-energy continuum. The comparison strongly suggests that the quantum effect observed by neutrons in CFTD [27] is also present in SCOC, and most likely in the cuprates in general. This observation is important for theories arguing that superconductivity occurs from strong magnetic fluctuations [28,29].

The  $Q$  dependence of the magnon energy extracted from the data of Fig. 1, and from similar data for the (110) direction and two different samples, is summarized in Fig. 3. The RIXS data are consistent with the small- $Q$  results from INS, but cover for the first time the full dispersion up to the boundary of the ZB. They reveal a striking 70 meV difference between the magnon energies of 310 meV at  $(\pi, 0)$  and 240 meV at  $(\pi/2, \pi/2)$ . This can be compared with the smaller  $\sim 20$  meV dispersion in LCO [7]. Dispersion along the ZB in all cuprates is also predicted by recent theory, which, however, underestimates the  $(\pi, 0)$  energy in SCOC by almost 50 meV [30].

For the simple  $S = 1/2$  2D Heisenberg model with NN exchange, linear spin-wave theory predicts a constant magnon energy  $\hbar\omega = 2J$  along the ZB. First order quantum corrections uniformly renormalize the dispersion by a

factor  $Z_c = 1.18$ . Numerical results [31,32] and neutron data on CFTD [27,33] have established that the magnon energy for purely NN exchange is actually 6% larger at  $(\pi/2, \pi/2)$  than at  $(\pi, 0)$ . The dispersion in Fig. 3 and in LCO is in the opposite direction to this quantum effect. It could be reproduced by adding freely adjustable further-neighbor exchange interactions. However, the Heisenberg (spin-only) Hamiltonian is the low-energy projection of an electronic system at half filling, and a better approach is to systematically consider higher orders to this projection. Indeed the dispersion in LCO [7] was described by projecting the one-band Hubbard model with effective Coulomb repulsion  $U$  to 4th order in the NN hopping  $t$ , giving rise to further-neighbor exchange interactions  $J$ ,  $J' = J''$  and  $J_c$ . The same approach gives for SCOC an unphysically low value of  $U = 1.59 \pm 0.04$  eV and  $t = 0.261 \pm 0.004$  eV. A more plausible approach is to include further-neighbor hoppings  $t'$  and  $t''$  [34]. We therefore extended the analysis to 4th order in  $t$ ,  $t'$ , and  $t''$  and find that this approach gives a more reasonable range of  $U$ , is consistent with higher-energy RIXS and angle-resolved photoemission spectroscopy (ARPES), and provides better fits to the shape of the dispersion [Fig. 3(b)].

Magnetic excitations provide accurate information on the interactions, but do not directly probe  $U$ . A more direct probe of the effective  $U$  was found in the higher-energy part of the RIXS Cu- $K$  spectra from the sister compound  $\text{Ca}_2\text{CuO}_2\text{Cl}_2$ , where a 2.5–4 eV dispersive feature analyzed within the one-band Hubbard model was reported consistent with  $U = 3.5$  eV [14]. However, both the experimental and the numerical accuracy of such determinations could be improved in the future. Therefore, we performed fits as a function of fixed  $U$ , as summarized in Fig. 4. The dispersion is symmetric in the signs of  $t'$  and  $t''$ , and leads to two possible solutions with  $t't'' < 0$  and  $t't'' > 0$ , respectively. In compliance with ARPES and theoretical estimates, we assume  $t' < 0$ , and lean towards  $t'' > 0$ . Both solutions for  $t''t \leq 0$  constrain  $U$  to larger than  $\sim 2$  eV and smaller than  $\sim 4$  eV for  $t''t > 0$ , and give essentially the same  $t/U$  and  $t'/t$ , which depend only weakly upon the chosen  $U$ , respectively, from 0.17 to 0.12 and from  $-0.31$  to  $-0.42$ . Hence, our data provide strict constraints on the effective parameters that can be used in the one-band Hubbard model for SCOC:  $U$  larger than 1.9 eV, significant second neighbor hopping  $|t'/t| > 0.31$ , and a unique set of hopping parameters for a given  $U$  [Fig. 4(e)]. For  $U = 3.5$  eV, we obtain  $t/U = 0.139 \pm 0.004$ ,  $t'/t = -0.41 \pm 0.01$  or  $-0.38 \pm 0.01$  and  $t''/t = 0.14 \pm 0.01$  or  $-0.32 \pm 0.01$ . These parameters are roughly consistent with ARPES results from SCOC [35], which were described by  $U = 3.5$  eV,  $t = 0.35$  eV,  $t'/t = -0.35$ , and  $t''/t = 0.22$ , with the accuracy of the comparison likely set by the broad ARPES linewidth. Thereby, we have derived a consistent description within a single model of both spin-wave and ARPES spectra.

To gain insight into the origin of the ZB dispersion, we performed the same extended Hubbard model analysis for

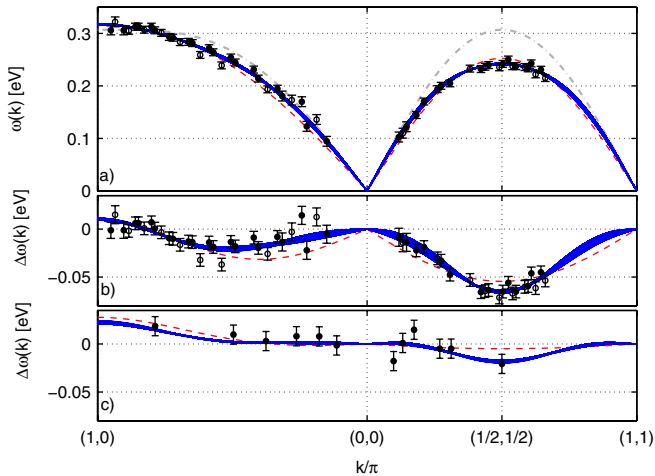


FIG. 3 (color online). (a) Magnon energies extracted from the RIXS data. Open and closed symbols stem from 2 independent measurements on different samples. The dot-dashed line is a NN Heisenberg model with  $J = 130$  meV. The red dashed line is a NN Hubbard model fit for  $t = 0.261 \pm 0.004$  eV and  $U = 1.59 \pm 0.04$  eV. Blue lines are the further-neighbor Hubbard fits. (b) same as (a) with NN Heisenberg dispersion subtracted to better visualize details of the dispersion. The blue band shows the spread in dispersions obtained for fits with  $1.9 \text{ eV} < U < 4 \text{ eV}$ . (c) The fit to the neutron data on  $\text{La}_2\text{CuO}_4$  [7], shifted by  $(\pi, \pi)$  for ease of comparison.



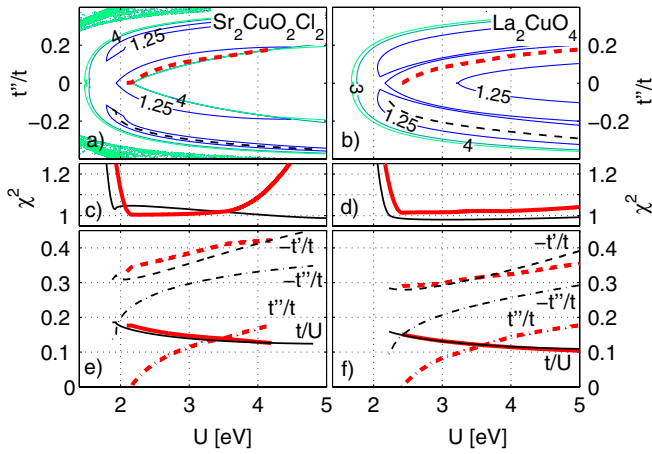


FIG. 4 (color online). Results of extended Hubbard model fits for SCOC (left) and LCO (right). (a),(b)  $\chi^2$  after fitting  $t$  and  $t'$  for fixed  $U$  and  $t''$ . Dashed lines mark the minima versus  $U$ , giving (c),(d) and (e),(f). (c),(d)  $\chi^2$  versus  $U$ , showing the range of  $U$  that our data can support. (e),(f) extracted hopping parameters  $t$ ,  $t'$ , and  $t''$  as function of  $U$ . For given  $U$ , the uncertainty on the  $ts$  is around 5 meV. In all panels, thick red lines are for  $t'' > 0$  and thin black lines for  $t'' < 0$ .

LCO (Fig. 4, right), using the 10 K data by Coldea *et al.* [7]. Also for LCO we find that the spin-wave dispersion can be described by a larger  $U$  more compatible with higher-energy probes, and that there is significant further-neighbor hopping, albeit slightly weaker than in SCOC. For the projected Heisenberg Hamiltonian, this means that the difference in spin-wave dispersion comes not from different main interactions  $J$  and  $J_c$ , but from the many additional further-neighbor hopping paths and hence magnetic interactions. The so-called “ring exchange”  $J_c$  coupling 4 spins on a plaquette is not unique and many further interactions and larger 4-spin loops have similar weight.

In summary, we have employed RIXS to obtain qualitative and quantitative new insight into the magnetic excitation spectrum of the representative two-dimensional antiferromagnetic insulator  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$ . Measuring the full spin-wave spectrum, we found a large zone-boundary dispersion, which we could reproduce with an extended  $t$ - $t'$ - $t''$ - $U$  Hubbard model, placing quantitative constraints on the hopping parameters. Most notably, we demonstrate sizable longer range hopping, and henceforth magnetic interactions. Taking into account the quantum corrections generated by these higher-order hopping terms is essential to achieving a quantitative description of the ground state properties of SCOC, namely, the reduced value of its ordered moment [34]. In a broader perspective, these results establish an important reference and suggest a general method, requiring only small crystals, to address the nature of the ground state, and the evolution of magnetic correlations throughout the phase diagram of the cuprates.

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