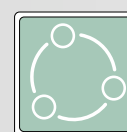


# A Multi-Objective Optimization Method to integrate Heat Pumps in Industrial Processes

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ESCAPE 21: 21st European Symposium on Computer Aided Process Engineering



LENI Systems



# Outline

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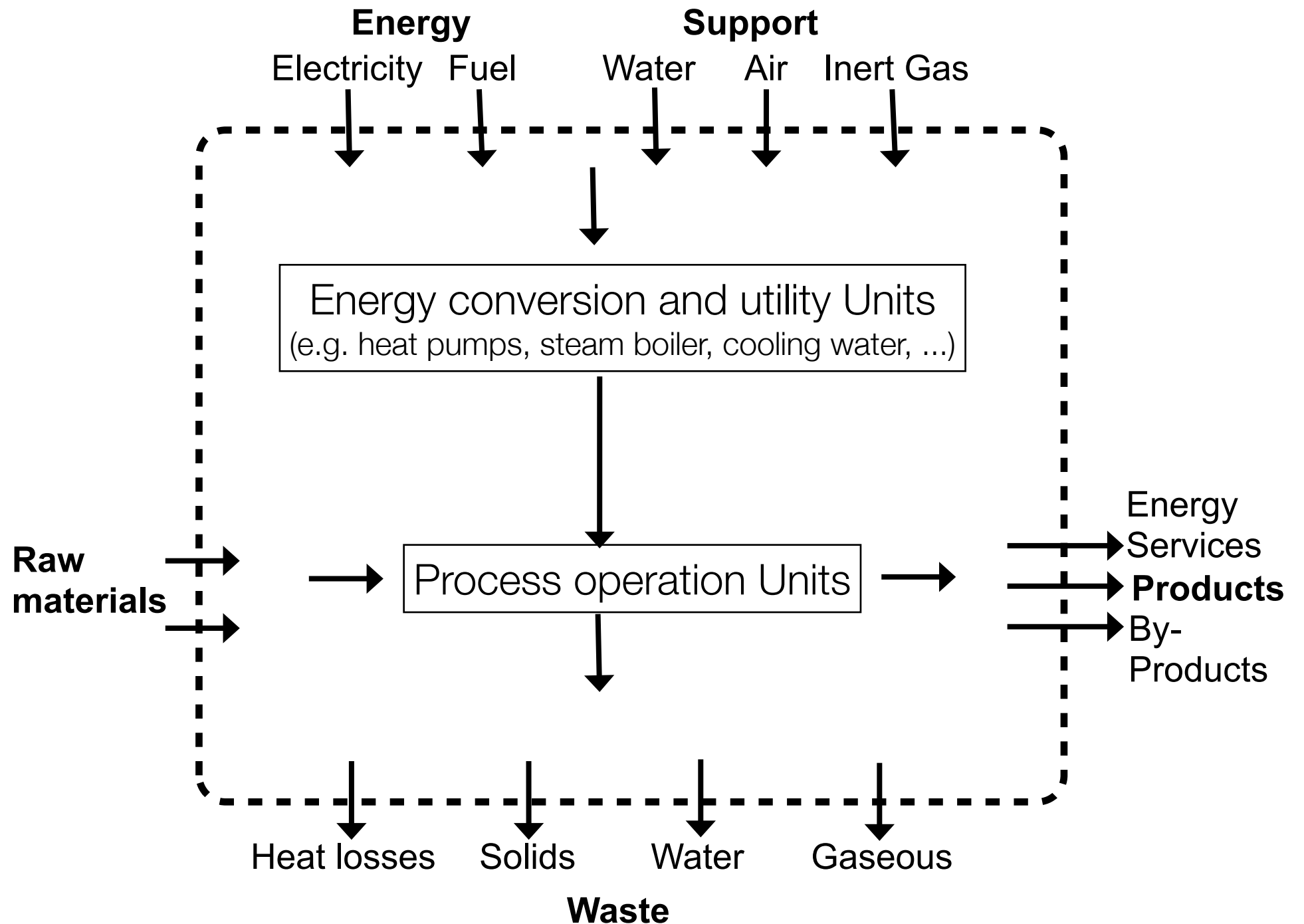
- Introduction
  - Process integration / Case study
  - Challenges
- Methodology
  - Multi - objective optimization
  - Heat pump data base
- Optimization Algorithm
- Results
- Conclusion

# Process integration: Optimize the energy efficiency

Representation of industrial processes

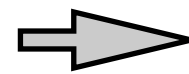
Reducing energy consumption and operating costs

Heat pump integration ?!

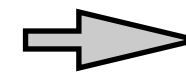


# Case study : Brewery process

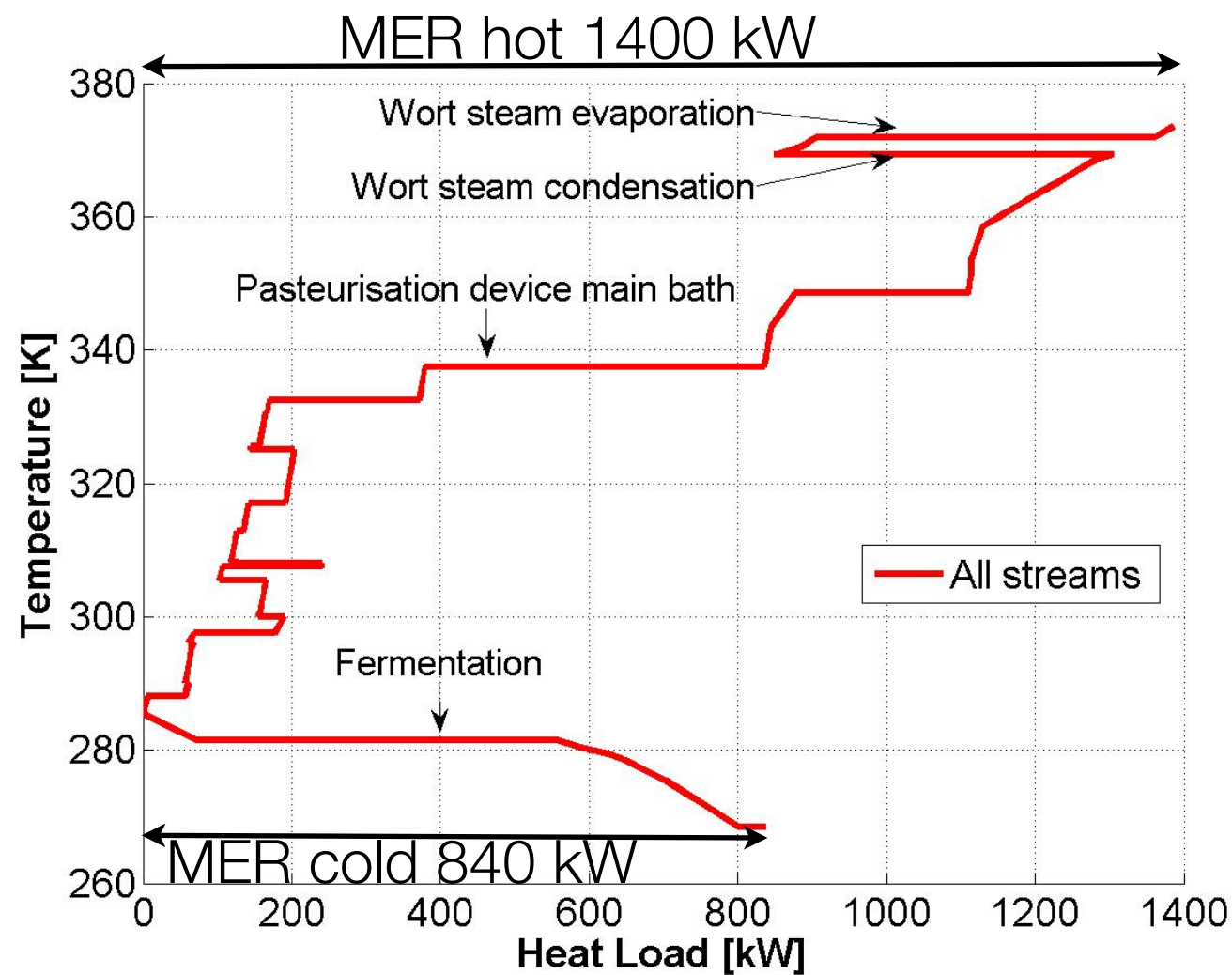
Definition of process requirements



Process integration  
Grand composite curve



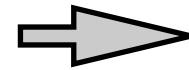
Definition of minimum energy requirements (hot/cold utility)



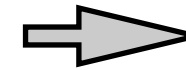
\* Dumbliauskaitė, M., Becker, H., Maréchal, F., 2010. Utility optimization in a brewery process based on energy integration methodology. Proceedings of ECOS 2010, 91–98.

# Case study : Brewery process

Definition of process requirements

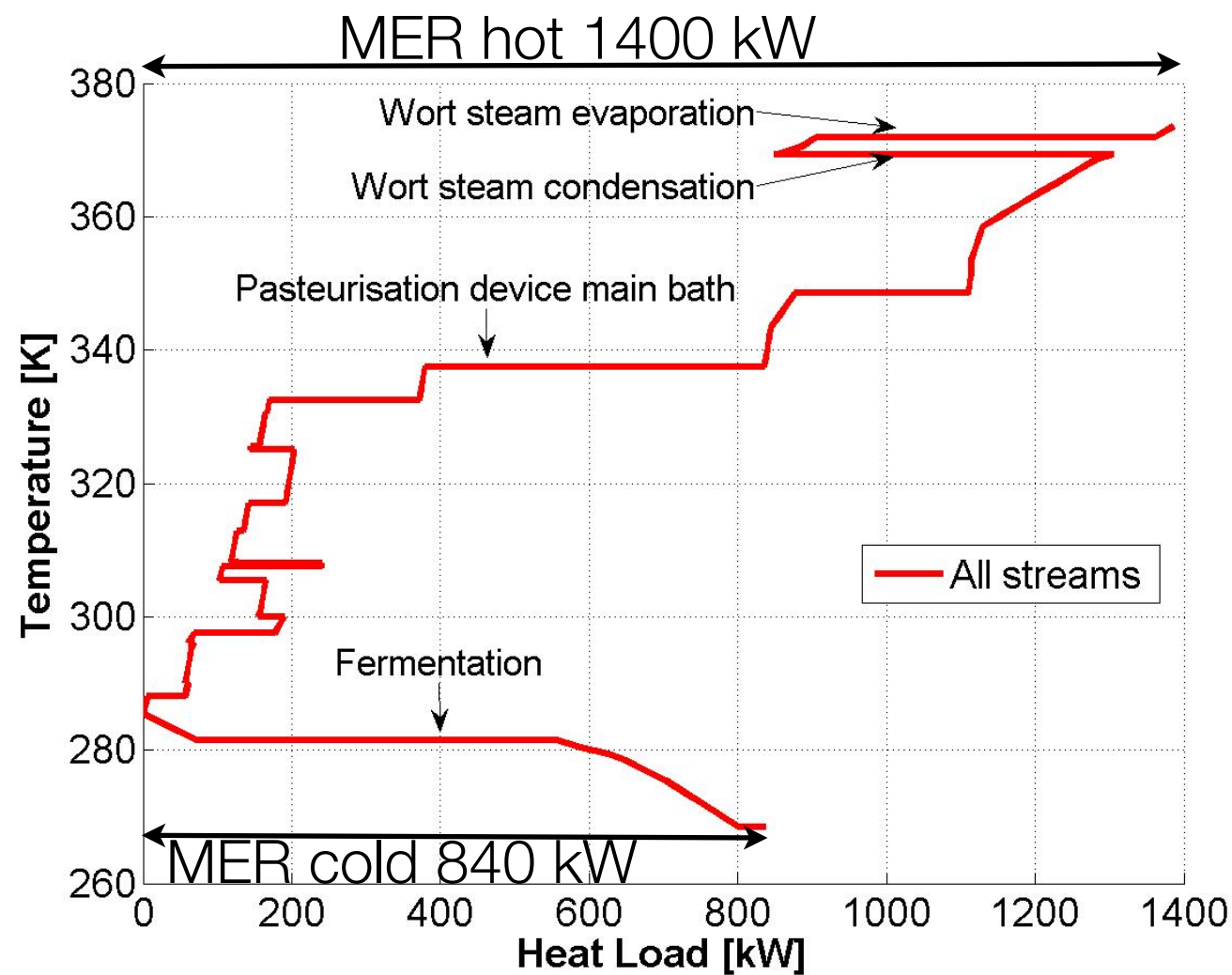


Process integration  
Grand composite curve



Definition of minimum energy requirements (hot/cold utility)

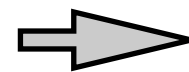
**Heat pump integration:**



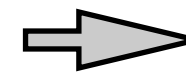
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# Case study : Brewery process

Definition of process requirements

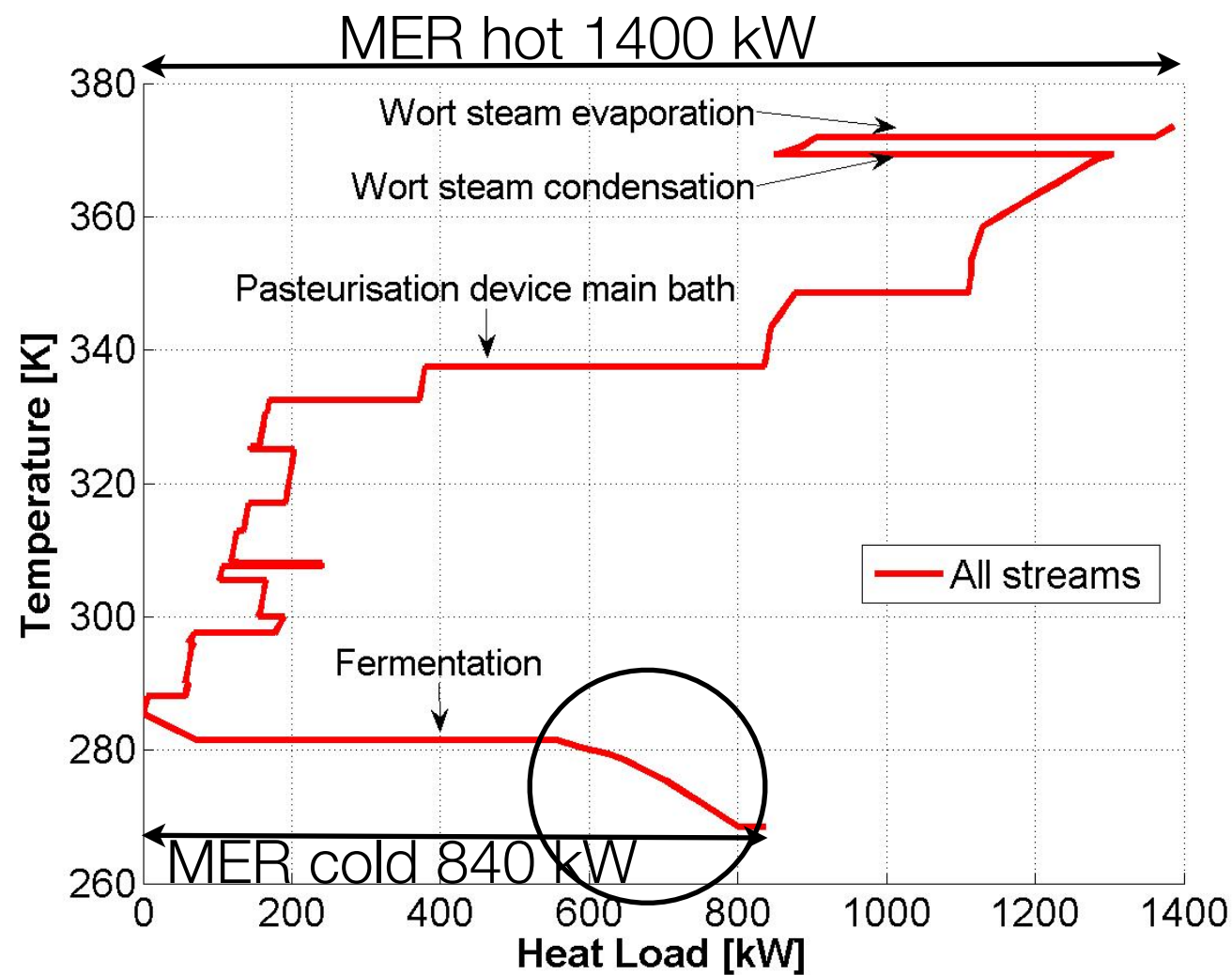


Process integration  
Grand composite curve



Definition of minimum energy requirements (hot/cold utility)

**Heat pump integration:**

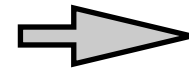


Temperature levels of refrigeration ?  
Different evaporation levels ?

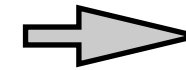
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# Case study : Brewery process

Definition of process requirements



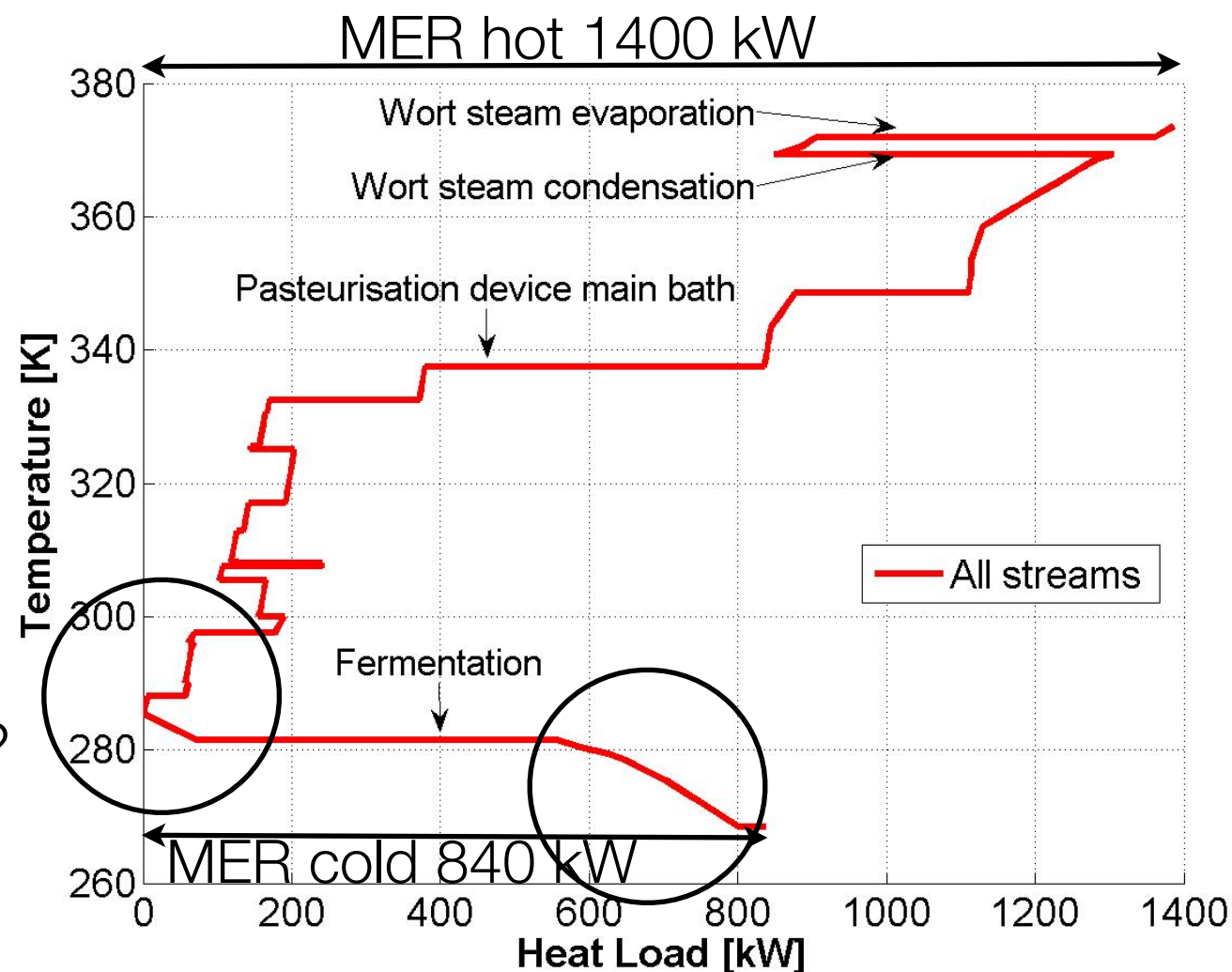
Process integration  
Grand composite curve



Definition of minimum energy requirements (hot/cold utility)

**Heat pump integration:**

Heat pump integration with refrigeration cycles ?



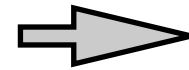
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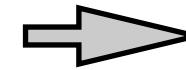


# Case study : Brewery process

Definition of process requirements

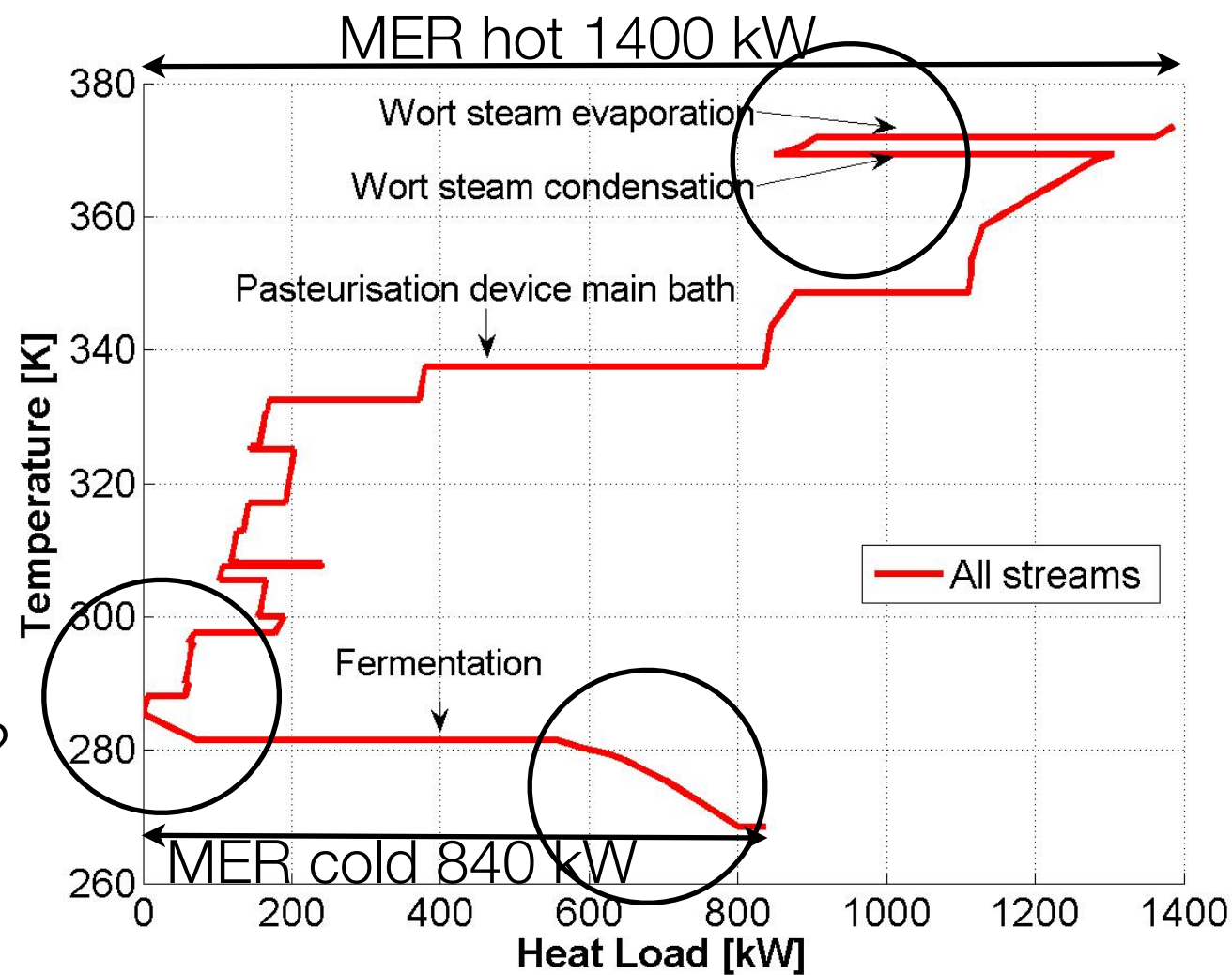


Process integration  
Grand composite curve



Definition of minimum energy requirements (hot/cold utility)

**Heat pump integration:**



Heat pump integration with refrigeration cycles ?

Heat pump potential ? e.g. Mechanical vapour compression ?

Temperature levels of refrigeration ?  
Different evaporation levels ?

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# Challenges for heat pump integration

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- Simultaneously integration with other utilities (e.g. cooling water, steam boiler, cogeneration units, ...)
- Find optimal integrated heat pump(s) system for a given process
  - Select appropriate fluids
  - Cycle configuration and operating conditions
  - Temperature / pressure levels (discontinuous optimization problem)
  - Size of installations and economic evaluation
- Realistic solutions: Heat pump data base (collection of realistic heat pumps to be integrated)
- Systematic methodology: Easy to add new heat pumps

# Method- Master & Slave Problem

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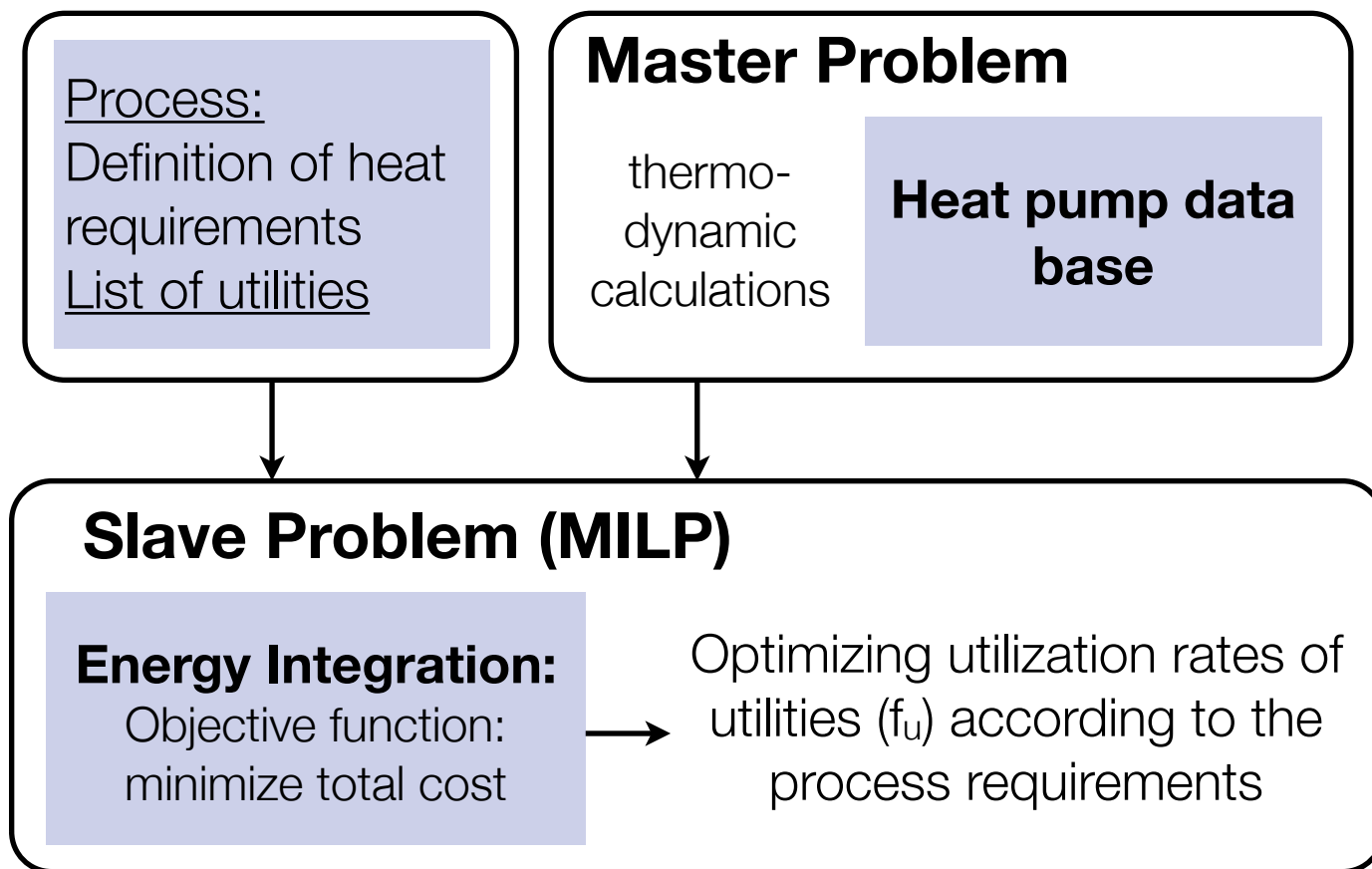
Process:  
Definition of heat requirements  
List of utilities

## Master Problem

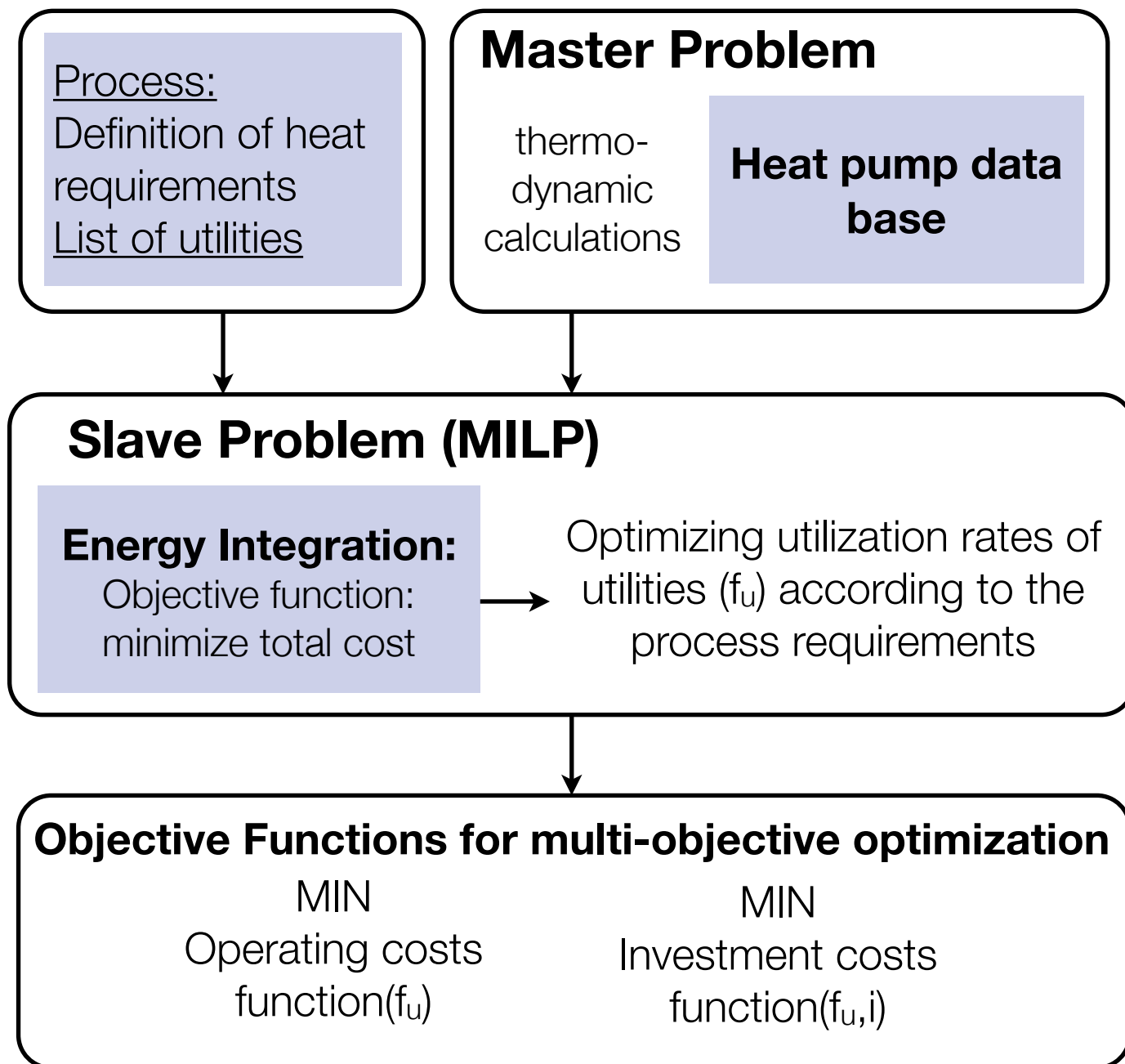
thermo-  
dynamic  
calculations

**Heat pump data  
base**

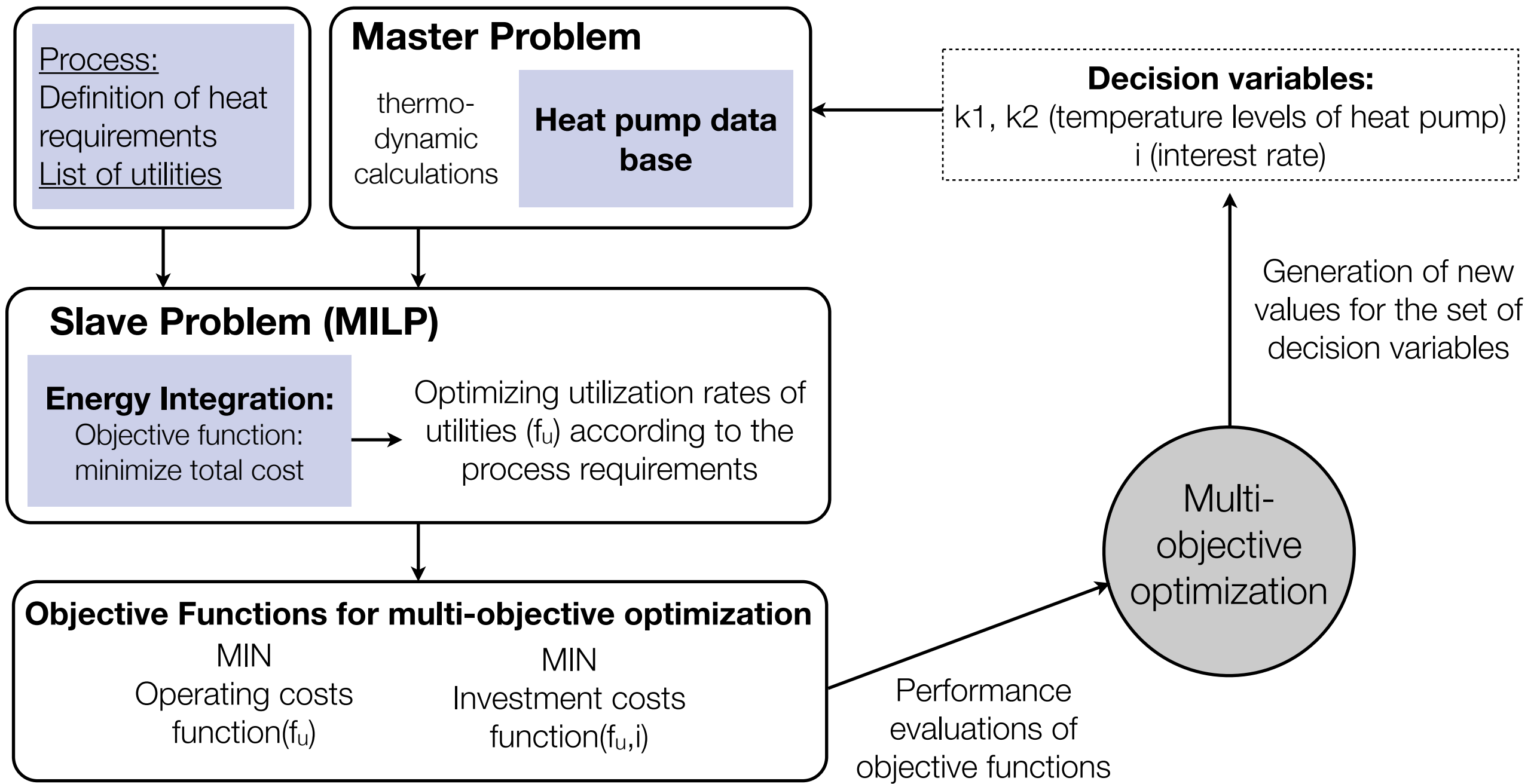
# Method- Master & Slave Problem



# Method- Master & Slave Problem



# Method- Master & Slave Problem



# Heat pump data base

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- Definition of heat pump technologies
  - Compressor types (8) --> Operating condition ranges (volumetric flow rate, pressure ratio)
  - Refrigerants (2) --> Operating condition ranges (temperature levels)
- Each technology is implemented n times --> possibility of multi-stage heat pumps and several times the same type of heat pump
- Heat pump data base is developed in a way that new heat pump models can be added easily
- User can define the list of available heat pumps & change the limits of operating conditions



# Optimization Algorithm

$$\forall c = 1 : n_c \quad \forall f = 1 : n_f$$

## 1. Definition of decision variables

**i** : investment rate [0%,20%]

**k<sub>1,c</sub> & k<sub>2,c</sub>** : temperature levels [0,0.99]

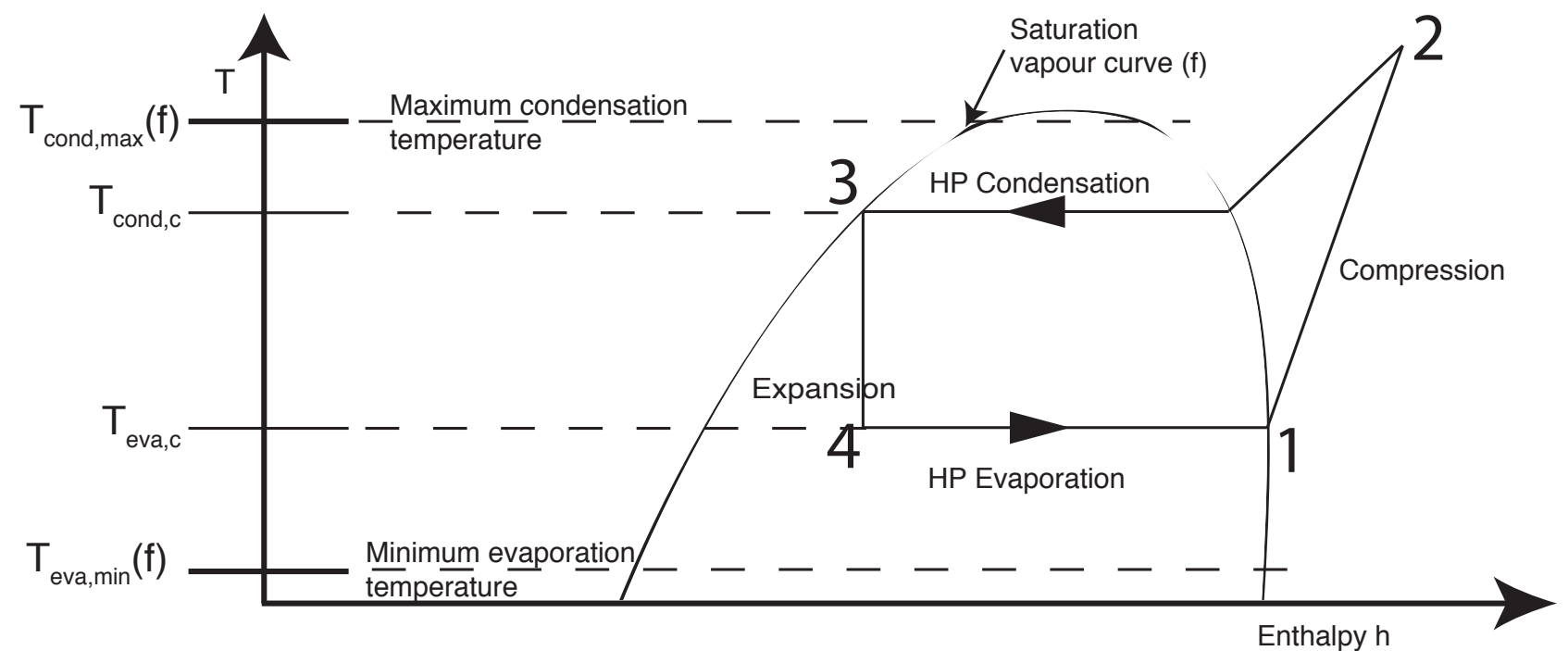
$$\forall c = 1 : n_c \quad \forall f = 1 : n_f$$

2. Master problem

3. Slave problem

4. Evaluation objective functions

### Example for one refrigerant



$$T_{cond,c} = T_{cond,max}(f) - k_{1,c} \cdot (T_{cond,max}(f) - T_{eva,min}(f))$$

$$T_{eva,c} = T_{eva,min}(f) + k_{2,c} \cdot (T_{cond,c} - T_{eva,min}(f))$$

# Optimization Algorithm

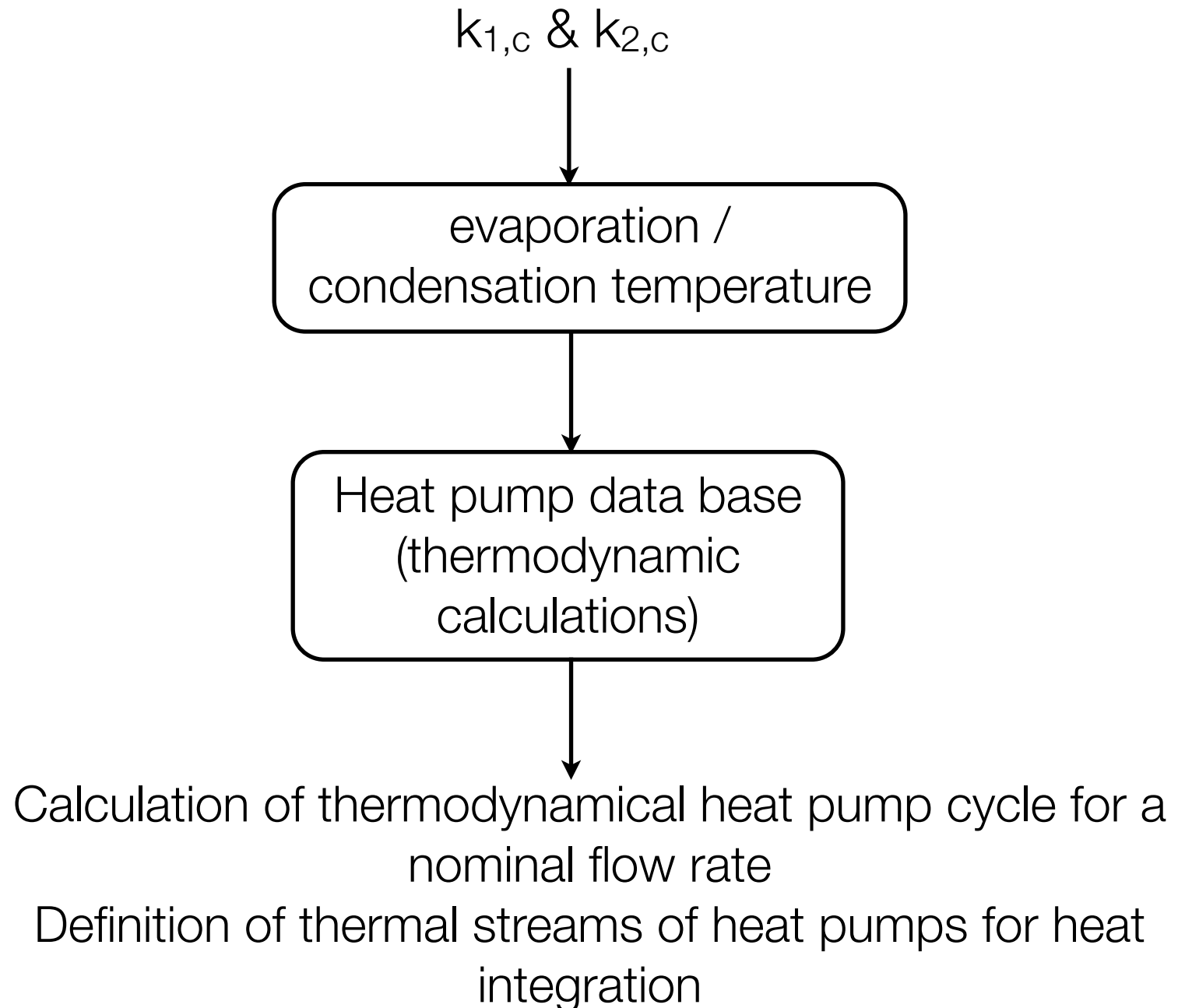
$$\forall c = 1 : n_c \quad \forall f = 1 : n_f$$

1. Definition of decision variables

## 2. Master problem

3. Slave problem

4. Evaluation objective functions



# Optimization Algorithm

$$\forall c = 1 : n_c \quad \forall f = 1 : n_f$$

1. Definition of decision variables
2. Master problem
- 3. Slave problem**
4. Evaluation objective functions

## Heat cascade for Energy integration

$$\sum_{h_k=1}^{n_{sh,k}} \dot{M}_h q_{h,k} - \sum_{c_k=1}^{n_{sc,k}} \dot{M}_c q_{c,k} + \dot{R}_{k+1} - \dot{R}_k = 0 \quad \forall k = 1, \dots, nk$$

$$\dot{R}_1 = 0 \quad \dot{R}_{nk+1} = 0 \quad \dot{R}_k^- \geq 0 \quad \forall k = 2, \dots, nk$$

$$\dot{M}_h = f_u * \dot{m}_h \quad \dot{M}_c = f_u * \dot{m}_c$$

## Operating costs

$$OpC = c_f^+ \sum_{u=1}^{nu} f_u \dot{E}_{f,u}^+ + c_{el}^+ \sum_{u=1}^{nu} f_u \dot{E}_{el,u}^+ - c_{el}^- \sum_{u=1}^{nu} f_u \dot{E}_{el,u}^-$$

## Minimize objective function (MILP - problem)

$$F_{obj,slave} = TC = OpC + InvC \left( \frac{i(i+1)^n}{(i+1)^n - 1} \right)$$

↓  
Optimizing flow rates and utilization factors ( $f_u$ ) of utilities

# Optimization Algorithm

1. Definition of decision variables
2. Master problem
3. Slave problem
4. **Evaluation objective functions**

## Minimize operating costs ( $f_u$ )

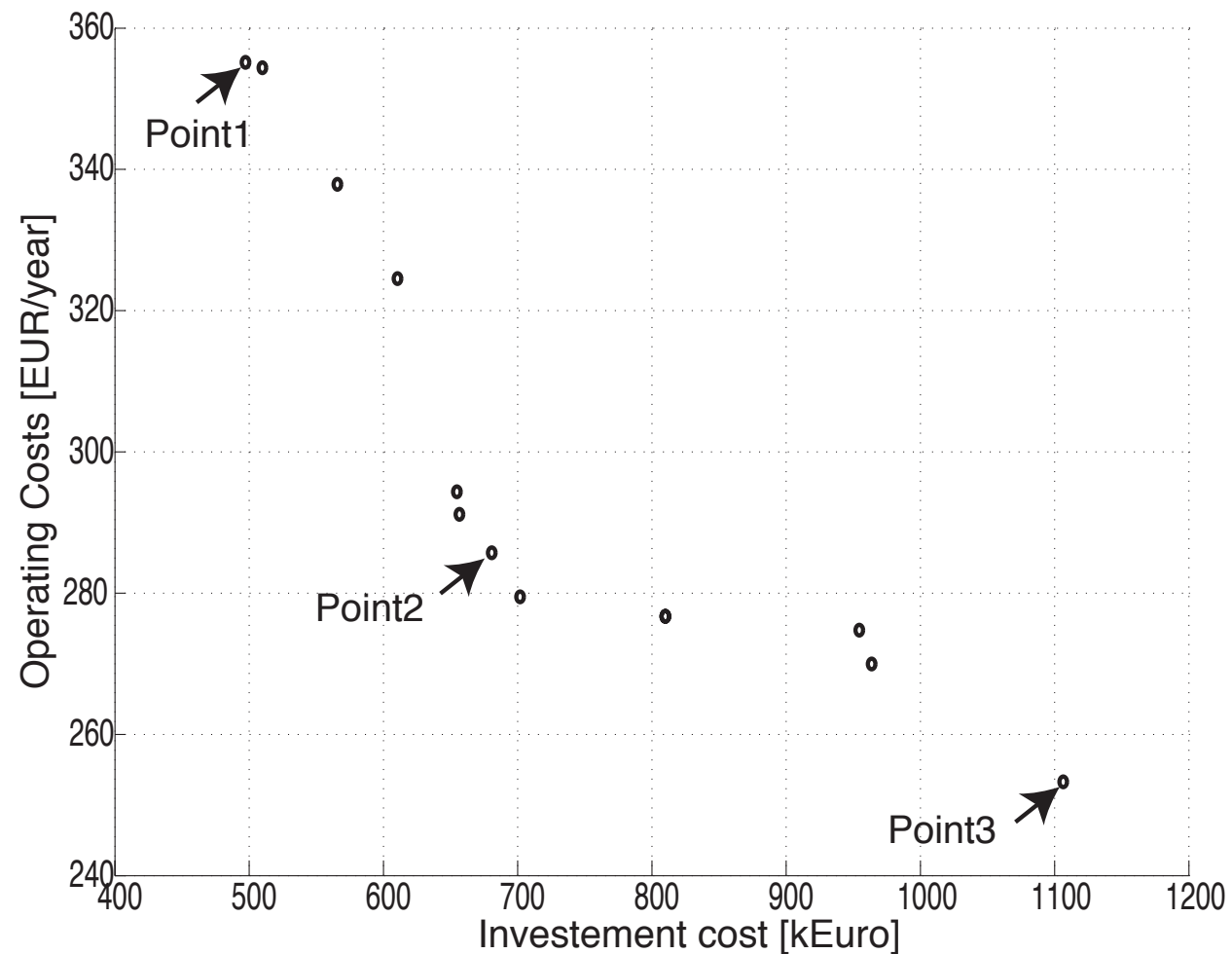
$$OpC = c_f^+ \sum_{u=1}^{nu} f_u \dot{E}_{f,u}^+ + c_{el}^+ \sum_{u=1}^{nu} f_u \dot{E}_{el,u}^+ - c_{el}^- \sum_{u=1}^{nu} f_u \dot{E}_{el,u}^-$$

## Minimize investment costs ( $f_{HPc}$ )

$$InvC = \sum a \cdot (f_{HPc} \dot{E}_{el_{HPc}}^+)^b$$

Performances to multi-objective optimization using evolutionary algorithm  
(Generating new values for the set of decision variables for the next iteration step)

# Results for the case study (brewery process)

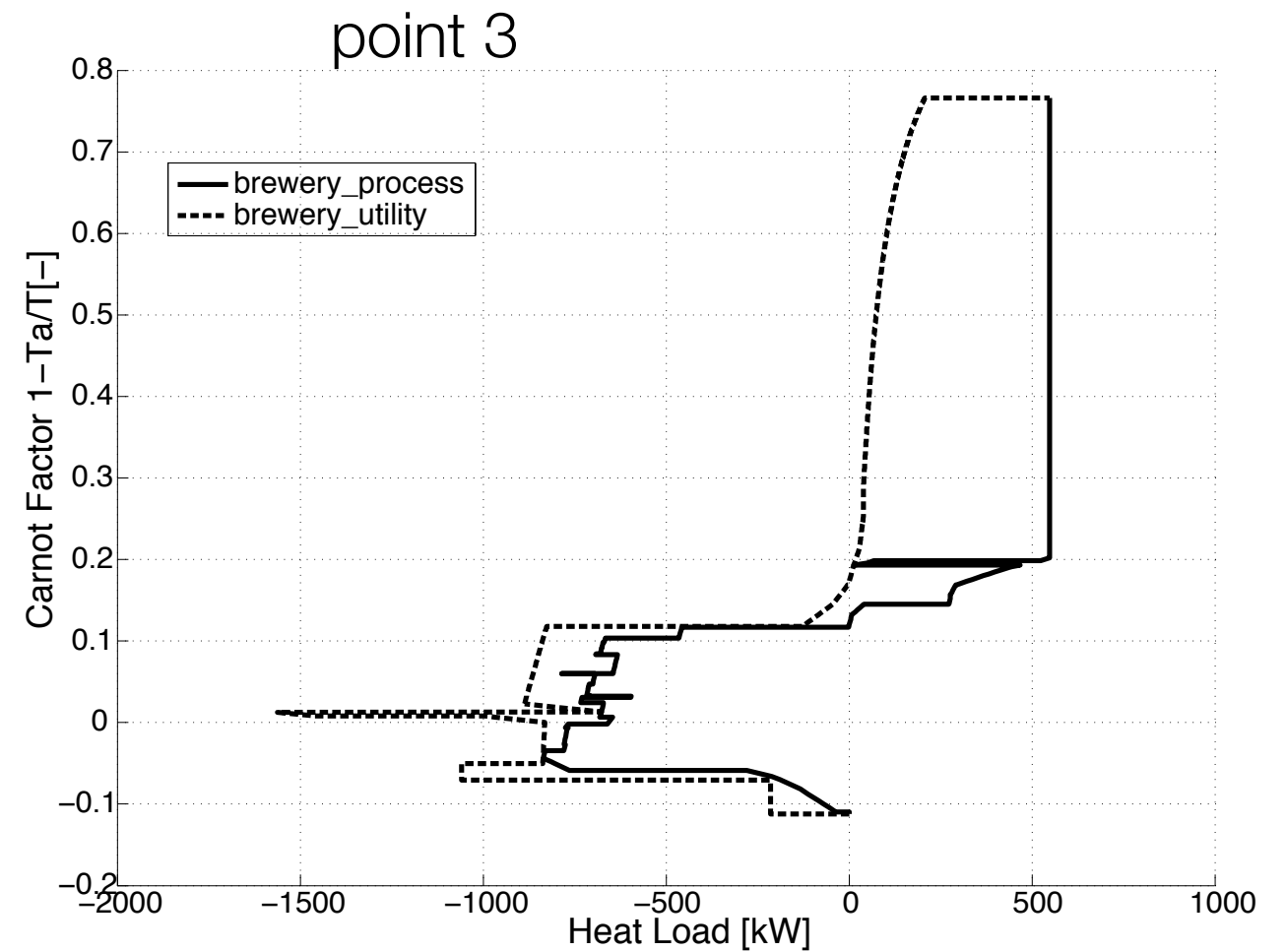
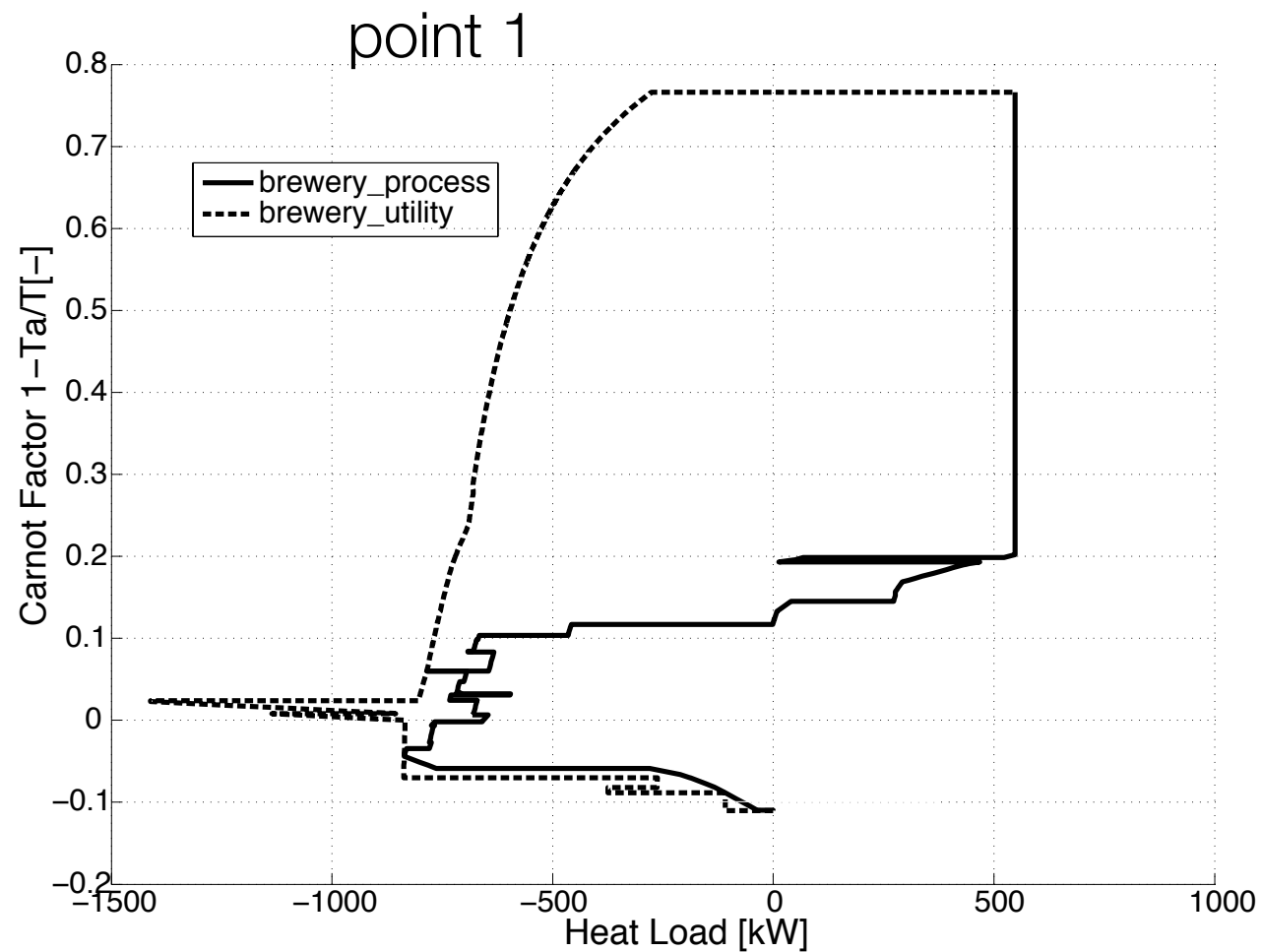


Pareto front: optimal solutions in terms of operating and investment costs

after 1000 iterations  
refrigerants: R717 / R134a HPs

	InvC [kEuro]	OpC [kEuro/year]	Fuel [kW]	Cooling water [kW]	Electricity [kW]	HP units [-]
point1	497.3	355.2	1485	860	206	3
point2	680.8	285.7	615.3	482.4	532.3	5
point3	1106.0	253.3	562.3	368.2	461.3	5

# Example of Integrated composite curves



	InvC [kEuro]	OpC [kEuro/year]	Fuel [kW]	Cooling water [kW]	Electricity [kW]	HP units [-]
point1	497.3	355.2	1485	860	206	3
point2	680.8	285.7	615.3	482.4	532.3	5
point3	1106.0	253.3	562.3	368.2	461.3	5



# Heat pump integration

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- Advantages

- Systematic and flexible integration of heat pumps (technologies, fluids, multi-stage)
- Optimal solutions which can be analyzed in a second step for approbation

- Drawbacks

- Time - consuming
- Experts can find easily good results by analyzing grand composite curves
  - Initialization procedure ?

# Conclusion

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- Optimal heat pump integration (single & multi stage)
- Systematic heat pump data base approach
  - Easy to add new heat pump model (fluids, mixtures, ...)
- All points on the pareto front represent optimal feasible solutions
- Final solution can be chosen by applying economical analysis

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Thank you for your attention !