

Two-Dimensional Vlasov Simulation of Driven, Nonlinear Electron Plasma Waves

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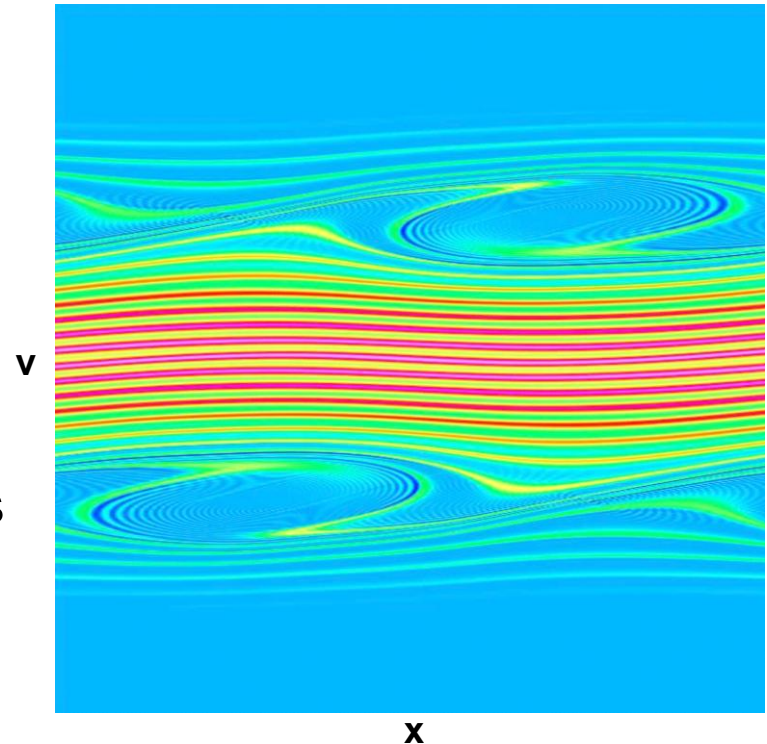
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Why two-dimensional Vlasov simulation?

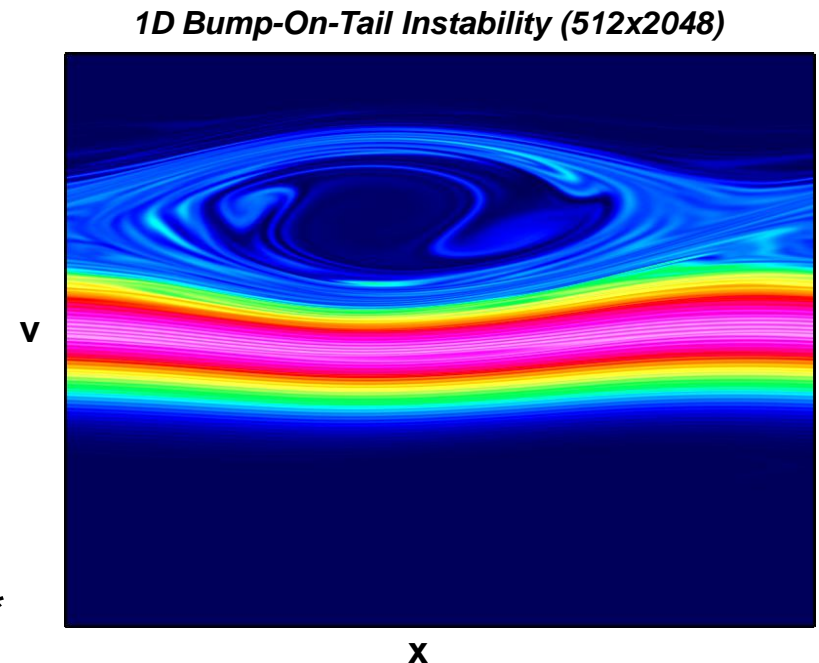
- Wave-particle interaction and particle trapping are important physical effects that influence:
 - ▶ Laser-plasma interactions
 - ▶ RF heating and current drive
 - ▶ Micro-instability and associated turbulence
- Simulation of wave-particle interactions requires a kinetic description
 - ▶ *Challenging for accurate and efficient representation*
- Two-dimensional Vlasov Simulation is **expensive**, but still valuable
 - ▶ Regimes where PIC fluctuations can mask or alter physical effects
 - ▶ Benchmark comparison for PIC results

1D Landau Damping (2048x2048)



To make 2D Vlasov simulation more practical, we have developed new algorithms

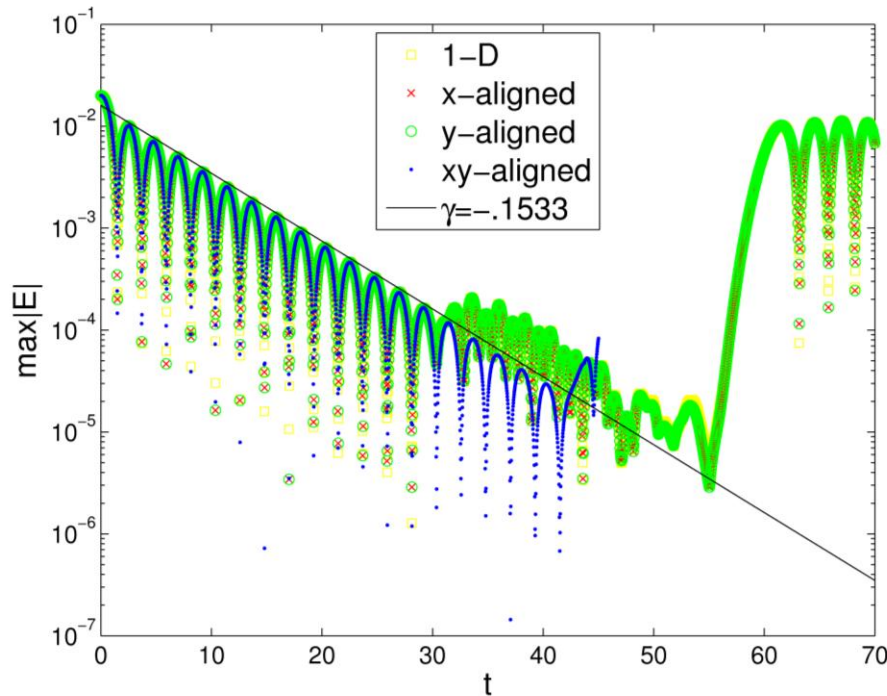
- Traditional Vlasov simulation typically semi-Lagrangian
- We have been developing new, high-order finite volume discretizations[†]
 - ▶ Conservative
 - ▶ Oscillation suppression
 - ▶ Inherently local (scalable)
 - ▶ Well suited for mesh adaptivity
- Our current (2+2)D Vlasov code:
 - ▶ Parallel
 - ▶ Single grid
 - ▶ Single species
 - ▶ Electrostatic and electromagnetic*



[†] Banks and Hittinger, IEEE Trans. Plasma Sci., to appear

*general boundary conditions not yet implemented for electromagnetics

We have verified our code using a variety of physically-motivated test problems



Example: Weak Landau Damping

$$f = f_0 [1 + 0.01 \cos(k_x x + k_y y)]$$

$$(x, y) \in [-L_x, L_x] \times [-L_y, L_y]$$

$$(v_x, v_y) \in [-2\pi, 2\pi] \times [-2\pi, 2\pi]$$

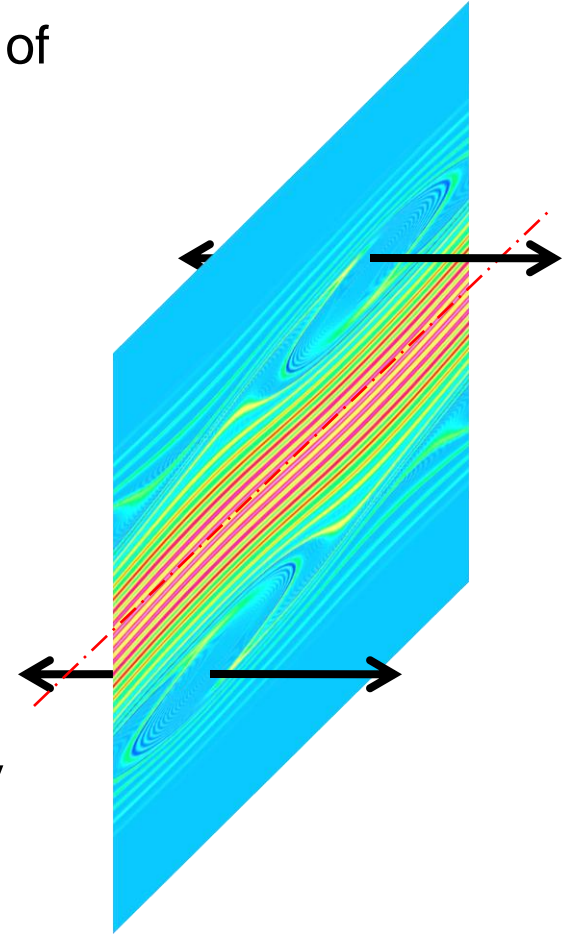
$$N_{v_x} = N_{v_y} = 64$$

(k_x, k_y)	(L_x, L_y)	$N_x \times N_y$
$(1/2, 0)$	$(2\pi, 2\pi)$	64×64
$(1/2, 0)$	$(2\pi, 2\pi)$	64×64
$(1/2, 1/2)$	$(2\sqrt{2}\pi, 2\sqrt{2}\pi)$	128×128

- In 2D, we performed simulations of 1D Landau damping in directions aligned with and diagonal to the grid
- We recovered the correct linear damping rate and frequency

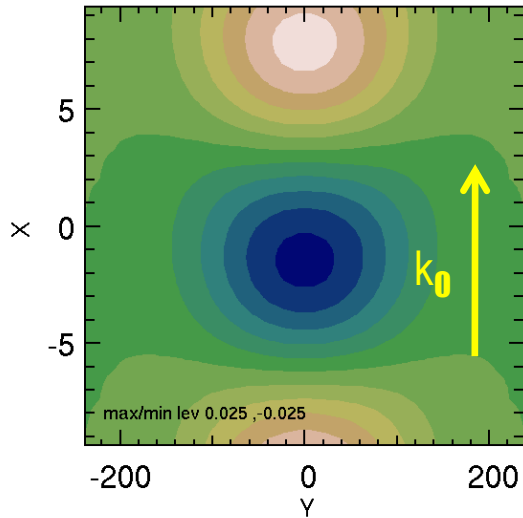
Consider trapping effects in a finite-amplitude Electron Plasma Wave (EPW)

- SRS-driven waves are localized in laser speckles of transverse size $f\lambda_0 \sim 3 \times 10^{-4}$ cm
 - ▶ Electrons trapped are lost in a time:
$$t_r \sim f\lambda_0/v_{th} = 10^{-13} \text{ s}$$
 - ▶ *Commensurate with the SRS growth time*
- Large-amplitude EPWs are more nonlinear in 2D
 - ▶ Self-focusing dependent on the transverse variation of the nonlinear frequency shift
- Two-dimensional Vlasov simulation can:
 - ▶ Test carefully theoretical models of the dependence of the trapped electron frequency shift and the damping rate on t_r
 - ▶ Eliminate doubts about the influence of non-physically large fluctuation levels

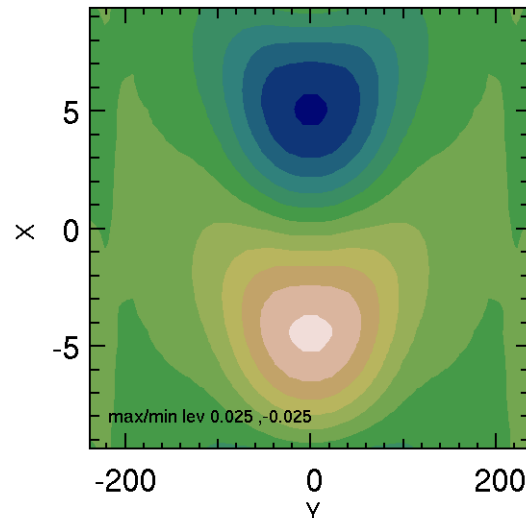


The field appears to focus and maintain its amplitude on axis even as electrons de-trap

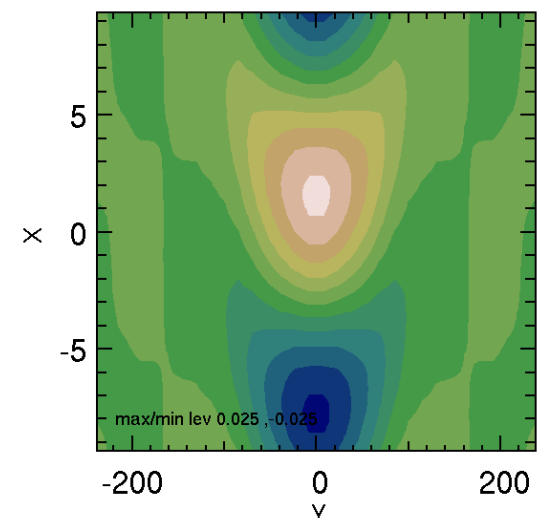
E_x vs x,y at $t = 80$



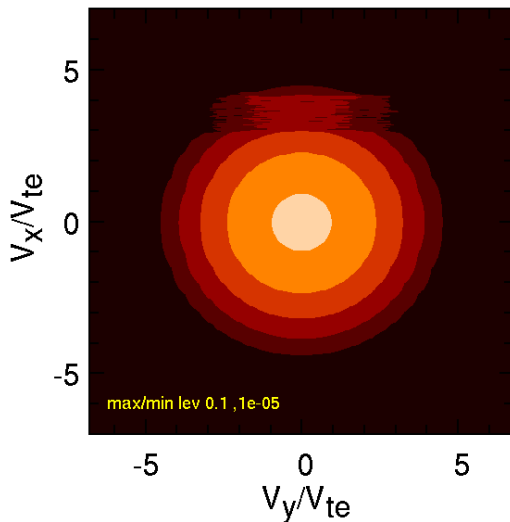
E_x vs x,y at $t = 230$



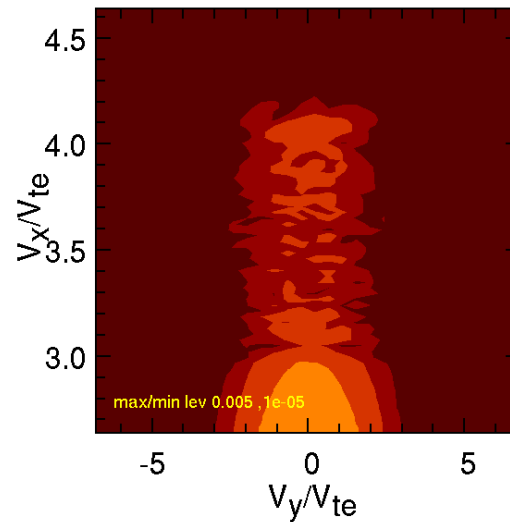
E_x vs x,y at $t = 380$



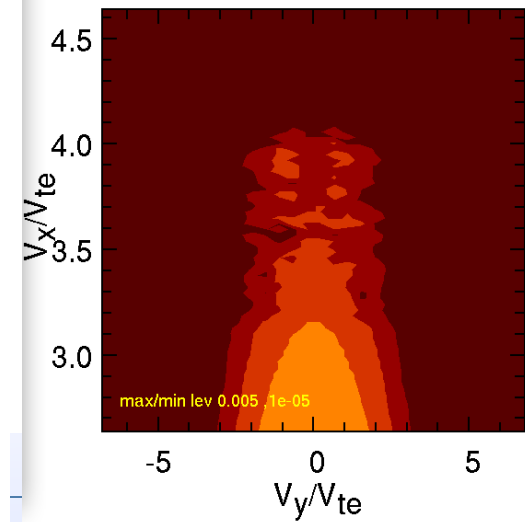
distribution at $t = 360$ and $y = 7.6$ at ϕ_{\max}



distribution at $t = 360$ and $y = 7.6$ at ϕ_{\max}



distribution at $t = 360$ and $y = 237.3$ at ϕ_{\max}



Simulation of a driven nonlinear traveling EPW of finite width in one-wavelength-long system ($L_x = \lambda$)

- The wave is driven by a traveling wave potential:

$$E_{\text{ext}} = A(Y) E_0 \cos(kx - \omega t) P(t)$$

with ω and k chosen to satisfy the linear dispersion:

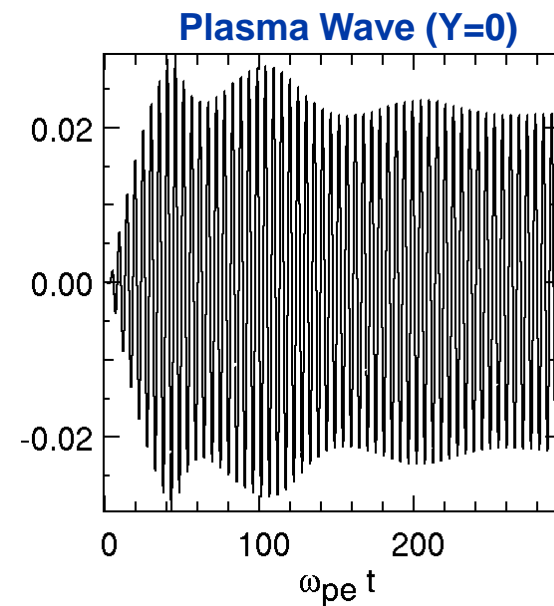
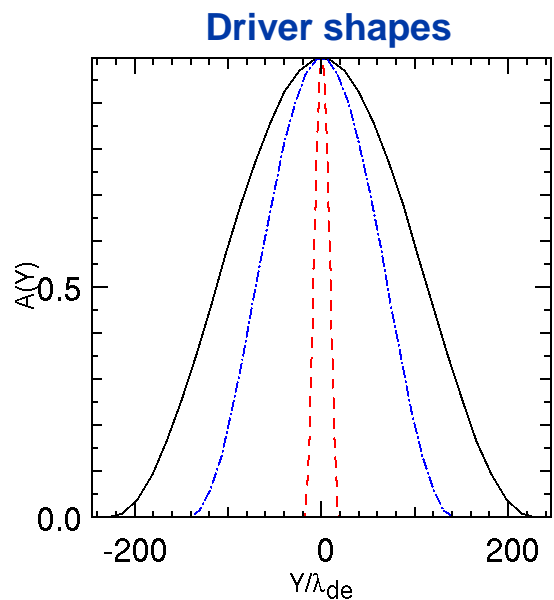
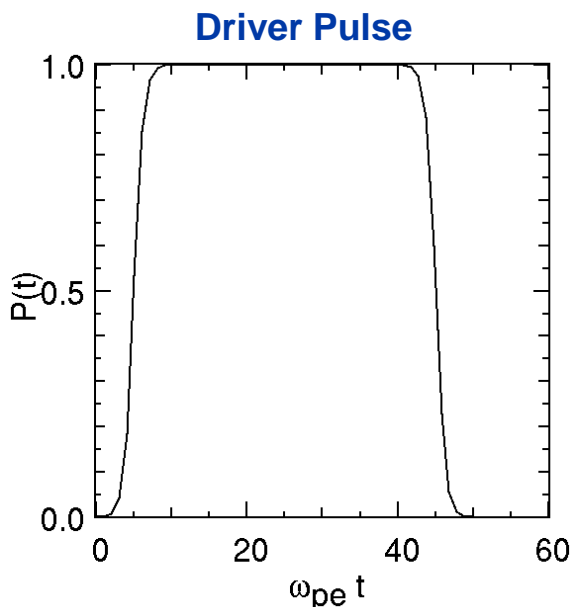
$$k\lambda_{de} = 1/3 \Rightarrow \omega/\omega_{pe} = 1.201$$

- Varied the driver width as shown: FWHM = 20, 144, 220 λ_{de}

$$L_x = \lambda = 2\pi/k$$

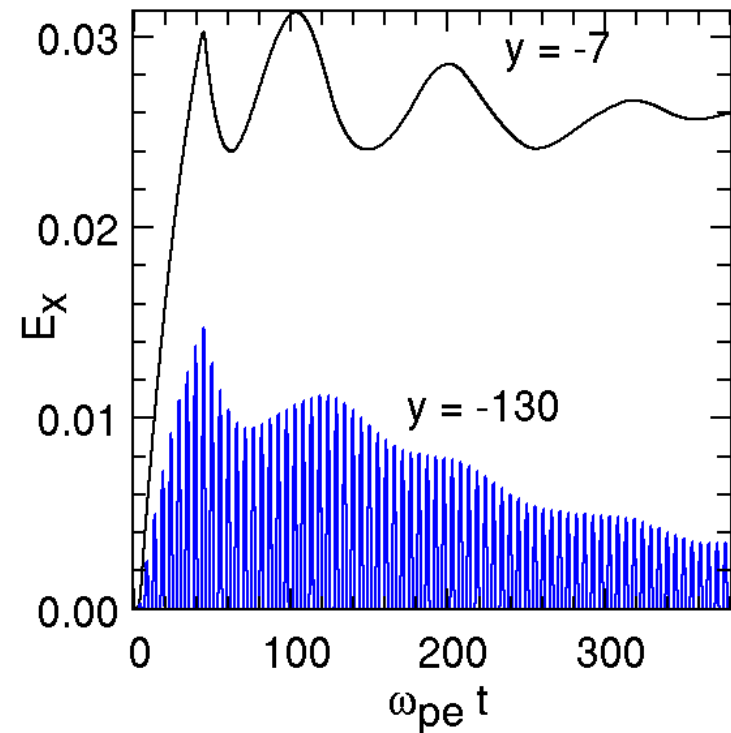
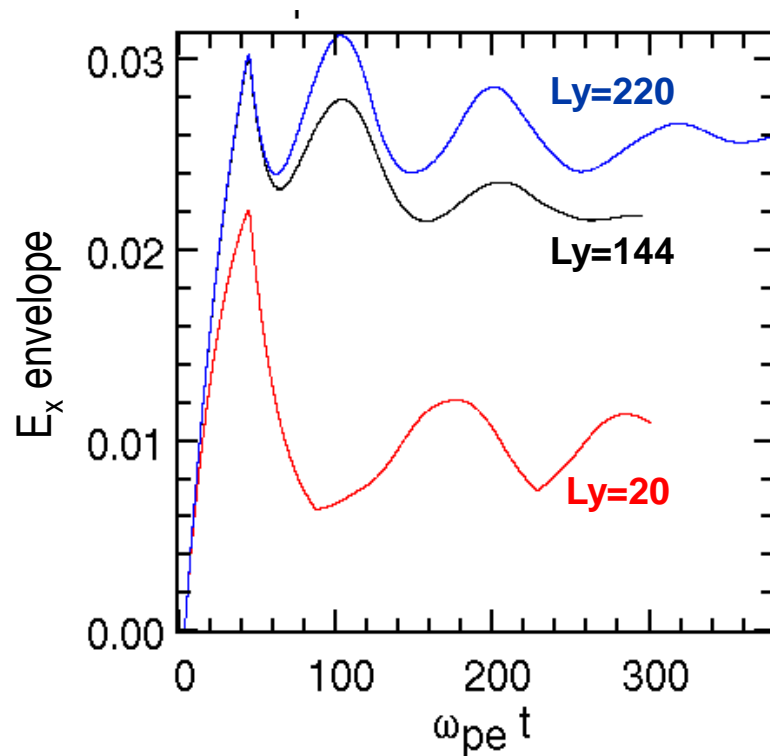
$$L_y \gg L_x$$

Periodic in x
In/Outflow in y



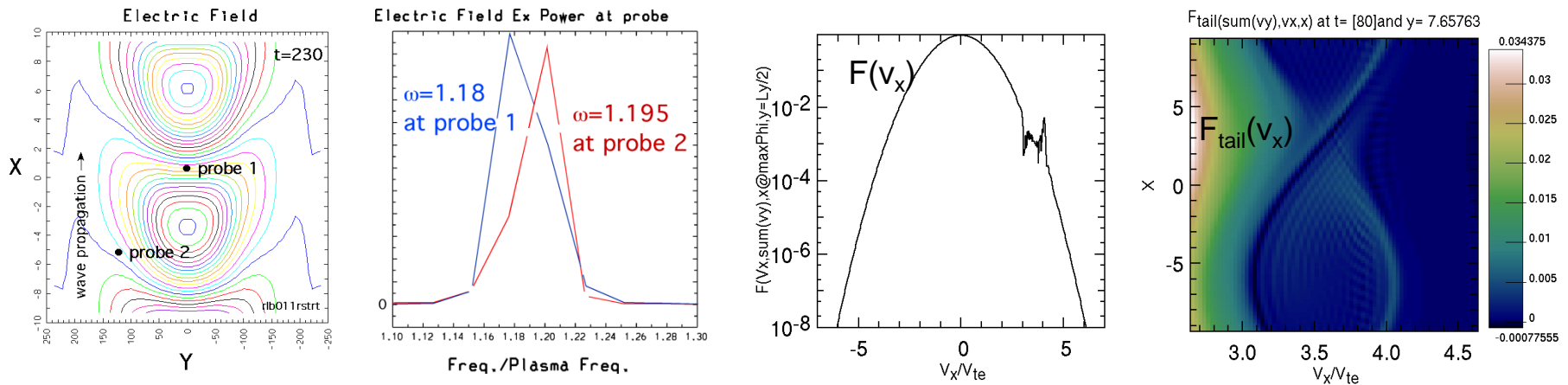
The final amplitude of the plasma wave depends on the width of the driving potential

- Narrow drivers produce lower amplitude EPWs
 - ▶ For laser speckle: $f\lambda_0/\lambda_{de} = 225$ [$f/8$, $\lambda_0=351\text{nm}$, $Te=2.5$, $N_e/N_c=0.1$]
- EPW amplitude in wings of driver decay after driver is off



Trapping effects in a 2D finite-amplitude EPW induce wave-front bending

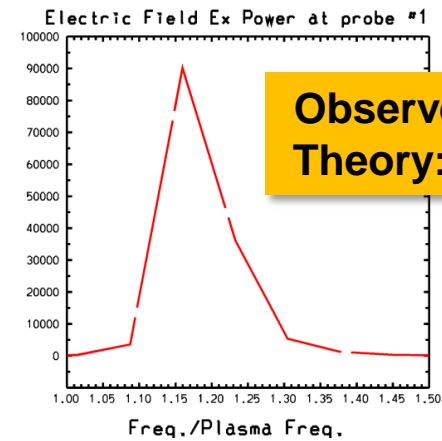
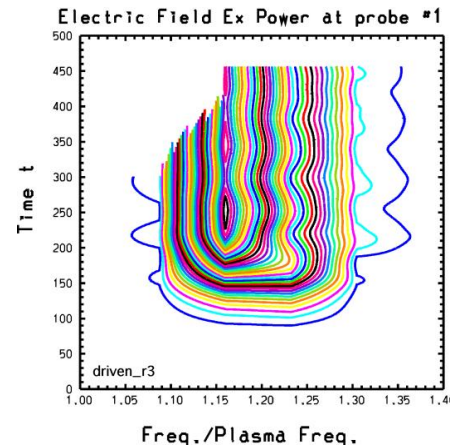
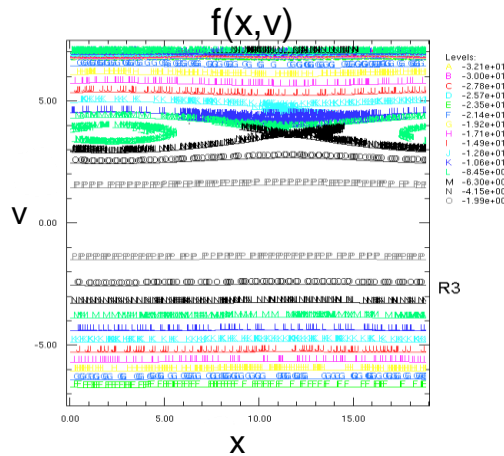
- Electrons are trapped in the wave
 - ▶ more are trapped **along the axis** of the wave where **amplitude is stronger**
- After the driver is off, a nonlinear shift (<0) of the normal mode frequency occurs
 - ▶ **Shift is smaller** at a finite y displacement **away from the axis**
 - ▶ Thus, the **phase velocity is larger** away from the axis
- This phase velocity variation causes the wave front to bow
 - ▶ Consistent with the Raman studies of Yin, *et al.*, PRL **99**, 265004 (2007)



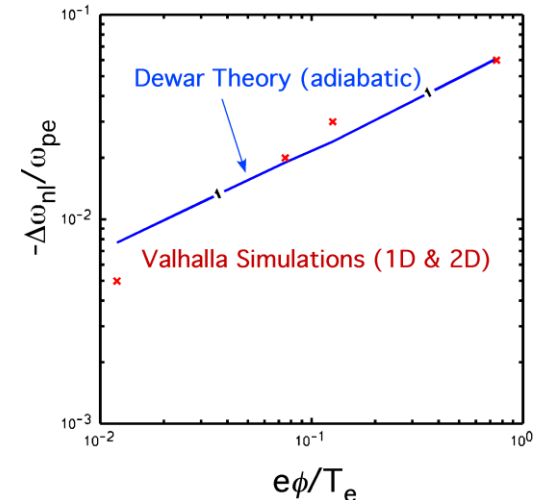
$$(N_x, N_y, N_{vx}, N_{vy}) = (128, 32, 512, 32)$$

For sufficient resolution, frequency shift dependence on wave amplitude agrees with adiabatic theory

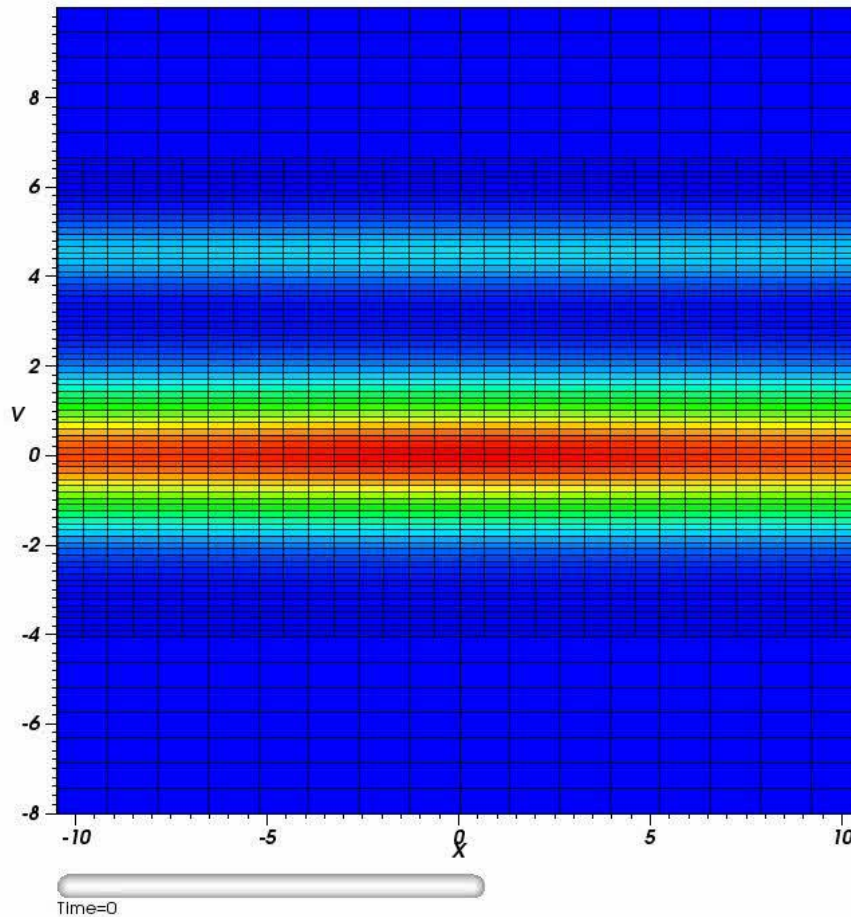
- Results of example 1D simulation with $(N_x, N_v) = (512, 1024)$:



- Scan in wave amplitude in 1D and 2D
 - With adequate (x,v) resolution, compares well with Dewar's theory (adiabatic drive)
- Less resolution in (x,v) space degrades the results
 - Trapped particles must be resolved
 - Particle motion links x and v resolution needs
 - Resolution scan done with uniform mesh



Adaptive Mesh Refinement (AMR) will further reduce the cost of 2D Vlasov simulation



- Our runs required 385 - 768 processors for ~24 hours
- AMR could further reduce the expense
 - ▶ Fewer cell
 - ▶ Larger time steps
 - ▶ Savings increase geometrically with dimension
- Current AMR code:
 - ▶ 1D Vlasov-Poisson
 - ▶ Multi-species
 - ▶ Same discretizations
 - ▶ Based on SAMRAI library

Conclusions and Future Work

- We have demonstrated two-dimensional detrapping effects on driven, nonlinear EPWs using Vlasov simulation
- We will continue to investigate Raman-relevant problems:
 - ▶ Parametric studies of driven EPWs
 - ▶ Vlasov-Maxwell simulation of SRS
- We will continue to improve our simulation capability:
 - ▶ Extend AMR implementation to 2D
 - ▶ Extend AMR implementation to electromagnetics
 - ▶ Investigate improved refinement criteria
 - ▶ Investigate improved time integration techniques
 - ▶ Investigate improved non-reflective boundary conditions

