

Physics Beyond the Standard Model

Riccardo Rattazzi

Department of Physics, CERN, CH-1211 Geneva 23, Switzerland

Abstract

I review recent theoretical work on electroweak symmetry breaking.

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1 Introduction

I have been assigned this broad title but my talk will be mostly concerned with the origin of the electroweak scale. I will attempt to give an overview of the theoretical ‘laborings’ that came up after the end of the LEP era and in preparation to the commissioning of the LHC. An appropriate subtitle for my talk could thus be ‘Electroweak Symmetry Breaking after LEP/SLC’.

There are two different sides from which to regard the legacy of LEP/SLC, and forming what is also known as the LEP paradox [1]. From one side it is an impressive triumph of human endeavour: the Standard Model (SM) is a complete theory of fundamental processes successfully tested at the per-mille precision. That means that small quantum corrections to the Born approximation are essential in the comparison between theory and experiment. However, when regarded from the other side, this great success becomes a huge conceptual bafflement, because the hierarchy problem, which inspired theoretical speculations for the last three decades, suggested that the SM should be overthrown right at the weak scale. That did not happen, so we must now understand why. I will discuss the paradoxical LEP/SLC legacy in the first part of my talk. In the second part I will attempt to give an overview on the new ideas that were stimulated partly by the LEP paradox, on the phenomenological side, and partly by field theory developments (concerning for instance the use of extra-dimensions and branes) on the theoretical side. I think it will emerge that, while potentially realistic and certainly very ingenious, these attempts still leave something to be desired. In fact it may even be fair to say that these models concretely embody the LEP paradox. Indeed, because of the increasing sense of frustration with the standard approaches, a radically different approach to the hierarchy problem has recently been advocated. That involves the use of variants of the anthropic principle to explain the puzzling values of apparently fundamental parameters, such as the cosmological constant or the Higgs mass. In the third part of my talk I will illustrate how anthropic considerations can explain the puzzling need, after LEP2, for tuning on models with low energy supersymmetry.

2 The legacy of LEP/SLC

The large set of data collected in electron–positron collision at LEP/SLC displays a remarkable $O(10^{-3})$ agreement with the SM for a relatively light Higgs. More precisely, a global electroweak fit [2] gives with 95% CL the bound $m_h < 219 \text{ GeV}$. On the other hand, the SM suffers from the hierarchy problem: the Lagrangian Higgs mass parameter m_H^2 , which is related to the physical mass by $m_h^2 = -2m_H^2$, is affected by uncalculable cut-off dependent quantum corrections. Whatever more fundamental theory replaces the SM above some scale Λ_{NP} , barring unwarranted cancellations, it is reasonable to expect the Higgs mass parame-

ter to be at least of the same size as (or bigger than) the SM contribution computed with a cut-off scale Λ_{NP} . (This way of estimating the size of the Higgs mass is made reasonable by many explicit examples that solve the hierarchy problem, and also by analogy with well-known quantities in low energy physics, such as the electromagnetic contribution to $m_{\pi^+}^2 - m_{\pi^0}^2$.) The leading quantum correction is then expected to come from the top sector and is estimated to be

$$\delta m_H^2 \sim -\frac{3\lambda_t^2}{8\pi^2}\Lambda_{\text{NP}}^2. \quad (1)$$

In the absence of tuning, this contribution is compatible with the allowed range of m_h^2 only if the cut-off is rather low

$$\Lambda_{\text{NP}} < 600 \times \left(\frac{m_h}{200 \text{ GeV}}\right) \text{ GeV}. \quad (2)$$

If we allow a fine-tuning of order ϵ then the bound is relaxed by a factor $1/\sqrt{\epsilon}$. Now, the question is: if the energy range of validity of the SM is as low as 500–1000 TeV, why did LEP/SLC not detect any deviation from the SM predictions in their rich set of data? Even though the center of mass energy of these experiments is significantly lower than 1 TeV, still their precision is high enough to make them sensitive to new virtual effects associated to a much higher scale than their center of mass energy. The effects from new physics at a scale Λ_{NP} can in general be parametrized by adding to the SM renormalizable Lagrangian the whole tower of higher dimensional local operators, with coefficients suppressed by the suitable powers of Λ_{NP} [3]:

$$\mathcal{L}_{eff}^{\text{NP}} = \frac{1}{\Lambda_{\text{NP}}^2} \left\{ c_1(\bar{e}\gamma_\mu e)^2 + c_2 W_{\mu\nu}^I B^{\mu\nu} H^\dagger \tau_I H + \dots \right\}. \quad (3)$$

At leading order it is also sufficient to consider only the operators of lowest dimension, $d = 6$. The constraints on the whole set of $d = 6$ operators have been studied in ref. [4]. The lower bound on Λ_{NP} for each individual operator \mathcal{O}_i , neglecting the effects of all the others and normalizing $|c_i| = 1$, ranges between 2 and 10 TeV. Turning several coefficients on at the same time does not qualitatively change the result, unless parameters are tuned. The interpretation of these results is that if New Physics affects electroweak observables at tree level, for which case $c_i \sim O(1)$, the generic lower bound on the new threshold is a few TeV. The tension between this lower bound and eq. (2) defines what is known as the LEP paradox. This is an apparently mild problem. But notice that the needed tuning ϵ grows quadratically with Λ_{NP} , so that for $\Lambda_{\text{NP}} = 6 \text{ TeV}$ we need to tune to 1 part in a hundred in order to have $m_H = 200 \text{ GeV}$. In view of this problem, things would look definitely better if New Physics affected low energy quantities only via loop effects. In this case $c_i \sim \alpha/4\pi$ and $\Lambda_{\text{NP}} < 600 \text{ TeV}$ would not lead to any tension with electroweak precision tests. It is at first reassuring that Supersymmetry with R -parity, arguably the leading candidate New Physics scenario,

precisely enjoys this property, with the mass scale of supersymmetric particles identified with Λ_{NP} . However the attraction of Supersymmetry largely lies in its giving a very plausible picture for physics way above the weak scale and up to the Planck scale where, in addition to electroweak symmetry breaking (EWSB), also Gauge Unification, neutrino masses and Dark Matter fit very well. In this extrapolation, however, the leading quantum contribution to the Higgs mass parameter is not eq. (1) but the larger one associated to renormalization group (RG) logarithms. In the Minimal Supersymmetric Standard Model (MSSM) the relation between the various mass parameters is then roughly

$$m_Z^2 \sim -2m_H^2 = -2\mu^2 + \frac{3}{2\pi^2}\lambda_t^2 m_{\tilde{t}}^2 \ln \frac{M_{Planck}}{m_{\tilde{t}}} + \dots \quad (4)$$

$$\sim -2\mu^2 + O(1) m_{\tilde{t}}^2 + \dots, \quad (5)$$

where we have not displayed the normally less relevant contributions. From the above we deduce that the natural expectation is to have the stop, the charginos and everything else at or below the vector boson scale

$$m_Z \sim m_{\tilde{t}}, \sim \mu \sim \dots \quad (6)$$

The above relation raised great hope of new discoveries at LEP/SLC. This did not happen, and so supersymmetry can no longer be viewed as completely natural. In fact, at least in the MSSM, the situation is made even worse by the indirect, and stronger, bound placed on the stop mass by the lower bound on the lightest Higgs mass. As is well know, in the MSSM the physical mass of the lightest Higgs has an upper bound, which in 1-loop accuracy reads roughly

$$m_h^2 \leq m_Z^2 + m_t^2 \frac{3\lambda_t^2}{2\pi^2} \ln m_{\tilde{t}}/m_t. \quad (7)$$

The second term on the right-hand side corresponds to the leading top/stop radiative correction to the Higgs quartic coupling. It is then only thanks to this correction that m_h can exceed its direct experimental (95% CL) lower bound of 114.4 GeV. However, this generically requires $m_{\tilde{t}} \gtrsim 500\text{--}1000$ GeV, which when compared to eq. (5) implies that a cancellation with 1 to 5% accuracy is needed. Although the description we give here is somewhat schematic, the problem is ‘robust’, in the sense that it does not depend in any significant way on the full structure of the soft terms. In particular things are not dramatically improved by considering the extra positive contribution to the right-hand side of eq. (7) that arises for large $\tilde{t}_L\text{--}\tilde{t}_R$ mixing. This is because the sizeable A -terms that are needed for that to happen require some tuning too. Another often heard criticism to the above simple argument concerns the fact that the bound on m_h in the MSSM is, strictly speaking, lower than 114.4 GeV. This is because the coupling of h to the Z-boson is a factor $\sin(\beta - \alpha)$ smaller than the one in the

SM. In some regions of the supersymmetric parameter space this suppression can become significant, making the bound on m_h weaker and thus giving the impression that the need for tuning is relaxed. However as a direct analysis shows [5, 6], the parameter space region where this happens corresponds to an even bigger tuning than the 1–5% estimated above. This is because one needs $\tan\beta \gg 1$ (which always entails some tuning), the mass of the second CP-even Higgs m_H tuned somewhat close to m_h and a still sizeable stop contribution to the Higgs quartic coupling.

While the problem is ‘robust’ within the MSSM, it can be somewhat relaxed just by adding a single superfield N to the model, thus upgrading the theory to the so-called NMSSM. In the presence of N there is an additional positive contribution to the right-hand side of eq. (7), due to the superpotential trilinear coupling NH_1H_2 . This allows a relaxation of the lower bound on the stop mass. A detailed analysis, described in ref. [7], shows that the amount of fine tuning can in general be relaxed to about 10%. This is encouraging, although my impression is that in several attractive scenarios for supersymmetry breaking, such as gauge or anomaly mediation, the soft terms have such a structure as to make the desired electroweak vacuum with $\langle H_2 \rangle, \langle H_1 \rangle, \langle N \rangle \neq 0$ rather hard to obtain, that is to say very tuned. Some extra model building effort in the context of the NMSSM is perhaps desirable.

In the end, should we really worry about tuning at the few per cent level? Perhaps not, but we should keep in mind that once we are willing to accept some tuning, the motivation for New Physics at the LHC becomes weaker. Notice indeed that, already with a tuning at the per mille level, the sparticles are out of reach at the LHC.

2.1 Technical parenthesis: LEP1 & LEP2 bounds on New Electroweak Physics

I now want to illustrate the impact of electron–positron data by focusing on the simplest scenario for New Physics in the electroweak sector, the so-called universal models. These are the models where deviations from the SM appear, at leading order, only through vector boson vacuum polarizations [8]

$$\begin{aligned} \mathcal{L}_{NP} &= W_+^\mu \Pi_{+-}(q^2) W_{+\mu} + W_3^\mu \Pi_{33}(q^2) W_{3\mu} & (8) \\ &+ W_3^\mu \Pi_{3B}(q^2) B_\mu + B^\mu \Pi_{BB}(q^2) B_\mu & (9) \end{aligned}$$

Most Technicolor, Little Higgs and Higgsless models practically belong to this class [9], showing that it is not an obviously idle exercise to focus on universality. I say ‘practically’, since the more realistic versions of these models almost always display extra effects involving the third-family fermions, and associated to the large value of the top quark Yukawa coupling. However, since the majority of the observables (and arguably those that are under better

experimental control) only involve the fermions of the first two families, the bounds on universal models indeed have a more general relevance.

The electroweak constraints on universal models were widely discussed in the 90's. However, as I will now show, and as it was recently discussed in ref. [9], some important aspects were always either missed or not emphasized. Consistent with the absence of new particles at LEP2, let me start by assuming that the scale of new physics Λ_{NP} is somewhat above the energy of LEP2. It then makes sense to expand the vacuum polarizations $\Pi(q^2)$ as a power series in q^2 and retain only the leading terms. In order to decide which terms are leading, it is useful to classify the vacuum polarizations in eq. (8) according to their transformation properties under custodial symmetry and under the electroweak group $SU(2)_L$ (the two relevant symmetries of the problem). Within any given symmetry class is then natural to retain only the term of lowest order in the Taylor expansion in q^2 . This is because, barring accidental cancellations that make the lowest-order term in a given class anomalously small, the higher-order terms in the same class will give effects at around the Z^0 pole that are smaller by at least a factor $M_Z^2/\Lambda_{\text{NP}}^2 \ll 1$. According to this criterion, and after reabsorbing the trivial redefinition of the electroweak input parameters (G_F, α_{EM}, m_Z), we are left with 4 leading form factors

Adimensional form factors	Operators	Custodial	$SU(2)_L$
$\hat{S} = g^2 \Pi'_{3B}(0)$	$\mathcal{O}_{WB} = (H^\dagger \tau^a H) W_{\mu\nu}^a B_{\mu\nu} / gg'$	+	-
$\hat{T} = \frac{g^2}{M_W^2} (\Pi_{33}(0) - \Pi_{+-}(0))$	$\mathcal{O}_H = H^\dagger D_\mu H ^2$	-	-
$Y = \frac{g'^2 M_W^2}{2} \Pi''_{BB}(0)$	$\mathcal{O}_{BB} = (\partial_\rho B_{\mu\nu})^2 / 2g'^2$	+	+
$W = \frac{g^2 M_W^2}{2} \Pi''_{33}(0)$	$\mathcal{O}_{WW} = (D_\rho W_{\mu\nu}^a)^2 / 2g^2$	+	+

where we have indicated respectively with + or - the symmetries they respect or break. We have also indicated the lowest dimension effective operator involving the Higgs and vector fields associated to each form factor. As was already pointed out long ago by Grinstein and Wise [10], the 4 leading form factors parametrize the $d = 6$ effective Lagrangian for the Higgs and gauge fields. They are thus the leading terms in a double expansion in $\langle H \rangle^2 / \Lambda_{\text{NP}}^2$ and in $q^2 / \Lambda_{\text{NP}}^2$. It follows, however, from our discussion that they are the leading effects in full generality, as we did not assume we could expand in the Higgs field, and our parametrization also encompasses the generic strongly coupled Higgsless scenario. We stress that according to our criterion the quantity $U = g^2 (\Pi'_{33}(0) - \Pi'_{+-}(0))$ is expected to be $\sim \frac{m_W^2}{\Lambda_{\text{NP}}^2} \hat{T} \ll \hat{T}$ so that it can always be safely neglected. The negligibility of U is indeed a known property of technicolor models [11]. The quantities Y and W are also small in the simplest technicolor models, but they can be important in models where there is new structure in the pure gauge sector, as in models with vector boson compositeness or as in Little Higgs models. On the

Type of fit	$10^3\hat{S}$	$10^3\hat{T}$	10^3Y	10^3W
One-by-one (light Higgs)	0.0 ± 0.5	0.1 ± 0.6	0.0 ± 0.6	-0.3 ± 0.6
One-by-one (heavy Higgs)	—	2.7 ± 0.6	—	—
All together (light Higgs)	0.0 ± 1.3	0.1 ± 0.9	0.1 ± 1.2	-0.4 ± 0.8
All together (heavy Higgs)	-0.9 ± 1.3	2.0 ± 1.0	0.0 ± 1.2	-0.2 ± 0.8

Table 1: *Global fit (excluding NuTeV) of dominant form factors including them one by one or all together, with a light ($m_h = 115$ GeV) and with a heavy ($m_h = 800$ GeV) Higgs.*

other hand there exists, as expected, no motivated scenario where S, T, U is the relevant set: it is either redundant or insufficient.

Notice that by the equations of motion the operators associated to Y and W are equivalent to a given combination of \hat{S}, \hat{T} plus vertex corrections and plus four-fermion contact interactions. Two classes of observables are then affected by (\hat{S}, \hat{T}, Y, W) :

1. Z^0 pole. Corrections to $(\delta\rho|_{m_Z}, m_W, \sin^2\theta_W|_{\text{current}})$, expressed via the ϵ 's of ref.[12] as

$$\epsilon_1 = \epsilon_1^{SM} + \hat{T} - W - \tan^2\theta_W Y \quad (10)$$

$$\epsilon_2 = \epsilon_2^{SM} - W \quad (11)$$

$$\epsilon_3 = \epsilon_3^{SM} + \hat{S} - W - Y. \quad (12)$$

2. Cross-sections and asymmetries in $e\bar{e} \rightarrow f\bar{f}$ at LEP2. These mostly constrain Y and W since their effect grows faster with energy than that of \hat{S} and \hat{T} (they involve more derivatives).

Notice that Z^0 pole tests correspond to the measurement of just 3 quantities, and are thus not sufficient to constrain the general set! (As is well known, the set S, T, U would indeed be constrained by Z^0 pole data: Is this the psychological reason why this inconsistent set was so popular for so long?). Fortunately LEP2 data allow us to fully and strongly constrain the set. It is interesting that the somewhat lower precision of LEP2 (about 1% versus about 0.1% at LEP1) is compensated by the higher center of mass energy, which enhances the effect of Y and W . Other low energy observables, such as atomic parity violation and Moeller scattering, also provide extra independent constraints, but they are weaker than those provided by LEP2. The bounds from the global (basically LEP1/SLC + LEP2) fit is shown in the table: all 4 quantities are bounded at the per-mille level. The message should then be clear: LEP2 data are crucial to perform a consistent analysis of new electroweak physics.

3 ‘New’ ideas on electroweak symmetry breaking

Because of the ‘uncomputability’ of the Higgs potential, the SM, while a perfectly consistent theory, does not give a satisfactory explanation of EWSB. Perhaps roughly: the SM can parametrize EWSB but cannot explain it. Sticking to theories with an elementary Higgs field, progress necessarily involves computational control of the Higgs mass parameter. That means that m_H^2 should be protected from ultraviolet corrections. The only way we know of achieving this is by introducing extra symmetries. There are various possibilities, by now well known. Supersymmetry is surely the most widely explored one. By supersymmetry the Higgs boson H is mass degenerate with a Higgs fermion Ψ_H within the same Higgs supermultiplet. The Higgs mass m_H therefore inherits by supersymmetry the good UV property of the fermion mass: the quadratic divergence is replaced by a mild logarithmic one, and the hierarchy problem is solved. Another, perhaps less popular but interesting, possibility is to promote the Higgs to a gauge field. We know indeed that a gauge symmetry $\delta A_\mu = \partial_\mu \alpha$ forbids a mass term $m^2 A_\mu A^\mu$. In order for this to work the Higgs H should be part of a vector multiplet, which at first glance conflicts with ordinary 4-dimensional Lorentz invariance. However, the conflict is solved if there exists (at least) one extra space dimension, in which case H can be associated to the vector polarization along the new dimension: $H \sim A_5$. It is amusing that also supersymmetry can be viewed as an extra dimension, though of fermionic type. Finally another, perhaps simpler, possibility is that the Higgs H is in lowest approximation the Goldstone boson of a spontaneously broken global symmetry. This means that H basically transforms by a constant shift $H \rightarrow H + c$ under the symmetry, which forbids any H interaction that does not involve at least one derivative $\partial_\mu H$. In particular it forbids a Higgs mass term, but also, which is less exciting, the standard Yukawa interactions and the Higgs self-coupling. In fact this is a more general problem: all the symmetries I mentioned above must be broken at some level in order to give rise to realistic models. Breaking the symmetry while preserving its benefits, and also avoiding the LEP paradox, is the main challenge in model building. I will now illustrate some of these model building efforts.

3.1 The Little Higgs model

The LEP paradox is overcome if we can construct a theory where m_H , with respect to Λ_{NP} , is much smaller than eq. (1) suggests. The Little Higgs (LH) idea is to achieve this construction by making the Higgs an approximate Goldstone boson (a pseudo-Goldstone in jargon) [13]. The inspiration for that comes from low energy hadron physics, where the pions π^+ , π^0 represent the Goldstone bosons associated to the spontaneous breakdown of the chiral symmetry group $SU(2)_L \times SU(2)_R$ down to the diagonal isospin group $SU(2)_I$. The quark

masses m_q and α_{EM} explicitly break chiral symmetry by a small amount, thus giving rise to the physical but small pion masses. In particular $m_{\pi^+}^2$ receives an electromagnetic correction of order $\frac{\alpha_{EM}}{4\pi}\Lambda_{QCD}^2 \ll \Lambda_{QCD}^2$. We can try and think of an extension of the SM where the Higgs is a composite Goldstone boson associated to some new strong dynamics at a scale Λ_{Strong} . Among several others, the top Yukawa interaction (as it does not involve derivatives of the Higgs field) breaks the Goldstone symmetry explicitly. Then, replacing $\alpha_{EM} \rightarrow \alpha_t$ and $\Lambda_{QCD} \rightarrow \Lambda_{\text{Strong}}$, we generically expect, in analogy with QCD, $m_H^2 \sim \frac{\alpha_t}{4\pi}\Lambda_{\text{Strong}}^2$. Since in this case $\Lambda_{\text{NP}} \sim \Lambda_{\text{Strong}}$ this is just eq. (1), and we are back to the LEP paradox. The Little Higgs [14] is precisely a clever construction to avoid the appearance of the lowest order contribution to m_H^2 . Consider indeed the expression for the mass of a Higgs pseudo-Goldstone boson, to all order in the coupling constants

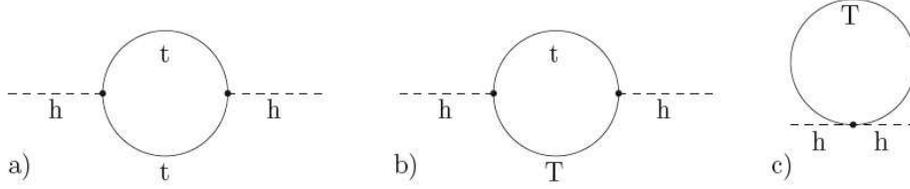
$$m_H^2 = \left(c_i \frac{\alpha_i}{4\pi} + c_{ij} \frac{\alpha_i \alpha_j}{(4\pi)^2} + \dots \right) \Lambda_{\text{Strong}}^2. \quad (13)$$

We can think of these couplings α_i as external sources that transform non-trivially under the Goldstone symmetry, thus breaking it, very much like an external electric field breaks the rotational invariance of atomic levels. As in atomic physics, the coefficients c_i, c_{ij}, \dots are controlled by the symmetry selection rules. We can then in principle think of a clever choice of symmetry group and couplings (thought of as external sources) such that the Goldstone symmetry is partially restored when any single coupling α_i vanishes. In that situation only the combined effect of at least two distinct couplings α_i and α_j can destroy the Goldstone nature of the Higgs thus contributing a mass to it. The symmetry is said to be collectively broken, $c_i = 0$ and

$$m_H^2 \sim \left(\frac{\alpha}{4\pi} \right)^2 \Lambda_{\text{Strong}}^2. \quad (14)$$

By this equation we then expect $\Lambda_{\text{Strong}} \sim 10 \text{ TeV}$, which seems to be what we need to avoid the LEP paradox.

The general symmetry structure of LH models involves a global group G_{glo} broken down to a subgroup H_{glo} with the Higgs doublet belonging to the Goldstone space $G_{\text{glo}}/H_{\text{glo}}$. Only a subgroup $G_{\text{loc}} \subset G_{\text{glo}}$ is gauged: gauge and Yukawa interactions collectively realize the explicit breaking $G_{\text{glo}} \rightarrow G_{\text{loc}}$. Therefore as a combination of spontaneous and explicit breaking only a gauge group $H_{\text{loc}} \subset H_{\text{glo}}$ survives between the fundamental scale Λ_{Strong} and the weak scale. Normally H_{loc} is just the electroweak group $G_{\text{weak}} = SU(2)_L \times U(1)_Y$. In order to realize this structure, the field content of the SM must be clearly extended, and the many different ways of achieving that define a variety of Little Higgs models. One feature of all these models is the presence of same spin partners for basically each SM field. When computing corrections to the Higgs mass, these partners enforce the selection rule $c_i = 0$ by cancelling the 1-loop quadratic divergent contribution of the corresponding SM field. For



instance, in all models the left-handed top doublet $(t, b)_L$ is extended to at least a triplet $\chi_L = (t, b, T')_L$, with T'_L an up-type $SU(2)_L$ singlet; in the right-handed sector, along with t_R and b_R , there is then a new up-type quark T'_R . The field χ_L transforms as a triplet of some $SU(3) \subset G_{\text{glo}}$. The ordinary Higgs boson arises as a (pseudo)-Goldstone from the spontaneous breaking of $SU(3)$ down to ordinary $SU(2)_L$. The triplet structure for third family fermions is a feature of the simplest models, even though G_{glo} is strictly bigger than $SU(3)$. For instance one simple model is the so-called Littlest Higgs for which $G_{\text{glo}} = SU(5)$ and $H_{\text{glo}} = SO(5)$.

The gauge group can either be extended by adding extra group factors to G_{weak} (product group models) or by embedding G_{weak} in larger simple group (simple group models). For instance, within the latter class the Simplest Little Higgs model [15] has a weak gauge group $SU(3) \times U(1)$. The simplest product group models instead, such as the $SU(5)/SO(5)$ Littlest Higgs, have gauge group $SU(2)_1 \times SU(2)_2 \times U(1)_Y$. The role of the extra charged W_H^\pm and neutral Z_H is to cancel the 1-loop correction $\delta m_H^2 \sim \frac{\alpha_W}{4\pi} \Lambda_{\text{Strong}}^2$ from SM vector bosons.

The partners of the SM states that are needed to enforce the LH mechanism naturally have a mass of order

$$m_{\text{partners}}^2 \sim \frac{\alpha}{4\pi} \Lambda_{\text{Strong}}^2 = g^2 f^2, \quad (15)$$

where I indicated by $\alpha = g^2/4\pi$ a generic coupling constant and I used the qualitative relation $\Lambda_{\text{Strong}} \sim 4\pi f$ between the strong scale and the Goldstone decay constant f (this is in analogy with the relation between strong scale and f_π in QCD). For $\Lambda_{\text{Strong}} \sim 10$ TeV, the partners then have a mass in the TeV range. Notice that the presence of these new states with intermediate mass is necessary for the LH mechanism to work.

As already said, from the viewpoint of the low energy effective theory, the partner loops cancel the leading quadratic 1-loop correction to m_H^2 . For instance in the top-quark sector the 3 diagrams in the figure add up to a quadratic correction

$$\delta m_H^2 = -\frac{3\Lambda_{\text{Strong}}^2}{8\pi^2} \left(\lambda_t^2 + \lambda_T^2 - 2\frac{\lambda_T m_T}{f} \right) = 0 \quad (16)$$

thus implying a sum rule involving the top Yukawa, the T - t mixing Yukawa, the heavy top partner mass m_T , and the Goldstone decay constant. An experimental validation of

this sum rule would be a spectacular confirmation of the LH mechanism. The cancellations among different diagrams are analogic to what happens in supersymmetry. The analogy goes indeed further, in that logarithmic divergences do not cancel, and play a role in triggering electroweak symmetry breaking. For instance in the Littlest Higgs model the t - T sector gives rise to a negative correction

$$\delta m_H^2 = -\frac{3}{8\pi^2} \lambda_t^2 m_T^2 \ln\left(\frac{\Lambda}{m_T}\right), \quad (17)$$

completely analogous to the t - \tilde{t} one in the MSSM.

Those we just described are undoubtedly attractive qualitative features for a theory of electroweak symmetry breaking. In the end, however, it is the comparison with the electroweak data that matters. In the LH models there are two classes of contributions to effective operators.

The first class is associated to the yet unknown physics at the cut-off Λ_{Strong} , at which the Higgs is composite. It necessarily gives rise to operators involving just the Higgs boson, where vector bosons appear only through covariant derivatives. For $\Lambda_{\text{Strong}} \sim 10$ TeV these effects are not in contradiction with the data. The situation would however be bad if light fermions as well were composite at Λ_{Strong} . This is because strong coupling would then demand $c_i \sim 16\pi^2$ with $\Lambda_{\text{NP}} = \Lambda_{\text{Strong}}$ for 4-fermion contact interactions in eq. (3). But with this normalization LEP2 data imply $\Lambda_{\text{Strong}} \gtrsim 50$ TeV [4]. Fortunately, fermion compositeness is not a necessary requirement of LH models, although Higgs compositeness requires some extra interactions in order to give rise to the SM Yukawa couplings.

The second class of effects is mainly associated to the intermediate mass $\sim gf \sim 1$ TeV vector bosons, W_H^\pm, Z^H, \dots . In product group models, all such effects arise from the mixing between heavy and light bosons. These models are therefore universal and all the new effects are faithfully parametrized by \hat{S}, \hat{T}, Y, W [9, 17]. Simple group models are not universal because of the new current-current interactions associated to the extended gauge structure, but the bounds are roughly the same [17, 18]. From the first analyses of electroweak data in LH models [16] to the most recent and comprehensive ones [17, 18], much work has been done. In what follows I will briefly discuss the results for product group models as studied in ref.[17]. One robust feature of these models is the contribution to \hat{S} and W ; in terms of the mass m_{W_H} and gauge coupling α_H for the new vectors, this is just

$$\hat{S} = \frac{m_W^2}{2m_{W_H}^2} \frac{1}{\sqrt{1 - \frac{\alpha_W}{\alpha_H}}}, \quad W = \frac{m_W^2}{2m_{W_H}^2} \frac{\frac{\alpha_W}{\alpha_H}}{\sqrt{1 - \frac{\alpha_W}{\alpha_H}}}, \quad (18)$$

while the contributions to \hat{T} and Y are more model-dependent. However, especially thanks to LEP2, it is possible to strongly bound the model even by treating \hat{T} and Y as free

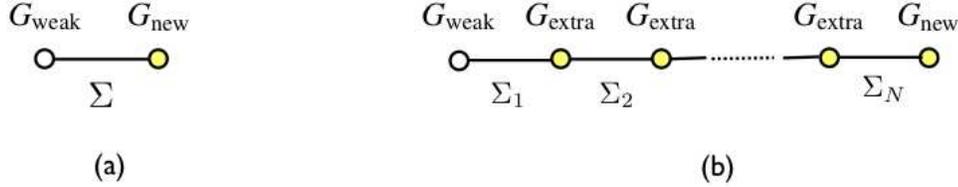
parameters. Notice that, by eq. (18), it is the intermediate scale $m_{W_H} \sim gf \sim 1 \text{ TeV}$, instead of $\Lambda_{\text{Strong}} = 4\pi f$, that plays the role of the new physics scale Λ_{NP} : we are back to the LEP paradox! In fact one may even say that the LH provides an explicit incarnation of the LEP paradox itself. By eq. (18) the bound on m_{W_H} and on f become weaker as α_H gets larger. For $\alpha_H > 0.3$ one gets (with 95% CL) $m_{W_H} > 1.2 \text{ TeV}$, by keeping \hat{T} free, and $m_{W_H} > 1.6 \text{ TeV}$ for $\hat{T} = 0$. The direct bound on m_{W_H}, α_H indirectly limits the mass of the top partner (via the bound on the LH decay constant f) roughly as

$$m_T > \frac{1}{\sqrt{\alpha_H}} \text{ TeV}. \quad (19)$$

We now see the LEP paradox in action. The Higgs mass is dominated by quantum correction $\delta m_H^2 \propto m_T^2$, and for a ‘normal’-size coupling $\alpha_H \lesssim 0.1$ we must tune the Higgs mass to at least 5% accuracy. Alternatively, tuning is minimized, if we are willing to accept a coupling $\alpha_H \sim O(1)$ on the verge of becoming strong. While it does not seem technically unacceptable to have such a large coupling at low energy, it may perhaps make things harder when trying to come up with a weakly coupled UV completion of the LH. The need for slightly extreme choices of parameters is not limited to product group models, but also holds for simple group ones, although the discussion is somewhat different [17, 18]. Notice also that, in addition to the general tension with electroweak data, specific models can have extra tuning [19], for instance in association with the Higgs quartic coupling. I do not know whether it is fair to emphasize these more specific tunings. However I think it is fair to say that for normally weak gauge couplings $\alpha_H \lesssim 0.1$ the LH is not less tuned than supersymmetry.

The basic problem involves the mixing between light and heavy vector bosons. However the cancellation of the leading quadratic correction to the Higgs mass does not rely on this mixing. In fact LH models have been constructed [20] involving an extra discrete symmetry, T-parity, with respect to which SM particles are even, while the heavy vector bosons are odd. This naturally forbids the mixing, implying $\hat{S} = W = 0$. This would be a great result, if it wasn’t that with T-parity there necessarily appear new and potentially disastrous loop corrections to 4-fermion contact terms. This is precisely what T-parity was asked to avoid! These new loop effects are tamed provided a partner for each SM fermion, including the light ones, is added with a mass around 500 GeV. This way, models with T-parity can probably be made technically less fine-tuned than models without it. T-parity is a smart idea, but it is not clear to me if the extra complications it entails are worth the effort.

In the end, even if these models are somewhat cornered by LEP data, it is only with the LHC that we will directly test them. The top partners are likely to be the lightest and most accessible states, in view of tuning considerations. T is directly produced in qb collisions via the flavour mixing vertex $W^+ \bar{T} b$. The parameters λ_T and m_T are thus extracted from the measured rate and from the reconstructed mass. The remaining parameter f , as well as



α_H , can be extracted from the Drell-Yan (DY) production and decay of the heavy vectors. Notice that the large α_H values that are favoured by low energy data suppress the coupling of W_H to light particles, thus leading to a suppression in the DY cross section. One can still conclude that, in case of a discovery up to $m_T < 2.5$ TeV and $m_{W_H} < 3$ TeV, the sum rule eq. (1) can likely be tested within 10% accuracy [21].

3.2 $H \sim A_5$ or Higgs as ‘holographic’ Goldstone boson

This is also a pretty ‘old’ idea [22, 23] on which, again, progress was made in recent years (see for instance ref. [24]) thanks to the use of new concepts such as branes, warping, deconstruction, etc. The basic remark is that when the gauge group G_{extra} breaks down to G_{weak} by some clever compactification, the extra-dimensional polarizations $A_5^\alpha, A_6^\alpha, \dots$, associated to the generators $T_\alpha \in G_{\text{extra}}/G_{\text{weak}}$, are massless at tree level. Very much as for the LH models, one can build models where $G_{\text{extra}}/G_{\text{weak}}$ contains the SM Higgs doublet. The extra dimensional gauge symmetry then forbids the presence of local contributions to the mass of such a Higgs boson, implying that all the contributions to m_H^2 must be associated to non-local, ie. finite, quantum corrections.

These models are indeed closely related to a large class of LH. These are the so-called moose models, which can be represented by diagrams where the dots indicate gauge group factors, while the links indicate scalar fields with quantum numbers under the two gauge dots they connect. A simple LH moose, depicted in figure (a), involves one extra gauge group factor G_{new} admitting $SU(2) \times U(1)$ as a subgroup. The link field Σ represents the set of Goldstone bosons associated to the breaking of the global symmetry group $G_{\text{glo}} = G_{\text{extra}} \times G_{\text{extra}}$ down to just G_{extra} . The gauge factors G_{weak} and G_{new} are embedded into each distinct G_{extra} factor of G_{glo} . The Goldstone field Σ breaks $G_{\text{weak}} \times G_{\text{new}} \rightarrow G_{\text{weak}}$, and the uneaten Goldstones $\in G_{\text{extra}}/G_{\text{new}}$ make up the Higgs doublet. Notice that this construction realizes collective symmetry breaking: in the limit of vanishing gauge coupling for any individual dot (either G_{weak} or G_{new}), Σ becomes an exact Goldstone. Now, one may imagine repeating this structure by adding N intermediate dots with gauge group $G_i \equiv G_{\text{extra}}$, linked by replicas of Σ , as shown in the figure. In the limit $N \gg 1$, this linear structure truly approximates a 5-dimensional theory, with gauge group G_{extra} , broken down

to respectively G_{weak} and G_{new} at each boundary. The scalars Σ_i play the role of $A_5(i)$, which makes the connection between $H \sim A_5$ and LH fully manifest. The moose diagram is called a *deconstruction* of the 5th dimension [25]. The Higgs mass is calculable at 1-loop, as in any LH model, but now the new states that cut-off the quadratic divergence are nicely interpreted as the Kaluza–Klein replicas of the SM fields. So we roughly have

$$m_H^2 \sim \frac{3\lambda_t^2}{16\pi^2} m_{KK}^2 + \dots \quad (20)$$

At the classical level one may think of achieving the continuum limit by sending $N \rightarrow \infty$. At the quantum level, however, that does not make sense, since 5-dimensional gauge theories have a UV cut-off Λ_{Strong} which sets a minimal length scale $1/\Lambda_{\text{Strong}}$. Indeed, studying the spectrum of the deconstructed theory one gets

$$N \sim \Lambda_{\text{Strong}}/m_{KK} \sim \Lambda_{\text{Strong}}R \quad (21)$$

so that N truly has a physical interpretation as the number of weakly coupled Kaluza–Klein resonances below the cut-off Λ_{Strong} (the KK levels are more or less equally spaced by an amount m_{KK}). The simple construction we have just sketched displays, perhaps roughly, some aspects of a more general idea, *holography*, born within string theory [26], but more and more influential in model building and phenomenology (see e.g. ref. [27]): weakly coupled 5D theories can be alternatively viewed as purely 4D theories with a large number of states N . Moreover, the more weakly coupled the 5D description (the larger Λ_{Strong}) the larger N .

Among the various realizations of $H \sim A_5$, the arguably most interesting one [28] was obtained within the Randall–Sundrum (RS) model [29]. In the RS model the 5th dimensional interval $y = [0, R]$ is warped and the metric is $ds^2 = e^{-2y/L} dx_\mu dx^\mu + dy^2$. The length L characterizes the distance along y beyond which curvature effects are important. The warp factor $e^{-y/L}$ describes the energy red-shift of any process taking place at y , relative to the same process taking place at $y = 0$. This is conceptually analogous to the relative red-shift of light emitted in a given atomic transition by atoms sitting at different heights in the gravitational field of the Earth. However, unlike on Earth, in the RS metric the curvature of space-time is large. The red-shift is then huge, and can be used to explain the Big Hierarchy problem. Indeed in the RS model the effective 4-dimensional force is mediated by a massless graviton localized near $y = 0$, and therefore the effective M_{Planck} is not red-shifted. However the lightest Kaluza-Klein states, for all fields, are localized near $y = R$ and their mass is red-shifted by a factor $e^{-R/L}$:

$$\frac{m_{KK}}{M_{\text{Planck}}} \sim e^{-R/L}. \quad (22)$$

If one succeeds in associating m_{KK} to the weak scale, then the exponential explains the Big Hierarchy for a fairly small radius $R/L \sim 35$. In the model of ref. [28] the Higgs is basically

the zero model of some components of A_5 : $H = \int_0^R A_5 dy$. Its mass, generated at 1 loop, is of the form in eq. (20) as expected in any $H \sim A_5$ construction. The peculiarity of this model is then that the calculability of m_H is combined with a solution of the Big Hierarchy problem. Unlike most LH theory, thanks to the embedding in the RS geometry, the model in ref. [28] gives a valid description of physics up to energies of the order of M_{Planck} . In this sense it can be considered a serious competitor of supersymmetry. As in supersymmetry, the extrapolation to the Planck scale is rather constraining:

- There are KK resonances for each SM particle.
- Perturbativity of the three SM gauge couplings up to the Planck scale implies $N \lesssim 10$, see eq. (21). By converse this bound implies that the coupling among KK modes is pretty strong: $g_{KK} \sim \frac{4\pi}{\sqrt{N}}$. The KK states behave like the resonances of a strongly coupled 4-dimensional field theory.
- The quark and lepton mass spectrum can be nicely explained via their localization in 5D, while implementing a GIM mechanism to suppress FCNC's [30].
- The right-handed top t_R , unlike the other SM states, strongly interacts with the KK modes. From the 4-dimensional perspective the interpretation is that t_R is composite.
- The electroweak constraints are similar to the LH as far as oblique corrections are concerned: they require about 10% tuning corresponding to a bound $m_{W_H} > 2.5 \text{ TeV}$ on the mass of the lightest vector KK mode, slightly stronger than for LH. However significantly stronger bounds are here associated to corrections to the $Zb\bar{b}$ vertex [31]. They lead to a bound of about 4 TeV on the mass of the top KK partners, thus implying a need for fine tuning at the few per cent level. These stronger bounds, unlike the more robust ones from \hat{S} , may however be a peculiarity of the specific model, and some possibilities to overcome them are outlined in ref. [31].

One last item concerns gauge unification, which in some leading, naive, approximation works very well, and in a novel way, totally alternative to what was thought so far [32]. The beta function are indeed not just modified by the addition of the contribution of new states, but also by the subtraction of the contribution of the Higgs H and the right-handed top t_R , which are by all means composite states just above the weak scale. The problem, however, is that higher order uncalculable effects are very important unless $N \sim O(1)$, which would drastically limit the overall calculability [32]. So, while the idea of unification by subtraction is new and interesting, it does not have yet a realization that can computationally compare to the fully weakly coupled supersymmetric unification.

5D models or moose models, can also be used to construct partially calculable Higgsless theories [33]. This corresponds to choosing G_{new} and its embedding in G_{extra} so that the

combined effect of the two boundaries is to break G_{extra} directly to electric charge $U(1)_Q$ (in the 1-link moose limit, diagram (a), the link field breaks $G_{\text{weak}} \times G_{\text{new}}$ to $U(1)_Q$). These models are very ambitious since, unlike in models with a Higgs field, the ratio $(m_Z/m_{W_H})^2$ is fixed in any given construction to be of order $g^2 N/16\pi^2$, and it is not tunable. This makes it harder to pass the electroweak precision tests: either small N is chosen [9], implying unacceptably strong coupling, or the simplicity of the idea must be spoiled by extra complications [34]. Moreover it is not yet clear if non-universal effects such as $Z \rightarrow b\bar{b}$ can be fully kept under control.

4 Anthropic approach to hierarchy problem(s)

The ideology underlying model building attempts, such as the ones I described so far, is that the measured parameters of the SM must be pointing toward a unique fundamental description of Nature. If that description is not perverse, any apparent tuning within the SM should not look so within the more fundamental description. Thus we must look for theories that effortlessly explain the value of the weak scale, θ -QCD, etc. The anthropic approach to physics, and to the hierarchy problems in particular, follows a different ideology, which could be based on a multiverse assumption:

- Our local universe represents but a small region of a multiverse in which some, perhaps all, physical parameters vary from region to region.

According to the multiverse assumption, the value of some physical quantities, which we so far considered a fundamental property of Nature, may instead have a purely environmental origin. One standard example of an environmental quantity is the radius of Earth's orbit around the Sun: while not fundamental, its value is pretty constrained by the prior that the Earth has a hospitable atmosphere with the presence of liquid water. The anthropic principle was for long considered powerless by the great majority, until Weinberg in 1987 [35] applied it to the cosmological constant Λ_{cosm} , thus providing a radically different viewpoint on the least understood of all hierarchy problems. Weinberg's assumed that (Structure Principle)

1. Λ_{cosm} is not a fundamental quantity.
2. The only environmental constraint on Λ_{cosm} is that it be small enough to allow the formation of galaxies.

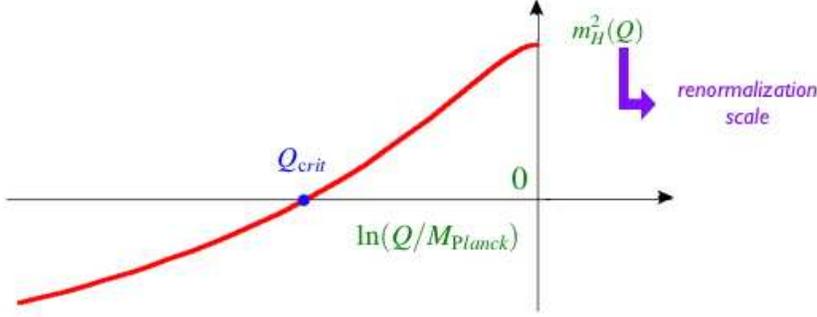
Weinberg then argued that, if the distribution of values of Λ_{cosm} is reasonably smooth, then the most natural expectation is that Λ_{cosm} be of the same order of magnitude as, or not much smaller than, the critical value Λ_c below which galaxies can form. Then, when there was still

no observational indication that $\Lambda_{\text{cosm}} \neq 0$, Weinberg predicted a likely value $\Lambda_{\text{cosm}} \sim \Lambda_c \sim 100\rho_c$, where ρ_c is the critical density for the closure of the Universe. The computation was later refined into roughly $\Lambda_c \sim 10\rho_c$ [36]. In the meanwhile the Type IA Supernovae data [37] had established the presence of a negative pressure energy density component, compatible with a cosmological constant $\Lambda_{\text{cosm}} \simeq 0.7\rho_c$. It is quite remarkable that Weinberg's logic correctly predicts, to within an order of magnitude, a mysterious quantity like Λ_{cosm} , which is otherwise apparently tuned by 120 orders of magnitude ($\Lambda_{\text{cosm}}/M_{\text{Planck}}^4 \sim 10^{-120}$).

Further to the success of the Structure Principle, the anthropic viewpoint has recently also been reinforced by advances in string theory, indicating the existence of a tremendous multitude of different vacua, forming what is called the Landscape. The universe would then be a multiverse with each different region (subuniverse) sitting at a different vacuum out in the Landscape. That and the frustration with standard approaches have stimulated the use of the anthropic viewpoint on the electroweak hierarchy problem. Ref. [38] introduced what is now called the Atomic Principle, according to which the Fermi scale is an environmental quantity whose value is nailed by the request that complex chemistry (atoms) exists. Remarkably the Atomic Principle sets an upper bound on $\langle H \rangle$, which is only about 5 times its experimental value. The Atomic Principle was later applied to the MSSM [39, 40] under the assumption that the soft terms, and thus the weak scale, are environmental quantities, and with the additional request that the lightest supersymmetric particle (LSP), a neutralino, provide the Dark Matter of the Universe. The resulting scenario, dubbed Split Supersymmetry, features superheavy (even up to 10^{13} GeV) squarks, leptons and one combination of Higgs scalars, while the charginos and the neutralinos have a mass which 'accidentally' ends up close to the weak scale in order to have the right amount of relic LSP. Remarkably, although the superspectrum is split, the successful unification of gauge couplings is maintained, as in supersymmetry that is mostly due to the contribution of Higgsinos and gauginos. Moreover the set up is rather predictive. In particular the gluino decays very slowly, via the virtual exchange of the heavy squarks, giving rise, over a significant portion of parameter space, to distinctive displaced vertex events. Split Supersymmetry has been the subject of a great amount of work in the last year. It would be fair and worthwhile to review this work, but unfortunately I do not have enough time. In the remaining part of my talk I would instead like to present a new, anthropic, viewpoint on the fine-tuning problem of the MSSM [6].

4.1 Back to Supersymmetry

Let us go back to the well known cartoon of EWSB by RG evolution in supersymmetry, shown in the figure. The Higgs mass parameter m_H^2 starts positive up at the Planck scale and is driven negative below some RG scale Q_{crit} by RG contributions, mostly due to the stops, until the running is frozen at the typical scale of sparticle masses m_{SUSY} . The physical



value of the Higgs mass is then approximatively

$$m_H^2|_{\text{phys}} = m_H^2(Q = m_{\text{SUSY}}) \quad (23)$$

Now, Q_{crit} is associated to a dimensional transmutation, and is expected to differ significantly from both m_{SUSY} and M_{Planck} . A generic expectation is $m_{\text{SUSY}} \ll Q_{\text{crit}} \ll M_{\text{Planck}}$ so that by the time the running is frozen at $Q \sim m_{\text{SUSY}}$ the Higgs mass is large and negative (cf. eq. (5))

$$m_H^2|_{\text{phys}} \sim -m_t^2 \sim -m_{\text{SUSY}}^2. \quad (24)$$

As we explained already, this is unfortunately not the situation favoured by the data. The data favour instead $-m_H^2|_{\text{phys}} \ll m_t^2$, which by direct glance at the figure is equivalent to

$$m_{\text{SUSY}} \simeq Q_{\text{crit}}. \quad (25)$$

An alternative way of phrasing the fine-tuning problem of supersymmetry then is to ask: Why should two totally unrelated parameters like m_{SUSY} and Q_{crit} almost coincide? Given the present constraints, if Supersymmetry is discovered at the LHC, we will almost certainly have to ask ourselves this question. Let me try and give an answer right now.

Let us assume that the overall SUSY mass scale m_{SUSY} is environmental. More precisely, let us assume that up at the Planck scale the various soft parameters are given by

$$m_i = c_i m_{\text{SUSY}}, \quad (26)$$

with the c_i fixed everywhere throughout the multiverse, while m_{SUSY} varies. Let us also assume that all the other dimensionless gauge and Yukawa couplings are fixed at the Planck scale. Notice that under these conditions Q_{crit} is also fixed, as it depends only on M_{Planck} , c_i , and the other dimensionless couplings, but not on m_{SUSY} . Two possibilities for the patch of Universe we live in are then given

1. $m_{\text{SUSY}} > Q_{\text{crit}}$, in which case $m_H^2|_{\text{phys}} > 0$, implying $\langle H \rangle = 0$.

2. $m_{\text{SUSY}} < Q_{\text{crit}}$, in which case $m_H^2|_{\text{phys}} < 0$, implying $\langle H \rangle \neq 0$.

It is pretty clear we do not live in region 1, and in fact it is not even sure if in region 1 there can exist anyone to ask this question [38, 41]. Now, compatibly with the prior that we must live in region 2, what is the most likely value we expect m_{SUSY} to have? The problem is phrased in complete analogy with Weinberg's approach to the cosmological constant, with $\langle H \rangle \neq 0$ replacing the datum that galaxies exist. Then, under the assumption that the distribution of m_{SUSY} is reasonably flat and featureless, and, which is quite likely, not peaked at $m_{\text{SUSY}} = 0$, we expect $m_{\text{SUSY}} \sim Q_{\text{crit}}$. A small Higgs mass parameter is then obtained through the brief running from Q_{crit} to m_{SUSY}

$$\frac{m_H^2|_{\text{phys}}}{m_{\tilde{t}}^2} \sim \frac{3\lambda_t^2}{2\pi^2} \ln(m_{\text{SUSY}}/Q_{\text{crit}}) \sim -\frac{3\lambda_t^2}{2\pi^2} \ll 1. \quad (27)$$

To be more precise let me assume the number $N(m)$ of vacua with $m_{\text{SUSY}} < m$ grows like m^n . The prior $m_{\text{SUSY}} < Q_{\text{crit}}$ leads to a conditional probability giving the average $\langle \ln(m_{\text{SUSY}}/Q_{\text{crit}}) \rangle \sim -1/n$, so that the expectation is

$$\frac{m_H^2|_{\text{phys}}}{m_{\tilde{t}}^2} \sim -\frac{3\lambda_t^2}{2\pi^2} \times \frac{1}{n}. \quad (28)$$

Notice that the loop factor $3\lambda_t^2/2\pi^2 \sim 0.15$, while it helps to explain the little hierarchy problem in supersymmetry, falls short to explain it completely. Indeed one can imagine field theoretic landscapes [6] where n is somewhat bigger than 1, say $O(\text{a few})$ but not much bigger (For instance if there are $O(10^{500})$ vacua, as perhaps suggested by string theory, and if m_{SUSY} can range up to M_{Planck} , then $n \lesssim 30$). So it is reasonable for the ratio in eq. (28) to be between 0.01 and 0.1 but not much smaller, thus providing an argument why supersymmetry should be elusive at LEP but not at the LHC. Of course there has been a price to pay. Supersymmetry looks tuned because throughout the Landscape it is much more likely to be in the region with $\langle H \rangle = 0$ than in the region $\langle H \rangle \neq 0$: the most likely points with $\langle H \rangle \neq 0$ are then close to the boundary of the two regions, where a little hierarchy is present.

Now, what does one do with an argument like the above? Can it be falsified? It certainly can. It predicts that m_H^2 will cross zero immediately above the supersymmetric threshold as we run the soft parameters up in energy. Now, although less typical, or even more tuned, there are choices of parameters where this does not happen, for instance when the beta function for m_H has a zero at the weak scale. Such values of the soft masses would rule out this scenario (although it would probably be hard, given the precision with which masses are measured at the LHC, to quickly reach a conclusion). Another situation that would rule out this scenario is that in which m_H^2 becomes negative at some high RG scale, as it would

happen in small deformations of gaugino mediation. In the end, is the possibility to falsify this scenario so exciting? Probably not, as, if supersymmetry is discovered, it will very likely look like that. I think the main lesson is that fine-tuning in supersymmetry, once we discover it, could be telling us something fundamental about the statistics of vacua and the nature of soft terms up at the Planck scale.

5 Summary

In recent years there have been many new proposals of calculable electroweak symmetry breaking, all trying to account for the baffling absence of new signals at LEP/SLC. In practically all the examples there are two separate energy scales

- $\Lambda_{\text{NP}} \sim 1 \text{ TeV}$, at which lay particles that regulate the Higgs mass divergence.
- $\Lambda_{\text{Strong}} \sim 10 \text{ TeV}$, which describes the underlying new (strong) dynamics.

In all the models there exists already some tension with electroweak precision tests mostly as a consequence of the need for states at a relatively low scale $\Lambda_{\text{NP}} \sim 1 \text{ TeV}$. In fact it is fair to say that models such as the Little Higgs or the Holographic Goldstone boson are explicit incarnations of the LEP paradox. The tension is not dramatic yet and can be relaxed at the price of some extra complications (large gauge couplings or T -parity in Little Higgs models), so perhaps one should not worry too much. After all the LHC will directly test, in many of these models, a sizeable portion of the parameter space, which is not constrained even indirectly by LEP. In particular the LHC will test the lower layer structure up to $\Lambda_{\text{NP}} \sim 3 \text{ TeV}$. The comparison of these new approaches to SUSY is a fair exercise. But one should be careful not to compare apples and oranges. Supersymmetry provides a weakly coupled calculable description for physics up to the Planck scale. The extrapolation is rather constraining and thus accounts for a good portion of the tuning that is needed in the MSSM. If we set ourselves the less ambitious goal of finding a theory of electroweak symmetry breaking valid only to slightly above the weak scale as is done in most Little Higgs models, then supersymmetry would look less tuned. The 5D supersymmetric model presented in Ref. [42] is an illustration of that possibility. On the other hand the holographic Higgs Goldstone model [28] can be extrapolated up to the Planck scale, which makes it fully comparable to the MSSM, and also very constrained [31]! More concretely, perhaps, the new models compare reasonably well with supersymmetry as Dark Matter is concerned. But this is largely due to the fact that any stable relic with weak scale annihilation cross-section is a potentially good Dark Matter candidate. In the models at hand the stability of the relic follows from a discrete symmetry, for instance T -parity in LH or KK parity in the 5D models, precisely as it follows from R -parity in supersymmetry. On the other hand, the

neatness of gauge unification in supersymmetry is in my opinion not matched by any of the new models, although new intriguing twists have emerged [32].

The biggest novelty of the last year is however that the anthropic principle has finally made it to the gauge hierarchy problem. Weinberg's impressive anthropic explanation of the size of the cosmological constant, together with the lack of a fully natural theory of electroweak symmetry breaking, is perhaps a serious indication that we do live in a multiverse of vacua. How do we proceed if that is the case? We can certainly toy with the Landscape and try to come up with alternative solutions to the problems of particle physics. In this respect I illustrated a new viewpoint on the supersymmetric fine-tuning problem. With Split Supersymmetry the anthropic approach has even materialized into a cleverly predictive model. However I find it worrisome that with the anthropic approach we are working with assumptions that are very hard, probably impossible, to test. The multiverse theory may become the greatest revolution after Copernicus, but will we ever test it?

Luckily a less speculative era will start in a couple of years, as the LHC will start to unravel under our eyes the riddle of the weak scale.

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References

- [1] R. Barbieri and A. Strumia, arXiv:hep-ph/0007265.
- [2] S. de Jong, these proceedings, arXiv:hep-ex/0512043.
- [3] W. Buchmuller and D. Wyler, Nucl. Phys. B **268** 621 (1986).
- [4] R. Barbieri and A. Strumia, Phys. Lett. B **462**, 144 (1999).
- [5] A. Romanino, private communication.
- [6] N. Arkani-Hamed, G.F. Giudice, R. Rattazzi, paper in preparation.
- [7] M. Bastero-Gil, C. Hugonie, S. F. King, D. P. Roy and S. Vempati, Phys. Lett. B **489**, 359 (2000).
- [8] M. E. Peskin and T. Takeuchi, Phys. Rev. Lett. 65 964 (1990); M. Golden and L. Randall, Nucl. Phys. B361 3 (1990); B. Holdom and J. Terning, Phys. Lett. B247 88 (1990).

- [9] R. Barbieri, A. Pomarol, R. Rattazzi and A. Strumia, Nucl. Phys. B **703**, 127 (2004).
- [10] B. Grinstein and M. B. Wise, Phys. Lett. B **265** 326 (1991).
- [11] M. E. Peskin and T. Takeuchi, Phys. Rev. D **46** 381 (1992) .
- [12] G. Altarelli and R. Barbieri, Phys. Lett. B **253** 161 (1991).
- [13] D. B. Kaplan and H. Georgi, Phys. Lett. B **136**, 183 (1984).
- [14] N. Arkani-Hamed, A. Cohen and H. Georgi, Phys. Lett. B **513** 232 (2001); N. Arkani-Hamed, A. Cohen, E. Katz and A. Nelson, JHEP **07** 034 (2002); N. Arkani-Hamed, A. G. Cohen, E. Katz, A. E. Nelson, T. Gregoire and J. G. Wacker, JHEP **0208** 021 (2002); for a nice review see M. Schmaltz and D. Tucker-Smith, arXiv:hep-ph/0502182.
- [15] M. Schmaltz, JHEP **0408**, 056 (2004).
- [16] C. Csaki, J. Hubisz, G. D. Kribs, P. Meade and J. Terning, Phys. Rev. D **67**, 115002 (2003).
- [17] G. Marandella, C. Schappacher and A. Strumia, Phys. Rev. D **72** 035014 (2005).
- [18] Z. Han and W. Skiba, Phys. Rev. D **72** 035005 (2005).
- [19] J. A. Casas, J. R. Espinosa and I. Hidalgo, JHEP **0503**, 038 (2005).
- [20] H. C. Cheng and I. Low, JHEP **0408**, 061 (2004); I. Low, JHEP **0410**, 067 (2004).
- [21] M. Perelstein, M. E. Peskin and A. Pierce, Phys. Rev. D **69**, 075002 (2004); T. Han, H. E. Logan and L. T. Wang, arXiv:hep-ph/0506313.
- [22] N. S. Manton, Nucl. Phys. B **158** (1979) 141; D. B. Fairlie, Phys. Lett. B **82** 97 (1979).
- [23] Y. Hosotani, Ann. Phys. **190** 285 (1989).
- [24] H. Hatanaka, T. Inami and C. S. Lim, Mod. Phys. Lett. A **13**, 2601 (1998); G. R. Dvali, S. Randjbar-Daemi and R. Tabbash, Phys. Rev. D **65**, 064021 (2002); I. Antoniadis, K. Benakli and M. Quiros, New J. Phys. **3**, 20 (2001); C. Csaki, C. Grojean and H. Murayama, Phys. Rev. D **67**, 085012 (2003); C. A. Scrucca, M. Serone and L. Silvestrini, Nucl. Phys. B **669**, 128 (2003).
- [25] N. Arkani-Hamed, A. G. Cohen and H. Georgi, Phys. Rev. Lett. **86**, 4757 (2001); H. C. Cheng, C. T. Hill, S. Pokorski and J. Wang, Phys. Rev. D **64**, 065007 (2001).

- [26] J. Maldacena, *Adv. Theor. Math. Phys.* **2** 231 (1998).
- [27] T. Gherghetta, arXiv:hep-ph/0601213.
- [28] K. Agashe, R. Contino and A. Pomarol, *Nucl. Phys. B* **719**, 165 (2005); R. Contino, Y. Nomura and A. Pomarol, *Nucl. Phys. B* **671**, 148 (2003).
- [29] L. Randall and R. Sundrum, *Phys. Rev. Lett.* **83**, 3370 (1999).
- [30] Y. Grossman and M. Neubert, *Phys. Lett. B* **474**, 361 (2000); T. Gherghetta and A. Pomarol, *Nucl. Phys. B* **586**, 141 (2000); S. J. Huber and Q. Shafi, *Phys. Lett. B* **498**, 256 (2001).
- [31] K. Agashe and R. Contino, arXiv:hep-ph/0510164.
- [32] K. Agashe, R. Contino and R. Sundrum, *Phys. Rev. Lett.* **95**, 171804 (2005).
- [33] C. Csaki, C. Grojean, H. Murayama, L. Pilo and J. Terning, *Phys. Rev. D* **69**, 055006 (2004).
- [34] G. Cacciapaglia, C. Csaki, C. Grojean, M. Reece and J. Terning, *Phys. Rev. D* **72**, 095018 (2005)
- [35] S. Weinberg, *Phys. Rev. Lett.* **59**, 2607 (1987).
- [36] H. Martel, P. R. Shapiro and S. Weinberg, *Astrophys. J.* **492**, 29 (1998).
- [37] A. G. Riess *et al.* [Supernova Search Team Collaboration], *Astron. J.* **116**, 1009 (1998); S. Perlmutter *et al.* [Supernova Cosmology Project Collaboration], *Astrophys. J.* **517**, 565 (1999).
- [38] V. Agrawal, S. M. Barr, J. F. Donoghue and D. Seckel, *Phys. Rev. D* **57**, 5480 (1998).
- [39] N. Arkani-Hamed and S. Dimopoulos, *JHEP* **0506** 073 (2005).
- [40] G. F. Giudice and A. Romanino, *Nucl. Phys. B* **699**, 65 (2004) [Erratum-ibid. *B* **706**, 65 (2005)]; N. Arkani-Hamed, S. Dimopoulos, G. F. Giudice and A. Romanino, *Nucl. Phys. B* **709**, 3 (2005).
- [41] N. Arkani-Hamed, S. Dimopoulos and S. Kachru, arXiv:hep-th/0501082.
- [42] R. Barbieri, L. J. Hall, G. Marandella, Y. Nomura, T. Okui, S. J. Oliver and M. Papucci, *Nucl. Phys. B* **663**, 141 (2003).