

>Geochemical and hydrological model for bauxite residue sand. >Combined hydrogeochemical simulation of bauxite residue sand under field conditions, in 2D, heterogeneous domain.
>Evaluation of management practise for the amelioration of bauxite residue sand as substrate for plant growth.

This manuscript illustrates an innovative application of detailed hydrogeochemical modelling to the field of bauxite residue management. A recently developed simulation tool that combines geochemical reaction calculations in PHREEQC with variably saturated flow and transport processes in COMSOL was employed to investigate the evolution of water availability and water quality in fertigated and amended bauxite residue sand as response to rainfall leaching. The level of detail in flow and reactions calculations is novel to studies of residue management and rehabilitation. Due to the general applicability, the employed simulation and parameterization techniques are of interest to a broad audience in the field of mining waste management.

Predictive Hydrogeochemical Modelling of Bauxite Residue Sand in Field Conditions

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1 **Abstract**

2 The suitability of residue sand (the coarse fraction remaining from Bayer's process of bauxite
3 refining) for constructing the surface cover of closed bauxite residue storage areas was
4 investigated. Specifically, its properties as a medium for plant growth are of interest to ensure
5 residue sand can support a sustainable ecosystem following site closure. The geochemical
6 evolution of the residue sand under field conditions, its plant nutrient status and soil moisture
7 retention were studied by integrated modelling of geochemical and hydrological processes.
8 For the parameterization of mineral reactions, amounts and reaction kinetics of the mineral
9 phases natron, calcite, tricalcium aluminate, sodalite, muscovite and analcime were derived
10 from measured acid neutralization curves. The effective exchange capacity for ion adsorption
11 was measured using three independent exchange methods. The geochemical model, which
12 accounts for mineral reactions, cation exchange and activity corrected solution speciation,
13 was formulated in the geochemical modelling framework PHREEQC, and partially validated
14 in a saturated flow column experiment. For the integration of variably saturated flow with
15 multi-component solute transport in heterogeneous 2D domains, a coupling of PHREEQC
16 with the multi-purpose finite-element solver COMSOL was established. The integrated
17 hydrogeochemical model was applied to predict water availability and quality in a vertical
18 flow lysimeter and a cover design for a storage facility using measured time series of rainfall
19 and evaporation from southwest Western Australia. In both scenarios the sand was fertigated
20 and gypsum-amended. Results show poor long-term retention of fertilizer ions and buffering
21 of the pH around 10 for more than 5 years of leaching. It was concluded that fertigation,
22 gypsum amendment and rainfall leaching alone were insufficient to render the geochemical
23 conditions of residue sand suitable for optimal plant growth within the given timeframe. The
24 surface cover simulation demonstrates that the soil moisture status in the residue sand can be

25 ameliorated by an appropriate design of the cover layer with respect to thickness, slope and
26 distance between lateral drains.

27 **Keywords**

28 bauxite refining residue, geochemical modelling, PHREEQC, IPhreeqc, COMSOL, PEST,
29 mineral reactions, cation exchange, vadose zone, variable saturation, revegetation, waste
30 management

31 **1 Introduction**

32 The worldwide production of alumina (83.3 Mt in 2008 [1]) is associated with the creation of
33 about 120 Mt of problematic bauxite refining residues each year [2]. In Western Australia,
34 where about a third of the alumina on the global market is produced [3], the residue is
35 disposed of in large impoundments close to the refineries, where it is left to drain and air-dry
36 (dry-stacking) [4, 5]. In anticipation of future storage capacity limits, the bauxite refining
37 industry seeks safe and economically feasible strategies of sustainable storage site closure.
38 Important objectives for successful closure are [6-11]

- 39 • reduction of infiltration into the underlying residue;
- 40 • dust control;
- 41 • erosion control;
- 42 • minimization of the need for future reworking; and,
- 43 • limitation of the visual obtrusiveness.

44 These objectives could be achieved by a self-sustaining vegetation cover on top of residue
45 storage areas. Since the reuse of residue sand (the coarse fraction of the residue; characteristic
46 grain size $> 10^{-4}$ m) as a medium for plant growth would greatly reduce the costs of
47 revegetation, research into its suitability as a substrate has been recently intensified.

48 However, plant productivity on residue sand is impeded by the geochemical conditions that
49 reactions of highly unstable minerals impose on the soil solution [12]. Characteristic
50 properties of the residue sand are [7, 11, 13-15]:

- 51 • high pH (10-12.5);
- 52 • high total alkalinity (ca. 20 meq l⁻¹);
- 53 • high electrical conductivity (ca. 1500 μ S cm⁻¹); and,
- 54 • high exchangeable sodium percentage (close to 100%).

55 Besides the general geochemical conditions, the plant nutrient status in the residue sand plays
56 a critical role for the long-term revegetation success [8, 12, 15]. Chen et al. [16, 17] therefore
57 investigated the retention of major nutrients in residue sand after additions of a standard
58 ammonium-phosphate fertilizer. In [17], they specifically focused on the loss of ammonia
59 (NH_3) due to volatilization. Fractionation and availability of micronutrients such as B, Cu,
60 Fe, Mn and Zn in residue sand was examined by Thiyagarajan et al. [10]. Motivated by the
61 observed Mn deficiency of plants on residue sand, Gherardi and Rengel [13] investigated the
62 detailed fractionation of this essential nutrient. Phillips and Chen [14] studied ion adsorption
63 onto variable charge adsorption sites as the main fractionating process for micronutrients.

64 To date the interference on adsorption sites of fertilizer retention and mineral dissolution
65 reactions as result of ion competition remains unclear. More importantly, the influence of soil
66 moisture dynamics and solute transport on the geochemical factors that determine sand
67 fertility in field conditions is largely unknown. Under natural leaching conditions, imposed
68 by rainfall and evaporation, geochemical processes of ion adsorption and mineral dissolution
69 are controlled by variably saturated soil moisture movement and influenced by changes in
70 local ion concentrations due to solute transport [18-21]. Therefore, flow and transport are
71 crucial components in the assessment of the long-term efficiency of management strategies,
72 such as fertilizer addition or gypsum amendment [22-24]. Besides its importance for ion
73 transport and solution reactivity, water availability plays a key role in residue sand fertility.

74 Integrated hydrogeochemical modelling is a powerful tool to investigate simultaneous
75 geochemical reactions, such as mineral reactions and ion adsorption, considering their
76 dependency on soil moisture dynamics and solute transport [25-28]. Here, we present the first
77 interdisciplinary modelling of bauxite refining residue sand by combining geochemical
78 reactions with rainfall- and evaporation-induced variably saturated flow in 2D heterogeneous
79 domains. The objectives are (1) to develop and parameterise submodels for the geochemical

80 and hydrological processes in residue sand, and (2) to predict the long-term effect of
81 fertilization and gypsum amendment on residue sand fertility in field conditions through
82 integrated hydrogeochemical modelling.

83 The paper is structured as follows: A geochemical model for residue sand is established in
84 Section 2. Mineral reactions are derived from measured acid neutralization curves in
85 combination with speciation modelling and linked parameter optimization. Ion adsorption is
86 considered by a cation exchange process using independent measurements to determine the
87 effective exchange capacity. The model is formulated in the geochemical modelling
88 framework PHREEQC [29] and is partially validated against results from saturated-flow
89 column experiments. Section 3 presents the hydraulic properties of residue sand with
90 relevance to hydrological modelling. The software for coupled simulations of geochemistry
91 and unsaturated hydrological processes is described briefly in Section 4. Details of novel
92 model features and the implementation of atmospheric boundary conditions are provided in
93 Appendices A-C. Section 5 describes the meteorological conditions at ALCOA's Pinjarra
94 Alumina Refinery in south-west Western Australia where the model is applied. Results from
95 predictive simulations of a constructed lysimeter and a surface cover design for residue
96 storage areas are presented in Sections 6 and 7. The main model uncertainties are discussed in
97 Section 8 together with implications for residue management. Conclusions with respect to the
98 fertilizer addition and gypsum amendment as well as the overall suitability of residue sand as
99 a plant growth substrate are drawn in Section 9.

100 2 Geochemical Model

101 2.1 Solid Phase Properties

102 The geochemistry of fresh, untreated residue sand is dominated by dissolution of readily
103 soluble salts and minerals [e.g., 30]. In order to simulate the geochemical conditions as a
104 response to fertigation, gypsum amendment and rainfall leaching, detailed knowledge of the
105 stoichiometry, quantity and reactivity of the soluble minerals is required. Taylor and Pearson
106 [31] found 58% quartz, 22% hematite, 7% gibbsite, 5% goethite, 1% anatase, 1% muscovite
107 and 0.3% boehmite as the major mineral fractions in residue sand. Because of their low
108 solubility and/or slow reactions kinetics, these major mineral fractions contribute little to the
109 overall geochemical conditions in the soil solution. Instead, highly reactive salts such as
110 natron ($\text{Na}_2\text{CO}_3 \cdot 10\text{H}_2\text{O}$), calcite (CaCO_3), tricalcium aluminate (TCA; $\text{Ca}_3\text{Al}_2\text{O}_6$) [32-34]
111 and the desilication product (DSP; e.g., sodalite $\text{Na}_8(\text{AlSiO}_4)_6\text{Cl}_2$) [15, 35-40] are responsible
112 for the high pH and large acid neutralization capacity of the bauxite residue [30, 41].
113 Although identified qualitatively by XRD [30], the proportions of these minerals in residue
114 sand is currently unknown.

115 For the parameterization of the geochemical model, the reactive mineral proportions were
116 found by matching measured acid neutralization curves with simulations performed in
117 PHREEQC. In this approach, the solution pH was regarded as a master variable and an
118 integrated measure for the overall geochemical conditions [42]. Similar to the procedure used
119 by Snars and Gilkes [30], buffering plateaus are associated with the dissolution of distinct
120 mineral phases and the persistence of buffering regions is related to the amount of the
121 minerals in the mineral assembly.

122 Acid neutralization was measured over the pH range of 2 – 12. 30 g of residue sand ($\phi < 2$
123 mm, oven-dried for > 2 d at 50°C) were placed into a series of 20 polystyrol screw-lid

124 beakers (190 ml, Semadeni). A 0.5 M HCl solution was added to the beakers in quantities
125 ranging from 0 to 14.25 ml in steps of 0.75 ml. The beakers were made up to volume using
126 Milli-Q deionised water to achieve a liquid to solid ratio of 5:1 by weight. Samples were
127 thoroughly mixed (20 rpm) using an end-over-end shaker. Excessive gas phase equilibration
128 was avoided by reducing the empty volume in each beaker to ca. 20 ml. The pH of each
129 suspension was recorded 2, 4, 24, 48, 72 and 96 h after acid addition using a robotic
130 titrosampler (Metrohm 855) with a platinum electrode (Metrohm 6.0257.000 Aquatrode
131 Plus).

132 **Fig. 1: Measured (a) and simulated acid neutralization curves at thermodynamic equilibrium (b) and including the**
133 **kinetic dissolution of TCA and sodalite (c).**

134 Acid neutralization curves show distinct buffering plateaus at pH 7 and pH 4 and a less
135 pronounced buffering region around pH 9-10 (Fig. 1a). Over time, acid consumption
136 increased due to kinetic mineral dissolution, giving the impression of a moving pH front.
137 After 72 h, the pH stabilised, suggesting that readily soluble alkalinity was consumed and that
138 fast kinetic reactions attained quasi-equilibrium. The extent of further buffering due to slowly
139 reacting minerals remains uncertain. However, over the time scale examined, the acid
140 neutralisation curves provide reliable information on the effects of acid on the geochemical
141 behaviour of residue sand.

142 In the first step of the model development, the acid neutralization at 2 h was reproduced by
143 simulating the solution in equilibrium with the fast reacting minerals natron, calcite,
144 muscovite and analcime. The latter two minerals provide buffering around pH 4 and are
145 therefore of minor importance under conditions typically observed for residue sand deposited
146 in the field ($\text{pH} > 7$). The quantity of natron and calcite were optimized to match the
147 measured acid neutralization curve through coupling PHREEQC with the model-independent
148 parameter estimation software PEST (version 12) [43]. The second step in model

149 development introduced the minerals TCA and sodalite, whose quantities were optimised in
 150 PHREEQC to reproduce the acid neutralisation curve observed after 96 h of reaction time.
 151 The mineral sodalite was included as a surrogate to represent the variety of components in the
 152 desilication product [44]. Similarly, TCA represents the mineral group of calcium aluminates.
 153 Since the buffering capacity around pH 4 was not exhausted during the experiment, the
 154 amount of muscovite was estimated from the mineralogical data of Taylor and Pearson [31]
 155 given above. The amount of sodium (Na) in fresh residue sand that is not accounted for by
 156 natron and sodalite was attributed to analcime. Reactive Na as measured by leach testing over
 157 a range of pH from 0.8 to 11.8 (data not shown) amounts to $5.415 \times 10^{-3} \text{ g g}^{-1}$. Measured and
 158 simulated acid neutralization curves at 2 and 96 h are presented in Fig. 1b. In a third step of
 159 model development, acid neutralization between 2 and 96 h was attributed to kinetic
 160 dissolution of TCA and sodalite. In agreement with transition state theory [e.g., 45], the rate
 161 expression

$$s_i \frac{dm_i}{dt} = k (1 - \Omega) A \left(\frac{M}{M_0} \right)^{\frac{2}{3}}, \quad (1)$$

162 given by the PHREEQC manual [29] was employed. In Eq. (1), s_i is the stoichiometric factor
 163 of component i in the mineral phase, m_i is the quantity of component i in the liquid phase
 164 (mol), k is the rate constant ($\text{mol m}^{-2} \text{ s}^{-1}$), Ω is the saturation ratio and A is the mineral surface
 165 area (m^2). The factor $\left(\frac{M}{M_0} \right)^{\frac{2}{3}}$ accounts for the change in mineral surface with dissolution
 166 progress for spherical mineral grains, where M is the current amount of mineral (mol) and M_0
 167 is the initial amount of mineral (mol). The saturation ratio Ω is defined by

$$\Omega = \frac{\prod a_i^{s_i}}{K}, \quad (2)$$

168 where a_i is the activity of component i and K is the equilibrium constant of the
 169 dissolution/precipitation reaction. The reactive surface area A of the mineral phases was set
 170 equal to the total surface area of residue sand. The total surface area ($2.708 \times 10^{-2} \text{ m}^2 \text{ g}^{-1}$) was
 171 calculated from laser diffraction particle analysis (LSTM 13 320, Beckman Coulter) assuming
 172 spherical particles (see Appendix D). The rate constant k and the initial amount M_0 were
 173 estimated by matching all measured acid neutralization curves at all time periods between 2
 174 and 96 h of reaction by the coupling of PHREEQC and PEST (Fig. 1c). The derived mineral
 175 properties for subsequent modelling are summarized in Table 1.

176 **Table 1: Mineral properties of residue sand as derived from acid neutralization.**

Mineral name Reaction formula	Equilibriu m constant	Rate constant ($\text{mol m}^{-2} \text{ s}^{-1}$)	Relative amount (mol $\text{kg}_{\text{solid}}^{-1}$)
Calcite $\text{CaCO}_3 = \text{CO}_3^{-2} + \text{Ca}^{+2}$	$10^{-8.48 \text{ a}}$	-	2.531×10^{-2}
Natron $\text{Na}_2\text{CO}_3 \cdot 10\text{H}_2\text{O} = 2\text{Na}^+ + \text{CO}_3^{-2} + 10\text{H}_2\text{O}$	$10^{-1.311 \text{ a}}$	-	3.991×10^{-2}
Muscovite $\text{KAl}_3\text{Si}_3\text{O}_{10}(\text{OH})_2 + 10\text{H}^+ = \text{K}^+ + 3\text{Al}^{+3} + 3\text{H}_4\text{SiO}_4$	$10^{14 \text{ b}}$	-	2.511×10^{-2}
Analcime $\text{NaAlSi}_2\text{O}_6 \cdot \text{H}_2\text{O} + \text{H}_2\text{O} + 4\text{H}^+ = \text{Na}^+ + \text{Al}^{+3} + 2\text{H}_4\text{SiO}_4$	$10^{6.719 \text{ a}}$	-	3.054×10^{-2}
Sodalite $\text{Na}_8(\text{AlSiO}_4)_6\text{Cl}_2 + 24\text{H}_2\text{O} = 8\text{Na}^+ + 6\text{Al}(\text{OH})_4^- + 6\text{H}_4\text{SiO}_4 + 2\text{Cl}^-$	$10^{-55.89 \text{ c}}$	3.405×10^{-9}	4.237×10^{-3}
TCA $\text{Ca}_3\text{Al}_2\text{O}_6 + 12\text{H}^+ = 3\text{Ca}^{+2} + 2\text{Al}^{+3} + 6\text{H}_2\text{O}$	$10^{74 \text{ d}}$	7.484×10^{-10}	5.569×10^{-3}

177 ^a minteq.dat (distributed with PHREEQC), ^b sit.dat (distributed with PHREEQC), ^c calculated from
 178 thermodynamic data in Komada et al. [46], ^d Khaitan et al. [34]

179 The results in Fig. 1b show excellent agreement between the simulated and measured acid
 180 neutralization curves after 2 h using the fast reacting minerals natron and calcite to represent

181 the buffering regions at pH 7 and around pH 10. The correlation coefficient according to
182 Cooley and Naff [47] amounts to 0.995. The measured decline in pH with the addition of 2
183 mmol HCl as well as the exhaustion of the buffering capacity after addition of 7 mmol HCl is
184 well reproduced. However, the pH is overestimated by about one pH unit in the strongly
185 alkaline region (pH > 9), whereas it is slightly underestimated for the addition of 2-7 mmol
186 acid. This is reflected also by the lower correlation coefficient of 0.973. The simulation of
187 kinetic pH buffering in Fig. 1c, with an overall correlation coefficient of 0.982, shows that
188 simple rate expressions are sufficient to produce reasonable agreement of this time-dependent
189 process. Since the field pH remains always in the alkaline range, the mismatch between
190 measured and simulated pH below 7 is of lower importance.

191 2.2 Adsorption Properties

192 The adsorption of fertilizers as result of cation exchange is critical to the understanding of
193 nutrient retention , which is crucial for plant growth. The effective cation exchange capacity
194 (CEC) of residue was measured using three independent methods: (i) the method of Ca-Mg
195 exchange for soils containing salts, carbonates and zeolites [48], (ii) the unbuffered salt
196 extraction method at field pH [modified after 49, in 50], and (iii) the cobalt hexamine
197 compulsive exchange method [51]. Measurements were taken from three replicates using
198 each method.

199 Prior to testing, the residue sand was washed to avoid errors due to the dissolution of readily
200 soluble salts. 40 g of oven-dried sand (50°C, > 2 d, $\phi < 0.5$ mm) were weighed into a 250 ml
201 Nalgene bottle, after which 200 ml of water (Milli-Q) was added to achieve a liquid to solid
202 ratio of 5:1. The bottles were shaken end-over-end for 1 h and centrifuged at 2×10^3 rpm for
203 30 min. The clear supernatant was manually decanted and care was taken not to lose any of
204 the fine material that deposited as a red layer on top of the coarse sand. Subsequently, the

205 bottles were made up to volume. The washing procedure was repeated 10 times, during which
206 the electrical conductivity decreased from 1513 $\mu\text{S cm}^{-1}$ to 53 $\mu\text{S cm}^{-1}$ indicating the removal
207 of the most soluble mineral fractions [52].

208 **Table 2: Cation exchange capacity on washed residue sand.**

Method	CEC ($\text{cmol kg}_{\text{solid}}^{-1}$)
(i): Ca-Mg	0.66
(ii): NH_4 -K	1.21
(iii): $\text{Co}(\text{NH}_3)_6\text{Cl}_3$	0.72

209 Each of the three methods yielded CEC values of the same order of magnitude (Table 2).
210 However, the value from the NH_4 -K exchange method was about twice as high as results
211 from the other two methods. The Ca-Mg exchange method and the cobalt hexamine method
212 lower the native pH of the residue sand. This may decrease the number of pH-dependent
213 surface sites, which could explain the lower measured exchange capacity. In the following
214 model applications the arithmetic mean of all three methods (CEC: $0.86 \text{ cmol kg}_{\text{solid}}^{-1}$) was
215 used as the effective exchange capacity of residue sand. For the definition of ion association
216 reactions, PHREEQC's default database *phreeqc.dat* was employed.

217 2.3 Column Study for Model Validation

218 Before modelling fertiliser transport under field conditions, the model representation of
219 geochemical processes under controlled laboratory conditions was evaluated. A column
220 leaching experiment in saturated upward flow conditions was performed to provide partial
221 validation of the geochemical model by comparison of simulated and measured pH, electrical
222 conductivity and element concentrations in the outflow. The experimental setup is displayed
223 in Fig. 2.

224 **Fig. 2: Upward flow column experiment.**

225 In order to achieve homogenous packing, the untreated, oven-dried residue sand (50°C, > 2 d,
226 $\varnothing < 2$ mm) was poured into a glass column in portions of 5 ± 2 g while a head of 2-5 cm of
227 Milli-Q water was maintained in the column [wet packing, 53]. This packing achieved a final
228 bulk density of about 1.56 g cm^{-3} . No particle separation was observed in the sand column
229 after packing. Deionised water was supplied at the base (inflow) of the vertical column at a
230 constant flux ($15.03 \text{ cm}^3 \text{ min}^{-1}$) using a peristaltic pump (Ismatec MCP). The discharge was
231 collected above the outflow plug in 75.15 cm^3 aliquots, and retained for analysis. Column
232 properties are shown in Table 3.

233 **Table 3: Column properties.**

Property	Value
Column diameter	40 mm
Column length	600 mm
Flux	$15.03 \text{ cm}^3 \text{ min}^{-1}$
Porosity	0.43
Fill volume	600 cm^3

234 The leaching experiment was performed in three replicates (Series I, II and III). Automated
235 measurements of pH and electrical conductivity in the outflow aliquots were taken using a
236 robotic titrosampler (Metrohm 855 Robotic Titrosampler) in combination with appropriate
237 electrodes (Metrohm 6.0257.000 Aquatrode Plus, Metrohm 712 Conductometer with
238 Metrohm 6.0912.110). For alkalinity measurements, samples were immediately titrated to pH
239 4.3 with 0.01 M HCl using an automated titrator (Metrohm 800 Dosino). The CO_2 gas
240 saturation was calculated from pH and alkalinity measurements using PHREEQC by
241 attribution of alkalinity to carbonate species, protons and hydroxyl ions. Major element
242 concentrations were measured in the outflow of Series III using an ICP-OES instrument

243 (Perkin Elmer Optima 3300 DV). Samples were filtered (Whatman Spartan 30 0.45 μm),
244 acidified to $\text{pH} < 2$ using HCl and stored at 4°C prior to analysis.

245 The column experiment was simulated using PHREEQC's 1D-transport capabilities and the
246 geochemical properties that were derived in Sections 2.1 and 2.2. The initial pore water and
247 the inflowing solution were assumed to be in equilibrium with atmospheric CO_2 and O_2 . Ion
248 diffusion and physical dispersivity were estimated as $3 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$ and 10^{-1} m , respectively.
249 Flushing the column with 100 pore volumes corresponds to approximately 35 y of rainfall
250 leaching in the climatic conditions of Western Australia with an estimated annual effective
251 recharge of 600 mm (see Section 5). Measured and simulated pH, alkalinity, electrical
252 conductivity (EC) and CO_2 saturation in the discharge are presented in

253 Fig. 3.

254 **Fig. 3: Results of column experiment for pH (a), alkalinity (b), electrical conductivity (c) and calculated CO_2**
255 **saturation (d).**

256 The pH buffering simulated with the suggested mineral assembly agrees well with
257 observations (

258 Fig. 3a). The overestimation of pH during the first few pore volumes can be attributed to the
259 assumed thermodynamic equilibrium with natron. The simulation of electrical conductivity
260 according to solution species mobility matches well the observations (

261 Fig. 3c). Alkalinity (

262 Fig. 3b), which mainly results from carbonate species, was overestimated by the model,
263 possibly due to equilibration with calcite. Despite this, reasonable agreement for CO_2 -
264 saturation in the column simulation was achieved (

265 Fig. 3d).

266 Results of the element analysis together with modelled total element concentrations in the
267 column outflow are displayed in Fig. 4.

268 **Fig. 4: Element concentrations (mol l⁻¹) in the column outflow for (a) Na, (b) K, (c) Al and (d) Ca.**

269 The simulation of Na concentrations in Fig. 4a agrees very well with observations.
270 Concentrations of potassium (K) (Fig. 4b) are largely underestimated due to the low
271 solubility of muscovite, which is the only source of K in the chosen mineral model.
272 Aluminium (Al) concentrations in Fig. 4c are overestimated by an order of magnitude
273 compared to measurements. This suggests too high solubility constants for DSP and TCA
274 obtained from the literature or reprecipitation of Al in the form of aluminium oxides such as
275 gibbsite and boehmite or aluminium silicates. The mismatch of Ca concentrations in Fig. 4d
276 together with the overestimated alkalinity from

277 Fig. 3b suggests that calcite may not be present as a pure phase, although it is modelled as
278 such.

279 Overall, the comparison of measured and modelled drainage composition shows that large
280 uncertainties exist in setting key mineralogical properties of residue sand. Despite these
281 shortcomings, the geochemical model is considered suitable for estimating the geochemical
282 evolution of residue sand in field conditions because it is capable of reproducing main
283 geochemical features such as pH, EC and Na concentrations.

284 **3 Hydraulic Model**

285 For the hydraulic characterization of residue sand in variably saturated flow conditions the
286 van Genuchten/Mualem model [54, 55] for water retention and unsaturated hydraulic
287 conductivity as in [56] was used. The van Genuchten function [55] is given by

$$\theta(h) = \begin{cases} \theta_r + \frac{\theta_s - \theta_r}{[1 + (\alpha h)^n]^m}, & h < 0, \\ \theta_s, & h \geq 0 \end{cases}, \quad (3)$$

288 where h is the pressure head (cm), θ is the actual moisture content, θ_r is the residual moisture
 289 content, θ_s is the saturated moisture content and α (cm^{-1}), n and $m = 1 - \frac{1}{n}$ are soil-specific
 290 parameters. The free parameters were determined by fitting Eq. (3) to measurements of water
 291 retention that were taken in a pressure range of 0 – 15 bars using the RETC code [57].

292 Unsaturated hydraulic conductivity according to the Mualem model [54] is given by

$$K(\theta) = K_s \theta^l \left[1 - \left(1 - \theta^{\frac{1}{m}} \right)^m \right]^2, \quad (4)$$

293 where $\theta = \frac{\theta - \theta_r}{\theta_s - \theta_r}$ is the reduced moisture content. The parameter l was taken as 0.5. The
 294 saturated hydraulic conductivity K_s (m d^{-1}) of the residue sand was measured in situ at
 295 various depths using a Guelph constant head permeameter. Its value at the soil surface was
 296 measured as 12.008 m d^{-1} . Measured values of water retention and the best fit of the van
 297 Genuchten function with parameters $\alpha = 0.075 \text{ cm}^{-1}$, $n = 1.822$, $\theta_s = 0.454$ and $\theta_r =$
 298 0.039 are displayed together with unsaturated conductivity in Fig. 5.

299 **Fig. 5: Water retention and unsaturated hydraulic conductivity of residue sand at the soil surface according to the**
 300 **van Genuchten/Mualem model.**

301 Conductivity measurements suggest a non-linear relation between K_s and distance to the soil
 302 surface z (m) of the form:

$$K_s(z) = a \exp(bz), \quad (5)$$

303 which was fitted to the data using a least square criterion. The parameters a and b were
 304 determined as 12.008 m d^{-1} and -0.885 m^{-1} , respectively, with a coefficient of determination
 305 of 0.92.

306 The saturated water content θ_s up to a depth of 3 m was calculated from the measured θ_s at
307 the surface and measured values of dry bulk density (1.3 g cm⁻³ at the surface versus 1.5 g
308 cm⁻³ at 3 m depth). Assuming a constant solid density, a linear relation between depth and
309 θ_s was established according to

$$\theta_s(z) = cz + d, \quad (6)$$

310 with $c = 0.028 \text{ m}^{-1}$ and $d = 0.454$. Depth-dependent measurements of K_s and θ_s together with
311 the fitted Eqs. (5) and (6) are displayed in Fig. 6.

312 **Fig. 6: Depth dependence of saturated hydraulic conductivity K_s (left) and saturated water content θ_s (right).**

313 All other parameters in the van Genuchten/Mualem hydraulic model were assumed constant
314 throughout the profile.

315 Transverse and longitudinal dispersivity in the residue sand were estimated as 10^{-1} m. For
316 simplicity, the influences of water saturation [58, 59] and scale [60] were neglected. The
317 coefficient of molecular diffusion was taken as $3 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$ according to the PHREEQC
318 default settings (temperature of 25°C).

319 **4 Software for Integrated Hydrogeochemical Modelling**

320 Processes of variably saturated liquid phase flow, multi-component solute transport and
321 geochemical reactions according to the geochemical and hydraulic properties described
322 earlier were combined into an integrated hydrogeochemical model of bauxite residue sand.
323 The employed software results from coupling the multipurpose finite element solver
324 COMSOL [61] with a component object model (COM) version of IPhreeqc. IPhreeqc is a
325 version of the geochemical modelling framework PHREEQC [29] that is specifically
326 designed for coupling to multi-component solute transport simulators [62].

327 **Fig. 7: Program flow and structure.**

328 The main modules of the coupled software and their interactions are illustrated in Fig. 7. The
329 coupling code is executed within the MATLAB scripting environment [63], which contains
330 the split-operator procedure, manages data transfer between the modules and performs pre-
331 and post-processing tasks. From MATLAB, the computation of aqueous phase flow and
332 solute transport for a single time step is directed to the COMSOL module. After updated
333 liquid phase saturations and solute concentrations are transferred back to the MATLAB
334 workspace, the assembly of chemical components that constitutes the liquid phase is sent to
335 IPhreeqc for geochemical speciation using its COM interface. The main advantage over
336 existing couplings of flow and multispecies transport codes with PHREEQC as reaction
337 engine, such as PHTRAN [64], PHT3D [65] and PHWAT [66], results from the fact that
338 IPhreeqc saves in memory the entire geochemical system state between calls to it. Thus, only
339 the information that is relevant to flow and transport computations (liquid phase saturation
340 and element concentrations) needs to be extracted and transferred to COMSOL. In addition,
341 the data transfer is processed entirely in memory, which avoids inefficient writing and
342 reading of data files. A detailed presentation of the software is provided in [67]. Additional
343 features that were specifically implemented for the presented simulations of bauxite residue
344 sand are documented in the Appendices A-C.

345 **5 Meteorological Conditions**

346 In the absence of vegetation, rainfall and evaporation are the driving forces of soil moisture
347 movement and solute transport in the field. Thus, the geochemical evolution of residue sand,
348 the volumes of drainage, and the magnitude of fertiliser leaching, strongly depend on the
349 local meteorological conditions. Daily rainfall and pan evaporation were obtained from
350 ALCOA's meteorological records for the Pinjarra residue storage area (latitude: -32.647036,

351 longitude: 115.930309). Missing values in the evaporation time series were reconstructed by
352 fitting the amplitude and phase of a sine function with wavelength of 365 d to the measured
353 data. The dominance of seasonal fluctuations of evaporation was verified by means of Fourier
354 analysis. Gaps in precipitation records were filled by linear interpolation between
355 measurements. Mean annual precipitation after the reconstruction of missing data amounts to
356 1005 mm. This value agrees well with the 967 mm y⁻¹ measured at the town of Pinjarra
357 during the period 1877-1991 [68]. The mean annual value of reconstruction potential
358 evaporation (2400 mm y⁻¹) is considerably higher than the value of 2075 mm y⁻¹ from an
359 independent 10-y record (1980-1990) [69]. Nevertheless, the interpolation method for
360 potential evaporation was retained because the influence of evaporation on the overall water
361 balance in the highly conductive sand is limited by water availability in the surface layer. The
362 reconstructed time series of rainfall and potential evaporation at the Pinjarra residue storage
363 site are illustrated in Fig. 8.

364 **Fig. 8: Time series of rainfall and potential evaporation with reconstructed missing values.**

365 In its current form, the model represents bare residue sand prior to or shortly after plant
366 seeding. Therefore, the influence of plants on water availability and water quality is not
367 incorporated in the model. As shown in Wissmeier and Barry [67], however, element-specific
368 root water uptake can be included into the model by using space- and pressure-dependent
369 sink terms in solute transport equations.

370 **6 Simulation of a Field Lysimeter**

371 Currently, no data on fertiliser leaching in residue sand profiles under field conditions are
372 available. At ALCOA's Pinjarra site, however, a field lysimeter has recently been constructed
373 to quantify water and nutrients dynamics in rehabilitated residue sand [70]. In the following,
374 we present a simulation of the geochemical evolution of fertigated and gypsum-amended

375 residue sand in this field lysimeter in response to rainwater leaching under the prevailing
376 meteorological conditions. The simulation period starts with the construction of the lysimeter
377 in August 2007 and ends after 930 d in February 2010.

378 *6.1 Domain, Boundary and Initial Conditions*

379 The lysimeter consists of a 3-m deep pit with vertical walls and a square surface area with
380 sides of 24 m length. The pit is sealed with a high-density plastic liner and drained by
381 regularly spaced (2.5 m spacing) drainage pipes located at 2.8 m below ground level. The
382 domain was simulated as a 2D slice orthogonal to the drainage pipes. Due to symmetry
383 planes halfway between the drainage pipes, at the midpoint of the drainage pipes and at the
384 lateral boundaries, the domain could be reduced to a 1-m wide and 3-m deep column.

385 **Fig. 9: Lysimeter simulation domain and finite element representation.**

386 The simulation domain and its finite element discretization are displayed in Fig. 9. The half
387 circle at $x = 0$ m, $z = -2.8$ m represents part of the drainage pipe where a seepage face
388 boundary according to Eq. (C.1) in Appendix C with $k_{sp} = 10^{-4} \text{ s}^{-1}$ was applied. At $z = 0$, an
389 atmospheric boundary according to Eq. (C.4) with $H_{crit} = -30$ m, $\xi = 0.4 \text{ s}^{-1}$, $H_{po} = 0$ m and
390 $k_{po} = 10^{-4} \text{ s}^{-1}$ was used. A zero-flux condition was employed for the remaining boundaries.
391 The upper part of the domain with predominantly vertical flow was discretized by a
392 quadrilateral mesh with a vertical element size of 3×10^{-3} m at the top boundary. The fine
393 discretization was necessary to capture the sudden changes between infiltration and
394 evaporation in the highly conductive sand. From $z = -2$ m downwards, a triangular mesh with
395 a compressed z -direction and local refinement around the seepage boundary was used. The
396 initial pressure head at the start of the simulation was taken as -1 m. At the top boundary,
397 equilibrium of the infiltrating and evaporating rainwater with atmospheric CO_2 at 3.16×10^{-4}

398 atm and O₂ at 1.99×10^{-1} atm was assumed. The split-operator time step for alternations
399 between flow, transport and reaction calculations was set to 1 d.

400 6.2 *Fertigation and Gypsum Amendment*

401 Further to its natural geochemical properties, residue sand in the 0 – 1.5 m depth interval was
402 amended with gypsum at a rate of 1% by weight. Furthermore, the top 0.2 m of the profile
403 received a one-off addition of 2.7 t/ha of inorganic fertiliser mix mainly comprised of di-
404 ammonium-phosphate (DAP), K₂SO₄ and MgSO₄. Phosphate (from DAP) in contact with
405 gypsum is likely to reprecipitate as hydroxyapatite, which is why this mineral was included in
406 the simulations with an initial amount of 0. This is also in agreement with observation in an
407 independent column experiment (data not shown).

408 The amendments were included in the model through additional equilibrium dissolution
409 reactions according to the reaction formulas, equilibrium constants and amounts listed in
410 Table 4.

411 **Table 4: Fertilizer and amendment properties.**

Mineral name Reaction formula	Equilibrium constant	Relative amount (mol l _{soil} ⁻¹)
Gypsum ^a CaSO ₄ ·2H ₂ O = Ca ⁺² + SO ₄ ⁻² + 2 H ₂ O	10 ^{-4.61 c}	1.10 × 10 ⁻¹
DAP ^b (NH ₄) ₂ HPO ₄ = 2 NH ₄ ⁺ + HPO ₄ ⁻²	10 ^{0.3 d}	5.67 × 10 ⁻³
Arcanite ^b K ₂ SO ₄ = SO ₄ ⁻² + 2 K ⁺	10 ^{-1.776 e}	2.41 × 10 ⁻³
MgSO ₄ ^b MgSO ₄ = Mg ⁺² + SO ₄ ⁻²	10 ^{4.8781 f}	1.50 × 10 ⁻⁴
MnSO ₄ ^b MnSO ₄ = Mn ⁺² + SO ₄ ⁻²	10 ^{2.669 c}	1.42 × 10 ⁻⁴
CuSO ₄ ^b CuSO ₄ = Cu ⁺² + SO ₄ ⁻²	10 ^{3.01 c}	1.55 × 10 ⁻⁴
Zincosite ^b ZnSO ₄ = Zn ⁺² + SO ₄ ⁻²	10 ^{3.01 c}	1.11 × 10 ⁻³
Borax ^b Na ₂ (B ₄ O ₅ (OH) ₄):8H ₂ O + 2 H ⁺ = 4 B(OH) ₃ + 2 Na ⁺ + 5 H ₂ O	10 ^{12.464 e}	2.62 × 10 ⁻⁵
Hydroxyapatite Ca ₅ (PO ₄) ₃ OH + 4 H ⁺ = H ₂ O + 3 HPO ₄ ⁻² + 5 Ca ⁺²	10 ^{-3.421 g}	0.00

412 ^a applied to the top 1.5 m, ^b applied to the top 0.2 m, ^c minteq.dat, ^d calculated from solubility in pure water [71],
 413 ^e pfitzer.dat, ^f lnl.dat, ^g phreeqc.dat

414 As can be seen from Eq. (1), the rate of concentration changes due to the kinetic dissolution
 415 of TCA and sodalite is dependent on the ratio of reactive surface to solution volume. In
 416 unsaturated residue sand with an average moisture content of 0.2, this ratio is approximately
 417 40 times larger than in the acid neutralization experiment. Therefore, the assumption of local
 418 thermodynamic equilibrium was extended to TCA and sodalite.

419 6.3 Results and Discussion

420 6.3.1 Dynamic Water Balance

421 Results of the dynamic water balance for the simulation period of 930 d starting on 1 August
422 2007 are displayed in . The surface flux in (Fig. 10a) was normalized by the infiltrating area
423 and reflects the strong events during winter, which were immediately followed by marked
424 evaporation. Despite high potential evaporation during summer, actual evaporation was
425 effectively shut down due to the limited water availability in the upper soil profile. Discharge
426 in Fig. 10b was also normalized with respect to the infiltrating area for better comparability.
427 The water infiltrated during the 2007 rainfall season at the beginning of the simulation
428 reaches the drainage pipe after 60 d. Before any discharge is produced, the domain below the
429 drainage pipe was saturated. The initial filling of the lysimeter bottom during the first 60 d
430 can be followed in the evolution of average moisture contents (Fig. 10c). The fast discharge
431 recession leads to very low outflow rates during summer months. Despite the fully saturated
432 lysimeter bottom, the moisture content frequently declined below a domain average of 0.15
433 during summers. This is also confirmed experimentally by in-situ moisture probes and
434 neutron probe measurements.

435 **Fig. 10: Dynamic water balance of lysimeter simulation with (a) surface flux (mm d^{-1}), (b) drainage at the drainage**
436 **pipe (mm d^{-1}) and (c) average soil moisture content θ .**

437 Overall, the simulation of soil moisture in the lysimeter (Fig. 10) indicates very dry
438 conditions throughout the entire simulation period. During summers, the water content
439 frequently decreased to values close to the residual (i.e., plant-unavailable) moisture content
440 in the upper metre of the profile. Despite low moisture contents, the average fluid pressure
441 did not drop below the permanent wilting point (PWP: $h = -15$ bar). However, near the
442 surface the PWP was frequently reached. In addition, the sand contains only marginally more
443 water at -1 bar than at -15 m due to the steep gradient of water retention $\frac{dh}{d\theta}$ (Fig. 5). Even

444 during rainfall seasons, the moisture content hardly exceeded 0.2 in the upper 2.5 m of the
445 domain. Despite the poor water holding capacity of the sand, only about 46% of the total
446 rainfall left the lysimeter as drainage. The rest was lost by evaporation or stored in the
447 initially dry profile. Thus, the water supply alone imposed conditions that were challenging,
448 but not inhibiting, for plant growth in the lysimeter.

449 6.3.2 Solution Chemistry

450 Fig. 11 illustrates the evolution of vertical profiles of moisture content, pH and selected
451 solution element concentrations at the right domain boundary ($x = 1$ m). Despite the local
452 outflow at the drainage pipe ($x = 0$ m), only minor lateral variations of geochemistry and
453 moisture conditions were observed. Moisture content profiles show the development of the
454 groundwater table below the drainage pipe as response to the winter rainfall around 50 d. The
455 upper part of the soil column then dried out over summer until the beginning of the following
456 rainy season. The pH profiles show a fast reduction of pH in the upper soil profile to about 11
457 from an initial value of 12.5 caused by gypsum dissolution and calcite precipitation. In the
458 lower profile below -1.5 m, the pH was governed by dissolved natron.

459 **Fig. 11: Evolution of moisture content, pH and concentration of selected elements at the right domain boundary of**
460 **the lysimeter simulation.**

461 With the second winter's rainfall starting at around 300 d, the pH reduced to values around
462 10 in the upper soil profile and with the third winter's rainfall in the entire profile. The
463 initially high Na concentration from natron dissolution was flushed into the lower part of the
464 domain with the first rainfall. The second rainfall period almost completely removed Na from
465 the system, due to the comparatively low solubility of sodalite and analcime. Carbon, as
466 carbonate (CO_3^{-2}) from natron dissolution, immediately reprecipitated as calcite in the upper
467 part of the domain due to the large supply of Ca from gypsum dissolution. The remaining
468 carbon in the un-amended region of the domain was removed after approximately 50 d. Ca

469 concentrations show a complex pattern mainly governed by the solubility of calcite and
470 gypsum, both of which are controlled by pH. The decrease in Ca at the top boundary during
471 the second and third rainfall period indicates complete removal of gypsum, which was not
472 observed in the field. This is most likely due to non-equilibrium of gypsum with the soil
473 solution as result of inhomogeneous amendment of the gypsum. During the following
474 evaporation events, the upwards flowing solution was concentrated due to the removal of
475 H₂O at the surface. However, evaporation essentially stops during the dry season because of
476 low moisture contents at the surface. Sulphur, as sulphate (SO₄⁻²), behaved similarly to Na in
477 the region of gypsum amendment above -1.5 m. Its high initial concentration, resulting from
478 the equilibrium between gypsum and calcite, was flushed almost entirely within the first 300
479 d. Nitrogen (N(-3) as sum of NH₄⁺ and NH₃) was decoupled from oxidized forms (e.g., NO₃⁻)
480 to avoid instantaneous conversion to N(+5). N(-3) concentrations are displayed representative
481 for the fertilizer elements copper (Cu), zinc (Zn) and boron (B), which show very similar
482 concentration patterns. Their concentration ranges correspond to the amounts of the applied
483 fertilizer minerals (Table 4). The fertilizer elements were carried downwards through the soil
484 profile with the first winter rainfall, and with the second winter's rainfall, they were flushed
485 from the profile without significant retention. Due to high Ca concentrations the model
486 predicted reprecipitation of hydroxyapatite (Ca₅(PO₄)₃OH), which retains phosphate (P) in
487 the profile. K concentrations were significantly retarded compared to nitrogen because of
488 temporary adsorption on the cation exchange sites. Magnesium (Mg) shows a mixture of the
489 conservative transport pattern of nitrogen and the exchange pattern of K. High initial Al
490 concentrations in the lower half of the domain resulted from the dissolution of TCA, which is
491 enhanced by reprecipitation of Ca as calcite. In the gypsum-amended part of the soil, TCA
492 dissolution was inhibited by gypsum dissolution. Silica (Si) shows the same concentration

493 pattern as chloride. Both elements were controlled by the dissolution of sodalite, which was
494 activated after the complete removal of TCA.

495 6.3.3 Minerals

496 Fig. 12 illustrates the evolution of the main mineral phases in residue sand. Muscovite and
497 analcime did not show any significant response towards leaching during the simulation period
498 and so are omitted in the figure. The other residue minerals show only minor changes in the
499 upper few decimetres of the domain. Gypsum was removed from the top 0.5 m after 3 y of
500 rainfall. However, due to the equilibrium assumption, a considerable amount of gypsum in
501 the top 1.5 m instantaneously transformed into calcite, taking up most of the CO_3^{-2} from
502 natron dissolution. Apart from this increase, calcite shows little response to leaching. Almost
503 half of the initial amount of TCA was immediately dissolved in the untreated residue sand
504 where Ca re-precipitated to calcite with the CO_3^{-2} from natron dissolution. This
505 transformation was suppressed by gypsum in the in the upper part of the domain. However,
506 the fertilizers in the top 0.2 m enhanced TCA dissolution. Leaching of the third rainfall
507 season around 700 d removed TCA from the top 0.2 m. Sodalite shows no reaction towards
508 gypsum and fertilizer amendment. It was slowly leached from the first few centimetres of the
509 soil profile during the three simulated rain seasons once TCA and gypsum were removed.

510 **Fig. 12: Evolution of the main minerals at the right domain boundary of the lysimeter simulation.**

511 6.3.4 Cation Exchange

512 The evolution of the exchange species is illustrated in Fig. 13. The initial exchanger
513 composition was dominated by Na, which was replaced mainly by Ca during the course of
514 the simulation. Al is omitted in the figure due to insignificant adsorption in the high pH
515 environment, where it was mainly present in anionic form as $\text{Al}(\text{OH})_4^-$. At the transition from
516 the Na to Ca-dominated exchanger, adsorption of K, N(-3), Mg and Mn took place. Despite

517 the higher affinity of standard exchangers for divalent ions, K was the most adsorbed
518 fertilizer element. This is because of its higher concentration compared to divalent fertilizer
519 elements and its large affinity relative to other monovalent fertilizer elements. N(-3) as NH_4^+ ,
520 which was retained in the upper part of the profile during the first summer, was almost
521 completely removed during the second rainfall period. The low adsorption of N(-3) resulted
522 from its speciation into uncharged NH_3 at pH values above 9. The amount of adsorbed Mg,
523 which is representative for the adsorption pattern of Mn (maximum adsorbed amount $1.5 \times$
524 $10^{-5} \text{ mol l}_{\text{soil}}^{-1}$), increased after 400 d. The adsorption of zinc and copper was insignificant due
525 to low solution concentrations (maximum adsorbed amounts $10^{-8} \text{ mol l}_{\text{soil}}^{-1}$ and $3 \times 10^{-11} \text{ mol}$
526 $\text{l}_{\text{soil}}^{-1}$, respectively).

527 **Fig. 13: Evolution of the exchanger composition at the right domain boundary of the lysimeter simulation.**

528 Overall, the predicted geochemical conditions in the lysimeter were still unfavourable for
529 plant growth after 3 y, both in terms of water availability and quality. Even though the main
530 soluble ions Na^+ and SO_4^{-2} were flushed from the system, a pH of 10 was maintained. The
531 plant nutrient status was not sustainably improved by fertilizer amendment. Only K was
532 significantly retained by initially Na-filled adsorption sites. Adsorption of other fertilizer
533 cations including NH_4^+ was insignificant due to (i) their low concentrations compared to the
534 major solutions ions Na and Ca, (ii) their speciation into neutral or negatively charged ions at
535 high pH, and (iii) the low exchange capacity of residue sand. The chromatographic sequence
536 from a Na-dominated exchanger through the temporary adsorption of fertilizer cations to a
537 Ca-dominated system can be interpreted as a snowplough [72-74]. The buffering minerals,
538 TCA, sodalite and calcite that stabilize the pH around 10 were removed from the top few
539 centimetres of the profile. As intended by the gypsum amendment, solution alkalinity was
540 converted to calcite [75, 76]. This procedure, however, did not remove the alkalinity from the
541 system converted it into solid form and prevents the removal of TCA [77].

542 7 Simulation of Surface Cover for Storage Facilities

543 In order to evaluate the performance of fertigated and gypsum-amended residue sand as a
544 surface cover for storage facilities, the hydrogeochemical model was applied to a stratum of
545 sand overlaying low permeability residue mud. Apart from the domain geometry and
546 discretization, the hydrological and geochemical conditions of the lysimeter simulation were
547 adopted including fertigation and gypsum amendment. In contrast to the lysimeter with
548 predominantly vertical flow, the development of a water table at the border to the residue
549 mud introduces a considerable horizontal flow component.

550 7.1 Domain, Boundary and Initial Conditions

551 The simulation represents a 3-m thick by 100-m wide layer of residue sand on top of a
552 storage impoundment. Due to symmetry across the centre line, the actual simulation domain
553 was confined to a slice of the cover layer from $x = 0$ m to $x = 50$ m with a symmetry
554 boundary at the right hand side border of the domain. The domain was represented by 10,829
555 computational nodes. For enhanced lateral drainage, the cover layer was conceptualized with
556 a slope of 1.74%. Water losses at the interface to the residue mud at the domain bottom were
557 approximated by a constant flux of 8.3×10^{-7} m s⁻¹ in water-saturated conditions and zero
558 flux otherwise. The magnitude of this deep percolation was taken as the saturated hydraulic
559 conductivity of red mud [3], in which case the flux corresponds to gravity-driven drainage.
560 The left hand side of the domain was represented by a seepage face boundary according to
561 Eq. (C.1) with a stiff-spring constant of $k_{sp} = 10^{-3}$ s⁻¹. Atmospheric forcing of the system was
562 imposed via an atmospheric boundary condition at the top of the domain. In order to predict
563 the evolution of the sand cover for 5 y, the measured meteorological time series of 3 y were
564 repeatedly applied to the soil surface.

565 7.2 Results and Discussion

566 7.2.1 Dynamic Water Balance

567 The dynamic water balance of the surface cover simulation is illustrated in Fig. 14. For better
568 comparability with the lysimeter simulation (Fig. 10), the y-axis scaling was retained.
569 Compared to the lysimeter simulation the surface cover exhibits much larger water storage
570 capacity and slower recession of discharge during dry periods due to impeded drainage (Fig.
571 14b). As in Fig. 10, the drainage flux was normalized to the inflow area for comparability. At
572 the beginning of the simulation period, a perched water table evolved at the border to the
573 low-permeability mud. Due to this water table, the average soil moisture (Fig. 14c) was at
574 much higher levels (0.2-0.3) compared to the lysimeter simulation.

575 **Fig. 14: Dynamic water balance of surface cover simulation, with (a) surface flux (mm d^{-1}), (b) drainage (mm d^{-1}) and**
576 **(c) average soil moisture content θ .**

577 7.2.2 Solution Chemistry

578 Time-dependent profiles of normalized soil moisture, $\Theta = \frac{\theta - \theta_r}{\theta_s - \theta_r}$, selected total element
579 concentrations and pH are displayed in Fig. 15 with different scales for the x- and y-axes.
580 Different colour scales were used for the plots from 1 to 50 d and from 400 to 1825 d because
581 the low fertilizer concentrations after the first rainfall period would otherwise be
582 indistinguishable in the later profiles. Display times were selected during the first rainfall
583 period (1-50 d), in the middle of the second rainfall period (400 d), after the third rainfall
584 period (1000 d) and at the end of 5 y of atmospheric leaching (1825 d).

585 Normalized water contents illustrate the build-up of soil moisture at the border of the residue
586 mud and the evolution of a perched water table. The results at 400 and 1000 d show water
587 table fluctuations from winter to summer.

588 **Fig. 15: Evolution of normalized moisture content, concentrations of selected elements and pH profiles of the surface**
589 **cover simulation at 1, 20, 50, 400, 600 and 1825 d.**

590 Until the last profile at 1825 d, Ca that mainly originates from gypsum and TCA dissolution
591 did not enter the saturated zone. Declining concentrations at the top of the domain indicate
592 complete removal of gypsum and TCA. Na was flushed from the unsaturated zone with the
593 first rainfall event. Due to the velocity field in the saturated groundwater lens, concentrations
594 were more persistent towards the right hand side of the domain. However, after the third
595 rainfall season (1000 d) most of the Na has been removed. N(-3) is representative for all
596 fertilizer elements besides K. Through dilution and dispersion, concentrations decreased with
597 the first infiltration water. During the second rainfall period around 400 d, the fertilizers were
598 removed from the unsaturated zone. However, they remained in the groundwater lens at
599 roughly a tenth of their original concentration. Fertilizer concentrations decreased further
600 during the third rainfall season until they were removed completely after 5 y of leaching. The
601 behaviour of K, the most adsorbing element, was very similar to N(-3). As result of the
602 exchange process, however, its removal was delayed compared to the other fertilizer
603 elements. During the first rainfall period, the pH behaved similarly to the lysimeter
604 simulation because of essentially 1D flow. After the perched water table has established, two
605 pH regions were separated by the line of the groundwater table in moist conditions. The pH
606 in the saturated region was persistent until it was eventually leached to pore water levels in
607 the unsaturated zone after 5 y. In the profiles at 1000 and 1825 d the removal of gypsum and
608 TCA at the top of the domain decreased the pH to around 9.

609 7.2.3 *Minerals*

610 The evolution of the main minerals in the surface cover is illustrated in Fig. 16. During 5 y of
611 rainfall, gypsum was removed from the top metre of the profile. In this zone, calcite showed
612 hardly any response to leaching. However, additional precipitation was predicted at the lower

613 boundary of the gypsum-amended region and in the saturated zone. TCA was removed from
614 the top 0.5 m and from the saturated zone, while sodalite was only removed from the top few
615 decimetres. Exchange processes are dominated by Na-Ca exchange, and are omitted since the
616 results are similar to those for the lysimeter.

617 In summary, the results show that water availability was improved in the surface cover by the
618 formation of a perched groundwater table. Waterlogged conditions with evaporation-induced
619 salt accumulation at the soil surface [78-80] were avoided by the slope of the underlying low-
620 permeability mud and lateral drainage. Due to its large water volume, the saturated zone
621 acted as a buffer for infiltrating solutes and retained fertilizer ions. However, enhanced water
622 retention also retained adverse soil properties such as high pH and Na concentrations, which
623 decreased the efficiency of natural leaching.

624 **Fig. 16: Evolution of the main minerals of the surface cover simulation for 1 and 1825 d.**

625 **8 General Discussion**

626 *8.1 Model Uncertainties*

627 The model for mineral reactions in bauxite residue sand comprises large uncertainties, even
628 though all components of the mineral assembly have been previously identified in residue of
629 different origins [30, 34, 41, 81]. The mineral assembly as deduced from acid neutralization
630 alone is not unique and other combinations of minerals may reproduce pH buffering equally
631 well. Sodalite and additional amounts of natron, for instance, yield excellent agreement with
632 acid neutralization at 96 h. However, this would require the kinetic dissolution of natron at a
633 timescale of days, which is not plausible unless it is partially occluded within the profile. In
634 order to increase the reliability of the predictions, detailed quantification of the reactive
635 minerals specifically for Pinjarra residue sand would be required. Furthermore, equilibrium

636 constants vary widely among authors and databases, particularly for different forms of
637 tricalcium aluminates but also for muscovite and analcime. Measurements of the
638 stoichiometry and solubility of reactive minerals on phases isolated from the residue would
639 be desirable. This is also important because most reactive minerals form during the refining
640 process, so that their reactivity and stoichiometry depends on the bauxite source and
641 processing conditions [32, 33, 39, 82, 83]. The fact that Khaitan et al. [34] attribute the pH
642 buffering capacity of residue from Jamaican bauxite mainly to TCA and calcite whereas
643 Menzies et al. [41] and Snars and Gilkes [30] hold mainly sodalite and calcite responsible for
644 pH control indicates the large uncertainty in the recent literature. In the mineral assembly
645 determined in this study, both phases contribute to pH buffering in roughly equal parts.
646 Acknowledging the large uncertainties, the derived mineral composition can be regarded as a
647 surrogate for major geochemical properties such as pH, electrical conductivity and Na
648 concentrations. Concentrations of elements that are not components of an included mineral,
649 such as iron, Mg and titanium (Ti), cannot be predicted.

650 In a recent study, Phillips and Chen [14] found a large contribution ($8-12 \text{ cmol kg}_{\text{solid}}^{-1}$) of
651 pH-dependent variable charge adsorption sites to the overall adsorption characteristics of
652 residue sand. Menzies et al. [41] measured the effective exchange capacity of seawater
653 neutralized residue sand as $18.6 \text{ cmol kg}_{\text{solid}}^{-1}$ from which they attributed $6 \text{ cmol kg}_{\text{solid}}^{-1}$ to
654 variable charge. These values exceed the cation exchange capacity measured in this study by
655 a factor of 10-20. However, both previous studies rely on compulsive exchange of K^+ with
656 NH_4^+ . As shown in Fig. 4b, considerable amounts of K are released by mineral dissolution.
657 Therefore, K concentrations cannot be considered to result solely from exchange processes,
658 which may lead to an overestimation of the effective exchange capacity. The presumed pH-
659 dependency of the exchange sites may in fact reflect the solubility of the source mineral (e.g.,
660 muscovite). On the other hand, the effective exchange capacity in our study may have been

661 reduced by the washing procedure, particularly through the removal of surface aluminous and
662 ferric oxides that contribute to variable charge adsorption sites. Nevertheless, we employ the
663 lower value of cation exchange capacity on washed residue since it gives a more conservative
664 estimate of nutrient retention. Because pH levels during the simulations were well above the
665 point of zero charge of ferrous and aluminous oxides [84, 85], charge characteristics are not
666 expected to change significantly. This justifies the use of a simple exchange model for
667 adsorption. However, the adsorption behaviour of cations onto zeolites such as sodalite is
668 influenced by the window size of their cage structure [86-90]. Thus, the applicability of
669 standard affinity constants for the simulation of cation exchange remains uncertain [91].

670 The dynamic water balance is regarded as relatively reliable since the parameters for soil
671 moisture movement are directly measured or derived from measurements according to
672 standard procedures (e.g., water retention).

673 An obvious weakness of the simulations is the lack of in-depth model validation due to the
674 scarcity of analytical data.

675 *8.2 Implications for Bauxite Residue Management*

676 Despite the model uncertainties, the main results are plausible and consistent with
677 observations. Because the model is adapted to the geochemical and meteorological conditions
678 at the Pinjarra refinery, findings are site-specific but can be generalized to residue sand with
679 similar properties and in comparable climatic conditions.

680 The lysimeter simulation illustrates the poor water retention in the residue sand with low
681 plant-available soil moisture content. Thus in well-drained systems water availability is a
682 limiting factor for plant growth. The simulation of the cover layer shows that the moisture
683 status in residue sand can be improved by the appropriate design of the horizontal distance

684 between drains, the thickness of the cover layer and its slope. If these parameters are not
685 chosen carefully, for example if the distance between drains is too large, waterlogged
686 conditions with adverse effects on plant growth may result (simulation results not shown).
687 The development of a shallow water table increases evaporation losses during the summer
688 months. Although not observed in our simulations, this may lead to salt accumulation at the
689 soil surface [e.g., 78, 79]. The amendment of residue sand with fine-textured residue mud
690 would improve the soil water retention but at the same time worsens the geochemical
691 properties through enhanced pH buffering [92]. Compared to the hydrological situation, the
692 geochemical properties of the residue sand are seen as more severe constraints for plant
693 growth. Mineral reactions in amended fresh residue sand are governed by the initial
694 dissolution of natron and gypsum, where Ca and CO_3^{2-} precipitate as calcite while the soluble
695 $\text{Na}_2\text{SO}_4^{2-}$ is flushed. Even though gypsum amendment reduces the solution pH to 10, leaching
696 of TCA and therefore the sustainable decrease of pH buffering in the sand is inhibited. From
697 the main buffering minerals, TCA and sodalite are very resistant to rainwater leaching due to
698 their low solubility. Efficient retention of fertilizers is prevented by (i) the low cation
699 exchange capacity of residue sand, (ii) competition with high levels of Ca and Na for
700 exchange sites, and (iii) the speciation of fertilizer elements into uncharged or negative ions
701 at elevated pH (e.g., NH_3). Therefore, the addition of fertilizers to gypsum-amended fresh
702 residue sand only temporarily improves the plant nutrient status. Natural attenuation of
703 gypsum-amended and fertigated residue sand through atmospheric leaching is not a viable
704 long-term option to improve the hydrogeochemical properties for establishing a sustainable
705 vegetation cover.

706 Instead, we propose a comprehensive treatment scheme that aims at improving all major
707 aspects of soil fertility:

- 708 1. Removal of most soluble mineral fractions – e.g., through seawater neutralization [5,
709 41, 93, 94] – to decrease the solid pH buffering capacity and attenuate the competition
710 with fertilizer ions for exchange sites;
- 711 2. Amendment with a fine textured mineral soil (not residue mud) to improve water
712 retention and cation exchange capacity;
- 713 3. Adaption of surface cover dimensions to the hydraulic properties of the substrate with
714 regularly spaced drains to improve the water balance;
- 715 4. Amendment with organic fertilizer to establish a natural microbial community,
716 increase the adsorption capacity [6, 8, 95-97]; and
- 717 5. Application of inorganic fertilizers [10, 12, 16, 17, 95, 98] to improve the plant
718 nutrient status.

719 **9 Conclusions**

720 We present the application of a software coupling of COMSOL and IPhreeqc for interactions
721 of comprehensive geochemical reactions and 2D variably saturated soil moisture movement
722 to evaluate the environmental behaviour of bauxite refining residue sand. The main findings
723 of the simulations are:

- 724 • In well-drained residue sand, the average moisture content drops below 0.1 for
725 extended periods during summer, which poses limitations to plant growth.
- 726 • By adapting the dimensions and drainage of residue storage facilities to the hydraulic
727 properties of the cover material (e.g., mixtures of sand and clay), a plant-suitable
728 moisture content can be maintained also during the dry summer months.
- 729 • Nonrecurring fertilizer application on fresh residue sand does not alter the long-term
730 plant nutrient status due to low cation exchange capacity, competition with
731 predominant solution ions and speciation into neutral or negative form.

- 732 • Gypsum amendment ameliorates the pH to around 10 but suppresses the dissolution
733 of TCA and therefore hampers the sustainable leaching of solid alkalinity.

734 Thus, we conclude that gypsum-amendment and application of inorganic fertilizers alone
735 does not sufficiently improve the geochemical conditions in residue sand to promote a
736 vigorous and sustainable vegetation cover. Since the minerals in residue sand have a very
737 high buffering capacity and annual recharge rates in southwest Western Australia are low,
738 natural attenuation of the sand's pH via rainfall leaching is predicted to be in the order of tens
739 of years. For the successful revegetation of residue storage facilities all aspects of soil fertility
740 need to be addressed before residue sand can serve as valuable medium for plant growth. A
741 logical step for future model development would be the incorporation of biological
742 transformations by plants and soil microbes.

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1034

1035 **Appendix A: Sequential Solution of Flow and Transport**

1036 Using the coupling of COMSOL and IPhreeqc, the simultaneous solution of the non-linear
1037 partial differential equation of variably saturated flow together with numerous transport
1038 equations for multi-component solutions in complex domains quickly becomes unstable with
1039 excessive memory requirements. In order to increase the efficiency and stability of COMSOL
1040 computations, flow and transport were solved sequentially using COMSOL's segregated
1041 solver. This assumes a strict one-way coupling between the two processes. Thus, the iterative
1042 solution of Richards' equation is only computed for the pressure variable. The resulting time-
1043 dependent flow field is then input into the multi-component solute transport equations, which
1044 are linear and thus easier and faster to solve.

1045 **Appendix B: Parallelization**

1046 During reaction calculations in IPhreeqc, each node of the discretized simulation domain is
1047 represented by an independent geochemical batch system. Thus, large domains require the
1048 computation of several thousands of batch systems, which may lead to long computation
1049 times particularly if complex kinetic reactions are involved. For increased computational
1050 efficiency, reaction calculations were parallelized, making use of MATLAB's *single program*
1051 *multiple data* algorithm. In this procedure, an IPhreeqc COM-object is initialized on each of
1052 the engaged processors and the number of batch systems for evaluation is distributed evenly.

1053 The speed increase that results from distributed reaction calculations scales well with the
1054 number of available processors.

1055 **Appendix C: Implementation of Atmospheric and Seepage Face Boundaries**

1056 The interface for Richards' equation in COMSOL's Earth Science Module provides
1057 predefined settings for pressure head and flux boundary conditions. In the case of seepage
1058 face and atmospheric boundaries, however, a flux condition may turn locally into a head
1059 condition and vice versa according to a head-based criterion [e.g., 99, 100]. Since the type of
1060 boundary condition cannot be changed during a simulation, the stiff-spring approach, where a
1061 Neumann statement about flux is used to achieve a Dirichlet condition for the pressure head,
1062 has to be employed [101].

1063 A seepage face boundary conceptualizes a porous medium that drains freely and where the
1064 out-flowing water is removed rapidly enough such that it does not build up on the surface.
1065 Consequently, a zero head condition applies as long as there is potential outflow from the
1066 domain (the pressure head within the domain is greater than zero). In unsaturated conditions
1067 (negative pressure head), the boundary turns into a no-flow boundary. The stiff-spring
1068 representation of a seepage face boundary is given by

$$q_0 = \begin{cases} 0, & H_0 \leq 0 \\ -k_{sp}H_0, & H_0 > 0 \end{cases} \quad (\text{C.1})$$

1069 where q_0 (m s^{-1}) is the inward flux crossing the boundary, H_0 (m) is the actual pressure head
1070 at the boundary and k_{sp} (s^{-1}) is the positive spring constant. The flux $-k_{sp}H_0$ must be of a
1071 magnitude sufficient to prevent build-up of water and fix the pressure head at the boundary
1072 effectively to zero. Therefore, the accuracy of the stiff-spring representation increases with
1073 the magnitude of k_{sp} , however at the cost of numerical efficiency and stability [102, 103].

1074 Atmospheric boundary conditions are governed by the recharge flux $r(t)$ (m s^{-1}), which is the
1075 difference between the absolute values of rainfall and potential evaporation. In the case of
1076 bare soil evaporation, $r(t)$ is limited by the water availability in the soil. Once a critical
1077 negative pressure head, H_{crit} (m), at the soil surface is reached, the boundary conceptually
1078 switches from a specified flux boundary to a head condition. H_{crit} is the pressure potential of
1079 the atmosphere and a measure of the atmospheric evaporation demand [100]. In dry and hot
1080 weather situations, it may exceed in magnitude -10^3 m. Thus, in contrast to the seepage face
1081 boundary, the change between constant head and specified flux occurs in the dry range of the
1082 moisture spectrum, where H_0 is extremely sensitive to the applied flux. In order to avoid
1083 oscillations of the numerical scheme a smooth spring function is required that merges
1084 seamlessly with the flux in unconstrained conditions. For the representation of evaporation
1085 boundaries, we therefore make use of the following condition:

$$q_0 = -r(t) \tanh \left[\frac{\xi}{r(t)} (H_0 - H_{crit}) \right], \quad (\text{C.2})$$

1086 where ξ (T^{-1}) is the derivative of q_0 with respect to H at H_{crit} , which determines implicitly
1087 the width of the transition zone between unconstrained and limited evaporation.

1088 **Fig. 17: Boundary flux during negative recharge in the vicinity of the critical pressure head H_a .**

1089 The behaviour of q_0 in the vicinity of H_{crit} is illustrated in Fig. 17. As H_0 approaches H_{crit} ,
1090 the magnitude of the evaporation flux is reduced continuously until evaporation stops
1091 completely and even gives positive values (condensation) if H_{crit} is surpassed. This
1092 behaviour is consistent with the physical process, where evaporation from dry soils is
1093 gradually reduced due to limited water availability. Low values of H_{crit} require a larger
1094 smoothing zone (lower ξ) and very fine domain discretization near the boundary [104] in
1095 order to achieve numerical convergence.

1096 In the case of positive recharge the boundary flux is limited by the infiltration capacity at the
 1097 maximum surface pressure head H_{po} (m), which represents the maximum height of ponded
 1098 water [56]. Conceptually, the specified flux condition $q_0 = r(t)$ turns into a head condition
 1099 when H_0 exceeds H_{po} . This can be expressed as a conventional stiff-spring boundary
 1100 according to:

$$q_0 = \begin{cases} r(t), & H_0 \leq H_{po} \\ r(t) - k_{po}(H_0 - H_{po}), & H_0 > H_{po} \end{cases}, \quad (C.3)$$

1101 where k_{po} (s^{-1}) is the spring constant. The flux $-k_{po}(H_0 - H_{po})$ reduces infiltration until the
 1102 ponded boundary head is established.

1103 The full atmospheric boundary condition results from combining the evaporation boundary
 1104 Eq. (C.2) with the infiltration boundary Eq. (C.3), yielding:

$$q_0 = \begin{cases} -r(t) \tanh \left[\frac{\xi}{r(t)} (H_0 - H_{crit}) \right], & r(t) < 0 \\ r(t) \mathcal{H}(H_{po} - H_0) + [r(t) - k_{po}(H_0 - H_{po})] \mathcal{H}(H_0 - H_{po}), & r(t) \geq 0 \end{cases}, \quad (C.4)$$

1105 where \mathcal{H} is the Heaviside step function [e.g., 105].

1106 Instead of the tanh-function in Eq. (C.4), COMSOL's smoothed version of the Heaviside
 1107 function *flc2hs* can be used. The inwards recharge flux then becomes

$$q_0 = r(t)[-1 + 2 \text{flc2hs}(H_0 - H_{crit}, \varrho)], \quad r(t) < 0. \quad (C.5)$$

1108 In Eq. (C.5) the transition zone is explicitly determined by the parameter ϱ (m). However the
 1109 slope of q_0 with respect to H_0 at H_{crit} , which is relevant for numerical stability, depends on
 1110 H_{crit} and q_0 .

1111 **Appendix D: Particle Size Distribution, Surface Area**

1112 It is generally accepted that the rate of mineral reactions is proportional to the area of the
1113 reacting surface [45, 52]. In order to determine the macroscopic surface area a particle-size
1114 analysis was performed on washed residue sand (see Section 2.2 for details on washing
1115 procedure) using laser diffraction particle size analysis (LS 13 320 Beckman Coulter). In Fig.
1116 18, the relative solid volume against particle diameter is displayed as the mean of four
1117 replicates.

1118 **Fig. 18: Particle size distribution of washed residue sand.**

1119 With the assumption of spherical particles and a measured solid density of 2.74 g cm^{-3} the
1120 specific surface area of residue sand, as derived from the particle size distribution, amounts to
1121 $0.0264 \text{ m}^2 \text{ g}^{-1}$.

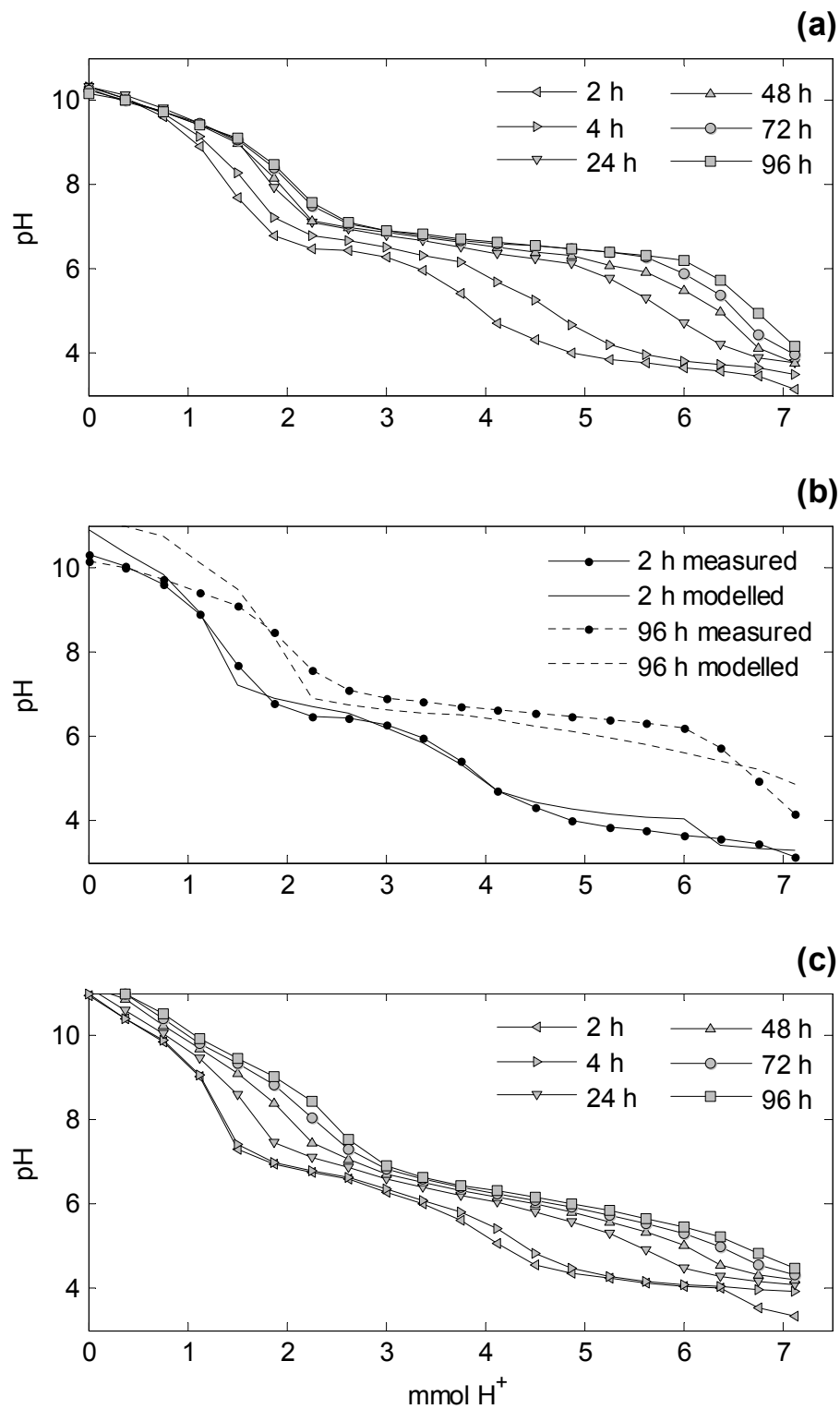


Fig. 1: Measured (a) and simulated acid neutralization curves at thermodynamic equilibrium (b) and including the kinetic dissolution of TCA and sodalite (c).

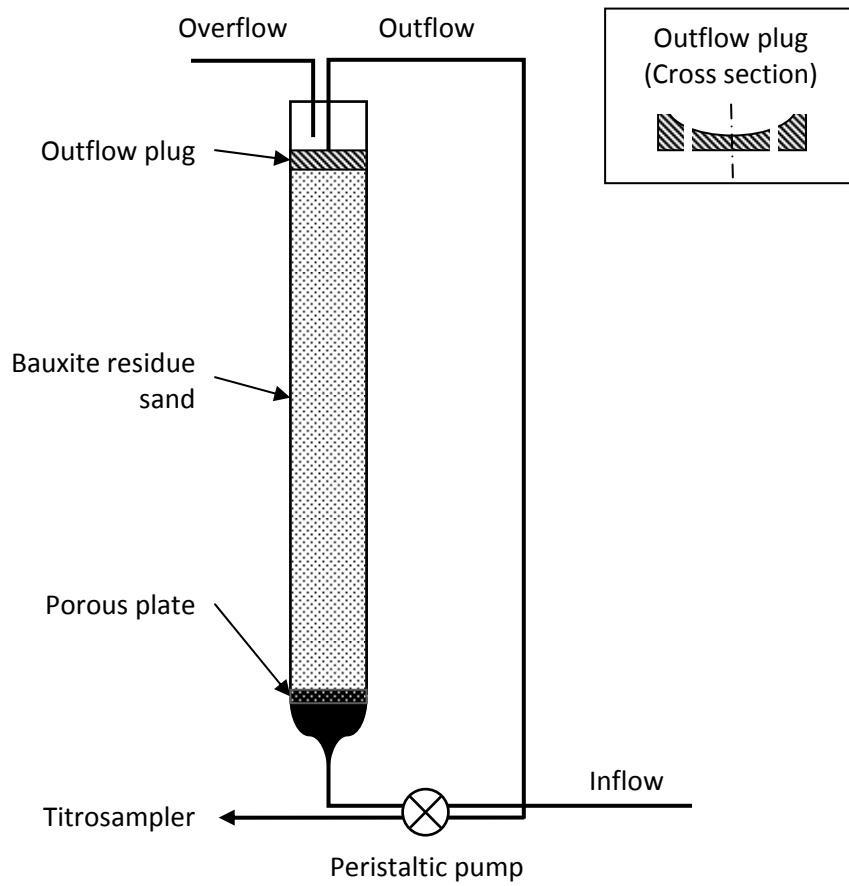


Fig. 2: Upward flow column experiment.

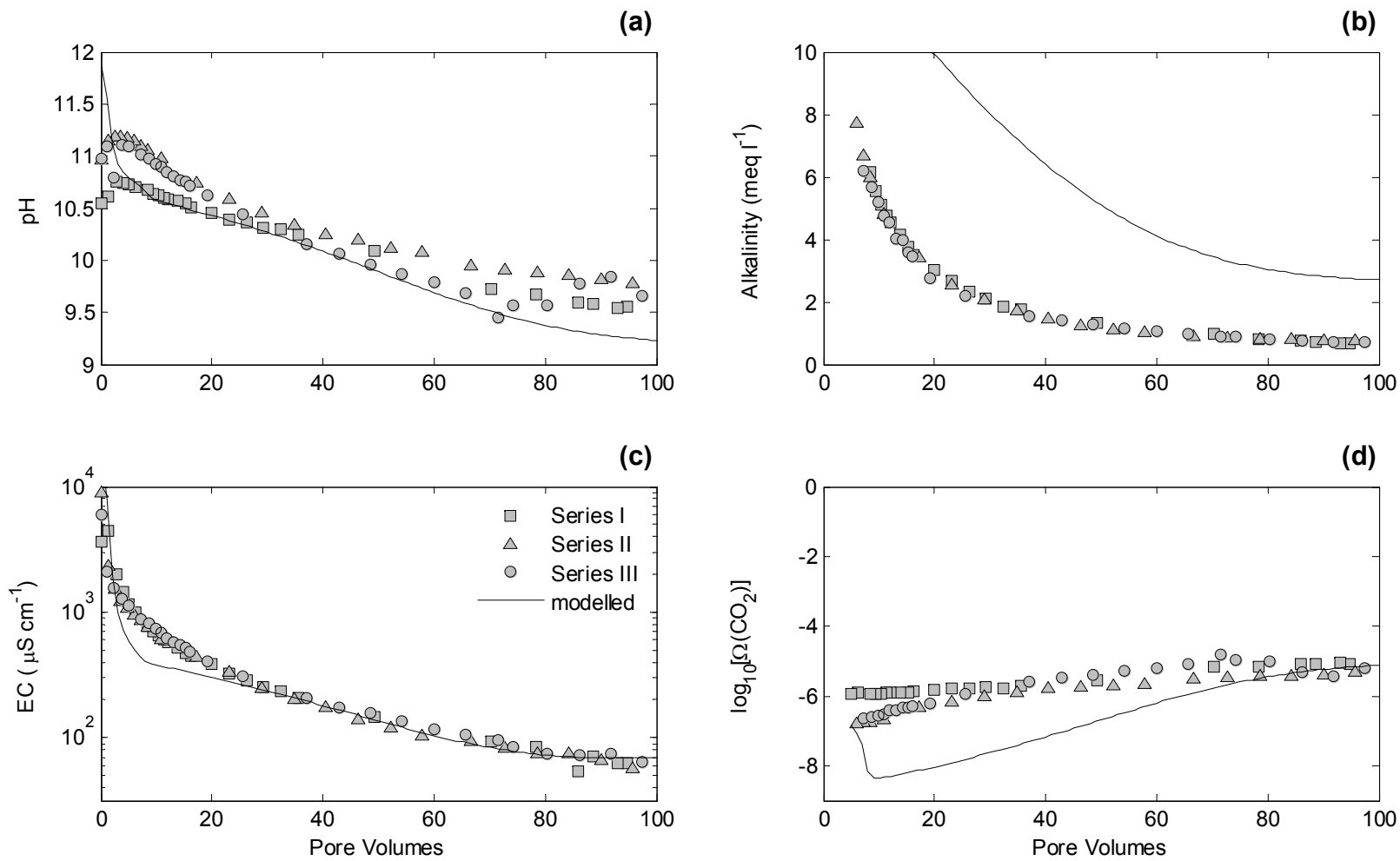


Fig. 3: Results of column experiment for pH (a), alkalinity (b), electrical conductivity (c) and calculated CO₂ saturation (d).

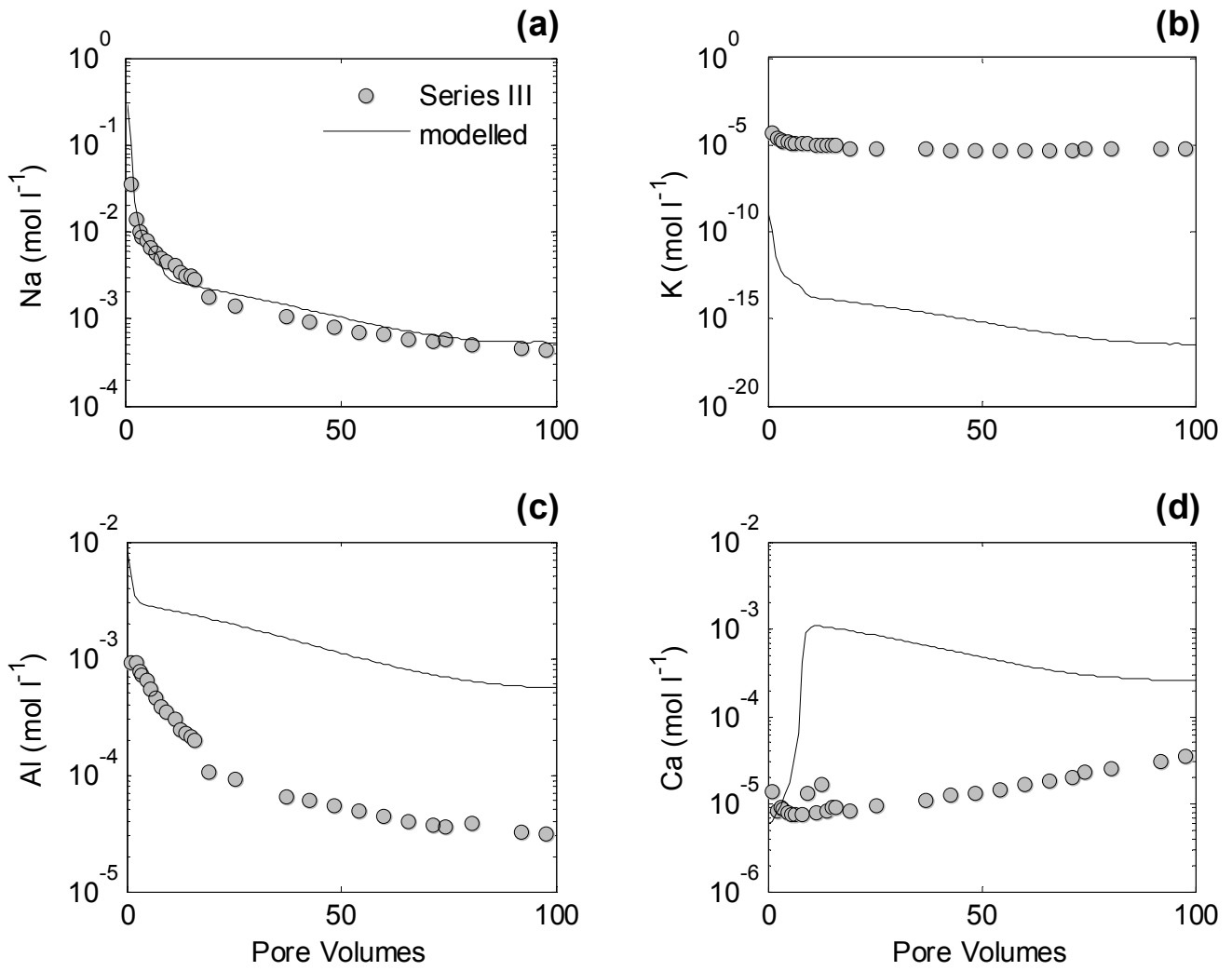


Fig. 4: Element concentrations (mol l^{-1}) in the column outflow for (a) Na, (b) K, (c) Al and (d) Ca.

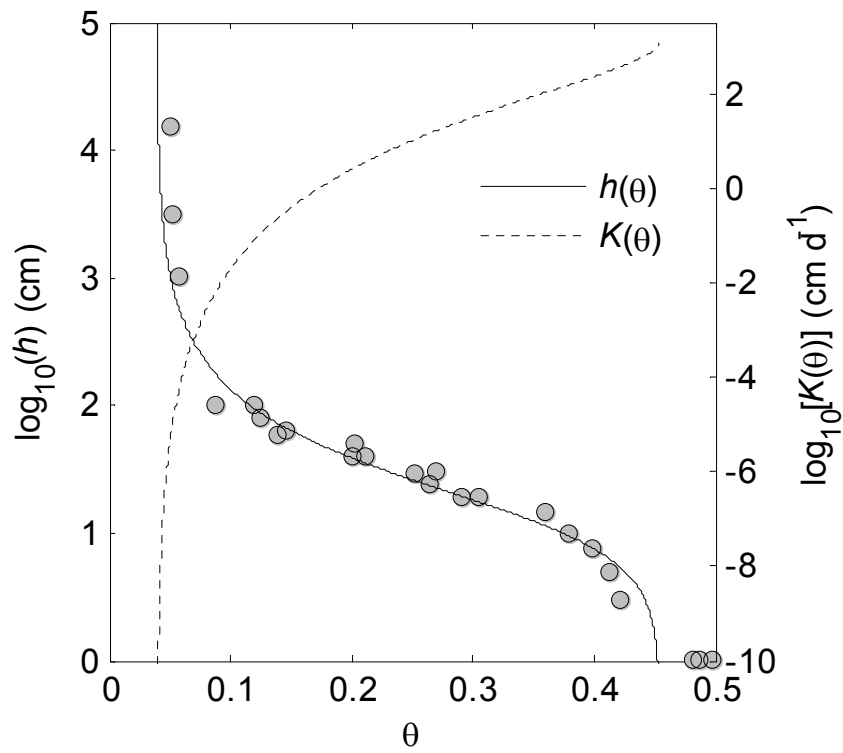


Fig. 5: Water retention and unsaturated hydraulic conductivity of residue sand at the soil surface according to the van Genuchten/Mualem model.

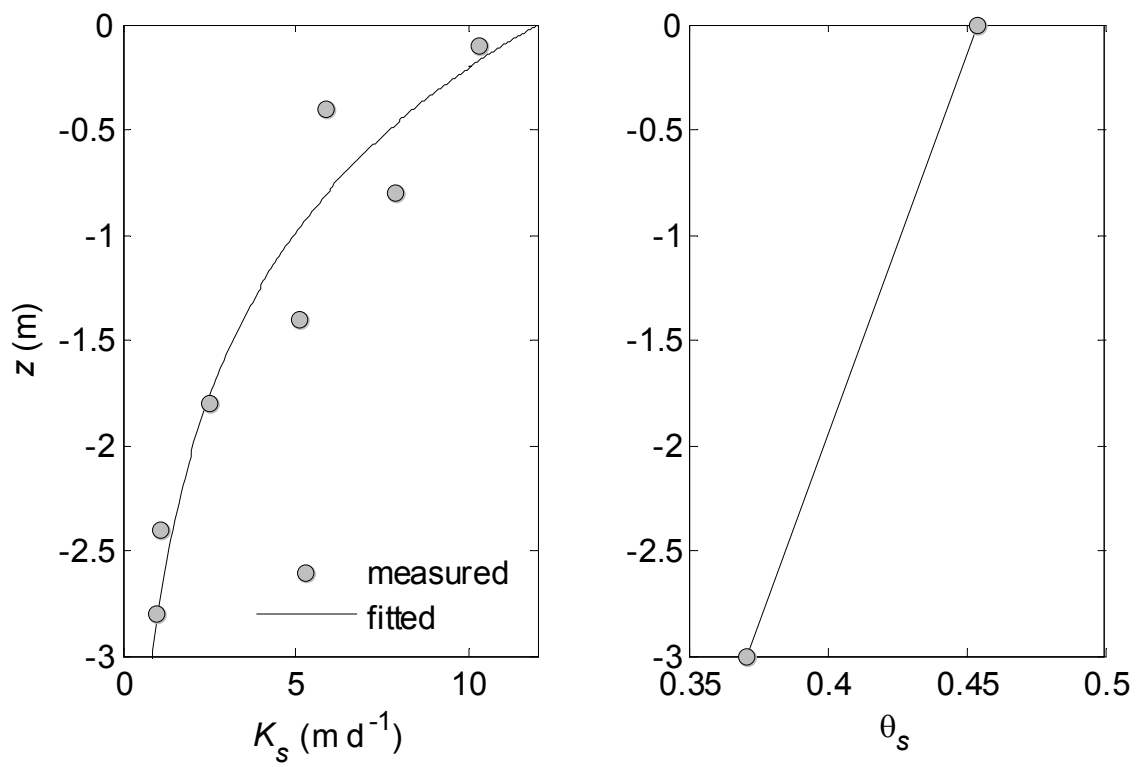


Fig. 6: Depth dependence of saturated hydraulic conductivity K_s (left) and saturated water content θ_s (right).

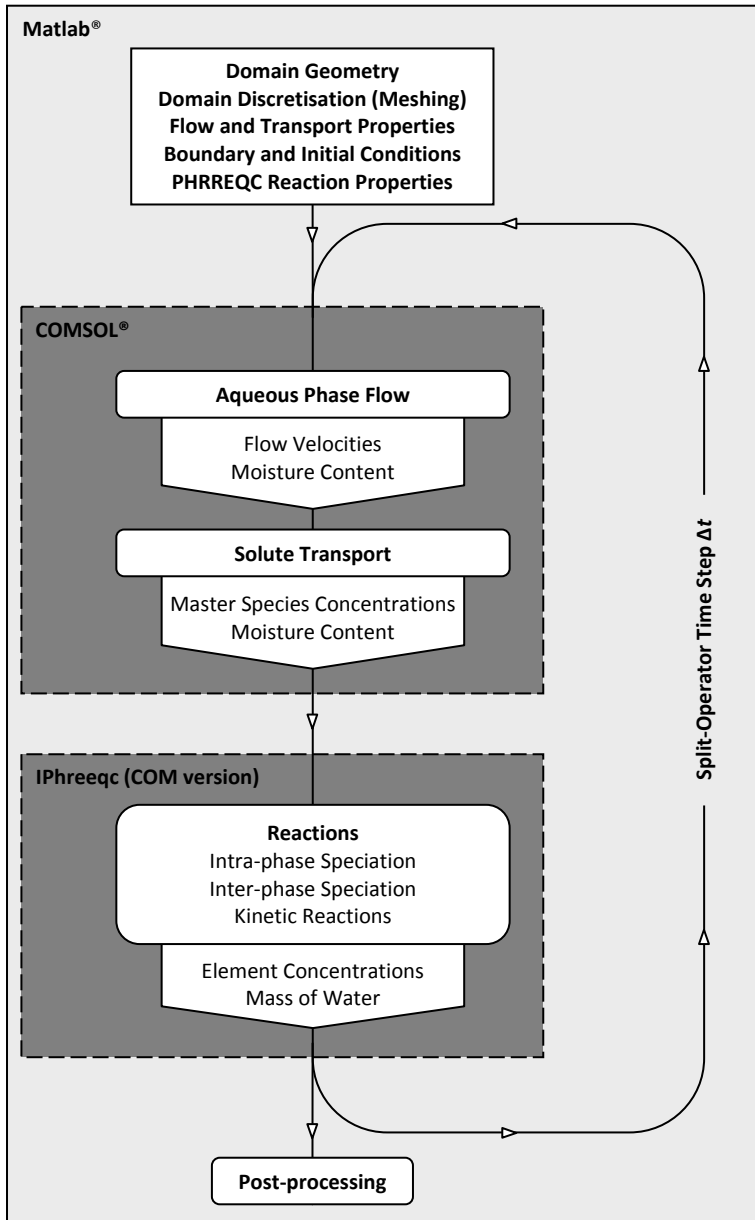


Fig. 7: Program flow and structure.

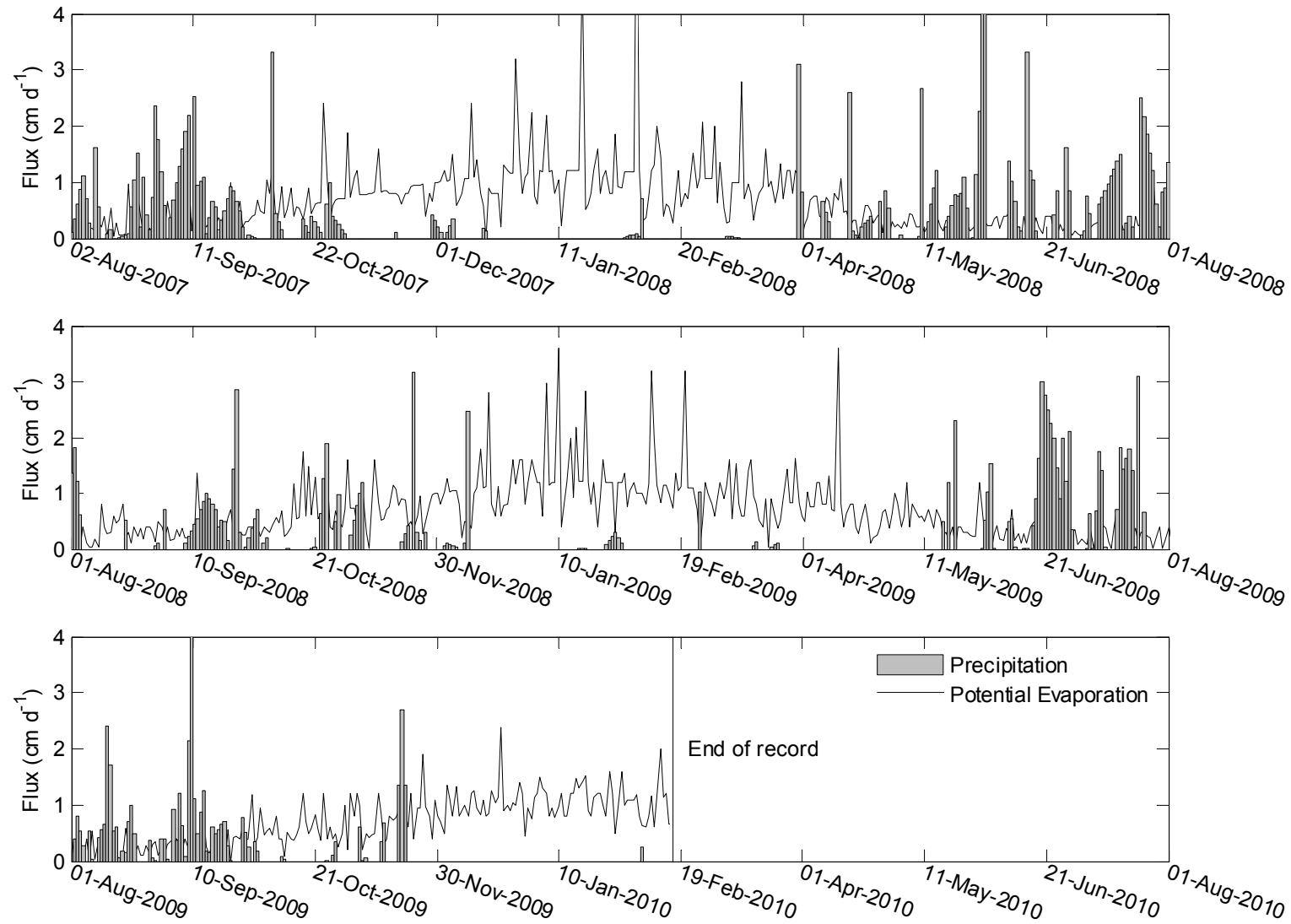


Fig. 8: Time series of rainfall and potential evaporation with reconstructed missing values.

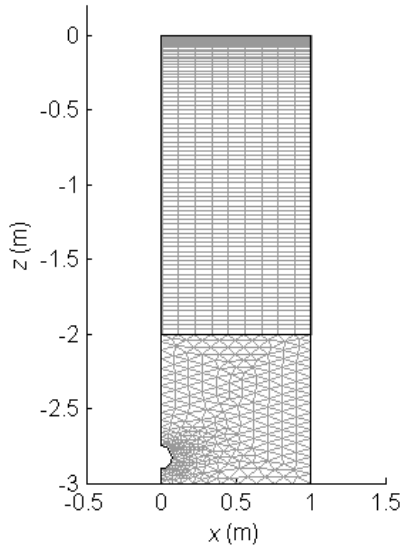


Fig. 9: Lysimeter simulation domain and finite element representation.

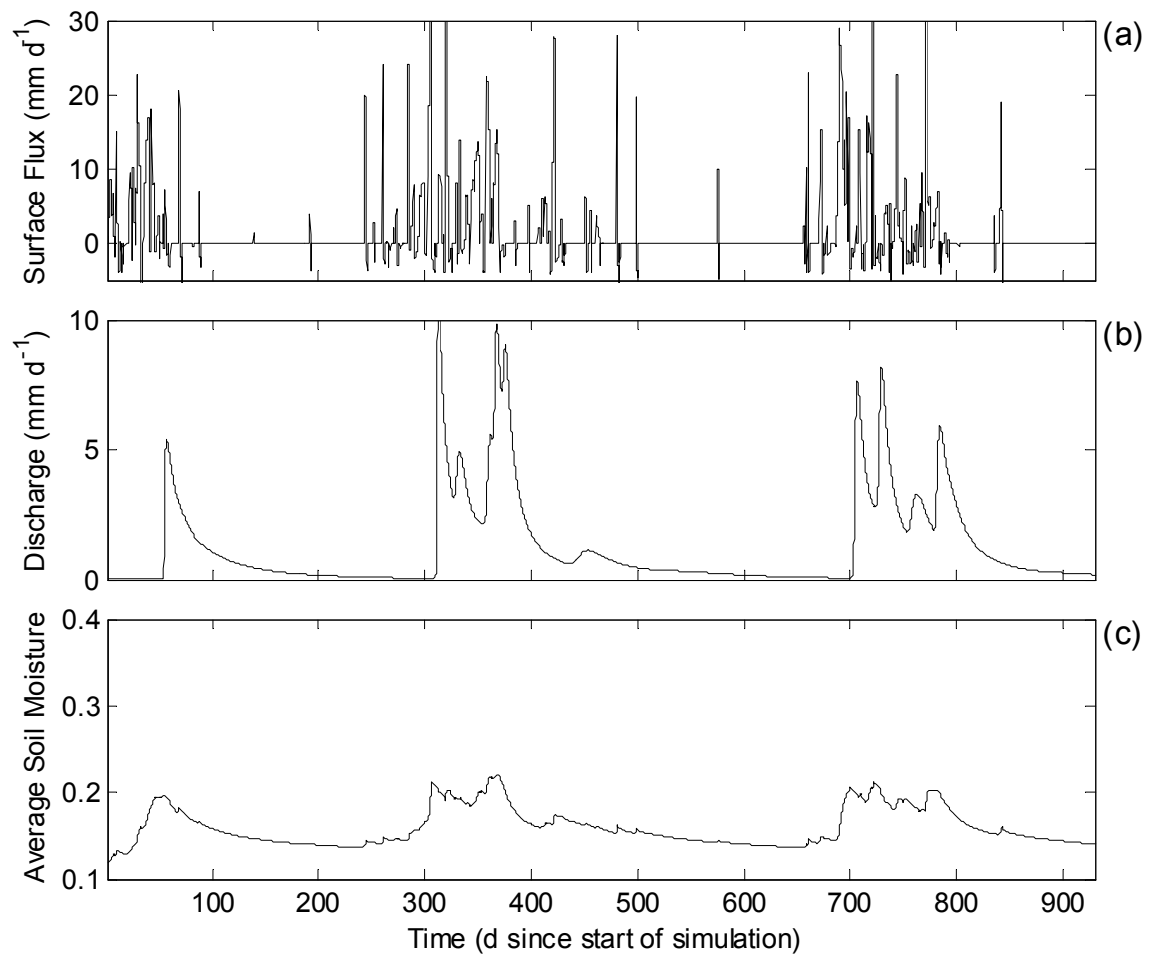


Fig. 10: Dynamic water balance of lysimeter simulation with (a) surface flux (mm d^{-1}), (b) drainage at the drainage pipe (mm d^{-1}) and (c) average soil moisture content θ .

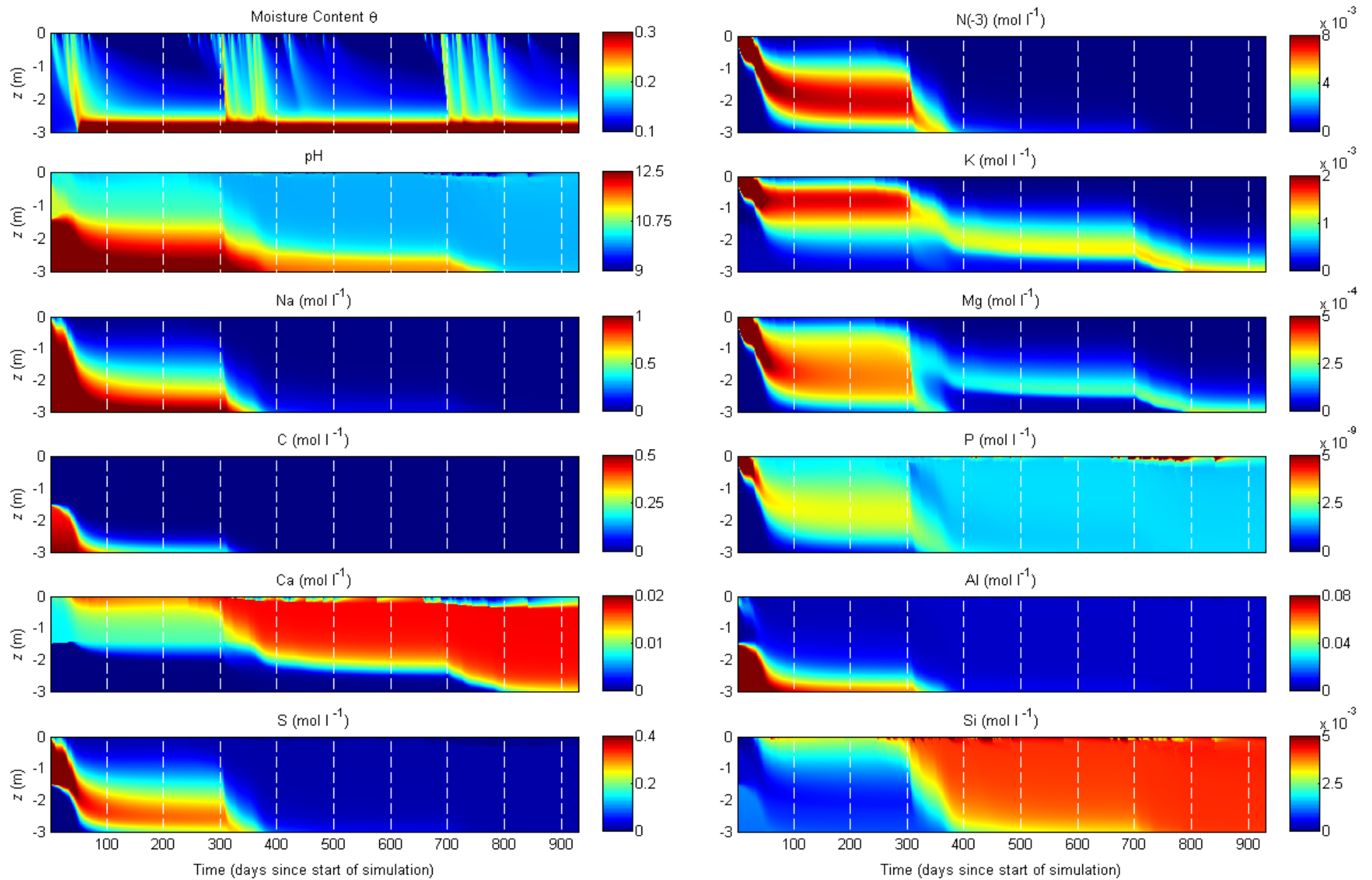


Fig. 11: Evolution of moisture content, pH and concentration of selected elements at the right domain boundary of the lysimeter simulation.

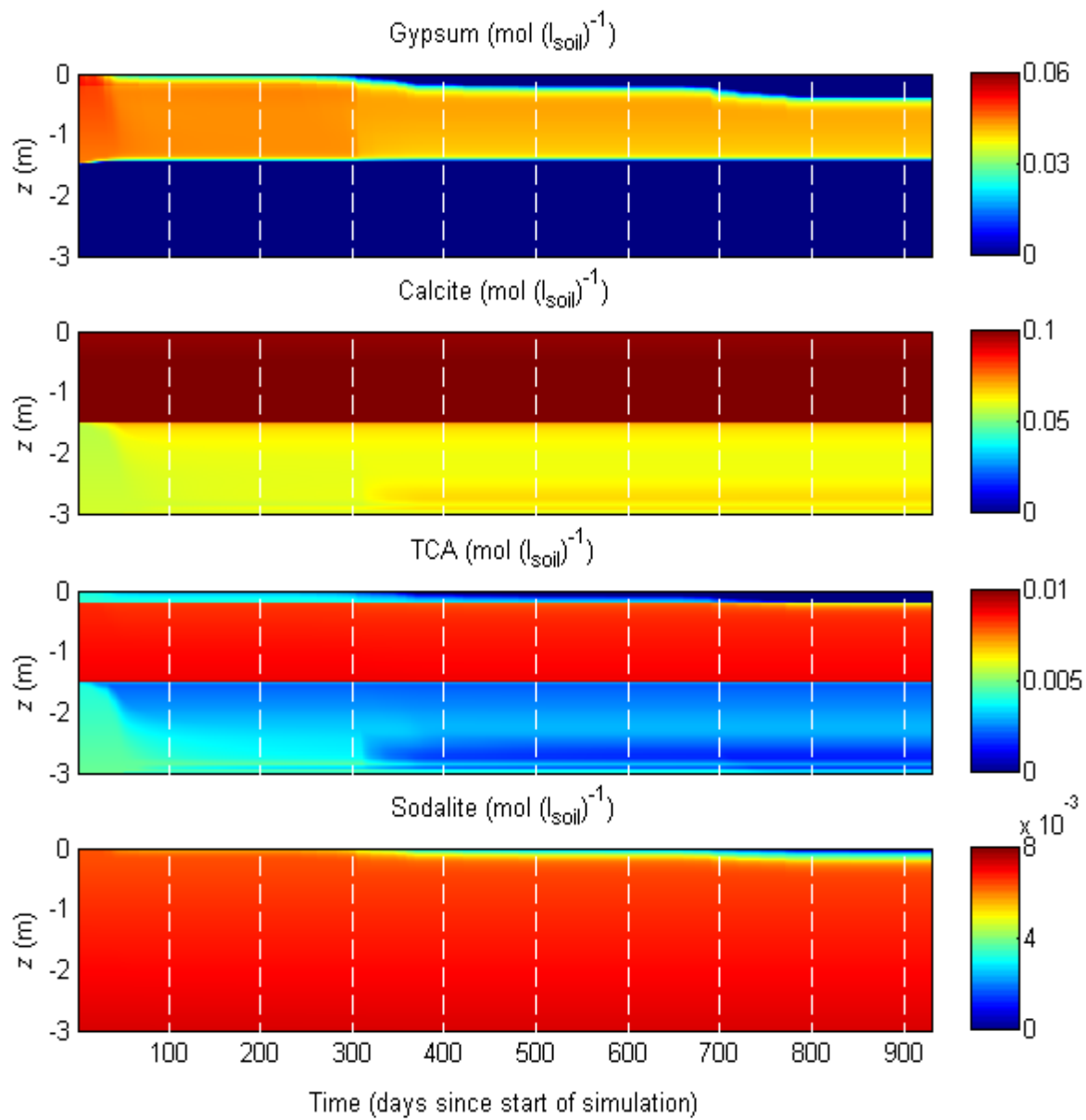


Fig. 12: Evolution of the main minerals at the right domain boundary of the lysimeter simulation.

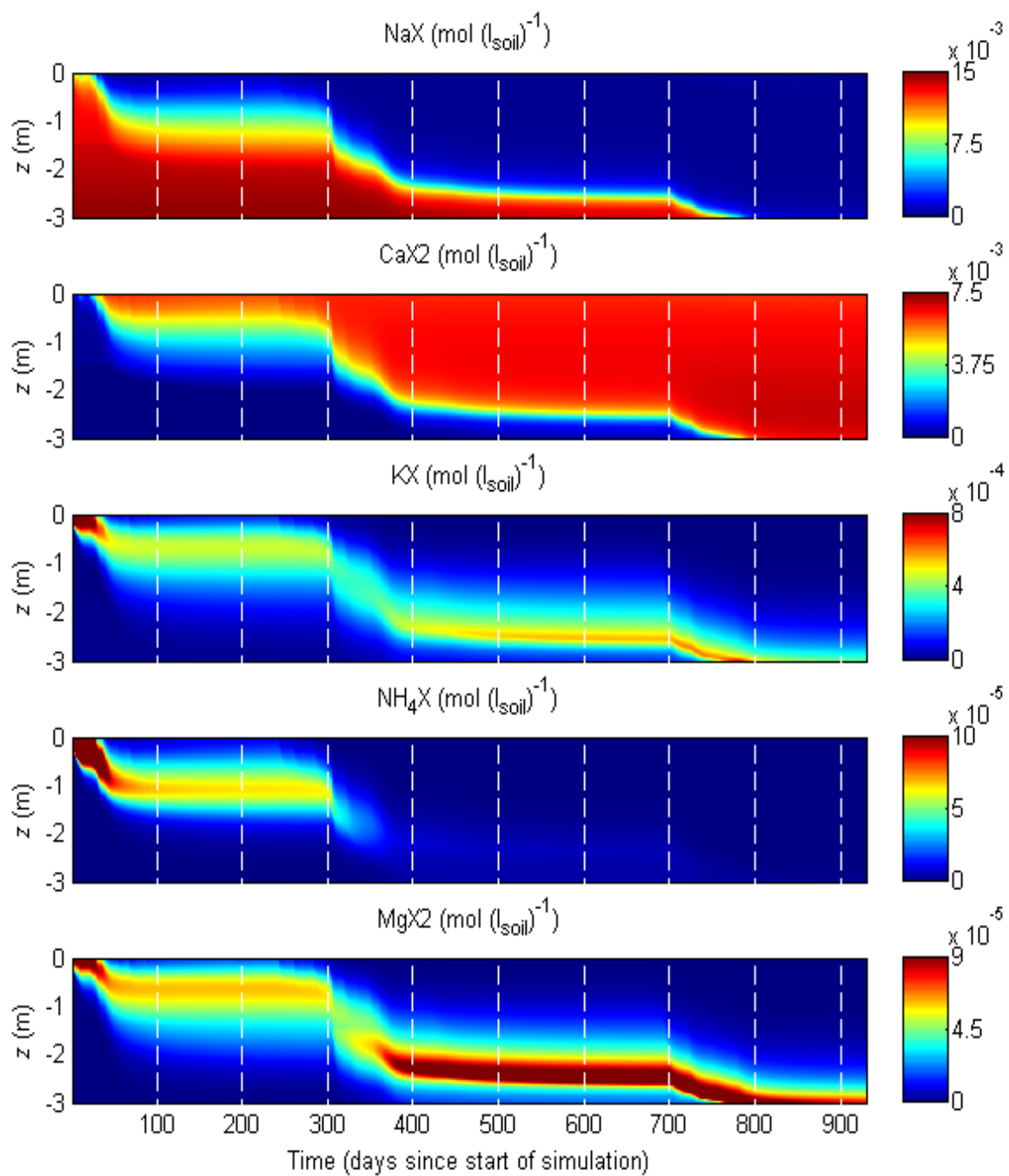


Fig. 13: Evolution of the exchanger composition at the right domain boundary of the lysimeter simulation.

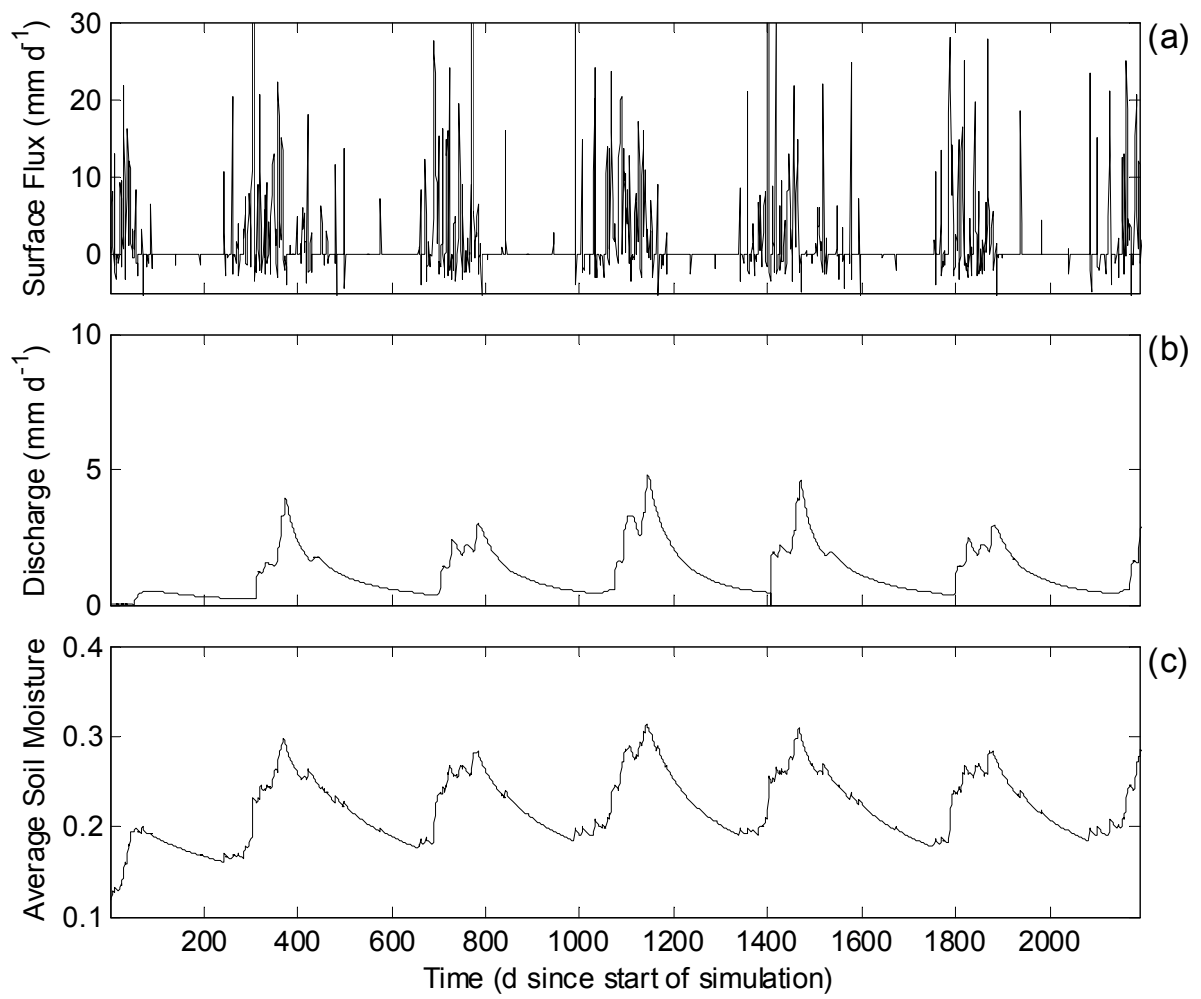


Fig. 14: Dynamic water balance of surface cover simulation, with (a) surface flux (mm d^{-1}), (b) drainage (mm d^{-1}) and (c) average soil moisture content θ .

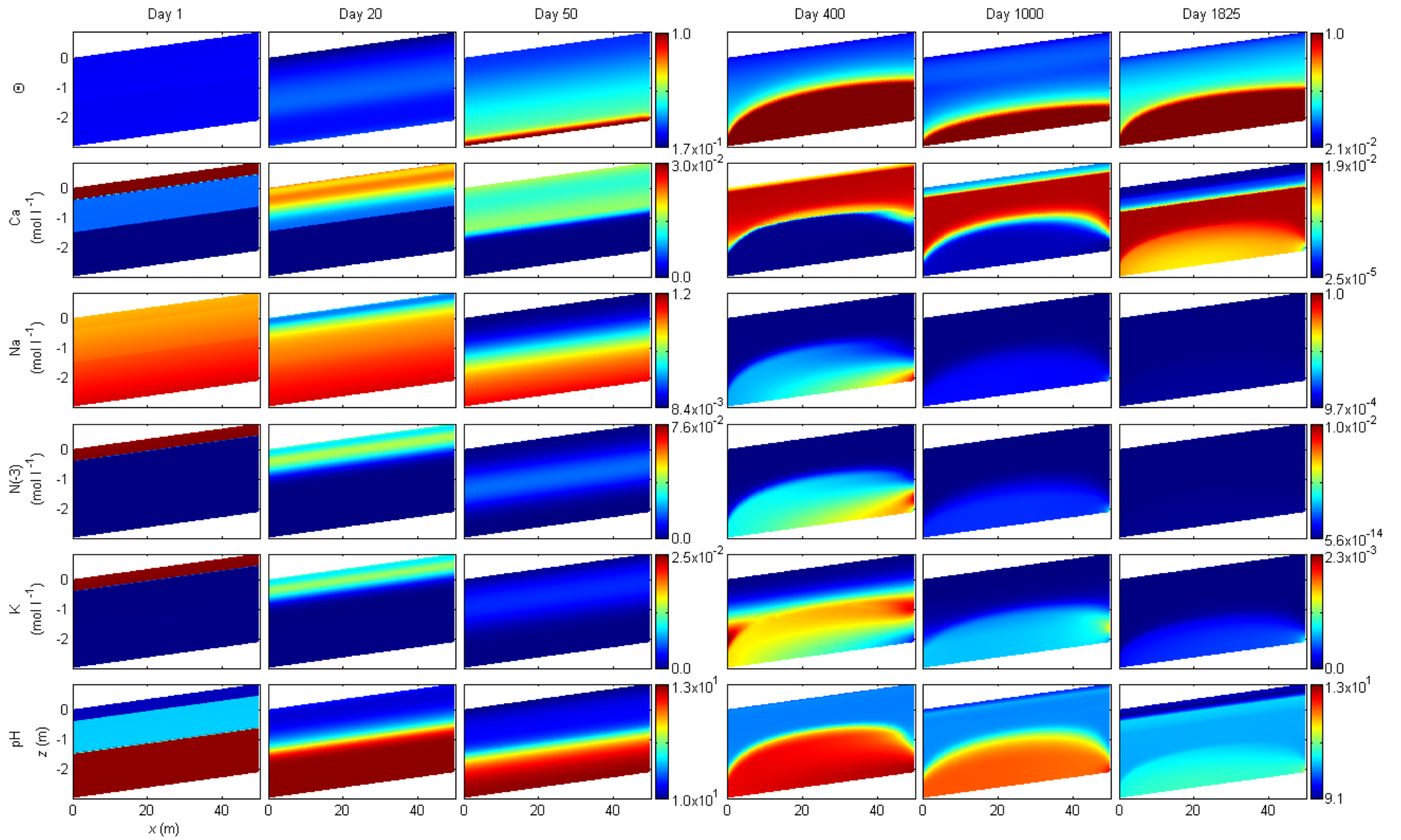


Fig. 15: Evolution of normalized moisture content, concentrations of selected elements and pH profiles of the surface cover simulation at 1, 20, 50, 400, 600 and 1825 d.

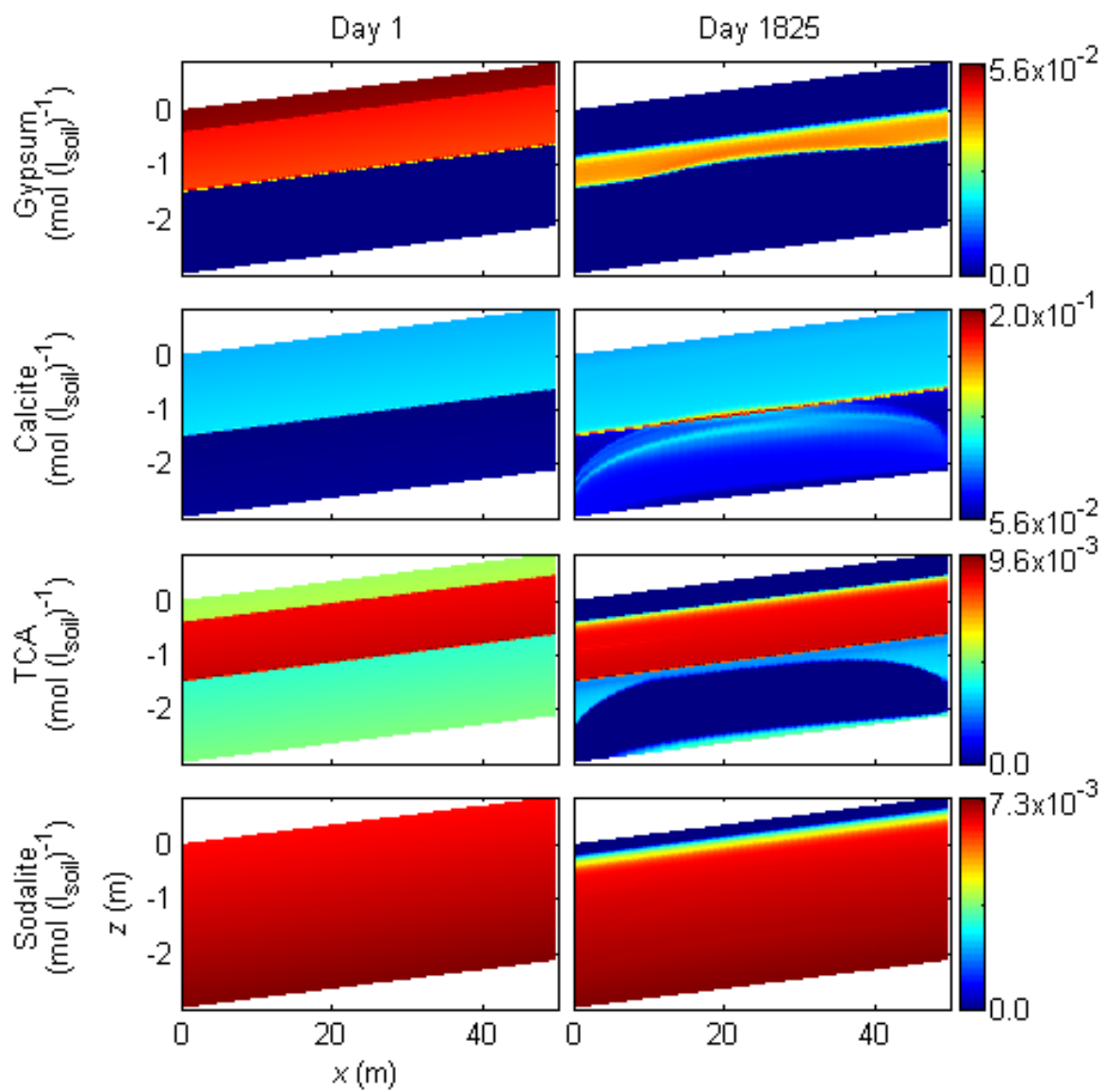


Fig. 16: Evolution of the main minerals of the surface cover simulation for 1 and 1825 d.

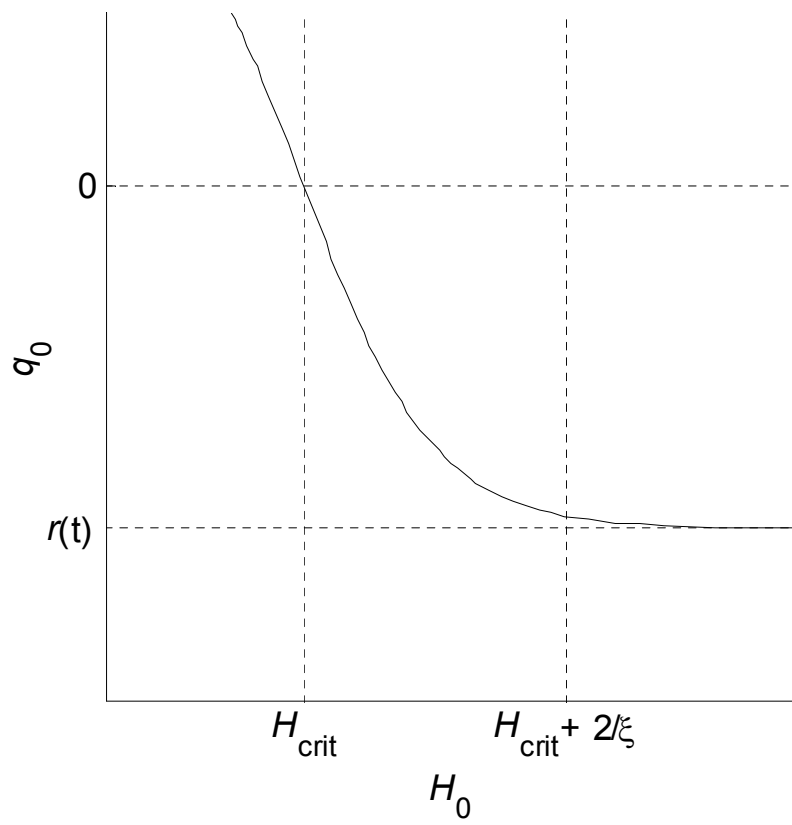


Fig. 17: Boundary flux during negative recharge in the vicinity of the critical pressure head H_a .

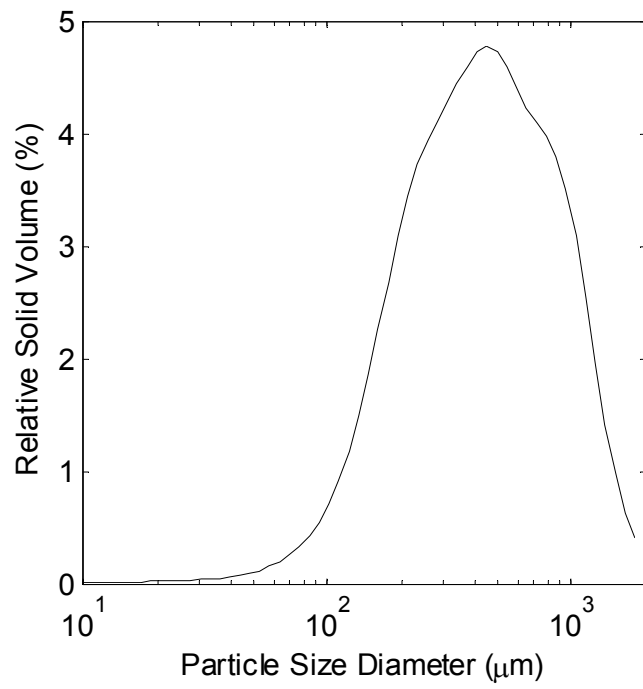


Fig. 18: Particle size distribution of washed residue sand.