

# Large-Eddy Simulation of the Convective Atmospheric Boundary Layer over Heterogeneous Land Surfaces



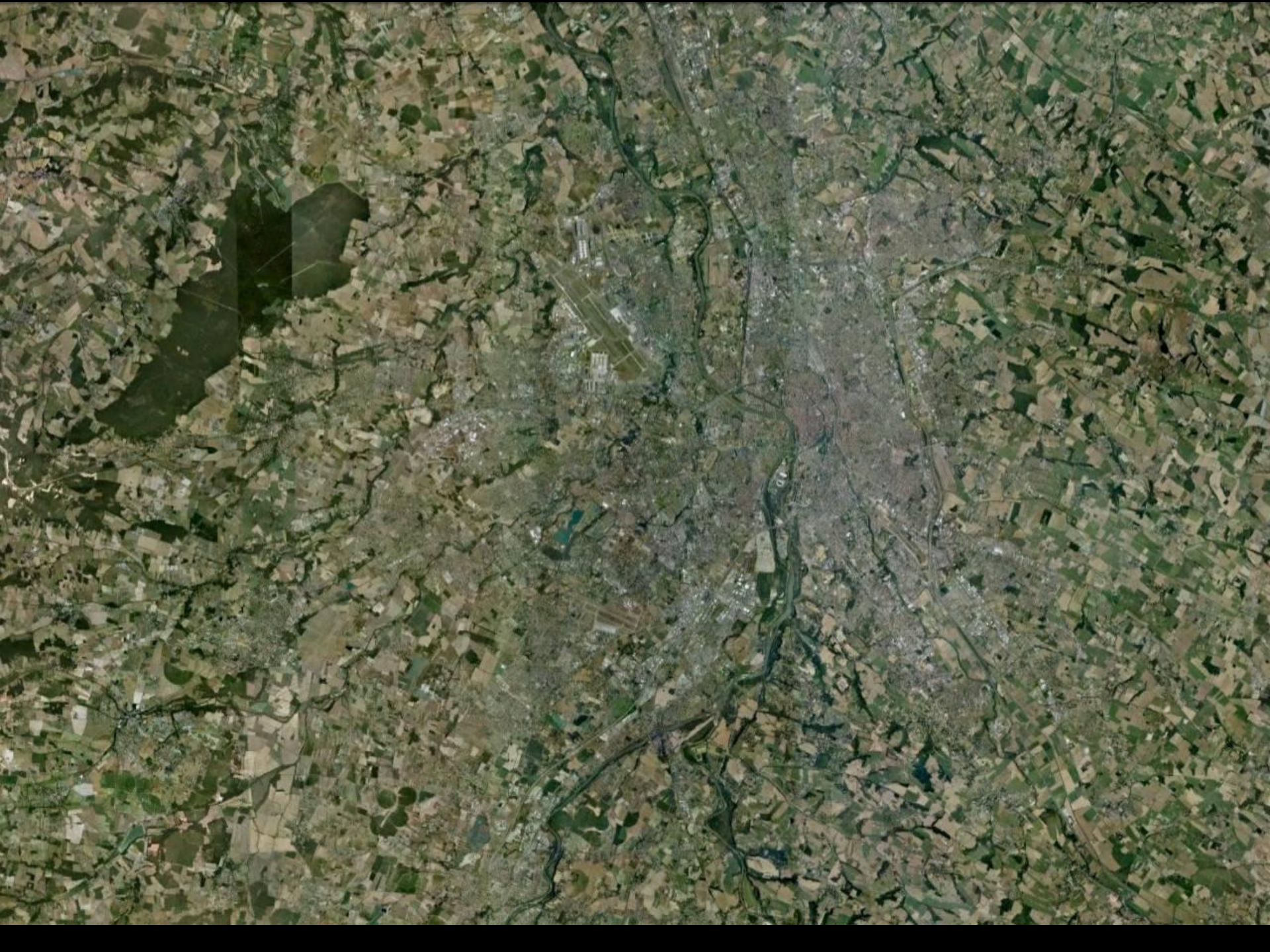
**Daniel Nadeau**

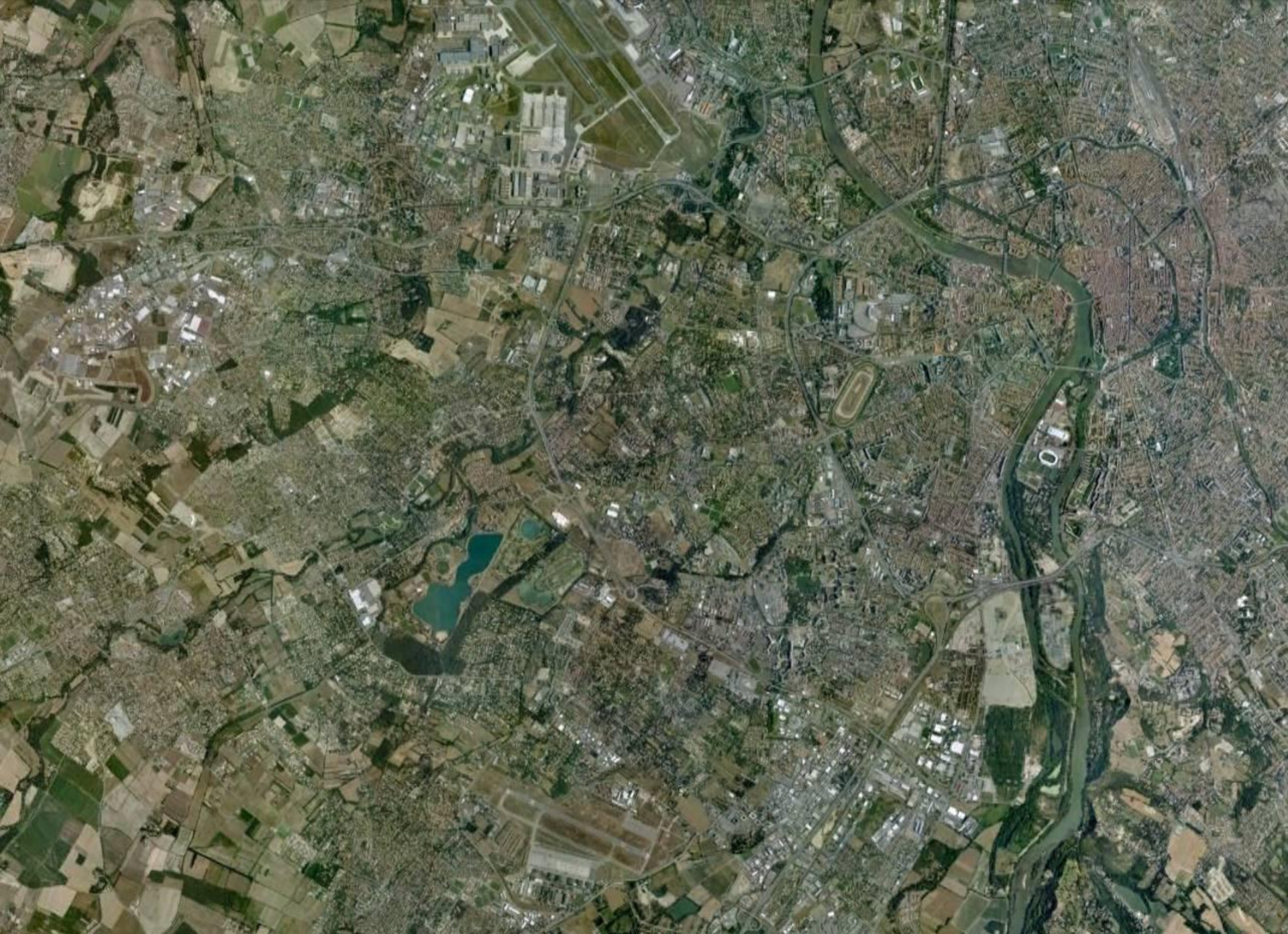
V. Kumar, C. Higgins, M. B. Parlange

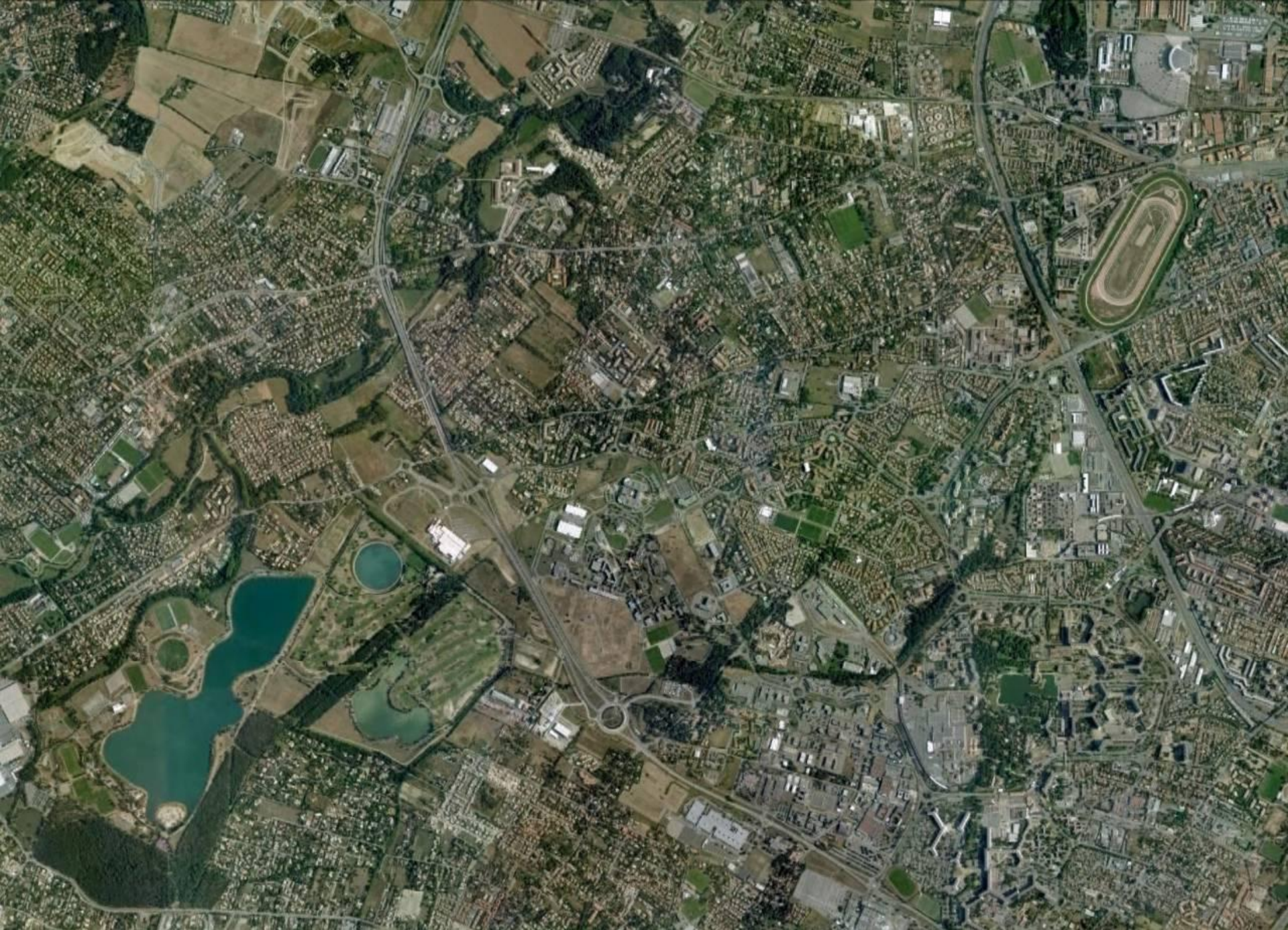
Toulouse, 2 October 2009

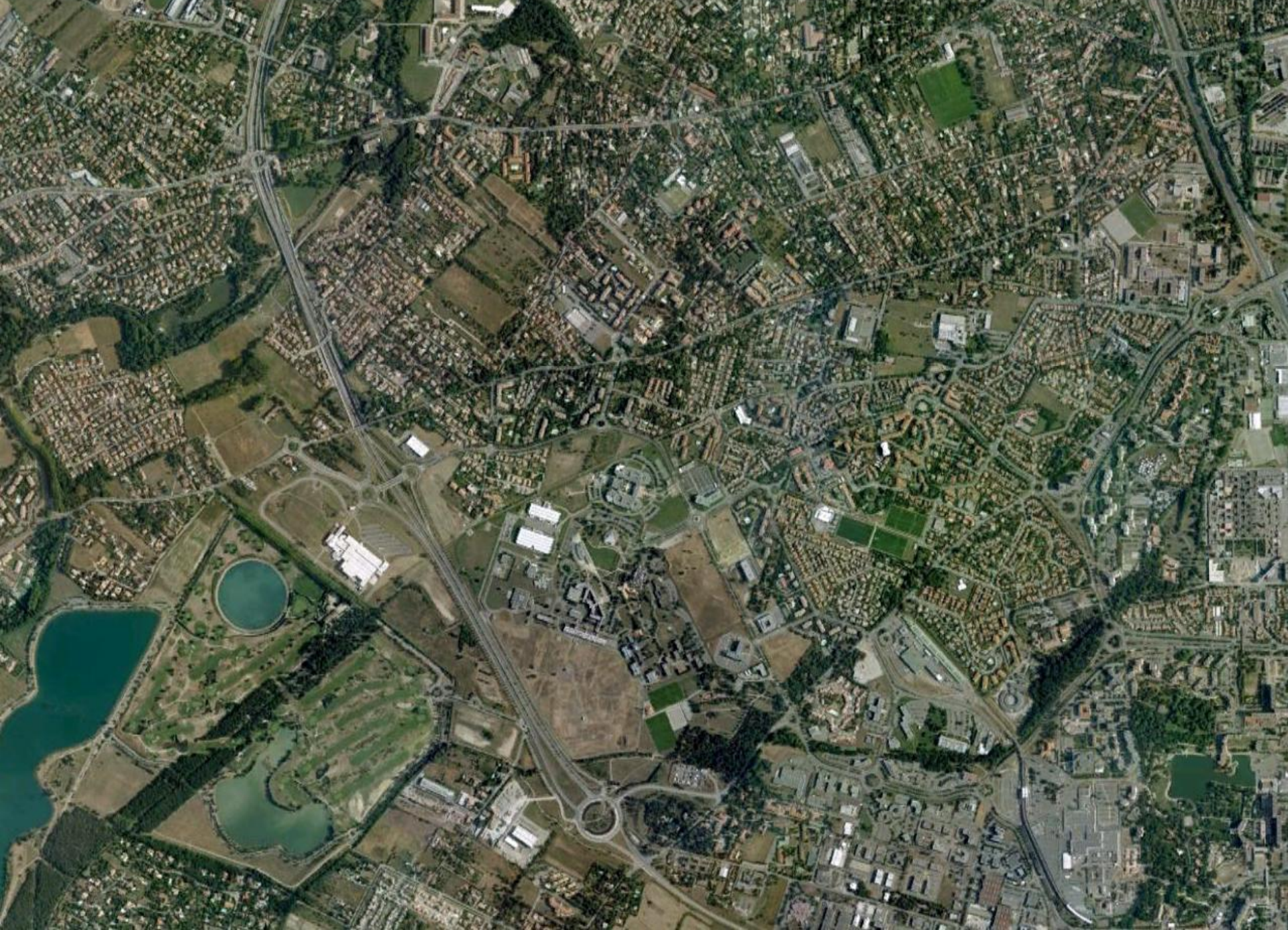








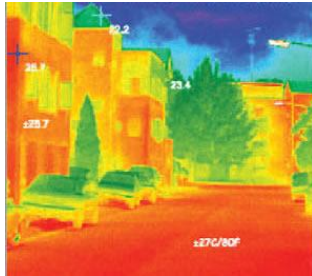




# Motivations

## Surface heterogeneities

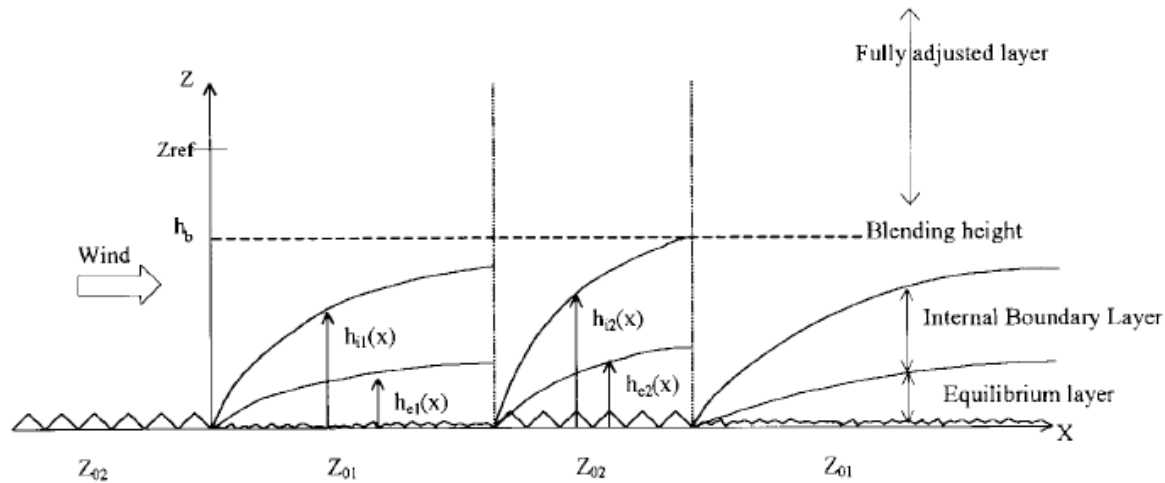
... in thermal properties (affects  $T_s$ )



... in shape, geometry (affects  $z_0$ )



What is the impact of these heterogeneities on the **blending heights**?



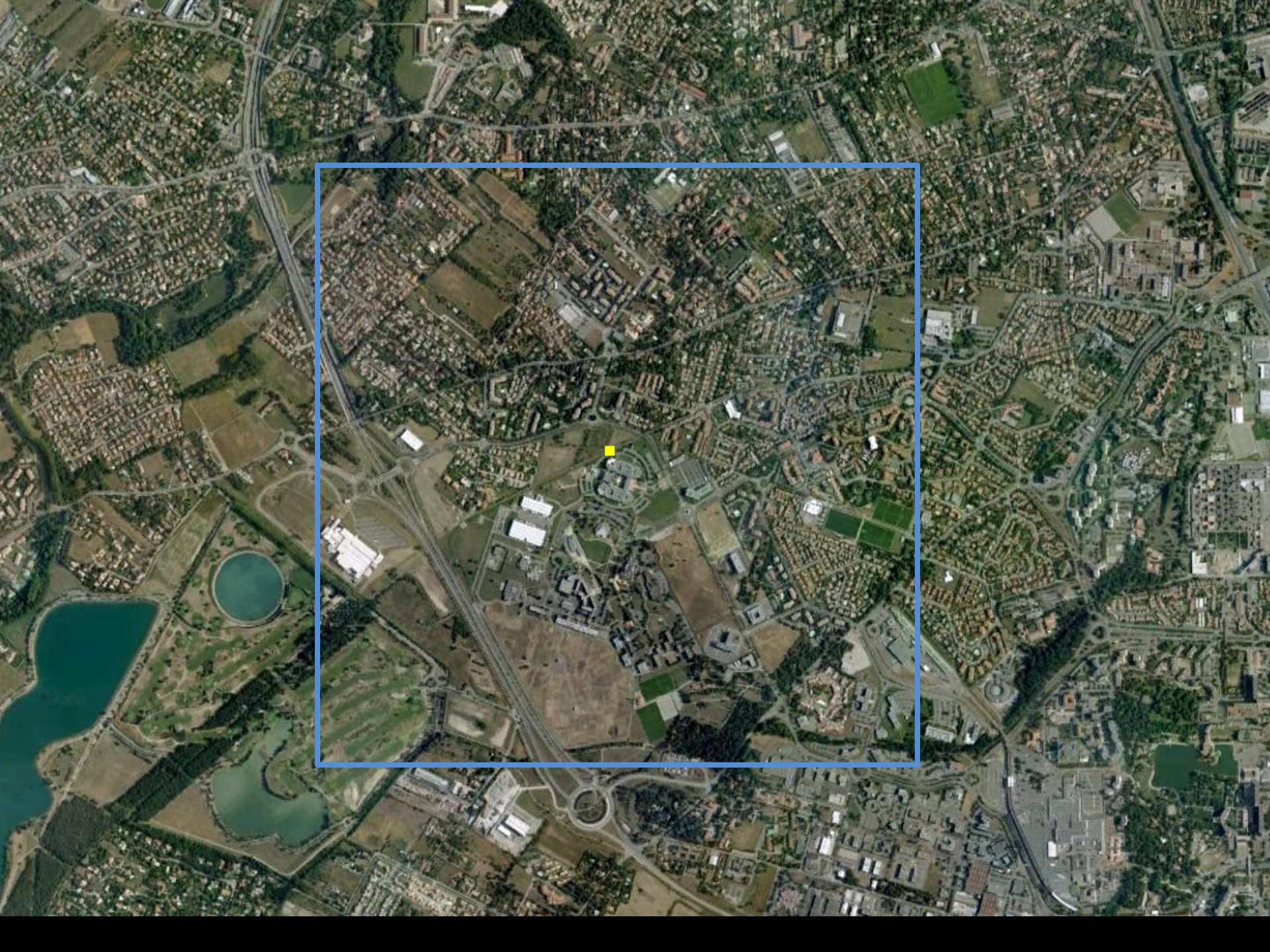
Source: Goode and Belcher, BLM, 1999



Mesoscale model grid size (~ 2 km)

LES grid size (~ 30 m)



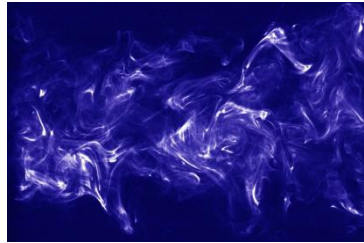


# Background

## Scales of motion in the ABL



largest scales ~ 1 km



smallest scales ~ 1 mm

---

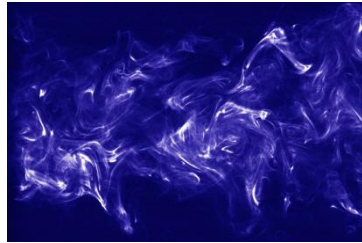
~  $10^6$

# Background

## Scales of motion in the ABL



largest scales ~ 1 km



smallest scales ~ 1 mm

~  $10^6$

**Impossible to resolve all these scales explicitly!**

# Background

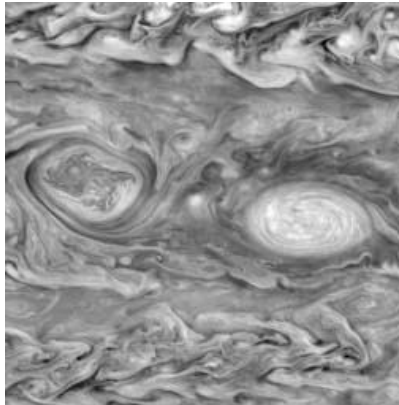
## Large-eddy simulation

### Large scale motions:

- affected by the BCs
- carry the turbulent fluxes of momentum and heat

### Small scale motions:

- more homogeneous and isotropic
- receive their energy from the larger scales



# Background

## Large-eddy simulation

### Large scale motions:

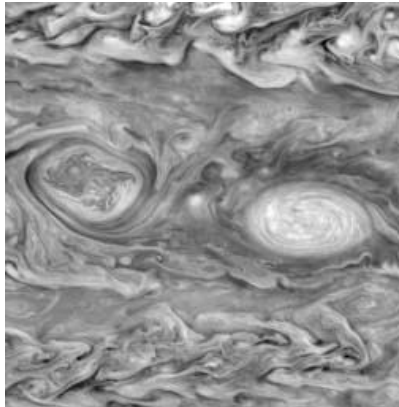
- affected by the BCs
- carry the turbulent fluxes of momentum and heat

**solve them**

### Small scale motions:

- more homogeneous and isotropic
- receive their energy from the larger scales

**parameterize them**



# Background

## Set of governing equations

- Incompressible Navier-Stokes
- Boussinesq approximation
- Coriolis forcing

$$\frac{\partial u_i}{\partial x_i} = 0$$

$\sim$	filtered variable
$f$	Coriolis parameter
$U_g, V_g$	geostrophic wind
$\tau_{ij}$	SGS stress tensor
$\pi_j$	SGS flux of temperature

$$\frac{\partial u_i}{\partial x_i} + u_j \left( \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right) = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + g \left( \frac{\theta - \langle \theta \rangle}{\langle \theta \rangle} \right) \delta_{i3} - \frac{\partial \tau_{ij}}{\partial x_j} + f (u_2 - V_g) \delta_{i1} - f (u_1 - U_g) \delta_{i2}$$

$$\frac{\partial \theta}{\partial t} + u_j \frac{\partial \theta}{\partial x_j} = -\frac{\partial \pi_j}{\partial x_j}$$

# Background

## Set of governing equations

- Incompressible Navier-Stokes
- Boussinesq approximation
- Coriolis forcing

$$\frac{\partial u_i}{\partial x_i} = 0$$

$\sim$	filtered variable
$f$	Coriolis parameter
$U_g, V_g$	geostrophic wind
$\tau_{ij}$	SGS stress tensor
$\pi_j$	SGS flux of temperature

$$\frac{\partial u_i}{\partial x_i} + u_j \left( \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right) = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + g \left( \frac{\theta - \langle \theta \rangle}{\langle \theta \rangle} \right) \delta_{i3} - \frac{\partial \tau_{ij}}{\partial x_j} + f (u_2 - V_g) \delta_{i1} - f (u_1 - U_g) \delta_{i2}$$

$$\frac{\partial \theta}{\partial t} + u_j \frac{\partial \theta}{\partial x_j} = -\frac{\partial \pi_j}{\partial x_j}$$

**A SGS model is needed!**



# Background

## Sub-grid scale model

- Lagrangian scale-dependant dynamic model (Bou-Zeid et al., PF, 2005)
- Constant SGS Prandtl number

*Smagorinsky model (Prandtl's mixing length hypothesis)*

$$v_T = C_s \cdot \Delta \cdot \Delta |S|$$

velocity scale  
length scale  
Smagorinsky constant

$$\rightarrow \tau_{ij}^{SMAG} = -2 (C_{s,\Delta} \Delta)^2 |S| S_{ij}$$

$$\rightarrow \pi_{ij}^{SMAG} = - \frac{(C_{s,\Delta} \Delta)^2 |S|}{Pr_{SGS}} \frac{\partial \theta}{\partial x_j}$$

$v_T$	turbulent eddy viscosity
$\Delta$	filter size
$S_{ij}$	resolved strain rate tensor
$\tau_{ij}^{SMAG}$	modelled SGS stress
$\pi_{ij}^{SMAG}$	modelled SGS scalar flux

# Model Setup

## LES code details

- Geostrophic forcing → can vary with height and time (Kumar et al., JAMC, 2009, accepted)
- Temperature is implemented, but not humidity
- 2<sup>nd</sup> order centered finite differences in a staggered grid formulation in the vertical direction
- Spectral code in the horizontal directions
- Monin-Obukhov Similarity applied at the first grid point
- Time integration: 2<sup>nd</sup> order Adams-Bashforth method
- Parallelization (MPI) using a domain decomposition with horizontal slices
- Dealiasing of nonlinear terms in Fourier space using the 3/2 rule

**Used in several studies of the ABL:** (Albertson & Parlange, AWR, 1999)  
(Albertson & Parlange, WRR, 1999)  
(Porté-Agel et al., JFM, 2000)  
(Bou-Zeid et al., PF, 2005)  
(Kumar et al., WRR, 2006)  
(Yue et al., EFM, 2008)

# Model Setup

## Boundary conditions

**LITFASS – 2003** (Lindenberg Inhomogeneous Terrain - Fluxes between Atmosphere and Surface: a long-term Study)

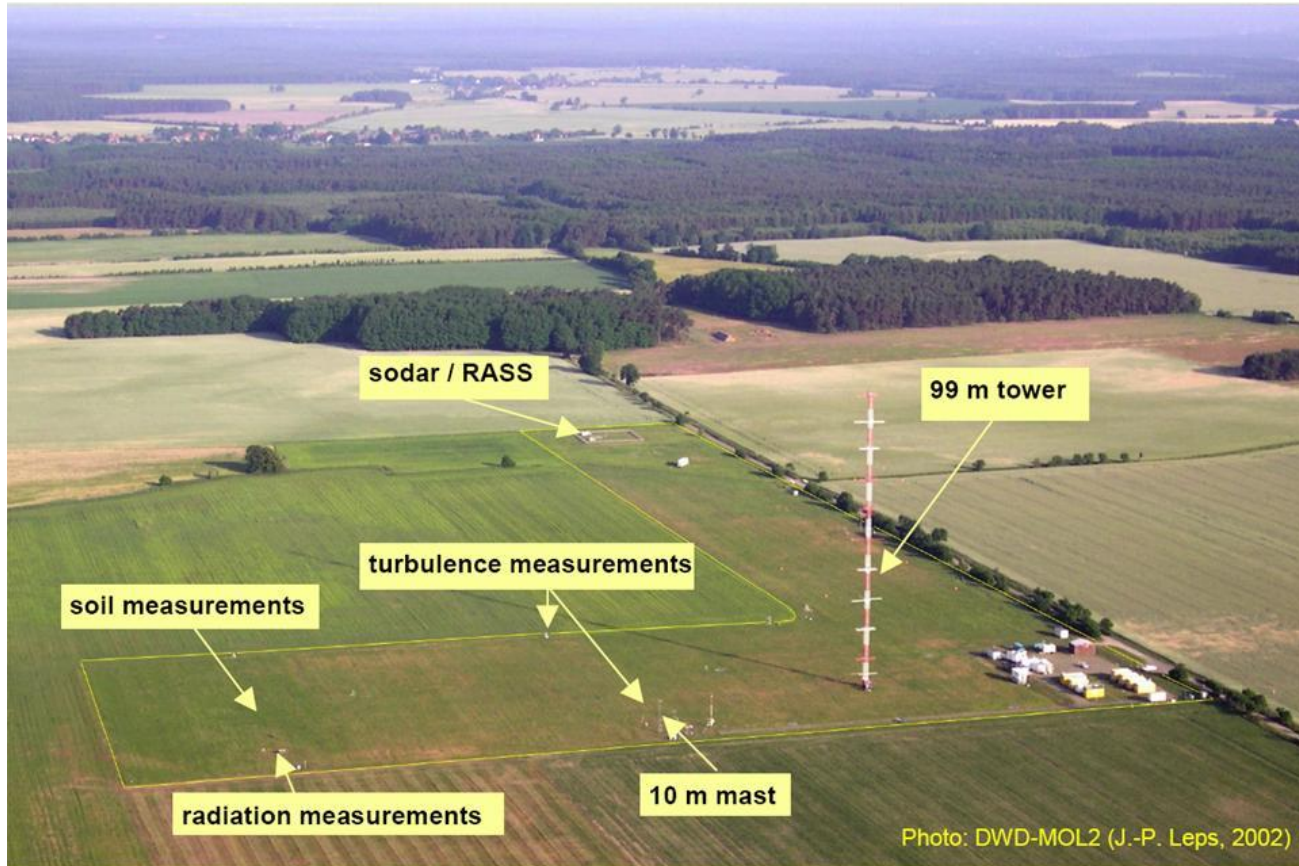
- Strong heterogeneities over flat terrain
- 20 x 20 km area
- 99-m meteorological mast
- Energy balance weather stations over different surface types
- Regular radiosonde launches
- and much more...



**Ideal for a LES validation over heterogeneous terrain!**

# Model Setup

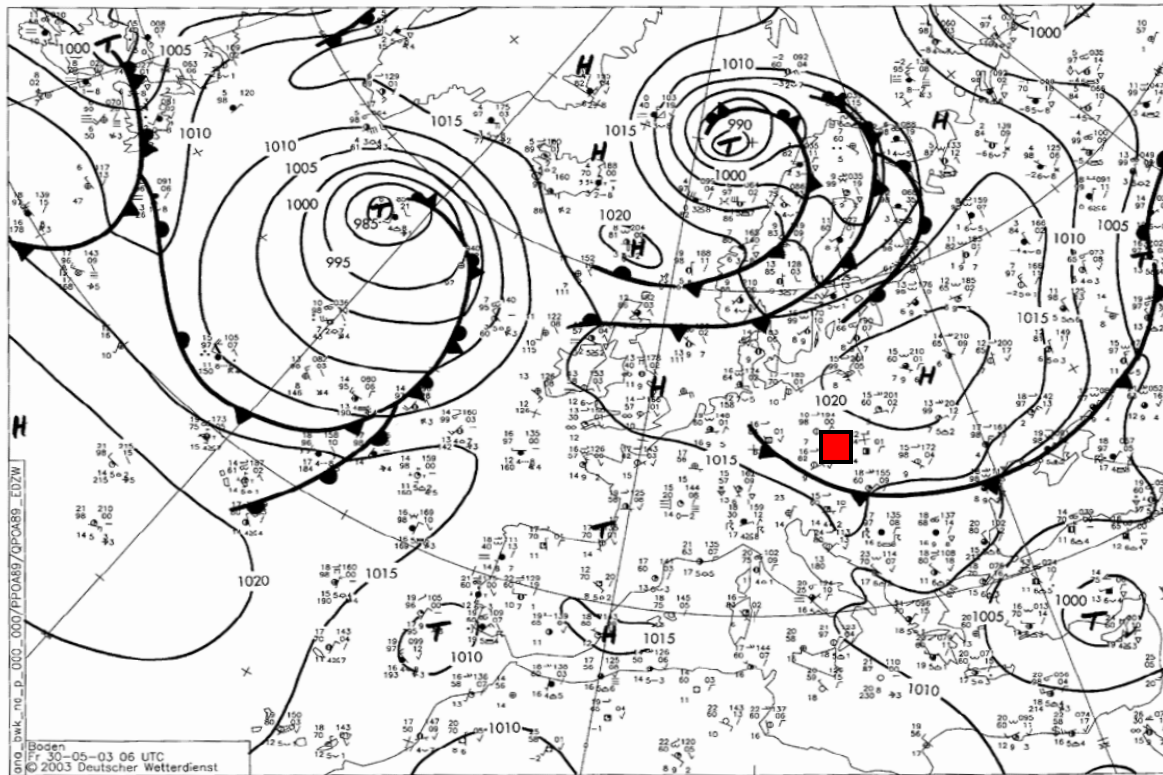
Center of the LES domain: the 99 m tower



# Model Setup

**30 May 2003**

- anticyclonic conditions
- no clouds
- cold easterly winds



# Model Setup

## Simulation details

**Number of grid points :** 128 x 128 x 128 (~ 2.1 million)

**Domain size –  $L_x, L_y, L_z$  :** 6 km x 6 km x 3 km

Horizontal mesh spacing –  $\Delta x, \Delta y$  : 47.9 m

Vertical mesh spacing –  $\Delta z$  : 23.4 m

Number of iterations : 180 000 with  $\Delta t = 0.1$  sec (total of 5 h)

**Number of processors:** 16 CPUs

Geostrophic wind  $U_g$  : -5 m/s

Initial conditions for wind speed : log-profile with randomly imposed TKE

Initial conditions for temperature : convective profile with randomly imposed TKE

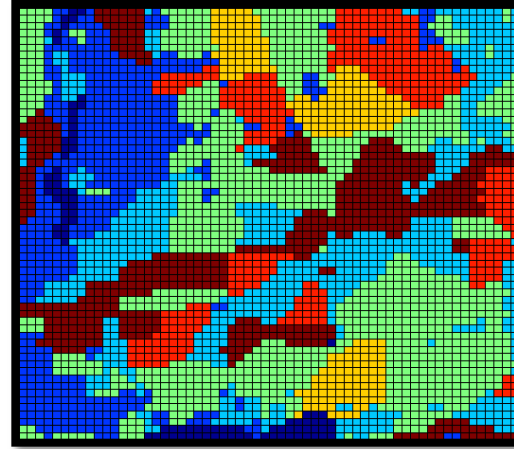
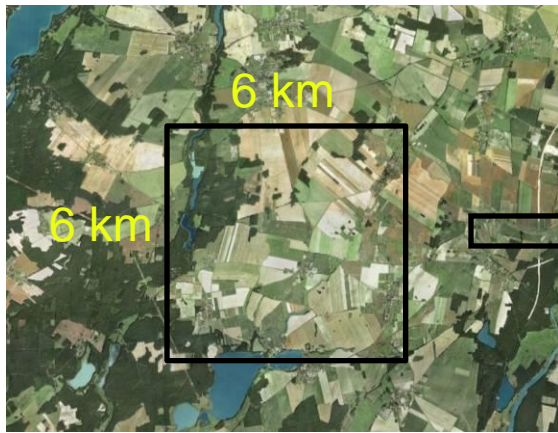
CBL inversion strength : 0.01 K/m

Top boundary condition : stress-free

**Warm-up period :** first 4 h of simulation

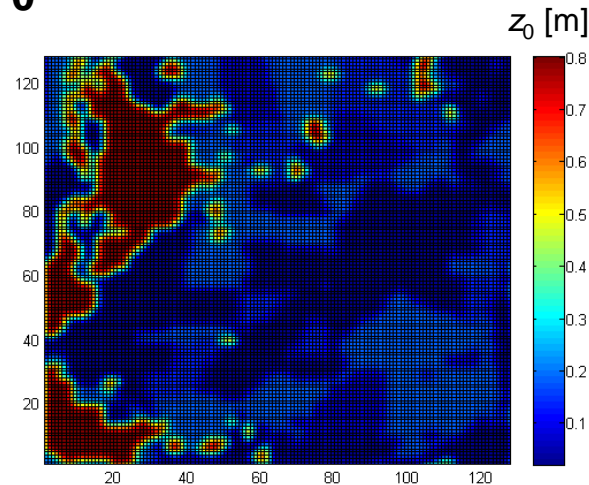
# Model Setup

## Surface type fields



- maize
- triticale
- barley
- rye
- grass
- forest
- water

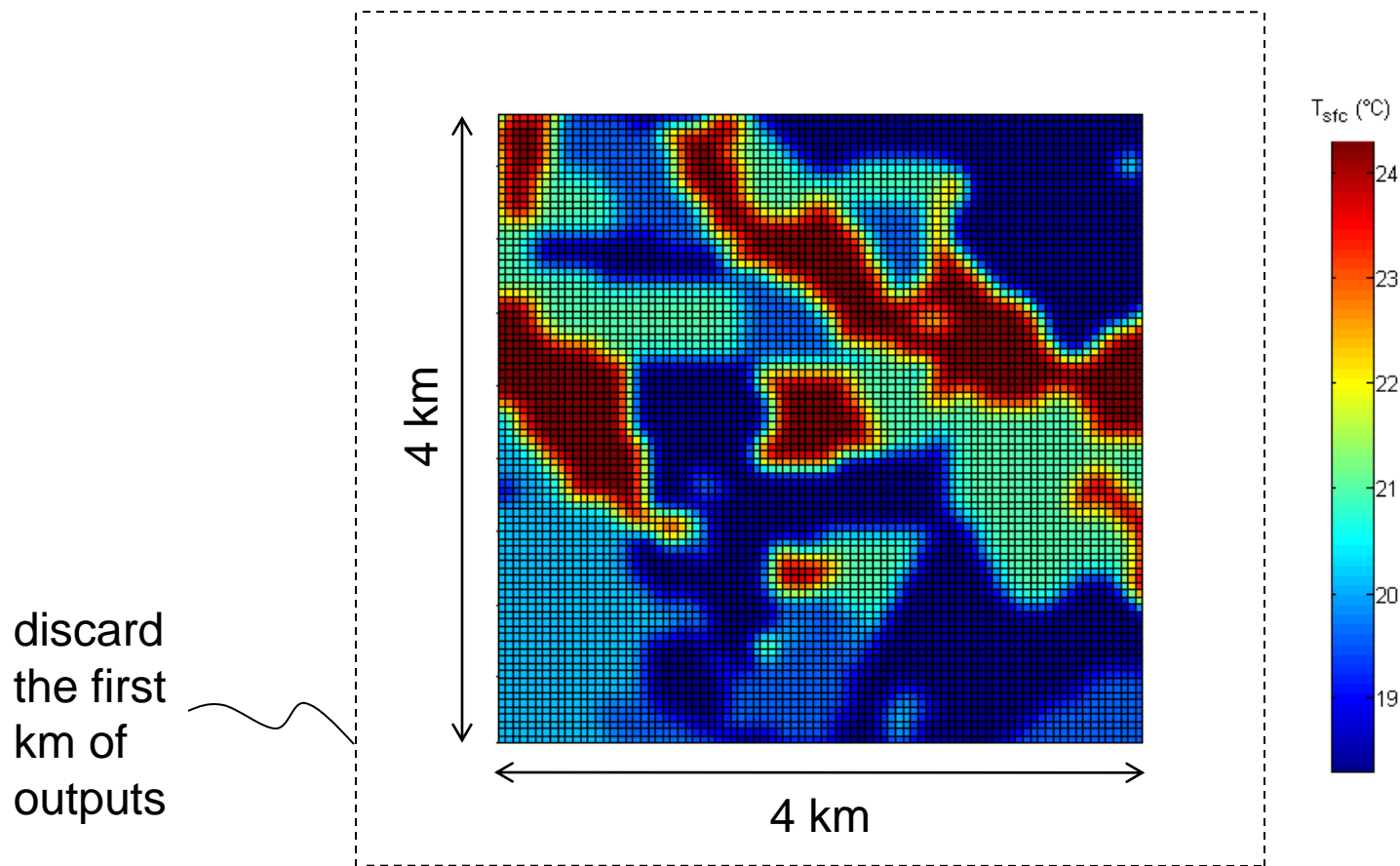
## Surface roughness $z_0$



# Results

## Convective heterogeneous test case

- Uniform  $z_0$  ( $\approx 0.2$  m)
- Patches of surface temperature from 30 May 2003 at 7 UTC



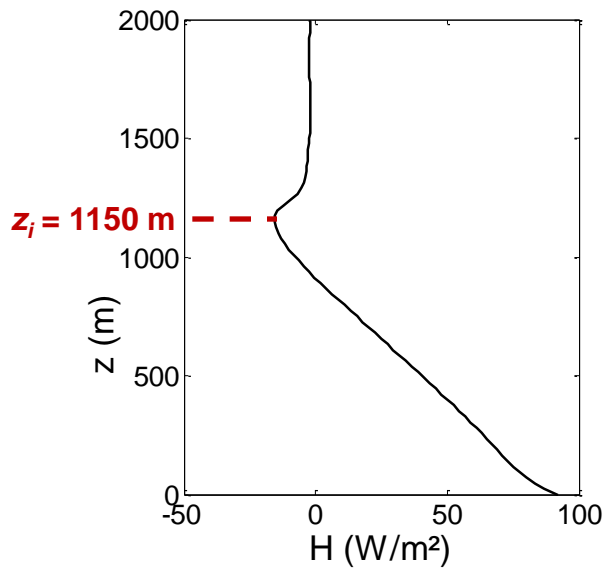


# Results

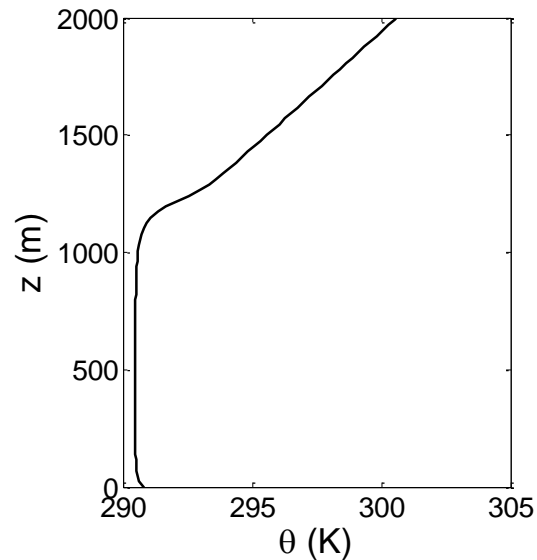
## Convective heterogeneous test case

*Time-averaged and horizontally averaged vertical profiles*

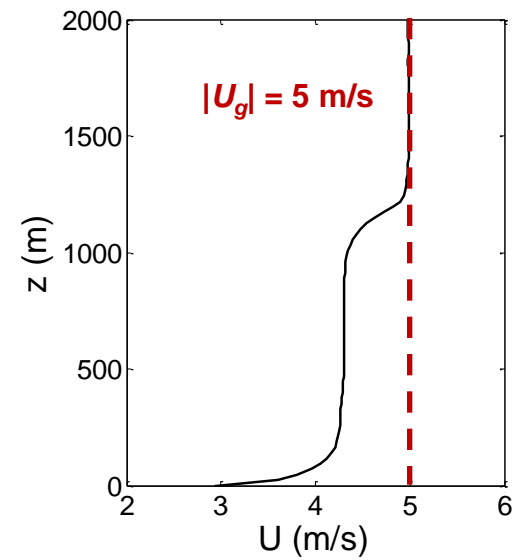
sensible heat flux



potential temperature



wind speed

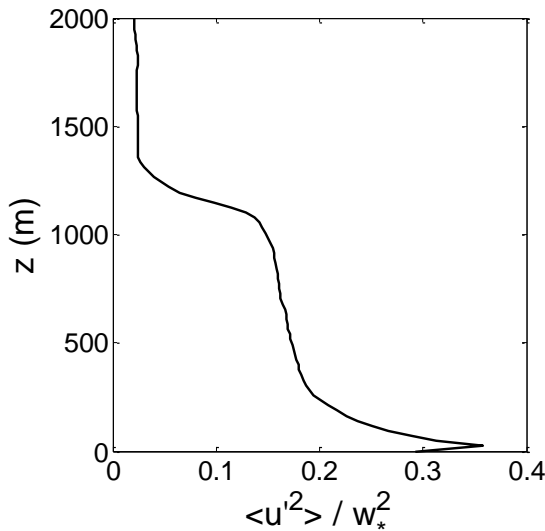


# Results

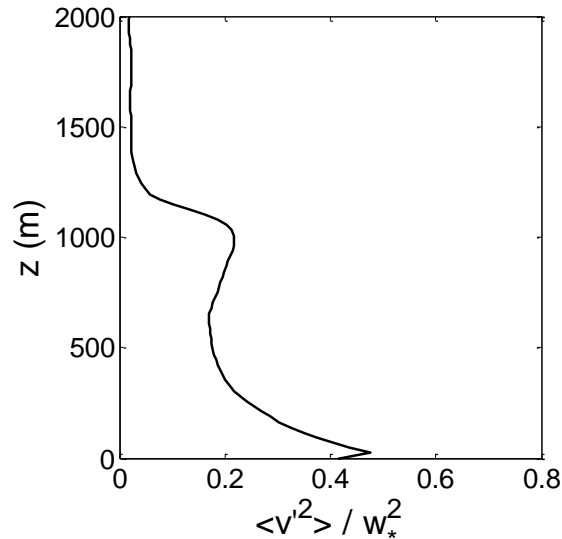
## Convective heterogeneous test case

*Time-averaged and horizontally averaged vertical profiles*

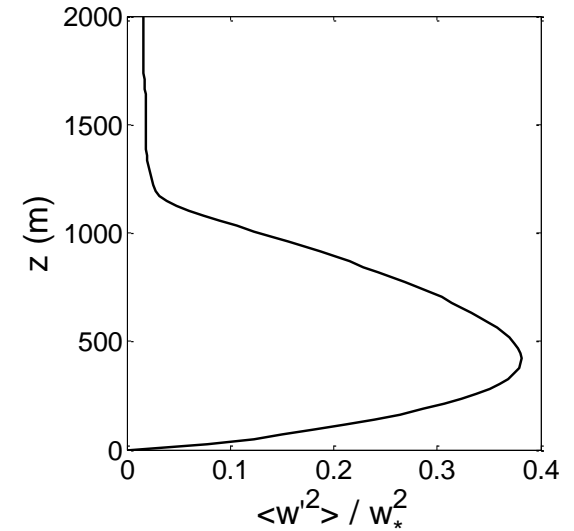
*u* velocity variance



*v* velocity variance



*w* velocity variance

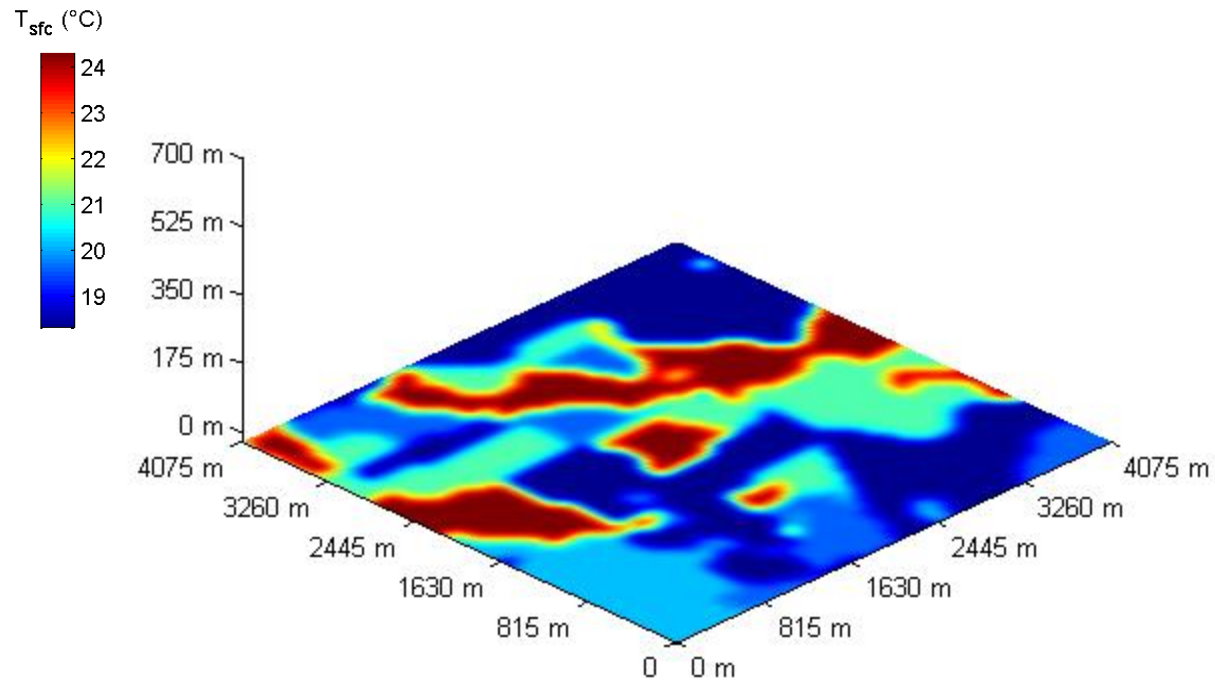


Convective velocity scale

$$w_* = \left( \frac{g}{T_0} \langle w' \theta' \rangle_0 z_i \right)^{1/3} \approx 1.42 \text{ m/s}$$

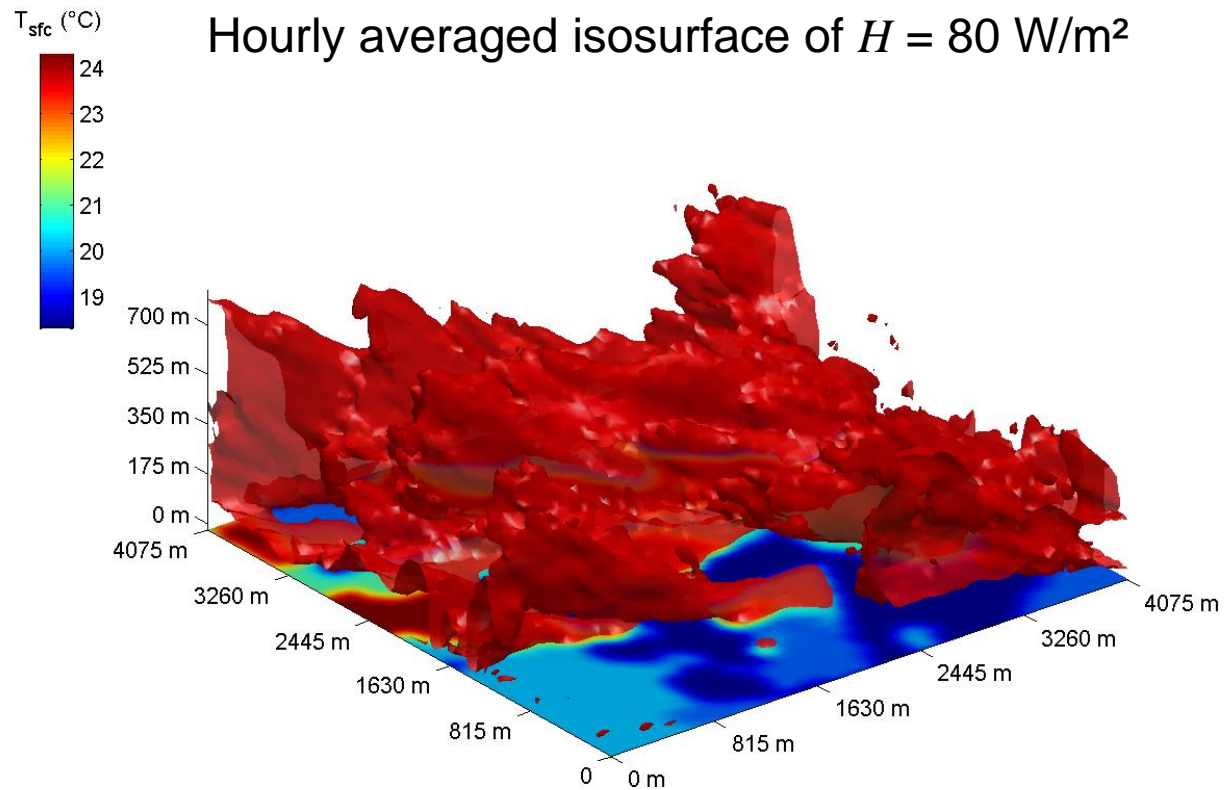
# Results

## Heat flux distribution



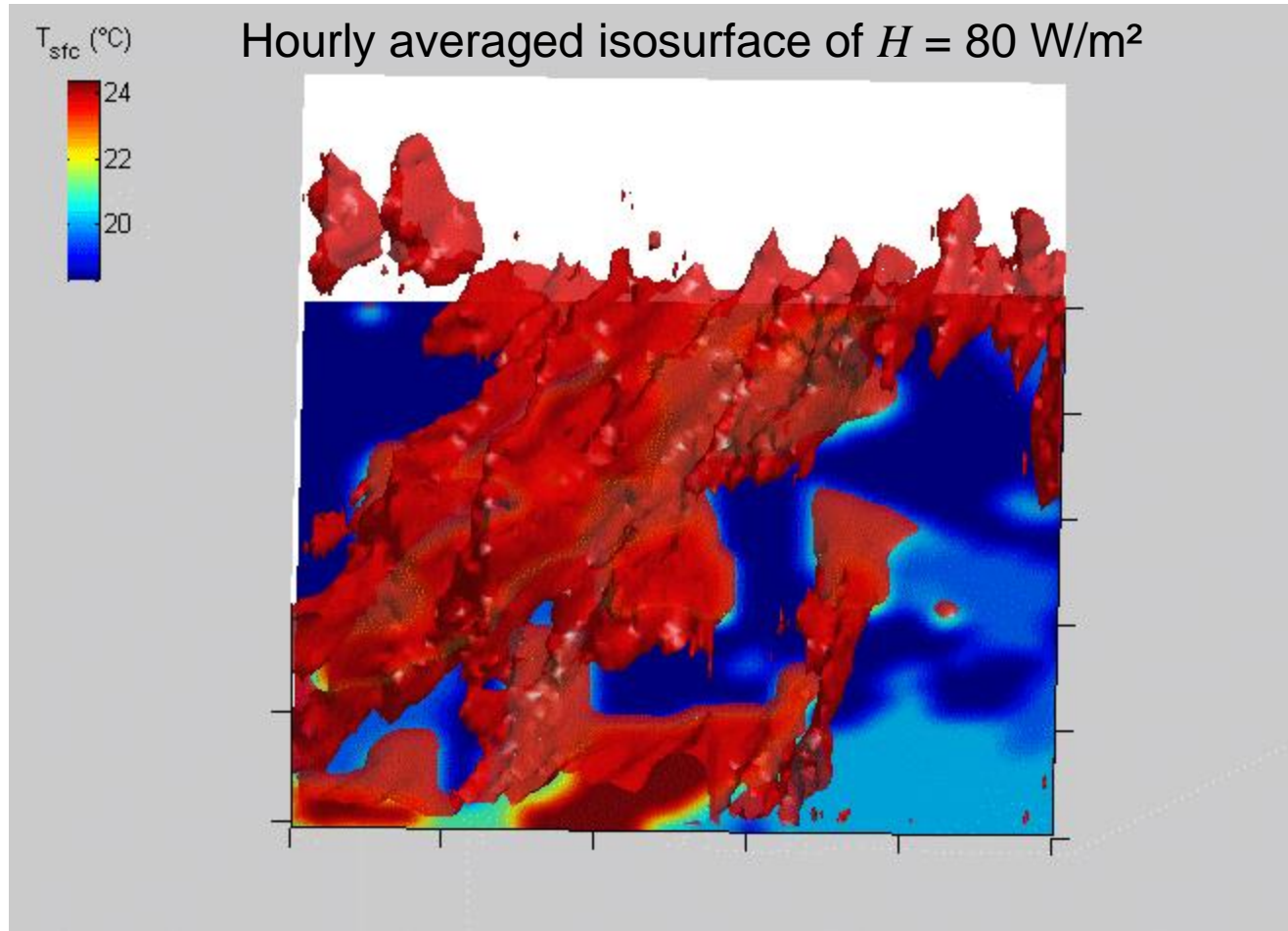
# Results

## Heat flux distribution



# Results

## Heat flux distribution

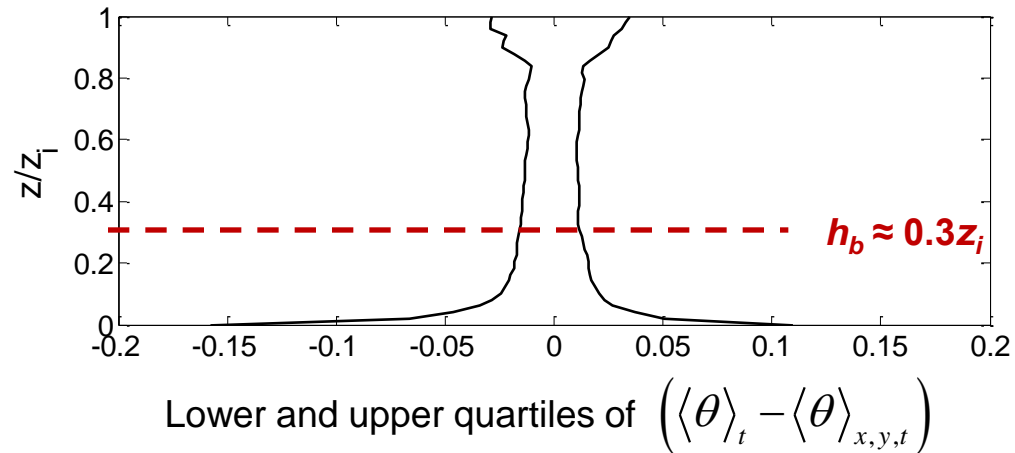


# Results

## Blending heights $h_b$

*Height at which heterogeneities at the surface are completely blended due to turbulent mixing*

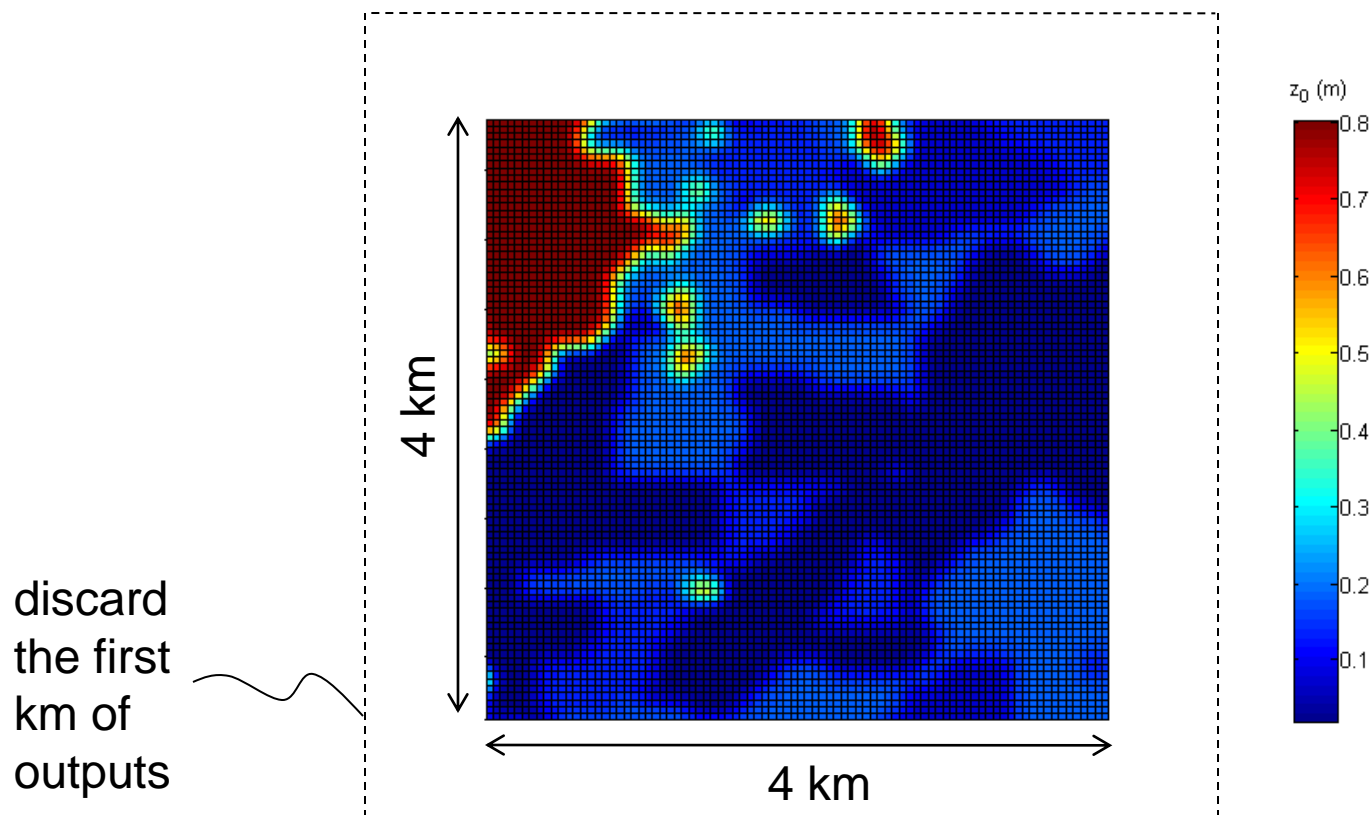
Thermal  $h_b$   
(convective run)



# Results

## Neutral heterogeneous test case

- Inhomogeneous surface roughness  $z_0$
- Neutral conditions
- Assume  $z_i = 1000$  m

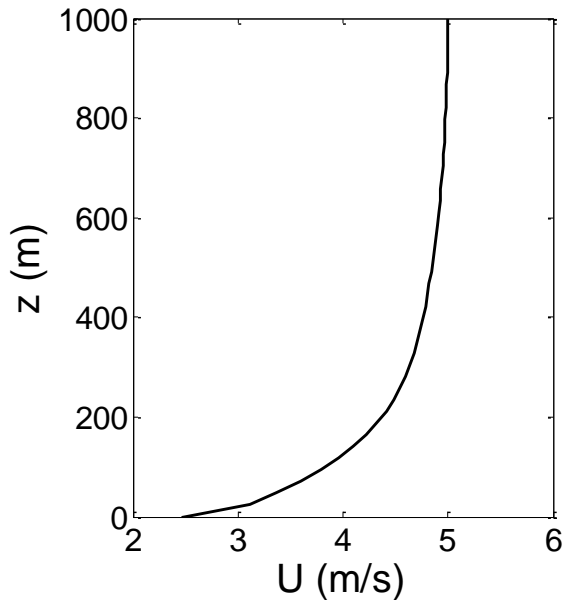


# Results

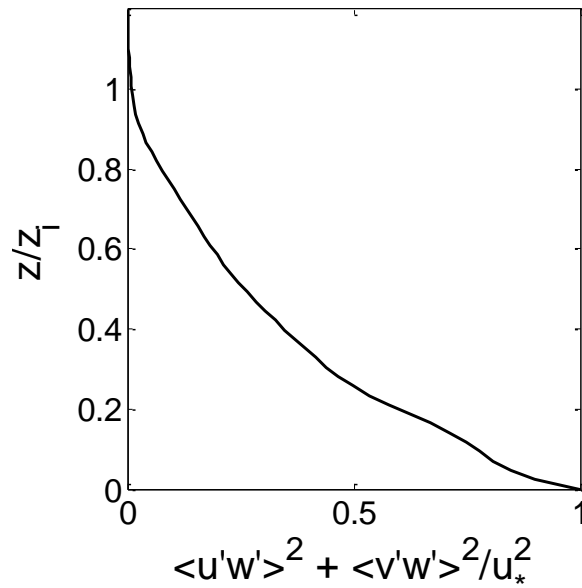
## Neutral heterogeneous test case

*Time-averaged and horizontally averaged vertical profiles*

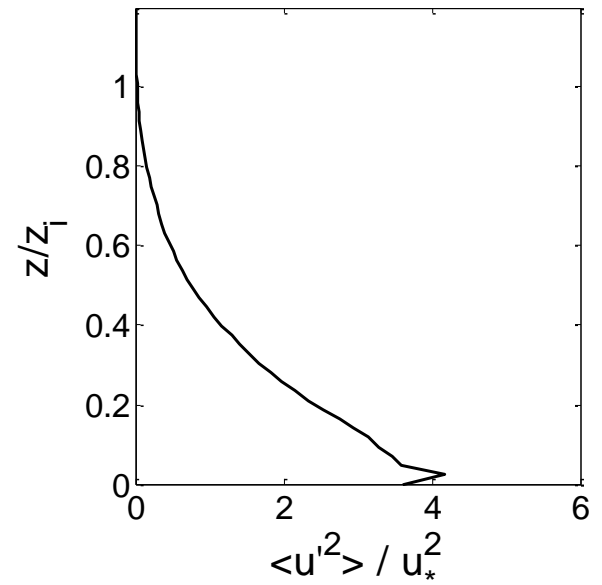
wind speed



Reynolds stress



$u$  velocity variance



$$u_* \approx 0.22 \text{ m/s}$$

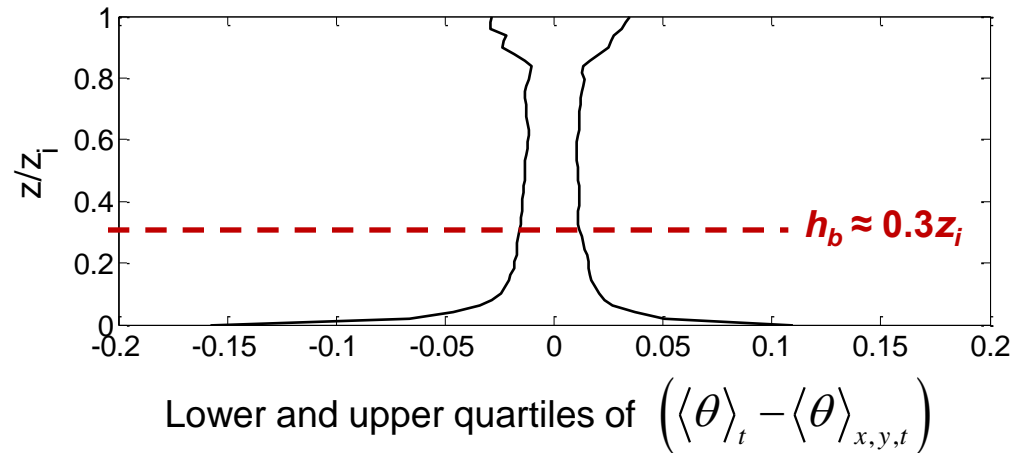


# Results

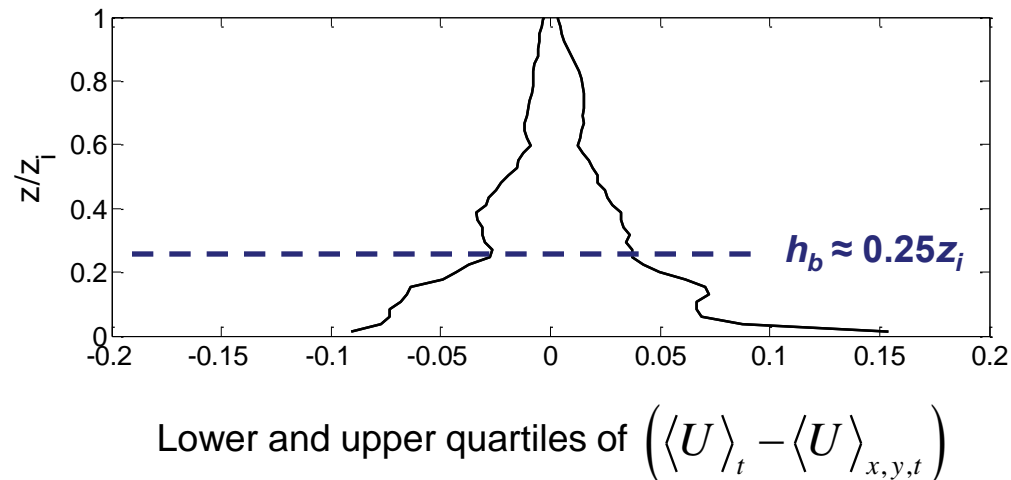
## Blending heights $h_b$

Height at which heterogeneities at the surface are completely blended due to turbulent mixing

Thermal  $h_b$   
(convective run)



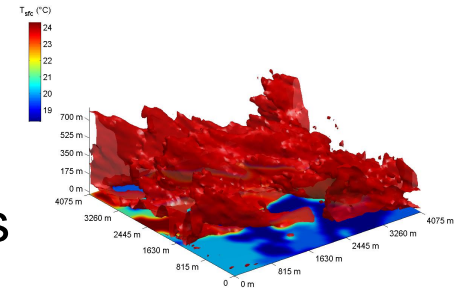
Momentum  $h_b$   
(neutral run)



# Preliminary Conclusions

## LES over heterogeneous terrain

- Successful to run with realistic BCs
- Can reproduce main ABL characteristics
- Found "periodic" turbulent structures in the heat plumes



## Blending heights

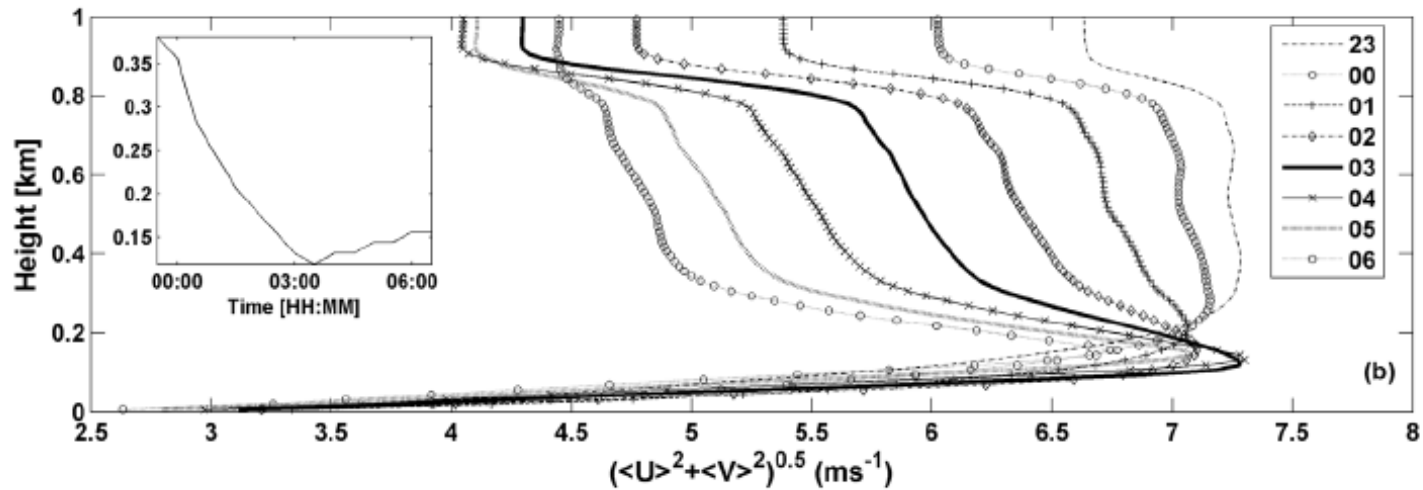
- For the given LES domain and BCs: thermal  $h_b \sim$  momentum  $h_b$
- Combining of the surface roughness and surface temperature fields...

Blending height – smaller or larger?

# Future Work

## LITFASS – 2003

- simulate over the entire diurnal cycle
  - compare with experimental data to validate the code



Source: Kumar et al., WRR, 2006

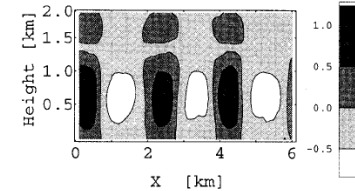
**Thank you!**

# Background

## Land-atmosphere interactions over heterogeneous terrain with LES

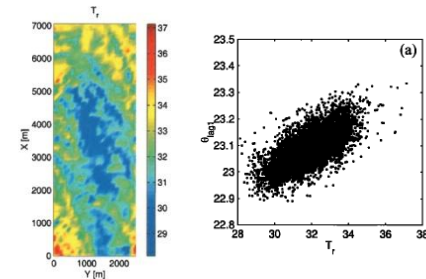
### Avissar and Schmidt, JAS, 1998

- effects on the CBL of surface heterogeneities produced by  $H$  with waves of different means, amplitudes, etc.
- Idealized BCs



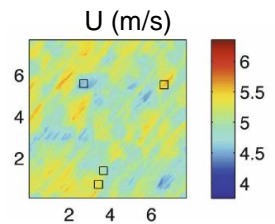
### Albertson et al., WRR, 2001

- correlation between  $T_s$  and  $\theta$  dependant on length scales of surface features
- scale-invariant SGS model, imposed pressure gradient



### Bertholdi et al., JAMC, 2008

- surface-energy balance scheme coupled with LES
- Smagorinsky model



### Huang and Margulis, WRR, 2009

- realistic surface BCs using SMACEX-2002 data
- Lagrangian dynamic scale-dependant SGS model

