Experimental observation of slow mode dispersion in photonic crystal coupled-cavity waveguides

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We experimentally investigate the dispersion curve of an integrated silicon-on-insulator coupled-cavity waveguide in a photonic crystal environment using a technique based on far-field imaging. We show that a chain of eight coupled cavities of a moderate Q factor can form a continuous dispersion band. The experimental results are well reproduced by theoretical calculations based on the guided-mode expansion method.

Evanescently coupled optical resonators concatenated in a chain, so-called coupled-cavity waveguides (CCWs) [1,2], are currently regarded as a possible solution for integrated delay lines in on-chip optical circuits [3,4]. Their ability to slow down the light pulses relies on the storage time associated with each of the cavities that form the CCW. The periodic in-line arrangement of the cavities leads to a dispersion relation that governs the propagation properties of the guided light. A decrease of the coupling between the cavities results in a decrease of the slope of the dispersion curve, i.e., a drop in the group velocity of the guided light.

The length of the CCW has a strong impact on the dispersion properties. For a CCW of a finite length, the dispersion curve is sampled with a number of points equal to the number of the cavities N. If the linewidth $\Delta \omega$ of the cavity mode is narrow compared to the entire bandwidth $\Delta \omega$ of the CCW divided by N, the optical transmission is composed of well-separated sharp peaks [5,6]. In such a regime, an input pulse of bandwidth $\Delta \omega$ is transformed into its convolution with a frequency comb formed by the CCW, and a propagating pulse is slowed down at the expense of the distortion of its shape. In the other case, i.e., if $\Delta \omega \geq \Delta \omega/N$, the dispersion curve of the CCW is expected to be smooth and continuous and a transmission band is formed. Creation of such a band is essential for practical applications, as the optical signal can propagate without distortion only if all its spectral components are equally transmitted. Taking into account that the propagation loss of the CCW mode is scaled with $\Delta \omega$, the optimum case for the management of propagation of light pulses is achieved when $\Delta \omega = \Delta \omega/N$.

To predict the behavior of light pulses in real CCWs as well as the limitations of these structures, a precise experimental knowledge of the entire dispersion curve is crucial. However, when an entire band is transmitted instead of separated sharp peaks, the dispersion curve cannot be inferred from a simple transmission experiment as in [5].

In this Letter, we accurately determine the experimental dispersion curve of an integrated silicon-on-insulator (SOI) CCW in the regime of a continuous transmission. The measurement is based on a Fourier space imaging technique that analyzes the intrinsic out-of-plane losses of the CCW structure. We show that a chain of eight cavities can support a slow-light mode with group index of 105±20 over a bandwidth as large as 0.33 THz (2.6 nm).

The coupled-cavity structure under consideration is shown in Fig. 1(a). It is based on a standard photonic crystal single-line-defect waveguide (W1), the lattice constant of which is periodically decreased in the propagation direction by 10 nm to create a double heterostructure. It is well established that such a structure supports resonant modes [7]. The optical cavities are formed by four successive periods of lattice constant $a = 430$ nm, separated by potential barriers consisting of two periods of $a_s = 420$ nm [highlighted in Fig. 1(a)]. The total length of the CCW is 25.8 $\mu$m, and it comprises eight cavities, which are

![Image](image-url)
coupled to the access waveguides by an intermediate photonic crystal waveguide region of $a=430$ nm. The hole diameter of $d=286$ nm is constant in the whole photonic crystal, corresponding to the filling factor of $f=40\%$ in the cavities. In the present study, an experimental quality factor in the range of 1355 was measured for the cavities processed in 220 nm thick SOI [see Fig. 1(b)].

A dispersion diagram of the structure calculated by the guided-mode expansion (GME) method [8] is presented in Fig. 2(a) (dotted curve). At reduced frequencies larger than 0.279, the mode dispersion is similar to the dispersion of a standard W1 waveguide, folded by the periodicity of the supercell defined by $\Lambda=4a+2a_b$. In this frequency range, the barrier regions still support a propagating mode, and the upper band represents a dispersion curve of a weakly corrugated W1 waveguide. The coupled-cavity mode appears approximately 4 nm below the cutoff of the "W1 mode" and is characterized by cosine-shaped dispersion and a bandwidth spanning 2.6 nm (0.33 THz). Formation of such a CCW mode can be equally understood in terms of a perturbed W1 waveguide; it is a result of the anticrossing of the folded W1 modes, which are coupled owing to the periodic perturbation introduced by the barriers. This is illustrated in Fig. 2(b), which shows how the W1 mode splits and the band diagram is formed once the coupling interaction is introduced.

To experimentally probe the CCW dispersion, the sample was fabricated on an SOI material system (220 nm thick Si layer on 2 $\mu$m buried oxide) using a complementary metal–oxide semiconductor compatible deep-UV lithography [9]. A 330-nm-thick resist layer with a bottom antireflective coating was patterned by 193 nm illumination. The resist served directly as an etch mask for inductively coupled plasma–reactive ion etching (ICP–RIE), which followed the writing process to transfer the pattern into the silicon device layer. The top view scanning electron microscopy (SEM) image of the sample surface shown in Fig. 1(a) confirms the high quality of the structure pattern. The fabricated structure was excited using a highly monochromatic cw laser of a linewidth of $\Delta \lambda < 1$ pm, tunable within the wavelength range of 1470–1660 nm. TE polarized light was coupled into the sample by use of lensed fiber and adiabatically tapered access waveguides.

Unlike typical low-loss optical waveguides that support fully guided, nonradiative modes, the CCWs are intrinsically lossy. The imposed periodicity of the coupled cavity chain acts as a diffraction grating, which perturbs the guided field and scatters a part of the propagating light into the radiative continuum [10]. Although detrimental for energy performance, this permits us to study the light propagation within the structure by means of standard optical imaging. Light radiated from the sample surface was collected using a high numerical aperture objective (NA=0.9) and projected onto a sensitive infrared (IR) camera.

The real-space image showing the near-field intensity distribution of the CCW mode is presented in Fig. 1(c). Although the field decay along the propagation direction is significant (~3 dB per 10 $\mu$m), it can be clearly seen that all eight cavities are excited and that the light is well localized within the core of the CCW structure. The weak but apparent transversal oscillation of the near-field pattern is attributed to subnanometer structural disorder, which notably disturbs the signal propagation in the sensitive slow-light regime.

To probe the spectral properties of the CCW mode including the dispersion relation, we use a Fourier-space imaging technique, which was discussed in detail in [10,11]. By projecting the back focal plane of the collecting lens on the IR camera, we access the far-field or $k$-space image, which represents the optical Fourier transform of the near-field pattern. In such an image, every point $(k_x, k_y)$ is uniquely related to a wave vector of the radiated field and, according to the wave-vector conservation, also to a wave vector of mode propagating in the structure. Hence, by recording the $k$-vector distribution for each excitation frequency $\omega$, we can retrieve the dispersion relation $\omega(k)$ of the guided field.

The experimental dispersion diagram showing both the CCW and the corrugated W1 waveguide mode is plotted in Fig. 2(a) together with the result of the GME simulation. The direct comparison demonstrates a good agreement between the theory and the measurement in respect to both the position and the slope of the investigated modes. The NA of our imaging system allows us to probe the first three Brillouin zones nearest to the center of the dispersion plane. Hence, in the dispersion map we observe three dispersion curves that are identical in shape but offset along the $k$-vector coordinate by the reciprocal vector of the coupled-cavity chain $2\pi/\Lambda=2.45$ $\mu$m$^{-1}$. Their peak intensities reflect the energy distribution in individual Brillouin zones, i.e., the relative intensities of the spectral components of the Bloch mode.

Intensity profiles of the far-field spectra of the CCW mode at different excitation wavelengths be-

![Fig. 2.](image-url) (Color online) (a) Experimental dispersion diagram compared to the GME calculation. (b) Simulation of the CCW mode formation upon increasing the lattice constant difference between the cavities ($a=430$ nm) and the barriers ($a_b=430, 425, 420$, and 410 nm). (c) Line profiles of the CCW mode dispersion.
between 1546.8 and 1548.7 nm are presented in Fig. 2(c). Upon increasing the frequency of excitation, the peaks follow the dispersion of the CCW mode. The linewidth of the far-field spectra does not change notably within the CCW mode bandwidth and is primarily determined by the finite length of the measured structure. The intensity of the collected light is maximum at the top of the CCW dispersion band, which is attributed to higher out-of-plane radiation loss of the symmetric CCW mode. A closer zoom on the CCW mode dispersion is given in Fig. 3, which presents the experimental dispersion curve in the second Brillouin zone normalized in intensity, together with the theoretical band diagram calculated by the GME method. Markers that depict the maxima of the experimental data help to visualize the measured dispersion curve. The experimental dispersion function \( \omega(k) \) is smooth enough to be numerically differentiated to obtain the group index and its frequency dependence, as shown in Fig. 3 (right). The experimental dispersion relation agrees well with the theoretical calculations until a maximum group index of approximately \( n_g = 330 \). This is one of the largest experimental group index values reported for an optical waveguide, although the error bars are delicate to estimate in such a narrow energy and wave-vector range. Above this value, the CCW mode deflects from the ideal cosine-shaped dispersion and gets smoothly coupled into a fast-decaying evanescent mode that emerges from the top and the bottom of the dispersion band. The maximum achievable value of the group index \( n_g = 330 \) is strongly limited by the structural disorder and intrinsic out-of-plane losses, which significantly modify the ideal dispersion diagram as was discussed in [12].

To evaluate the buffering capacity of the measured device we calculate the normalized delay-bandwidth product (DBP\(_N\)) of the CCW [4], which can be expressed as a product of the group index and the bandwidth of the mode of interest. The group index does not drop below 105±20 in the entire bandwidth of the CCW mode (0.33 THz), which corresponds to a DBP\(_N\) as large as 0.18. It should be remarked that within 2 nm of this bandwidth the dispersion of the mode is very close to linear, so the propagating pulse (of time duration down to 2 ps) will not be distorted owing to group-velocity dispersion.

In summary, we have presented a dispersion curve of a double heterostructure CCW probed by a technique of far-field imaging. The experimental data taken with high spectral resolution allowed us to retrieve the dispersion curve of the CCW mode with a high accuracy and calculate its group index, which was found to be larger than 105±20 within a 2.6 nm wavelength range.

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