Intracellular Ca\(^{2+}\) Stores Can Account for the Time Course of LTP Induction: A Model of Ca\(^{2+}\) Dynamics in Dendritic Spines

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**SUMMARY AND CONCLUSIONS**

1. A model of Ca\(^{2+}\) dynamics in spines of CA1 hippocampal neurons is presented. In contrast to traditional models, which concentrate on the effects of Ca\(^{2+}\) influx, diffusion, buffering, and extrusion, we also consider the additional effect of intracellular Ca\(^{2+}\) stores.

2. It is shown that traditional models without Ca\(^{2+}\) stores cannot account for the time course of long-term potentiation (LTP) induction as found in recent experiments. Experimental data suggest that the intracellular Ca\(^{2+}\) concentration should be elevated for up to 2 s, whereas the Ca\(^{2+}\) concentration in standard models of Ca\(^{2+}\) dynamics decays much faster.

3. When intracellular Ca\(^{2+}\) stores are taken into account, a much slower decay is found. In particular, a model simulation with a tetanic stimulation paradigm consisting of two bursts of four impulses at 100 Hz each and variable interburst intervals can reproduce experimental results found for primed or theta-burst stimulation.

4. In our model, Ca\(^{2+}\) release from the store has a nonlinear, bell-shaped dependence on the intracellular Ca\(^{2+}\) concentration, similar to the one found for inositoltrisphosphate and ryanodine receptors. These receptors are known to control calcium release from intracellular stores.

5. Our model suggests an important role of intracellular calcium stores in the induction of LTP. The stores serve as a long-term calcium source that can sustain an intracellular Ca\(^{2+}\) concentration above the resting level for 1–2 s.

**INTRODUCTION**

Long-term potentiation (LTP) of synaptic efficacy has been extensively studied during recent years, both in experiments (for reviews, see for example Bindman et al. 1991; Brown et al. 1991; Madison et al. 1991) and in model approaches (Brown et al. 1988; Gamble and Koch 1987; Gold and Bear 1994; Holmes and Levy 1990; Kitajima and Hara 1990; Zador et al. 1990). This interest is partly due to the fact that LTP could be the neuronal implementation of a Hebbian learning rule (Hebb 1949) that is used, in one form or another, in various mathematical models of neural networks (cf. for example Amit 1989; Domany et al. 1991; Hertz et al. 1991; Müller and Reinhard 1991; Peretto 1992). Phenomenologically, LTP of a synaptic link between presynaptic and postsynaptic neurons, e.g., in the CA1 region of the hippocampus, can be induced if brief tetanic stimuli to presynaptic pathways are applied. The exact molecular mechanism leading to the potentiation is still unclear (Brown et al. 1991; Lisman and Harris 1993; Madison et al. 1991). It has, however, been shown in several experiments that a transient rise of the intracellular Ca\(^{2+}\) concentration ([Ca\(^{2+}\)]) is a necessary condition for LTP induction (Bliss and Collingridge 1993). To explain this, calcium influx through N-methyl-D-aspartate (NMDA) receptor channels has been assumed to be the essential source of calcium. Models of Ca\(^{2+}\) dynamics in which NMDA channels are the only source of calcium yield a time course of intracellular [Ca\(^{2+}\)] that is consistent with experimental findings on CA1 hippocampal neurons, at least for the tetanic stimulus paradigm (Gamble and Koch 1987; Gold and Bear 1994; Holmes and Levy 1990; Zador et al. 1990). There is, however, a key experiment by Malenka et al. (1992) that makes a reconsideration of Ca\(^{2+}\) dynamics during LTP induction inevitable. In this experiment a weak stimulation scenario of 100 impulses at 100 Hz was used. Under normal conditions, this stimulation paradigm leads to reliable induction of LTP. By activation of a photolabile Ca\(^{2+}\) buffer, however, it was possible to limit the rise in intracellular Ca\(^{2+}\) to a specified period. It turned out that LTP was induced only if the Ca\(^{2+}\) buffer was activated \(>2\)–2.5 s after the beginning of the stimulus. In the following, we will refer to this as the 2-s criterion. It is safe to conclude from this experiment that the intracellular [Ca\(^{2+}\)] has to be elevated for \(\approx1.5\) s after the stimulus to successfully induce LTP. Our simulation studies, presented below, will show that this cannot be achieved if NMDA channels or other voltage-gated Ca\(^{2+}\) channels are the only source of calcium.

To account for the 2-s criterion, we propose an extended model that takes intracellular Ca\(^{2+}\) stores into account. Over the past two or three years there has been growing evidence for an important role of intracellular Ca\(^{2+}\) stores in the induction of LTP. Ca\(^{2+}\) release from these stores is mediated by ryanodine receptors (RYR) and inositol 1,4,5-trisphosphate (InsP\(_3\)) receptors, as has been shown in a variety of experiments. Drugs that deplete intracellular calcium stores (thapsigargin) or inhibit calcium-induced calcium release from intracellular stores (ryanodine) substantially reduce the transient rise in intracellular [Ca\(^{2+}\)] during synaptic activation of NMDA channels (Bliss and Collingridge 1993). On the other hand, the induction of LTP is inhibited by applying thapsigargin and dantrolene, a drug that blocks the ryanodine receptor (Harvey and Collingridge 1992; Obenaus et al. 1989). Activation of metabotropic glutamate receptors, which play a role during InsP\(_3\) synthesis, can induce LTP without the participation of NMDA receptors (Bortolotto and Collingridge 1993). Because this mechanism is sensitive to thapsigargin, it is most likely that release of Ca\(^{2+}\) from intracellular stores alone can be sufficient for the induction of LTP. These experiments imply an important role of intracellular stores in the induction of LTP.
The simulations of Gamble and Koch (1987), Zador et al. (1990), and Holmes and Levy (1990) using NMDA channels as the principal source of Ca\(^{2+}\) during LTP induction have shown that the amplitude of a transient rise in the intracellular [Ca\(^{2+}\)] is directly related to both the stimulation frequency and the number of coactivated synapses. Because in experiments there is a similar relation between LTP and the stimulation frequency or the number of stimulated synapses (Madison et al. 1991), it is likely that there is a direct connection between the maximum intracellular [Ca\(^{2+}\)] and the induction of LTP. In this interpretation the models give a qualitative, if not quantitative, explanation of the experiments. On the other hand, the above models cannot account for the experimental results of Malenka et al. (1992). In fact, our model studies presented in this paper show that the [Ca\(^{2+}\)] decays too fast after the end of the stimulus to account for the 2-s criterion, if NMDA receptors were the only Ca\(^{2+}\) source (Simulations of the experiment of Malenka et al. with standard dynamics, below). In our opinion, intracellular stores serving as “long-term” calcium sources could bridge the gap between the short-time and the long-time behavior. Here we present an extended model including intracellular Ca\(^{2+}\) stores. The model is introduced in METHODS. It is applied to the experiments of Malenka et al. (1992) in Simulations of the experiment of Malenka et al. with intracellular stores. Furthermore, it is shown that the extended model can also explain the time course of the induction of LTP with primed and theta-burst stimulation (Intracellular stores with primed and theta-burst stimulation). These stimulation patterns are of particular interest because they resemble activity patterns measured in vivo in hippocampus. We close with a discussion of our results.

**METHODS**

In our simulations we use a nine-compartment electrical model of a CA1 pyramidal cell (Fig. 1) to which an equivalent circuit of a synapse (Fig. 2) has been attached. In the first part of our simulations (Simulations of the experiment of Malenka et al. with standard dynamics, below), calcium dynamics in the dendritic spine have been modeled on the basis of the approach of Zador et al. (1990). Spine head and spine neck are assumed to be cylindrical and consist of several diffusion compartments. Ca\(^{2+}\) that enters the spine head through NMDA channels diffuses into the spine neck and the dendrite, is buffered by intracellular buffers, and is pumped out of the spine by calcium extrusion mechanisms. The central results in Simulations of the experiment of Malenka et al. with intracellular stores and Intracellular stores with primed and theta-burst stimulation have been achieved with an extended model that also includes intracellular calcium stores in the spine head. The description of calcium stores is given in Model of intracellular calcium stores, whereas the basic model is introduced in Equivalent circuit for a synapse, Model neuron, and Standard calcium dynamics.

**Equivalent circuit for a synapse**

The passive electrical properties of the spine head membrane are modeled by a capacitor $C_s$ parallel to a leak conductance $g_l$. A battery $E_s$ in series with $g_l$ provides the resting potential of the membrane. We consider two types of neurotransmitter-gated ion channels, $\alpha$-amino-3-hydroxy-5-methyl-4-isoxazolepropionic acid (AMPA) and NMDA channels, both described as time-dependent functions; see the text for details. The spine capacitance $C_s$ and the conductivity $g_s$ of the spine membrane, and the spine neck conductivity $g_{neck}$ are constant parameters ($C_s = 0.04 \text{ pF}$, $g_s = \tau/C_s$, $E_s = -80 \text{ mV}$, $g_{neck} = 1/100 \text{ M} \Omega$, and $F_s = F_e = 0$) where $F_s$, $F_e$, and $E_n$ are the reversal potentials of leakage, NMDA, and AMPA channels, respectively. $C_s$ is the capacitance, $g_s$ and $g_{neck}$ are the transversal and longitudinal conductivity of a dendritic compartment.

![Fig. 2. Electrical model of a synapse on an spine.](image)

where $V$ is the spine head potential, $E_s$ is the AMPA reversal potential, and $g_s$ is the maximum AMPA conductivity, $e$ is the Euler constant.
The change of spine head voltage that is attached to the dendritic compartment under consideration.

adjusted according to measurements as discussed in Zador et al.

synaptic input current

synapses to the same dendritic compartment. Let us consider the AMPA channels

amplitude and this is where we will focus.

Given electrical constants

Membrane time constant

Specific membrane resistance

Specific membrane capacity

Input resistance

Compartment constants

Resistance, somatic compartment

Resistance, dendritic compartments

Resistance, basilar bush

Resistance, lower apical branch

Resistance, spine head

Longitudinal conductance, dendritic compartment

Longitudinal conductance, basilar bush

Longitudinal conductance, lower apical branch

Longitudinal conductance, spine neck

NMDA channels

Reversal potential

Maximum conductance

Channel closing time

Channel opening time

Prefactor of magnesium block

Voltage factor of magnesium block

Magnesium concentration

Global electrical constants

Membrane time constant

Specific membrane resistance

Specific membrane capacity

Input resistance

AMPA, α-amino-3-hydroxy-5-methyl-4-isoxazolepropionic acid; NMDA, N-methyl-d-aspartate.

constant, and \( t > 0 \) is the time after the stimulation. For the NMDA current we use a double exponential (Zador et al. 1990)

\[
I_{nmda} = (V - E_n)g_n \frac{\exp(-t/\tau_1) - \exp(-t/\tau_2)}{1 + \eta[Mg^{2+}] \cdot \exp(-\gamma V)}
\]

where \( E_n \) is the NMDA reversal potential and \( g_n \) is a conductivity parameter. Depending on the membrane voltage, NMDA channels are blocked by Mg\(^{2+}\) ions. This is expressed by the denominator in the above equation, whereas the numerator expresses the intrinsic conductivity of the NMDA channels. Constants in Eq. 2 are adjusted according to measurements as discussed in Zador et al. (1990) and Brown et al. (1991). We adopt the parameters of Zador et al. (1990) listed in Table 1.

LTP induction involves the coactivation of many synapses. For the sake of simplicity, we did not model tens or hundreds of synapses explicitly. Instead we made two assumptions.

1) All coactivated synapses are situated in a relatively small area of the neuron.

2) These synapses are activated synchronously.

Because of the first assumption, we can attach all coactivated synapses to the same dendritic compartment. Let us consider the synaptic input current \( I_{syn} \) into a specific spine head with index \( i \) that is attached to the dendritic compartment under consideration. The change of spine head voltage \( V_s \) is described by

\[
\frac{dV_s}{dt} = \frac{1}{C_i} \left[ E_s(I_s - V_s) + g_{neck}(V_d - V_s) + I^{long} \right]
\]

where \( V_s \) is the membrane voltage in the dendritic compartment. The capacitance \( C_i \) and the conductivity \( g_i \) are dendritic membrane parameters and \( I_{long} \) denotes longitudinal currents from other dendritic compartments. If all synapses are activated synchronously and if they are all connected to the same dendritic compartment, then the time course \( V_s(t) \) is identical for all spine heads \( 1 \leq i \leq N \). In this case, we can replace the sum over \( N \) by a multiplication with the factor \( N \)

\[
\frac{dV_d}{dt} = \frac{1}{C_d} \left[ \left( E_i - V_d \right) - \sum_{i=1}^{N} g_{neck}(V_d - V_s) + I^{long} \right]
\]

In real neurons, synchronous coactivation of many synapses is rather unlikely. Also, coactivated synapses will in general not be located on the same dendritic compartment. Because, according to Eq. 1 and 2, the input current is a function of the local membrane potential, summation of different inputs is nonlinear and, in general, depends on the location of all coactivated synapses. For these reasons, we consider the factor \( N \) in our simplified approach (Eq. 5) not as an exact measure of the number of coactivated synapses but rather as a semiquantitative measure of the overall stimulation strength.

Model neuron

We model a pyramidal cell with two major apical dendrites and a basilar bush as commonly found in the hippocampal CA1 region (e.g., Turner and Schwartzkroin 1980) by a simplified neuron model with nine compartments (Fig. 1). The stimulated synapses are assumed to be located on the fourth compartment of the upper branch of the apical dendrite. This branch has been divided in six equal compartments to model a smooth spread of the incoming signals. Soma, lower apical branch, and basilar bush are modeled by a single compartment only. We have checked by preliminary simulations with more complex model neurons that the above nine compartments are sufficient for an accurate description of the electrical potential in the model spine head on the upper apical dendrite; and this is where we will focus.

For the electrical constants of the neuron, we use typical values listed in Table 1. The values for \( \tau \) = 30 ms and input resistance \( (R_s) = 100 \text{ MΩ} \) have been taken from the paper of Spruston and Johnston (1992), the values for specific membrane capacity \( (C_m) \) from Brown et al. (1981), and the membrane resistance has been computed from specific membrane resistance \( (R_m) = \tau/C_m \). The electrotonic length \( (L) \) is assumed to be 0.7 for each of the apical branches and the basilar bush. We assume a soma membrane surface of 1,000 µm\(^2\) corresponding to a soma membrane resistance of 3,000 MΩ. The input conductivities of the dendritic branches have been computed by standard procedures (Perkel and Mulloney 1978) from \( R_s \) and \( L \). In particular, for the core and membrane resistance of the six compartments of the upper apical dendrite, we find values of 18 and 1,800 MΩ, respectively. It turns out that our results are not sensitive to the precise value of these parameters. Thus the values have been fixed in some plausible regime. The computer code has been developed locally. The system of differential equations has been integrated numerically with the program lsoda of the odepack library (Hindmarsh 1983; Petzold 1983). This is a standard library routine for stiff and nonstiff equations. The program adjusts the integration step automatically during each run. In our simulations, numerical values were written in a file after every 0.1 ms of simulated time. This limits the integration step to a maximum size of 0.1 ms. If necessary, shorter steps where

<table>
<thead>
<tr>
<th>Description</th>
<th>Parameter Value</th>
</tr>
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<tbody>
<tr>
<td>AMPA channels</td>
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</tr>
<tr>
<td>Reversal potential</td>
<td>( E_n ) = 0 V</td>
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<tr>
<td>Maximum conductance</td>
<td>( g_n ) = 0.5 nS</td>
</tr>
<tr>
<td>Channel time constant</td>
<td>( t ) = 1.5 ms</td>
</tr>
</tbody>
</table>

| NMDA channels        |                 |
| Reversal potential   | \( E_n \) = 0 V |
| Maximum conductance  | \( g_n \) = 0.2 nS |
| Channel closing time | \( \tau_1 \) = 80 ms |
| Channel opening time | \( \tau_2 \) = 0.67 ms |
| Prefactor of magnesium block | \( \eta \) = 0.33 nM |
| Voltage factor of magnesium block | \( \gamma \) = 0.06 mV |
| Magnesium concentration | [Mg\(^{2+}\)] = 1.2 mM |

<table>
<thead>
<tr>
<th>Global electrical constants</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Membrane time constant</td>
<td>( \tau ) = 30 ms</td>
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<tr>
<td>Specific membrane resistance</td>
<td>( R_m ) = 30 kΩ/cm(^2)</td>
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<tr>
<td>Specific membrane capacity</td>
<td>( C_m ) = 1 µF/cm(^2)</td>
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<tr>
<td>Input resistance</td>
<td>( R_s ) = 100 MΩ</td>
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<table>
<thead>
<tr>
<th>Compartment constants</th>
<th></th>
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<tbody>
<tr>
<td>Resistance, somatic compartment</td>
<td>( R_{soma} ) = 3,000 MΩ</td>
</tr>
<tr>
<td>Resistance, dendritic compartments</td>
<td>( R_{nd} ) = 1,800 MΩ</td>
</tr>
<tr>
<td>Resistance, basilar bush</td>
<td>( R_b ) = 240 MΩ</td>
</tr>
<tr>
<td>Resistance, lower apical branch</td>
<td>( R_{ap} ) = 240 MΩ</td>
</tr>
<tr>
<td>Resistance, spine head</td>
<td>( g_{sp} ) = 750 MΩ</td>
</tr>
<tr>
<td>Longitudinal conductance, dendritic compartment</td>
<td>( g_{nd} ) = (18 MΩ(^{-1})) (-1)</td>
</tr>
<tr>
<td>Longitudinal conductance, basilar bush</td>
<td>( g_b ) = (60 MΩ(^{-1})) (-1)</td>
</tr>
<tr>
<td>Longitudinal conductance, lower apical branch</td>
<td>( g_{ap} ) = (60 MΩ(^{-1})) (-1)</td>
</tr>
<tr>
<td>Longitudinal conductance, spine neck</td>
<td>( g_{neck} ) = (100 MΩ(^{-1})) (-1)</td>
</tr>
</tbody>
</table>
chosen automatically on the basis of the criterion that the estimated error stays below a value of 0.1 nV for each voltage variable and below a value of 0.1 nM for concentration variables.

To test our model, we have simulated the activation of one or several synapses in the upper apical dendrite, cf. Fig. 3, A and B. The depolarization of the spine head due to a single spike at a single synapse (Fig. 3B, inset) is in the range of several millivolts, as in other models with up to several thousand dendritic compartments (Brown et al. 1991; Holmes and Levy 1990). Figure 3A, inset, shows the somatic excitatory postsynaptic potential (EPSP) caused by the activation of a single synapse. It has been estimated elsewhere that the activation of a single synapse causes a somatic EPSP with an amplitude of several hundred microvolts (McNaughton et al. 1981). Our result is in the expected range. Note that a spike train of four spikes at 100 Hz leads to a pronounced summation at the soma, but there is only a small increase of the peak voltage at the spine head. If 30 synapses are coactivated simultaneously (Fig. 3, A and B, full-sized graphs), there is a strong depolarization both at the spine head and the soma.

**Standard calcium dynamics**

Our model of standard calcium dynamics follows Zador et al. (1990). It includes Ca\textsuperscript{2+} pumps to extrude calcium from the cell in addition to Ca\textsuperscript{2+} buffers, NMDA channels, and calcium diffusion. Spine head and spine neck are assumed to be cylindrical. For Ca\textsuperscript{2+} diffusion, we use a discretized form of the diffusion equation

\[
\frac{\partial [\text{Ca}^{2+}]}{\partial t} = D \left( \frac{\partial^2 [\text{Ca}^{2+}]}{\partial x^2} + \frac{\partial^2 [\text{Ca}^{2+}]}{\partial y^2} + \frac{\partial^2 [\text{Ca}^{2+}]}{\partial z^2} \right)
\]

where \(x, y, \) and \(z\) are spatial coordinates and \(D = 0.6 \mu m^2/s\) is the diffusion coefficient of calcium. Spine head and spine neck consist of three diffusion compartments each (see Fig. 4). Radial diffusion was neglected. This has been checked using several more accurate discretizations with and without radial diffusion, without any significant difference of the results.

Ca\textsuperscript{2+} enters the spine head at the top of the spine through NMDA channels. The Ca\textsuperscript{2+} current is assumed to be a fixed fraction of 10% of the total NMDA current \(I_{\text{NMDA}} = 0.1 \times I_{\text{NMDA}}\) (Garaschuk 1995).

It is known that there are large intracellular quantities of calmodulin (CaM) and smaller unknown quantities of other Ca\textsuperscript{2+} binding proteins. We have included CaM as a Ca\textsuperscript{2+} buffer in our model. CaM has four Ca\textsuperscript{2+} binding sites per molecule, to which Ca\textsuperscript{2+} is bound sequentially (Klee et al. 1980). The intracellular CaM concentration is estimated to lie at \(\sim 30 \mu M\) (Carafoli 1987). Thus we have chosen a concentration of Ca\textsuperscript{2+} binding sites of \([b_{\text{tot}}] = 120 \mu M\) for all compartments \(1 \leq i \leq 6\). Cooperativity effects due to sequential binding at the four different sites have been neglected. To check this assumption, we included sequential binding in some simulations and we sometimes also doubled the CaM concentration in the first compartment (which may be considered as the locus of the postsynaptic density), but this did not modify the results. A standard rate equation for binding of Ca\textsuperscript{2+} to buffer molecules yields for the change of the free calcium concentration in compartment \(i\) due to buffering

\[
\frac{d[\text{Ca}^{2+}]}{dt} = -k_1[\text{Ca}^{2+}][b_{\text{tot}}] + k_1([b_{\text{tot}}] - [b_{\text{tot}}])
\]

**FIG. 3.** Response to synaptic input. **A:** simulated postsynaptic potential at the soma. **B:** voltage at the spine head. **C:** calcium concentration in the spine head. In the simulations plotted in the full-sized graphs, the neuron has been activated at \(N = 30\) synapses with a burst of 4 spikes at 100 Hz. Insets: respective quantities after 1 (thick lines) or 4 (thin lines) spikes at a single synapse. A single spike evokes a depolarization of \(-0.4 \mu V\) at the soma \((A)\) and \(-5 \mu V\) at the spine head \((B)\). Subsequent spikes lead to a summation effect, which is most pronouncedly seen at the soma. Note the different scales insets of \(A\) and \(B\). The calcium amplitude \((C)\) in response to a single spike is \(-0.1 \mu M\). More spikes or a larger number of coactivated synapses lead to a higher calcium concentration in the spine head.

**FIG. 4.** Model of Ca\textsuperscript{2+} dynamics in a dendritic spine. To describe calcium diffusion, the spine has been discretized into 6 diffusion compartments labeled 1–6. The length scale indicated by the bar at right is given in \(\mu m\). In our simulations, the dendrite below compartment 6 contains a constant calcium concentration of 0.5 \(\mu M\).
while at the same time the concentration of free buffering site \([\text{bufree}]\) changes according to

\[
\frac{d[\text{bufree}]}{dt} = -k_1[\text{Ca}^{2+}][\text{bufree}] + k_1([\text{bufree}]-[\text{bufree}])
\]  

(8)

Here, \([\text{bufree}]\) is the total concentration of buffering sites in compartment \(i\), whereas \(k_1\) and \(k_1\) are the forward and backward buffering rates, respectively. The buffering rates are unknown but there are estimates for the dissociation constant \(K_d = 1\ \mu M\) (Klee et al. 1980). As described in Simulations of the experiment of Malemska et al. with standard dynamics, we varied \(k_1\) and \(k_1\) in the range of 0.05 \(\mu M\)/ms \(\leq k_1 \leq 5 \mu M\)/ms and 0.05 ms\(^{-1}\) \(\leq k_1 \leq 5\) ms\(^{-1}\). We have chosen \(k_1 = 0.5 \mu M\)/ms and \(k_1 = 0.5\) ms\(^{-1}\) as standard values.

There are two known calcium extrusion mechanisms, the CaATPase, an ATP-driven Ca\(^{2+}\) pump, and the Ca/Na exchange (Dipolo and Beaugé 1983). The first is a low-capacity, high-affinity pump, whereas the latter is a high-capacity, low-affinity mechanism. Little is known, however, about the density of these extrusion mechanisms in hippocampal neurons. Following Zador et al. (1990), we use first-order Michaelis-Menton kinetics to describe each of the two extrusion mechanisms, i.e.,

\[
\frac{\partial[\text{Ca}^{2+}]}{\partial t} = \frac{A}{V} \left( J_{\text{ leak}} - P, K_{\text{max}} \frac{[\text{Ca}^{2+}]}{[\text{Ca}^{2+}]+K_d} \right)
\]  

(9)

Here \(A\) is the surface area and \(V\) the volume of the compartment under consideration. The leak flux \(J_{\text{ leak}}\) was adjusted such that at a resting concentration of 50 nM the net extrusion of calcium was zero (Table 2). The value of \(K_d\) was taken from Zador et al. (1990). For abbreviations, see Table 1.

**TABLE 2. Parameters of calcium dynamics**

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<tr>
<th>Calcium dynamics</th>
<th>Value</th>
<th>Units</th>
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<tbody>
<tr>
<td>Diameter, spine head</td>
<td>(a_{\text{head}})</td>
<td>0.5 (\mu m)</td>
</tr>
<tr>
<td>Diameter, spine neck</td>
<td>(a_{\text{neck}})</td>
<td>0.1 (\mu m)</td>
</tr>
<tr>
<td>Diffusion constant</td>
<td>(D)</td>
<td>0.6 (\mu m^2/)s</td>
</tr>
<tr>
<td>Initial concentration of calcium</td>
<td>([\text{Ca}^{2+}]_0)</td>
<td>50 nM</td>
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<tr>
<td>Calcium fraction of NMDA current</td>
<td>(I_{\text{Ca/NMDA}}/I_{\text{Ca}})</td>
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<tr>
<td>Concentration of buffering sites</td>
<td>([\text{bufree}])</td>
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<tr>
<td>Forward buffering rate</td>
<td>(k_f)</td>
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<tr>
<td>Backward buffering rate</td>
<td>(k_b)</td>
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<td>Calcium pumps</td>
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<td>Pump efficiency, ATPase</td>
<td>(P, K_{\text{max}})</td>
<td>1 (\times) 10(^{-15}) (\mu mol/(m^2 \cdot m^2))</td>
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<tr>
<td>Pump efficiency, Na/Ca exchange</td>
<td>(P, K_{\text{max}})</td>
<td>5 (\times) 10(^{-15}) (\mu mol/(m^2 \cdot m^2))</td>
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<td>Pump affinity, Na/Ca exchange</td>
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<td>Leakage flux, ATPase</td>
<td>(J_{\text{ leak}})</td>
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<td>Leakage flux, Na/Ca exchange</td>
<td>(J_{\text{ leak}})</td>
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<tr>
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<td>(V_{\text{max}})</td>
<td>0.1 \times V_{\text{spinehead}}</td>
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<tr>
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<td>Depletion rate</td>
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<td>Store time constant</td>
<td>(\tau_{\text{store}})</td>
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<td>Calcium response threshold</td>
<td>([\text{Ca}^{2+}]_0)</td>
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<tr>
<td>Calcium response maximum</td>
<td>([\text{Ca}^{2+}]_{\text{max}})</td>
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**Model of intracellular calcium stores**

As mentioned in the INTRODUCTION, it is most likely that Ca\(^{2+}\) stores play an important role in the induction of LTP. We studied a model of intracellular stores in the spine head of a synapse, in particular the dynamics of calcium release by this store. Intracellular stores consist of three components: pumps to sequester calcium, calcium binding proteins such as calmodulin, and store calcium, and RYR and InsP\(_3\) receptor channels to release calcium from the stores. Neurons are supposed to contain both receptor types. For a detailed review see Berridge (1993).

To activate the InsP\(_3\) receptor both InsP\(_3\) and calcium are needed. The dependence on InsP\(_3\) is a all or none response, viz., the receptor is inactive below some critical value and becomes active above it (Berridge 1993). The activation level depends on the calcium concentration of the surrounding medium. As the concentration of Ca\(^{2+}\) rises it becomes increasingly active. Beyond a Ca\(^{2+}\) of ~200–300 nM, InsP\(_3\) becomes inhibitory (Bezprozvanny et al. 1991). Thus there is a bell-shaped calcium response (Bezprozvanny et al. 1991; Finch et al. 1991). The RYR receptor displays a similar bell-shaped calcium dependence (Hyml et al. 1988), but it seems that no coagonist is needed. Because there may be different subtypes of receptors with varying characteristics in different types of neurons and because little is known about these receptors in CA1 neurons, a model of their properties can only be qualitative. In particular, the mechanism of how the two types of receptors contribute to calcium release during LTP induction is still unclear. We therefore have decided to model both receptors by a single, phenomenological equation. This seems to be reasonable because both mediate calcium-induced calcium release with a similar bell-shaped calcium-dependent response.

Not much is known about the number and shape of intracellular calcium stores in CA1 neurons. For reasons of simplicity we as-
summed that there is a single store in the spine head. Its volume was set to be 1/10 of the spine head volume. The store was placed in the second diffusion compartment; see Fig. 4. Because calcium released from the store spreads almost instantaneously all over the spine head, the shape and distribution of buffers is of no importance for our results. For the maximum concentration of stored $\text{Ca}^{2+}$, we have chosen values between 2 and 25 mM. These values are consistent with measurements in frog muscle sarcoplasmic reticulum (Hasselbach and Oetiker 1983).

In our model the dynamics of calcium release from the store is given by

$$\frac{d}{dt}[\text{Ca}^{2+}]_{\text{store}} = \rho X ([\text{Ca}^{2+}]_{\text{store}} - [\text{Ca}^{2+}]_{\text{spine}})$$

(10)

where $[\text{Ca}^{2+}]_{\text{store}}$ and $[\text{Ca}^{2+}]_{\text{spine}}$ are the calcium concentrations inside the store and in the spine head, respectively. The depletion rate $\rho$ depends on the number of channels, the maximum channel conductivity, and the volume of the store. In our simulations we use $\rho = 1/(150 \text{ ms})$. The factor $X$ is the fraction of open channels, which depends on both the calcium concentration in the spine and the probability (RA) of receptor agonist binding. To be specific, we assume first-order kinetics, viz.

$$\frac{d}{dt} X = -\frac{1}{\tau_{\text{store}}} \{ X - (RA) \text{Re}([\text{Ca}^{2+}]_{\text{spine}}) \}

(11)

where \text{Re}([\text{Ca}^{2+}]_{\text{spine}}) models the bell-shaped $\text{Ca}^{2+}$ response of the receptors and $\tau_{\text{store}}$ is some channel time constant. We have checked that our results are not sensitive to the value of $\tau_{\text{store}}$ and we have fixed $\tau_{\text{store}}$ to 100 ms. As mentioned before, (RA) is the probability of receptor agonist binding. In our simulations, we consider two situations, viz., first the case where no agonist is available, that is (RA) = 0, and second, the case where we have a large amount of agonist (e.g., InsP3). In the latter situation all available receptor sites are saturated and we set (RA) at 1.

Equations 10 and 11 are assumed to give a phenomenological description of $\text{Ca}^{2+}$ transport out of the store and are certainly not a full model of the microscopic processes of calcium release from the store. In all simulations the store contained a maximum amount of $\text{Ca}^{2+}$ at the beginning of the simulated experiment. In our model, the calcium response $\text{Re}([\text{Ca}^{2+}]_{\text{spine}})$ is 0 below a threshold value of $[\text{Ca}^{2+}]_{\text{spine}}$ of 150 nM. For $[\text{Ca}^{2+}]_{\text{spine}}$ > $[\text{Ca}^{2+}]_{\text{spine}}$ it obeys the equation

$$\text{Re}([\text{Ca}^{2+}]_{\text{spine}}) = R_0 \frac{[\text{Ca}^{2+}]_{\text{spine}} - [\text{Ca}^{2+}]_{\text{spine}}}{[\text{Ca}^{2+}]_{\text{spine}} - [\text{Ca}^{2+}]_{\text{spine}}} \exp \left[ -\frac{[\text{Ca}^{2+}]_{\text{spine}} - [\text{Ca}^{2+}]_{\text{spine}}}{[\text{Ca}^{2+}]_{\text{spine}} - [\text{Ca}^{2+}]_{\text{spine}}} \right]

(12)

a so called $\alpha$-function; cf. Fig. 6. The response function $\text{Re}([\text{Ca}^{2+}]_{\text{spine}})$ takes its maximum of 1 at a concentration of $[\text{Ca}^{2+}]_{\text{max}}$ = 250 nM, which is in the range of measured values for $\text{Ca}^{2+}$.

**Fig. 6.** Bell-shaped $\text{Ca}^{2+}$ response $\text{Re}([\text{Ca}^{2+}]_{\text{spine}})$ of the receptor as a function of the calcium concentration. The curve has its maximum at an intracellular $[\text{Ca}^{2+}]$ of 250 nM. The maximum is scaled to the value of 1. The response vanishes for $[\text{Ca}^{2+}] < 150$ nM.

**Fig. 7.** Decay of intracellular $[\text{Ca}^{2+}]$ after 10 impulses, 30 impulses (thin lines), or 50 impulses (thick line) at 100 Hz. $N = 20$ synapses have been stimulated simultaneously (strong stimulation paradigm). In all cases the decay is fast and the resting concentration is reached within ~100 ms.

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In our simulations we varied the buffering constants systematically in order to find a reasonable set of constants that would yield an increased calcium level for sufficiently long times. In a first attempt we fixed $\tau_{\text{store}}$ and $k_f$ and $k_i$ in a reasonable regime (i.e., by a factor of 1/10 or 1 and combinations thereof). The buffers serve as short-time integrators that smooth the time course of the intracellular $\text{Ca}^{2+}$. Buffering also has some influence on the peak value of calcium concentration during stimulation; cf. Holmes and Levy (1990), Gold and Bear (1994). A change of the buffering constants does not, however, prolong the calcium decay after stimulation.

Next we reduced the $\text{Ca}^{2+}$ fraction of the NMDA current...
to 2% (cf. Zador et al. 1990). As a result, the overall Ca\(^{2+}\) during stimulation is significantly lower. The decay time after stimulation remains unchanged.

Examining the effects of the Ca\(^{2+}\) extrusion mechanisms is a rather complicated and arduous task because there are many potentially relevant parameters. In some cases (with very weak pumps) even the influence of dendritic calcium comes into play. We conducted many simulations examining this problem and find that a decrease in pump efficiency has a similar effect to that of an increase of the Ca\(^{2+}\) fraction of the NMDA current. A typical result with reduced pump efficiency is shown in Fig. 5. If the pump efficiency is lowered by a factor of 5, the weak stimulation paradigm (50 Hz at \(N = 10\) synapses) leads to an average Ca\(^{2+}\) of \(~20\ \mu\text{M}\) in the spine head. This value must be considered unrealistic because it is much larger than the one suggested by the experiments of Muller and Connor (1991). Note that, independent of the pump efficiency, the decay of the Ca\(^{2+}\) is rather fast and occurs within some 100 ms.

In conclusion, all of the above simulation results indicate that an additional active Ca\(^{2+}\) source that sustains an increased Ca\(^{2+}\) level after the end of a tetanic stimulation is necessary to explain the 2-s criterion. It is not possible to change the parameters of passive decay such that there is a clear elevation of intracellular Ca\(^{2+}\) levels lasting 1–2 s after the end of the stimulation. As will be shown in the next two parts, intracellular stores can take over the role of this source.

**Simulations of the experiment of Malenka et al. with intracellular stores**

In this part we present results with the extended model including intracellular calcium stores. We simulated the scenario of Malenka et al. (1992), but because we are interested in the decay, we restricted the simulation to four impulses at 100 Hz (\(N = 30\)). Figure 8A shows the time course of Ca\(^{2+}\) in a simulation where we used an initial calcium concentration of 25 mM for the store. It can be seen that Ca\(^{2+}\) levels \(>400\ \text{nM}\) can be maintained for \(>1\) s. Because of the bell-shaped response function, calcium release is not possible while the intracellular Ca\(^{2+}\) is high, as during stimulation. After the end of the stimulation at \(t = 30\) ms, the internal calcium concentration drops rapidly. If the calcium concentration has decreased to \(~500\ \text{nM}\), the stores open and additional calcium is released. We note that the exact duration of the period during which the Ca\(^{2+}\) is significantly above its resting value depends on parameters such as the size of the store, the initial Ca\(^{2+}\) inside the store, the dimensions of the spine, and the pump rates. Because the present model is supposed to be qualitative, we did not examine this dependence in more detail. There are, however, certain requirements concerning the minimum amount of stored calcium. In Fig. 8B, the time course of Ca\(^{2+}\) inside the store during the simulation of Fig. 8A is plotted. During the stimulation, the intracellular calcium concentration is high and blocks the release. Comparing Fig. 8, A and B, it is evident that the Ca\(^{2+}\) in the spine head stays at relatively high values (\(>400\ \text{nM}\)) as long as the store is not empty and is able to supply extra calcium to compensate for the loss of calcium due to extrusion and diffusion. This accounts for the almost linear decline of the Ca\(^{2+}\) in the store. In this regime, the receptor activation function can be understood as a controller in a closed circuit. If the store is nearly empty, calcium release stops and standard Ca\(^{2+}\) decay takes over. The specific time dependence of the decay depends on the form of the activation function \(R_e\). We used an \(\alpha\)-function because it is easy to compute and its maximum can be easily adjusted. It should be clear that there are more complicated activation functions that might contain additional parameters by which the decay can be modified in different ways. We feel, however, that our model with a bell-shaped \(\alpha\)-function-type calcium response yields reasonable results.

**Intracellular stores with primed and theta-burst stimulation**

To demonstrate the power of the above concept of intracellular stores, we applied our model to a scenario of primed and theta-burst stimulation. Before we discuss the results of our simulations, we give a short overview of the specific properties of both paradigms.

A priming stimulus (e.g., 4 impulses at 100 Hz) followed by a burst of four impulses at 100 Hz at another group of synapses applied after an interburst interval of 200 ms is termed "primed burst stimulation." Experiments with variable interburst intervals were conducted by Larson and Lynch (1986). It turned out that strongest LTP was induced at an interburst interval of 200 ms. LTP was weak at an interval of 100 ms and invisible at an interval of 2,000 ms. For reasons of simplicity we refer to all of these stimulation patterns as the primed burst scenario.

In other experiments Larson and Lynch applied several
bursts of four impulses at 100 Hz with variable interburst intervals to a single group of synapses (Larson et al. 1986). This stimulation pattern is termed "theta-burst stimulation." The strength of the induced LTP has a similar dependence on the interburst interval to the one found with the primed burst scenario. The strongest LTP is induced at an interval of 200 ms; intervals of 100 and 1,000 ms induce weaker LTP; but virtually no LTP has been found with intervals of 200 ms. Below we refer to these experiments as the theta-burst scenario. The similarities in the induction of LTP indicate, in our opinion, that both scenarios are based on the same microscopic effects. We have therefore simulated a single scenario that is supposed to cover qualitatively both primed and theta-burst experiments. As our stimulation paradigm, we take two bursts with four impulses at 100 Hz each (N = 10) and vary the interburst interval. We thus take a property of the primed burst scenario, two stimuli only, and combine it with a property of the theta-burst scenario, namely stimulating a single group of synapses. A discussion of the limitations of this approach will be deferred to the DISCUSSION section.

Figure 9A shows the results of a simulation of the above scenario. Several runs with variable interburst intervals are plotted in the same graph. The first peak of the intracellular Ca\(^{2+}\) is due to influx of extracellular calcium during the first burst. After the burst, the stores open and the Ca\(^{2+}\) stays at an elevated level (thick line). If a second burst is applied after an interburst interval of 200, 500, 1,000, or 1,500 ms (thin lines), the Ca\(^{2+}\) shows a second peak. The peak amplitude is maximal for an interburst interval of 200 ms. It is slightly reduced but still larger than in the model without stores (Fig. 9B) for interburst intervals of 500 or 1,000 ms. The store has, however, no effect if the interburst interval is \(\geq \)1,500 ms.

These results regarding the time course of the calcium concentration can be related to LTP induction if one assumes that LTP is possible only if the peak Ca\(^{2+}\) exceeds a critical concentration Ca\(^{2+}\). In a simple model, we can take the strength of LTP to be proportional to the excess concentration Ca\(^{2+}\) - Ca\(^{2+}\). If the critical concentration necessary for LTP induction is \(\sim 1.5 \mu M\), then according to our simulation results of Fig. 9A, LTP can be induced at interburst intervals of 200, 500, or 1,000 ms, but not with an interburst interval of 1,500 ms.

DISCUSSION

This section is divided into two parts. In the first part we discuss conclusions from our simulations of the experiment of Malenka et al. (1992) concerning the possible role of intracellular Ca\(^{2+}\) stores in the induction of LTP. In the second part we focus on the interpretation of the results relating to the primed and theta-burst stimulation paradigm.

The experiments of Malenka et al. (1992) indicate an elevation of the intracellular Ca\(^{2+}\) during 1-1.5 s after the end of the stimulus for this particular stimulation pattern. We do not know whether this would also hold for other experimental paradigms of LTP induction. In any case, the experiments of Malenka et al. can be used to check the plausibility of some models of calcium dynamics. As shown in Simulations of the experiment of Malenka et al. with standard dynamics, standard calcium dynamics fails to give a time course of Ca\(^{2+}\) in the spine head, consistent with the experiments of Malenka et al. (1992). NMDA channels close rapidly after the end of the stimulation and cannot sustain a persistent rise in intracellular calcium. Furthermore, the standard model cannot be adapted by a mere change of parameters. Thus an additional source of calcium is needed. As mentioned in INTRODUCTION, there is growing evidence for an important contribution of RYR- and InsP\(_3\)-receptor-mediated calcium release from intracellular stores.

We have introduced a model of intracellular stores with bell-shaped calcium response and have shown that calcium-induced calcium release from stores can indeed account for a significant elevation of the intracellular calcium level after the end of synaptic stimulation. Of course, such a model cannot be quantitative because the distribution of intracellular stores and the properties of receptors in CA1 pyramidal cells are not known in sufficient detail. Our studies suggest, however, that the bell-shaped Ca\(^{2+}\) response, a common property of both RYR and InsP\(_3\) receptors, plays an important role. In fact, with a bell-shaped response, calcium release from the store starts only after the stimulation when the Ca\(^{2+}\) drops below a certain value.

We emphasize that our model is not intended to give a detailed description of the molecular processes leading to calcium release from the stores. In particular, we do not...
model the reaction chain leading to a binding of the agonist (e.g., \text{InsP}_3) to the receptor; cf. Eq. 11. In the present version of our model we simply assume that a sufficient amount of \text{InsP}_3 (or none at all) is available at the stores. In this case, a short burst of three or four spikes arriving at a single synapse will trigger the process of calcium release from the stores. Furthermore, if the pump efficiency \( P, K_{\text{max}} \) is reduced (cf. Zador et al. 1990), then even a single spike at a single synapse starts the process of calcium release, a result that is rather implausible. The fact that the calcium release can be triggered even by a small amount of calcium is generic and not sensitive to buffer rates and neuronal time constants. On the other hand, the process of self-sustained calcium release is sensitive to the depletion rate \( \rho \) and the portion of open channels \( X \). If \( \rho \) or \( X \) is reduced by a factor of 10, calcium supply from the stores is not sufficient to compensate the loss due to diffusion and extrusion. In this case a sustained calcium release cannot be achieved, not even after a strong stimulation of the neuron. Thus our model of intracellular stores shows two completely different regimes. For low values of \( \rho \) and \( X \), self-sustained calcium release is not possible at all; for higher values, calcium release from the stores is induced even by a small number of spikes. The amount of agonist (e.g., \text{InsP}_3) could be used to switch between the two regimes. This suggests an important role of metabotropic glutamate receptors, because \text{InsP}_3 can be produced by a reaction chain starting at metabotropic glutamate receptors (Bliss and Collingridge 1993). In the present version of the model, the mechanisms of \text{InsP}_3 production are not described explicitly, but we suppose that our main results remain unchanged, if the dynamics of metabotropic glutamate receptors and \text{InsP}_3 are included.

We mention that stores are not the only solution that yields a sustained increase in \( \text{Ca}^{2+} \). Alternatively, voltage-dependent \( \text{Ca}^{2+} \) channels could serve as long-lasting calcium sources. Calcium channels are known to play an important role during LTP induction in CA3 mossy fiber synapses (Fisher and Johnston 1990; Jaffe and Johnston 1990) and in kitten visual cortex (Komatsu and Iwakiri 1992). To account for the 2 s criterion, such channels must have intrinsic time constants longer than a few hundred milliseconds. Otherwise they close as soon as the membrane potential returns to the resting value, i.e., within 100–200 ms; cf. Fig. 3. In the present study we have neglected the potential relevance of voltage-dependent calcium channels and have focused on intracellular stores in spines of hippocampal CA1 neurons.

There is overwhelming experimental evidence that NMDA receptors are crucial for LTP induction in CA1 neurons (Bliss et al. 1993), but, as we have shown here, they cannot be the only \( \text{Ca}^{2+} \) source. Both our results and the experiments of Malenka et al. (1992) suggest that there might be two basic effects due to the intracellular \( \text{Ca}^{2+} \) playing an important role in the induction of LTP.

1) Brief tetanic stimulation or other special stimulation patterns cause short but high peaks in the intracellular \( \text{Ca}^{2+} \) because of calcium influx through NMDA channels, which might trigger a biochemical reaction chain.

2) To maintain the reaction chain and eventually induce LTP, a persistent rise in the intracellular \( \text{Ca}^{2+} \), possibly at lower levels around a few hundred nanomolars, is necessary. This is the potential task of intracellular stores.

The way in which both effects interact could determine the duration and strength of the induced potentiation. We are aware of the fact that because of uncertainties in the measurement of important parameters such as pump efficiency, buffer rate, channel conductivity, or the distribution of intracellular stores, the model as well as our conclusions cannot be quantitative. But, in our opinion, stores lead to an interesting and potentially relevant behavior that deserves examination by future experiments.

As we have shown in the previous section, our theory of intracellular stores can also explain some of the temporal requirements of primed and theta-burst stimulation. With primed or theta-burst stimulation, LTP can be induced if the interburst interval is in the range of 200–1000 ms. This suggests that two different time constants indicating two different processes are involved. We make no attempt to explain the molecular process leading to the minimum interburst interval of 200 ms. This time constant could be due to the reaction chain starting at metabotropic glutamate receptors, which eventually leads to binding of \text{InsP}_3 at the stores, a sequence of reactions that is not modeled in our present work. Our model of intracellular stores does, however, provide a plausible scenario for the 1,000-ms time constant. Because of their similar dependence on interstimulus intervals, we have assumed that the same processes are involved both in primed and theta-burst stimulation. This means that theta-burst stimulation is equivalent to a repeated primed burst stimulation. Larson and Lynch (1986) have demonstrated that the first burst causes a diffuse priming effect all over the neuron that lasts for \( \sim 2 \) s. Because of this, long-duration depolarization alone cannot be the main cause of priming. We suggest that the priming burst induces an influx of calcium through voltage-gated calcium channels at each spine. The influx alone would not be sufficient to induce LTP, but it causes intracellular stores to release calcium, if the agonist \text{InsP}_3 or RYR is available. As we have seen in the last section, the release has a characteristic time of 1–2 s. This allows us to suggest the following interpretation. The first burst does not induce LTP, because the critical level of \( \text{Ca}^{2+} \) is not reached, but it triggers calcium release from the stores. When the second burst is applied, the influx of \( \text{Ca}^{2+} \) through NMDA channels at the stimulated synapses and the remaining efflux of \( \text{Ca}^{2+} \) from intracellular stores sum up to a peak \( \text{Ca}^{2+} \) high enough to induce LTP. Because of buffer saturation this summation is nonlinear, which means that relatively high concentrations can be reached with a rather weak stimulation pattern. The induction of LTP with theta-bursts could work in the same way. The only difference is that “priming” is applied at the same synapses as the following burst.

To summarize, we have presented a model of intracellular \( \text{Ca}^{2+} \) stores that can explain several experimental results, in particular the primed and theta-burst scenario, which cannot be explained by standard calcium dynamics. Because of a lack of experimental data, however, our model must remain tentative. Future experiments will hopefully supply enough data for refining the model to allow fully quantitative predictions.
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