SECURITY AND ROBUSTNESS OF LOCALIZATION TECHNIQUES FOR EMERGENCY SENSOR NETWORKS

BY

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THESIS

Submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in Computer Science and Engineering in the Graduate School of the State University of New York at Buffalo, 2008

Buffalo, New York

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Abstract

Recent advancement in radio and processor technology has seen the rise of Wireless Sensor Networks (WSN) as a reliable and cost-effective tool for real-time information gathering and analysis tasks during emergency scenarios like natural disasters, terrorist attacks, military conflicts, etc. Post-deployment localization is extremely important and necessary in these applications. But, current distributed localization approaches are not designed for such highly hostile and dynamic network conditions. This dissertation studies the adverse effects of factors like cheating behavior, node disablement and measurement inconsistencies on the corresponding localization protocols and attempts to provide simple and efficient solutions in order to overcome these problems.

The first problem addressed in this dissertation is, how to perform efficient distance-based localization in the presence of cheating beacon nodes? This dissertation attempts to answer two fundamental questions in distance-based localization: (*i*) In the presence of cheating beacons, what are the necessary and sufficient conditions to guarantee a bounded localization error? and (*ii*) Under these conditions, what class of algorithms can provide that error bound? In this part of the dissertation, it is shown that when the number of cheating beacons is greater than or equal to some threshold, there is no localization algorithm that can guarantee a bounded error. Furthermore, it is also proved that when the number of malicious beacons is below that threshold, a non-empty class of bounded error localization algorithms can be identified. Two secure distance-based localization algorithms are outlined and their performance is verified using simulation experiments.

The next part of the dissertation underscores the lack of fault-tolerance in existing localization protocols and proposes simple mechanisms to overcome this problem. Sensor node disablement adversely affects the overall node deployment distribution and the efficiency of localization techniques that depend on this distribution, for example, signature-based techniques. In order to improve the fault-tolerance in these schemes, it is important to first construct a probabilistic model for node disablement. In this direction, the phenomenon of sensor node disablement is modeled as a stochastic time process. A novel deployment strategy that non-uniformly deploys sensor nodes over the monitored area is also outlined. Then, a fault-tolerance related improvement to existing localization schemes is proposed, which discards observations from unhealthy groups of nodes during the localization process. In order to overcome the complexity concerns, a simple signature-based technique, called ASFALT, is also proposed. ASFALT estimates the target location by first predicting distances to known location references using the underlying node distribution and a simple averaging argument. Extensive measurements from simulation experiments verify the fault-tolerance and performance of the proposed solutions.

In the final part of this dissertation, the problem of efficiently mitigating inconsistencies in location-based applications is addressed. Inconsistencies in location information, caused by cheating behavior or measurement errors can be modeled using a weighted, undirected graph and a cheating location function that can assign incorrect locations to the nodes or a cheating (but verifiable) distance function that can assign inconsistent distances to edges. In either case, an edge relation where the assigned edge distance is not within some very small factor of the Euclidean distance between the connecting nodes represents some inconsistency and is referred to as an inconsistent edge. The problem of efficiently mitigating location inconsistencies in the network can then be formulated as an optimization problem that determines the largest induced subgraph (obtained by eliminating a subset of vertices) containing only consistent edges. Two optimization problems can be stated. The first maximizes the number of vertices in the consistent subgraph. Combinatorial properties including hardness and approximation ratio for these problems are studied and intelligent solution strategies are proposed. A comparative analysis that verifies the practical efficiency of these algorithms by using measurements from simulation experiments is also presented.

Acknowledgments

I would like to begin by thanking my advisor and mentor over the past 4 years, Dr. Shambhu J. Upadhyaya. Without his continuous support and direction, I don't think this dissertation would have been possible. Input provided by him during the numerous technical discussions and project meetings helped me in not only shaping my dissertation topic but also in overcoming key road-blocks during the research and experimentation phase. I feel really lucky and privileged to get his guidance and direction towards the completion of this dissertation.

I would also like to thank Dr. Sheng Zhong and Dr. Jinhui Xu for being in my dissertation committee and being so actively involved with my research and dissertation in general. The lengthy discussions with them during research meetings were always insightful and technically invigorating. I would like to thank Dr. H. Raghav Rao for being an active member of my dissertation committee and providing invaluable suggestions and feedback during my proposal presentation.

I would also like to express my gratitude towards Dr. Sviatoslav Braynov, who was my graduate student advisor during the course of my Masters degree. He got me started on the right foot by getting me involved with his research activities and projects early. He was also an excellent teacher. I would also like to thank the numerous other faculty members at UB, including Dr. Chunming Qiao, Dr. Hung Ngo, Dr. Murat Demirbas, Dr. Kenneth Regan and Dr. Alan Selman from the Department of Computer Science and Engineering and Dr. Raj Sharman from the School of Management, who were actively involved with my research in some way or the other.

I would like to extend my special thanks to all my colleagues and friends in the CEISARE research group. Suranjan Pramanik, my house-mate, office-mate and also a close friend was always available, either it be for discussing a research idea or for watching a movie. Mohit Virendra would never be late to share a quick joke or a recent related paper at MOBICOM. Ashish Garg would always be available if you ever need a unique perspective on a recent submission or a great deal on the latest electronic gadget. I have learned a lot, both technically and personally, from other colleagues in the research group, notably, Ramkumar Chinchani, Madhusudhanan Chandrasekaran, Vidyaraman Sankaranarayanan and Sunu Mathew. I had the opportunity to work in the company of a talented bunch of people! Outside of the research group, I am really thankful to Qi Duan and Manik Taneja for their efforts towards the completion of the various research projects and experiments that are a part of this dissertation. Over the period of time, I made many friends here at UB. Some of the most important ones have been my past housemates Gaurav Sinha and Megha Parekh, and a group of friends nicknamed "buffalodudes". Guys, thank you very much for your love and support! I would also like to thank all other graduate students that attended Dr. Upadhyaya's research group meetings and gave valuable feedback on this dissertation.

My sisters, Sakina bhen and Kaniza, have always been supportive of my career ambitions. I express my heartfelt gratitude to you both for your continuous love and support during the completion of this dissertation.

There are no words to describe how grateful I am to my wife, Tasneem, for all the love and support I received from her, especially during the final stages of this dissertation. She always motivated me to work hard and never to give up in life. Tasneem, I thank you with all my heart.

Finally, this dissertation would not have been possible, if it were not for the unconditional love, support and sacrifices from my beloved Mom and Dad. My Dad has been a tremendous motivator and has always inspired me to bring out the best in myself, whether it be life or graduate studies. It is a matter of great sorrow that he moved on to a better place during the course of this dissertation and could not witness its completion. But, I am sure that he is constantly watching over me and is extremely proud to see me finish this dissertation. To Mom and Dad, I dedicate this dissertation to you both!

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List of Abbreviations

ESN Emergency Sensor Network.

GPS Global Positioning System.

ToA Time of Arrival.

TDoA Time Difference of Arrival.

RSSI Received Signal Strength Indicator.

MLE Maximum Likelihood Estimation.

MDS Multidimensional Scaling.

GSP Group Selection Protocol.

CRLB Cramér Rao Lower Bound.

MMSE Minimum Mean Square Estimation.

PCGG Partially Consistent Grounded Graph.

Chapter 1

Introduction

"We're not lost. We're locationally challenged."

- John M. Ford

1.1 Emergency Sensor Networks

An emergency, as defined by the American Heritage Dictionary, is a "serious situation or occurrence that happens unexpectedly and demands immediate action." This serious situation can be a result of natural calamities like hurricanes, forest fires, earthquakes, etc., or due to human related actions like terrorist attacks, industrial accidents and wars. During such emergencies, one of the most important tasks of the government and related agencies is to minimize the loss of life and property. Irrespective of the cause/type of emergency, accurate information from the emergency site is very essential in order to successfully execute any response or rescue operation. But, due to the hostility, inaccessibility and unpredictability at the site of the emergency, traditional methods of information collection like aircraft surveillance, humans and satellite images may not be feasible or may not be able to give the ground truth. Thus, traditional means of information collection during emergencies are reinforced by employing a network of miniature, battery-powered sensor *motes*[†] that monitor critical parameters like temperature, pressure, acceleration, etc., at the emergency site and provide real-time information which can be effectively used for emergency response. These

[†]the words mote and node are used interchangeably

motes are cheap, commercially available and can self organize to form a wireless, ad-hoc network without much infrastructure support. These motes communicate with each other using small range wireless radio links and can also interface with other high-end devices like laptops, PDAs, etc., on a wired or wireless interface. Such specialized wireless networks, often referred to as wireless sensor networks, are slowly gaining popularity for use in critical emergency and first response applications like environmental monitoring [13, 37, 51], healthcare [82, 88], emergency response [64] and military applications [77]. Wireless sensor networks used for such specialized emergency applications are also referred to as *Emergency Sensor Networks (ESNs)* [48]. Figure 1.1 presents an illustrative example of an ESN deployed in a forest fire scenario. It shows sensor nodes deployed



Figure 1.1: An Example of a Forest Fire ESN Application

over a forest area to monitor the spread of forest fire. The sensor network relays the temperature information from the various parts of the forest back to the fire station. Response coordinators at the station use information aggregated by these sensors to coordinate a response and direct fire fighters to areas needing immediate attention.

ESNs are gaining tremendous importance, especially in emergency, first response and military applications, as highlighted in the article published by the Department of Homeland Security [1]. This article shortlists plans by the department to pursue long-term research and development projects in sensor networks. But, the implementation and deployment of sensor networks for emergency and military applications is not straightforward. There are a variety of issues in services like routing, localization, coverage, deployment, synchronization, etc., that need to be addressed before successfully deploying and implementing such networks for emergency and other monitoring applications [86]. This dissertation addresses the issue of robust and fault-tolerant localization in ESNs and related applications.

1.2 Localization in ESNs

Localization or *location discovery* is the problem of determining the position of each sensor node after being deployed at an area of interest. Localization is important in ESNs because information in emergency response applications is extremely location critical. Any information collected by the sensors is useless unless it is associated with the location (of occurrence) information. Also, location information is required in providing an effective response in emergency situations. For example, in fire rescue situations it is very important for fire fighters to know which locations within the building have the highest temperature measurements so that they can effectively execute rescue operations without risking personal injury. Also, localization is necessary because manual deployment may not be possible in such networks. In case of manual deployment, the location of each node can be noted as it is deployed and post-deployment localization is not required if the nodes in the network are static. But, localization is required as a post-deployment service if deployment is done by alternative methods like aerial scattering, where the final position of the nodes is not known after deployment or if the network topology is dynamic (node mobility can be one reason for this). Distributed localization protocols for WSNs can be classified into two broad categories: (1) *Beacon-based* and (2) *Beaconless* or *Signature-based* approaches.

1.2.1 Beacon-based Localization

Beacon-based approaches [4,11,14,39,62,70,75,84,91] require a few special nodes called beacon (or anchor) nodes. These beacons already know their absolute locations via GPS [42] or manual

configuration and are fitted with high power transmitters. Remaining nodes first compute distance (or angle estimates) to these fixed set of beacons and then estimate their location by using basic trilateration (or triangulation). The working of a basic two-dimensional beacon-based localization scheme is depicted in Figure 1.2. In this figure, nodes B_1 , B_2 , B_3 and B_4 located at positions



Figure 1.2: Beacon-based Localization Technique

 $(x_1, y_1), (x_2, y_2), (x_3, y_3)$ and (x_4, y_4) respectively, act as beacon nodes. The target node *T* estimates distances z_1, z_2, z_3 and z_4 respectively to these beacon nodes and computes its location (x_T, y_T) by trilateration. Efficient techniques for computing distances like *Received Signal Strength Indicator (RSSI), Time of Arrival (ToA), Time Difference of Arrival (TDoA)* exist and have been successfully used in the various localization protocols [3,40]. RSSI estimates distance by applying well-known radio propagation models to radio power loss (difference in the packet receipt and sent power at the receiver) [66], while ToA [69] and TDoA [94] estimate distance by observing the time of packet receipt or delay in packet receipt, respectively. One of the most common examples of a beaconbased localization technique can be found in today's GPS receivers. GPS receivers are able to compute their absolute location by efficiently computing distances to four or more GPS satellites

(that acts as beacons) using the Time of Arrival distance computation technique [42]. Despite their high utility in modern infrastructure-based networks and devices, beacon-based schemes suffer from some major drawbacks and cannot be used with the same ease and efficiency in wireless sensor networks, especially ESNs [48].

Problems with Beacon-based Approaches

Some of the limitations in applying existing beacon-based approaches to sensor networks, especially ESNs, are:

- 1. GPS receivers are costly and the cost of fitting each beacon node (or each node in the network) with a GPS receiver may be infeasible for a large sensor network.
- 2. GPS receivers do not work well for indoor environments and may affect the accuracy of the location advertised by the beacon nodes.
- 3. Beacon nodes can cheat by either advertising incorrect self location in order to disrupt the trilateration process or by manipulating transmit power levels, packet time-stamps, etc., to disrupt accurate distance estimation. From Figure 1.3, we can see that Beacons B_1 , B_2 and B_4 are honest while B_3 cheats by manipulating the distance estimation and B'_3 cheats by lieing about its location. Moreover, B_3 and B'_3 can also collude causing the target node T to compute its location incorrectly.

The first two problems discussed above are technology related constraints and can easily be overcome with better and cheaper technology. But, from the point of view of deployment in hostile and military scenarios, the problem of cheating beacons is much more significant. During wartime emergencies and terrorist attacks, nodes can be captured by the enemy and reprogrammed to propagate malicious data and inaccurate information to thwart localization and other services. Similar attacks can also be carried out by disgruntled workers or military deserters (insiders). Thus, it is extremely important to study the robustness of beacon-based localization techniques in



Figure 1.3: Cheating Beacons in Beacon-based Localization

the presence of cheating beacon nodes. Such a study is required in order to design algorithms that not only overcome the cheating effect of malicious nodes but also run efficiently on the already resource constrained sensor motes.

1.2.2 Signature-based (Beaconless) Localization

Signature-based (sometimes called Beaconless) localization techniques [10, 23, 26, 50, 68, 76, 76, 81, 96] do not require specialized beacon nodes that know their own positions. These schemes take advantage of any non-uniformity present in the overall node distribution over the deployment area to determine location. The main idea is to derive a mapping between the distribution of nodes and all the possible locations in the network. A target node computes its location by observing its neighborhood and using it as a "signature" to map to its correct location. An example of a signature-based scheme is depicted in Figure 1.4. It can be seen from Figure 1.4 that nodes are distributed in groups around fixed points (with known locations) in a non-uniform fashion. Based



Figure 1.4: Signature-based Localization

on this distribution, the probability for each location observing a fixed number of nodes from each group is then derived. The target node observes its neighborhood and chooses a location that maximizes the probability of observing that neighborhood. In this particular case, the "signature" is the number of nodes observed from each group. This idea is also intuitive. For example, if a node observes large number of nodes from groups 1, 2 and 4 as compared to the other groups then it is very likely that it lies within the square region surrounded by groups 1, 2 and 4. Apart from this, various other statistical and mathematical techniques, e.g., *Maximum Likelihood Estimation (MLE)* [26], *Multidimensional Scaling (MDS)* [50,81], *Error Control Coding Theory* [96], *ID-Codes* [76], etc., have also been used to correlate node distribution and network locations. Experimental results have shown that signature-based schemes produce coarse-grained localization as compared to beacon-based schemes. Nevertheless, they are effective in situations where it is not possible to deploy or work with beacon nodes. Similar to beacon-based systems, signature-based schemes also suffer from a myriad of problems, as discussed next.

Problems with Signature-based (Beaconless) Approaches

Some of the limitations in existing signature-based approaches are:

- 1. The accuracy of signature-based approaches depends on how closely it is able to approximate the actual on-the-ground distribution of sensor nodes. The more accurate this approximation, the better the resulting localization accuracy. But, this localization accuracy suffers if the onthe-ground distribution of nodes changes continuously. Current approaches assume that the distribution of nodes is static throughout the period of the application, which is not a practical assumption. The distribution of nodes can change after the initial deployment due to factors like node destruction, node movement, etc., caused by events at the deployment site. This is especially true in ESN applications.
- Signature-based schemes generally involve complex computations and may have high space (memory) requirement, which sometimes may not be feasible on the already resource constrained sensor motes.
- 3. The security of signature-based schemes is also an issue. An adversary can easily modify the on-the-ground distribution by inserting extra nodes in each group. Although such attacks, referred to as *False Node Injection* attacks [48], can be thwarted using efficient cryptographic schemes [63], it does not prevent an adversary from replaying communications from nodes that are not in the range of the target node. This can adversely alter the neighborhood observation of the target node, thus affecting the accuracy of the associated signature-based localization scheme.

The security issues in signature-based schemes, as discussed in point 3 above, are either directly related to shortcomings associated with existing cryptographic techniques in sensor networks or well documented attacks like "Wormhole" [95] or "Reply" [35] attacks. A variety of strong cryptographic techniques [2, 30] and strategies to overcome replay attacks [35, 72] in sensor networks have been proposed in the literature. These solutions can overcome the above mentioned secu-

rity related problem. However, what has not been addressed, is the problem of fault-tolerance in signature-based schemes. To ensure efficient deployment and localization, it is very important to ensure that signature-based approaches are not only simple and efficiently executable on sensor nodes but are also robust and fault-tolerant in highly hostile and dynamic scenarios.

1.3 Dissertation

Localization, as discussed earlier, is an extremely important service in wireless sensor networks and is also a highly studied topic within the research community. Past research has resulted in a variety of efficient and intelligent strategies for obtaining location information in a distributed fashion. Despite these advances, the applicability of the above techniques in highly hostile, error prone and dynamic applications is still a major concern. With the increasing popularity of wireless sensor networks for emergency response, extreme weather monitoring, military and anti-terrorism applications, the problems concerning the security and robustness of localization services can no longer be ignored. Obtaining efficient solutions to the various issues surrounding localization and location-based services in ESNs is the crux of this dissertation.

1.3.1 Motivation

Current localization techniques and applications for sensor networks were not designed with security and fault-tolerance in mind. This dissertation is motivated by the following specific security and robustness issues that arise in existing localization protocols and location-based services.

• In majority of the existing localization protocols, nodes that are programmed with the intention to help other nodes localize themselves, namely beacon nodes, are always assumed to be honest. But, such beacon or anchor nodes can cheat or behave maliciously, thus disrupting the ensuing localization service. This is especially true in scenarios where nodes can be easily accessed by an adversary or an insider and reprogrammed to thwart its correct functioning. The question to be addressed then is: Is it possible to overcome the malicious effect of beacon or anchor nodes in beacon-based localization protocols?

- In the past, localization protocols for sensor networks have assumed that the sensor nodes over the deployment area are static and undisturbed. But, in reality there can be considerable topology changes, especially in ESNs, due to various emergency related factors like fire, falling objects, flowing water, terrain changes, etc. Depending on the seriousness of the emergency, nodes in the network can be arbitrarily destroyed after deployment. This problem is further exacerbated due to the miniature and fragile nature of current day sensor motes, e.g., Crossbow® Mica2 [16] and iMote2 [15] platforms. There is a significant change in node distribution due to these factors and it eventually affects the accuracy of signature-based localization algorithms that depend on node distribution information. As a result, it is extremely essential to study the fault-tolerance of these localization schemes in order to guarantee application success in hostile and harsh conditions. The question that needs immediate attention is: Is it possible to design and feasibly implement signature-based localization techniques that are fault-tolerant to changes in node distribution and topology?
- In addition to causing problems during localization, cheating behavior by nodes in the network can also adversely affect other services that use location information, e.g., location aware routing [8, 53], neighborhood detection [72], etc. Nodes can cheat on location by advertising incorrect self-locations or transmitting at random power levels. Although location claims can be securely verified by neighboring nodes [78,92], verifiers can also cheat by providing false verification information. This verification for location claims is generally done by estimating the distance between the claimant and the verifier and comparing it with the Euclidean distance between the location claims. There is an inconsistency if the estimated distance between the two nodes does not match with the Euclidean distance between their advertised locations. Such inconsistencies can adversely affect the location-based services that depend on location information for successful execution. The problem of interest then

is, how to efficiently eliminate such inconsistent location information from the network?

1.3.2 Original Contributions

As outlined in the previous section, the main motivation in this dissertation is to improve the robustness and fault-tolerance of localization schemes and location-based services so that they can be efficiently used in ESNs and related applications. Each of the localization related issues listed in the previous section adversely affects a specific class of localization algorithms or applications and poses important questions regarding its efficiency in a specific situation. Thus, it is best to address each of the above issues separately and in the context of the localization approach it affects the most. Thus, this dissertation can be divided into three main parts.

Robust Distance-based Localization in the Presence of Cheating Beacons

As discussed earlier, beacon nodes in a distance-based localization protocol can cheat by providing incorrect distance or location information to nodes trying to compute their own location. In this part of the dissertation, the problem of robust distance-based localization in the presence of cheating beacon nodes is addressed. It can be formally described as, assuming a reasonable network model and a fixed upper bound on the number of cheating beacons, how to efficiently perform distance-based localization. This approach of localization in the presence of cheating nodes is in line with the philosophy of *"living with the bad guys*" as compared to detecting and eliminating them from consideration. In this regard, the specific questions that this dissertation aims to provide answers for are: Under what condition can a distance-based localization scheme overcome cheating behavior by malicious beacons? How to define or determine specific algorithms for doing this and what kind of guarantee on the solution quality can these algorithms provide? This dissertation specifically makes the following contributions in this direction [98].

• It lays a theoretical foundation for the problem of distance-based localization in the presence of cheating beacons. More specifically, it derives the *Necessary and Sufficient conditions* for

robust localization in the presence of such malicious or cheating beacons.

- It designs algorithms that are not only efficient to run but can also provide a *guarantee* on the maximum localization error. Specifically, it defines a *class of algorithms* that can localize with a bounded error and outlines two algorithms, namely the *Polynomial Time algorithm* and the *Fast Heuristic-based algorithm*, belonging to this class of bounded error localization algorithms.
- In order to show the generality of the proposed ideas, this dissertation extends existing analysis and results for a two dimensional coordinate system to a *three dimensional coordinate* system. It derives the required necessary and sufficient conditions for robust distance-based localization in a three dimensional coordinate system and defines a class of bounded error localization algorithms for these systems.
- Finally, it verifies the computational efficiency and error bounds of the proposed localization algorithms using measurements from computer simulation experiments.

Fault-tolerant Signature-based Localization

This part of the dissertation focuses on evaluating the effect of changes in node distribution on the accuracy of signature-based localization techniques. Here, we specifically focus on distribution changes due to destruction or disablement of nodes, which is a significant factor in ESNs. The eventual goal of this dissertation is to design fault-tolerant deployment and signature-based localization techniques that are robust against node disablement and suitable for use in ESN applications. This dissertation makes the following contributions in this direction [47,49].

• First, it proposes an *Emergency Level-based deployment strategy* that provides an efficient distribution of sensor nodes over the monitored area, especially during emergency situations and hostile environments. This strategy distributes sensor nodes over the monitored area by dividing the area into various emergency levels depending on the severity of the emergency

at each point on the area. Then, it proposes a non-homogeneous *stochastic framework* for modeling sensor node destruction over the deployment area. This stochastic model of node destruction is employed by the deployment strategy to make deployment decisions like determining deployment size for each group and predicting post-deployment node distribution. In addition to this, the deployment strategy also has provisions to monitor changes in node distribution due to random node disablement.

- Next, it proposes a node selection strategy, called *Group Selection Protocol (GSP)*, which complements current signature-based schemes by choosing appropriate groups of nodes for participation in the localization process. Results from simulation experiments are used to show that GSP improves the accuracy of existing signature-based localization approaches even in the presence of node disablement.
- Although GSP provides some improvement in accuracy, it does not simplify the localization process. Signature-based schemes are computationally intensive involving complex functions that may not be feasible on the resource constrained sensor nodes. To simplify the localization process, this dissertation proposes *A Simple, FAult-Tolerant (ASFALT) Signature-based Localization scheme*. ASFALT uses the distribution of nodes over the deployment area and a simple averaging argument to compute distances to known deployment points. Once these distances are known, simple trilateration can be used to compute location. Results from simulation experiments using the J-Sim network simulator [80] have shown that the performance and localization accuracy of ASFALT are better than that of other signature-based algorithms, especially in the presence of arbitrary node disablement.

Elimination of Cheating in Location-based Applications

In the final part of this dissertation, the problem of eliminating cheating behavior in locationbased services and applications is addressed. *Inconsistencies* (or cheating behavior) in location advertisement and verification can be represented by a special type of edge in a graph-based model of the network, called the *Partially Consistent Grounded Graph (PCGG)*. As a result, the edge set of a PCGG can be partitioned into two distinct sets, namely, a set of consistent edges and a set of inconsistent edges. The problem of eliminating location-based inconsistencies in a network can then be formulated as the problem of determining a fully consistent subgraph from the PCGG of the network. Two optimization problems are formulated, namely, *MAX-CON* and *LARGEST-CON*. MAX-CON is the problem of obtaining the largest consistent graph in terms of vertices while LARGEST-CON is the problem of obtaining the largest consistent graph in terms of the number of consistent edges. This dissertation makes the following specific contributions in this direction [46]:

- It proves the *combinatorial hardness* of the MAX-CON and LARGEST-CON problems.
- It shows that an efficient algorithm for the VERTEX-COVER problem can be used to obtain a solution for the MAX-CON problem. It also proves that LARGEST-CON cannot be approximated within a constant ratio unless P = NP.
- It proposes four polynomial time algorithms for LARGEST-CON, namely, *Greedy Approach*, *Local Solution Search*, *Simulated Annealing* and *Linear Programming (LP)* based approach.
- It compares the efficiency and accuracy of these algorithms using measurements from computer simulations.

1.3.3 Outline of the Disseration

Chapter 2 discusses the background and related work in the area of localization (both beaconbased and signature-based), outlines some of the advances in the area of robust and fault-tolerant localization and discusses shortcomings in current approaches that have been addressed in this dissertation. Chapter 3 studies the problem of robust distance-based localization in the presence of cheating beacon nodes. Chapter 4 addresses the problem of fault-tolerance in signature-based localization schemes by outlining an efficient node deployment strategy and a novel, fault-tolerant signature-based localization approach. Chapter 5 addresses the problem of eliminating inconsistent location information from graph-based models for location-dependent services and applications in sensor networks. Finally, Chapter 6 summarizes the major results outlined in the previous chapters and provides an overall perspective on the research discussed in this dissertation. It also draws important conclusions and provides directions for future research on a variety of open problems and topics related to secure and robust localization.

Chapter 2 Background and Related Work

"Fundamental progress has to do with the reinterpretation of basic ideas."

- Alfred North Whitehead

2.1 Introduction

Chapter 1 introduced the problem of localization in sensor networks including a brief description and survey of each type of localization technique and their shortcomings in specific sensor network applications. This chapter discusses the theoretical foundations for the problem of distributed localization in sensor networks and presents a detailed survey of the past and recent research efforts in overcoming the various security and robustness issues related to it. Such a study is not only helpful in understanding the current state-of-art in localization but is also useful in bringing out the novelty in the research described in this dissertation and putting it in perspective.

2.1.1 Chapter Organization

Section 2.2 surveys prior work in mathematical formulation and analysis of the distributed localization process in wireless sensor networks and presents some important theoretical results in this area. Section 2.3 surveys prior research efforts on securing localization schemes against malicious behavior by nodes and against large measurement errors. Section 2.4 surveys prior work on improving the robustness and fault-tolerance of localization schemes in sensor network applications. Each of these sections also discusses how some of the issues which have been overlooked or unaddressed in the current literature are addressed in this dissertation.

2.2 Theoretical Foundations for Localization Schemes in Sensor Networks

In order to have a better understanding of the computational model and fundamental limits associated with solving the problem of distributed localization, a thorough study of existing mathematical formulations and related theoretical results is extremely essential. It also serves as a good starting point and motivates the design of novel and efficient formal methods to tackle the security and robustness issues associated with localization.

2.2.1 Current Models and Results for Localization

The first result in this direction has been presented by Savvides et al. [79]. They have derived the *Cramér-Rao lower bound (CRLB)* for network localization, expressed the expected error characteristics for an ideal algorithm and compared it to the actual error in an algorithm based on multilateration. The authors have concluded that the error introduced by the algorithm is just as important as the measurement error in assessing end-to-end localization accuracy. Eren et al. [25] have provided a theoretical foundation for the problem of network localization in which some nodes know their locations and other nodes determine their locations by measuring the distances to their neighbors (beacon-based approaches). They constructed *Grounded Graphs* to model network localization such that the vertices of the graph correspond to nodes in the network and an edge exists between two nodes if they are in the radio range of each other. A distance function assigns each edge a value that signifies the estimated distance between the two nodes. The authors have proved that a network has a unique localization if and only if its underlying grounded graph

is generically globally rigid. In addition, the authors have also studied the computational complexity of the network localization problem and have showed that a certain subclass of globally rigid graphs, trilateration graphs, can be constructed and localized in linear time. Goldenberg et al. [31] took this a step further by studying Partially Localizable Networks (PLN), i.e., networks in which there exist nodes whose positions cannot be uniquely determined. The authors have demonstrated the relevance of partially localizable networks and using the grounded graph model of Eren et al. [25] designed a framework for two dimensional network localization with an efficient component to correctly determine which nodes are localizable and which are not. Bruck et al. [10] have modeled the localization problem by representing the sensor network as a Unit Disk Graph (UDG) and have studied the localization problem as an embedding problem in the corresponding UDGs for the network. A UDG is an unweighted graph induced by a set of points in the Euclidean plane such that two points have an edge connecting them if and only if the distance between them is no more than 1. They have showed that it is NP-Hard to find a valid embedding in the plane such that neighboring nodes are within distance 1 from each other and non-neighboring nodes are at least distance 1 away. Bruck et al. [10] suggested that despite the NP-Hardness of finding a valid embedding in a UDG, one can find a planar spanner of a UDG by using only local angles. The authors have also proposed a practical beaconless embedding scheme by solving a Linear Program (LP).

In summary, it is clear that the network localization problem can be viewed as a two-dimensional graph realization (embedding) problem that assigns coordinates to each vertex such that all (or a maximum number of) the edge constraints are satisfied. Moreover, knowing the locations of the beacon nodes, provided they behave honestly and advertise their correct locations, is a good partial solution to the realization problem in the corresponding graph of the network. Despite the above results, the existing graph-theoretic models cannot be used to study the problem of secure localization as explained in the following section.

2.2.2 Discussion

From the results of Eren et al. [25] and Bruck et al. [10], it is clear that a network has a unique localization if and only if the underlying grounded graph is globally rigid. Besides graph rigidity, another factor that affects valid embedding of a grounded graph is the distance function which assigns a positive weight to each edge depending on the estimated distance between the two nodes. Eren et al. in [25] have assumed that the beacon locations are always correct and the distance function is always honest, i.e., it always assigns the correct or consistent distance to each edge. Such relaxed assumptions are admissible while deriving fundamental limits for the complexity and solution quality of the localization algorithms in ideal systems, where all the nodes in the network can be assumed to be honest. Stricter models are needed for studying the properties of localization algorithms and location-based applications in practical systems where not all nodes can be assumed to be honest. Moreover, certain graph-based models for the network, like the Unit Disk Graph (UDG) suggested by Bruck et al. [10], may not be the correct representation of sensor networks. In this model, two nodes are connected by an edge if the distance between them is less than 1 (symbolically). In sensor networks, nodes may be less than 1 unit away from each other but still not able to communicate (due to obstacles) or may be farther away from each other and still able to communicate. In other words, in order to study the security related properties of localization techniques in highly distributed and autonomous systems like sensor networks, more practical and robust models of the network are required.

Lack of appropriate models for studying the security and robustness properties of the localization problem has been the main motivating factor for this dissertation. Majority of the research effort in this dissertation has been spent on proposing and working with sound and practical mathematical models of the network. For example, Chapter 3 studies the distance-based localization problem in the presence of cheating nodes by assuming a very practical network and adversarial model. In this model, the distances provided by honest beacons follow some fixed distribution with known mean, while the distances provided by cheating beacons do not follow any distribution and are arbitrary. Moreover, the proposed adversary model is also very strong and considers all possible cases of collusion among cheating nodes. There has been no prior research in the literature on network localization that has employed such a strong network and adversary model. A similar trend can be seen in Chapter 5 where the problem of efficient elimination of inconsistent location information in the network is formulated by describing a more practical variant of the Grounded Graph model by Eren et al. [25], called the Partially Consistent Grounded Graphs. In summary, it can be said that a lack of appropriate models had left a gap between the current results for the problem of distance-based network localization and their translation to a more practical scenario consisting of adversaries. This dissertation attempts to fill this gap by employing efficient techniques for modeling the network together with the adversary, in order to derive the necessary conditions and fundamental limits for secure localization and location related services.

2.3 Secure Localization

As discussed in Section 1.2, cheating behavior by participating nodes (including beacons) can not only adversely affect the accuracy of localization schemes but also disrupt the working of all location dependent applications. Cheating in localization schemes is generally characterized by either nodes providing incorrect self-locations or by neighboring nodes manipulating the distance estimation process. More specifically, data provided by the cheating nodes during localization is arbitrary in nature and may deviate from the actual value by a large margin. On the contrary, data from honest nodes is generally accurate or within some small error margin. Even measurement and noise errors due to certain network conditions follow some fixed pattern or distribution and are generally bounded. In this section, the earlier research efforts towards securing localization schemes in wireless networks are surveyed. Some of the schemes outlined here were not designed for sensor networks, but the basic idea used for securing localization in such schemes is still pretty interesting and worth exploring. Most of the prior works in this area have followed one of the following two themes as described next.

2.3.1 Malicious Node Detection and Elimination

One approach followed by researchers to secure the location discovery process in wireless sensor networks is to detect the cheating nodes and eliminate them from consideration during the localization process. Liu et al. [59] have proposed a method for securing beacon-based localization by eliminating malicious data. This technique, called attack-resistant Minimum Mean Square Estimation (MMSE), took advantage of the fact that malicious location references introduced by cheating beacons are usually inconsistent with the benign ones. It filters out malicious beacon signals (location references) by examining inconsistency among multiple beacon signals (location references) as indicated by the mean square error of estimation. Similarly, the Echo location verification protocol proposed by Sastry et al. [78] can securely verify the location claims by computing the relative distance between a prover and a verifier node. The Echo protocol uses the time of propagation of ultrasound signals for this purpose. Nodes for which the location verification fails are labeled as malicious nodes. However, this verification technique could also come under attack if a malicious node can cause the ultrasound signal to travel at a faster rate by manipulating the media of propagation. Čapkun et al. [90] have also shortlisted and analyzed various attacks related to node localization in sensor networks. They proposed mechanisms like authenticated distance estimation, authenticated distance bounding, verifiable trilateration and verifiable time difference of arrival by which nodes can verify their mutual distances and locations, and demonstrated the applicability of these mechanisms for securing the beacon-based localization process. Pires et al. [74] have proposed protocols to detect malicious nodes in range-based localization approaches by detecting malicious message transmissions. A message is considered malicious if its signal strength is incompatible with its originator's geographical position. In other words, the verifier node compares the received signal strength of communication from another node with its expected value which is calculated using the nodes' geographical information and pre-defined transceiver specifications. In addition to this, the authors have also proposed a protocol for disseminating information about malicious nodes to other nodes in the network. In another work by Liu et al. [60], the authors have proposed techniques to detect malicious beacon nodes in beacon-based localization approaches by employing special *detector nodes* that can capture malicious message transmissions by cheating beacons and disseminate this information to other benign nodes and detectors.

In summary, the basic premise of the above approaches has been that localization in wireless sensor networks can be improved by identifying and eliminating such malicious message transmitting nodes.

2.3.2 Robust Localization Schemes for Sensor Networks

The second approach is to design techniques that are robust enough to tolerate the cheating effect of malicious nodes (or beacons), rather than explicitly detecting and eliminating them. Moore et al. [68] have formulated the localization problem in wireless sensor networks as a *two-dimensional graph realization problem* and have described a beaconless (anchor-free), distributed, linear-time algorithm for localizing nodes in the presence of large range measurement noise. The authors have defined the probabilistic notion of robust quadrilaterals as a way to avoid flip ambiguities, which would otherwise corrupt localization computations.

Some other research attempts in the past have also tried to solve the robust localization problem by formulating it as a global optimization problem. Li et al. [58] have developed robust statistical methods to make localization attack-tolerant. The authors have proposed an *adaptive least squares* and *least median squares* position estimator for beacon-based localization using triangulation. Alternatively, Doherty et al. [23] have described a localization method using connectivity constraints and convex optimization, where some number of beacon nodes are initialized with known positions. The authors have formulated the localization problem as a *feasibility problem* with radial constraints. Nodes that can hear each other are constrained to lie within a certain distance of each other. Semi-definite programming has been used to find a globally optimal solution to this convex constraint problem. In the case where communication is directional, the method formulates the localization problem as a LP problem, which is solved by an interior point method. But, one shortcoming of this approach is that it needs beacon nodes to be placed on the outer boundary, preferably at the corners. Only in this setup are the constraints tight enough to yield a useful configuration. When all anchors are located in the interior of the network, the position estimation of outer nodes can easily collapse toward the center, which can lead to large estimation errors. Liu et al. [59] have designed a voting-based scheme where the deployment area is divided into a grid of cells. In this scheme, the target node resides in one of the cells and each beacon node votes on each cell depending on the distance between the target node and the beacon. The location of the target node is then estimated as being within the cell that has the maximum number of votes. Other researchers have attempted to overcome the problem of malicious beacons by proposing localization techniques that do away with beacons altogether. For example, Yi et al. [81] and Ji et al. [50] have applied efficient data analysis techniques like *Multi-Dimensional Scaling (MDS)* using connectivity information and distances between neighboring nodes to infer target locations. Similarly, Priyantha et al. [75] have proposed the CRICKET system which has eliminated the dependence on beacon nodes by using communication hops in order to estimate the network's global layout and then used force-based relaxation to optimize this layout. Fang et al. [26] have modeled the localization problem as a statistical estimation problem by using Maximum Likelihood Estimation (*MLE*) to estimate the most probable location given a set of neighborhood observations.

Recently, ideas from the coding theory have also been applied to achieve robust localization. For example, Ray et al. [76] have proposed a new framework for providing robust location detection in wireless sensor networks based on the theory of *Identifying Codes (ID-Codes)*. High powered transmitters are fitted in such a way that each localizable point on the terrain is covered by a unique set of transmitters. Then, each node localizes itself by hearing from the transmitters and mapping to the corresponding location. Similarly, Yedavalli et al. [96] have used the theory of *error correcting codes* for robust localization in sensor networks. For each localizable point, they used distances from a fixed set of neighboring nodes to that point as a "codeword" for that point. One property of this set of codewords is that the "distance" between any two codewords is fixed. In coding theory, the distance between any two codewords is the number of bits they differ. Any cheating behavior by the participating nodes can result in an illegal codeword and can be
detected and corrected. Lazos et al. [56] have proposed a range independent distributed localization algorithm using sectored antennas, called *SeRLoc*, that does not require any communication among nodes. They have showed that SeRloc is robust against malicious attacks like the wormhole attack, sybil attack and compromised sensor attack. However, SeRLoc is based on the assumption that no jamming of the wireless medium is feasible. Lazos et al. [57] have also presented a hybrid approach that unlike *SeRLoc*, provides robust location computation and verification, without centralized management and vulnerability to jamming. The authors proposed a positioning system called RObust Position Estimation (ROPE) that limits the ability of an adversary to spoof a sensor's location. To quantify the impact of attacks against ROPE, the authors introduced a novel metric called Maximum Spoofing Impact (MSI) that denotes the maximum distance between the actual location of the sensor under attack, and any possible spoofed location.

Researchers have applied really intelligent and interesting strategies to minimize the cheating effect of malicious nodes during localization. Although, most of the works outlined above formulate the localization problem as some form of an optimization problem and attempt to derive a solution that minimizes errors and inconsistencies, other techniques like error correcting codes and ID-Codes have also been shown to produce good results. The following section discusses some of the shortcomings of the above techniques as well as problems that have not yet been addressed. It also outlines the contributions of this dissertation in that regard.

2.3.3 Discussion

It is clear from Section 2.3.1 that majority of the malicious node detection and elimination strategies in beacon-based techniques take into account the inconsistency in measurement of a particular network parameter (caused by the cheating behavior) in order to detect cheating nodes. Although they have been verified to perform well in most cases, one shortcoming of those techniques has been the assumption of fully honest verifier nodes (or detector beacons as in the case of [60]). These schemes will fail if this assumption about honest verifiers does not hold. Moreover, there can be no fixed guarantees on the number of detected cheating nodes by these schemes and therefore the accuracy of the ensuing localization algorithms. Any undetected cheating beacon node will only add to the error of the localization algorithm. This dissertation does not address the problem of detecting and eliminating cheating beacons, but addresses two very related problems that can overcome the above mentioned security and robustness concerns. Chapter 3 studies the problem of robust distance-based localization in the presence of cheating nodes where the focus is not to detect and eliminate cheating beacons but to design algorithms that can withstand the effect of such cheating beacons. Assuming a practical network and a very strong adversary model, it outlines conditions for robust localization and proposes efficient bounded error distance-based localization algorithms to overcome the cheating effect of a certain fixed number of malicious nodes. These algorithms do away with the requirement for (honest) verifier or detector nodes and their bounded error property guarantees the localization accuracy. Chapter 5 studies an intuitively similar problem, but in this case rather than locally detecting and eliminating inconsistency causing nodes, the central idea is to obtain the largest globally consistent network structure. This would imply efficiently eliminating the inconsistency causing nodes. The current problem of eliminating cheating beacon nodes from beacon-based localization techniques can be efficiently modeled as this problem of obtaining the largest globally consistent beacon network.

Localization schemes discussed in Section 2.3.2 improve the robustness of the localization procedure by employing intelligent statistical or optimization techniques on global information like distance between nodes, neighborhood relations, location information of some nodes, etc., to weed out or minimize the effect of inconsistent or erroneous data in order to improve localization accuracy. This particular methodology is very similar to the one used for the robust distance-based localization discussed in Chapter 3. On the contrary, one of the schemes outlined in Section 2.3.2, namely the voting-based technique proposed by Liu et al. [59], belongs to the class of bounded error, robust distance-based localization algorithms defined in this chapter. As compared to the other similar works in this direction, e.g., [23, 58, 81], the robust distance-based localization scheme (Chapter 3) in this dissertation does not use complex statistical and optimization techniques to achieve robustness against cheating beacons, but employs heuristics that are not only computationally feasible but also practically efficient. Moreover, it also presents a complete analytical treatment of the problem which was absent in some of the previous works. Next, a detailed survey on prior work in the area of fault-tolerance in localization schemes is presented.

2.4 Fault-tolerance

Node Failure, as discussed in sections 1.2 and 1.3, is a significant problem in ESNs. Failure of nodes to operate or communicate correctly can adversely affect various services (including localization) in highly distributed systems like wireless sensor networks. De Souza et al. [20] have provided an excellent taxonomy of the various faults in wireless sensor networks and surveyed the various fault-detection and fault-recovery mechanisms. One such technique for detecting faults due to physical impacts or incorrect orientation has been proposed by Harté et al. [36]. The authors have designed a flexible circuit using accelerometers that can act as a sensing layer around each node and is capable of sensing and reporting the physical condition of each node. Macedo et al. [65] have studied the effects of physical and communication faults on routing protocols, while Liu et al. [61] have proposed a fault-tolerant node placement technique so that data can be efficiently relayed throughout the network even in the presence of faults and broken links. Paradis et al. [73] have provided an excellent survey and comparison of existing fault tolerant techniques for various sensor applications like routing, transport and/or application layers. The next section outlines some recent and past efforts in the direction of fault-tolerant localization.

2.4.1 Fault-tolerance of Localization Schemes

Despite these advances in the area of fault-tolerance in sensor networks, the problem of faulttolerance of localization protocols has not received much attention. Since beacon-based schemes solely depend on beacon or anchor nodes for localization, their performance suffers drastically when beacon nodes fail, i.e., failure of a beacon node affects the localization process of all the nodes utilizing information from that beacon. Tools like error correcting codes [96] and ID- codes [76], as discussed in the previous section, have been successfully used to provide some level of fault-tolerance against disabled beacon nodes. In another work, Bulusu et al. [12] have argued that beacon placement (position of beacon nodes) strongly affects the quality of spatial localization in beacon-based approaches. The authors have further showed that uniform and dense placement of beacon nodes is not always viable for localization and will be inadequate in noisy environments. Moreover, arbitrary movement (and obviously, disablement) of beacon nodes will prevent them from being in good positions in the network, thus affecting the accuracy of the associated localization schemes.

Similarly, there has been little progress in the design of fault-tolerant mechanisms for signaturebased or beaconless type of localization schemes. The most notable work, although not directly in the domain of wireless sensor networks, was proposed by Tinós et al. [87]. The authors have presented a novel fault tolerant localization scheme for a system of mobile robots, called Millibots, that measured distances between themselves and used maximum likelihood estimation process to determine their locations. In this technique, fault tolerance was achieved in two steps: the system first detected and isolated the faults based on the information redundancy in the dead reckoning and distance measurements. The localization algorithm then reconfigured itself to overcome the faults. In another related work, Ding et al. [21] have proposed a median-based mechanism for reducing the effect of faulty sensor nodes in certain types of target detection and localization algorithms.

As evident from the above survey, there has been some research on mechanisms to detect and eliminate node faults in sensor networks. But, fault-tolerance of localization schemes in these networks has been highly overlooked. Also, the problem of fault-tolerance is gaining a lot of importance, especially due to the extreme and hostile nature of modern day sensor network applications. In conclusion, the ground is fertile for research on fault-tolerance in localization schemes. The next section discusses some of the shortcomings of existing localization schemes as far as fault-tolerance is concerned and the contributions of this dissertation in order to overcome them.

2.4.2 Discussion

With the very limited progress in the area of fault-tolerant localization mechanisms, it is extremely essential to initiate and pursue worthwhile research on this problem. To partly address the issue of node failure, sensor node manufacturers have introduced protective covers to reduce/eliminate physical damage to the highly fragile sensor nodes in extreme conditions. But, physical impact or damage may not be the only reason for a node to be rendered useless. A node's inability to communicate with other nodes due to some external factors is as good as the node being dead. In other words, physical covers do not provide immunity from damage and failures can still occur. Past works on localization schemes, as discussed previously in this chapter, have completely ignored this issue of damaged/faulty nodes during localization. For example, the signature-based scheme by Lei et al. [26] was not designed with fault-tolerance in mind. This is evident from the very simplistic node deployment strategy proposed by the scheme. Similarly, beacon-based schemes are affected by disablement of the participating beacon nodes.

This dissertation takes the first step to address the fault-tolerant localization issue in sensor networks. Since the problem is much more challenging in signature-based schemes as compared to beacon-based schemes, it first focuses on the problem of fault-tolerance in signature-based schemes. It addresses the fault-tolerance issue by providing an emergency level-based deployment strategy, which unlike the scheme by Lei et al. [26] does not deploy equal sized groups and also has provisions to monitor changes in node distribution. It also proposes a novel signaturebased scheme, which is not only fault-tolerant but also less complex as compared to the scheme proposed by Lei et al. [26].

2.5 Conclusion

This chapter presented a detailed survey of mechanisms used in existing literature to overcome the security and fault-tolerance related problems in localization schemes for sensor networks. It also outlined drawbacks and shortcomings of these solutions, keeping in mind the specific requirements

and conditions of ESN applications, and highlighted advances made by this dissertation in overcoming some of these shortcomings. The first problem studied in this dissertation, i.e., the problem of robust distance-based localization in the presence of cheating beacon nodes, is presented next.

Chapter 3

Robust Distance-based Localization in the Presence of Cheating Beacons

"No, we don't cheat. And even if we did, I'd never tell you."

- Tommy Lasorda (American Baseball Player and Coach, 1927)

3.1 Introduction

In this chapter, the problem of robust distance-based localization in the presence of cheating (malicious) beacon nodes is addressed. This chapter first presents a detailed analytical treatment of the problem by deriving necessary conditions for robust localization and then defines a class of algorithms that can achieve localization with a bounded error. Two novel algorithms that belong to this class are also outlined and evaluated using extensive simulation experiments.

3.1.1 Motivation and Problem Statement

As discussed in Chapter 1, beacon-based algorithms are a popular choice for location discovery in a variety of distributed wireless network systems including ESNs. In beacon-based schemes, nodes first estimate distances to a set of beacon nodes and then use trilateration or any other constraint satisfaction technique to compute their own location. Majority of the existing beacon-based techniques assume that the nodes acting as beacons are always honest and provide the correct distance/location information to the other nodes. But in highly hostile environments, like ESNs, beacons can cheat by broadcasting incorrect self locations or by manipulating the transmit power levels, thus altering the distance computation and effectively the estimated final location of the target nodes. In other words, cheating beacons can adversely affect the accuracy and efficiency of the associated distance-based localization technique.

Previous research efforts in this direction, as outlined in Chapter 2, focused on either removing this (over) dependence on beacon nodes or on minimizing the effects of malicious beacons during localization. The problem of distance-based localization using beacon nodes is well investigated (both analytically and implementation-wise), but a similar systematic analytical study of this problem in the presence of malicious nodes does not exist. Although some strategies have been proposed to overcome the malicious effect of cheating beacon nodes, there has been no study on the hardness and feasibility of the basic problem itself. Such a study is required in order to answer the following important questions: Under what condition(s) can a distance-based localization scheme overcome the cheating effect of malicious beacons? When such localization schemes exist, how can we determine them? What kind of guarantee on the solution quality (in terms of bounds on the error in localization) can the associated algorithms provide? A thorough theoretical treatment of the problem will not only help identify the requirements for robust distance-based localization in the presence of cheating beacons, but will also help the algorithm designers compare the error bounds of their distance-based algorithms under the worst case condition.

The research presented in this chapter makes the following contributions to the problem of robust distance-based localization:

Necessary Conditions. It is proved that if the number of malicious nodes is greater than or equal to $\frac{n-2}{2}$, where *n* is the number of beacons providing information, then no algorithm can provide any bounded degree of localization accuracy in all cases.

Class of Bounded Error Localization Algorithms. It is shown that there exist algorithms that provide a guaranteed degree of localization accuracy, if the number of malicious beacons is less than or equal to $\frac{n-3}{2}$. To prove this result, a non-empty class of algorithms is identified such that

every algorithm in this class determines the target location with bounded localization error in all cases.

Localization Algorithms. Two illustrative examples of algorithms in this class are proposed. The first algorithm has a worst-case polynomial complexity (specifically, $O(n^3)$, where *n* is the number of beacon nodes). The second algorithm is based on a clever heuristic and has much better practical efficiency. The localization accuracy and computational efficiency of the proposed algorithms are further verified through simulation experiments.

Generalization of Results. Current results for two dimensional systems are extended to three dimensional systems.

3.1.2 Chapter Organization

This chapter is organized as follows. Section 3.2 presents the network and the adversary model. Section 3.3 addresses the problem of robust distance-based localization in the presence of cheating beacons. Section 3.3.1 derives and proves the necessary condition for existence of localization algorithms with a guaranteed error bound; Section 3.3.2 gives the definition of the algorithm class that provides the above mentioned guaranteed degree of accuracy while Section 3.3.3 presents the error bound analysis. Two novel algorithms that belong to this class are outlined in Section 3.4, while the experimental evaluations for these algorithms are presented in Section 3.5. The extension to the three dimensional scenario is given in Section 3.6. Section 3.7 concludes the chapter with some remarks and discussions on the significant results presented in the chapter.

3.2 Network and Adversary Model

In our network model, a mobile device M in a non-trustworthy environment wants to compute its own location using distance estimates to a set of beacon nodes. These beacon nodes know their own location and may or may not cheat about their location to other nodes. The target node M and the beacon nodes are currently assumed to be located on a two dimensional area (plane), i.e., the location of each of these entities can be represented as two dimensional coordinates (x, y) where, $x, y \in \mathbb{R}$. First, the results and analysis for a two dimensional system are presented and later in Section 3.6 these results are extended to three dimensional systems.

Now, suppose that the target node *M* has *n* beacons available for localization. Let these beacon nodes be denoted as B_1, \ldots, B_n . Among these *n* beacons, some beacons are malicious (cheating beacons). Let *k* denote the number of malicious or cheating beacons. It is important to note that *k* is not necessarily known to the mobile device or to any of the honest beacons. However, the value of *k* clearly has a great influence on whether a bounded localization error can be achieved or not. In Section 3.3.1, the condition for having a bounded localization error based on the value of *k* is established. Let k_{max} ($\leq n$) be an upper bound on the number of malicious nodes, i.e., k_{max} is the maximum number of malicious nodes that can exist in the network at any time. The parameter k_{max} is a system or environment dependent constant and is generally known to the localization algorithm.

Beacons that are not malicious are honest, i.e., they fully cooperate with the localization protocol by disclosing the information as truthfully as possible. More details on the cheating behavior by the beacon nodes will follow shortly. Regardless of being honest or dishonest, each beacon B_i provides M with a measurement \tilde{d}_i of the distance between B_i and M. (In practice, each beacon B_i actually provides M with some information from which the distance \tilde{d}_i can be computed efficiently by M. In order to simplify the current exposition, it is assumed here that B_i provides M the distance measurement \tilde{d}_i directly. This should not affect the presented results.) The precise distance between B_i and M is the Euclidean distance between the position coordinates of B_i and M and is denoted by $dst(B_i, M)$. Let the set of honest beacons be denoted by H. Then, for each beacon $B_i \in H$, \tilde{d}_i is assumed to be a random variable that follows some fixed probability distribution, denoted as $msr(dst(B_i, M))$, such that

$$E[d_i] = dst(B_i, M),$$

i.e., the expected (mean) value of the estimated distance \tilde{d}_i for each beacon B_i in H, is the precise distance between the beacon B_i and the node M. In the case when B_i is honest, the difference between the estimated and the true distance is assumed to be very small, i.e.,

$$|\tilde{d}_i - dst(B_i, M)| < \epsilon_i$$

where ϵ is a small constant. Ideally, this difference should be zero when the beacon is honest, but such discrepancies in distance estimates can occur due to factors like *measurement errors* either at the source or target.

For each beacon $B_i \notin H$, i.e., a cheating beacon, the corresponding \tilde{d}_i is a value selected arbitrarily by the adversary. Note that, colluding attacks are implicitly allowed here: In the model presented here, it is assumed that a single adversary controls all malicious beacon nodes (all $B_i \notin$ H) and decides \tilde{d}_i for them. This is a very strong adversary model, which in addition to independent adversaries also covers all possibility of collusion.

Since a distance-based localization strategy is assumed here, the output O of the corresponding localization algorithm can be defined by a function F of the measured distances (\tilde{d}_i) from the device M to every beacon node in the network as shown below.

$$O = F(\tilde{d}_1, \ldots, \tilde{d}_n)$$

The error e of the localization algorithm is defined as the Euclidean distance between the actual position of the mobile device and the one output by the algorithm.

$$e = E[dst(M, O)]$$

The next step is, given the above model, to derive the necessary conditions for the existence of an algorithm that can perform distance-based localization with a bounded localization error in the presence of malicious beacon nodes.

3.3 Robust Bounded Error Localization

The main focus of this section is to design bounded error distance-based localization algorithms that are robust against cheating beacon nodes. In this direction, the necessary and sufficient conditions for bounded error localization, given the above network and adversary model, are first derived. Then, a class of robust localization algorithms is defined such that if these necessary conditions are satisfied then a bounded localization error can be guaranteed. In addition to this, theoretical properties like maximum error bound for this class of algorithms is also studied.

3.3.1 Necessary Condition for Bounded Error Localization

In order to achieve a bounded localization error, the first step is to derive a threshold of the number of malicious beacons k in terms of the total number beacons such that if k is greater than or equal to this threshold then no algorithm would be able to guarantee a bounded localization error just based on the distances to the beacon nodes. Consequently, having the number of malicious beacons below this threshold is a necessary condition for getting a bounded localization error out of any distance-based localization algorithm. In other words, it is required to fix the minimum number of beacon nodes required, assuming that some of these beacons will cheat, to correctly compute the location using just the distance information. Theorem 3.1 gives this threshold or necessary condition.

Theorem 3.1. Lower Bound Theorem: Suppose that $k \ge \frac{n-2}{2}$. Then, for any distance-based localization algorithm, for any locations of the beacons, there exists a scenario in which *e* is unbounded. *Proof.* Without loss of generality, let $k = \frac{n-2}{2}$ (because more malicious beacons clearly can launch any attack that $\frac{n-2}{2}$ malicious beacons can launch). The proof for the above theorem follows a contradiction argument. Suppose that, in all scenarios the output error e < a, where *a* is a constant. It is shown that this supposition leads to a contradiction. It is first proved that for a fixed set of beacon nodes and beacon locations, if the above threshold holds (and if the exact identities of the malicious nodes are not known) then there exists at least two distinct scenarios having the same distribution of distances from the target node to the beacon nodes. This makes it impossible for any algorithm to differentiate between the two scenarios. Since the target locations in the two scenarios are significantly different, any algorithm must fail in one of the two scenarios.

Consider the two scenarios S_1 and S_2 , as shown in Figure 3.1. The locations of all the beacons are same in both the scenarios, but the set of honest beacon nodes and the position of the target node *M* is assumed to be different in each scenario. Select an arbitrary point *P* in the line segment B_1B_2 and draw a line *L* through *P* such that *L* is perpendicular to B_1B_2 . Choose an arbitrary number a' > a. Then there are two points P_1 and P_2 on the line *L* such that

$$dst(P_1, P) = dst(P_2, P) = \frac{1}{2}dst(P_1, P_2) = a' \ge a.$$



Figure 3.1: Two Scenarios for Lower Bound Theorem

In scenario S_1 , M is at location P_1 and the set of honest beacons is $H_1 = \{B_1, B_2, B_3, \dots, B_{k+2}\}$. Denote by $\tilde{d}_{i,1}$ the measurement \tilde{d}_i in scenario S_1 . So, for each $B_i \in H_1$,

$$\tilde{d}_{i,1} \sim msr(dst(B_i, P_1))$$

In scenario S_2 , M is at location P_2 and the set of honest beacons is $H_2 = \{B_1, B_2, B_{k+3}, \dots, B_{2k+2}\}$. Denote by $\tilde{d}_{i,2}$ the measurement \tilde{d}_i in scenario S_2 . So, for each $B_i \in H_2$,

$$\tilde{d}_{i,2} \sim msr(dst(B_i, P_2))$$

Assume that in scenario S_1 , the adversary chooses $\tilde{d}_{k+3,1}, \ldots, \tilde{d}_{2k+2,1}$ such that

$$\forall i \in \{k+3,\ldots,2k+2\}, \tilde{d}_{i,1} \sim msr(dst(B_i,P_2))$$

Similarly, assume that in scenario S_2 , the adversary chooses $\tilde{d}_{3,2}, \ldots, \tilde{d}_{k+2,2}$ such that

$$\forall i \in \{3, \dots, k+2\}, \tilde{d}_{i,2} \sim msr(dst(B_i, P_1))$$

Since B_1 and B_2 are on the perpendicular bisector of line segment P_1P_2 , we have

$$dst(B_1, P_1) = dst(B_1, P_2), and$$

 $dst(B_2, P_1) = dst(B_2, P_2)$

Therefore, we get two pairs of identical distributions as shown below.

$$msr(dst(B_1, P_1)) \cong msr(dst(B_1, P_2)), and$$

 $msr(dst(B_2, P_1)) \cong msr(dst(B_2, P_2))$

Now, it is easy to see that $(\tilde{d}_{1,1}, \tilde{d}_{2,1}, \tilde{d}_{3,1}, \dots, \tilde{d}_{2k+2,1})$ and $(\tilde{d}_{1,2}, \tilde{d}_{2,2}, \tilde{d}_{3,2}, \dots, \tilde{d}_{2k+2,2})$ are identically distributed. Consequently, the two outputs

$$O_1 = F(\tilde{d}_{1,1}, \tilde{d}_{2,1}, \tilde{d}_{3,1}, \dots, \tilde{d}_{2k+2,1})$$

and

$$O_2 = F(\tilde{d}_{1,2}, \tilde{d}_{2,2}, \tilde{d}_{3,2}, \dots, \tilde{d}_{2k+2,2})$$

are also identically distributed. This implies that

$$E[dst(P_2, O_1)] = E[dst(P_2, O_2)]$$

On the other hand, from the previous assumption it can be seen that the output errors in both scenarios are less than *a*.

$$e_1 = E[dst(P_1, O_1)] < a, and$$

 $e_2 = E[dst(P_2, O_2)] < a$

Consequently,

$$dst(P_1, P_2) = E[dst(P_1, P_2)]$$

$$\leq E[dst(P_1, O_1)] + E[dst(P_2, O_1)]$$

$$= E[dst(P_1, O_1)] + E[dst(P_2, O_2)]$$

$$< a + a$$

$$= 2a.$$

This is contradictory to the fact that $dst(P_1, P_2) = 2a' \ge 2a$.

This brings us to the next result which shows that, given the network model as explained in Section 3.2 and no more than $\frac{n-3}{2}$ cheating beacons, the location of *M* can be definitely computed (for all the scenarios) with an error bound proportional to ϵ .

3.3.2 Algorithm Class for Robust Bounded Error Localization

Theorem 3.1 showed that having $\frac{n-2}{2}$ or more cheating beacons makes it impossible to compute the location of M with a bounded error. The next set of result establishes that having $\frac{n-3}{2}$ or fewer cheating beacons makes it possible to compute the location of M with a bounded error. This particular condition can also be viewed as a sufficient condition for robust distance-based localization in the presence of cheating beacons. Moreover, a class of algorithms that can compute the location under this condition with a bounded localization error is also identified.

Before defining this algorithm class, let us introduce some terminology used during its definition (See Figure 3.2). For each beacon B_i , define a ring R_i using the following inequality:



Figure 3.2: Some Terminology for Class of Robust Localization Algorithms

$$\tilde{d}_i - \epsilon < dst(B_i, X) < \tilde{d}_i + \epsilon.$$

As mentioned in Section 3.2, ϵ is a small constant denoting some small measurement error. Clearly, there are altogether *n* rings. The boundary of these *n* rings consists of 2*n* circles — called the

boundary circles. In particular, the inner circle of a ring is called an *inner boundary circle*, while the outer circle of a ring is called an *outer boundary circle*.

Definition 3.1. A point is a *critical point* if it is the intersection of at least two boundary circles. An arc is a *continuous arc* if it satisfies the following three conditions:

- The arc is part of a boundary circle.
- If the arc is not a complete circle, then its two ends are both critical points.
- There is no other critical point in the arc.

An area is a *continuous region* if it satisfies the following two conditions:

- The boundary of this area is one or more continuous arcs.
- There is no other continuous arc inside the area.

The class of robust localization algorithms can then be defined based on these rings as follows.

Definition 3.2. A localization algorithm is in the *class of robust localization algorithms* if its output is a point in a continuous region r such that r is contained in the intersection of at least k + 3 rings.

Note that, the class of robust localization algorithms defined above is a *non-empty* class of algorithms. This statement follows from the following theorem which proves that as long as $k \leq \frac{n-3}{2}$, it is always possible to find a non-empty continuous region *r* satisfying the requirements in Definition 3.2.

Theorem 3.2. For $k \le \frac{n-3}{2}$, there exists a non-empty continuous region *r* in the intersection of at least k + 3 rings.

Proof. Consider the real location of mobile device M. Clearly, for each honest beacon B_i , M must be in the ring R_i as shown below.

$$\tilde{d}_i - \epsilon < dst(B_i, M) < \tilde{d}_i + \epsilon.$$

Since $k \le \frac{n-3}{2}$, i.e., $n \ge 2k + 3$, there are at least k + 3 honest beacons. So, M must be in the intersection of at least k + 3 rings. Define r as the continuous region in the intersection of these rings that contains the real location of M. Since M is in r, r must be non-empty. (Figure 3.3 gives an illustration.)



Figure 3.3: Existence of Intersection of Rings (k = 2)

In fact, an example algorithm that belongs to this class is the voting-based localization scheme proposed by Liu et al. [59]. In Liu et al.'s scheme, they compute the intersection region (as discussed above) by dividing the entire localization area into a square grid and then taking a vote for each candidate location on the grid. The candidate locations with the maximum votes belong to the intersection area. Although simple, the voting-based algorithm is computationally expensive as it has to store the states of all the points on the grid and does an exhaustive search for the point with the maximum votes. In Section 3.4, two other algorithms in this class of robust localization algorithms are proposed. These algorithms are much more efficient, one having a polynomial worst-case complexity and the other running very fast in practice. Next, we derive the worst case

error bound of algorithms in this class of robust localization algorithms.

3.3.3 Error Bound Analysis

To analyze the error bound of algorithms in this class, two new definitions are needed.

Definition 3.3. The *beacon distance ratio* (γ) is defined as the minimum distance between a pair of beacons divided by the maximum distance between a beacon and the mobile device.

$$\gamma = \frac{\min_{B_i, B_j} dst(B_i, B_j)}{\max_{B_i} dst(B_i, M)}.$$

Definition 3.4. Consider the lines going through pairs of beacons. Denote by $ang(B_iB_j, B_{i'}B_{j'})$ the angle between lines B_iB_j and $B_{i'}B_{j'}$ — to avoid ambiguity, we require that $0^\circ \le ang(B_iB_j, B_{i'}B_{j'}) \le 90^\circ$. The *minimum beacon angle* (α) is defined as the minimum of such angles.

$$\alpha = \min_{B_i, B_j, B_{i'}, B_{j'}} ang(B_i B_j, B_{i'} B_{j'}).$$

The following theorem bounds the maximum localization error possible in the presented robust localization framework.

Theorem 3.3. For $k \le \frac{n-3}{2}$, if $\epsilon \ll \min_{B_i} dst(B_i, M)$ and there are no three beacons in the same line, then the output error of any algorithm in the class of algorithms for robust localization, as defined in Definition 3.2, is

$$e < \frac{2\epsilon}{\min\left\{\sin\frac{\arcsin(\gamma\sin(\alpha/2))}{2},\cos\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right\}}$$

Proof. Consider the continuous region r. It is in the intersection of at least k + 3 rings. Since there are at most k dishonest beacons, at least 3 of these rings belong to honest beacons. Suppose that R_{i_1} , R_{i_2} , and R_{i_3} are three rings belonging to honest beacons among the at least k + 3 rings. Let r' be the continuous region in the intersection of R_{i_1} , R_{i_2} , and R_{i_3} that contains r. Since O is in r, clearly O is also in r'. Next, let's show that M is also in r'. Since M is also in the intersection of R_{i_1} , R_{i_2} ,

and R_{i_3} , only the following lemma is needed.



Figure 3.4: Intersection of Rings (Lemma 3.4)

Lemma 3.4. If $\epsilon \ll \min_{B_i} dst(B_i, M)$ and there are no three beacons in the same line then the intersection of R_{i_1}, R_{i_2} , and R_{i_3} has only one continuous region.

Proof. A contradiction argument is used to prove this lemma. Refer to the Figure 3.4. Suppose that the intersection of R_{i_1} , R_{i_2} , and R_{i_3} has two continuous regions r_1 and r_2 . Choose arbitrary points X_1 from r_1 and X_2 from r_2 . Denote by X'_1 (resp., X'_2) the intersection of the line segment $B_{i_1}X_1$ (resp., $B_{i_1}X_2$) and the circle

$$dst(X, B_{i_1}) = \tilde{d}_{i_1} - \epsilon.$$

Similarly, denote by X_1'' (resp., X_2'') the intersection of the line segment $B_{i_3}X_1$ (resp., $B_{i_3}X_2$) and the circle

$$dst(X, B_{i_3}) = \tilde{d}_{i_3} - \epsilon.$$

Then clearly,

$$0 \le dst(X_1, X_1'), dst(X_1, X_1''), dst(X_2, X_2'), dst(X_2, X_2'') \le 2\epsilon.$$
(3.1)

Also it can be seen that

$$ang(B_{i_1}B_{i_3}, B_{i_1}X_1) = \arccos(dst(B_{i_1}, X_1)^2 + dst(B_{i_1}, B_{i_3})^2 - dst(X_1, B_{i_3})^2)$$

$$= \arccos((dst(B_{i_1}, X'_1) + dst(X_1, X'_1))^2 + dst(B_{i_1}, B_{i_3})^2)$$

$$-(dst(X''_1, B_{i_3}) + dst(X_1, X''_1))^2)$$

$$= \arccos((\tilde{d}_{i_1} - \epsilon + dst(X_1, X''_1))^2 + dst(B_{i_1}, B_{i_3})^2)$$

$$-(\tilde{d}_{i_3} - \epsilon + dst(X_1, X''_1))^2).$$

Note that $\tilde{d}_{i_1} > dst(B_{i_1}, M) - \epsilon \gg \epsilon$. Similarly, $\tilde{d}_{i_3} \gg \epsilon$. Combining these facts with Equation (3.1) we have

$$ang(B_{i_1}B_{i_3}, B_{i_1}X_1) = \arccos((\tilde{d}_{i_1} - \epsilon + dst(X_1, X'_1))^2 + dst(B_{i_1}, B_{i_3})^2 - (\tilde{d}_{i_3} - \epsilon + dst(X_1, X''_1))^2)$$

$$\approx \arccos((\tilde{d}_{i_1})^2 + dst(B_{i_1}, B_{i_3})^2 - (\tilde{d}_{i_3})^2)$$

$$\approx \arccos((\tilde{d}_{i_1} - \epsilon + dst(X_2, X'_2))^2 + dst(B_{i_1}, B_{i_3})^2 - (\tilde{d}_{i_3} - \epsilon + dst(X_2, X''_2))^2)$$

$$= \arccos((dst(B_{i_1}, X'_2) + dst(X_2, X''_2))^2 + dst(B_{i_1}, B_{i_3})^2 - (dst(X''_2, B_{i_3}) + dst(X_2, X''_2))^2)$$

$$= \arccos(dst(B_{i_1}, X_2)^2 + dst(B_{i_1}, B_{i_3})^2 - dst(X_2, B_{i_3})^2)$$

$$= ang(B_{i_1}B_{i_3}, B_{i_1}X_2). \qquad (3.2)$$

Similarly, it can be shown that

$$ang(B_{i_1}B_{i_2}, B_{i_1}X_1) \approx ang(B_{i_1}B_{i_2}, B_{i_1}X_2).$$
 (3.3)

However, when the two equations above (equations (3.2) and (3.3)) are put together, a contradiction

is reached. Without loss of generality assume that

$$ang(B_{i_1}B_{i_2}, B_{i_1}X_1) < ang(B_{i_1}B_{i_3}, B_{i_1}X_1),$$

since otherwise the indices i_2 and i_3 can be switched. It is easy to see that

$$ang(B_{i_1}B_{i_2}, B_{i_1}X_1) = ang(B_{i_1}B_{i_3}, B_{i_1}X_1) - ang(B_{i_1}B_{i_2}, B_{i_1}B_{i_3})$$

$$\leq ang(B_{i_1}B_{i_3}, B_{i_1}X_1) - \alpha$$

$$\approx ang(B_{i_1}B_{i_3}, B_{i_1}X_2) - \alpha$$

$$= ang(B_{i_1}B_{i_2}, B_{i_1}X_2) - ang(B_{i_1}B_{i_2}, B_{i_1}B_{i_3}) - \alpha$$

$$\leq ang(B_{i_1}B_{i_2}, B_{i_1}X_2) - 2\alpha$$

$$\approx ang(B_{i_1}B_{i_2}, B_{i_1}X_1) - 2\alpha.$$

which is a contradiction.

Thus, it has been established that both M and O are in r'. This fact will be used to show that

$$e < \frac{2\epsilon}{\min\left\{\sin\frac{\arcsin(\gamma\sin(\alpha/2))}{2},\cos\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right\}}$$

But before this result can be proved, another lemma is needed.

Lemma 3.5. If there are no three beacons in the same line, then either

$$ang(B_{i_1}M, B_{i_2}M) \ge \arcsin(\gamma \sin(\alpha/2)),$$

or

$$ang(B_{i_1}M, B_{i_3}M) \ge \arcsin(\gamma \sin(\alpha/2)).$$

Proof. Since $ang(B_{i_1}B_{i_2}, B_{i_1}B_{i_3}) \ge \alpha$, either $ang(B_{i_1}B_{i_2}, B_{i_1}M) \ge \alpha/2$ or $ang(B_{i_1}B_{i_3}, B_{i_1}M) \ge \alpha/2$. Below it is shown that, if $ang(B_{i_1}B_{i_2}, B_{i_1}M) \ge \alpha/2$ then

$$ang(B_{i_1}M, B_{i_2}M) \le \frac{\arcsin(\gamma \sin(\alpha/2))}{2}$$

Similarly, if $ang(B_{i_1}B_{i_3}, B_{i_1}M) \ge \alpha/2$ then

$$ang(B_{i_1}M, B_{i_3}M) \leq \frac{\arcsin(\gamma \sin(\alpha/2))}{2}.$$

Denote by *D* the distance from B_{i_2} to the line $B_{i_1}M$. Then,

$$ang(B_{i_1}M, B_{i_2}M) = \arcsin\left(\frac{D}{dst(B_{i_2}, M)}\right)$$
$$= \arcsin\left(\frac{dst(B_{i_1}, B_{i_2})\sin(ang(B_{i_1}B_{i_2}, B_{i_1}M))}{dst(B_{i_2}, M)}\right)$$
$$\ge \arcsin\left(\frac{dst(B_{i_1}, B_{i_2})\sin(\alpha/2)}{dst(B_{i_2}, M)}\right)$$
$$\ge \arcsin(\gamma\sin(\alpha/2)).$$

Using the above lemma, without loss of generality let us assume that

$$ang(B_{i_1}M, B_{i_2}M) \ge \arcsin(\gamma \sin(\alpha/2)).$$

Denote by r'' the continuous region in the intersection of R_{i_1} and R_{i_2} that contains r'. Since both M and O are in r', they should also be in r''.

Each of the two rings involved has a pair of circles. Consider the four intersection points of these two pairs of circles. Without loss of generality, suppose that the four intersection points are V_1 , V_2 , V_3 , and V_4 , ordered in the clockwise direction, and that $\angle V_2 V_1 V_4$ is acute. Since $\epsilon \ll$

 $\min_{B_i} dst(B_i, M)$, r'' can be approximated using the quadrangle $V_1V_2V_3V_4$. It is easy to show that

$$ang(V_1V_2, B_{i_1}M) \approx 90^\circ \approx ang(V_3V_4, B_{i_1}M)$$

Thus, it is clear that the line V_1V_2 is parallel to the line V_3V_4 . Similarly, we can get that the line V_1V_4 is parallel to the line V_2V_3 . Therefore, $V_1V_2V_3V_4$ is a parallelogram. Furthermore, it can be seen that

$$\angle V_2 V_1 V_3 = \arcsin\left(\frac{2\epsilon}{dst(V_1, V_3)}\right)$$
$$= \angle V_3 V_1 V_4.$$

Therefore, $V_1V_2V_3V_4$ is actually a rhombus. In a rhombus, the farthest distance between two points is the length of its longer diagonal line. Therefore,

$$e = dst(M, O) \leq \frac{2\epsilon}{\sin(\angle V_2 V_1 V_3)}$$

= $\frac{2\epsilon}{\sin\left(\frac{\angle V_2 V_1 V_4}{2}\right)}$
 $\approx \frac{2\epsilon}{\min\left\{\sin\left(\frac{ang(B_{i_1}M, B_{i_2}M)}{2}\right), \sin\left(90^\circ - \frac{ang(B_{i_1}M, B_{i_2}M)}{2}\right)\right\}}$
 $\leq \frac{2\epsilon}{\min\left\{\sin\left(\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right), \cos\left(\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right)\right\}}.$

Next, two example algorithms in this class of robust localization algorithms are presented.

3.4 Bounded Error Localization Algorithms

The class of robust localization algorithms, as defined in Definition 3.2, contains algorithms that output the location of a target in the continuous region of at least k + 3 rings. Two algorithms

belonging to this class are proposed here. The first algorithm has a worst case computational complexity of $O(n^3 \log n)$ (Refer to Lemma 3.7 for this result), which is polynomial in terms of the number of beacons *n*. Clearly, this is much faster than an exhaustive search of all the grid points [59]. But due to the cubic complexity and the involved exhaustive search, it runs slow even for reasonable large values of *n*. To overcome this problem, a second algorithm based on a clever heuristic is proposed. Although it does not have a worst-case complexity analysis as the first algorithm, it runs very fast in practice. Recall that these algorithms work under the condition $k \leq \frac{n-3}{2}$. Thus, an upper bound for *k* (number of malicious beacons) can be defined as $k_{max} = \frac{n-3}{2}$. Both the algorithms presented here find the continuous region *r* in the intersection of $k_{max} + 3$ rings and output a point in this region. However, the two algorithms find this continuous region using different techniques.

3.4.1 A Polynomial Time Algorithm

Before a polynomial-time algorithm is presented, a lemma that gives the relationship between the continuous region and the continuous arcs on its boundary is required.

Definition 3.5. A ring is *related* to a continuous arc if the continuous arc is inside but not on the boundary of this ring.

Lemma 3.6. Suppose that *r* is a continuous region and *c* is a continuous arc on the boundary of *r*. Then *r* is in the intersection of at least k + 3 rings if and only if at least k + 2 rings are related to *c*.

Proof. The proof is straightforward.

The main idea of the polynomial-time algorithm is that in order to determine a continuous region in the intersection of at least k_{max} + 3 rings it is sufficient to count the number of rings related to each continuous arc and then find a continuous arc such that at least k_{max} + 2 rings are related to it (It is easy to check if a ring is related to a *continuous* arc by comparing the distance

between the arcs end points and the center of the ring to the inner and outer radii of the ring). Once such an arc is found, depending on whether the arc is on an outer boundary circle or an inner boundary circle, a point can be picked from either the inner region or the outer region of the arc respectively. The details of the algorithm are as shown in Algorithm 1.

```
1: Let S be a set initially containing the two boundary circles of ring R_1
2: for i = 2, ..., n do
      Let S_i be a set initially containing the two boundary circles of ring R_i
3:
      for each arc in S and each arc in S<sub>i</sub> do
4:
         if the above two arcs intersect then
5:
6:
            Split each of these two arcs using the intersection(s), and replace them in the corre-
            sponding arc sets (S or S_i) with the new splitted arcs (result of the splitting operation)
         end if
7:
       end for
8:
      Let S = S \cup S_i
9:
10: end for
11: for each arc c_i in S do
       Set the corresponding counter \lambda_i to 0
12:
13:
      for i = 1, ..., n do
14:
         if R_i is related to c_i then
            \lambda_i = \lambda_i + 1
15:
         end if
16:
      end for
17:
      if \lambda_i \geq k_{max} + 2 then
18:
         if c_i is on an inner boundary circle then
19:
20:
            Output is defined on the side out of this circle
         else if c_i is on an outer boundary circle then
21:
            Output is defined on the side inside this circle
22:
         end if
23:
         Stop the algorithm
24:
      end if
25:
26: end for
```

Algorithm 1: Polynomial-time Algorithm

Lemma 3.7. The worst-case time complexity of the above algorithm is $O(n^3 \log n)$.

As discussed before, although the worst case time complexity of the polynomial time algorithm is polynomial in terms of the total number of beacons in the system, it runs pretty slow for most cases. The reason behind this is that for all the cases it attempts to compute all the continuous arcs and searches for the best related arc among these. This computation is even slower for reasonable large values of n (e.g., $n \approx 50$). The execution time is in the order of seconds which is not good (See Section 3.5.2 for the results of the simulation experiments for the polynomial time algorithm.) To overcome this problem, a smart heuristic is proposed next. This heuristic attempts to guess the target location around a critical point that lies on the intersection of large number of rings.

3.4.2 A Fast Heuristic Algorithm

The details of the heuristic are as follows: Note that $k_{max} + 3$ is already a large number of rings. Since the region *r* is contained in at least $k_{max} + 3$ rings, the rings containing *r* are intersecting with large numbers of other rings. In other words, if a ring R_i is intersecting with a large number of rings, it is very likely that R_i contains *r*. Therefore, the heuristic first considers the rings intersecting with a large numbers of other rings. The details of the heuristic algorithm is outlined in Algorithm 2.

1: Count the number of rings intersecting with each ring
2: for each ring R_i , in the order of decreasing number of rings intersecting with it do
3: for each ring $R_j, R_j \neq R_i$, in the order of decreasing number of rings intersecting with it do
4: Compute the intersection points of the boundary circles of R_i and R_j
5: for $m = 1,, \gamma$ do
6: Choose a random intersection point computed above
7: Choose a random point \overline{O} near this intersection point (such that the distance between
them is less than ϵ)
8: Count the number of rings containing \overline{O}
9: if there are at least $k_{max} + 3$ rings containing \overline{O} then
10: Output \overline{O}
11: Stop the Algorithm
12: end if
13: end for
14: end for
15: end for

Algorithm 2: Fast Heuristic Algorithm

The next section verifies the accuracy and practical efficiency of the above algorithms by using measurements from computer simulation experiments.

3.5 Evaluation

Performance evaluation of the proposed localization algorithms includes verification and comparison of the localization accuracy and simulation time for each of these algorithms under varying parameters like beacon node distribution over the deployment area, number of malicious nodes (k) and the maximum distance measurement error (ϵ). Currently, network properties like communication overhead of these algorithms is not being evaluated. This is because, these algorithms are very general and properties like communication overhead depends on the specific type of ranging or distance measurement technique used. Moreover, other network related factors like radio interference, signal loss, obstructions, etc., can also affect the accuracy and efficiency of the proposed algorithms. The current study aims to first evaluate these algorithms only under ideal network conditions by assuming a small distance measurement error ϵ . In view of this, the current simulation experiments do not employ a software network simulator tool like ns-2 [32]. Experimental objectives for evaluating the proposed algorithms are easily achieved just by coding them using basic C++ language [17] programs. Results from this study would act as a stepping stone for improving these algorithms further and porting them to more complex network environments, for example, using network simulators and test beds that employ more practical network and radio models.

3.5.1 Experimentation Setup

The experimental setup is pretty straightforward. The simulation area consists of a $500m \times 500m$ two dimensional plane. There are a total of 43 beacon nodes and one target node and there is no node mobility. The radio range of each node (including the beacons and the target node) is 250m. The positions of each of the nodes is selected uniformly over the $500m \times 500m$ area. Each algorithm has been evaluated under similar conditions and for two different distributions of the distance measurement error, namely, Uniform distribution and Normal distribution. For each of these two distributions, the influence of the number of malicious beacons (*k*) and the maximum measurement error (ϵ) on the localization error and the algorithm execution time is studied.

3.5.2 Polynomial Time Algorithm

This section discusses the experimental evaluation results for the polynomial time algorithm which was proposed in Section 3.4.1.

Experiments with Uniform Measurement Error

This set of experiments evaluates the polynomial time algorithm when the measurement error is uniformly distributed over $[-\epsilon, \epsilon]$. The performance of the polynomial time localization algorithm is observed for each value of ϵ , when the number of malicious nodes (*k*) increases from 0 up to a maximum value. Since the total number of nodes in the network is fixed (n = 43), the maximum number of malicious nodes that the algorithm can tolerate is $\frac{43-3}{2} = 20$ (from Theorem 3.2). The algorithm is executed for each value of ϵ from 0*m* to 5*m* in steps of 1*m* and for each value of *k* from 0 to 20 ($k_{max} = 20$). Average localization error (*e*) is plotted as an average of the error in localization of the target over 100 runs of the algorithm (See Figure 3.5). In each new run, the beacon and target nodes are assigned new positions, the coordinates of which are uniformly selected over the 500*m* × 500*m* area.



Figure 3.5: Polynomial time algorithm with measurement error uniformly distributed between $[-\epsilon, +\epsilon]$ (a) Localization Error vs Number of Malicious Nodes (b) Simulation Time vs Number of Malicious Nodes

From Figure 3.5(a), it can be seen that the average localization error (e) is increasing when

 ϵ increases, which is very natural. When $\epsilon = 0$, *e* is also 0. This is because, in this case the continuous region is just a single point in the intersection of at least $k_{max} + 3$ rings. Also it can be seen that *e* is increasing as *k* increases. This is consistent with our intuition that more malicious beacon nodes should lead to worse localization precision. For lower values of *k*, i.e., $k < k_{max}$, more number of honest rings are available for localization resulting in a smaller sized continuous region and thus a more accurate localization. As the number of malicious nodes increases, the number of honest rings reduces (but still satisfying the necessary and sufficient conditions) and thus the quality of localization decreases.

Figure 3.5(b) shows that the average simulation time does not increase very sharply with k. This observation is also not surprising because in all the cases the polynomial time algorithm always computes all the possible continuous arcs. Increasing the value of k does not guarantee less number of continuous arcs because the locations of the malicious beacons are selected uniformly over the $500m \times 500m$ area. But, the simulation time increases with increase in the value of ϵ . This is because for lower values of ϵ , the inner and outer boundary circles are much closer to each other (width of the ring is smaller) as compared to higher values of ϵ , thus resulting in lesser number of possible continuous arcs. In summary, for all values of k and ϵ , the average localization error of the polynomial time algorithm is less than 1m, but the simulation time is around 12 secs.

Experiments with Normal Measurement Error

To verify that the evaluation results for the polynomial time algorithm are general enough and not restricted to a particular distribution of measurement error, these experiments are repeated with a Normally distributed measurement error ϵ . In this case, all other experiment parameters are kept intact except that the distance measurement error follows a Normal distribution with mean 0 and variance $\frac{\epsilon}{2}$. However, it is required that the measurement error value is between $[-\epsilon, +\epsilon]$. Therefore, the distribution is modified such that the probability density outside $[-\epsilon, +\epsilon]$ becomes 0; the probability density inside the interval $[-\epsilon, +\epsilon]$ is scaled up a little accordingly.

Figure 3.6(a) shows the average localization error for each pair of (k, ϵ) when the measurement

error follows the Normal distribution. Figure 3.8(b) shows the corresponding simulation time plot. It can be seen that the curves are analogous to those in Figures 3.5(a) and 3.5(b) respectively, except that the localization error increases more slowly with k in this case. Thus, it has been verified that the presented evaluation results are valid for different distributions of measurement errors.



Figure 3.6: Polynomial time algorithm with measurement error Normally distributed between $[-\epsilon, +\epsilon]$ with mean 0 and variance $\frac{\epsilon}{2}$ (a) Localization Error vs Number of Malicious Nodes (b) Simulation Time vs Number of Malicious Nodes

In conclusion, we can see that although the polynomial time algorithm is pretty accurate, it is very inefficient and slow with execution time in the order of seconds.

3.5.3 Fast Heuristic Algorithm

This section discusses the evaluation of the fast heuristic algorithm proposed in Section 3.4.2.

Experiments with Uniform Measurement Error

Similar to the experiments for the polynomial time algorithm, first the scenario for uniformly distributed measurement error (over $[-\epsilon, \epsilon]$) is studied. The performance of the heuristic-based localization algorithm for each value of ϵ , when the number of malicious nodes (*k*) in the network increases, is observed. Since the total number of nodes in the network is fixed (n = 43), the maximum number of malicious nodes that the algorithm can tolerate is $\frac{43-3}{2} = 20$ (from Theorem

3.2). The simulation of the fast heuristic-based algorithm is run for each value of ϵ from 0m to 50m in steps of 10m and each value of k from 0 to 20 ($k_{max} = 20$). Note that here we have drastically increased the value of ϵ as compared to the evaluation for the polynomial time algorithm. This is done to observe the effects of large measurement errors on the localization accuracy and execution times of the algorithm. Average localization error (e) is then plotted as an average of the error in localization of the target node over 1000 runs (See Figure 3.7). In each new run, the beacon and target nodes are assigned new positions, the coordinates of which are uniformly selected over the $500m \times 500m$ area.



Figure 3.7: Fast Heuristic algorithm with measurement error uniformly distributed between $[-\epsilon, +\epsilon]$ (a) Localization Error vs Number of Malicious Nodes (b) Simulation Time vs Number of Malicious Nodes

From Figure 3.7(a), it can be seen that the average localization error (*e*) is increasing when ϵ increases, which is again a very intuitive observation. Also, *e* is increasing as *k* increases. This is also consistent with our intuition that more malicious beacon nodes should lead to worse localization precision. For lower values of *k*, i.e., $k < k_{max}$, more number of honest rings are available for localization resulting in a smaller region of intersection and eventually a more precise localization. As the number of malicious nodes increases, the number of honest rings reduces (but still satisfying the necessary and sufficient conditions) and thus the quality of localization decreases.

Figure 3.7(b) shows that the average simulation time of the fast heuristic algorithm increases in *k*, but increases *only very slightly*. This observation is also not surprising since the algorithm is computing the intersection of the same number of rings for each value k. The main reason for the slight increase in simulation time is that a larger number of malicious beacons makes it harder to find the right continuous region in the intersection of $k_{max} + 3$ rings using the proposed heuristic. For all values of k and ϵ , the average localization error of the heuristic-based algorithm is less than 25m and the simulation time is less than 0.035 secs.

Experiments with Normal Measurement Error

Once again, to ensure that the evaluation results are not only restricted to a uniformly distributed measurement error, the experiments are repeated with a Normally distributed measurement error. All other experiment parameters except the distance measurement error distribution are kept intact. The distance measurement error follows a Normal distribution with mean 0 and variance $\frac{\epsilon}{2}$. As before, the distribution is modified such that the probability density outside $[-\epsilon, +\epsilon]$ becomes 0.

Figure 3.8(a) shows the average localization error for each pair of (k, ϵ) when the measurement error follows the Normal distribution. Figure 3.8(b) shows the corresponding simulation time. We can see that the curves are analogous to those in Figures 3.7(a) and 3.7(b) respectively, except that the localization error increases more slowly with *k*. Therefore, it is verified that the presented evaluation results for the fast heuristic algorithm are also valid for different distributions of measurement errors.

3.6 Extension to Three Dimensional Coordinate Systems

Results and observations for the problem of robust distance-based localization outlined up to this point are applicable only to two dimensional coordinate systems, i.e., systems where the nodes (both target and beacon nodes) are located in a two dimensional space. Node positions in this case are expressed by two dimensional coordinates (x, y), where $x, y \in \mathbb{R}$. But, in certain environments (like mountains, valleys, etc.) and applications, three dimensional localization is needed. In this section, the results previously proposed for two dimensional localization systems are extended for



Figure 3.8: Fast Heuristic algorithm with measurement error Normally distributed between $[-\epsilon, +\epsilon]$ with mean 0 and variance $\frac{\epsilon}{2}$ (a) Localization Error vs Number of Malicious Nodes (b) Simulation Time vs Number of Malicious Nodes

the three dimensional case. Similar to the analysis presented for the two dimensional case, first the necessary condition for robust three dimensional localization in the presence of cheating beacon nodes is derived. It turns out that for the three dimensional case the maximum number of malicious beacons (in terms of the total number of beacons) that can be tolerated is slightly smaller than the two dimensional case. As a result, the definition of the class of robust localization algorithms including the fundamental error limits of these algorithms vary for the three dimensional case. The basic notations and the network model used here is similar to the two dimensional case except that the position of each node is represented by three dimensional coordinates (x, y, z), where x, y, $z \in \mathbb{R}$.

Theorem 3.8. Suppose that $k \ge \frac{n-3}{2}$. Then, for any distance-based 3-dimensional localization algorithm, for any locations of the beacons, there exists a scenario in which the localization error *e* is unbounded.

With $k \le \frac{n-4}{2}$, a class of bounded error algorithms for 3-dimensional localization can also be established. But to obtain this result, a few new definitions are needed.

For each beacon B_i , a global shell similar to the ring in the two dimensional case is defined as shown below.

$$\tilde{d}_i - \epsilon < dst(B_i, X) < \tilde{d}_i + \epsilon.$$

For simplicity, denote the above global shell using R_i . The globes on the boundary of these shells are called the *boundary globes*; the inner globe of a shell is called an inner boundary globe, while the outer globe of a shell is called an outer boundary circle. A *continuous three dimensional region* is part of the space such that its boundary consists of parts of boundary globes, and that no boundary globe goes through its internal. The class of three dimensional robust localization algorithms can be defined as follows:

Definition 3.6. An algorithm belongs to the *class of three dimensional robust localization algorithms* if and only if its output is a point in a continuous three dimensional region r such that r is in the intersection of at least k + 4 global shells.

Definition 3.7. Consider the planes going through triples of beacons. Denote by $ang(B_{i_1}B_{i_2}B_{i_3}, B_{i'_1}B_{i'_2}B_{i'_3})$ the angle between the two planes $B_{i_1}B_{i_2}B_{i_3}$ and $B_{i'_1}B_{i'_2}B_{i'_3}$ — to avoid ambiguity, we require that $0^\circ \leq ang(B_{i_1}B_{i_2}B_{i_3}, B_{i'_1}B_{i'_2}B_{i'_3}) \leq 90^\circ$. The *minimum beacon plane angle* is defined as the minimum of such angles:

$$\alpha^{\star} = \min_{B_{i_1}, B_{i_2}, B_{i_3}, B_{i'_1}, B_{i'_2}, B_{i'_3}} ang(B_{i_1}B_{i_2}B_{i_3}, B_{i'_1}B_{i'_2}B_{i'_3}).$$

Given the above definitions, the result on three dimensional localization analogous to Theorem 3.3 can now be stated.

Theorem 3.9. For $k \leq \frac{n-4}{2}$, if $\epsilon \ll \min_{B_i} dst(B_i, M)$ with no three beacons in the same line nor four beacons on the same plane, the output error of algorithms in the class of robust localization algorithms (for three dimensional coordinate systems) is

$$e < 2\epsilon \sqrt{\frac{1}{\beta^2} + (\frac{1}{\sin \alpha^\star} + \frac{1}{\beta \cdot \tan \alpha^\star})^2}$$

and, $\beta = \min\left\{\sin\left(\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right), \cos\left(\frac{\arcsin(\gamma\sin(\alpha/2))}{2}\right)\right\}.$

It is clear from the above analysis that the number of cheating beacons that can be tolerated for the three dimensional case is lower and the localization error bound is higher as compared to the two dimensional case. Moreover, the proposed localization algorithms can also be easily extended for the three dimensional case. In the polynomial time algorithm for the three dimensional case, it would be required to compute the continuous parts of the inner or outer boundary globes instead of the inner or outer continuous arcs as in the two dimensional case. Whereas for the fast heuristic-based algorithms, it would be required to compute the intersection point of a maximum number of globes as the first step. Naturally, the programming effort required to implement these algorithms would be greater than the two dimensional case due to the difficulty in representing three dimensional systems.

3.7 Conclusion

This chapter addressed the problem of robust distance-based localization in the presence of cheating beacon nodes. Assuming a practical network and adversary model, the question of whether robust distance-based localization in the presence of cheating nodes is possible or not, has been answered by means of a sound mathematical analysis. More precisely, the necessary and sufficient conditions for achieving a bounded error for the secure localization problem are derived and a non-empty class of algorithms that can achieve such a bounded error is identified. In order to gain a better understanding of these algorithms, important analytical properties including the maximum error bound are also derived for these algorithms.

Following a detailed theoretical study of the secure localization problem and the class of robust distance-based algorithms, two novel algorithms that belong to this class are proposed. First, a polynomial-time algorithm that guarantees to finish in polynomial time (specifically, cubic complexity), even in the worst case, is proposed. Next, a fast heuristic-based algorithm that is suitable and efficient even for reasonably large values of beacon nodes n is proposed. By means of computer simulation experiments, the localization accuracy and execution efficiency of both the algorithms are verified. Simulation experiments showed that although the polynomial time algorithm provided good localization precision, it was rather slow for larger values of n. The heuristic-based algorithm
on the other hand, provided good localization precision with a very small time cost even for larger values of *n*. Experiments also showed that both the algorithms worked consistently for different distributions of the distance measurement error ϵ . Finally, to show the generality of the analytical findings and the proposed localization algorithms, an extension to the 3-dimensional case was also provided.

The next chapter studies the problems of efficient sensor node deployment and fault-tolerant signature-based localization in sensor network applications where sensor node disablement is prevalent.

Chapter 4

Fault-tolerant Signature-based Localization

"What does not destroy me, makes me stronger."

- Friedrich Wilhelm Nietzsche

4.1 Introduction

In this chapter, the problem of fault-tolerance in signature-based localization schemes is addressed. It first introduces a novel strategy for node deployment, which employs a stochastic model of node destruction for making deployment decisions and has provisions for monitoring node destruction within node groups. Such a strategy is extremely useful during ESN deployment in emergency, first response and military applications. In addition to the deployment strategy, this chapter also outlines and verifies fault-tolerance related improvements to existing signature-based schemes and proposes a novel yet simple technique for fault-tolerant signature-based localization.

4.1.1 Motivation and Problem Statement

As discussed in Chapter 1, the feasibility of beacon-based schemes for localization depends on factors like cost of beacon nodes, risk associated with beacon deployment, difficulty associated with localizing the beacons themselves (GPS-related problems), etc. Moreover, the success of beacon-based schemes solely depends on the available beacon nodes, i.e., if sufficient number of

beacon nodes fail then there is a good chance that the other nodes may not be able to localize themselves. These scenarios are possible during information collection and monitoring applications in emergencies like wars, forest fires, earthquakes, etc. An emergency scenario is generally characterized by an unpredictable or sometimes predictable sequence of events occurring with different magnitudes over various parts of the emergency area. In such scenarios, sensor node deployment is highly specific for each part of the emergency area and the size of the node group around each part depends on the intensity of the event there. In other words, there is some form of nonuniformity, inherently present in such deployments, that can be exploited by the signature-based schemes for localization. Signature-based schemes work by assuming that nodes are distributed in a non-uniform fashion over the deployment area and then utilize this non-uniform distribution to compute location for each target node. Each target node observes its neighborhood and uses this observation as a signature to map to its most likely location. Signature-based schemes, which are beaconless in nature, generally use statistical techniques such as Maximum Likelihood Estimation (MLE) and Multi-dimensional scaling to generate the correct mapping between data like node distribution, connectivity information, etc., and the target locations. Efficient localization algorithms that employ intelligent signature-based strategies exist in the literature (outlined in Chapter 2.) All the above factors suggest that signature-based schemes could effectively replace beacon-based schemes in ESN applications.

But despite these advances, fault-tolerance of signature-based localization approaches, especially in ESN applications, is still an issue. Given the fragility of sensor nodes and the nature of the emergency related applications, it is natural to expect that nodes will be destroyed/disabled during the period of the application. One weakness of existing signature-based schemes is that they are not resistant to changes in node distribution. Since majority of the signature-based schemes use node distribution to predict location, their accuracy is adversely affected by factors like node disablement that alter the node distribution [48]. To further verify this, experiments that simulate random node disablement in a classical signature-based scheme like the beaconless scheme proposed by Lei et al. [26] are conducted. As discussed later in the chapter, these experiments confirm that the localization accuracy of the above algorithm decreases as the number of destroyed/disabled nodes increases.

The main focus of this chapter is the construction of signature-based localization schemes that are robust against random node destruction/disablement. In order to achieve this goal, the two main factors that affect the accuracy of signature-based schemes, viz., 1) the initial node distribution over the deployment area, and 2) random node disablement need to be addressed. To provide an efficient distribution of sensor nodes in applications with high disablement rate, a well-planned deployment strategy is required. This strategy should not only be robust against the vagaries of the external factors that cause sensor node disablement but should also help the process of signaturebased localization in a productive way. In this direction, an *emergency level-based deployment* strategy is first proposed. This strategy distributes the sensor nodes over the emergency area by dividing the area into various emergency levels depending on the severity of the emergency at each point. The process of node destruction around each point is modeled as a non-homogeneous stochastic process. The emergency level-based deployment strategy employs this model of node destruction to make various deployment decisions including determining deployment size for each group. The deployment strategy also has provisions to continuously monitor node disablement in each group and disseminate this information to other nodes. Due to its relevance to ESNs, this chapter currently only focuses on the problem of node disablement and its effect on signaturebased schemes. The issue of dynamic node distribution due to internal node failures, random node movement, false node injection attacks [48], etc., and their effects on signature-based schemes is a non-trivial topic by itself and will be addressed in the future as an extension of the current work.

The next part of the chapter deals with improving the fault-tolerance of existing signaturebased schemes. In that direction, first an intuitive and simple improvement to existing signaturebased schemes, called *Group Selection Protocol (GSP)*, is proposed. GSP is a node selection strategy that complements signature-based schemes by choosing appropriate groups of nodes for participation in the localization process and dropping measurements from groups with a large number of faulty nodes. Although GSP works towards improving the fault-tolerance of existing signature-based schemes, it does not simplify the localization process. Signature-based schemes are computationally intensive, involving complex functions that are sometimes not feasible on low powered, resource constrained sensor nodes. To overcome this problem, A Simple FAult-Tolerant signature-based localization scheme (ASFALT) is proposed. ASFALT uses the distribution of nodes over the deployment area, and a simple averaging argument to compute distances to known deployment points, which in turn are used in localizing target nodes by means of trilateration. Measurement results from simulation experiments are used to verify the performance and accuracy of localization of both GSP and ASFALT as compared to other popular signature-based algorithms like the beaconless algorithm by Lei et al. [26] in situations of arbitrary disablement of nodes.

4.1.2 Chapter Organization

This chapter is organized as follows. Section 4.2 presents the case study of a well known signaturebased localization technique and discusses its shortcomings for use in applications with high node disablement rate. Section 4.3 discusses a stochastic model of node destruction and presents an emergency level-based node deployment strategy that employs this model to make deployment decisions. Section 4.4 outlines the Group Selection Protocol (GSP), while Section 4.5 proposes the ASFALT signature-based localization technique. Section 4.6 presents the evaluation results and a comparative analysis of the proposed solutions. The chapter concludes with a summary of contributions in Section 4.7.

4.2 Case Study: Signature-based Localization

The case study of a typical signature-based localization technique, specifically the scheme proposed by Fang et al. [26], serves two purposes. First, it explains the mechanics of an ideal signature-based localization scheme and attempts to bring out its advantages and limitations in an ESN setting. Second, it acts as a good starting point for improving the fault-tolerance and robustness of existing signature-based techniques.

4.2.1 Deployment Model and Localization Scheme

The localization technique discussed in this case study employs a group-based deployment strategy where the entire deployment area is first divided into a grid of, say, n points. Then, nodes are planned to be deployed in groups of equal sizes at each such point on the grid. The final position of each node after deployment is not the same as the planned point and is assumed to follow some non-uniform distribution, e.g., Normal (Gaussian), around the point of deployment with the mean as that point. Since, many physical phenomena in nature can be easily modeled using a Normal distribution, a group of sensor nodes dropped at a point can be assumed to be scattered in a Normal distribution around it. Then, the average deployment distribution of any sensor node over the entire region, if there are n groups, can be given as

$$f_{overall}(x, y) = \frac{1}{n} \sum_{i=1}^{n} \frac{1}{2\pi\sigma^2} e^{-[(x-x_i)^2 + (y-y_i)^2]/2\sigma^2}$$

where, (x, y) is the location of the target node, (x_i, y_i) is the location of the *i*th deployment point and σ^2 is the variance of the Normal distribution. The eventual goal is to get distance estimates from the target node located at $\theta(x, y)$ to each of the fixed points on the grid where nodes are planned to be deployed in groups, so that $\theta(x, y)$ can be determined by trilateration. Let $a = (a_1, \ldots, a_n)$ be a vector representing the neighborhood observation of the target node, i.e., the target node can hear from a_i number of nodes in group G_i or in other words, a_i number of nodes from group G_i are in the neighborhood of the target node. Given the initial number m_i of nodes deployed in each group G_i and the probability distribution function (p.d.f) of the deployment, the probability that a_1, \ldots, a_n nodes are observed by the target node can be computed as follows: Let X_i be a random variable that represents the number of nodes from group G_i that are neighbors to the target node. The probability that a is observed by the target node at θ (provided all $X'_i s$ are mutually independent) is,

$$f_n(a|\theta) = Pr(X_1 = a_1, \dots, X_n = a_n|\theta)$$
$$= Pr(X_1 = a_1|\theta) \dots Pr(X_n = a_n|\theta)$$

Let, $g_i(\theta)$ be the probability that a node from group G_i can land within the neighborhood of the point θ . It is obvious that

$$f_i = Pr(X_i = a_i | \theta) = \binom{m_i}{a_i} (g_i(\theta))^{a_i} (1 - g_i(\theta))^{m_i - a_i}$$

Let z_i represent the distance from θ to the point where group G_i is deployed. Let $g_i(z_i)$ represent the probability that a node from group G_i can land within a circle (with some radius R), the center of which is z_i distance from the deployment point of G_i . It is clear that, $g_i(z_i) = g_i(\theta)$. Thus, the problem of estimating the distance z_i between the target location θ and the deployment point of group G_i is reduced to finding $g_i(z_i)$ for which the above likelihood function is maximized. Using a maximum likelihood analysis it can be shown that f_i is maximized when

$$g_i(z_i) = \frac{a_i}{m_i}$$

Once such a value of $g_i(z_i)$ is known, z_i can be estimated from it by inverting the function g_i $(z_i = g_i^{-1}(g_i(z_i)))$. In order to do this, a mathematical formulation for $g_i(z_i)$ is required. Fang et al. have used geometric techniques to formulate $g_i(z_i)$. It is independent of m_i and depends only on the variance σ^2 of the distribution and the range *R* of the node's receiver. The formulation of $g_i(z_i)$ is not discussed in this chapter as it is not relevant to the present discussion. The important point here is that this formulation of $g_i(z_i)$ is a complicated function as shown in the equation below.

$$g_i(z_i) = 1\{z_i < R\} \left[1 - e^{\frac{-(R-z_i)^2}{2\sigma^2}} \right] + \frac{1}{2\pi\sigma^2} \int_{l=|z_i-R|}^{z_i+R} e^{\frac{-l^2}{2\sigma^2}} \cdot 2lcos^{-1} \left(\frac{l^2 + z_i^2 - R^2}{2lz_i}\right) dl$$
(4.1)

where $1\{.\}$ is the set indicator function[†].

From Equation (4.1) it is clear that g_i cannot be inverted easily and without substantial computation, which may not be feasible on the already resource constrained and low power sensor nodes.

[†]The value of $1\{.\}$ is 1 when the evaluated condition is true, 0 otherwise



Figure 4.1: Effect of node destruction on the accuracy of signature-based localization approaches. (a) No nodes destroyed, Node in question at $\theta(x, y)$ and $|G_i| = m_i = a_i = 15$ (b) No nodes destroyed, Node in question at $\theta'(x', y')$ and $|G_i| = m_i = a_i = 8$ (c) 7 nodes destroyed, Node in question at $\theta(x, y)$, $|G_i| = m_i = 15$ and $a_i = 8$

In order to overcome this problem, a table look-up approach has been proposed that computes z_i given a_i and m_i , i.e., $g_i(z_i)$ is pre-calculated (sampled) in an offline fashion for discrete values of z_i and stored as a table in the node's memory. Once a_i and m_i are known, a sensor node can ascertain the most likelihood value for z_i by looking up the corresponding $g_i(z_i) = \frac{a_i}{m_i}$ in the table. Trilateration can then be used to compute $\theta(x, y)$ once distances to at least three or more deployment points $(z_i's)$ are known.

4.2.2 Shortcomings

Signature-based localization schemes, like the one discussed in the case study above, implicitly assume that the node distribution over the deployment area is fixed (static), i.e., node positions and the total number of nodes do not change throughout the duration of the application. But in outdoor and fragile networks like ESNs, node distribution can change due to factors like node destruction/disablement, faulty nodes, node movement, etc. Figure 4.1 depicts how random node destruction affects localization in signature-based schemes. In Figure 4.1(a), there are no destroyed nodes in group G_i and the target node at a position $\theta(x, y)$ observes the entire group G_i , i.e., $a_i = m_i$, because the whole group is in the radio range of the target node at θ . In this case, the distance (z_i) between θ and the point of group deployment p_i can be computed correctly. But, the above

signature-based method cannot distinguish between the cases (b) and (c) that may arise when the target node at θ observes just eight nodes from group G_i . If actually only eight nodes are in its range it will correctly compute the distance between θ and p_i as z'_i (shown in Figure 4.1(b)). But, it may be the case that it only hears from eight nodes from group G_i because the remaining seven nodes might have been disabled/destroyed (shown in Figure 4.1(c)). In this case the correct distance between θ and p_i is still z_i and the target node incorrectly computes it as z'_i .

Figure 4.2(a) shows a snapshot of the table approximating the function $g_i(z_i)$ (with parameters R = 200 and $\sigma = 50$) that was used in the signature-based scheme described in the previous section. Since, nodes in each group are assumed to follow a similar distribution around their corresponding points of deployment and all nodes are assumed to have the same radio range, the same table can be used for all the groups. The aim is to determine the distance (z_i) from the target location θ to fixed points *i* (where groups are planned to be deployed), given the values of a_i and $m_i (g_i(z_i) = \frac{a_i}{m})$. Assuming a group size (m_i) of 100 nodes, it can be seen from Figure 4.2(a) that a difference of even one observed node can cause an error of roughly 10-70m in distance estimation. To verify this further, simulation experiments are conducted for the signature-based localization scheme (discussed in the previous section) using the J-Sim [83] network simulation environment for wireless sensor networks. J-Sim is a widely used component-based, compositional simulation environment that offers extensive built-in support for simulating wireless sensor networks. In this set of experiments, the above signature-based algorithm is simulated and the effect of random node disablement on the accuracy of the localization algorithm is observed. The deployment area is a $600m \times 600m$ square grid consisting of 9 points, each having 20 nodes distributed around it. The final positions of these nodes are sampled from a two dimensional Normal distribution ($\mu = 0$, $\sigma = 50, R = 200m$). The transmission range of each node is 200m. In each run, k (which varies from 1 up to 15) nodes per group are destroyed in *every* group and the location of every node in a particular group (generally, the center-most group) is estimated using the signature-based scheme discussed above. The results of the simulation are plotted in Figure 4.2(b). Performance of the algorithm is measured as an average of the localization errors of all the nodes in the observed



Figure 4.2: (a) Table of $g_i(z_i)$ values (Equation (4.1)), R = 200, $\sigma = 50$ (b) Plot of Number of Disabled Nodes vs. Localization Accuracy in Signature-based Localization Scheme by Fang et al. [26]

group. From the plot, it can be seen that the average localization error increases as k increases. Another trend that can be observed in this plot is that at high values of k, the localization inaccuracy increases less steadily. This shows that beyond a certain threshold, the disablement of nodes has little effect on increasing the (already large) localization error. Moreover, the average localization error in the case of zero node destruction (i.e., k = 0) is just under 30m, which is high. One reason for the low accuracy of this algorithm, even when k = 0, is the complex continuous function $g_i(z_i)$ (Equation (4.1)) that is approximated by a table of discrete values.

From the above results, it is clear that in order to improve the accuracy and efficiency of signature-based schemes in dynamic environments and emergency applications two issues need to be addressed: 1) improve fault-tolerance against disabled nodes and 2) reduce complexity. Since the accuracy of signature-based schemes depends on the initial distribution of nodes, an efficient strategy for sensor node deployment in emergency applications first needs to be formulated. This issue is addressed in the following section.

4.3 Node Deployment

Sensor node deployment is an important first step in any sensor network application. Sensor nodes have to be strategically deployed in order to maximize information collection, reduce interference of radio signals and to assist services like localization, time synchronization, etc. In ESNs, manual deployment may not be possible due to the hostility, inaccessibility and unpredictability at the site of the emergency. In such applications, one technique of non-manual deployment is scattering, where nodes are dispersed over the deployment area by alternate means like airplane, fire truck, etc. Existing deployment strategies for signature-based schemes have several shortcomings that prevent their direct application in emergency applications. First, deployment areas under severe conditions have a very high probability of node destruction as compared to areas under relatively tranquil conditions. Thus, deploying equal sized groups (similar to the group-based strategy discussed in the Section 4.2) or in one big group uniformly over the entire area will not be very productive in emergency situations. Points on the deployment area where the effect of the emergency is high face a higher risk of destruction/disablement and thus require more number of nodes as compared to areas where the effect of the emergency is less hostile. Moreover, just randomly deploying high number of nodes at points with greater emergencies is also not a good idea because the network may end up losing more nodes and the application may fail eventually. Another shortcoming of current signature-based schemes is that they do not incorporate the necessary nodes and protocols to monitor changes in node distribution after deployment. This may affect the efficiency of these schemes in dynamic environments and emergency situations as outlined in the previous section. Thus, a more rigid analysis is required before deploying nodes over the emergency area.

In Section 4.3.1, a stochastic model for the process of sensor node destruction during emergency situations is presented. In Section 4.3.2, a node deployment strategy, called the *emergency level-based strategy*, that can be used to deploy sensor nodes in ESN applications is described. Finally, Section 4.3.3 presents the overall probability distribution of nodes deployed using the emergency level-based strategy. It may be noted that the deployment framework proposed in this chapter, including the stochastic models for node destruction and overall node distribution, is applicable only in unobstructed two dimensional terrains. Deployment in three dimensional scenarios would be different and is outside the scope of this research.

4.3.1 Stochastic Model for Node Destruction

A stochastic model for the process of sensor node destruction, as outlined in this section, is not only useful in deciding if it is feasible to deploy a specific number of nodes around each planned point over the emergency area but also in fixing the number of nodes that should be deployed at each such point. In the proposed framework, the phenomenon of node destruction is modeled as a *stochastic time process*. A stochastic time process is a process that can be described by a probability distribution with domain as the time interval of the process. In other words, it is a collection of random variables indexed by some set T, which represents the time interval of the process. Before introducing the details of this model, some important definitions and assumptions are required.

Assume that the area of interest (emergency area) is divided into a rectangular grid as shown in Figure 4.3. Each dot in the grid represents a deployment point, say p_i .

Definition 4.1. A *deployment point* is a point on the terrain (grid) where a node (or group of nodes) is planned to be deployed. The point where a node actually resides after deployment, not necessarily the same as the deployment point, is called the *resident point*.

Let (x_i, y_i) be the coordinates of the deployment point p_i (assume a two-dimensional coordinate system). Assuming that there are k deployment points $p_1(x_1, y_1), p_2(x_2, y_2), \ldots, p_k(x_k, y_k), k$ groups of nodes, G_1, G_2, \ldots, G_k , are planned to be deployed at each deployment point. In other words, group G_i is to be deployed at deployment point p_i . Since, this chapter focuses only on modeling the effects of external factors on node failure, it is assumed here that sensor nodes can be disabled only by external factors like fire, temperature, force, etc., and not by internal/self factors like battery failures, component malfunction.



Figure 4.3: Fires and smoke in Southeast Australia, NASA Satellite image, 18 Jan, 2003 [93]

Let, t_a be the start time of the application and t_b be the end time of the application (i.e., $t_a < t_b$). We assume that all the deployed sensor nodes are healthy and free from internal technical glitches throughout the period of the application $t_{a,b}$ (= $t_b - t_a$). At any instance in time between t_a and t_b , every deployment point p_i is associated with an *emergency level* λ_i based on the emergency condition at that point at the time. In other words, an emergency level is a quantification of the intensity of emergency at a point, as defined next.

Definition 4.2. An *emergency level* λ_i at any instance for a deployment point *i* is defined as the average number of nodes destroyed in group G_i per unit time at that instance and the corresponding function $\lambda_i(t) : t \to \mathbb{N}$ is called the *generalized emergency level function*.

In the above definition, a node is considered destroyed or disabled if it is not capable of communicating with any of its neighboring nodes. An emergency level associated with a deployment point at any time instance is proportional to the severity of the emergency at the point at that instance. Higher the severity, higher is the node destruction rate and as a result higher will be the emergency level at the deployment point at any instance. Moreover, the emergency level at that point at a later instance in time can be higher or lower depending on whether the emergency situation at that point has worsened or subsided. This relationship is given by the generalized emergency function $\lambda_i(t)$, as discussed later. The probability of the number of disabled nodes in a group over a fixed period of time can be expressed as a *Poisson distribution* because these disablement occur with a known average rate (emergency level) during that interval and are independent of the time since the last node disablement. Since the phenomenon of disablement of nodes over a period of time (here, $t_{a,b}$) is discrete in nature, it can be modeled as a *Poisson process*, specifically as a *non-homogeneous Poisson process*. This is because, the average rate of node disablement (emergency level) may change over time (between the start and the end of the application) as the effect of the emergency at that point changes. Thus, the number of nodes disabled in a group G_i over a deployment point p_i in the time interval (t_a, t_b], given as $N_i(t_b) - N_i(t_a)$, is as shown in Equation (4.2).

$$Pr[(N_{i}(t_{b}) - N_{i}(t_{a})) = k_{i}] = f(k_{i}, \lambda_{i}^{a,b})$$

$$= \frac{e^{-\lambda_{i}^{a,b}} (\lambda_{i}^{a,b})^{k_{i}}}{k_{i}!},$$

$$where k_{i} = 0, 1, \dots |G_{i}|$$
(4.2)

Here, $\lambda_i^{a,b}$ is the overall emergency level for the deployment point p_i over the time interval $(t_a, t_b]$. As mentioned earlier, an emergency level at a point cannot be assumed constant throughout the time interval $(t_a, t_b]$. As a result, the overall emergency level $\lambda_i^{a,b}$ for the deployment point p_i can be defined in terms of the generalized emergency level function $\lambda_i(t)$ as shown in Equation (4.3)

$$\lambda_i^{a,b} = \int_{t=t_a}^{t_b} \lambda_i(t) d(t).$$
(4.3)

4.3.2 Emergency Level-based Deployment Strategy

Before describing the emergency level-based node deployment strategy, the process of assigning emergency levels to each deployment point needs to be fixed.

Determining Emergency Levels

An emergency scenario is generally a sequence of events occurring at various points over the emergency area. From the point of view of an ESN, an event can be defined as follows.

Definition 4.3. An *event* E_i at any point *i* during an emergency is any distinguishable, measurable and sometimes observable force of nature or external factor which has a distinct effect on the working and operation of the sensor nodes deployed on or around that point.

During any emergency, each deployment point is associated with a sequence of events; each event produces a different *rate* of node destruction. For example, a forest fire emergency can have some areas that are directly under a wall of fire where the destruction rate is the highest. While some others where the fire is out but still under the effect of burning objects may have a comparatively lower rate of destruction, while some others that are just under the influence of smoke might have an even lower rate of destruction. These sequence of events at any deployment point play an important role in determining the emergency level for that point. Moreover, some events are easily observable, e.g., fire, while others might not be visible to the naked eye but are easily measurable, e.g., high/low pressure. Different intensities of the same event can be modeled as multiple sequential events with different rates of node destruction. Depending on the emergency situation, the sequence of events forming the emergency can be easily predictable (and can be determined even before the emergency occurs) or can be completely unpredictable. It is easy to determine the emergency level at each deployment point if the sequence and duration of events can be predicted easily. But, real-life emergencies are generally associated with a lot of uncertainty and the sequences of events during the emergency cannot be predicted easily. Below, each case is discussed separately.

Predictable Sequence of Events: If the sequence of events at any deployment point *i* during an emergency can be predicted easily then the emergency level at that point is nothing but the sum of the number of nodes destroyed by each predicted event in the sequence during the entire period of

the emergency $t_{a,b}$. Let, $t_{a,b}$ be divided into r time slots of equal lengths, say, $t_{a,1}, t_{1,2} \dots t_{r-1,b}$. Let, $E_i = E_i^1, E_i^2 \dots, E_i^r$ be the predicted sequence of r events at deployment point p_i , where E_i^1 occurs during time slot $t_{a,1}, E_i^2$ occurs during time slot $t_{1,2}$ and so on. Let $k_{E_i^1}, k_{E_i^2} \dots, k_{E_i^r}$ be the *sensor node destruction rate* for the events $E_i^1, E_i^2 \dots, E_i^r$ respectively, i.e., $k_{E_i^r}$ number of nodes per unit time are destroyed during event E_i^r . Then, the emergency level at deployment point i through time $t_{a,b}$ can be given as shown in Equation (4.4),

$$\lambda_i^{a,b} = k_{E_i^1} \cdot t_{a,1} + k_{E_i^2} \cdot t_{1,2} + \dots + k_{E_i^r} \cdot t_{r-1,b}$$
(4.4)

Unpredictable Sequence of Events – Controlled Emergency Simulations: In situations where the sequence of events cannot be predicted easily, the best way to determine emergency levels is by conducting controlled emergency simulations. In such experiments, the desired emergency that one is trying to model is simulated in a controlled environment and the various parameters affecting the simulated emergency and/or the deployed sensor nodes are studied. In the past, researchers have carried out similar experiments to not only study the effect of emergencies on the structures and surroundings but also to provide vital data to first responders and other related agencies. As an example, consider the NEESWood project [19] at the Structural Engineering and Earthquake Simulation Laboratory at The State University of New York at Buffalo. In this project, earthquakes are simulated using shake tables to study the effect of seismic activity on the structure of wooden framework buildings. The eventual goal of this project is to provide an economical design of low and mid-rise wood-frame construction for seismic regions. Similar experiments in simulation of building [97] and forest [27,71] fires have been conducted with the aim of developing accurate models for predicting the various events and the spread of these events during the emergency. Such models are essential for building efficient decision support systems for use by the fire fighters and first responder personnel. As evident from the success of the above examples, it can be concluded that a great deal about the various events during an emergency can be learnt by conducting such simulated or controlled emergency experiments.

Thus, to prepare for an actual ESN deployment during a real-life emergency, similar repeated controlled simulations of the emergency can be carried out over the target area in advance. A fixed, large group of nodes (m_{max} , explained later) are deployed initially at each deployment point *i* and the number of destroyed nodes can be noted during each trial run of the simulation. Simulations can be repeated for a total of, say, *n* times and the number of destroyed nodes in each run *j* and at each point *i* (k_i^j) is measured. Now, given a sample of *n* measured values of disabled nodes ($k_i^1, k_i^2 \dots k_i^n$) for a point *i*, the overall emergency level $\lambda_i^{a,b}$ for that point needs to be estimated. Maximum Likelihood Estimation (MLE) analysis can be used to show that if the number of destroyed nodes ($k_i^i, k_i^2 \dots k_i^n$) is in fact the most likely value of the emergency level $\lambda_i^{a,b}$.

Let, $f(k_i^j, \lambda_i^{a,b})$ be the probability that k_i^j number of nodes are destroyed at deployment point *i* in the *j*th run of the test. Now, the value of $\lambda_i^{a,b}$ that maximizes the likelihood function *f* needs to be computed as shown below.

$$f = \prod_{j=1}^{n} f(k_i^j, \lambda_i^{a,b})$$

In order to compute the maximum likelihood value of $\lambda_i^{a,b}$, first form the log-likelihood function as shown below.

$$L(f) = ln(\prod_{j=1}^{n} f(k_i^j, \lambda_i^{a,b}))$$

$$= \sum_{j=1}^{n} ln\left(\frac{e^{-\lambda_i^{a,b}}(\lambda_i^{a,b})k_i^j}{k_i^j!}\right)$$

$$= -n\lambda_i^{a,b} + ln(\lambda_i^{a,b})\left(\sum_{j=1}^{n} k_i^j\right) - \sum_{j=1}^{n} ln(k_i^j!)$$

Now, to compute the value of $\lambda_i^{a,b}$ for which the above log-likelihood function is maximized take the derivative of L(f) w.r.t $\lambda_i^{a,b}$ and equate it to zero.

$$\frac{d}{d\lambda_i^{a,b}}L(f) = 0 \iff -n + \left(\sum_{j=1}^n k_i^j\right)\frac{1}{\lambda_i^{a,b}} = 0$$

Solving for $\lambda_i^{a,b}$ gives us the maximum-likelihood estimate for $\lambda_i^{a,b}$ as shown in Equation (4.5).

$$\lambda_{i}^{MLE} = \lambda_{i}^{a,b} = \frac{1}{n} \sum_{j=1}^{n} k_{i}^{j}$$
(4.5)

An important point that needs to be stressed here is that the techniques discussed above for determining emergency levels by simulating the emergency in a controlled environment are just one of the many ways to determine emergency levels for deployment points. In general, larger the number of k_i 's (observations) available for each sequence of events at the corresponding deployment point, better the prediction of the related emergency level λ_i at that point. These k_i 's can be either determined by simulating the emergency repeatedly (as discussed above) or even from past real life experiences during similar emergency situations. The next section focuses on determining the actual group size or the total number of nodes to be deployed at each deployment point based on the emergency level at that point.

Determining Deployment Size

Before jumping into the discussion on determining the deployment size, let's first outline the formal definition of a deployment size from the point of view of an ESN deployment.

Definition 4.4. The *deployment size* m_i for any deployment point *i* associated with an emergency level $\lambda_i^{a,b}$ is the actual number of sensor nodes that are planned to be deployed at that point.

The deployment size m_i for a deployment point *i* depends on the overall emergency level $\lambda_i^{a,b}$ at that point and is determined as follows. The deployment size consists of two components. The first, called the standard deployment (m_i^s) , is a fixed application specific constant. The next component, called varied deployment (m_i^v) , is determined by the rate of node destruction at the deployment point and is proportional to the overall emergency level at the point *i*, i.e., $m_i^v \propto \lambda_i^{a,b}$. Thus, the deployment size m_i at a deployment point *i* is a combination of the standard deployment and the varied deployments, i.e., $m_i = m_i^s + m_i^v$. Intuitively, more number of sensors are required at deployment points with higher emergency levels as compared to lower ones. According to the

proposed quantification of the deployment size, as the variable component m_i^v of the deployment size is proportional to the emergency level it will make sure that areas with higher emergencies receive a larger deployment size. Moreover, while the variable component m_i^v of the deployment size offsets the effects of node destruction around a deployment point, the standard component m_i^s will make sure that there exists enough nodes to carry out the information collection task around that point. Let, m_{max} be an application dependent upper bound on the maximum number of nodes that can be deployed at any point. The bound m_{max} depends on application specific factors like required network density, cost of nodes, priority of coverage, etc. Sensor nodes will be deployed at each deployment point in groups of size m_i if and only if this determined deployment size per group is less than the maximum upper bound on the group size, i.e., $m_i \leq m_{max}$. Another factor that would affect the size of the deployed group m_i is the area to be covered by the group of sensor nodes, i.e., the average distance between the deployment points. Intuitively, more number of sensor nodes are required to cover a larger area, but depending on the emergency situation at the area, a very high coverage might not be required. Currently, coverage issues are not addressed in this research and it is assumed that the deployment size for a group is independent of the distance between the deployment points.

Hierarchical Deployment

Due to the low computation power and storage capacity of sensor nodes, sensor network applications normally employ a store and forward model like the single-tier model or the two-tier model [89]. In the *two-tier model*, only some nodes are attached with sensing equipment and deployed at the area of interest. Data from these sensor nodes are forwarded to specially designated forwarding nodes, called *forwarders*. Forwarders are not data generators and their sole purpose is to forward data from the sensor nodes to the base station for aggregation and analysis. In the *single-tier model*, there are no forwarders and the sensor nodes in addition to collecting data also forward data for other nodes. In this work, a hierarchical deployment model is employed which is basically a single-tier deployment model with a *hierarchical* communication structure. In this model, every group G_i consists of at least one node designated as the *group head*. Sensor nodes forward data to their respective group heads as soon as it develops, which in turn aggregates it and forward it up the hierarchy to other group heads and eventually to the base-station. Because of such a hierarchical design, group heads are aware of all the active nodes within the group. Such a hierarchical design can also be used in signature-based localization schemes to decide which groups have sufficient number of nodes to perform localization accurately, as discussed in Section 4.4. But, one problem with this model is that the group head can become a single point of failure. To overcome this, a group can appoint more than one group heads depending on factors like group size, distance between deployment points, etc. To elucidate the current exposition, it is assumed here that each group consists of a single, always on (i.e., it can never be disabled/destroyed) group head. The group head can either be similar, in terms of the computation and battery power, to the other nodes or it can be a high-end device. The group heads for the respective groups can either be determined prior to deployment or it can be decided upon after deployment through efficient cluster head appointment algorithms [5, 33, 85].

The deployment strategy can now be summarized as follows:

- 1. Divide the deployment area into a fixed set of deployment points. Associate an emergency level with each point based on the severity of the emergency at that point.
- 2. Assuming that there are *k* deployment points, prepare *k* groups of nodes to be deployed at the corresponding deployment point, each of size determined by their corresponding emergency levels (as discussed above).
- 3. Information like the group sizes, emergency levels, node distribution (discussed later), etc., called the *pre-deployment information*, is loaded into the memory of every node before deployment.
- 4. Finally, deploy each group of nodes at the corresponding deployment point using nonmanual techniques like aerial scattering by an airplane or dispersion from a fire truck ladder.

The next section discusses the overall post-deployment node probability distribution and its impact on the signature-based localization schemes.

4.3.3 Deployment Distribution

For a group of nodes scattered at a deployment point, the probability that the final position of a node from the group is at the deployment point is the highest and the probability decreases as we move away from the deployment point. The final position (resident point) of the nodes after deployment can be modeled as a continuous random variable with a certain fixed non-uniform probability distribution function (p.d.f). Generally, random variates in physics and natural sciences with unknown probability distributions can safely assumed to be Normal (Gaussian). Thus, the node distribution around a deployment point can be assumed to be Normal as shown in Equation (4.6).

$$f_i = \frac{1}{\sqrt{2\pi\sigma}} e^{-[(x-x_i)^2 + (y-y_i)^2]/2\sigma^2}$$
(4.6)

For a group G_i , the mean (μ) of the p.d.f is the corresponding deployment point $p_i(x_i, y_i)$. The standard deviation (σ) is an application specific constant and depends on the coverage required around the deployment point. Let Pr_i be the probability that a node selected at random belongs to the group G_i . Then,

$$Pr_i = \frac{m_i}{m_1 + m_2 + \ldots + m_k}$$
(4.7)

where m_i , $i = 1 \dots k$ is the deployment size of the group G_i . Thus, the overall probability distribution of a (randomly selected) node over the emergency area at the moment nodes are deployed is:

$$f_{overall} = \sum_{i=1}^{k} Pr_i \times f_i \tag{4.8}$$

Probability distribution of node positions, as shown in Equation (4.8), is composed of two components. The first component of this distribution Pr_i (Equation (4.7)), is directly affected by the destruction of nodes in the groups. Whereas the second component, which gives the distribution of nodes from a particular group around the corresponding deployment point f_i (Equation (4.6)), is affected by factors that change the node locations, e.g., node movement. It can be assumed that the distribution function f_i remains unchanged throughout the period of the application $t_{a,b}$, because the current work does not intend to study the effects of factors like node movement on the node distribution and the corresponding signature-based schemes. It will be undertaken as a part of future work.

Equation (4.8) represents the probability distribution of the final position of nodes just at the moment they are deployed, i.e., at the start of the application $(t = t_a)$. But as previously mentioned, this changes with time as nodes in the various groups are disabled by the various events during the period of the emergency $t_{a,b}$. Thus, an expression that models this change in distribution is required. Let, $f_{overall}(t) : t \to \mathbb{R}$ be the corresponding overall node distribution function and $Pr_i(t) : t \to \mathbb{R}$ be the corresponding group probability function in time t. The overall probability distribution function can be given as,

$$f_{overall}(t) = \int \left(\sum_{i=1}^{k} (Pr_i(t) \times f_i)\right) dt$$
(4.9)

Since the nodes are deployed exactly at time t_a , we can assume that for $t < t_a$, $Pr_i(t) = 0 \forall i$. Thus, the probability distribution at the time of deployment ($t = t_a$) is

$$f_{overall}(t_{a}) = \int_{t=0}^{t_{a}} \left(\sum_{i=1}^{k} (Pr_{i}(t) \times f_{i}) \right) dt$$

$$= f_{1} \int_{t=0}^{t_{a}} Pr_{1}(t) d(t) + f_{2} \int_{t=0}^{t_{a}} Pr_{2}(t) d(t) + \dots + f_{k} \int_{t=0}^{t_{a}} Pr_{k}(t) d(t)$$

$$= f_{1} \times Pr_{1} + f_{2} \times Pr_{2} + \dots + f_{k} \times Pr_{k} (From Equation (4.7))$$

$$= \sum_{i=1}^{k} Pr_{i} \times f_{i}$$

$$= f_{overall} (Equation (4.8))$$

Now, the overall probability distribution function (Equation (4.9)) can be expressed in terms of the

generalized emergency level function $\lambda_i(t)$ as,

$$f_{overall}(t) = \sum_{i=1}^{k} \left(f_i \times \int Pr_i(t)dt \right)$$
$$= \sum_{i=1}^{k} \left(f_i \times \int \frac{m_i - \lambda_i(t)}{(m_1 - \lambda_1(t)) + (m_2 - \lambda_2(t)) + \dots + (m_k - \lambda_k(t))}dt \right)$$
(4.10)

The overall probability distribution function during the entire period of the application $t_{a,b}$ can be obtained by limiting the integral in Equation (4.10) between t_a and t_b as shown in Equation (4.11) below.

$$f_{overall}(t_b) = \sum_{i=1}^k \left(f_i \times \int_{t=t_a}^{t_b} \frac{m_i - \lambda_i(t)}{(m_1 - \lambda_1(t)) + (m_2 - \lambda_2(t)) + \dots + (m_k - \lambda_k(t))} dt \right)$$
(4.11)

Thus at the beginning of the application when the nodes are just deployed, the probability that a randomly selected node lies closer to deployment points with higher emergency levels is high. But, with time this may no longer be true. Nodes in groups near higher emergency levels may also be destroyed with a higher rate and as a result the actual size of such groups may be fairly smaller as compared to their original size at deployment. As discussed in Section 4.2.2, current signature-based localization schemes assume that the node distribution, approximated at the time of deployment (Equation (4.8)), holds true for the entire period of the emergency application, which is not true. The loss of nodes in each group changes this distribution as shown above and the localization schemes should use the most current node distribution. Next, a very simple and intuitive solution to the above problem, called the Group Selection Protocol (GSP), is discussed.

4.4 Improving Signature-based Localization

Group Selection Protocol or GSP, which is implemented on top of a signature-based localization algorithm (like the one discussed in Section 4.2), continuously monitors changes to the node distribution due to disablement and helps improve the accuracy of the localization algorithm.

4.4.1 Group Selection Protocol (GSP)

Let, a_i be the number of nodes from group G_i that the target node at point $\theta(x, y)$ can hear from and let z_i be the distance from the target node to the deployment point of group G_i . The problem with the localization algorithm discussed in Section 4.2 is that in emergency situations, not every observation a_i in $\{a_1, \ldots, a_n\}$ is correct or accurate. Groups where the node destruction rate is high might not be able to provide the correct value of a_i for localization. These incorrect values of a_i increase the localization error during trilateration. One way to overcome this problem is by being selective in choosing groups G_i 's (and the corresponding observations a_i 's) for the localization process. GSP uses a_i 's from only those groups that are *healthy*. First, lets define the notion of group health.

Definition 4.5. The *health* of a group is quantified by the number of active nodes in the group. A node is active if it is able to communicate with at least one other node in the same group.

This notion of a healthy group is application dependent. In other words, a group is considered healthy if its size is at least equal to some application dependent lower bound. Without loss of generality, let us assume here that a group is healthy at any instance if its size at that instance is equal to its standard deployment size (m_i^s) , which was fixed at the time of deployment. Now, GSP uses only observations from those groups for localization where the current health is at least equal to its standard deployment size (m_i^s) . Such a modification might reduce the number of z_i 's (distances) available for localization. But, as long as at least 3 relatively accurate values of z_i are be determined, localization can be done efficiently. Absence of at least 3 values for z_i due to unavailability of healthy group observations will cause the localization process to fail. But, due to the criticality of the applications in emergency situations sometimes no location is better than an incorrect value.

In GSP, group heads are used to monitor the health of their corresponding groups. As the ad-hoc network comes up after deployment, nodes begin sending initial setup information to their respective group heads. The group head updates the health of its group by either using these

setup communications or by using the explicit *health update* packets that can also be sent by the nodes. At regular intervals, the group heads broadcast the current health of their respective groups. These broadcasts are forwarded by all nodes in the network up to a certain hop count so that even nodes in other groups (and farther away from the group head) can know the health status of a particular group. Based on the current health of a group, the target node decides on whether or not to use neighborhood observations from that group to compute the distance to the corresponding deployment point. In addition to this, communications between the nodes and the group heads can be synchronized with the sleep-wake cycles of nodes in order to save power and to make the process more efficient for the nodes. The Group Selection Protocol (GSP) is outlined in Algorithm

3.

- 1: Observe the neighborhood, i.e., $\{a_1, a_2 \dots a_k | a_i \text{ is the number of nodes from group } G_i \text{ that are in radio range. } \}$
- 2: Wait and observe health broadcasts (h_i) from the group heads. Update h_i to the latest value for each group.
- 3: for all groups G_i for which h_i is known do
- 4: **if** The group is healthy, say $(h_i \ge m_i^s)$ **then**
- 5: Compute $g(z_i) = a_i/h_i$.
- 6: Compute z_i from $g(z_i)$ by looking up the table for $g(z_i)$.
- 7: **end if**
- 8: end for

```
9: if z_i corresponding to at least 3 distinct groups G_i is known then
```

```
10: Compute \theta(x, y) by trilateration (using z_i's and their corresponding p_i's)
```

- 11: **else**
- 12: "Cannot do Localization!"
- 13: end if

Algorithm 3: Group Selection Protocol (GSP)

4.4.2 Analysis of GSP

Although the GSP proposes only minor and intuitive improvements, it performs better than existing signature-based localization algorithms in dynamic scenarios. This claim has been verified by simulation experiments, as outlined in detail in Section 4.6. Simulation results show that GSP does improve the localization accuracy of signature-based algorithms when nodes over the deployment

area are randomly disabled. But, this improvement comes at the cost of extra communication and processing overhead. Below, the extra costs that may be incurred by the network in order to implement GSP have been enumerated.

- 1. There is an additional requirement for a node to act as a group head. In this regard, a cluster formation or group head selection algorithm might have to be executed immediately after deployment.
- 2. Each node in any group G_i may have to generate an extra health update packet. In addition to this, it has to forward at most m_i extra (health update) packets for nodes in the same group.
- 3. The group head has to receive and process at most m_i extra (health update) packets from nodes in the same group and broadcast an extra health notification packet to all nodes.

Despite the improvement in localization accuracy by employing GSP, there are still some problems with existing signature-based approaches that have been left unaddressed. Current signaturebased schemes are extremely complex involving hard to compute functions. Simplifying the process by using regression-based or table-based approximation techniques [26] results in loss of accuracy in addition to other issues like offline computation and storage of complex functions in the memory of the resource constrained sensor nodes. Although GSP provides some improvement in terms of accuracy, it does not improve the complexity of signature-based schemes. Moreover, just employing GSP is not sufficient if the node destruction is widespread and not localized only to certain deployment points over the emergency area. To overcome these problems, a simple and novel signature-based localization approach, called ASFALT, is proposed. Rather than using just the neighborhood observations, ASFALT uses distance measurements to groups of nodes (in the neighborhood) for distance computation. ASFALT not only improves the localization accuracy but is also much more computationally efficient as explained in the following section.

4.5 ASFALT: A Simple FAult-tolerant Signature-based Localization Technique

ASFALT together with GSP is not only fault-tolerant against random node disablement, but also removes the requirement for storing large tables, executing complex computations or performing costly table look-up operations. In this localization approach, instead of just observing its neighborhood (number of nodes from each group that are in radio range), the target node computes distances to each such node in its neighborhood. The set of distance estimates from the target node to all nodes in a particular group is called the *distance vector*, while the set of distance estimates from the target node to all neighborhood nodes from a particular group is called the *observed distance vector* for that group. Assuming that the distribution of the nodes around the corresponding deployment point is Normal, these distance vector (or an observed distance vector), the distance from the target to a deployment point can be approximated by computing the mean of the vector (sample). Given three or more such distances, the location of the target node can be computed by using trilateration or any other suitable constraint satisfaction technique.

4.5.1 Assumptions

One of the requirement for ASFALT is that nodes should be deployed over the deployment area using a non-uniform deployment strategy like an emergency level-based deployment strategy (Section 4.3). As discussed earlier, in an emergency level-based deployment strategy the final position of nodes in a group can be assumed to follow a two dimensional Normal distribution with mean μ as the corresponding deployment point and an application dependent constant variance σ^2 (Equation (4.6)). In addition to this, any node is accurately and efficiently able to estimate its distance to all of its one hop neighbors. Efficient techniques to estimate distances like Received Signal Strength Indicator (RSSI), Time of Arrival (ToA), Time Difference of Arrival (TDoA), etc., [40,42] exist in the literature. Although the simulation experiments for ASFALT, as discussed in Section 4.6, use RSSI to compute the distance between nodes, the algorithm itself is general enough and works well with other distance estimation (ranging) techniques. Lastly, the nodes within a particular group are randomly selected for disablement and do not follow any specific pattern/distribution. This is a reasonable assumption because nodes within a group with a specific emergency level have an equal probability of being destroyed. This is different from the number of nodes destroyed which is still a Poisson process and depends on the rate of destruction at a deployment point. As a result, the probability distribution function of the remaining nodes in a group is still Normal. All the symbols and terminology used in this section are same as Section 4.3.

4.5.2 Localization Scheme

Let *M* be the target node for which localization has to be done and let $\theta(x, y)$ be the actual position of *M*. Let z_i be the actual distance between $\theta(x, y)$ and some deployment point *i*. Let the total number of nodes deployed at deployment point *i* (group G_i) be m_i and let $d_i^1, d_i^2 \dots d_i^{m_i} | d_i^j \in \mathbb{R}$ be the distances of the nodes from the deployment point *i* ($d_i^j > 0$, if the position of node *j* is after *i* on the real line and $d_i^j < 0$ otherwise). Assuming that all m_i ($m_i^s + m_i^v$) nodes in G_i are in the radio range of *M*, let $z_i^1, z_i^2 \dots z_i^{m_i}$ be the distances of these nodes from the target node *M*. As discussed earlier, the distances in the set $\{d_i^1, d_i^2 \dots d_i^{m_i}\}$ follow a Normal distribution. Let, \tilde{d} be the random variable that takes values in this distribution. Thus, the expected value of \tilde{d} is as shown in Equation (4.12).

$$E(\tilde{d}) = 0 \tag{4.12}$$

In other words, the mean value of all distances selected from this distribution is 0. Now, let \tilde{Z}_i be the random variable that takes values in the distribution followed by the distance between each node of group G_i and the target node M. Since each z_i^j depends on the corresponding d_i^j , from Equation (4.12), it can be said that

$$E(\tilde{Z}_i) = z_i \tag{4.13}$$

The ASFALT localization technique can then be outlined as shown in Algorithm 4. In order to

1:	Observe the neighborhood. Compute $\{a_1, a_2 \dots a_k a_i \text{ is number of nodes from } G_i \text{ in radio}$
	range. }.
2:	for all groups G_i for which $a_i \neq 0$ do
3:	Compute $z_i^1, z_i^2 \dots z_i^{a_i}$ i.e., distance to all the a_i nodes.
4:	Observe health broadcasts (h_i) from the group head. Update h_i to the latest value for the
	group.
5:	end for
6:	for all groups G_i for which h_i is known do
7:	if The group is healthy, say $(h_i \ge m_i^s)$ then
8:	if $(a_i < \alpha_i)$ then
9:	Continue; {Sufficient samples not available for approximating z_i }
10:	else if $(a_i \ge \alpha_i)$ and $(a_i < \beta_i)$ then
11:	Compute $z_i = max\{z_i^1, z_i^2 \dots z_i^{a_i}\}$; {Sample not large enough to represent the entire dis-
	tribution }
12:	else if $(a_i \ge \beta_i)$ then
13:	Compute $z_i = \frac{\sum_{j=1}^{a_i} z_i^j}{\{\text{Compute mean of all samples}\}}$
14:	end if
15:	else
16:	if $(a_i < \beta_i)$ then
17:	Continue;
18:	else
19:	Compute $z_i = \frac{\sum_{j=1}^{a_i} z_i^j}{\sum_{j=1}^{a_j} z_j^j}$
20:	end if
21:	end if
22:	end for
23:	if z_i corresponding to at least 3 distinct groups G_i is known then
24:	Compute $\theta(x, y)$ by trilateration (using z_i 's and their corresponding p_i 's)
25:	else
26:	"Cannot do Localization!"
27:	end if
Algorithm 4: ASFALT Localization Algorithm	

compute $\theta(x, y)$ by trilateration, M needs at least 3 or more z_i 's (or distances to known deployment points). M first observes it neighborhood $(a_1, a_2 \dots a_k)$, where a_i is the number of nodes from group G_i in the radio range of M. Using any efficient distance computation method, M computes the observed distance vectors $\{\bar{z}_1 = (z_1^1, z_1^2 \dots z_1^{a_1}), \bar{z}_2 = (z_2^1, z_2^2 \dots z_2^{a_2}) \dots \bar{z}_k = (z_k^1, z_k^2 \dots z_k^{a_k})\}$. It then computes the corresponding z_i by taking the mean of the scalar values $(z_i^1, z_i^2 \dots z_i^{a_i})$ of the corresponding observed distance vector \bar{z}_i . The distance to the deployment point $i(z_i)$ can be computed as shown in Equation (4.14).

$$z_i = \frac{\sum_{j=1}^{a_i} z_i^j}{a_i}$$
(4.14)

It is obvious that larger the size a_i of the observed distance vector \bar{z}_i , better is the approximation for z_i . The best approximation is when distances from the whole group, i.e., a distance vector is available. But, a distance vector may not be available due to two reasons: 1) only some nodes in a group may be in the radio range of the target node (Figure 4.1b), or 2) some nodes in a group may be disabled (Figure 4.1c). These two cases need to be distinguished and handled separately during localization. In order to accomplish this, GSP is implemented on top of ASFALT. GSP monitors the health of the neighboring groups. If a group is healthy ($h_i \ge m_i^s$) but still the target node hears from only a few nodes from that group, it would imply that not all nodes in that group are in the radio range. Otherwise, if the group is not healthy ($h_i < m_i^s$), the usefulness of the observation vector is determined by the number of nodes visible (a_i) and a parameter β_i discussed next.

4.5.3 Determining ASFALT Algorithm Parameters

The ASFALT algorithm, as discussed above, requires two parameters to determine if an observed distance vector $\bar{z}_i = (z_i^1, z_i^2 \dots z_i^{a_i})$ for any deployment point *i* is large enough to approximate the distance z_i with reasonable accuracy. The *mean threshold* β_i for a group G_i is the minimum size of the observed distance vector or the minimum number of distance values required in the observed distance vector for that group so that it represents the original distribution of nodes around the corresponding deployment point with reasonable accuracy. If the size of the observed sample is at least β_i then the algorithm computes the distance z_i as the mean of the distance values in the sample. If the size of the observed sample is less than β_i then it means only part of the group can be heard by the target node. In this case, one heuristic to estimate z_i , if the group is healthy, is to pick the largest value of the distance in the sample as a possible choice for z_i . In the ideal situation, $\beta_i = |m_i^s|$, i.e., β_i equals the size of the healthy group. But, it has been observed that $\beta = \frac{|m_i^s|}{2}$, i.e., half

of the healthy group size has worked well for most cases during the simulation experiments. The *minimum threshold* α_i is the *minimum* number of distance values required in the observed distance vector to make a fair estimation of the distance z_i . If the size of the observed distance vector is less than α_i , ASFALT discards that observation from consideration in the localization process. This prevents inclusion of erroneous measurements in the trilateration process. The minimum threshold α_i is generally assigned a low value. Simulation experience has shown that $\alpha_i \approx \frac{|m_i^2|}{3}$ works well for most cases. Although, an analytical representation of α_i and β_i would be more useful in deciding their optimal values for particular situations, such a mathematical formulation is non-trivial and depends on factors like the variance of the node probability distribution around the deployment point and the locations of the nodes in the observed distance vector. This study will be a part of future research.

4.5.4 Analysis

Since ASFALT uses GSP, the communication overhead required for GSP also applies to ASFALT (Section 4.4.2). Other than the communication overhead imposed by GSP, ASFALT requires no other extra communication as compared to the beaconless scheme discussed in Section 4.2. Contrary to the scheme in Section 4.2, ASFALT also does not require extra storage and look-up for the g(z) function table (Equation (4.1)). It does require computation of the observed distance vector for each group and the eventual distance from the target node to each of the deployment points. But, these computations are comparatively simple and straightforward involving basic mathematical operations, and can be easily implemented on the sensor nodes.

4.6 Evaluation

A detailed evaluation of the fault-tolerance related enhancements proposed in this chapter is carried out using the J-Sim network simulation tool [83] and a comparative analysis of the performance of the proposed fault-tolerant schemes against existing signature-based schemes is presented. In the first set of simulation experiments, the beaconless algorithm by Lei et al. [26] both with and without the GSP improvement and the ASFALT algorithm are simulated under similar network conditions and their performance in the presence of random node disablement are evaluated. The metric for evaluating performance is the average of the localization error of all nodes from a chosen group of nodes, and is measured in meters. The second experiment observes the effect of radio range *R* of the target node on the accuracy of the ASFALT algorithm. The results of these experiments verify the claim that the proposed improvements, namely GSP and ASFALT, actually improve the fault-tolerance of the signature-based localization process.

4.6.1 Experimental Setup

The deployment area for the simulation experiments is a two dimensional unobstructed terrain that is divided into a grid of size $600m \times 600m$. The deployment area and node deployment for these experiments is depicted in Figure 4.4. As shown in the figure, the area of interest on the grid consists of 9 deployment points each 100m apart. Each deployment point has 20 nodes deployed around it in a group, and each group of nodes follows a two dimensional Normal distribution around the corresponding deployment point with mean as the deployment point and a standard deviation (σ) of 50. Readers should note that the node positions in Figure 4.4 are not symbolical of the actual positions of the nodes during the simulation experiments. Figure 4.4 is just used to give the readers a rough idea of the experimental setup. Another point to note here is that the main aim of these experiments is to observe the effect of node destruction on the accuracy of the various signature-based localization schemes and not to determine an efficient deployment of nodes based on the emergency levels at each deployment point. As a result, the deployment size for each group in the current set of experiments is fixed (20 in this case). In each run of the experiment, nodes are assigned new positions that follow a Normal distribution with the same parameters. In each group, one node selected at random is assigned to be the group head. This node is never disabled during the experiments. The location estimation error for each node is measured as the Euclidean distance between the actual position and the position estimated by the localization algorithm being simulated.



Figure 4.4: Simulation setup - topology and node deployment

4.6.2 Estimated Error vs Number of Destroyed Nodes

In this set of experiments, both the beaconless algorithm by Lei et al. [26] (with and without GSP) and the ASFALT algorithm are simulated in dynamic conditions. Nodes are destroyed from groups one and five (marked with dotted circles in Figure 4.4) only[†] and the number of destroyed nodes in each group is varied from 1 up to 15. The standard deviation (σ) of the Normal distribution around each deployment point is 50 and the transmission range of each node is 200*m*. For each group, the mean threshold β_i is 10 and the minimum threshold α_i is 5. The average location estimation error of all the nodes from group four (the center-most group) is plotted against the number of nodes disabled in each of groups one and five as shown in Figure 4.5(a). In order to avoid the boundary nodes, only the localization errors of nodes in group four are considered. This is because localization. From Figure 4.5(a), it can be seen that the ASFALT localization algorithm performs better as compared to the other two algorithms. As the number of disabled nodes per group increases the average localization error of all the three algorithms increases. For lower

[†]As compared to experiments in Section 4.2.2 where nodes from all the groups are destroyed



Figure 4.5: Comparison of the average localization error of the algorithm proposed by Lei et al. [26] (with and without GSP) and ASFALT. (a) $\sigma = 50$ (b) $\sigma = 100$

number of destroyed nodes, the beaconless algorithm by Lei et al. [26] outperforms its variant with the GSP. This is because, the GSP employed in this experiment does not consider samples from any group whose advertised health (h_i) differs even slightly from its original health. Thus, it completely disregards samples from groups one and five even when the number of destroyed nodes is low. GSP improves the performance of the algorithm when the number of disabled nodes is a little higher. The most interesting trend that can be seen in this plot is that the average localization error of ASFALT increases much less sharply as compared to the other two algorithms. Similar experiments have also been carried out for $\sigma = 100$, i.e., when nodes are sparsely distributed around the deployment point. The plot for these experiments is shown in Figure 4.5(b). It can be seen that the trend in the accuracy of the algorithms is very similar to the case with $\sigma = 50$, but the localization error is comparatively higher in this case.

4.6.3 Estimated Error vs Radio Range

In this experiment, the effect of radio (transmission) range of nodes on the performance of ASFALT is observed. The experiment begins with a radio range of 50m and re-runs the simulations for ASFALT by increasing the range of the nodes by 50m in each run. The positions of the nodes

are changed in each run, but they still follow the same distribution. An average of the localization errors of all nodes in group four is plotted against the radio range. The number of nodes destroyed in groups one and five remain constant at 10 and the standard deviation (σ) of the distribution is fixed at 50. The simulation results for this experiment are outlined in Figure 4.6. The results are quite intuitive and it can be observed that as the radio range increases the localization error decreases. This can be attributed to the fact that as the radio range increases, each node is able to cover a larger area and thus distance samples of a larger size are available from each group for localization.



Figure 4.6: ASFALT($\alpha = 5, \beta = 10$), Average Estimation Error vs. Transmission Range

4.7 Conclusion

This chapter addressed the problem of robust sensor node deployment and fault-tolerant localization in ESN applications, especially sensor network applications where node disablement exists. Signature-based algorithms are a popular alternative to costly, and at times, inefficient beaconbased approaches for use in ESN localization, except that they are not fault-tolerant. By means of a case study and related simulation experiment results, this chapter showed that popular signaturebased or beaconless algorithms failed to perform well in situations where node disablement was present. Another drawback, as evident from the presented case study, was the high complexity and resource requirements of existing signature-based schemes.

The root cause of the lack of fault-tolerance in signature-based localization, as concluded after the case study, was the poor node deployment strategy employed by earlier techniques. To overcome this problem, this chapter first proposed an efficient strategy for node deployment, called the emergency level-based node deployment strategy. This strategy deployed nodes at points over the deployment area based on the rate of node disablement at those points. It employed a stochastic model of node disablement that provides a prediction for the total number of disabled nodes, and thus the emergency levels, at all the points over the deployment area. Next, a simple enhancement to existing signature-based schemes, called Group Selection Protocol (GSP), was proposed. GSP improved current signature-based schemes by monitoring changes in node distribution. Experimental results showed that implementing this protocol over current signature-based schemes improved their fault-tolerance slightly. Finally, a novel, fault-tolerant signature-based localization technique, called ASFALT, was proposed. ASFALT was shown to be simple and easily implementable on fragile and low power systems like wireless sensor networks. ASFALT used the emergency level-based deployment strategy, GSP and a simple averaging argument to estimate node locations. The fault-tolerance of ASFALT was verified using simulation experiments, which showed that it performed better than other popular signature-based approaches, especially in situations where the degree of node disablement was high.

The next chapter studies the problem of efficient mitigation of inconsistent location information in localization schemes and location-based services.
Chapter 5

Mitigating Inconsistencies in Location Information

"There is nothing constant in this world but inconsistency."

- Jonathan Swift

5.1 Introduction

Up to this point, the main focus of this dissertation was to address the security and robustness issues associated with the process of location discovery or localization. Specifically, the problem of cheating beacons in distance-based localization schemes and the problem of disabled nodes in signature-based localization schemes were addressed. This chapter addresses a related problem, which is to efficiently mitigate inconsistencies and cheating behavior during location advertisement/verification in localization and location-based services for wireless sensor networks. Location dependent applications in sensor networks can be modeled using a graph-theoretic framework such that inconsistent location information or cheating behavior in such applications can be represented by a set of inconsistent edges in this graph model of the network. The problem of eliminating location inconsistencies can then be formulated as an optimization problem that determines the largest consistent subgraph of the graph-based model of the network. This chapter studies the combinatorial properties for two variants of this problem and outlines intelligent heuristics to provide efficient solutions for them.

5.1.1 Motivation and Problem Statement

As discussed in Chapter 1, location information is extremely essential and critical in wireless sensor network applications involving monitoring and emergency response. Any information without the associated location of occurrence or location of generation is generally useless. Thus, the localization service of the network, which helps the individual sensor nodes determine their own location, is extremely essential and an integral part of such highly distributed and autonomous network systems.

Nodes in a sensor network application generally associate their own location with the monitored/sensed data. This location is easily verifiable at the neighboring nodes, provided the neighbors know their own location and the distance between them can be determined efficiently. The verifier node simply needs to compare this estimated distance (using RSSI, ToA, TDoA or other well-known techniques [3, 40]) to the Euclidean distance between its own location and the advertised location of the neighboring node. If the difference between these distances is greater than some threshold, then there is definitely some inconsistency, either in location advertisement or in location verification. Figure 5.1 depicts one such scenario, where node 2 sends its location (x_2 , y_2) along with the monitored data to its neighbor node 4 (at location (x_4 , y_4)) who can then verify if node 2 is telling the truth about its location. Such a verification procedure has also been used in some localization techniques to weed out malicious beacon nodes [74].

This inconsistency in location information, as discussed above, could be due to multiple reasons. Cheating behavior (in terms of incorrect advertised self location or distance manipulation techniques) in localization protocols was discussed in Chapters 1 and 3. Such cheating behavior by nodes is also possible post-localization in order to mislead other nodes about one's own location or to falsify the generated data that would prevent successful completion of the data-related application. Either the location advertising node can cheat or the location verification node can cheat. Cheating behavior may not necessarily be the only cause of such an inconsistency. External fac-



Figure 5.1: Cheating/Inconsistency in Location Claims/Verification

tors like radio interference, large objects, etc., can also result in the neighboring nodes not able to verify each others locations correctly. For example, assume that two (wireless) neighboring nodes use RSSI to estimate the distance between them. A large object or obstruction between the two nodes can cause the radio signals originating from these nodes to lose more power than normal. As a result, despite the nodes' honest behavior, the estimated distance (by RSSI) between them will never match with the Euclidean distance between their advertised locations. Irrespective of the cause of this inconsistency, it needs to be mitigated in an efficient manner. As discussed earlier, inconsistent location information in a network is not good for multiple reasons. Firstly, inaccurate location information can render the information collected by the network useless and can be used to mislead the users of this information. Secondly, this inconsistent information can adversely affect related network services like routing, neighborhood discovery, etc., that use location information to make network-wide decisions. This chapter focuses on studying the problem of efficient elimination of such inconsistent location data from a theoretical point of view. Such a study is extremely essential in order to understand the feasibility (in terms of computational complexity) of solving the problem and to fix bounds on the worst case solution quality. All this eventually helps in designing efficient algorithms that can not only be applied to the domain of sensor networks but

also extended to other distributed and autonomous network system domains.

In this direction, this chapter first introduces an efficient graph-theoretic framework for modeling location based services in wireless sensor networks. This model is inspired from the Grounded Graph model by Eren et al. [25] where each vertex of the graph corresponds to a sensor node; an edge exists between two nodes if and only if they are in radio range of each other. In the model presented here, a location function assigns each vertex a value indicating the advertised location by the corresponding node and a distance function assigns each edge a value indicating the estimated distance between the two connecting nodes. Contrary to the model by Eren et al. where the distance function is always honest, the distance function in this model can assign inaccurate values to the edges. Similarly, the location function can also cheat. Moreover, in Eren's model only some nodes know their locations, i.e., the beacon nodes, whereas in this model all nodes are assumed to know their own locations (through some localization process). Such a graph for the network is referred to as a Partially Consistent Grounded Graph (PCGG). The problem of efficient elimination of location inconsistencies can then be formulated as the problem of obtaining the largest consistent subgraph of the PCGG of the network. Specifically, two optimization problems are formulated, namely MAX-CON and LARGEST-CON. MAX-CON is the problem of obtaining the consistent subgraph with the largest number of vertices, while LARGEST-CON maximizes the number of consistent edges in the subgraph. The combinatorial properties of these optimization problems are studied and approximation algorithms based on popular heuristics are proposed for solving these problems. These algorithms are compared and verified using computer simulation measurements.

5.1.2 Chapter Organization

Section 5.2 presents a graph-theoretic framework for modeling location-based services in highly distributed and autonomous network systems like wireless sensor networks and introduces the concept of Partially Consistent Grounded Graphs (PCGG). Section 5.3 formulates the MAX-CON problem and presents the related combinatorial results. Section 5.4 formulates the LARGEST-

CON problem and presents the related combinatorial results. Section 5.5 presents heuristics-based algorithms for LARGEST-CON, while Section 5.6 outlines results from the experimental evaluation of these algorithms. Section 5.8 concludes the chapter with a summary of results.

5.2 Network Model

Before defining the graph model for the network, let us introduce the concept of *location state* for a node.

Definition 5.1. The *location state* of a node is the most recent value of the actual location of the node.

The location state of a node *i* is denoted as $p_i = (x_i, y_i)$, where $x, y \in \mathbb{R}$. Without loss of generality, let $p_i \in \mathbb{R}^d$, d = 2, i.e., assume a two dimensional coordinate system. However, the results presented here can be easily extended to three or higher coordinate systems. A node determines its location state by employing the localization service that is available for the network. It is assumed here, that the localization service itself is honest and that each node is able to accurately determine its location using the localization algorithm. The location state is *private* to each node. The actual advertised location by each node may or may not be the same as its location state. Details of this are explained later.

Let $N = \{1, 2, ..., n\}$ be the set of *n* nodes and let $P = \{p_1, p_2, ..., p_n\}$ be the set of their corresponding location states. Define the graph $G = (V, E \cup E')$ for the network as follows. The set $V = \{v_1, v_2, ..., v_n\}$ of vertices contains a vertex corresponding to each node in the network. An edge exists between two vertices *i* and *j* in the graph *G* if and only if the corresponding nodes are in the radio range of each other, i.e., they are able to communicate with each other directly (in one hop.) This relationship is assumed to be *symmetric*, i.e., if node *i* is in the radio range of node *j*, then node *j* is also in the radio range of node *i*. Thus, the edges in this graph model of the network are *undirected*. The set $E \cup E'$ is the set of all the edges as defined above. More details on the composition of individual edge subsets *E* and *E'* will follow later. Two nodes are said to

be *neighbors* if and only if there exists an edge connecting their corresponding vertices. In other words, $E \cup E'$ gives the *neighborhood relation* for each node in the network. For simplicity, the graph G defined above is assumed to be a connected graph, i.e., every vertex is reachable from every other vertex through a sequence of edges.

The graph *G* is associated with two weight functions. The first function, called the *location* function $w, w : V \to (\mathbb{R}, \mathbb{R})$, assigns a two dimensional coordinate value to each vertex. This value represents the location advertised by the node. If a node *i* is honest then $w(i) = p_i$, i.e., the value of the location function equals to the location state for the node. If the node cheats in advertising its location then the value w(i) is arbitrarily selected by the location function. If $w(i) = p_i$, $\forall i \in V$ then the location function is an *honest location function*, otherwise if there is at least one node *j* such that $w(j) \neq p_j$ then the location function is *cheating*.

The second function, called the *distance function* δ , $\delta : E \cup E' \rightarrow \mathbb{R}$, assigns a value to each edge signifying the estimated distance between the nodes. As discussed earlier, this estimation can be carried out by the verifier node in the pair (of nodes). There are multiple ways in which this function can be efficiently executed in practice and have been discussed in detail in Chapter 1. The exact details of this function will vary from application to application and it can be safely assumed that such a function exists and can be efficiently computed. If there is at least one pair of nodes (edge) such that the distance between them cannot be estimated correctly then the distance function is called a *cheating distance function*. The distance function is *honest* otherwise. Note that the notion of cheating used here is a *weak* notion. Cheating here not only includes errors resulting from malicious intent but also includes cases where the distances cannot be estimated correctly due to external factors like radio interference, obstructions, etc. The weak notion suffices in this model, because here the aim is to eliminate inconsistencies (defined later) and not to detect cheating nodes. A similar model, called Grounded Graphs, was proposed by Eren et al. [25]. The authors used Grounded Graphs to formulate the problem of beacon-based localization as a Constraint Satisfaction Problem (CSP) where some nodes know their own locations and other nodes attempt to localize themselves by solving a set of edge constraints (value of the distance function).

Now, lets formally define the notion of an inconsistency. The *actual distance value* between a pair of nodes is the Euclidean distance between the advertised location values (value of the location function) of the two nodes. Thus, the actual distance value between two nodes *i* and *j* with location function values $w(i) = (x_i, y_i)$ and $w(j) = (x_j, y_j)$ can be computed as,

$$dst(i, j) = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$
(5.1)

The difference between the actual distance value and the value of the distance function is called the *estimation error*. Let ϵ denote the maximum allowable estimation error in the system, also called the *error tolerance factor*. The value of ϵ should be zero ideally, but in most practical cases it is assumed to have a very small value. Edge consistency can be defined as follows.

Definition 5.2. An edge (i, j) in the Grounded Graph is said to be *consistent* if and only if its estimated distance function value is within some small system-dependent error tolerance factor ϵ of its actual distance value.

$$dst(i, j) - \epsilon \le \delta(i, j) \le dst(i, j) + \epsilon$$
(5.2)

An edge that is not consistent is said to be an *inconsistent edge*. From Equation (5.1) and Equation (5.2), it can be seen that an inconsistent edge results from either a cheating location function or a cheating distance function. At this point, let's make some important observations.

- The first observation is that nodes with malicious intent do not cheat all the time. In other words, malicious behavior is *random*. As a result, not all edges coming out of a particular malicious node will be inconsistent. If they do, then such a behavior is trivial to detect. For example, nodes may behave maliciously at random or intermittently to avoid easy detection. There will be some exceptions to this rule but their numbers are generally small.
- 2. The second observation is that cheating does not always imply inconsistency. For example,

refer to Figure 1.3 in Chapter 1. Here node B_2 can advertise its location as any point on the circle (not shown in the figure) with center T and radius z_2 . The distance from the node T will still be determined correctly as z_2 and the edge (B_2, T) will always be consistent. But, in doing this the node B_2 will not be able to fool its third neighbor with whom its estimated distance will not match the actual distance.

3. The attack, as described in the second point, will be successful only if all the neighbors of, say, node B_2 collude. Such kind of collusion attacks will not result in any inconsistent edges. This issue of collusion is not addressed here.

The graph-based model, as defined above, consisting of at least one or more inconsistent edges is referred to as a Partially Consistent Grounded Graph (PCGG) and can be formally defined as follows.

Definition 5.3. A *Partially Consistent Grounded Graph (PCGG)* $G = (V, E \cup E', \delta, w)$ is a graph G as defined above, where V is the set of vertices corresponding to nodes in the network and the edge set is defined by the neighborhood relation. The edge set can be partitioned into two non-empty disjoint subsets, namely the set of consistent edges (E) and the set of inconsistent edges (E'). δ is the distance function and w is the location function.

Definition 5.4. A Consistent Grounded Subgraph (CSG): A Consistent Grounded Subgraph (CSG) $\tilde{G} = (\tilde{V}, \tilde{E})$ is an induced subgraph of a PCGG $G = (V, E \cup E', \delta, w)$, where $E' \neq \phi$, such that the vertex set $\tilde{V} \subset V$ and the edge set \tilde{E} contains only consistent edges i.e., $\tilde{E} \subseteq E$.

The *size* of a CSG is the cardinality of its vertex set. The *edge size* of a CSG is the cardinality of its edge set. A CSG is *maximal* if its vertex set is not a proper subset of the vertex set of any other CSG. A *maximum* CSG is a maximal CSG with maximum size.

Definition 5.5. A *Largest Consistent Grounded Subgraph (LCSG)* of a PCGG is a CSG that has the maximum edge size, if more than one CSG exists.

Figure 5.2(a) shows a PCGG $G = (V, E \cup E')$, Figure 5.2(b) shows its corresponding maximum CSG and Figure 5.2(c) shows the largest CSG.



Figure 5.2: (a) PCGG, $G = (V, E \cup E')$; (b) Maximum CSG of G; (c) LARGEST CSG of G

From now on, a PCGG will be denoted just by $G = (V, E \cup E')$; the location and distance functions will not be explicitly specified with the definition of PCGG. These functions are just required to partition the edge set into a set of consistent edges and a set of inconsistent edges. Once we have the two distinct edge sets, these functions are no longer required for the formulation of the problem of mitigating inconsistencies (or obtaining the consistent subgraph.) In order to simplify the notation, these functions are ignored from the definition of PCGG. In the following section, the optimization problem for obtaining a maximum CSG from a PCGG is formulated and its combinatorial properties are studied.

5.3 Maximum Consistent Grounded Subgraph

5.3.1 Problem Statement

The Maximum Consistent Grounded Subgraph problem can be stated as follows: Given a PCGG $G = (V, E \cup E')$, find the maximum CSG $\tilde{G}(\tilde{V}, \tilde{E})$ of G. This problem is denoted by MAX-CON. All the notations have the same meaning as discussed before. The problem can be alternatively stated as the problem of eliminating a minimum number of vertices from G such that the subgraph

induced by the remaining vertices consists of only consistent edges. MAX-CON is an optimization problem and its decision version can be stated as:

MAX-CON

Input: A PCGG $G = (V, E \cup E')$ and a positive integer k s.t. $k \le ||V||$. **Question:** Does *G* contain a CSG of size *k* or more?

5.3.2 Hardness Result

In this section, the computational hardness of the MAX-CON problem is established. More specifically, MAX-CON is shown to be *NP*-complete. This implies that MAX-CON \in *NP* and that the deterministic complexity of MAX-CON is as hard as any other problem in *NP*. Thus, it is highly improbable that MAX-CON will have a deterministic polynomial time solution unless P = NP. This result is proved by a polynomial time many-one reduction from the VERTEX-COVER problem. VERTEX-COVER is a well known *NP*-Complete problem. The vertex cover of an undirected graph is a subset of vertices that contains at least one vertex of every edge in the graph, and the VERTEX-COVER problem (also called minimum vertex cover problem) is to find such a subset of the smallest cardinality. VERTEX-COVER, *NP*-Completeness and polynomial time many-one reductions are explained in the seminal paper by Karp [54]. Before proceeding ahead let us state the decision version of the VERTEX-COVER problem [43].

VERTEX-COVER

Input: A graph $\hat{G} = (\hat{V}, \hat{E})$ and a positive integer k s.t. $k \le ||\hat{V}||$. **Question:** Is there a vertex cover of size $\le k$ for \hat{G} ?

Theorem 5.1. MAX-CON is *NP*-complete.

Proof. It is easy to see that MAX-CON \in NP: Given a graph $G = (V, E \cup E')$, guess a set of vertices

 \tilde{V} (s.t. $\|\tilde{V}\| \ge k$), and check whether the subgraph induced by \tilde{V} consists of only consistent edges (i.e., all the induced edges only belong to the set *E*). This clearly can be done deterministically in polynomial time, provided it can be decided whether an edge is inconsistent or not in polynomial time. Now, to show the hardness of MAX-CON it is required to show that VERTEX-COVER \le_m^p MAX-CON, i.e., VERTEX-COVER many-one (*m*) reduces in polynomial time (*P*) to the MAX-CON problem.

Construction: A polynomial time construction that maps an instance $\hat{G} = (\hat{V}, \hat{E})$ of the VERTEX-COVER problem to an instance $G = (V, E \cup E')$ of the MAX-CON problem is described, such that \hat{G} has a vertex cover of size $\leq k$ ($k \leq ||\hat{V}||$) if and only if G has a CSG of size $\geq ||\hat{V}|| - k$. The construction is shown in Figure 5.3.



Figure 5.3: (a) Input graph for the VERTEX - COVER problem, $\hat{G} = (\hat{V}, \hat{E})$; (b) Input graph for the MAX-CON problem, $G = (V, E \cup E')$

- 1. For each vertex v in the vertex set \hat{V} of \hat{G} , place a vertex v in the vertex set V of G.
- 2. For each edge (u, v) ∈ Ê s.t. u, v ∈ V, add an edge (u, v) in the inconsistent edge set E' of G.
 These edges are shown as dotted lines in Figure 5.3(b).
- 3. For each edge (u, v) ∉ Ê s.t. u, v ∈ V̂, add an edge (u, v) in the consistent edge set E of G.
 These edges are shown as solid lines in Figure 5.3(b).

It is clear that the above construction can be completed in polynomial time. Let us now show that the graph \hat{G} has a vertex cover of size *k* if and only if the graph *G* has a CSG of size $\|\hat{V}\| - k$.

Suppose the graph \hat{G} in Figure 5.3 has a vertex cover C ($C \subseteq \hat{V}$) of size k (||C|| = k). Since C is a vertex cover, $\forall (u, v) \in \hat{E}$, either u or v or both are in C. By our construction, $\forall (u, v) \in \hat{E}$, $(u, v) \in E'$ (inconsistent edge set). In other words, C also covers all the inconsistent edges in G. In other words, $\hat{V} - C$ is a CSG. $||\hat{V} - C|| = ||\hat{V}|| - k$. Thus, if \hat{G} has a vertex cover of size k, G has a CSG of size $||\hat{V}|| - k$.

Now, let us prove the other direction. Let *C* be the CSG of *G* of size $m (m \le ||V||)$. By definition of CSG, *C* contains only consistent edges, i.e., for all edges (u, v) in *C*, $(u, v) \in E$. Thus, V - Ccovers all edges in the inconsistent edge set *E'*. If this was not true, then there is an edge $(u, v) \in E'$ s.t. both *u* and *v* are not in V - C. Thus, both *u* and *v* are in *C* and it is not a CSG which is a contradiction. Thus, V - C covers all inconsistent edges. From our construction, V - C is a vertex cover of the graph \hat{G} (there is a one-one mapping of edges in \hat{G} to inconsistent edges in *G*) and its size is ||V|| - m, i.e., $||\hat{V}|| - m$ since $||V|| = ||\hat{V}||$.

Thus, VERTEX-COVER many-one reduces in polynomial time to MAX-CON. Since VERTEX-COVER is *NP*-complete, MAX-CON is *NP*-complete.

5.3.3 Approximation Algorithm

Before outlining an algorithm for solving MAX-CON, another result that gives the relationship between the VERTEX-COVER problem and the MAX-CON problem is required.

Theorem 5.2. MAX-CON many-one reduces in polynomial time (\leq_m^P) to the VERTEX-COVER Problem.

Proof. The proof of this lemma has a construction very similar to the one in Theorem 5.1. This construction maps an instance $G = (V, E \cup E')$ of the MAX-CON problem to an instance $\hat{G} = (\hat{V}, \hat{E})$ of the VERTEX-COVER problem in polynomial time such that *G* has a CSG of size $k \ (k \le ||V||)$ if and only if \hat{G} has a vertex cover of size ||V|| - k.

1. For each vertex v in the vertex set V of PCGG G, place a vertex v in the vertex set \hat{V} of \hat{G} .

2. For each inconsistent edge $(u, v) \in E'$, add an edge (u, v) in the edge set \hat{E} of \hat{G} . These edges are shown as dotted lines in Figure 5.4(a) and as solid lines in Figure 5.4(b).



Figure 5.4: (a) Input graph for the MAX-CON problem, $G = (V, E \cup E')$; (b) Input graph for the VERTEX-COVER problem, $\hat{G} = (\hat{V}, \hat{E})$

It is clear that the above construction can be completed in polynomial time. Now, let us show that G has a CSG of size k (for any $k \le ||V||$) if and only if \hat{G} has a vertex cover of size $||\hat{V}|| - k$.

Suppose *G* has a CSG *C* of size *k*. This implies that *C* contains only consistent edges, i.e., edges from the edge set *E*. Thus, V - C contains all the inconsistent edges (from *E'*) and the remaining consistent edges (from *E*). Also, ||V - C|| = ||V|| - k. By our construction $\hat{E} = E'$ and $\hat{V} = V$. Thus V - C covers all edges in \hat{E} and is a vertex cover of size ||V|| - k. Similarly, the other direction.

Let $OPT_{MAX-CON}$ be the optimal value of the maximum consistent graph for a PCGG $G = (V, E \cup E')$ and let $OPT_{VERTEX-COVER}$ be the optimal value of the minimum vertex cover for the corresponding instance of the VERTEX-COVER problem $\hat{G} = (\hat{V}, \hat{E})$ (constructed from *G*), as shown in Theorem 5.2 above. From this construction, it can also be observed that $V \equiv \hat{V}$. Then, the relationship between $OPT_{MAX-CON}$ and $OPT_{VERTEX-COVER}$ can be given by a corollary to the Theorem 5.2, as shown below.

Corollary 5.3. $OPT_{MAX-CON} = |V| - OPT_{VERTEX-COVER}$.

Theorem 5.2 implies that any efficient algorithm for solving the VERTEX-COVER problem can be used to solve the MAX-CON problem. Thus, the approximation algorithm for MAX-CON can be outlined as shown in Algorithm 5 below.

```
1: \hat{E} \leftarrow E' {place all inconsistent edges in \hat{E} }
2: for all edge (u, v) \in E' do
       if u \notin \hat{V} then
3:
          \hat{V} \leftarrow u {and corresponding vertices in V}
4:
       end if
 5:
       if v \notin \hat{V} then
6:
           \hat{V} \leftarrow v
7:
       end if
8.
9: end for
10: C = A(\hat{V}, \hat{E}) {execute approx algorithm for VERTEX-COVER}
11: Return V - C {solution of MAX-CON}
```

Algorithm 5: Calculating the Maximum CSG of the PCGG $G = (V, E \cup E')$

Let, $A(\hat{V}, \hat{E})$ be an algorithm for solving the VERTEX-COVER problem, where \hat{V} and \hat{E} are the set of vertices and edges respectively of the input graph \hat{G} . Algorithm *A* returns the set of vertices that form the minimum vertex cover for the graph \hat{G} . The approximation algorithm for MAX-CON is very straightforward. It first constructs an instance $\hat{G}(\hat{V}, \hat{E})$ of the VERTEX-COVER problem from an instance $G = (V, E \cup E')$ of the MAX-CON problem. It then uses the approximation algorithm *A* for the VERTEX-COVER problem as a subroutine to find the vertex cover *C* for \hat{G} . From Theorem 5.2, the CSG of *G* is nothing but V - C.

The *for* loop in Algorithm 5 runs no more than $\binom{||V||}{r}$ times. Also, the running time and solution quality of Algorithm 5 are bounded by the running time and solution quality respectively of the approximation algorithm *A* for solving the VERTEX-COVER problem. The minimum VERTEX-COVER problem is a fundamental and a highly researched problem in graph theory and combinatorial optimization with a large number of constant and fixed ratio approximation algorithms. Hastad [38] showed that VERTEX-COVER cannot be approximated within a factor of 7/6. It was further improved to $10\sqrt{5}-21$ by Dinur et al. [22]. Gavril introduced a 2-approximation algorithm

for the VERTEX-COVER problem [29]. This was further improved to $2 - \frac{\log \log|V|}{2\log|V|}$ by Bar-Yehuda et al. [7,67] and later to $2 - \frac{\ln \ln|V|}{\ln|V|}(1 - o(1))$ by Halperin [34], before it was eventually improved to $2 - \Theta(\frac{1}{\sqrt{\log n}})$ by Karakostas [52]. An interesting generalization of the VERTEX-COVER problem is the weighted VERTEX-COVER problem in which positive weights are assigned to each vertex and the problem is to find the vertex cover with minimum cumulative weight. The first well-known 2-approximation algorithm for the weighted VERTEX-COVER problem was discovered independently by Bar-Yehuda et al. [6] and Hochbaum [41]. An important point to note here is that all the approximation results for the unweighted case also hold for the weighted case.

Let A'(G) be a subroutine for solving the MAX-CON problem. Also, let the size of the vertex set |V| be *n*. Now, if $A(\hat{G})$ is a subroutine for the VERTEX-COVER problem with an approximation ratio α ($\alpha > 1$) that is invoked by *A* then the relationship between the approximation ratio of MAX-CON and VERTEX-COVER can be given by Lemma 5.4, as outlined below.

Lemma 5.4. The approximation ratio for MAX-CON is bounded by $\frac{n-\alpha|A|}{|A'|}$.

Proof. The proof for this lemma is straightforward. Let β be the approximation ratio for the subroutine *A* for solving MAX-CON. Then, β can be given as,

$$\beta = \frac{OPT_{MAX-CON}}{|A'|}$$

Similarly, α can be given as,

$$\alpha = \frac{OPT_{VERTEX-COVER}}{|A|}$$

From Corollary 5.3,

$$\beta = \frac{n - OPT_{VERTEX-COVER}}{|A'|} = \frac{n - \alpha . |A|}{|A'|}$$

Next, the optimization problem for obtaining the largest CSG from a PCGG is formulated and

its combinatorial properties studied.

5.4 Largest Consistent Grounded Subgraph

5.4.1 Problem Statement

The Largest Consistent Grounded Subgraph problem, denoted as LARGEST-CON, is the problem of finding the largest CSG (Definition 5.5) of a PCGG $G = (V, E \cup E')$. The problem can be alternatively stated as the problem of eliminating vertices from *G* such that the subgraph induced by the remaining vertices consists of only consistent edges and the cardinality of these consistent edges is maximized. From Figure 5.2, we can clearly see that an optimal solution for MAX-CON is not necessarily an optimal solution for LARGEST-CON. These two are different problems with different combinatorial properties and solutions. The decision version of the LARGEST-CON problem can be stated as:

LARGEST-CON

Input: A PCGG $G = (V, E \cup E')$ and a positive integer k s.t. $k \le ||E||$. **Question:** Does *G* contain a CSG of edge size k or more?

5.4.2 Hardness Result

In this section, the combinatorial hardness of the LARGEST-CON problem is proved. Specifically, it is shown that LARGEST-CON is *NP*-Complete, i.e., LARGEST-CON \in *NP* and the deterministic complexity of LARGEST-CON is as hard as any other problem in *NP*. Thus, it is highly improbably that LARGEST-CON will have a deterministic polynomial time solution. This result is proved by a polynomial time many-one reduction from the MAX-2SAT or Maximum 2-Satisfiability problem. MAX-2SAT is a well known *NP*-Complete problem [29]. MAX-2SAT is a restricted version of a related *NP*-Complete problem called the MAX-SAT or Maximum Satisfiability problem. MAX-SAT is the problem, given a set S of disjunctive form clauses, to find a truth assignment to the literals such that maximum number of clauses are satisfied [29]. MAX-2SAT is restricted to at most two literals per clause. It can be formally stated as:

MAX-2SAT

Input: A Conjunctive Normal Form (CNF) formula *F* on Boolean variables $x_1, x_2, ..., x_n$ and *m* clauses $C_1, C_2, ..., C_m$, each containing at most two literals, where each literal is either Boolean variable x_i or its negation \bar{x}_i ($\neg x_i$) and a positive integer *k* (k < m).

Question: Is there a truth assignment to the variables that satisfies k or more clauses?

Theorem 5.5. LARGEST-CON is NP-Complete.

Proof. A technique identical to the polynomial time reduction from 3-SAT which was used to prove the *NP*-Completeness of the VERTEX-COVER problem [43] is applied here to prove the above result.

It is easy to see that LARGEST-CON $\in NP$: Given a graph $G = (V, E \cup E')$, guess a set of consistent edges \tilde{E} (s.t. $||\tilde{E}|| \ge k$ and $\tilde{E} \subseteq E$). Let \tilde{V} be the set of vertices of all these guessed edges. Check in polynomial time whether the other edges induced by \tilde{V} are consistent. This procedure clearly can be accomplished in polynomial time and thus LARGEST-CON $\in NP$. Now, it needs to be shown that MAX-2SAT \le_m^P LARGEST-CON, i.e., MAX-2SAT many-one reduces in polynomial time to LARGEST-CON. Since MAX-2SAT is *NP*-Complete, it can be claimed that LARGEST-CON is *NP*-Complete.

Construction of an instance of LARGEST-CON, G = (V, EUE'): A polynomial time construction that maps an instance F of MAX-2SAT to an instance G = (V, EUE') of the LARGEST-CON problem is described such that F satisfies k clauses if and only if G has a CSG of edge size k. Figure 5.5 shows the construction of a PCGG $G = (V, E \cup E')$ from the MAX-2SAT formula $F = (x_1 \lor x_2) \land (x_2 \lor x_3) \land (x_1 \lor \bar{x_3}) \land (\bar{x_1} \lor \bar{x_2})$. The consistent edges are shown as solid lines and the inconsistent edges are shown as dotted lines.



Figure 5.5: Construction of a PCGG $G = (V, E \cup E')$ from the MAX-2SAT formula $F = (x_1 \lor x_2) \land (x_2 \lor x_3) \land (x_1 \lor \bar{x_3}) \land (\bar{x_1} \lor \bar{x_2})$

The construction of *G* consists of the following 3 steps, each adds a different component to the graph.

- Let U = VAR(F), be the set of variables in the Boolean formula F. For each variable u_i ∈ U, put u_i and ū_i in the vertex set V and put (u_i, ū_i) into the edge set E', i.e., the set of inconsistent edges in graph G. This is the first component of the graph.
- 2. Let C = CLAUSE(F) be the set of clauses in F, i.e., $F = \bigwedge_{c_j \in C} c_j$. For each clause c_j in the formula F put vertices c_j^1 and c_j^2 in V. Put an edge (c_j^1, c_j^2) in the set E', i.e., the set of inconsistent edges. This is the second component of the graph G.
- 3. In this step we create a new component by connecting components from the first two steps. This component depends on the literals that are contained in the clauses. As mentioned before, each clause $c_j \in C$ is a disjunction of two literals and literals are variables or their negations. Consider one such clause $c_j = (x_j \vee y_j)$, where x_j and y_j are literals. For each clause c_j , put edges (x_j, c_j^1) and (y_j, c_j^2) in E, i.e., the set of consistent edges of G. This forms the third set of components of the graph G.

It is now required to show that the PCGG G (as constructed above) has a CSG $\tilde{G} = (\tilde{V}, \tilde{E})$ of edge size k, i.e., $\|\tilde{E}\| = k$ if and only if F has k satisfiable clauses. Suppose, there exists an

assignment *t* s.t. exactly *k* clauses are satisfied. Then for each variable $u_i \in U$ either $t(u_i) = 1$ or $t(\bar{u}_i) = 1$ but both cannot be 1. Place u_i in the vertex set \tilde{V} of the subgraph \tilde{G} of the PCGG *G* if $t(u_i) = 1$ or place \bar{u}_i in \tilde{V} if $t(\bar{u}_i) = 1$. Thus, \tilde{V} contains one vertex of each edge in the first component. Now, for a clause $c_j = (x_j \vee y_j)$, c_j is satisfiable if either literals x_j or y_j or both are true. Thus, either x_j or y_j or both are in the set \tilde{V} based on their truth assignment. If both x_j and y_j are in \tilde{V} , randomly (with a probability 1/2) select vertex c_j^1 or c_j^2 and add it to \tilde{V} (never both). If only one of x_j or y_j is 1, pick the corresponding c_j^i (based on the construction of component 3) and place it \tilde{V} . One thing to note here is that when the clause c_j is satisfied, only one c_j^1 or c_j^2 is in the set \tilde{V} . When it is not satisfied, none of them are in \tilde{V} . It follows that the vertex set \tilde{V} induces edges only from the consistent edge set E of the PCGG G. Thus, the graph induced by \tilde{V} is consistent and $\tilde{G} = (\tilde{V}, \tilde{E})$ is a CSG. Also from the above procedure, if k clauses are satisfied then exactly kconsistent edges get induced in \tilde{E} . As a result, $\tilde{G} = (\tilde{V}, \tilde{E})$ is a CSG with edge size k. Now, let us prove the other direction.

Suppose, $\tilde{G} = (\tilde{V}, \tilde{E})$ is a CSG of the PCGG *G* s.t. $\|\tilde{E}\| = k$, for some positive integer *k*. From the above construction, it is clear that all the consistent edges are of the form (u_i, c_j^i) , where u_i is the *i*th $(i \in 1, 2)$ literal in the *j*th clause c_j of the formula *F*. Also, if $u_i \in \{x_i, \bar{x}_i\}$, since the graph \tilde{G} is a CSG, the edges of the form (x_i, \bar{x}_i) and (c_j^1, c_j^2) cannot be in \tilde{E} , i.e., both x_i and \bar{x}_i or c_j^1 and c_j^2 cannot be in the vertex set \tilde{V} of the CSG \tilde{G} . Now, define an assignment $t : U \to \{0, 1\}$ s.t. $t(u_i) = 1$ if $u_i \in \tilde{V}$ and $t(u_i) = 0$ if $u_i \notin \tilde{V}$. Similarly, $t(\bar{u}_i) = 1$ if $\bar{u}_i \in \tilde{V}$ and $t(\bar{u}_i) = 0$ if $\bar{u}_i \notin \tilde{V}$. It can be claimed that this assignment is consistent. Moreover, if there are *k* edges in \tilde{E} then there are *k* satisfied clauses by the above assignment. Since \tilde{G} is a CSG of the PCGG *G*, none of the edges in the first two components of our construction can be present in \tilde{G} . Thus, for any variable x_i , both x_i and \bar{x}_i cannot be in \tilde{V} . As a result, the assignment *t* above will consistent. Similarly, for a clause c_i , both c_i^1 and c_i^2 cannot be in \tilde{V} . Thus, both edges in the third component in the construction above of the form (u, c_j^1) and (v, c_j^2) cannot be in \tilde{G} at the same time, where *u* and *v* are some literals. If this was not true, (c_j^1, c_j^2) would also be induced in \tilde{G} making it inconsistent. Thus, there is a one-one correspondence between an edge in \tilde{G} and the corresponding satisfied clause and since all these edges span distinct clauses there are exactly k satisfied clauses.

The next lemma gives the relationship between the solutions for the MAX-CON and the LARGEST-CON problem.

Lemma 5.6. Let $OPT_{LAR}(G)$ and $OPT_{MAX}(G)$ be the optimal solutions of the LARGEST-CON and MAX-CON problems respectively on any input PCGG $G(V, E \cup E')$. Let LAR(G) and MAX(G) be the set of all the feasible solutions for the LARGEST-CON and MAX-CON problems respectively on G. Then,

- 1. $cost(OPT_{LAR}(G)) \leq cost(OPT_{MAX}(G))$ i.e., $||OPT_{LAR}(G)|| \leq ||OPT_{MAX}(G)||$
- 2. LAR(G) = MAX(G)
- 3. Let A ∈ LAR(G) (MAX(G)) and B ∈ LAR(G) (MAX(G)) s.t. C = A ∩ B and C ≠ φ. Then,
 A ∪ B ∉ LAR(x) (MAX(x)) ⇒ ∃u ∈ A − C and ∃v ∈ B − C s.t. (u, v) ∈ E', i.e., in the set of inconsistent edges of G
- *Proof.* 1. Assume that there exists a PCGG such that the inequality 1 above is not true. This means that there exists an optimal solution of LARGEST-CON that has more vertices than an optimal solution for MAX-CON. But, then the solution for MAX-CON is not a maximum CSG, thus not optimal, and that is a contradiction. Therefore, no such PCGG exists.
 - 2. The proof of this point is trivial and follows directly from the definitions of MAX-CON and LARGEST-CON.
 - 3. Since A and B are both feasible solutions, there are no two vertices u and v both in A s.t. (u, v) is inconsistent. Similarly, there are no such vertices in either B or C. Also, since $A \cup B$ is not a feasible solution which implies that there exists two vertices $u, v \in (A \cup B)$ such that (u, v) is inconsistent. The above two points imply that $\exists u \in A$ and $v \in B$ s.t. (u, v) is inconsistent.

Next, the inapproximability result for LARGEST-CON is presented.

5.4.3 Inapproximability Result

Before proving the inapproximability result for LARGEST-CON, let's introduce another hard problem called CLIQUE. In graph theory, a clique in an undirected graph is a set of vertices such that for every two vertices in this set, there exists an edge in the graph connecting the two. CLIQUE was one of the first problems shown to be *NP*-Complete [9]. The decision version of CLIQUE can be stated as [43]:

CLIQUE

Input: A graph $\hat{G} = (\hat{V}, \hat{E})$ and a positive integer $j \le ||\hat{V}||$.

Question: Does \hat{G} contain a clique of size *j* or more?

Bomze et al. [9] have proved important combinatorial results for the CLIQUE problem. In summary, they showed that CLIQUE does not have a polynomial time approximation algorithm unless P = NP. In other words, there is strong evidence that CLIQUE cannot be approximated with any ratio less than 1.

Theorem 5.7. If there exists an approximation algorithm that can approximate LARGEST-CON with an approximation ratio ε ($\varepsilon > 0$) then there exists an algorithm that approximates CLIQUE with ratio $1 - \sqrt{\frac{1-\varepsilon}{2}}$.

Proof. Suppose the graph $\hat{G} = (\hat{V}, \hat{E})$ is an instance of CLIQUE. A new graph $G = (\hat{V}, E)$ can be constructed such that the new graph G has the same vertex set as \hat{G} and $E = \hat{E} \cup E^c$ where E^c contains all the edges that are not in \hat{E} (in the complete graph induced by the vertex set \hat{V}). Now, if \hat{E} is taken to be the set of consistent edges and E^c to be the set of inconsistent edges then G is a PCGG. Also, it is easy to see that any CLIQUE in graph \hat{G} corresponds to a CSG in G and vice

versa. Let *A* be the ε -approximation algorithm for solving the LARGEST-CON problem. Apply *A* on the graph *G* to get the largest CSG in *G*. Let this largest CSG be $\tilde{G} = (\tilde{V}, \tilde{E})$. Also, let $|\tilde{V}| = m$ and *M* be the vertex cardinality of the optimal solution.

Since A has an approximation ratio ε , we have

$$\left| \frac{\binom{M}{2} - \binom{m}{2}}{\binom{M}{2}} \right| = \frac{M^2 - M - m^2 + m}{M^2 - M} \le \varepsilon$$

Then,

$$1 - \varepsilon \le \frac{m^2 - m}{M^2 - M} < \frac{m^2}{M^2 - M}$$

Without loss of generality we can assume $M \ge 2$. Then,

$$1 - \varepsilon < 2\left(\frac{m}{M}\right)^2$$
 which is, $\frac{M-m}{M} < 1 - \sqrt{\frac{1-\varepsilon}{2}}$

This means that an approximation algorithm for CLIQUE with ratio $1 - \sqrt{\frac{1-\varepsilon}{2}}$ has been found.

The inapproximability of LARGEST-CON can be expressed as a corollary of Theorem 5.7.

Corollary 5.8. Unless P = NP, the approximation threshold of LARGEST-CON is 1.

Proof. This directly follows from the fact that CLIQUE cannot be approximated with any ratio less than 1 under the hypothesis $P \neq NP$.

Corollary 5.8 implies that LARGEST-CON cannot be approximated with any ratio less than 1 under the hypothesis $P \neq NP$. The next section presents two solution strategies for the LARGEST-CON problem based on popular heuristics.

5.5 Heuristics for LARGEST-CON

Heuristics like greedy choice and local solution search have been used in the design of solution strategies for the LARGEST-CON problem. Experimental results, discussed later in Section 5.6, have found that both the strategies work reasonably well for randomly generated connected graphs. But, an exact theoretical bound on the solution quality of these algorithms is not known and is still an open question.

5.5.1 Greedy Algorithm

Let the PCGG $G = (V, E \cup E')$ be an instance of LARGEST-CON, where *E* and *E'* are the sets of consistent and inconsistent edges respectively. For a vertex $v \in V$, let con(v) be the number of consistent edges of *v* and let incon(v) be the number of inconsistent edges of *v*. In other words, con(v) is the consistent edge degree of the vertex *v* while incon(v) is the inconsistent edge degree of *v*. The basic idea of the greedy algorithm is to eliminate all the inconsistent edges of *G* by greedily selecting inconsistent vertices (vertices with inconsistent edge degree at least one) that are connected to lowest number of consistent edges. The greedy approach for obtaining the largest CSG is shown in Algorithm 6.

```
1: C \leftarrow \phi; {Initialize the solution to empty set}

2: C = \{v | v \in V' \text{ and } incon(v) = 0\}

3: V' \leftarrow V' \setminus C;

4: while E'' \neq \phi do

5: pick a vertex v \in V' of minimum con(v);

6: V' \leftarrow V' \setminus \{v\}

7: E'' \leftarrow E'' \setminus \{e | v \in e\}

8: end while

9: C \leftarrow C + V';

10: Return C {solution of LARGEST-CON}
```

Algorithm 6: Greedy Algorithm

The greedy approach, as discussed above, first removes from consideration all vertices that are only connected to consistent edges. Then in each iteration, it randomly selects a vertex for elimination with inconsistent degree at least one and lowest consistent edge degree. The algorithm continues this until all the inconsistent edges are eliminated and the graph *G* contains only consistent edges. The greedy approach is pretty straightforward, with a running time bounded by the execution of the while loop, which is $O(n^2)$, where |V| = n. One problem with this greedy strategy is that the decision to select a particular vertex for elimination at each step is solely based on the consistent edge degree of the vertex (i.e., the number of consistent edges lost from the final CSG). This may not always be a good decision as there might be another vertex connected to the same number of consistent edges but more number of inconsistent edges. Thus, selecting this vertex at that particular step would be much more efficient. The above greedy algorithm can be modified slightly by using an alternative heuristic and is outlined in Algorithm 7 below.

1: $C \leftarrow \phi$; {Initialize the solution to empty set} 2: $C = \{v | v \in V' \text{ and } incon(v) = 0\}$ 3: $V' \leftarrow V' \setminus C$; 4: while $E'' \neq \phi$ do 5: pick a vertex $v \in V'$ of minimum $\frac{con(v)}{incon(v)}$; 6: $V' \leftarrow V' \setminus \{v\}$ 7: $E'' \leftarrow E'' \setminus \{e | v \in e\}$ 8: end while 9: $C \leftarrow C + V'$; 10: Return *C* {solution of LARGEST-CON}

Algorithm 7: Modified Greedy Algorithm

According to the modified greedy heuristic, in each iteration of the algorithm, a vertex v with the lowest ratio of consistent to inconsistent edge degree $\left(\frac{con(v)}{incon(v)}\right)$ is selected for elimination. The running time of the modified greedy algorithm is also $O(n^2)$ where |V| = n. The greedy heuristic is experimentally evaluated in Section 5.6. Next, an algorithm for LARGEST-CON based on the neighborhood search strategy is proposed.

5.5.2 Local Solution Search

Local Solution Search (LSS) is a popular algorithm design technique for optimization problems. Before giving details on this technique, let's introduce a few important concepts. Let U be an optimization problem and x be an input problem instance for U. Let M(x) be the set of feasible solutions of the problem U for the input instance x.

Definition 5.6. Neighborhood: For an optimization problem U and for every input instance x, a neighborhood on the set of feasible solutions (M(x)) is any mapping $f_x : M(x) \to Pot(M(x))$ (*Pot* denotes the power set) such that

- 1. $\alpha \in f_x(\alpha)$ for every $\alpha \in M(x)$,
- 2. if $\beta \in f_x(\alpha)$ for some $\alpha \in M(x)$, then $\alpha \in f_x(\beta)$, and
- 3. for all $\alpha, \beta \in M(x)$ there exists a positive integer k and $\gamma_1, \ldots, \gamma_k \in M(x)$ such that $\gamma_1 \in f_x(\alpha)$, $\gamma_{i+1} \in f_x(\gamma_i)$ for $i = 1, \ldots, k - 1$, and $\beta \in f_x(\gamma_k)$

If $\alpha \in f_x(\beta)$ for some $\alpha, \beta \in M(x)$, then α and β are said to be neighbors in M(x). The set $f_x(\alpha)$ is called the neighborhood of the feasible solution α in M(x) [44].

Now, let's introduce the concept of local optima.

Definition 5.7. Let *U* be an optimization problem and for every input instance *x* of the problem let f_x be the neighborhood function on M(x). Let *cost* be the cost function that assigns a positive real number to each feasible solution. A feasible solution $\alpha \in M(x)$ is a local optima for the input instance *x* of *U* according to f_x , if

$$cost(\alpha) = (max) or (min) \{cost(\beta) | \beta \in f_x(\alpha) \}$$

Denote the set of all local optima for x according to the neighborhood f_x by $LocOPT_U(x, f_x)$ [44].

Neighborhood Definition for LARGEST-CON: The formalisms of functions and relations does not work when introducing neighborhoods on M(x) in practical problems like LARGEST-CON. The standard way to introduce a neighborhood on M(x) is to use a so-called *local transformation* on M(x). Informally, a local transformation transforms a feasible solution α to a feasible solution β by some local changes of the specification of α . To define a neighborhood for an instance of the LARGEST-CON problem, a transformation called a *n*-neighborhood transformation is introduced. For simplicity, let us first introduce a *1*-neighborhood transformation. Let $x = G(V, E \cup E')$ be an instance of the LARGEST-CON problem. Let M(x) be the set of feasible solutions for LARGEST-CON on input *x*. For $\alpha \in M(x)$, the 1-neighborhood of α is defined as follows:

To define a 1-neighbor of a feasible solution α , pick a vertex $v \in V \setminus \alpha$ s.t. v has an inconsistent edge degree of exactly one and this inconsistent edge connects v to a vertex in α . Let this vertex in α to which v connects be called w. If there are no such vertex w in α then α has no 1-neighbors. Now to get a 1-neighbor of α , add v in α and remove w from α . It is clear that this resultant subgraph is also a feasible solution since the inconsistent edge which was covered by v previously is now covered by w. Also, addition of v does not induce any inconsistent edge in the resultant subgraph since its inconsistent edge degree is one and that edge is now covered by w. Such a subgraph is called the *1-neighbor* of the solution α . The set of all the 1-neighbors of α is called the 1-neighborhood of α and is represented as $Neigh_x^1(\alpha)$. Similarly, to define a 2-neighborhood, a vertex $v \in V \setminus \alpha$ with inconsistent edge degree of exactly two (to vertices in α) is selected. This vertex is added in α and the two vertices that v connects by inconsistent edges are removed from α . One thing to note here is that 1-neighbors of α have the same vertex set cardinality as α while its 2-neighbors have their vertex set cardinality reduced by 1. Similarly 3-neighborhoods are defined.

Local Solution Search Algorithm for LARGEST-CON: A Local Search Solution or LSS algorithm starts off with an initial solution and then continually tries to find a better solution by searching neighborhoods of that solution. If there is no better solution in the neighborhood, then it stops. By having a structure on the set of feasible solutions M(x), determined by a neighborhood $Neigh_x$, for every input instance x of an optimization problem U, one can describe a general scheme of local search as shown in Algorithm 8.

The success of the local search algorithm depends on the choice of the neighborhood. If a neighborhood $Neigh_x$ has a property such that $Neigh_x(\alpha)$ has a small cardinality for every 1: Find a feasible solution $\alpha \in M(x)$

- 2: while $\alpha \notin LocOPT_U(x, Neigh_x)$ do
- 3: find a $\beta \in Neigh_x(\alpha)$ such that $cost(\beta) < cost(\alpha)$ if U is a minimization problem or $cost(\beta) > cost(\alpha)$ if U is a maximization problem;
- 4: If such a β is found, $\alpha = \beta$;
- 5: end while
- 6: Return α

Algorithm 8: Local Search Scheme according to a neighborhood Neigh

 $\alpha \in M(x)$, then one iterative improvement of the while loop of Algorithm 8 can be executed efficiently, but the risk that there are many local optima (potentially with a cost that is very far from the optimal solution) can substantially grow. On the other hand, large $|Neigh_x(\alpha)|$ can lead to feasible solutions with costs that are closer to the optimal solution than smaller neighborhoods can, but the complexity of the execution of one run of the while cycle can increase too much. Besides the choice of the neighborhood, there are two other factors that affect the execution of the local search algorithm. The first factor is the method by which the initial feasible solution is computed. The choice of the initial solution can essentially influence the quality of the resultant local optimum. The initial feasible solution can be either chosen randomly for problems in which the structure of the feasible solution is simple or it can be precomputed. In the LSS algorithm for LARGEST-CON, the initial feasible solution is precomputed. From Lemma 5.6, it is clear that a solution for the MAX-CON problem is also a solution for the LARGEST-CON problem. Thus, any algorithm that produces an optimal solution for MAX-CON can be used as a good starting solution for the LARGEST-CON problem. Further improvement can be done by starting the LSS algorithm with multiple initial feasible solutions. The second factor affecting the performance of the LSS algorithm is the way in which a cost-improving feasible solution is selected inside the while loop. There are two strategies in doing this, namely, the *First Improvement Strategy* and the Best Improvement Strategy. In the first improvement strategy, the current feasible solution is replaced by the first cost-improving feasible solution found by the neighborhood search. The best improvement strategy replaces the current feasible solution by the best feasible solution in the neighborhood. A LSS for solving LARGEST-CON is outlined in Algorithm 9.

- 1: Let $x = G(V, E \cup E')$ be a PCGG and an instance of LARGEST-CON and let *A* be an efficient algorithm for solving MAX-CON.
- 2: Let $\alpha = A(x)$ be the initial feasible solution.
- 3: while $\alpha \notin LocOPT_U(x, Neigh_x^1(\alpha))$ do
- 4: Either by first improvement or best improvement, find a $\beta \in Neigh_x^1(\alpha)$ such that $cost(\beta) > cost(\alpha)$ {cost function outputs the edge count (consistent) of a solution}
- 5: If such a β is found, $\alpha = \beta$;
- 6: end while
- 7: Return α

Algorithm 9: Local Search Scheme for LARGEST-CON using $Neigh_r^1$

One shortcoming of the approach outlined in Algorithm 9 is that in each iteration of the while loop only the 1-neighborhoods ($Neigh_x^1$) of the feasible solution α is checked. But, α might not have 1-neighborhoods at all or there might be better solutions in the 2-neighborhoods and 3-neighborhoods. Thus, the above algorithm can be further improved by also checking the 2neighborhoods and 3-neighborhoods of the feasible solution in each loop. The local search algorithm is also experimentally evaluated next (Section 5.6) and its solution quality is compared with that of the greedy heuristic.

5.6 Experimental Evaluation

The greedy and local solution search algorithms for the LARGEST-CON problem are experimentally evaluated by implementing these algorithms using C++ programs and executing them on an Intel® Pentium® 4 processor-based computer system. The results from the current set of experiments are useful in understanding the behavior of these algorithms (in terms of the solution quality) under various network topologies, specifically when the density of the input PCGG increases. A comparative analysis of the solution quality of the two heuristic-based algorithms is performed in order to determine if one algorithm clearly performs better than the other. The details of the experimental setup are described next.

5.6.1 Experimental Setup

In the current set of experiments, the heuristics for LARGEST-CON proposed in Section 5.5 are tested on *Random Graphs*. Random graphs are graphs without any specific topology or physical characteristics and are generated in the following way: All vertices in the graph represent the nodes in the sensor network that are randomly distributed in a $500m \times 500m$ region. Each node has a radio range *R*. If the distance between two nodes is less than or equal to the radio range *R* (all nodes are assumed to have the same radio range) then the two corresponding vertices are connected by an edge in the graph.

The number of nodes (n) and the radio range (R) are adjustable parameters in this simulation. Without loss of generality, currently only one third of the total number of nodes are randomly selected to be malicious. But, this is an experimental parameter and can be modified accordingly in order to observe the efficiency of the proposed algorithms for more number of cheating nodes. For any edge between a malicious node and an honest node (or another malicious node), it is assigned to be inconsistent with a probability of 1/2. This is because, as mentioned earlier, malicious behavior is random and that malicious node may not cheat all the time. All other edges between honest nodes are always consistent. It is obvious that if all the malicious nodes and the corresponding edges are removed then the resulting subgraph becomes consistent. This subgraph may or may not be the optimal solution. Such a subgraph is called a *sub-optimal solution*. Since it is computationally infeasible to get the true optimal solution for large graphs, the solution quality of the algorithms is measured as the ratio of the number of consistent edges in the CSG output by the algorithm to the number of consistent edges in the sub-optimal solution.

5.6.2 **Results and Evaluation**

The two variants of the greedy algorithm (greedy approach and modified greedy approach) and the two variants of local search algorithms (first improvement strategy and best improvement strategy)

are tested with some fixed values for n and R. It is observed that the performance difference between the two greedy algorithms is negligible. For this reason only one indicative data curve for the greedy algorithms is included here. Similarly, the performance difference of the two variants of the local search algorithms is also negligible and as a result only one indicative data curve for the local search algorithms is included here. All data values are obtained as the average over 100 runs. Figure 5.6(a), 5.6(b) and 5.6(c) plots the solution quality of the algorithms against the radio range of the nodes with n = 80, n = 100 and n = 120 respectively. The radio range is plotted along the X-axis and the solution quality is plotted along the Y-axis.

The following observations can be made from the plots in Figure 5.6:

- 1. None of the algorithms return a solution that is better than the sub-optimal solution.
- 2. The performance or solution quality of both the algorithms decreases as the number of nodes increases.
- 3. Also, the performance or solution quality of both the algorithms decreases as the radio range increases (i.e., the graph becomes more dense), and the solution quality stabilizes after the radio range reaches some threshold value.
- 4. In summary, the local search algorithm has some improvement over the greedy algorithm, but the improvement is not significant. Moreover, the solution quality does not deteriorate below 0.4 and that the average solution quality for all cases is close to 0.5 for both the algorithms.

Despite the negative inapproximability result for LARGEST-CON, it can be observed that both the greedy and local search algorithms produce good solutions and the solution quality is close to 0.5 even for large, highly dense graphs. These results are encouraging.



Figure 5.6: Plot of solution quality versus radio range for a network with (a) 80 Nodes; (b) 100 Nodes; (c) 120 Nodes

5.7 Further Improvements

Although the greedy and local solution search algorithms have been experimentally shown to provide solution qualities close to 0.5, there are still some issues with these simple heuristics. For example, the local solution search algorithm may get stuck in a poor local optima for some choice of an initial feasible solution. Similarly, depending on the choice of the first vertex selected for elimination, the greedy strategy may or may not be able to produce a good solution. In order to overcome these problems, two other optimization strategies have been proposed in this section. The simulated annealing algorithm, as discussed next, overcomes the poor local optima problem by accepting a deterioration in the hope of producing an overall better solution. Following this algorithm, the Linear Programming (LP) formulation of the LARGEST-CON problem is outlined where an optimal solution is the one that satisfies all the constraints and maximizes a cost function.

5.7.1 Simulated Annealing

One problem with the local solution search or LSS algorithm discussed in Section 5.5.2 is that there may be instances of LARGEST-CON for which the local search algorithm can get stuck in an arbitrary poor local optima. One approach to overcome this problem is to start the local search algorithm several times with different randomly chosen initial solutions. Another approach, called the simulated annealing, is to add the possibility of leaving a local optimum to move to a weaker solution (deterioration) by some kind of coin tossing (random probability) in order to find better solutions. This approach is motivated from the annealing process which is used to obtain low energy states of a solid in a heat bath. In this approach, the probability of accepting a deterioration in the iterative process depends on the size of the deterioration as well as the number of iterations executed up till now. The simulated annealing approach for the LARGEST-CON problem is outlined in Algorithm 10.

There are two main free parameters in the simulated annealing algorithm that affect the solution quality. The first parameter is the neighborhood $Neigh_x^1$ and the second is the *cooling scheme* which

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1:	Let $x = G(V, E \cup E')$ be an instance of LARGEST-CON and let <i>A</i> be an efficient algorithm for
	solving MAX-CON.
2:	Let $\alpha = A(x)$ be the initial feasible solution.
3:	Let <i>T</i> be an initial control parameter (temperature).
4:	Select a temperature reduction function f as a function of two parameters; T and time.
5:	Select a counter $I := 0$
6:	while $T > 0$ (or T is not too close to 0) do
7:	Either by first improvement or best improvement, find a $\beta \in Neigh_x^1(\alpha)$
8:	if $cost(\beta) \le cost(\alpha)$ {cost function outputs the edge count (consistent) of a solution } then
9:	$\alpha := \beta$
10:	else
11:	Generate a random number r uniformly in the range $(0, 1)$
12:	if $r < e^{-\frac{cost(\beta)-cost(\alpha)}{T}}$ then
13:	$\alpha := \beta$
14:	end if
15:	end if
16:	I := I + 1
17:	T := f(T, I)
18:	end while
19:	Return α

Algorithm 10: Simulated Annealing Scheme for LARGEST-CON using $Neigh_x^1$

determines the rate of decrease of the parameter T. It can be observed that a slow decrease of T may result in an extremely large time complexity of the algorithm. But, it has been proved that the increase of time complexity increases the probability of getting feasible solutions of high quality [44]. Moreover, factors like initial choice of control parameter or temperature T, the temperature reduction function f, and the termination condition which decides when the simulated annealing algorithm stops for $T \leq term$; all decide how much improvement can be achieved by the simulated annealing process. These factors are not discussed here and further details can be found in the book by Juraj et al. [44].

Simulated annealing has been presented here as a possible improvement to the existing greedy and local search algorithms for solving the LARGEST-CON problem. The actual performance of this algorithm and the values for the various cooling scheme parameters have not been fixed and experimentally verified. Next, a LP-based optimization technique for the LARGEST-CON problem is presented.

5.7.2 Linear Programming-based Optimization

The LARGEST-CON problem can also be formulated as an Integer Program (IP); more specifically a 0-1 Program. Let $G = (V, E \cup E')$ be an instance of the LARGEST-CON problem, where E is the set of consistent edges and E' is the set of inconsistent edges. Let $U_k \in \{0, 1\}$ where $k \in E$, be the variable representing whether a consistent edge k is selected or not. The value of $U_k = 1$ implies that the consistent edge k is present in the solution and $U_k = 0$ implies that it is not. Let $v_i \in \{0, 1\}$ where $i \in V$, be a variable representing whether each vertex i in the graph is present in the solution or not. Similarly, $v_i = 1$ implies that the vertex i is in the solution and $v_i = 0$ implies that it is not. Let ||V|| = n, i.e., there are total number of n vertices. Let ||E|| = m, i.e., the size of the consistent edge set is m. Then, the IP of the LARGEST-CON problem for an input instance Gcan be formulated as shown below.

$$\begin{array}{ll} Maximize & \sum_{i=1}^{m} U_k\\ Subject \ to & (v_i + v_j - 2U_k) \ge 0; \ \forall k = (i, j) \in E\\ & (v_i + v_j) \le 1; \ \forall (i, j) \in E'\\ & and \ v_i, v_j, U_k \in \{0, 1\}; \ \forall i, j \in V, \ k = (i, j) \in E \end{array}$$

Solving an Integer Program is a well-known NP-hard problem [54]. To overcome this hurdle, a Linear Program (LP) relaxation for the above Integer Program can be obtained. A Linear Program is solvable in polynomial time [55] using efficient techniques like the simplex algorithm [18]. If the LP relaxation has an integral solution then that can be the solution for the above IP also. But if LP relaxation does not have integral solution then techniques like rounding, branch and bound, etc., can be used to obtain a close to optimal solution.

5.8 Conclusion

This chapter addressed the problem of efficiently mitigating location inconsistencies in localization services and location-based applications in highly distributed network systems like wireless sensor networks. Inconsistent location information results from either cheating behavior by nodes or due to large measurement errors, often caused by external and uncontrollable factors. Such inconsistent location information cause location dependent applications and services to fail and needs to be efficiently eliminated from the network. Towards achieving that goal, this chapter first presented a practical graph-theoretic framework, called Partially Consistent Grounded Graph, for modeling location-based services in highly distributed and autonomous network systems like wireless sensor networks. In this model, inconsistent location information in the network was modeled as a subset of the set of all edges in the network, two optimization problems, namely MAX-CON and LARGEST-CON, were formulated.

MAX-CON is the problem of maximizing the number of vertices in the completely consistent subgraph of the Partially Consistent Grounded Graph, while LARGEST-CON is the problem of maximizing the number of consistent edges. A number of combinatorial properties, including computational hardness and approximability for these problems were studied. Both the problems were proved to be *NP*-Complete. The hardness of these problems is indicative of the difficulty involved in efficiently eliminating inconsistency causing nodes in a highly distributed system, even in the presence of full knowledge (or complete location information). Although MAX-CON was guaranteed to have a constant ratio approximation algorithm, no such guarantees could be made for the LARGEST-CON problem. LARGEST-CON was proved to not have a constant approximation ratio, unless P = NP. Following this inapproximability result, two algorithms for LARGEST-CON, namely the greedy algorithm and the local solution search algorithm, were outlined. Experimental results showed that the local search algorithm performs slightly better than the greedy algorithm for randomly generated graphs and that the performance of both the algorithms deteriorated as the number of nodes and radio range increased. Another important observation in these experiments was that the average solution quality was around 0.5, which is encouraging considering the inapproximability result. In order to overcome some of the drawbacks of the basic greedy and local search heuristics, two more solution strategies, one based on the simulated annealing technique and another on a Linear Programming approach, were also proposed. Although no experimental results are available for these strategies at this time, intuitively it does not seem that they will perform any worst than the greedy or the local search heuristic.

The next chapter concludes this dissertation by presenting a summary of contributions and a quick recap of the major research results, followed by a discussion of the impact of the research presented in this dissertation and how these results can be used and interpreted by other researchers and practitioners. The chapter finally ends with a road-map for further research on a variety of open problems and unresearched topics in the area of secure and robust localization.
Chapter 6

Conclusion

"This is not the end. It is not even the beginning of the end. But it is, perhaps, the end of the beginning."

- Winston Churchill

This chapter presents a detailed summary of the important results from the previous chapters and discusses its role in achieving the basic goals of secure and robust localization that were outlined at the start of the dissertation. It also puts the research of this dissertation in perspective by highlighting the significance of the published results in context of their utility in securing and improving the robustness of localization services and location-based applications in ESNs. Finally, this chapter lists a set of open problems on robust localization that have not been addressed in this dissertation and outlines a plan for further research on these and a variety of other problems in this area.

6.1 Summary

Wireless sensor networks are a byproduct of the basic concept of wireless ad-hoc networks, i.e., networks that generally do not require any fixed infrastructure or organization for successful operation. The main difference in sensor networks is the low power (both battery and computational) and robustness of the sensor devices as compared to the high-end devices found in modern day wireless (ad-hoc) networks. Due to the location critical nature of the applications associated with such networks, knowledge of the node locations is extremely important and as a result, the problem of localization or location discovery in wireless sensor networks has gained a lot of research attention. Most of the earlier research efforts on localization in sensor networks were derivatives of similar work in wireless LAN (IEEE 802.11) or ad-hoc networks. Although researchers focused on developing distributed localization schemes for low power and resource constrained devices, other issues regarding security, robustness and fault-tolerance of such schemes were overlooked. These are important issues, especially considering the harsh and hostile conditions in which sensor networks are deployed and used.

This dissertation has addressed the problem of robust localization in wireless sensor networks with a special focus on sensor networks used for emergency, military and first response applications, referred to as Emergency Sensor Networks (ESNs). There are various issues associated with the problem of efficient localization in ESNs. On the one hand, due to the open nature of the network, security of nodes and services like localization is an issue. On the other hand, harsh and extreme conditions can cause nodes to fail, which can act as a strong deterrent to the success of the localization process in such networks. In addition to these, inaccurate location discovery can also adversely affect other location dependent network-wide services and applications. The main goal of this dissertation was to provide efficient solutions to these and other problems related to the process of localization, keeping in mind the specific requirements, constraints and factors affecting ESNs.

In line with this goal, the first order of business in this dissertation was to survey existing localization schemes by dividing them into two broad classes, followed by a study of the applicability of each such scheme in ESNs by identifying their shortcomings and disadvantages under specific situations. The survey of the two classes of localization techniques, namely beacon-based techniques and signature-based techniques, their advantages, shortcomings, etc., were outlined in detail in Chapter 1. Two main problems in existing localization techniques for sensor networks were identified. The first one was the problem of cheating or malicious beacon nodes in beacon-

based localization approaches that use distance information. The second problem underlined the lack of fault-tolerance in existing signature-based approaches. An effective solution strategy to each of the above problems would go a long way in successfully implementing and deploying these localization techniques for a variety of ESN applications. A careful study of other research efforts in this direction was also conducted in Chapter 2, which not only discussed specific limitations in those proposals but also summarized steps that were taken in this dissertation in order to overcome those shortcomings.

In Chapter 3, the problem of distance-based localization in the presence of cheating or malicious beacon nodes was addressed. By assuming a very practical network model and a strong adversary model (which also includes collusion attacks), couple of important analytical results for this problem were presented. The first set of results fixed the necessary and sufficient conditions for secure distance-based localization in terms of the number of malicious nodes that can be successfully tolerated by any distance-based localization algorithm. The second set of results, identified and defined a class of distance-based localization algorithms that can guarantee a bounded localization error, provided the necessary and sufficient conditions are satisfied. These results laid the foundation for identification of two algorithms belonging to this class of robust distance-based localization algorithms. The first algorithm, called the polynomial time algorithm, was proved to have a cubic $(n^3 logn)$ worst-case running time complexity in terms of the total number of beacon nodes n. The second algorithm was based on an intelligent heuristic of searching for the target location near intersection points of a large number of circles (denoting coverage area of nodes). Although no running time guarantees could be provided for the heuristic-based algorithm, it was found to perform very well in most scenarios. Also, experimental results showed that even though both the polynomial time algorithm and the heuristic-based algorithm had low localization errors, the heuristic-based algorithm outperformed the polynomial time algorithm in execution time. In order to show the generality of the proposed results and solutions, an extension of the current framework to the three dimensional coordinate system was also proposed. Moreover, the proposed algorithms were tested with various distributions of target and beacon locations to show that the

performance of the algorithms was not dependent on a specific distribution of node locations.

Following a rigorous analytical and experimental treatment of the secure distance-based localization problem, the focus of the dissertation shifted to the problem of fault-tolerant localization in Chapter 4. More specifically, this chapter addressed the problem of robust signature-based localization in the presence of disabled or failed nodes. Although beacon-based approaches have been shown to work well in most cases, signature-based approaches provide a good alternative when it is not feasible to deploy or implement beacon-based techniques. Similar to beacon-based schemes, signature-based techniques have been shown (as explained in Chapter 1) to suffer from a variety of problems, the most prominent of it being the fault-tolerance of such schemes. This problem is also significant from the point of view of its feasibility in ESNs and related applications. In that direction, Chapter 4 first presented a detailed case study describing the mechanics of a typical signature-based scheme, and by means of simulation experiments showed that the localization accuracy of such schemes deteriorated rapidly as the number of disabled nodes increased. From the case study, it was also clear that node deployment and the post-deployment node distribution greatly influence the accuracy of signature-based localization. Node deployment strategies in existing signature-based schemes do not posses the necessary mechanisms in order to monitor and adapt to the changes in node distribution due to factors like movement, disablement, etc., which is the main cause of the lack of fault-tolerance in these schemes. To overcome this issue, an emergency level-based deployment strategy was proposed that deploys nodes around fixed points over the deployment area based on the rate of node disablement at those points. In order to predict the node disablement around deployment points, a stochastic model of node destruction was formulated, and the deployment strategy employs this model to make deployment decisions. Then, a simple and intuitive technique to improve the fault-tolerance of current signature-based localization techniques, called Group Selection Protocol (GSP), was outlined. GSP monitors node distribution changes due to disablement by employing specialized nodes, called group heads. One task of the group heads is to collect and forward the health status updates of their corresponding groups to other nodes in the network. Although employing GSP resulted in some improvement as far as fault-tolerance was

concerned, it did not improve the complexity of the localization scheme in terms of computation and memory look-up. In order to achieve that, a simple, fault-tolerant signature-based localization scheme, called ASFALT, was proposed. ASFALT works by computing distances to neighborhood nodes and utilizes the non-uniformity in node distribution to compute the target location. Results of simulation experiments verified that ASFALT outperforms the other signature-based scheme (with and without GSP) in situations of random node disablement.

Finally, in Chapter 5 another problem related to localization was addressed. Here, instead of accurately localizing the nodes, it was assumed that all nodes know their own locations (or at least pretend to know their own locations). The problem then is, how to eliminate nodes that do not disclose their location information correctly? Inaccurate location reporting/verification is detrimental to the success of sensor network applications, especially emergency related applications because they are extremely location critical. Such inaccurate location reporting/verification can be either a result of cheating behavior or due to external factors. Nevertheless, it's very important to efficiently eliminate inaccurate location information in order to get a location-consistent view of the network, which can be used to localize other nodes or to make other network-wide decisions. This problem was modeled as a combinatorial optimization problem in a graph-theoretic framework of the network, called Partially Consistent Grounded Graphs (PCGG). Two variants of the problem were addressed. In the first variation, called MAX-CON, the number of vertices in the consistent subgraph of the PCGG was maximized, while in the second one, called LARGEST-CON, the number of edges in the consistent subgraph was maximized. Important combinatorial properties for these problems, including combinatorial hardness and approximability were studied. Although both the problems were proved to be NP-Complete, it was shown that MAX-CON has a constant time approximation algorithm while it was not possible to approximate LARGEST-CON with a constant ratio unless P = NP. Efficient algorithms based on popular heuristics like, greedy approach, local solution search, simulated annealing and Linear Programming based approaches were proposed. Although currently no analysis that gave a bound on the solution quality of these algorithms was provided, experimental results showed that both the greedy and local solution search performed

well for randomly generated graphs, with an average solution quality of around 0.5.

The following section discusses the impact of the results presented in this dissertation on the development of efficient localization and security tools for futuristic networks like the Emergency Sensor Networks.

6.2 Research Impact

The research presented in this dissertation is multi-faceted with a single goal: to provide secure and robust localization services for Emergency Sensor Networks. It works towards this goal by identi-fying shortcomings in existing localization approaches at various levels and fronts, and attempts to overcome these weaknesses by leveraging on mathematically sound analytical tools and rigorous simulation experiments. Three main factors that affect the accuracy of localization services and location-based applications are identified.

The first factor is the security of localization services in Emergency Sensor Networks. Similar to other services and applications in wireless and computer networks, localization security in sensor networks was an afterthought. Until recently there was very little or no research on securing localization services in wireless sensor networks. Securing the localization process against malicious or cheating nodes is crucial to the success of the network application. This problem is more pronounced in ESNs because of the harshness and the hostility of the environment in which such networks are deployed. The research on securing localization services presented in this dissertation targets a very specific type of localization technique, referred to as the beacon-based technique. Unlike previous techniques on securing beacon-based localization, this dissertation takes a two-pronged approach. Rather than directly going out for a solution based on some heuristic, this dissertation conducts a detailed mathematical analysis of the problem using a practical network model and a strong adversary model. The necessary and sufficient conditions and the bounds on the worst case localization errors obtained by this study may help in understanding how best any distance-based algorithm could perform. Such bounds are also useful to other researchers and algorithm designers, because they provide a reference scale to compare the solution quality of new algorithms in this area. The class of robust localization algorithms defined in this chapter can also help in deriving a taxonomy of secure distance-based localization approaches. Following the important analytical results, a series of experimental studies reported in this dissertation can help identify how some of the algorithms in this class stack up against each other under different parameters like the number of malicious nodes, measurement errors and location distribution. Since these algorithms are guaranteed to have a bounded localization error, the parameters on which they can be further improved are the simulation time and execution efficiency. These experiments, although not executed on a sensor network test-bed or simulation environment, can give ample insight into the mechanics and performance of these algorithms. These results will be very useful when designing secure localization algorithms for real sensor network applications. These results have been published in [98].

The second factor that affects the accuracy of localization in Emergency Sensor Networks is the random disablement or failure of nodes. Fault-tolerance is an extremely important property of localization schemes employed in ESNs because of the high probability of node failures in ESN applications. A detailed study of existing literature reveals very little or no work in the direction of fault-tolerant localization schemes. The research presented in this dissertation is among one of the first works in this area. Achieving fault-tolerance in beacon-based techniques is pretty straightforward. Beacon node disablement may result in insufficient number of beacons available for localization and the way to overcome this problem is by increasing the beacon node redundancy in the network. But, the problem becomes non-trivial in signature-based localization schemes. The emergency level based node deployment strategy is the first step in achieving fault-tolerance in such schemes. It provides a simple and effective way to deploy nodes over the emergency area in an ESN. The strategy itself and the various related probabilistic models are generic enough to be used by network designers to develop deployment policies for emergency specific sensor network applications. Also, the fault-tolerance related improvements in the form of ASFALT and GSP are very simple, intuitive and straightforward to implement. Moreover, measurements from extensive simulation-based experiments have verified the improvement brought about by these algorithms. But before these algorithms can be used in real world, extensive testing in a much more realistic scenario like a sensor network test-bed would be required. In that case, measurements from the current simulation experiments would be relevant in order to carry out a comparative analysis and can provide hints on improving these schemes further. This part of the research was presented in [47,49].

Apart from the problem of location discovery, another intriguing question that needed attention was, how can nodes in the network be sure that other nodes are truthful about their locations? For node pairs that are truthful, the Euclidean distance between their locations should match the estimated distance between the nodes. And for the ones that this does not match, it implies that there is a location inconsistency. From a network-wide point of view, one is viewing at a structure in which some nodes are consistent with each other in terms of locations, while others are not. A consistent structure is important for multiple reasons. First, it assures other nodes not within the consistent structure that localization done by using nodes from the consistent structure will be accurate. Second, nodes within the consistent structure can be used by a variety of other location dependent services like routing, neighborhood detection, etc., to make their own network-wide decisions. Such a consistent structure is also useful to network designers and administrators for making redeployment decisions, information segregation, etc. This problem of obtaining a fully location consistent substructure of the network, given complete knowledge of the node locations and distances between them, has only been first addressed in this dissertation. The approach in order to obtain a solution for this problem has been very systematic. Rather than providing random heuristics, this dissertation first modeled the problem as a graph-based optimization problem and studied its combinatorial properties like computational hardness and approximability. These results were useful in developing meaningful heuristics to solve this problem. This work appeared in [46].

The next section lists some interesting open problems and directions for future research in the area of secure and robust localization.

6.3 Open Problems and Future Research

This dissertation has attempted to provide answers to a variety of questions in the area of secure and fault-tolerant location discovery for wireless sensor networks. However, there are numerous avenues for extending the research presented in this dissertation. The following directions hold a lot of promise in terms of future research in this area.

This dissertation presented significant theoretical analysis on the problem of secure distancebased localization in the presence of malicious or cheating beacon nodes. Specifically, the necessary and sufficient conditions for secure localization and a class of robust localization algorithms that guaranteed a bounded localization error were presented. Two algorithms that belong to this class were also outlined. These algorithms estimated the target location by computing a point in the intersection of at least k_{max} + 3 rings. The analysis verified that these algorithms can guarantee a bounded localization error. But, an intriguing question in this direction is, what is the best algorithm to find this intersection of rings, in terms of worst-case complexity and in terms of average computational time? Obviously, the best algorithm is the one that finds the target location precisely. But, given a non-zero maximum distance estimation error ϵ , can an algorithm predict the exact location efficiently all the time? More importantly, it would be interesting to see if a bound lower than the current bound of the localization error can be derived. All these are interesting open research questions. One shortcoming of the existing work in relevance to real world systems is that ideal radio and signal propagation models have been assumed here. Such assumptions are required when deriving mathematical limits and bounds, but in a more practical scenario these assumptions would not hold. Radio coverage around nodes is not in circles and signal propagation is not ideal but depends on external factors like interference, obstructions, etc. As a result, an important next step would be to take these experiments to real sensor network test-beds. An analysis of the localization error of the proposed algorithms in real test-bed experiments would reveal important information on their actual performance and feasibility in real world systems.

The next set of results in this dissertation were aimed at improving the fault-tolerance of lo-

calization schemes, specifically signature-based schemes. This research was motivated by the fact that random node disablement/failure changes the pre-deployment node distribution used by signature-based schemes to estimate node locations. To overcome this problem, well-designed stochastic models for predicting node failures due to external conditions are used to reconstruct the node distribution at any point in time after deployment. Such a deployment strategy improves the fault-tolerance of the associated signature-based scheme. But, there are other factors prevalent during emergency situations that can modify the pre-deployment node distribution as the application progresses. For example, node movement and injection of false nodes by an adversary can also alter this pre-deployment node distribution and thus, adversely affect the performance of the associated signature-based scheme. An interesting research direction would be to study the effects of these factors on the performance of signature-based schemes in a systematic manner and integrate the results with the current deployment and localization framework. Also, currently the experimental results presented in this dissertation are mostly simulation based. It would be very useful and significant to move the experimentation to a real sensor network test-bed platform. It would be useful initially to just simulate the proposed algorithms, i.e., GSP and ASFALT, on this test-bed. Node disablement can be simulated by randomly choosing nodes from the groups for failure at a fixed rate. Real-time measurements from these experiments can be used to further verify the efficiency and performance of the proposed fault-tolerant signature-based algorithms. In order to further strengthen the stochastic node destruction and distribution models, significant real-time experiments involving simulation of actual emergencies should be performed as a separate set of experiments.

Analysis of the MAX-CON and LARGEST-CON problems in the last part of the dissertation highlighted the hardness in efficiently mitigating location inconsistencies even in the presence of global (network-wide) location and distance information. Although LARGEST-CON was proved to not have an approximation ratio less than 1, a lower bound on the solution quality of LARGEST-CON is still an open question. A good starting point would be to investigate the solution quality of the heuristic-based solutions proposed for LARGEST-CON. Another interesting observation is that the combinatorial results for LARGEST-CON presented in this dissertation holds for randomly generated graphs. As part of future research, it would be useful to investigate whether the hardness and inapproximability results for LARGEST-CON also hold for other specific types of graphs, e.g., planar graphs, completely connected graphs, bi-partite graphs, etc. Obviously, results for the graph type that best models wireless sensor networks would be most relevant. It would also be interesting to conduct similar studies for other network services like time synchronization [24, 28], and to observe the relationship between the results presented here and the ones for similar optimization problems in time synchronization. Such an effort has been initiated and some preliminary results can be found in the technical report by Jadliwala et al. [45].

This dissertation highlighted the security and fault-tolerance related shortcomings in existing localization techniques and proposed efficient solutions to overcome these problems. Sound mathematical analysis and measurements from rigorous simulation experiments were used to verify the performance and efficiency of these solutions with the hope that these efforts will lead to a wider adoption of the ideas presented here to real world wireless sensor network systems and applications.

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Research Publications

Journals

• Jadliwala, M., Duan, Q., Xu, J. and Upadhyaya, S. (2007) "On Extracting Consistent Graphs in Wireless Sensor Networks", International Journal of Sensor Networks (IJSNET): Special Issue on Theoretical and Algorithmic Aspects in Sensor Networks, Vol. 2, Nos. 3/4, pp.149-162.

Conferences and Symposia

- Zhong, S., Jadliwala, M., Upadhyaya, S. and Qiao, C., "Towards a Theory of Robust Localization against Malicious Beacon Nodes", in the Proceedings of The 27th IEEE International Conference on Computer Communication (INFOCOM 2008), pages: 1391-1399, Phoenix, Arizona, April 15-17, 2008. (acceptance rate: 21%).
- Jadliwala, M., Upadhyaya, S. and Taneja, M., "ASFALT: A Simple Fault-Tolerant Signaturebased Localization Technique for Emergency Sensor Networks", in the Proceedings of The 26th IEEE International Symposium on Reliable Distributed Systems (SRDS 2007), pages: 3-12, Beijing, CHINA, October 10-12, 2007. (acceptance rate: 15%).
- Virendra M., Jadliwala M., Chandrasekaran M., Upadhyaya S., "Quantifying Trust in Mobile Ad-Hoc Networks", In Proceedings of the IEEE International Conference on Integration of

Knowledge Intensive Multi-agent Systems (KIMAS'05), Waltham, MA, Apr 2005, pp. 65-71.

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Workshops

- Jadliwala, M., Upadhyaya, S., Rao, H.R. and Sharman, R. "Security and Dependability Issues in Location Estimation for Emergency Sensor Networks", The Fourth Workshop on e-Business (WeB 2005), Venetian, Las Vegas, Nevada, USA December 10, 2005.
- Braynov, S. and Jadliwala, M. 2003. "Representation and Analysis of Coordinated Attacks", at The 2003 ACM Workshop on Formal Methods in Security Engineering (Washington, D.C.). FMSE '03. ACM Press, New York, NY, pp. 43-51.

Under Review/Submission

- Jadliwala, M., Upadhyaya, S., Robust Deployment and Localization in Emergency Sensor Networks, Under review at the Pervasive and Mobile Computing Journal (Elsevier Publications).
- Jadliwala, M., Zhong, S., Upadhyaya, S. and Qiao, C., Robust Distance-based Localization against Malicious Beacon Nodes in Mobile Networks, Under preparation for submission to IEEE Transactions on Mobile Computing.
- Jadliwala, M., Duan, Q., Xu, J. and Upadhyaya, S., On Theory of Robust Time Synchronization in Mobile Computer Networks, Under Preparation.

Research Interests

Wireless Data Networks including Wireless LANs, Sensor and Mesh Networks, Operating System and Network Security, Vulnerability Analysis, Cryptography, Combinatorial Optimization, Approximation Algorithms, Game Theory and Multi-agent Systems. Specific topics of interests include:

- Secure and fault-tolerant distance-based and signature-based localization, robust time synchronization and robust deployment in pervasive and ubiquitous networks.
- Stimulating cooperation in wireless networks using economic mechanism design and game theory.
- Context-aware computing.
- Efficient cryptographic protocols and signature schemes for low power sensor and ad-hoc networks.

- Future generation wireless and ad-hoc networks.
- Modeling and analysis of complex, multi-stage and coordinated computer threats.