



# Line narrowing in $^1\text{H}$ NMR of powdered organic solids with TOP-CT-MAS experiments at ultra-fast MAS

Federico M. Paruzzo, Brennan J. Walder, Lyndon Emsley\*

Institut des Sciences et Ingénierie Chimiques, École Polytechnique Fédérale de Lausanne (EPFL), 1015 Lausanne, Switzerland

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## ABSTRACT

The residual broadening observed in  $^1\text{H}$  spectra of rigid organic solids at natural abundance under 111 kHz magic angle spinning (MAS) is typically a few hundred Hertz. Here we show that refocusable and non-refocusable interactions contribute roughly equally to this residual at high-fields (21.14 T), and suggest that the removal of the non-refocusable part will produce significant increase in spectral resolution. To this end, we demonstrate an experiment for the indirect acquisition of constant-time experiments at ultra-fast MAS (CT-MAS) which verifies this hypothesis. The combination of this experiment with the two-dimensional one pulse (TOP) transformation reduces the experimental time to a fraction of the original cost while retaining the narrowing effects. Results obtained with TOP-CT-MAS at 111 kHz MAS on a sample of  $\beta$ -AspAla yield up to 30% higher resolution spectra than the equivalent one-pulse experiment, in less than 10 min.

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## 1. Introduction

$^1\text{H}$  is often considered a perfect nucleus for nuclear magnetic resonance (NMR): it is ubiquitous in chemistry, it has the highest gyromagnetic ratio of all the stable nuclei and nearly 100% natural isotopic abundance. However, this ensemble of qualities is not sufficient to guarantee success in solid-state NMR. Indeed, the use of  $^1\text{H}$  is very limited in solids, where spectra of nuclei such as carbon-13, phosphorus-31 or silicon-29 are more common. This is mainly due to the line-broadening induced by strong  $^1\text{H}$  homonuclear dipolar couplings – of the order of a few tens of kHz in organic solids – which leads to poor resolution in  $^1\text{H}$  solid-state NMR. (In contrast, in liquid-state NMR rapid molecular tumbling largely averages dipolar couplings to zero, leading to very high-resolution spectra).

$^1\text{H}$  spectral resolution in solids can be improved dramatically by magic angle spinning (MAS) [1,2]. Due to the strength of the homonuclear dipolar coupling, and due to the fact that it is a homogeneous interaction in the nomenclature of Maricq and Waugh [3], low to moderate spinning regimes (say <30 kHz MAS rates) lead, in general, to  $^1\text{H}$  NMR spectra with line narrowing by factor  $\sim 40$ –50, but this is not sufficient to alleviate the resolution problem (see Fig. 1a) [4–7]. Further decoupling can be achieved with the so-called combined rotation and multi-pulse spectroscopy (CRAMPS) approaches [8], which involve the simultaneous application of MAS and pulse sequences designed to remove

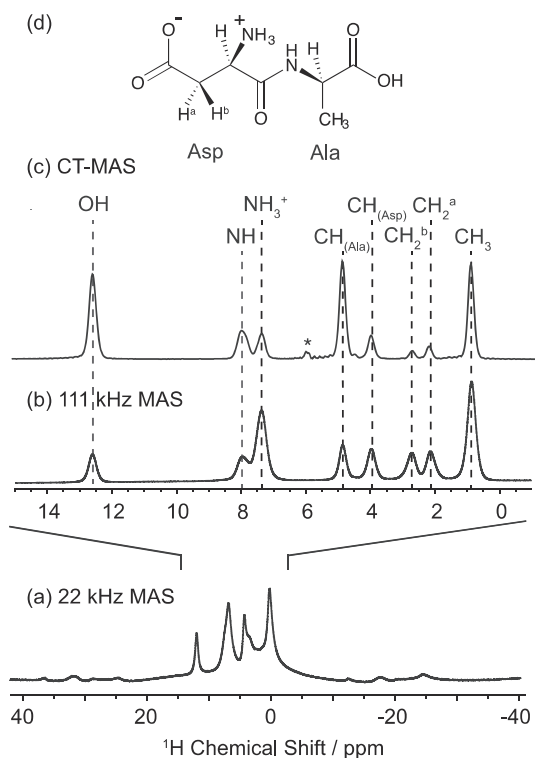
homonuclear dipolar couplings while retaining isotropic chemical shifts [9–18]. This approach yields the best resolution available today for spinning rates up to  $\sim 65$  kHz, yielding linewidths in rigid organic solids on the order of 400 Hz [19,20]. These approaches have enabled a number of methods to characterise structure and dynamics in powdered solids [21–33]. However, the application of high-power decoupling for several milliseconds is a severe drawback as it is experimentally complex, technically demanding, and limits the maximum achievable resolution and sensitivity.

The recent introduction of probes capable of spinning samples up to 111 kHz [34,35] made the acquisition of reasonably high-resolution solid-state  $^1\text{H}$  NMR spectra possible with MAS alone, as shown in Fig. 1b with the  $^1\text{H}$  111 kHz MAS spectrum of  $\beta$ -AspAla. With measured  $^1\text{H}$  linewidths of about 250/300 Hz ( $\approx 0.3$  ppm on a 900 MHz spectrometer), the spectral resolution is comparable to that obtained using state-of-the-art CRAMPS methods at lower MAS frequencies [16,17,20,36]. Despite the good resolution, the residual line broadening (which is estimated to be roughly 1% of the original broadening for organic solids in static conditions) still limits the use of  $^1\text{H}$  NMR in the solid state, especially for complex systems.

Here, we develop a new experiment to further improve the resolution at ultra-fast MAS. Developing on the idea proposed by Lesage et al. [37] for CRAMPS spectra, we make use of constant-time acquisition in the indirect dimension of a 2D experiment to obtain spectra in which non-refocusable broadening is removed. We show results obtained on a sample of powdered microcrystalline  $\beta$ -AspAla, where spectral resolution is increased by up to 40% compared to one-pulse

\* Corresponding author.

E-mail address: [lyndon.emsley@epfl.ch](mailto:lyndon.emsley@epfl.ch) (L. Emsley).



**Fig. 1.** (a–c) 1D <sup>1</sup>H spectra of powdered β-AspAla. (a and b) MAS spectra at 22 (a) and 111 (b) kHz MAS rates. (c) 111 kHz CT-MAS spectrum. Spectra (a–c) were acquired at 900 MHz using a one-pulse acquisition sequence (a and b) and the sequence of Fig. 2b (c). (d) Chemical formula of β-AspAla.

acquisition. Since the indirectly acquired spectrum is conventionally acquired point-by-point, however, obtaining high-resolution constant-time spectra from CT-MAS can require very long experiment times. Strategies utilizing spectral aliasing [38,39], non-uniform sampling [40], or covariance processing [41] are means of enhancing the resolution and information of such spectra in a time effective manner and are being actively developed.

In a unique alternative approach, Davis et al. demonstrated that the spectral windows of the direct and indirectly acquired dimensions in the 2D PASS experiment for sideband separation in rotating solids can be effectively swapped by the action of an affine transformation on the 2D dataset [42]. This allowed the indirectly detected signals to inherit the large spectral window of the directly acquired dimension. This method of transferring spectral windows by affine transformation of uniformly sampled data was referred to as TOP processing and was later shown to generalize to other sideband separation experiments [43,44]. Here we demonstrate that TOP processing is not specific to this class of solid-state NMR experiment but is applicable to any case where two interactions coevolve in the directly acquired signal and evolve independently along other coordinates in the 2D plane. We do this by showing how the TOP transformation permits an unaliased <sup>1</sup>H CT-MAS spectrum to be recovered from an indirect dimension that is severely undersampled with respect to the Nyquist rate of the <sup>1</sup>H shift spectrum. This approach improves the economy of the CT-MAS experiment by one to two orders of magnitude, leading to peaks up to 30% narrower than in the one-pulse experiment, acquired in less than 10 min.

## 2. Methods

### 2.1. NMR

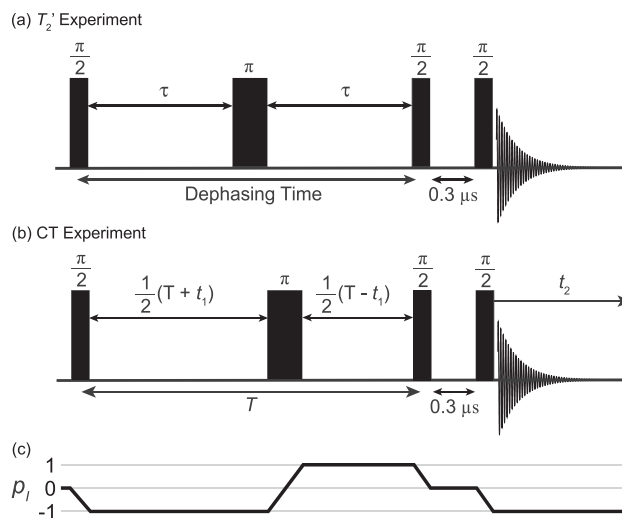
Experiments were performed on a Bruker 900 US<sup>2</sup> wide-bore Avance Neo NMR spectrometer operating at a transmitter fre-

quency 900.1448 MHz for <sup>1</sup>H, equipped with a H/C/N 0.7 mm CPMAS probe. All spectra were recorded using a rotor spinning rate ( $\nu_r$ ) of 111 kHz, with the only exception being the spectra of Fig. 1a which was recorded with  $\nu_r = 22$  kHz. A sample of powdered β-AspAla ((2S)-2-amino-3-[[[(1S)-1-carboxyethyl]carbamoyl]propionic acid, purity > 99%) was purchased from Bachem and used for all experiments without further recrystallization.

The transverse dephasing times ( $T_2$ ) were measured using the Hahn echo sequence [45], shown in Fig. 2a. The measurement was done through a pseudo 2D experiment, based on the acquisition of a series of 1D MAS <sup>1</sup>H spectra where the time  $\tau$  of decoupling was systematically increased in a multiple of the rotor period ( $\tau_r$ ). The dephasing curve was then obtained by plotting the area under each resonance as a function of the dephasing time ( $2\tau$ ).  $T_2$  values were then extracted by fitting the dephasing curve to an exponential decay ( $S(2\tau) = a \cdot \exp(-2\tau/T_2)$ ).

Fig. 2b shows the pulse sequence used for the acquisition of constant-time MAS (CT-MAS) experiments. The initial  $\pi/2$  pulse is followed by a  $\tau_1 - \pi - \tau_2$  block ( $t_1$  dimension), then a z-filter is applied before direct <sup>1</sup>H detection in  $t_2$ . During the experiment, the total time  $T$  of the block  $\tau_1 - \pi - \tau_2$  is kept constant. The evolution of the magnetization during  $t_1$  is induced by concomitantly increasing  $\tau_1$  in a multiple of the rotor period, while  $\tau_2$  is decreased. During  $t_1$  evolution, the  $\pi$  pulse is incrementally moved from the center (where  $t_1 = 0$ ) to the end of the  $T$  period. Analogously to the CT-CRAMPS [37] experiment, this experiment makes use of hypercomplex acquisition in the manner of States, Haberkorn, and Ruben [46] to acquire the negative  $t_1$  quadrant. The result is a two-dimensional dataset with the ordinary MAS <sup>1</sup>H spectrum in  $\omega_2$  and the <sup>1</sup>H spectrum free of non-refocusable broadening (the homogeneous interactions) in  $\omega_1$  [37].

All CT-MAS experiments were acquired with 256 points in the indirect dimension. The indirect sampling intervals ( $\Delta t_1$ ) were 0.036 ms, 0.054 ms, 0.072 ms, and 0.144 ms respectively for the experiments with constant time intervals of  $T = 4.6$  ms, 6.9 ms, 9.2 ms, and 18.5 ms. Note that the increment used for  $T = 18.5$  ms corresponds to a 7 kHz window, which leads to aliasing of the <sup>1</sup>H spectrum. The 1D spectrum shown was reconstructed from the 2D dataset by merging the 1D spectra obtained summing the signals in the columns between 0.25 and 2.38 ppm, 2.39 and 9.87 ppm, 9.88 and 13.80 ppm.



**Fig. 2.** (a and b) Pulse sequences for: (a) measurement of the transverse dephasing time ( $T_2$ ), (b) CT-MAS experiments. (c) Symmetry pathway selected by phase cycling for the TOP-CT-MAS implementation of the pulse sequence in panel (b). Detailed pulse program, experimental details for the spectra recorded, and the phase cycle are given in the experimental section and the ESI.

Formally, the TOP-CT-MAS experiments are implemented with a pulse sequence identical to the sequence used in the CT-MAS experiment, shown in Fig. 2b. Each TOP-CT-MAS experiment was run with an indirect sampling interval of  $\Delta t_1 = 1.081$  ms. For the experiments at constant time intervals of  $T = 4.9$  ms, 9.8 ms, and 17.8 ms, there were 8, 16, and 32 points in the indirect dimension, respectively. Application of the TOP transformation is facilitated by phase cycling for the symmetry pathway shown in Fig. 2c and running the  $\pi$  pulse from the beginning to the end of the constant time interval. This results in direct, phase-sensitive acquisition of the negative  $t_1$  signal quadrant to permit absorption mode lineshapes without resorting to hypercomplex acquisition [46,47], as chosen for the conventional CT-MAS implementation.

$^1\text{H}$  chemical shifts were referenced to the  $\text{CH}_3$  resonance observed for  $\beta$ -AspAla at 0.86 ppm with respect to the signal for neat tetramethylsilane (TMS) [16]. All linewidths reported are full width at half maximum linewidths. The processing of the spectra was done either using the Bruker program TopSpin 3.5 for 1D and 2D CT-MAS experiments or using RMN 1.8.4 for 2D TOP-CT-MAS [48]. The post-processing procedures for the  $T_2$  measurements (extraction of 1D spectra, evaluation of the area under each peak, fitting and extraction of  $T_2$  value), as well as the extraction of the experimental  $^1\text{H}$  linewidths for all spectra, were done in MATLAB using home-written scripts. Full details of acquisition parameters, phase cycles and pulse sequences are given in SI.

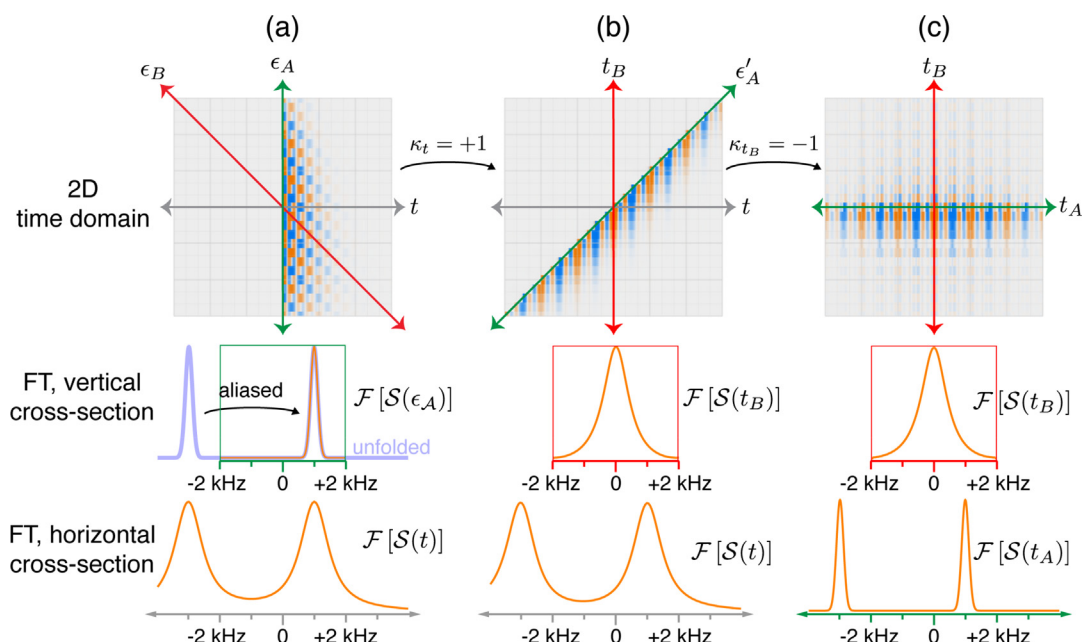
## 2.2. TOP-CT-MAS processing

Fig. 3 gives a visual outline of the TOP processing algorithm applied to simulated CT-MAS data. The two-dimensional dataset as acquired separates the constant-time signal evolution, which proceeds along the vertical  $\epsilon_A$  axis (which corresponds to  $t_1$  in

the pulse sequence of Fig. 2b), from the decay due to non-refocusable signal components, which evolves purely along the diagonal axis  $t = -\epsilon_A$ . This coordinate is designated  $\epsilon_B$ . Along the horizontal  $t$  axis (which corresponds to  $t_2$  in the pulse sequence of Fig. 2b), the directly detected MAS spectrum evolves with both refocusable and non-refocusable contributions to its linewidth. This structure, where separated interactions evolve along nonorthogonal dimensions and coevolve in the directly acquired signal, is like that of the 2D PASS experiment, where the use of the TOP transformation to effectively swap the sampling intervals of the direct and indirectly acquired dimensions was first described by Davis et al. [42]. Indeed, we can achieve the same effect in the CT-MAS experiment using the affine transformation:

$$\begin{bmatrix} t_B \\ t_A \end{bmatrix} = \underbrace{\begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}}_{K_{t_B}} \underbrace{\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}}_{K_t} \begin{bmatrix} \epsilon_A \\ t \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \epsilon_A \\ t \end{bmatrix}. \quad (1)$$

The strategy is to actively transform the data such that the two interaction dimensions,  $\epsilon_A$  and  $\epsilon_B$ , lie along the horizontal and vertical dimensions of the coordinate grid. The new respective coordinates,  $t_A$  and  $t_B$ , inherit the sampling properties of the grid axis onto which they are transformed. The first shear, represented by the matrix  $K_t$ , maps the  $\epsilon_B$  coordinate onto the vertical axis of the grid. Because only signal amplitude changes along this coordinate, the spectrum is centered about zero with a linewidth that reflects the non-refocusable linewidth of the MAS spectrum, suitable for the narrow spectral window of the vertical dimension. This is evident in the spectrum corresponding to the vertical cross-section of the 2D dataset after the first shear shown in Fig. 3b. After the second shear, represented by the matrix  $K_{t_B}$ , the original  $\epsilon_A$  axis is mapped onto the horizontal axis of the grid. In practice, the sam-



**Fig. 3.** The TOP double shear transformation of a simulated signal comprised of two peaks. (a) Representation of the undersampled CT-MAS dataset. The constant-time shift evolution (interaction 'A') evolves along the vertical axis designated by the time coordinate  $\epsilon_A$  (green) while the decay from non-refocusable components (interaction 'B') evolves along the line  $t = -\epsilon_A$ , designated by the time coordinate  $\epsilon_B$  (red). Fourier transform of the signal along  $\epsilon_A$  yields an aliased constant-time shift spectrum where the peak at  $-3$  kHz from the full spectrum (overlaid in blue) is aliased into the window, directly onto the peak at  $+1$  kHz. The directly acquired  $t$  coordinate (horizontal, gray), having a much higher bandwidth, contains the unaliased but broadened spectrum. (b) After the first active shearing transformation parallel to  $t$  (shear factor  $\kappa_t = +1$ ), the signal along  $\epsilon_A$  is shifted onto the vertical axis, along the coordinate designated  $t_B$ , while the  $\epsilon_A$  coordinate now runs parallel to the line  $t = +t_B$ . Fourier transform of the signal along  $t_B$  yields the lineshape due to non-refocusable components, whereas the spectrum along  $t$  is unchanged. (c) The second active shearing transformation, parallel to  $t_B$  (shear factor  $\kappa_{t_B} = -1$ ), shifts the signal along the  $\epsilon'_A$  axis onto the horizontal axis, along the coordinate designated  $t_A$ . Fourier transform of the signal along  $t_A$  presents the unaliased constant-time shift spectrum. Note the coordinate grid itself is unaffected by the active transformations. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

pling interval of this dimension can be set very small, and the originally undersampled spectrum is unaliased as the correspondingly large bandwidth of the horizontal axis is inherited, as can be seen in Fig. 3c.

In most useful circumstances, applying the TOP transformation matrix  $K_{t_b} K_t$  directly to the data vectors will map most of them off the grid nodes. Therefore, interpolation back onto the sampling grid is required. This is conveniently achieved by applying the shearing transformations as their operational equivalents in the mixed time-frequency domain according to the Fourier Affine Theorem. We carried this out using the macOS application RMN, as described in the TOP-CT-MAS processing walkthrough given in the ESI.

Not all linearly sampled 2D signals can have their sampling intervals effectively swapped by TOP processing. Qualifying conditions are discussed in Section 3.3.

### 3. Results and discussion

#### 3.1. Lineshape contributions

Fig. 4a shows the dephasing curves of the eight  $^1\text{H}$  resonances of  $\beta$ -AspAla, acquired using the sequence of Fig. 2a. As described above, by fitting these curves to an exponential decay it is possible to obtain the corresponding  $T_2$  values, which by definition corresponds to the residual broadening induced by non-refocusable interactions, such as homonuclear dipolar coupling [49]. From these curves, we can estimate that non-refocusable interactions contribute up to about a third of the measured line broadening observed in a one-pulse acquire experiment of the type shown in Fig. 1b, as it is shown in Fig. 4b. This is in line with previous obser-

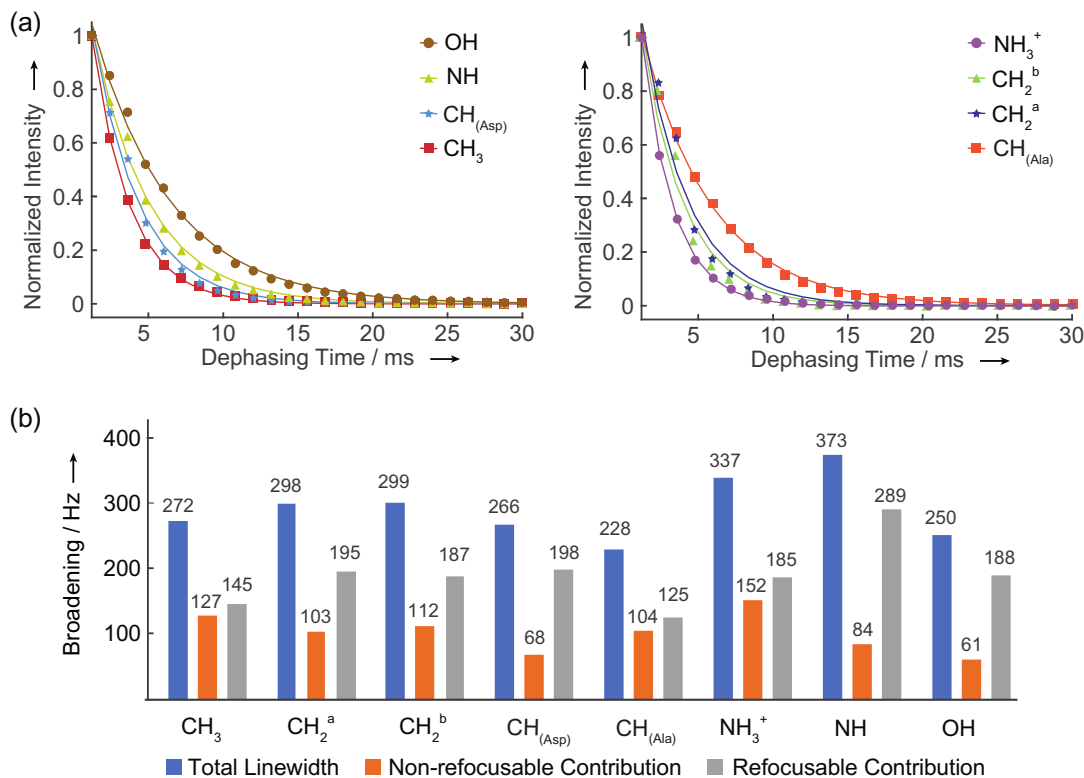
vations under both CRAMPS and fast MAS [7,17,37]. Removing this contribution would in principle lead to a significant improvement in the spectral resolution, without affecting chemical shift information (which would be refocused by the application of the  $\pi$  pulse).

#### 3.2. CT-MAS

The constant-time (CT) principle [50–55] has already proven to be an effective way to remove broadening due to non-refocusable interactions from  $^1\text{H}$  spectra in the solid-state. This idea was introduced by Lesage et al. with the CT-CRAMPS experiment [37]. They have shown that constant time acquisition in the indirect dimension of a 2D dataset leads to pure refocusable spectra, which have 2–3 times narrower resonances compared to CRAMPS experiments at 12.5 kHz MAS. In this experiment, the application of high power homonuclear decoupling was necessary to enter the weak coupling regime where the CT principle is likely to be most valid.

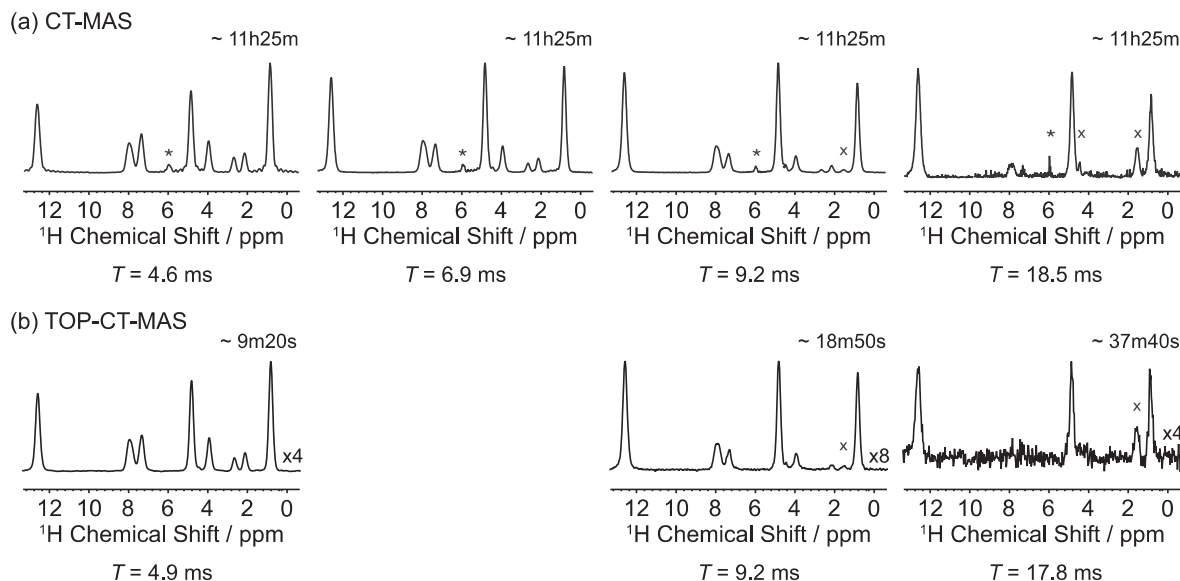
Today, with the line narrowing achieved using the highest MAS rates available, we can make use of the CT principle with MAS alone [56]. We can then obtain pure refocusable spectra by using the CT-MAS experiment, shown in Fig. 2b. Fig. 5a shows the 111 kHz CT-MAS spectra of  $\beta$ -AspAla acquired using constant time periods ( $T$ ) ranging from 4.6 to 18.5 ms.

When compared with the one-pulse  $^1\text{H}$  spectra recorded at 111 kHz MAS (Fig. 1b), all spectra show a significant improvement in the spectral resolution. Line narrowing is already achieved at  $T = 4.6$  ms, despite truncation of the signal due to the short CT period. In this spectrum the experimental linewidths are on average 17% narrower than the ones obtained with the one-pulse experiment. The  $\text{CH}_2$  resonances give the highest gain in resolution with 30% narrower linewidths (from about 300 to 210 Hz). On the other



**Fig. 4.** (a) Dephasing curves for the  $^1\text{H}$  resonances of powdered  $\beta$ -AspAla recorded using the pulse sequence of Fig. 2a. Each curve is normalized with respect to the corresponding highest intensity point. (b) Histogram of the contributions to the line broadening of the resonances of powdered  $\beta$ -AspAla at 111 kHz MAS. The total linewidth (in blue) is the linewidth measured from the experimental spectrum of Fig. 1b, the contributions of non-refocusable interactions (in orange) were calculated from the  $T_2$  values ( $\Delta_{\text{homo}} = 1/\pi T_2$ ) and the contributions of the refocusable interactions (in grey) were obtained from the difference between the total and non-refocusable broadenings. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)





**Fig. 5.** Comparison between different 1D  $^1\text{H}$  spectra of  $\beta$ -AspAla acquired with (a) the CT-MAS experiment and (b) the TOP-CT-MAS experiments. CT-MAS spectra were acquired using constant-time periods ( $T$ ) of 4.6, 6.9, 9.2 and 18.5 ms, while TOP-CT-MAS using  $T$  of 4.9, 9.2 and 17.8 ms. CT-MAS spectra are the vertical projection of the two-dimensional experiments, while TOP-CT-MAS spectra are the extraction of the central row. The transmitter peak is indicated with an asterisk, which is better suppressed in the TOP-CT-MAS experiments due to a superior phase cycle (see ESI). Peaks due to impurities are marked with an x. On the top-right corner of each spectrum is reported the corresponding acquisition time for comparison.

hand, nearly no line narrowing effect was observed for the OH resonance, probably due to the presence of dynamics or exchange.

The spectral resolution can be further improved by increasing the  $T$  value. This, however, comes at the expense of sensitivity, which decreases when increasing  $T$  at a rate that depends on the  $T_2$ . The dependence on  $T_2$  also affects the relative signal intensities in the CT-MAS spectra, which become different to those obtained with ordinary MAS experiments (Fig. 1b and c). The resonances with longer  $T_2$  will decay at a slower rate, resulting in higher relative intensities. At  $T = 6.8$  ms the resonances are on average 23% sharper than in the one-pulse experiment, with each resonance being at least 8% narrower than the corresponding peak in the one-pulse spectrum.  $T = 6.8$  ms is also short enough to allow the observation of all the  $^1\text{H}$  resonances in our sample. Further increase of  $T$  still provides additional line-narrowing effects, but decreases the sensitivity down to a point where some of the resonances are no longer visible. At the longest CT period we used ( $T = 18.5$  ms) only three peaks remain: the  $\text{CH}_3$ ,  $\text{CH}_{(\text{Ala})}$  and the OH. Of these, the  $\text{CH}_3$  shows a remarkable improvement in resolution, with a linewidth of 171 Hz, about 37% smaller than the 272 Hz observed in the one-pulse experiment. The improvement for the other two resonances is less: 16% for the  $\text{CH}_{(\text{Ala})}$  and only 3% for the OH. Note that in the spectra there are also two additional peaks at 1.6 and 4.5 ppm (which appear already at  $T = 9.2$  ms). These might be due to impurities with long  $T_2$  which are not observed in the one-pulse experiment. The full set of measured linewidths for these experiments is given in SI.

At this point, it is important to underline that in this experiment the line narrowing effect is not only due to the CT effect. As shown previously for the CT-CRAMPS experiment [37], part of the reduction in linewidth is due to the presence of the long echo which delays signal acquisition. During this delay the signal of protons in the more strongly coupled average orientations will dephase preferentially, leaving relatively stronger signals from protons in more weakly coupled average orientations, leading to line narrowing.

This is supported by the fact that in these spectra we observe significant line narrowing both in  $\omega_1$  and in  $\omega_2$  (where there is no CT effect). In particular, we observed that at 111 kHz MAS rate

the narrowing due to the CT effect contributes only 35% of the total line narrowing. This is in contrast with what has been observed for CT-CRAMPS experiments where most of the narrowing was induced by the CT acquisition.

### 3.3. TOP-CT-MAS

The most significant difference between conventional CT-MAS and the TOP-CT-MAS implementation is that the indirect dimension of the latter is sampled at 0.925 kHz, well below the Nyquist rate of the  $^1\text{H}$  chemical shift spectrum (about 12 kHz for  $\beta$ -AspAla at 21.14 T). Because of the correspondingly large indirect sampling interval (1.081 ms), the entire constant-time signal envelope can be collected with far fewer discrete samples than the conventional approach, making the TOP-CT-MAS implementation potentially far more economical in terms of experiment time. The obvious disadvantage is that Fourier transform of the indirect dimension, as acquired, presents a useless  $^1\text{H}$  shift spectrum because of severe spectral aliasing resulting from the undersampling.

The affine transformation specified by Eq. (1) nullifies this disadvantage by reconstructing the unaliased, high-resolution constant-time  $^1\text{H}$  spectrum in the large spectral window of the directly acquired dimension from a CT-MAS experiment with an undersampled  $\epsilon_A$  coordinate. The sampling rate of the indirect dimension using the TOP transformation needs only to be small enough to accommodate the frequency components which evolve along the vertical grid axis after transformation of the dataset. This is controlled by the design of the experiment and processing protocol. Here, the TOP transformation maps the residual non-refocusable broadening onto the vertical axis. For each site in our  $\beta$ -AspAla sample linewidths are no greater than 160 Hz, as shown in Fig. 4b. A sampling rate of less than 1 kHz suffices for sampling the  $\epsilon_A$  dimension in the TOP approach, for a potential reduction in experiment time by one to two orders of magnitude when TOP processing principles are leveraged. Note that if the indirect sampling rate dimension is so low that the  $t_B$  coordinate is undersampled, the TOP transformation will introduce sidebands into the spectrum along the  $t_A$  coordinate at integer multiples of the indirect sam-

pling rate. Generally, the decay of the non-refocusable contributions is exponential, so these sidebands manifest more strongly among the undesired long-tailed dispersive signal components, as shown in Fig. S1 in the ESI. This improves the robustness of the approach in the face of a poor estimation of an appropriate indirect sampling interval.

In Fig. 5a that has an indirect sampling rate of 27.75 kHz, conventional CT-MAS experiments took more than 11 h to complete. Note that an unnecessarily long 32-step phase cycle was used, but even if the conventional CT-MAS experiments had used the 14-step phase cycle to select the symmetry pathway in Fig. 2c directly, each experiment would still have taken nearly six hours to complete. In Fig. 5b, we see comparable high-resolution constant-time  $^1\text{H}$  spectra constructed from undersampled  $c_A$  coordinates using the TOP approach. When  $T = 4.9$  ms, just eight points in the indirect dimension are enough to obtain the narrowed proton spectrum, in an experiment lasting less than ten minutes. Furthermore, in the TOP-CT-MAS experiments with constant time intervals of 4.9 ms and 17.8 ms no loss in signal-to-noise per unit time was observed when compared to the CT-MAS experiment at 4.6 and 18.3 ms, while the experiment with  $T = 9.2$  ms shows about 30% less sensitivity when the TOP transformation is applied. Here, the overall reduction in experiment time for experiments at comparable  $T$  normalised to the number of scans was between a factor 8 and 32 using the TOP implementation.

Undersampling the indirect dimension of the CT-MAS experiment does not quantitatively affect the line width measurements when TOP processing is used. We show in the ESI that linewidths in the constant-time  $^1\text{H}$  spectra are comparable between conventional CT-MAS and the TOP-CT-MAS implementation. In fact, we see from Fig. 3c that the final 2D TOP-CT-MAS dataset correlates evolution along the  $t_A$  and  $t_B$  coordinates along orthogonal dimensions. We can therefore measure site-specific non-refocusable contributions to linewidths in the dimension orthogonal to the constant-time  $^1\text{H}$  spectrum. We also show in the SI that the non-refocusable contributions determined from the TOP-CT-MAS experiments are comparable to those determined from the  $T_2'$  experiments shown in Fig. 4b.

At first sight, it might appear that the TOP transformation circumvent a seemingly fundamental limitation on the bandwidth of linearly sampled signals. This is not the case. First, the Nyquist criterion should only be expected to apply strictly to directly acquired signals, since acquisition actually proceeds along the indirect dimension by concatenation of separate experiments. More importantly, however, is that interactions 'A' and 'B' coevolve in the directly acquired signal. Signals acquired along the indirect dimension need then only supply the information necessary to allow deconvolution of the two interactions. When, as in 2D PASS and CT-MAS, the experiment is designed such that interactions 'A' and 'B' evolve independently along oblique coordinates in the initial 2D coordinate system, an affine transformation exists for separating and correlating them along orthogonal dimensions in the final 2D coordinate system. For the classes of 2D experiments that do not possess this property, however, TOP processing cannot effectively swap the direct and indirect sampling intervals. This is true, for example, of the two shift spectra axes in a 2D heteronuclear correlation experiment.

Finally, it is worth noting that when using the strategy of direct pathway selection, use of the z-filter with hypercomplex acquisition is unnecessary to obtain pure absorption mode lineshapes provided that the pulse is moved from the beginning to the end of the constant-time interval. Thus, only the first two pulses are necessary for the minimal CT-MAS experiment, allowing a phase cycle with as few as 3 steps. If sensitivity is not a limiting factor, this would permit acquisition of constant time  $^1\text{H}$  spectra in less than two minutes.

## 4. Conclusions

In summary, we find that the non-refocusable contribution to residual line broadening at 111 kHz MAS in  $\beta$ -AspAla is around 30–40%, from  $T_2'$  measurements. We show that this contribution can be removed in 2D constant time experiments, leading to linewidths up to 40% narrower than the one-pulse experiment. We observe that this narrowing due both to the CT effect, and the effect of the delayed acquisition due to the constant-time echo. Despite the line narrowing effect, this experiment requires long experimental times to obtain high-resolution in the indirect dimension. We overcome this drawback by adapting the experiment to the TOP transformation. The resulting TOP-CT-MAS experiment provides comparable results to the conventional CT-MAS experiment, but in a fraction of the experimental time. For  $\beta$ -AspAla we obtained  $^1\text{H}$  spectra with up to a 30% improvement in resolution as compared to the one-pulse experiment, in less than 10 min.

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## Declaration of Competing Interest

There are no conflicts to declare.

## Appendix A. Supplementary material

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.jmr.2019.06.015>.

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