

Na₂V₃O₇: An unusual low-dimensional quantum magnet

J.L. Gavilano^{a,*}, E. Felder^a, D. Rau^a, H.R. Ott^a, P. Millet^b,
F. Mila^c, T. Cichorek^d, A.C. Mota^d

^aLaboratorium für Festkörperphysik, ETHZ, CH-8093 Zürich, Switzerland

^bCentre d'Elaboration des Matériaux et d'Etudes Structurales, 29, rue J. Marvig, 31055 Toulouse Cedex, France

^cInstitute of Theoretical Physics, EPFL, CH - 1015 Lausanne, Switzerland

^dMax-Planck-Institut für Chemische Physik fester Stoffe, 01187 Dresden, Germany

Abstract

Results of present and previous measurements of the ²³Na NMR response, dc- and ac-magnetic susceptibilities and the specific heat of Na₂V₃O₇ at low temperatures suggest that this material is close to a quantum critical point (QCP) at $\mu_0 H = 0$ T. The experimental data can be explained by assuming that below 100 K the localized *V* magnetic moments ($S = \frac{1}{2}$) form a collection of dimers, with a broad distribution of singlet–triplet gaps. Most of the dimers adopt a singlet ground state with gaps between 0 and 350 K. A small fraction of them forms triplet ground states with gaps between 0 and 15 K. The degeneracy of the triplet ground states is lifted by a phase transition at an unusually low temperature of 0.086 K. Modest magnetic fields effectively quench this low-temperature state and the system is driven away from the QCP as the applied fields are enhanced to above 1 T.

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Na₂V₃O₇ is an insulating compound, first reported in 1999 by Millet and coworkers, with very unusual structural features [1]. The *V* ions (with spin $\frac{1}{2}$) are arranged on the walls of nanotube-type structural units with 5 Å diameter. During the last few years, various experimental results that reveal unusual behavior have been obtained for Na₂V₃O₇. One of the most interesting features is that upon varying the temperature *T* from well above to well below 100 K, most of the *V* moments seem to be gradually quenched [2,3]. Below 20 K, only $\frac{1}{9}$ of the *V* moments contribute to the magnetic susceptibility χ . At lower temperatures, the ²³Na NMR spin–lattice relaxation rate $T_1^{-1}(T)$ reveals a maximum at a field-dependent temperature T_a , which shifts to zero as the applied field *H* is reduced to zero. This was previously interpreted [2] as evidence for a quantum critical point (QCP) at $\mu_0 H = 0$ T. We present and discuss here a model to explain experimental results of the specific

heat C_p , $T_1^{-1}(T)$ and $\chi(T)$, of Na₂V₃O₇ at low temperatures.

Results of extensive measurements of the magnetic, i.e., in excess of the lattice contribution, specific heat $C_m(T, H)$ for Na₂V₃O₇, shown in Fig. 1, revealed [4] the presence of broad maxima in $C_m(T, H)/T$ at $T_{\max}(H)$, which shift to zero as *H* decreases to zero. For comparison we also plot, in the same figure, the positions of the maxima in $T_1^{-1}(T)$ at T_a vs. *H*, using data from Ref. [2]. We note a close agreement between $T_a(H)$ and $T_{\max}(H)$, which seems to indicate some kind of phase transition at $T_{\max}(H)$. Because we also find a broad maximum in $C_m(T)$ at field-dependent temperatures $T_0(H)$, rather far from $T_{\max}(H)$ and with a completely different field dependence, another interpretation seems to be needed, however. A sharp anomaly in $\chi(T)$ at 0.086 K at $\mu_0 H = 0$ T indicates a phase transition at an unusually low temperature and therefore Na₂V₃O₇ should still be regarded as being close to a QCP.

Attempts to interpret our $C_m(T, H)$ data lead us to consider them as exhibiting Schottky-type anomalies due

*Corresponding author. Tel./fax: +41 044 633 2245.

E-mail address: gavilano@phys.ethz.ch (J.L. Gavilano).

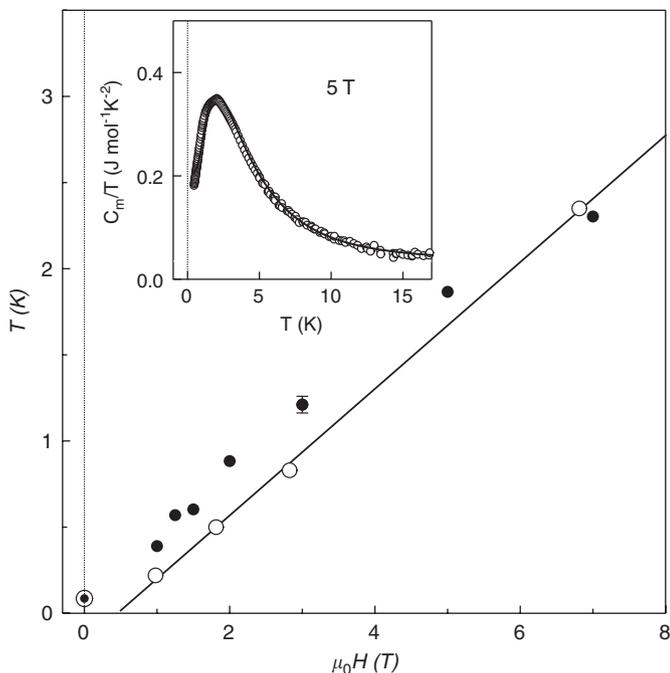


Fig. 1. Position of the maxima in $C_m(T)/T$ at T_{\max} (filled circles) and of the maxima in $T_1^{-1}(T)$ at T_a (empty circles) as a function of H . The symbol at the lowest temperature corresponds to a sharp maximum in $\chi(T)$ for $\mu_0 H = 0$ T. The solid line represents the best fit to the $T_a(H)$ data using a linear function. Inset C_m vs. T . The solid line represents the best fit to the data using the model described in the text.

to an ensemble of singlet–triplet units. The corresponding singlet–triplet gaps Δ exhibit a broad distribution $P(\Delta)$. The low-temperature part of $P(\Delta)$ consistent with our experimental results is shown in Fig. 2. A broad range of gap distribution, from -15 K to up to above room temperature, is quite remarkable for any regular solid. The flat part of $P(\Delta)$ yields a linear-in- T term in $C_m(T, H)$ and the model also predicts a Curie-type behavior for $\chi(T)$, with a change of the Curie constant near 1 K. All these features are experimentally observed [2,4]. The fraction of dimers with negative gaps, i.e., adopting a triplet ground state, are believed to order at 0.086 K, as suggested by the entropy release at low temperatures [4].

To explain the anomaly in $T_1^{-1}(T, H)$ at $T_a(H)$, further assumptions have to be made. For instance, $T_a \propto H$ suggests a “slowing down” of the relevant V moments fluctuations with decreasing T [4]. The equality of the prefactors, however, i.e., $T_a(H) \approx T_{\max}(H) = \alpha H$, is rather provocative and may point to the significance of the substantial spectral weight of $P(\Delta E_{\min})$ at exactly $2\mu_0 H/k_B$ (see vertical lines at 0 and 9.4 K in the inset of Fig. 2). This weight arises from the dimers adopting a triplet ground state which is split in an external magnetic field. It is these dimers which influence T_{\max} in $C_m(T)/T$. If the same dimers also play a central role in $T_1^{-1}(T, H)$, its behavior suggests that their associated moments are actually slowing

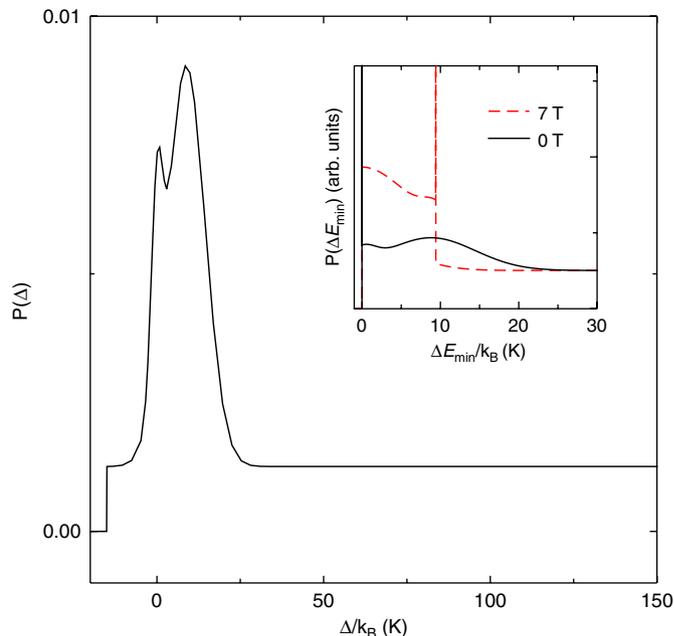


Fig. 2. Distribution $P(\Delta)$ of singlet–triplet gaps Δ . We note that in an applied magnetic field, H , Δ does not represent the excitation energy ΔE_{\min} from the ground state. Even if $\mu_0 H = 0$ T, for the case that $\Delta < 0$, $\Delta E_{\min} = 0$. Inset: Minimum excitation energy distribution $P(\Delta E_{\min})$ for 0 and 7 T.

down with decreasing T , leading to the phase transition at 0.086 K. The rest of the dimers, i.e., the majority, is of less importance for the low-temperature behavior.

We conclude that, well above 100 K, the system may be considered as paramagnetic with the V moments interacting via a very wide range of couplings. This is unusual for a well ordered solid, and points out to a delicate balance between the exchange interactions among the V moments and geometrical frustration imposed by the unusual structural features of $\text{Na}_2\text{V}_3\text{O}_7$. Near 100 K, the V moments undergo a dimerization process leading to a wide range of singlet–triplet gaps. The resulting system is very close to a QCP. The dimers with triplet ground states are involved in a phase transition at 0.086 K.

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