

Numerical optimization of the ramp-down phase with the RAPTOR code

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MODEL

Research directions

1. Development of an optimization procedure for the ramp down phase of the plasma discharge to terminate plasmas in the fastest and safest way:

- Determination of the **optimal time evolution** of the plasma parameters, like plasma current I_p , plasma elongation κ , auxiliary power P_{aux} to terminate plasmas (decrease I_p) as fast as possible.
- For the safe termination **physical constraints** have to be specified: a constraint on **normalized β_N and poloidal β_{pol}** (not too high) to avoid MHD modes, a constraint on the **plasma inductance l_i** to avoid vertical instability,...
- Define **technical constraints** to match experimental limits, like the **max ramp rate of the plasma current I_p** , a constraint on the **rate of change in the vertical magnetic field B_v** for radial position control,...

Determination of the optimal time of H- to L-mode transition.

2. Development of the RAPTOR code:

The **RAPTOR code** – Rapid Plasma Transport simulator [1,2]:

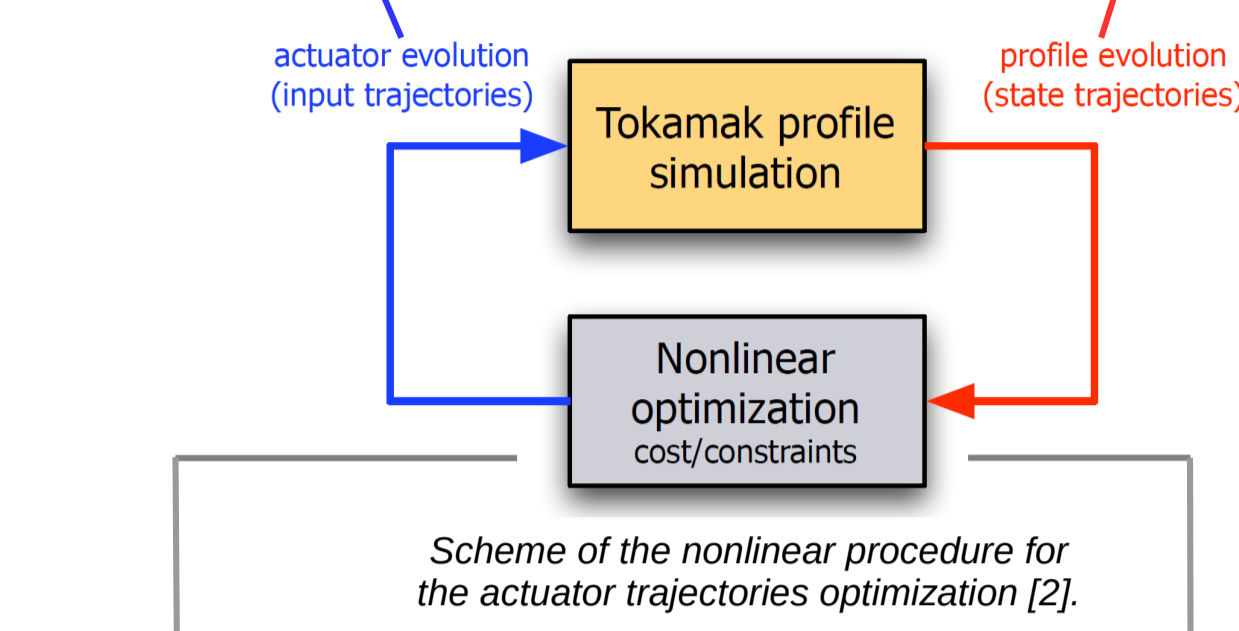
- The 1D control-oriented transport code without an equilibrium solver.
- A time dependent geometry can be used.
- The **gradient-based transport models** [3,4] for the electron heat and particles transport have been implemented.
- Successful validation via simulations of TCV and AUG entire plasma discharges and comparison with the experimental measurements [5].

- [1] F. Felici et al 2011 Nucl. Fusion 51 083052
 [2] F. Felici, O. Sauter 2012 PPCF 54 025002
 [3] O. Sauter et al 2014 Phys. of Plasma 21 055906
 [4] D. Kim, A. Merle et al 2016 PPCF 58 055002
 [5] A.A. Teplukhina et al 2017 PPCF doi:10.1088/1361-6587/aa857e

The trajectories optimization [2]

To get a good trajectory optimization
 1) **realistic predictive simulations** => appropriate transport models;
 2) **a fast solver** => RAPTOR.

- Plasma current I_p
- ECH power P_{ECH}
- NBI power P_{NBI}
- Plasma elongation κ
- Poloidal flux $\psi(\rho,t)$
- Electron temperature $T_e(\rho,t)$
- Electron density $n_e(\rho,t)$
- Ion temperature $T_i(\rho,t)$



Cost function:

$$J = \sum_{i=1}^n v_i J_i; \min(J)$$

Examples: $J_1 = \|v(t_f) - v_{ref}\|_{W_1}^2$

$$J_2 = \|\partial U_p / \partial \rho\|_{W_2}^2$$

$$J_3 = \int I_p dt$$

Constraints:

- Safety factor $q > 1.0$
- Plasma inductance $l_i > 3$
- Edge loop voltage U_{pl}
- ... various physical and technical constraints (I_p max ramp rate)

The RAPTOR code transport equations

Diffusion equations: the poloidal flux, the electron temperature and density

$$\sigma_{||} \left(\frac{\partial \psi}{\partial t} - \frac{\hat{\rho} \Phi_b}{2\Phi_b} \frac{\partial \psi}{\partial \hat{\rho}} \right) = \frac{(R \cdot B_\theta)^2}{16\pi^2 \mu_0 \Phi_b^2 \hat{\rho}} \left(\frac{g_2 g_3}{\hat{\rho}} \frac{\partial \psi}{\partial \hat{\rho}} - \frac{B_\theta V'_\rho}{2\Phi_b \hat{\rho}} \langle (J_{BS} + J_{aux}) \cdot B \rangle \right)$$

$$\frac{3}{2} \frac{1}{(V'_\rho)^{5/3}} \left(\frac{\partial}{\partial t} - \frac{\Phi_b}{2\Phi_b} \frac{\partial}{\partial \hat{\rho}} \right) \left[(V'_\rho)^{5/3} n_e T_e \right] = \frac{1}{V'_\rho} \frac{\partial}{\partial \hat{\rho}} \left[\frac{g_1}{V'_\rho} n_e \frac{\partial T_e}{\partial \hat{\rho}} \right] + P_e$$

$$\frac{1}{V'_\rho} \left(\frac{\partial}{\partial t} - \frac{\Phi_b}{2\Phi_b} \frac{\partial}{\partial \hat{\rho}} \right) \left[(V'_\rho)^{5/3} n_e \right] = \frac{1}{V'_\rho} \frac{\partial}{\partial \hat{\rho}} \left[\frac{g_1}{V'_\rho} D_e \frac{\partial n_e}{\partial \hat{\rho}} - g_0 V_e n_e \right] + S_e$$

The inverse scale length [3]:

$$\frac{R}{L_{Te}} = -\frac{R_0}{a} \frac{d \ln T_e}{d \rho_V} = \begin{cases} 0 & \text{for } \rho_V < \rho_{Te,inv} \\ \frac{R_0 \lambda_{Te}}{a} & \text{for } \rho_{Te,inv} < \rho_V < \rho_{Te,ped} \\ \frac{R_0}{a} \frac{\mu_{Te}}{T_e(\rho_V)} & \text{for } \rho_V > \rho_{Te,ped} \end{cases}$$

λ_{Te} – a fixed parameter for L-/H-mode for the T_e/n_e core gradient

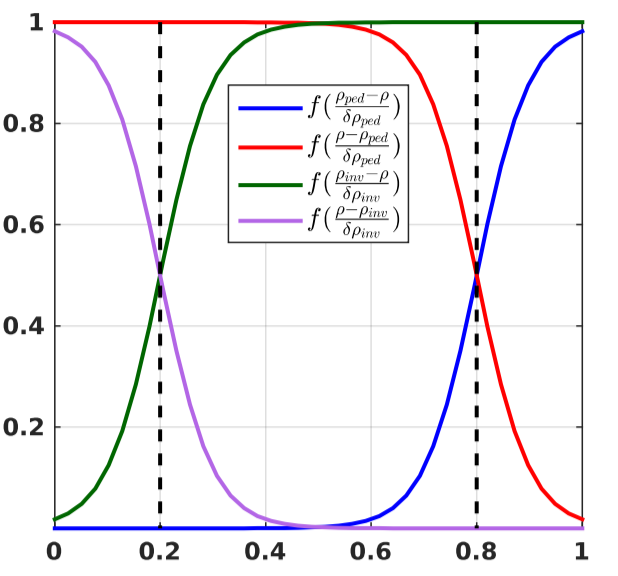
μ_{Te} – a controlled parameter to get given H_e or n_{e0}

Transport coefficients: the gradient-based model [3,4]

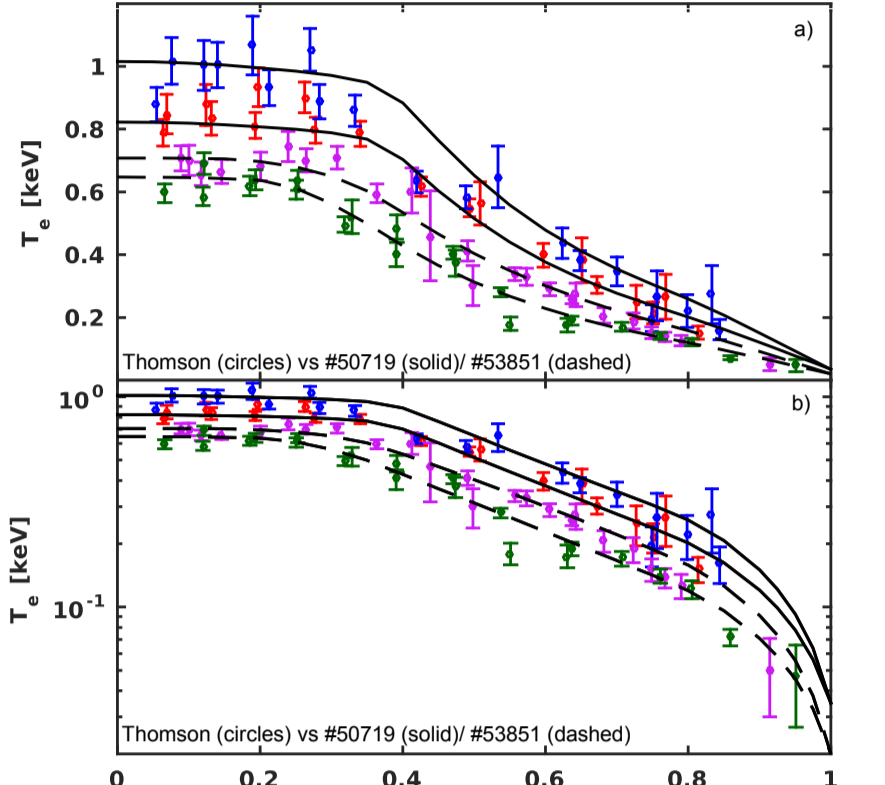
$$\frac{V_e}{D_e} = - \left[\frac{\mu_{ped}}{n_e \rho_{edge}} f \left(\frac{\rho - \rho_{ped}}{\delta \rho_{ped}} \right) + \frac{\lambda_{ped}}{\rho_{edge}} f \left(\frac{\rho - \rho_{ped}}{\delta \rho_{ped}} \right) \right]^{-1} \times f \left(\frac{\rho_{inv} - \rho}{\delta \rho_{inv}} \right) \quad D_e = 0.2 \cdot \chi_e$$

$$\chi_e = \frac{q_e}{V'_\rho \langle (\rho)^2 \rangle n_e T_e} \left[\frac{\mu_{ped}}{T_e \rho_{edge}} f \left(\frac{\rho - \rho_{ped}}{\delta \rho_{ped}} \right) + \frac{\lambda_{ped}}{\rho_{edge}} f \left(\frac{\rho - \rho_{ped}}{\delta \rho_{ped}} \right) \right]^{-1} \times f \left(\frac{\rho_{inv} - \rho}{\delta \rho_{inv}} \right) + \chi_{ST} f \left(\frac{\rho - \rho_{inv}}{\delta \rho_{inv}} \right)$$

f-functions for χ_e and V_e/D_e

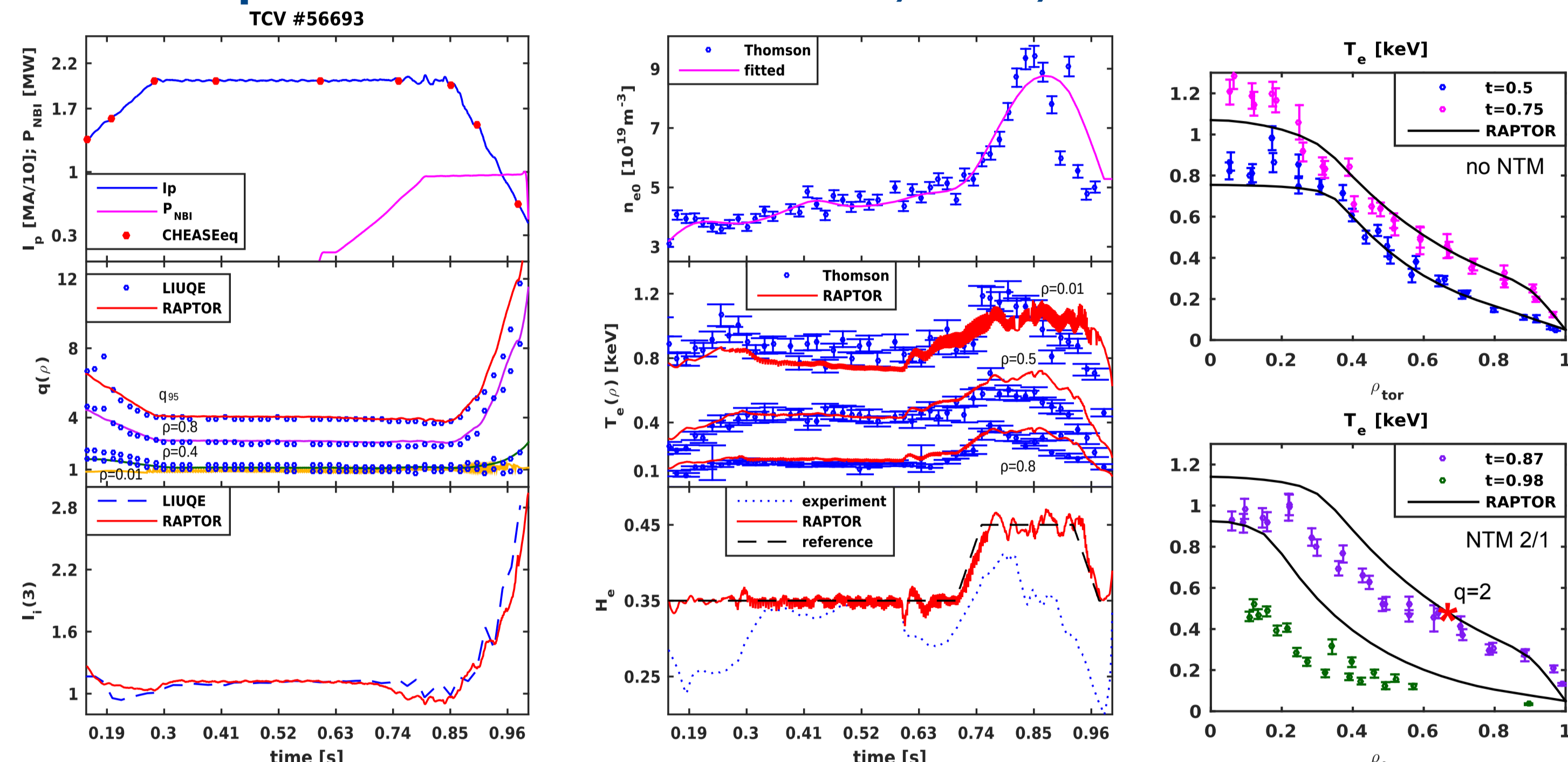


T_e profiles for TCV #50719 and #53851



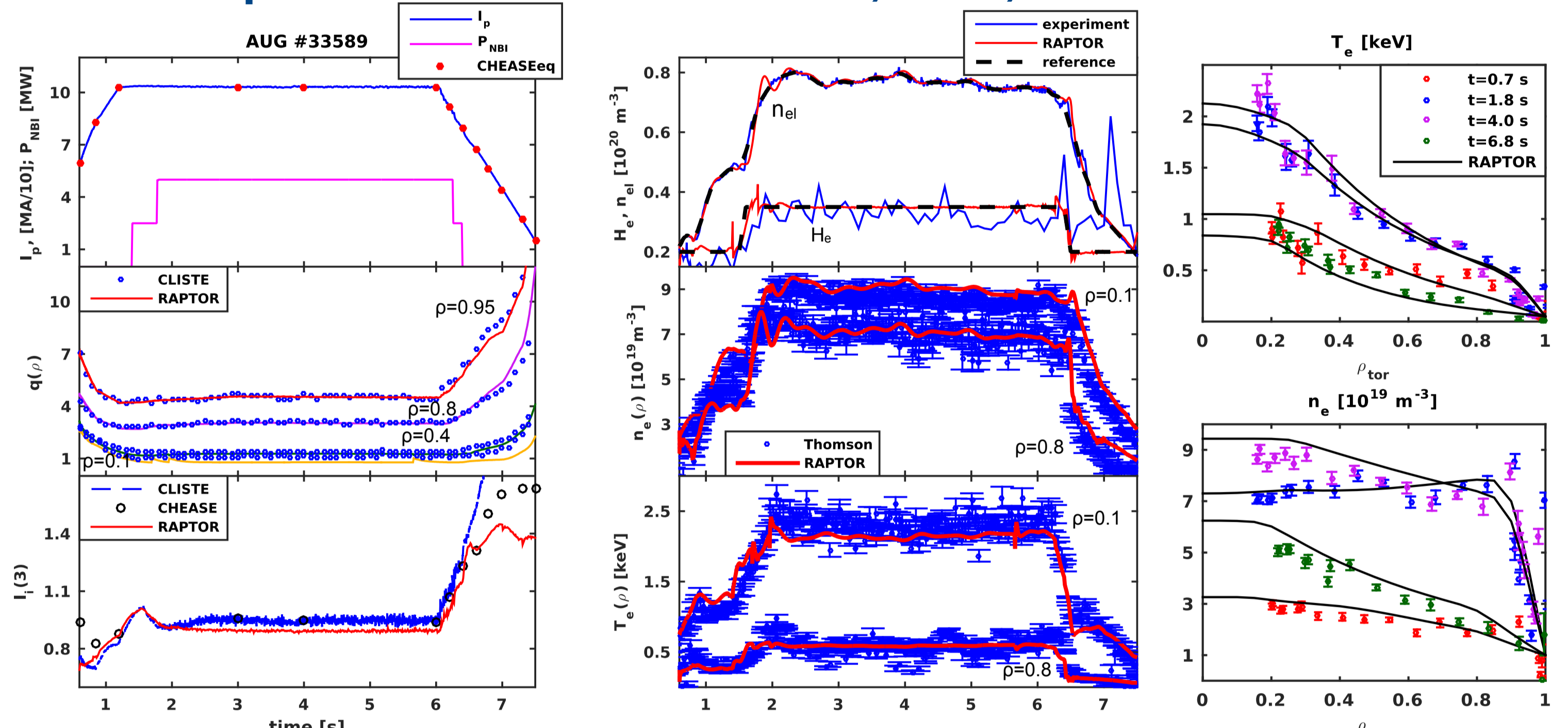
VALIDATION

The TCV plasma simulation: #56693, NBH, LHL-modes



Prescribed parameters: the total plasma current I_p , radial profiles of the electron density n_e , the total input NBI power with central deposition and the prescribed Gaussian radial profile, $H_e=0.35/0.45$ and $\lambda_{Te}=3.2/2.3$ for L-/H-mode.
Predicted variables: the electron temperature T_e , the poloidal flux ψ , the electron heat diffusivity χ_e , various physical quantities.
Equilibrium: 9 CHEASE equilibria (marked as \bullet on the I_p plot).
CPU time: ~1 min for a time grid with 1 ms step (the shot duration 1 s) on a standard PC.
Note: L-H at 0.7 s, H-L at 0.93 s, NTM 2/1 from 0.85 s.

The AUG plasma simulation: #33589, NBH, LHL-modes



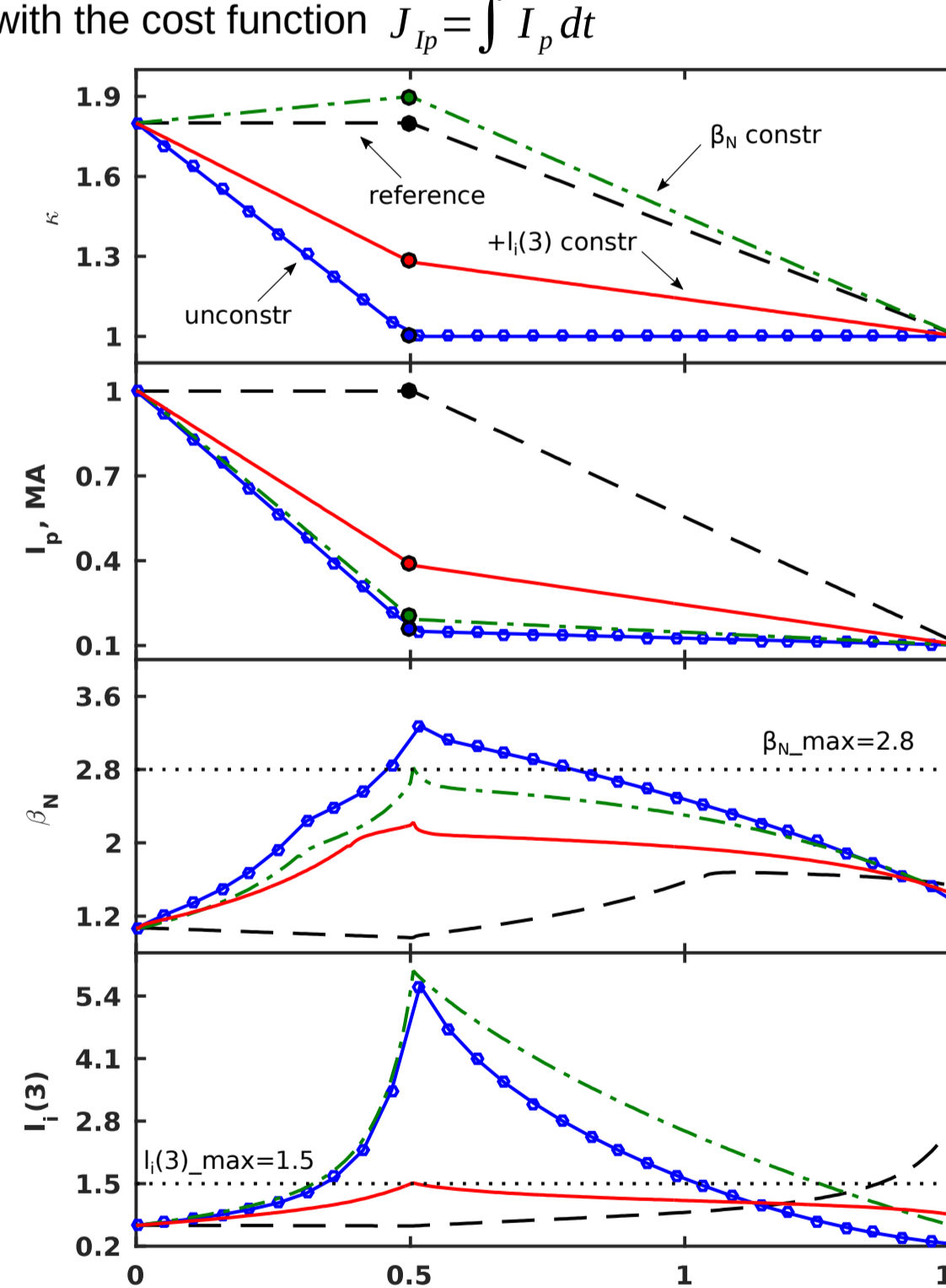
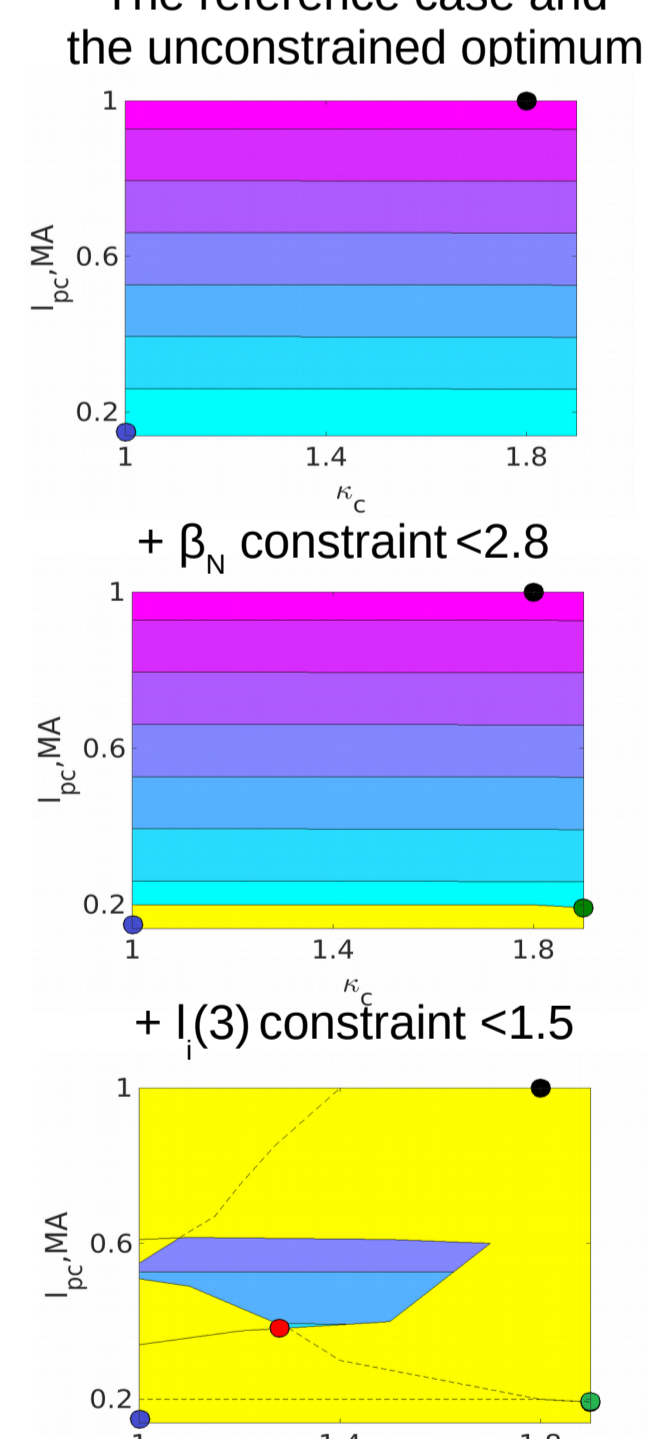
Prescribed parameters: same as for the TCV case except n_e profiles, $H_e=0.2/0.35$ and $\lambda_{Te}=3.0/2.3$ for L-/H-mode, the line-averaged electron density n_{e0} , $\lambda_{Te}=1.0/0.5$ for L-/H-mode.
Predicted variables: as for the TCV case + the electron density n_e .
Equilibrium: 13 CHEASE equilibria (marked as \bullet on the I_p plot).
CPU time: ~1.5 min for a time grid with 10 ms step (the shot duration 7 s) on a standard PC.
Note: L-H at 1.5 s, H-L at 6.4 s.

OPTIMIZATION

The generic ramp-down optimization

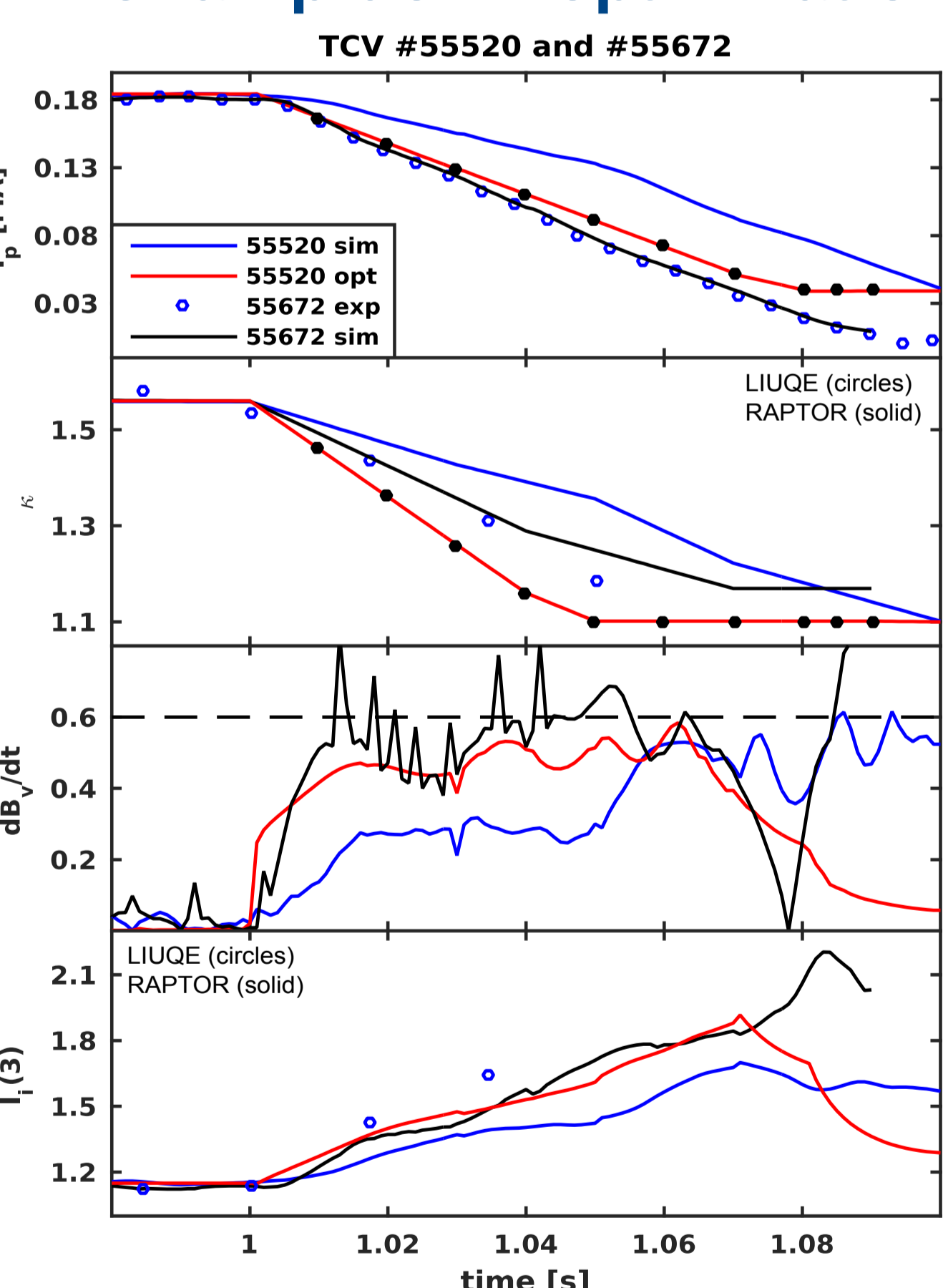
The ramp down optimization of the plasma current and the boundary elongation at $t=0.5$ s for the AUG-like plasma with the cost function $J_{I_p} = \int I_p dt$

The reference case and the unconstrained optimum



The contours for J_{I_p} are shown with the coloured circles which correspond to values of I_p and κ at $t=0.5$ s. An area where the constrained parameter violates the constraint is yellow-marked.

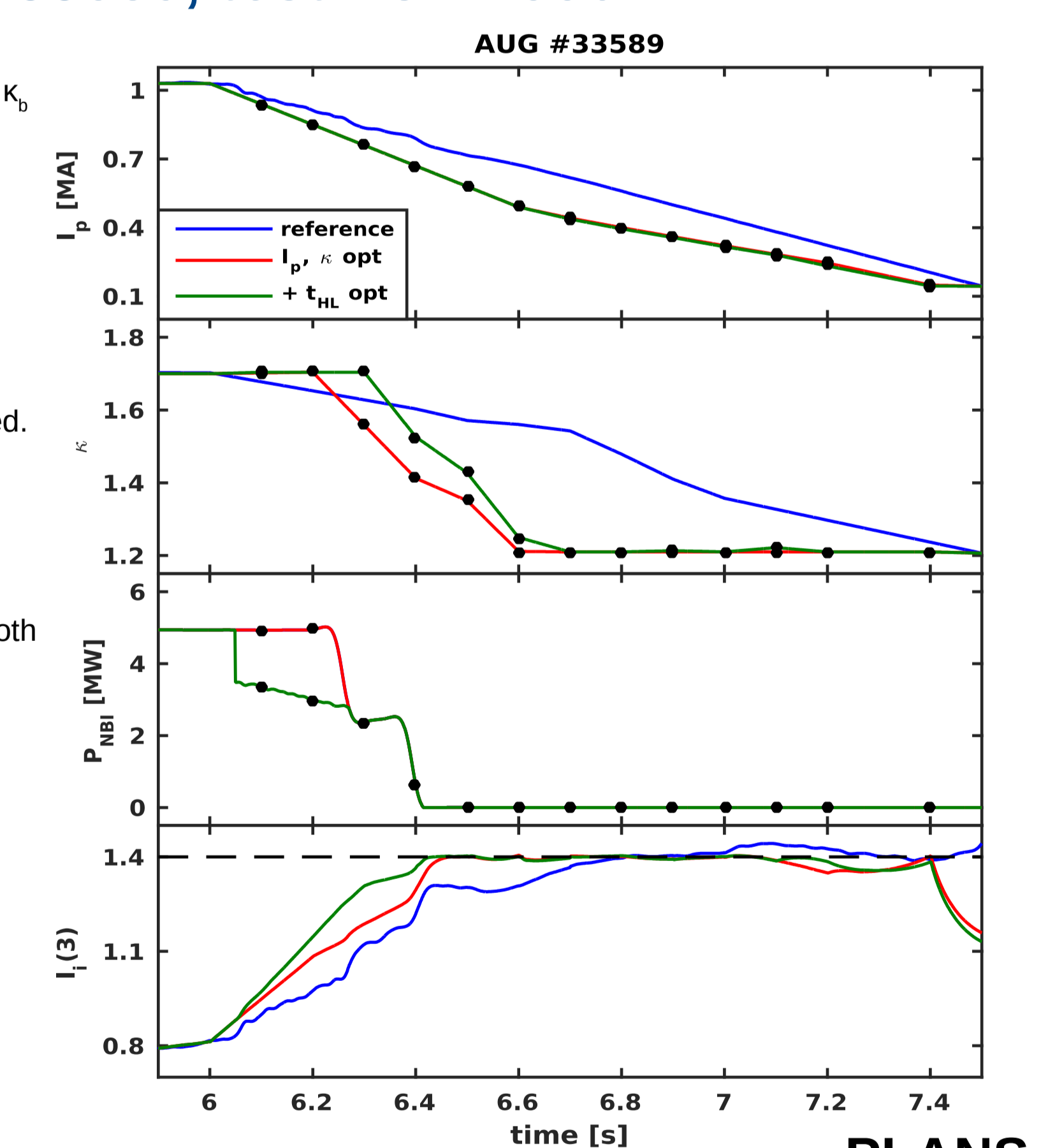
The ramp-down optimization: TCV #55520 and AUG #33589, test TCV #55672



TCV #55520: L-mode, the optimization of I_p and κ at $t = [1.01-1.09]$ s with 10 ms step.
 Technical constraints:
 $dI_p/dt < -1.9$ [MA/s], $dB/dt < 0.6$ [T/s]
 $B_v = \frac{\mu_0 I_p}{4\pi R} \left(\ln \left(\frac{8R}{aq_{0.5}} \right) + \beta_p + 0.5 l_i - 1.5 \right)$
 The cost function: $J_{I_p} = \int I_p dt$
 * Faster I_p and κ ramp-down can be programmed.

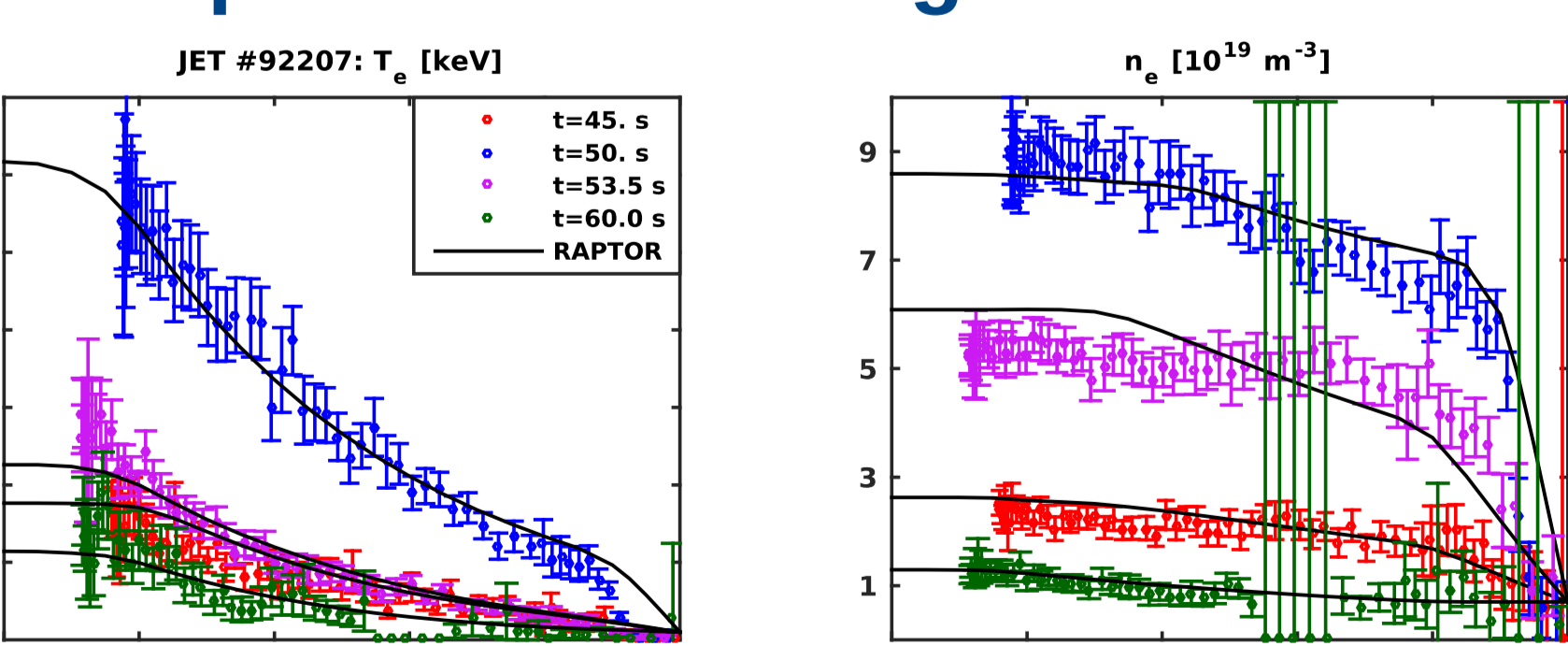
TCV #55672: an experimental test of the TCV #55520 optimized trajectories.
 * Faster I_p but slower κ ramp-down obtained.
 * dB/dt is within the required limit except sawtooth peaks.

AUG #33589: the optimization of I_p , κ , and t_{HL} at $t = [6.1-6.9]$ s with 100 ms step.
 Technical constraints:
 $dI_p/dt < -0.7$ [MA/s], $I(3) < 1.4$
 The cost function: $J_{I_p} = w_1 \int I_p dt + w_2 \int P_{aux} dt$
 * Reducing κ during the ramp-down would allow to better control I_p .
 * An earlier power drop might be possible.

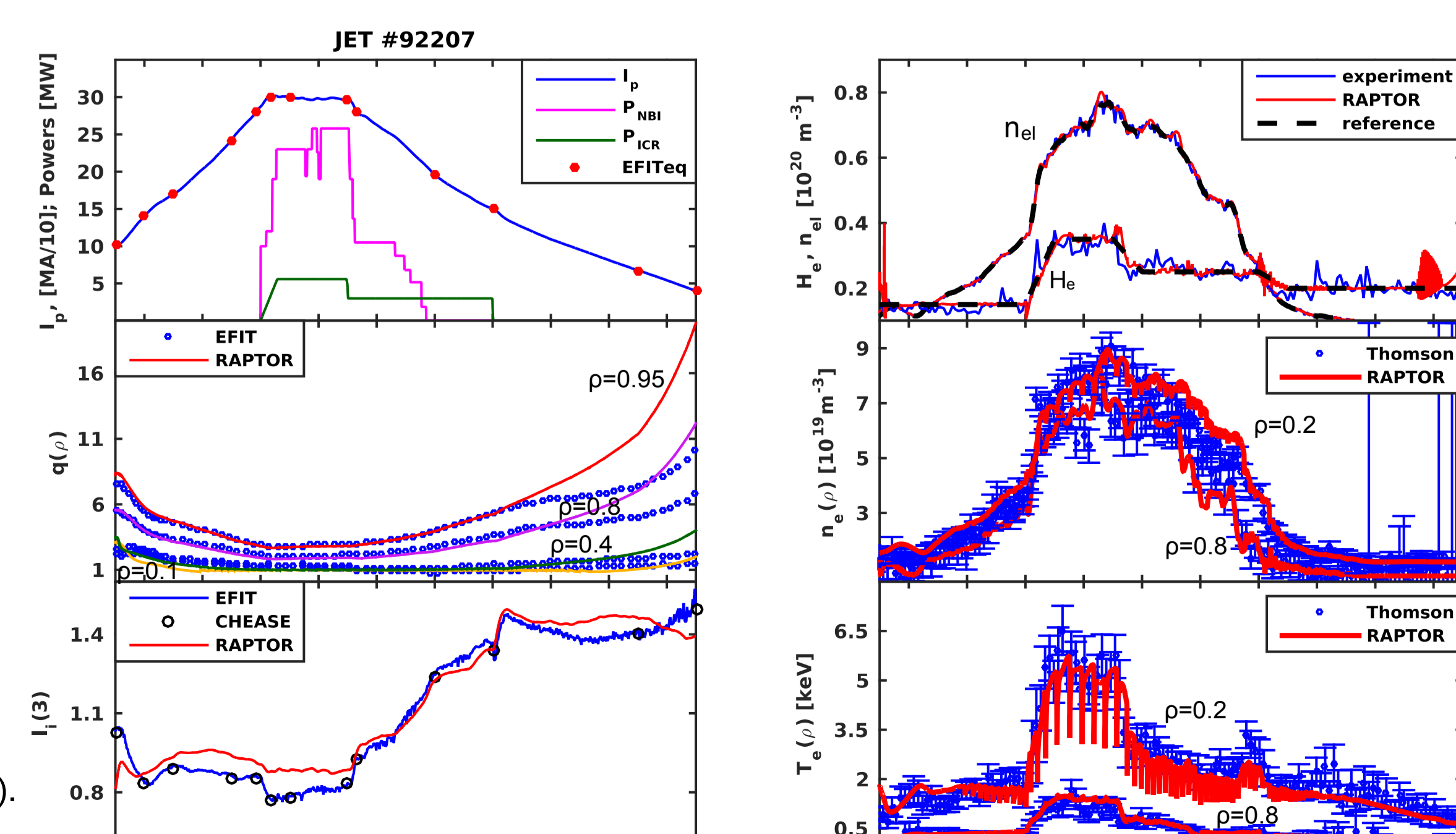


PLANS

JET plasma modelling: #92207



Prescribed parameters: same as for the AUG case; $\lambda_{Te}=3.0/2.3$ and $H_e=0.15(0.2)/0.35(0.25)$ for L-/H-mode, $\lambda_{Te}=1.0/0.5$ for L-/H-mode.
Predicted variables: as for the TCV case + electron density n_e .
Equilibrium: 13 EFIT equilibria (marked as \bullet on the I_p plot).
CPU time: ~4 min for a time grid with 10 ms step (the shot duration 20 s).
Note: L-H at 47 s, H-L at 52 s.



Future directions

- The RAPTOR code development:**
- T_e and impurities transport equations;
 - A scaling law for the pedestal pressure for L-/H-mode to determine μ_{Te} directly.
 - A radial-dependent core gradient λ_{Te} .
 - Continue the model validation with JET simulations.
 - Continue for ITER simulations.
- The ramp-down optimization:**
- Constraints related to radiated power and impurities.
 - Technical constraints on the rate of change in the electron density.
 - Technical constraints related to the plasma shape control.
 - Technical constraint on the vertical position control (constraint on dI/dt).
 - JET/ITER ramp-down optimization.

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